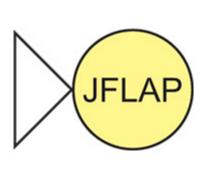
# An Interactive Approach to Formal Languages and Automata with JFLAP



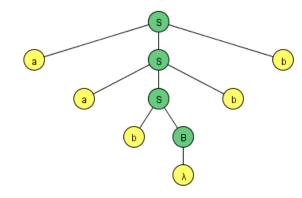
#### NSF Grant DUE CCLI-EMD 0442513



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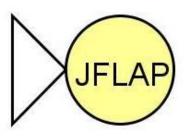
SIGCSE 2011 AlgoViz Workshop March 9, 2011

# Formal Languages and Automata Theory

- Traditionally taught
  - Pencil and paper exercises
  - No immediate feedback
- Different
  - More mathematical than most CS courses
  - Less hands-on than most CS courses
  - Programming is in most of their CS courses, not here

#### Why Develop Tools for Automata?

Textual	$(\{q_0, q_1, q_2\}, \{a, b\}, \delta, q_0, \{q_2\})$ $\delta = \{(q_0, b, q_0), (q_0, a, q_1), (q_1, a, q_0), (q_1, b, q_2), (q_2, a, q_1)\}$
Tabular	$egin{array}{c c c} & a & b \\ \hline q_0 & q_1 & q_0 \\ \hline q_1 & q_2 \\ \hline q_2 & & \end{array}$
Visual	do a do
Interactive	a q1 b q2



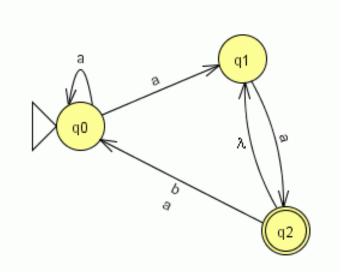
## Overview of JFLAP

- Java Formal Languages and Automata
   Package
- Instructional tool to learn concepts of Formal Languages and Automata Theory
- Topics:
  - Regular Languages
  - Context-Free Languages
  - Recursively Enumerable Languages
  - Lsystems
- With JFLAP your creations come to life!

## JFLAP – Regular Languages

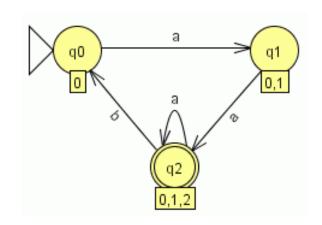
#### Create

- DFA and NFA
- Moore and Mealy
- regular grammar
- regular expression



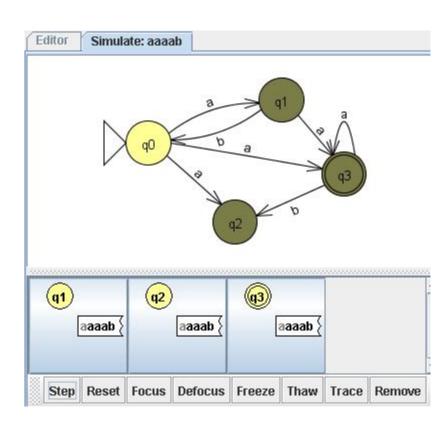
#### Conversions

- NFA to DFA to minimal DFA
- NFA  $\leftarrow \rightarrow$  regular expression
- $-NFA \leftarrow \rightarrow$  regular grammar



#### JFLAP – Regular languages (more)

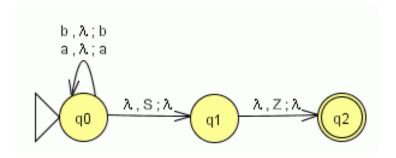
- Simulate DFA and NFA
  - Step with Closure or Step by State
  - Fast Run
  - Multiple Run
- Combine two DFA
- Compare Equivalence
- Brute Force Parser
- Pumping Lemma



