Coq, Chapar, and Coq Again

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The Coq Proof Assistant





"Software Foundations"

Chapar: Certified Causally Consistent Distributed Key-Value Stores

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Chapar@POPL'2016

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"A framework for modular verification of causal consistency for replicated key-value store implementations and their client programs."

I: KV Store Implementation

Causally Content

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Causal Consistency

Causally Content

 COS_A : Abstract Causal Operational Semantics

 \mathbb{I} : KV Store Implementation

Causal Consistency

Definition (Causally Content)

A client program is causally content if it avoids assertion failures when executed with COS_A .

 $\mathbb{P} \text{: } \text{Client Program}$

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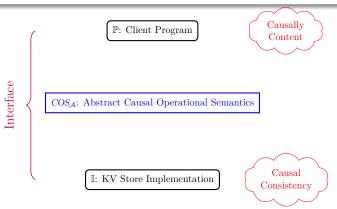
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A KV store impl. is causally consistent if it satisfies COS_A .

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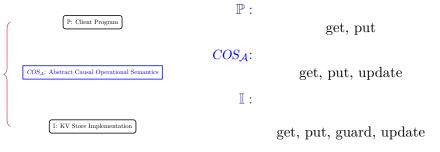


Definition (Causally Consistent)

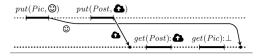
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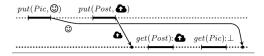
 $COS_{\mathcal{A}}\!\!:$ Abstract Causal Operational Semantics

I: KV Store Implementation



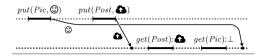
$\mathbb{P} \text{: } \mathbf{Client} \ \mathbf{Program}$





Program 1 (p_1) : Uploading a photo and posting a status

```
\begin{array}{c|c} 0 \rightarrow & \textbf{Alice} \\ put(Pic, \circledcirc); & \triangleright \text{ uploads a new photo} \\ put(Post, \spadesuit) & \triangleright \text{ announces it to her friends} \\ 1 \rightarrow & \textbf{Bob} \\ post \leftarrow get(Post); & \triangleright \text{ checks Alice's post} \\ photo \leftarrow get(Pic); & \triangleright \text{ then loads her photo} \\ assert(post = \spadesuit \Rightarrow photo \neq \bot) \end{array}
```



Program 1 (p_1) : Uploading a photo and posting a status

 $assert(post \neq \bot \implies photo \neq \bot)$

 $COS_{\mathcal{A}} \colon$ Abstract Causal Operational Semantics

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Abstract:

without referring to the details of specific implementations; do not involving message passing.

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labelled transition system
executable (like TLA+)

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Causal:

explicitly track happens-before dependencies



 $W_{\mathcal{A}} : N \to (S \times D \times U \times A \times M)$

$$W_{\mathcal{A}}: N \to (S \times D \times U \times A \times M)$$

c:C Clock

$$W_{\mathcal{A}}: N \to (S \times D \times U \times A \times M)$$

c : C

Clock

 $d: D = \mathcal{P}(N \times C)$

Dependencies

$$W_{\mathcal{A}}: N \to (S \times D \times U \times A \times M)$$

c:C Clock

 $d: D = \mathcal{P}(N \times C)$ Dependencies

 $u: U = (K \times V \times D)^*$ Updates

$$W_{\mathcal{A}}: N \to (S \times D \times U \times A \times M)$$

$$c:C$$
 Clock

$$d: D = \mathcal{P}(N \times C)$$
 Dependencies

$$u: U = (K \times V \times D)^*$$
 Updates

$$a: A = N \rightarrow C$$
 Applied

$$W_{\mathcal{A}}: N \to (S \times D \times U \times A \times M)$$

$$c:C$$
 Clock

$$d: D = \mathcal{P}(N \times C)$$
 Dependencies

$$u: U = (K \times V \times D)^*$$
 Updates

$$a: A = N \to C$$
 Applied

$$m: M = K \to (V \times N \times C \times D)$$
 Store

$$\begin{aligned} & \underset{u' = u}{\text{PUT}} & u' = u + + [(k, v, d)] & a' = a[n \mapsto a(n) + 1] \\ & \underline{m' = m[k \mapsto (v, n, |u'|, \emptyset)]} & d' = d \cup \{(n, |u'|)\} \\ & \overline{W_A[n \mapsto (put(k, v); s, d, u, a, m)]} \\ & \underbrace{N_A[n \mapsto (put(k, v); s, d, u, a, m)]}_{N, |u'| \mid put(k, v)} \\ & W_A[n \mapsto (s, d', u', a', m')] \end{aligned}$$
 GET
$$\begin{aligned} & m(k) = (v, n'', c'', d'') \\ & d' = \begin{cases} d \cup \{(n'', c'')\} \cup d'' & \text{if } n'' \neq n_0 \\ d & \text{otherwise} \end{cases} \\ & \overline{W_A[n \mapsto (s \in get(k); s, d, u, a, m)]} \\ & \underbrace{N_A[n \mapsto (s[x \coloneqq v], d', u, a, m)]}_{N', c'', n \vdash pget(k) \coloneqq v} \\ & W_A[n \mapsto (s[x \coloneqq v], d', u, a, m)] \end{aligned}$$
 UPDATE
$$\begin{aligned} & a_1(n_2) < |u_2| & u_2[a_1(n_2)] = (k, v, d) \\ & \bigwedge_{(n,c) \in d} c \le a_1(n) & a'_1 = a_1[n_2 \mapsto a_1(n_2) + 1] \\ & \underbrace{M_A[n_1 \mapsto (s_1, d_1, u_1, a_1, m_1)][n_2 \mapsto (s_2, d_2, u_2, a_2, m_2)]}_{N_A[n_1 \mapsto (s_1, d_1, u_1, a'_1, m'_1)][n_2 \mapsto (s_2, d_2, u_2, a_2, m_2)]} \end{aligned}$$

ASSERTFAIL

$$C[n \mapsto (\mathit{assertfail}, d, u, a, m)] \xrightarrow{\mathit{assertfail}}_{\mathcal{A}} C[n \mapsto (\mathit{skip}, d, u, a, m)]$$

$$\begin{aligned} & \text{GET} \\ & m(k) = (v, n'', c'', d'') \\ & \underline{d'} = \begin{cases} \underline{d} \cup \{(n'', c'')\} \cup \underline{d''} & \text{if } n'' \neq n_0 \\ \underline{d'} & \text{otherwise} \end{cases} \\ & \underline{W_{\mathcal{A}}[n \mapsto (x \leftarrow get(k); s, d, u, a, m)]} \\ & \underline{n'', c'', n \triangleright get(k) : v} \\ & W_{\mathcal{A}}[n \mapsto (s[x := v], d', u, a, m)] \end{aligned}$$

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$$W_{\mathcal{A}}[n \mapsto (x \leftarrow get(k); s, d, u, a, m)]$$

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$$W_{\mathcal{A}}[n \mapsto (x \leftarrow get(k); s, d, u, a, m)]$$

$$m(k) = (v, n'', c'', \mathbf{d''})$$

GET
$$m(k) = (v, n'', c'', d'')$$

$$d' = \begin{cases} d \cup \{(n'', c'')\} \cup d'' & \text{if } n'' \neq n_0 \\ d'' & \text{otherwise} \end{cases}$$

$$W_{\mathcal{A}}[n \mapsto (x \leftarrow get(k); s, d, u, a, m)]$$

$$n'', c'', n \triangleright get(k) : v \rightarrow \mathcal{A}$$

$$W_{\mathcal{A}}[n \mapsto (s[x := v], d', u, a, m)]$$

$$W_{\mathcal{A}}[n \mapsto (\mathbf{x} \leftarrow \mathbf{get}(\mathbf{k}); \mathbf{s}, d, u, a, m)]$$

$$m(k) = (v, n'', c'', \mathbf{d''})$$

$$\xrightarrow{n'',c'',n\rhd get(k):v}_{\mathcal{A}}$$

$$W_{\mathcal{A}}[n \mapsto (\mathbf{x} \leftarrow \mathbf{get}(\mathbf{k}); \mathbf{s}, d, u, a, m)]$$

$$m(k) = (v, n'', c'', \mathbf{d''})$$

$$\xrightarrow{n^{\prime\prime},c^{\prime\prime},n\rhd\,get(k):v}_{\mathcal{A}}$$

$$d' = \begin{cases} d \cup \{(n'', c'')\} \cup d'' & \text{if } n'' \neq n_0 \\ d & \text{otherwise} \end{cases}$$

$$\begin{aligned} & \text{GET} \\ & m(k) = (v, n'', c'', d'') \\ & d' = \begin{cases} d \cup \{(n'', c'')\} \cup d'' & \text{if } n'' \neq n_0 \\ & \text{otherwise} \end{cases} \\ & \overline{W_{\mathcal{A}}[n \mapsto (x \leftarrow get(k); s, d, u, a, m)]} \\ & \underline{n'', c'', n \triangleright get(k) : v} \\ & W_{\mathcal{A}}[n \mapsto (s[x := v], d', u, a, m)] \end{aligned}$$