## JFLAP – Context-free Languages

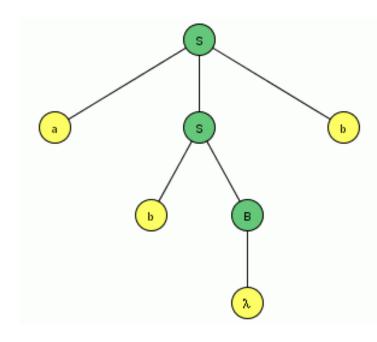
#### Create

- Nondeterministic PDA
- Context-free grammar
- Pumping Lemma



#### Transform

- $-PDA \rightarrow CFG$
- CFG → PDA (LL & SLR parser)
- $-CFG \rightarrow CNF$
- CFG → Parse table (LL and SLR)
- CFG → Brute Force Parser



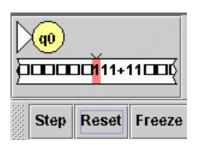
# JFLAP – Recursively Enumerable Languages

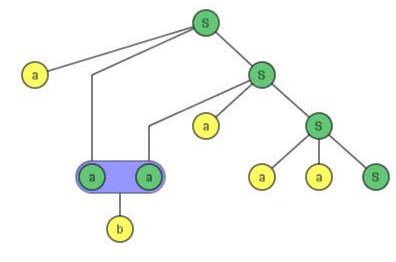
#### Create

- Turing Machine (1-Tape)
- Turing Machine (multi-tape)
- Building Blocks
- Unrestricted grammar

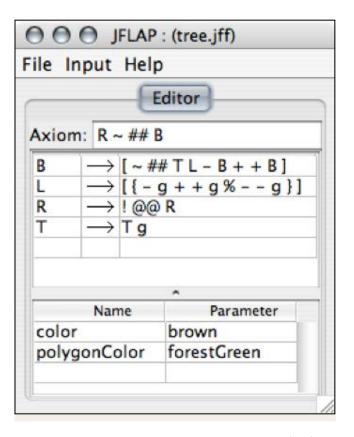
#### Parsing

 Unrestricted grammar with brute force parser

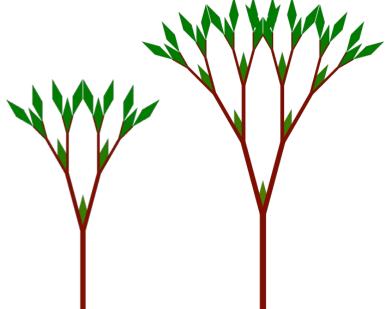




#### JFLAP - L-Systems

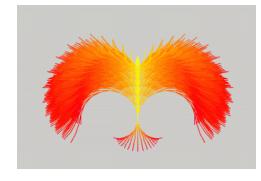


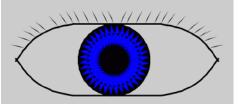
 This L-System renders as a tree that grows larger with each successive derivation step.

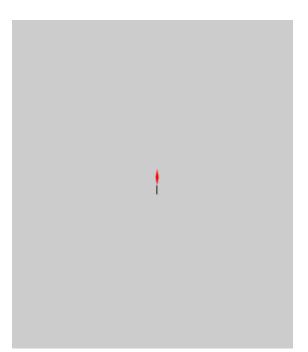


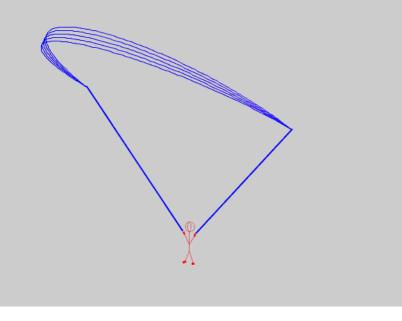
# Students love L-Systems

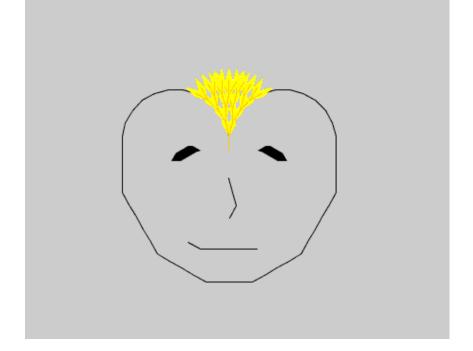












#### JFLAP's Use Around the World

- JFLAP web page has over 300,000 hits since 1996
- Google Search
  - JFLAP appears on over 9830 web pages
  - Note: search only public web pages
- JFLAP been downloaded in over 160 countries



#### Two-year JFLAP Study

Fourteen
Faculty Adopter
Participants

- -small, large
- public, private
- includes minority institutions

- Duke
- UNC-Chapel Hill
- Emory
- Winston-Salem State University
- United States Naval Academy
- Rensselaer Polytechnic Institute
- UC Davis
- Virginia State University
- Norfolk State University
- University of Houston
- Fayetteville State University
- University of Richmond
- San Jose State University
- Rochester Institute of Technology

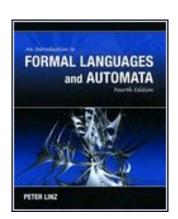
## **Key Findings**

- All the faculty used JFLAP in their courses
  - They used it mostly for homework, some used it for class demonstrations.
- Students had a high opinion of JFLAP
- Four-fifths of the students thought JFLAP was easy to use to draw automata, simulate and interpret the results.
- The majority of students felt that having access to JFLAP made learning course concepts easier, made them feel more engaged in the course and made the course more enjoyable.
- Over half of the students used JFLAP to study for exams, and thought that the time and effort spent using JFLAP helped them get a better grade in the course.
- There was a control group in the second year, but the difference in knowledge between the control group and the JFLAP group was not statistically significant.

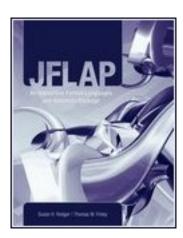
#### JFLAP Materials

JFLAP works well with Linz book

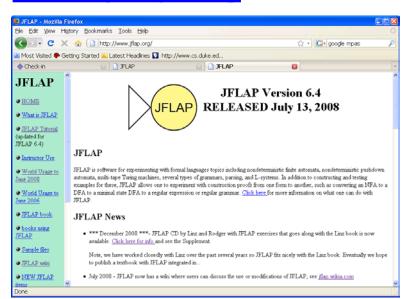
New CD supplement with JFLAP exercises to go with this book



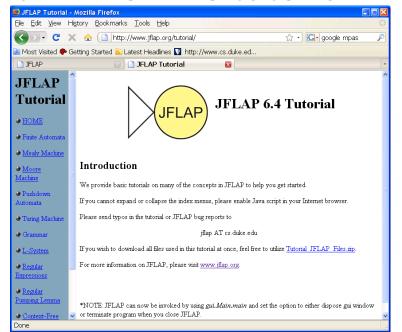
JFLAP book



#### www.jflap.org



#### JFLAP online tutorial



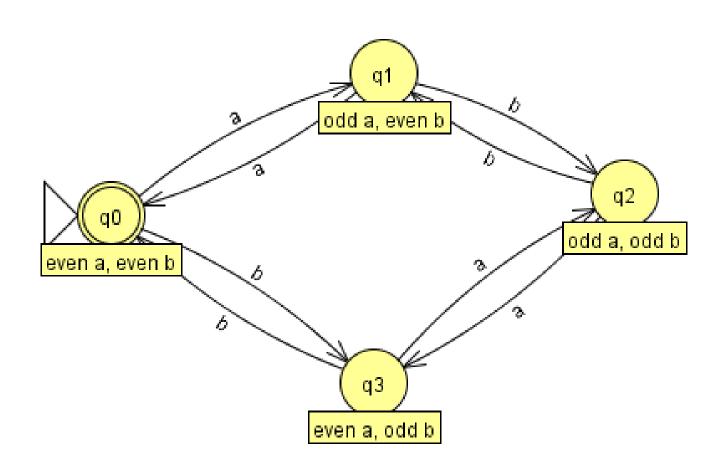
# JFLAP Examples in Lecture

## Example

 Create a DFA that recognizes strings with an even number of a's and an even number of b's