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$$W_{\mathcal{A}}[n \mapsto (s[x := v], \mathbf{d}', u, a, m)]$$



COS_A: Abstract Causal Operational Semantics

Program 1 (p_1) : Uploading a photo and posting a status

Alice $0 \rightarrow$ $put(Pic, \bigcirc);$ b uploads a new photo > announces it to her friends $post \leftarrow qet(Post);$ > checks Alice's post $photo \leftarrow qet(Pic)$: > then loads her photo $assert(post = \triangle \Rightarrow photo \neq \bot)$

 $\begin{aligned} & \text{PUT} \\ & u' = u + + [(k, v, d)] \quad a' = a[n \mapsto a(n) + 1] \\ & m' = m[k \mapsto \underbrace{(v, n, |u'|, \emptyset)]}_{} \quad d' = d \cup \underbrace{\{(n, |u'|)\}}_{} \end{aligned}$ $W_A[n \mapsto (put(k, v); s, d, u, a, m)]$ n, $|u'| \triangleright put(k,v)$ $W_A[n \mapsto (s, d', u', a', m')]$ m(k) = (v, n'', c'', d'') $W_A[n \mapsto (x \leftarrow get(k); s, d, u, a, m)]$ $W_A[n \mapsto (s[x := v], d', u, a, m)]$ UPDATE $a_1(n_2) < |u_2|$ $u_2[a_1(n_2)] = (k, v, d)$ $\bigwedge_{(n,c)\in d} c \le a_1(n)$ $a'_1 = a_1[n_2 \mapsto a_1(n_2) + 1]$ $m'_1 = m_1[k \mapsto (v, n_2, a'_1(n_2), d)]$ $W_A[n_1 \mapsto (s_1, d_1, u_1, a_1, m_1)][n_2 \mapsto (s_2, d_2, u_2, a_2, m_2)]$ $n_2, a'_1(n_2), n_1 \triangleright update(k, v)$ $W_A[n_1 \mapsto (s_1, d_1, u_1, a'_1, m'_1)][n_2 \mapsto (s_2, d_2, u_2, a_2, m_2)]$ ASSERTFAIL

 $C[n \mapsto (assertfail, d, u, a, m)] \xrightarrow{assertfail} C[n \mapsto (skin, d, u, a, m)]$



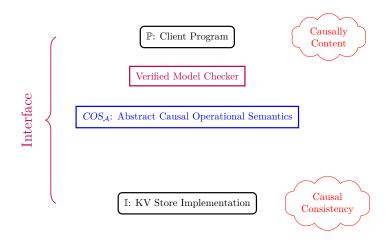
Verified Model Checker

COS_A: Abstract Causal Operational Semantics

Program 1 (p_1) : Uploading a photo and posting a status

```
Alice
0 \rightarrow
  put(Pic, \bigcirc);
                                                     > uploads a new photo
  > announces it to her friends
  post \leftarrow qet(Post);
                                                      > checks Alice's post
  photo \leftarrow get(Pic);
                                                     > then loads her photo
  assert(post = \triangle \Rightarrow photo \neq \bot)
```

```
\begin{aligned} & \text{PUT} \\ & u' = u + + [(k, v, d)] \quad a' = a[n \mapsto a(n) + 1] \\ & m' = m[k \mapsto \underbrace{(v, n, |u'|, \emptyset)]}_{} \quad d' = d \cup \underbrace{\{(n, |u'|)\}}_{} \end{aligned}
                          W_A[n \mapsto (put(k, v); s, d, u, a, m)]
                                      n, |u'| \triangleright put(k,v)
                               W_A[n \mapsto (s, d', u', a', m')]
                                   m(k) = (v, n'', c'', d'')
                       W_A | n \mapsto (x \leftarrow get(k); s, d, u, a, m) |
                           W_A[n \mapsto (s[x := v], d', u, a, m)]
       UPDATE
                    a_1(n_2) < |u_2| u_2[a_1(n_2)] = (k, v, d)
            \bigwedge_{(n,c)\in d} c \le a_1(n)  a'_1 = a_1[n_2 \mapsto a_1(n_2) + 1]
                          m'_1 = m_1[k \mapsto (v, n_2, a'_1(n_2), d)]
        W_A[n_1 \mapsto (s_1, d_1, u_1, a_1, m_1)][n_2 \mapsto (s_2, d_2, u_2, a_2, m_2)]
                              n_2, a_1'(n_2), n_1 \triangleright update(k,v)
        W_A[n_1 \mapsto (s_1, d_1, u_1, a'_1, m'_1)][n_2 \mapsto (s_2, d_2, u_2, a_2, m_2)]
ASSERTFAIL
C[n \mapsto (assertfail, d, u, a, m)] \xrightarrow{assertfail} A C[n \mapsto (skin, d, u, a, m)]
```