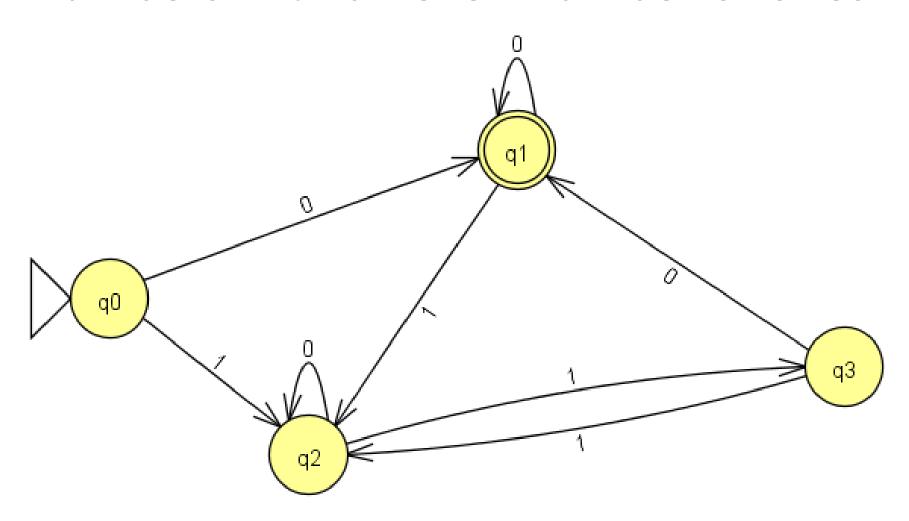
## Example

 Create a DFA that recognizes strings with an even number of a's and an even number of b's



# Example – DFA for even binary numbers with an even number of ones

# Example – DFA for even binary numbers with an even number of ones

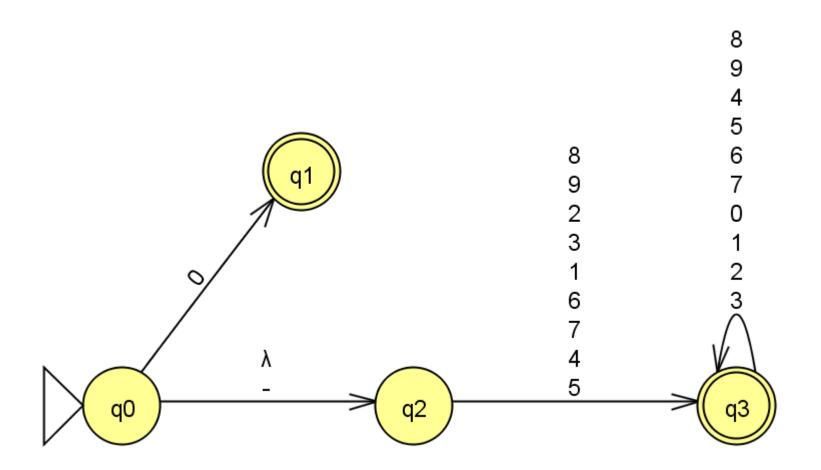


# Example: Build an NFA for valid integers

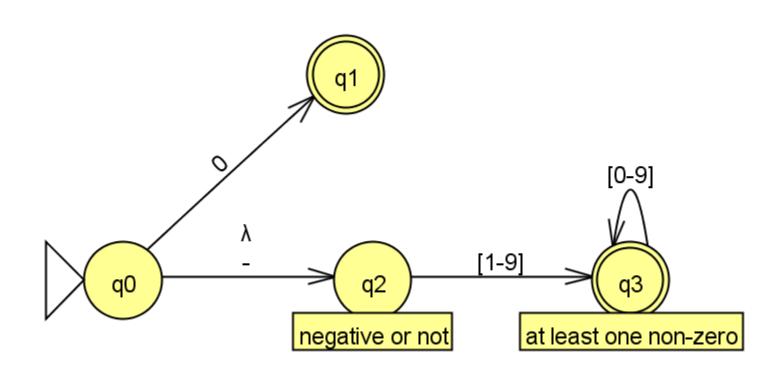
#### • Example:

- Valid integers {-3, 8, 0, 456, 13, 500, ...}
- Not valid: {006, 3-6, 4.5, ...}

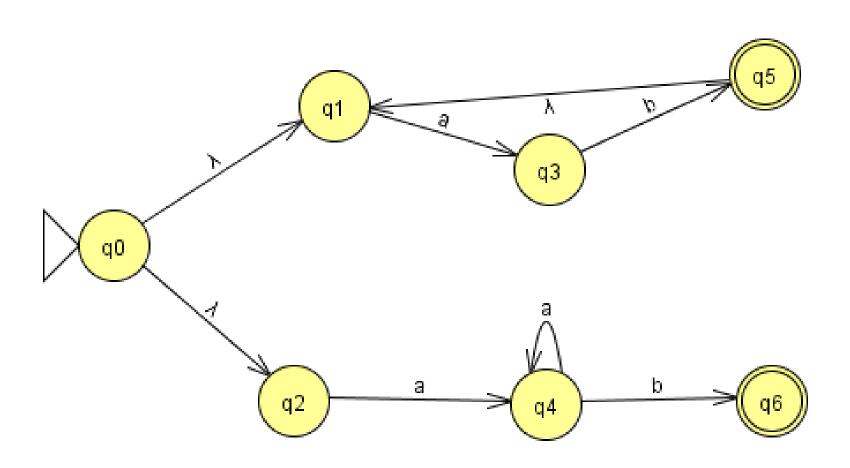
# NFA for all valid integers



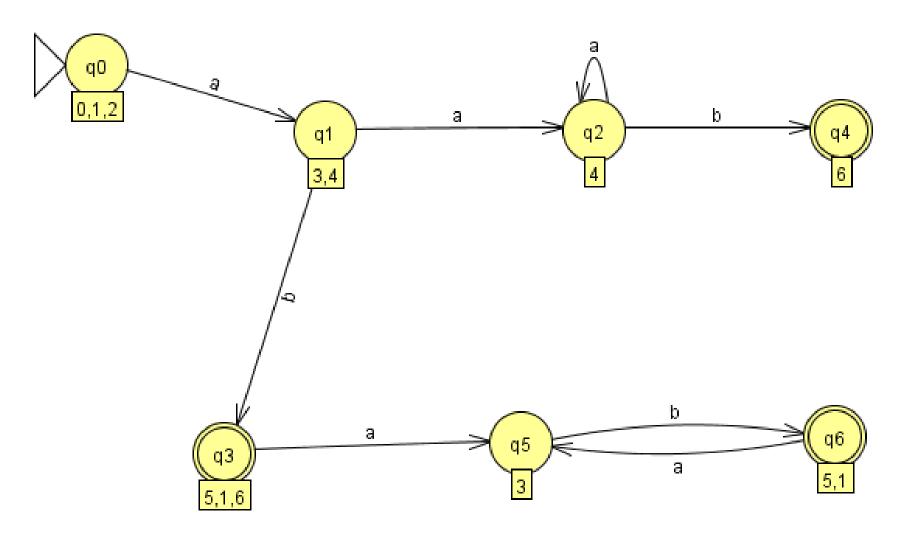
## DFA annotated and w/shortcut



# Example: NFA run and convert to DFA



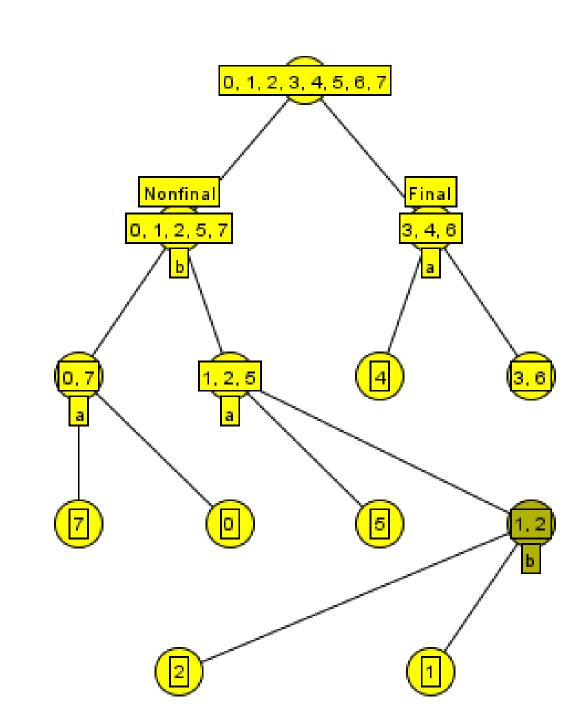
# **Corresponding DFA**



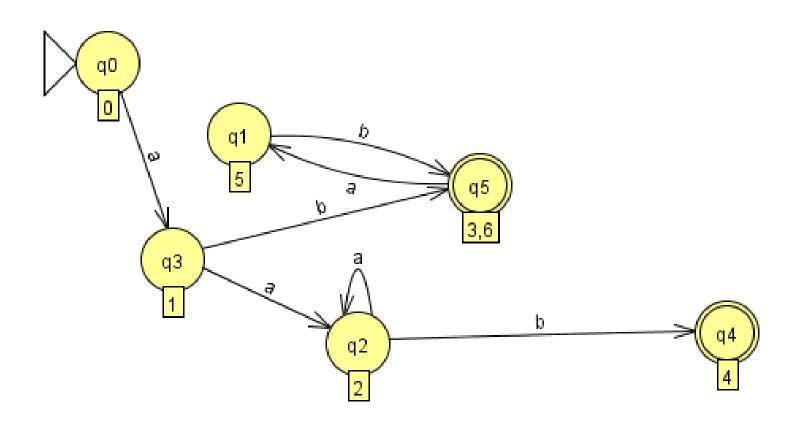
#### Minimize DFA

First add trap state q7

then build tree of distinguished states



#### Final Minimal State DFA



#### What next?

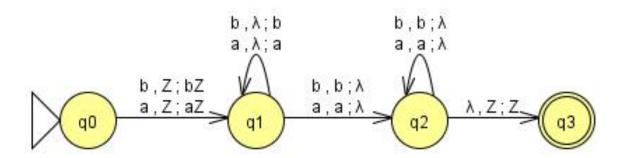
- Can convert to a regular expression ...
- Can convert to an NFA...

#### Using JFLAP during Lecture

- Use JFLAP to build examples of automata or grammars
- Use JFLAP to demo proofs