Concrete Operational Semantics

Concrete Operational Semantics

Instrumented Concrete Operational Semantics

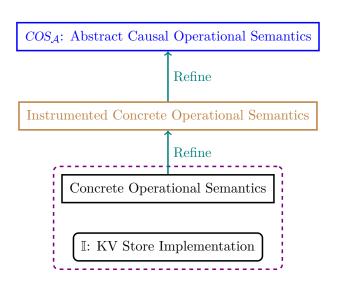
Concrete Operational Semantics

Refine

Concrete Operational Semantics

Refine

I: KV Store Implementation



 $\mathbb{I} \text{: } \mathrm{KV}$ Store Implementation

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 $W_{\mathcal{C}} : H \times T$

 \mathbb{I} : KV Store Implementation

$$W_{\mathcal{C}} : H \times T$$

$$h : H = N \rightarrow (S \times \text{State}(V))$$

Hosts

$$t : T = \mathcal{P}(M)$$

Transit

 $\mathbb{I} {:}\ \mathrm{KV}\ \mathrm{Store}\ \mathrm{Implementation}$

$W_{\mathcal{C}} : H \times T$

$$h: H = N \to (S \times \text{State}(V))$$
 Hosts

$$t: T = \mathcal{P}(M)$$
 Transit

$$m: M = N \times K \times V \times \text{Update}(V)$$
 Message

$$\sigma: \operatorname{State}(V)$$
 Alg State

$$u: \mathrm{Update}(V)$$
 Alg Update

$$\begin{aligned} & \text{PUT} \\ & \text{put}(V, n, \sigma, k, v) \leadsto^* (\sigma', u) \\ & t' = t \cup \{(n', k, v, u) \mid n' \in N \setminus \{n\}\} \\ & \underbrace{(h[n \mapsto (put(k, v); s, \sigma)], t)}_{C(1)} \\ & \underbrace{(h[n \mapsto (s, \sigma')], t')}_{C(1)} \end{aligned}$$

$$& \underbrace{\frac{n \mapsto put(k, v)}{C(1)}}_{C(1)} \\ & \underbrace{\frac{n \mapsto put(k, v)}{C(1)}}_{C(1)} \\ & \underbrace{\frac{n \mapsto put(k, v)}{C(1)}}_{C(1)} \\ & \underbrace{(h[n \mapsto (x \leftarrow get(k); s, \sigma)], t)}_{n \mapsto get(k) : v} \\ & \underbrace{(h[n \mapsto (s[x : = v], \sigma')], t)}_{C(1)} \end{aligned}$$

$$& \underbrace{(h[n \mapsto (s, \sigma)], t \cup \{(n, k, v, u)\}}_{n \mapsto update(k, v)} \\ & \underbrace{(h[n \mapsto (s, \sigma)], t \cup \{(n, k, v, u)\})}_{(n \mapsto update(k, v)} \end{aligned}$$

ASSERTFAIL

$$(h[n \mapsto (\mathit{assertfail}, \sigma)], t) \xrightarrow{\mathit{assertfail}}_{\mathcal{C}(\mathbb{I})} (h[n \mapsto (\mathit{skip}, \sigma)], t)$$

$$\begin{aligned} & \text{GET} \\ & \underbrace{\text{get}(V, n, \sigma, k)}_{\text{def}(h[n \mapsto (x \leftarrow get(k); s, \sigma)], t)} \\ & \underbrace{\frac{n \triangleright get(k) : \ v}{\mathcal{C}(\mathbb{I})}}_{\left(h[n \mapsto (s[x := v], \sigma')], t\right)} \end{aligned}$$

$$\begin{aligned} & \underset{\text{get}(V, n, \sigma, k) \, \leadsto^* \, (v, \sigma')}{\text{get}(V, n, \sigma, k) \, \leadsto^* \, (v, \sigma')} \\ & \underbrace{(h[n \mapsto (x \leftarrow get(k); s, \sigma)], t)}_{n \triangleright \, get(k) \, : \, v} \mathcal{C}^{(\mathbb{I})} \\ & \underbrace{(h[n \mapsto (s[x := v], \sigma')], t)}_{\text{}} \end{aligned}$$