- Load a JFLAP example and students work in pairs to determine what it does, or fix it if it is not correct.

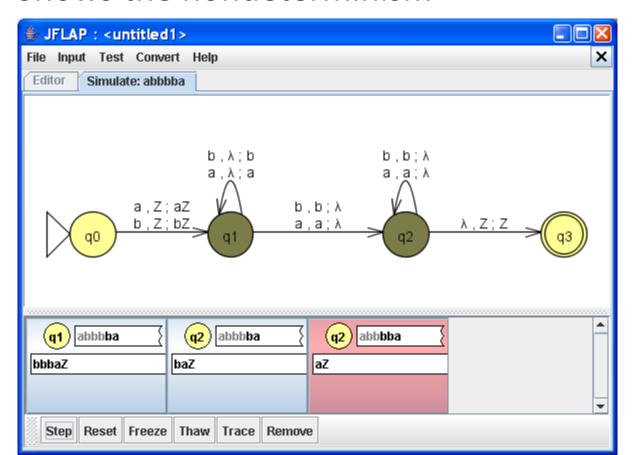
## Example: JFLAP during Lecture

- Ask students to write on paper an NPDA for palindromes of even length
- Build one of their solutions using JFLAP
  - Shows students how to use JFLAP



#### Example 1: JFLAP during Lecture (cont)

- Run input strings on the NPDA
  - Shows the nondeterminism



## Example: JFLAP during Lecture

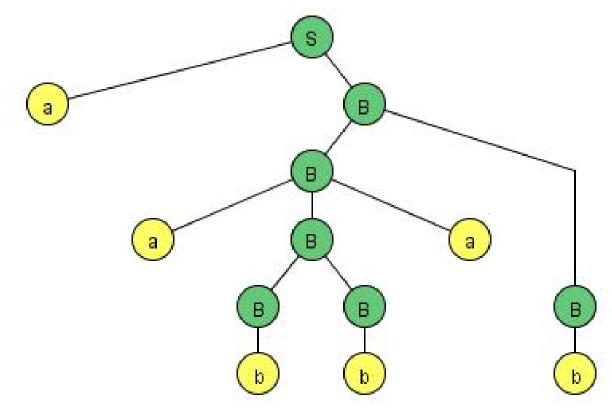
- Brute Force Parser
  - Give a grammar with a lambdaproduction and unit production
  - Run it in JFLAP, see how long it takes (LONG)
    - Is aabbab in L?
  - Transform the grammar to remove the lambda and unitproductions
  - Run new grammar in JFLAP,
     runs much faster!

S	->	aB
В	$\longrightarrow$	BB
В	$\rightarrow$	аВа
В	$\longrightarrow$	b
В	->	λ

S	$\rightarrow$	aВ
В	$\rightarrow$	ВВ
В	$\rightarrow$	aBa
В	$\rightarrow$	b
S	$\rightarrow$	а
В	$\rightarrow$	В
В	$\rightarrow$	aa

# Example 2 (cont) Parse Tree Results

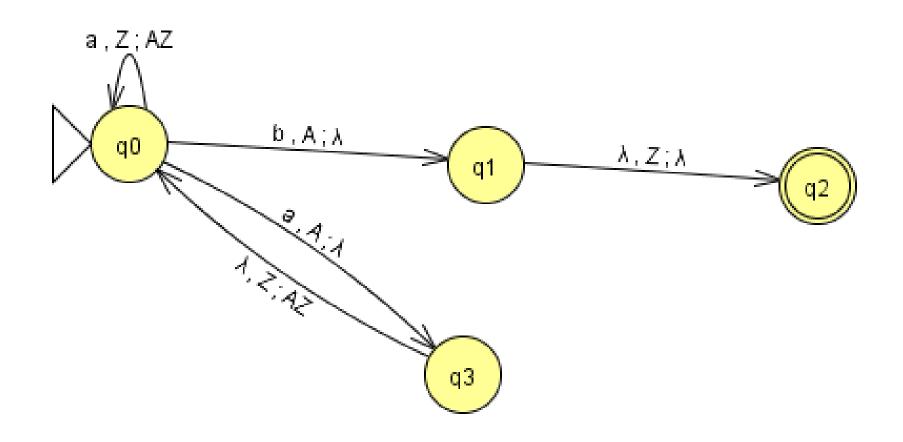
- First Grammar 1863 nodes generated
- Second Grammar 40 nodes generated
- Parse tree is the same.



# With JFLAP, Exploring Concepts too tedious for paper

- Load a Universal Turing Machine and run it
- See the exponential growth in an NFA or NPDA
- Convert an NPDA to a CFG
  - Large grammar with useless rules
  - Run both on the same input and compare
  - Transform grammar (remove useless rules)

#### NPDA to CFG



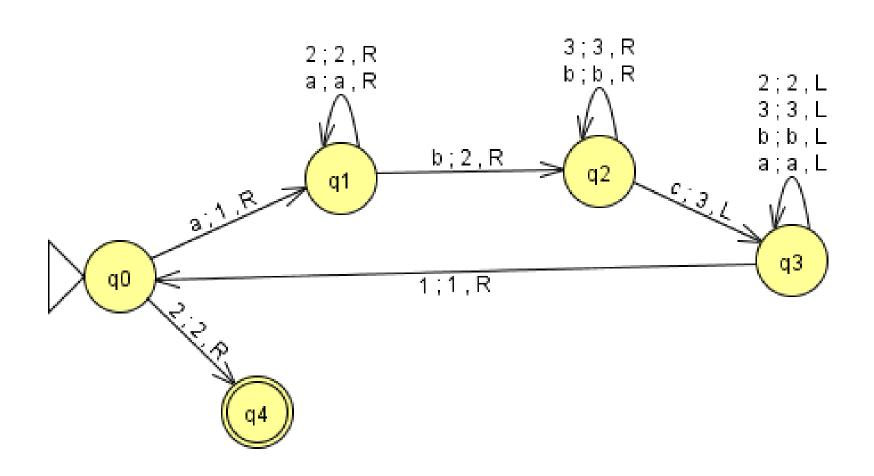
#### JFLAP's use Outside of