$$\begin{aligned} & \frac{\text{GET}}{\text{get}(V, n, \sigma, k)} \leadsto^* (v, \sigma') \\ & \overline{(h[n \mapsto (x \leftarrow get(k); s, \sigma)], t)} \\ & \xrightarrow{n \rhd get(k) : \ v} \mathcal{C}(\mathbb{I}) \\ & (h[n \mapsto (s[x := v], \sigma')], t) \end{aligned}$$

$$get(V, n, \sigma, k) \leadsto^* (v, \sigma)$$

$$\begin{aligned} & \frac{\text{GET}}{\text{get}(V, n, \sigma, k)} \leadsto^* (v, \sigma') \\ & \overline{(h[n \mapsto (x \leftarrow get(k); s, \sigma)], t)} \\ & \frac{n \bowtie get(k) : v}{(h[n \mapsto (s[x := v], \sigma')], t)} \end{aligned}$$

$$\gcd(V, n, \sigma, k) \leadsto^* (v, \sigma)$$

$$\xrightarrow{n \rhd get(k):v} C(\mathbb{I})$$

$$\begin{aligned} & \text{GET} \\ & \underbrace{\text{get}(V, n, \sigma, k) \leadsto^* (v, \sigma')}_{\left(h[n \mapsto (x \leftarrow get(k); s, \sigma)], t\right)} \\ & \underbrace{\frac{n \bowtie get(k) : v}{b(n[n \mapsto (s[x := v], \sigma')], t)}}_{\text{C}(\mathbb{I})} \end{aligned}$$

$$\gcd(V, n, \sigma, k) \leadsto^* (v, \sigma)$$

$$\xrightarrow{n \rhd get(k):v} C(\mathbb{I})$$

Operational: Model the executions of the implementation I

Instrumented Concrete Operational Semantics

Concrete Operational Semantics

 ${\bf Instrumented\ Concrete\ Operational\ Semantics}$

Concrete Operational Semantics

 ${\bf Instrumented\ Concrete\ Operational\ Semantics}$

Concrete Operational Semantics

Parametric on the implementation \mathbb{I}

 $\to_{\mathcal{I}(\mathbb{I})}$ is similar to non-instrumented $\to_{\mathcal{C}(\mathbb{I})}$

 COS_A : Abstract Causal Operational Semantics

 ${\bf Instrumented\ Concrete\ Operational\ Semantics}$

Concrete Operational Semantics

Parametric on the implementation \mathbb{I}

 $\to_{\mathcal{I}(\mathbb{I})}$ is similar to non-instrumented $\to_{\mathcal{C}(\mathbb{I})}$

"Uniquely identify put operations to track causal dependencies between them."

Refine

Instrumented Concrete Operational Semantics

Concrete Operational Semantics

Well-Reception | Refine

Instrumented Concrete Operational Semantics

Concrete Operational Semantics

 COS_A : Abstract Causal Operational Semantics

Well-Reception Refine

Instrumented Concrete Operational Semantics

Concrete Operational Semantics

Theorem (Sufficiency of Well-Reception)

Every well-receptive implementation is causally consistent.

 $COS_{\mathcal{A}}$: Abstract Causal Operational Semantics

Well-Reception Refine

Instrumented Concrete Operational Semantics

Concrete Operational Semantics

Definition (Well-Reception)

An implementation is *well-receptive* iff there exists a *function* Rec for the implementation such that the four conditions InitCond, StepCond, CauseCond, and SeqCond are satisfied.

$$c \leftarrow Rec(\sigma, n)$$



```
WellRec(I) \triangleq
    \exists Rec : (State(IV), N) \rightarrow C :
    let \operatorname{Rec}'(W, n', n) =
          let (H[n' \mapsto (\neg, \sigma, \neg)], \neg) = W in
           Rec(\sigma, n) in
    InitCond(I, Rec') \land StepCond(I, Rec') \land CauseCond(I, Rec')
      ∧ SeqCond(I)
 InitCond(I, Rec') \triangleq \forall p, n, n':
    Rec'(W_{I0}(p), n, n') = 0
 StepCond(I, Rec') \triangleq \forall p, h_T, W_T, l_T, W'_T:
    (W_{I0}(p) \xrightarrow{h_{I}}^{*} W_{I} \land W_{I} \xrightarrow{l_{I}} U_{I}) \xrightarrow{W'_{I}} \Rightarrow
       f \text{ Case } l_{\mathcal{I}} = n, \neg \triangleright put(\neg, \neg, \neg) : \neg, \neg
              Rec'(W_T', n, n) = Rec'(W_T, n, n) + 1 \wedge
              \forall n' : n' \neq n \Rightarrow \text{Rec}'(W'_{\tau}, n, n') = \text{Rec}'(W_{\tau}, n, n')
          Case l_{\mathcal{I}} = n, \neg \triangleright get(\neg, \neg): \neg, \neg

\forall n' : Rec'(W'_{\mathcal{I}}, n, n') = Rec'(W_{\mathcal{I}}, n, n')
          Case l_{\tau} = n', c', n \triangleright update(\_, \_, \_):
              \begin{array}{l} \operatorname{Rec}'(W_{\mathcal{I}}, n, n') + 1 = c' \land \\ \operatorname{Rec}'(W_{\mathcal{I}}, n, n') = \operatorname{Rec}'(W_{\mathcal{I}}, n, n') + 1 \land \\ \forall n'' : n'' \neq n' \Rightarrow \operatorname{Rec}'(W_{\mathcal{I}}, n, n'') = \operatorname{Rec}'(W_{\mathcal{I}}, n, n'') \end{array}
 CauseCond(I, Rec') \triangleq \forall p, h_T, W_T, l_T, W_T', l_T''
          (W_{\mathcal{I}0}(p) \xrightarrow{h_{\mathcal{I}}}^* W_{\mathcal{I}} \wedge W_{\mathcal{I}} \wedge W_{\mathcal{I}} \xrightarrow{l_{\mathcal{I}}} W_{\mathcal{I}}')
            \land LlsUpdate(l_T) \land
             let \_, \_, n \triangleright update(\_, \_, \_, m) : \_ = l_T
            let n'', c'' \triangleright put(\underline{\ \ \ \ \ \ \ \ )} : \underline{\ \ \ \ \ \ \ \ \ \ } = l''_{\tau} in
         Rec'(W_{\mathcal{I}}, n, n'') > c''
 SeqCond(I) \triangleq \forall p, h_C, W_C:
    W_{\mathcal{C}0}(p) \xrightarrow{h_{\mathcal{C}}}^* \underset{\mathcal{C}(\mathbb{I})}{\overset{*}{\longrightarrow}} W_{\mathcal{C}} \Rightarrow \exists W_{\mathcal{S}}' \colon W_{\mathcal{S}0} \xrightarrow{\mathsf{Eff}(h_{\mathcal{C}})}^* \underset{\mathcal{C}}{\overset{*}{\longrightarrow}} W_{\mathcal{C}}'
```

Causal memory: definitions, implementation, and programming

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DC'1995

Stronger Semantics for Low-Latency Geo-Replicated Storage

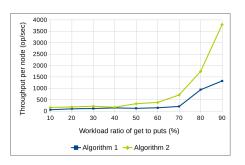
Wyatt Lloyd*, Michael J. Freedman*, Michael Kaminsky[†], and David G. Andersen[‡]
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NSDI'2013

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Chapar: Certified Causally Consistent Distributed Key-Value Stores

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Chapar@POPL'2016

Chapar for CC variants

Causal Consistency: Beyond Memory

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PPoPP'2016

Chapar for Op-based CRDT

Verifying Strong Eventual Consistency in Distributed Systems

VICTOR B. F. GOMES, University of Cambridge, UK MARTIN KLEPPMANN, University of Cambridge, UK DOMINIC P. MULLIGAN, University of Cambridge, UK ALASTAIR R. BERESFORD, University of Cambridge, UK

OOPSLA'2017

Chapar for State-based CRDT

Formal Specification and Verification of CRDTs

Peter Zeller, Annette Bieniusa, and Arnd Poetzsch-Heffter

University of Kaiserslautern, Germany {p_zeller,bieniusa,poetzsch}@cs.uni-kl.de

FORTE'2014



Coq for the equivalence between Op-based CRDT and State-based CRDT

A comprehensive study of Convergent and Commutative Replicated Data Types

Marc Shapiro, Nuno Preguiça, Carlos Baquero, Marek Zawirski

TR'2011

Coq for the "vis + ar" framework

syncope: Automatic Enforcement of Distributed Consistency Guarantees

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Gowtham Kaki Purdue

Suresh Jagannathan Purdue University

TR'2017

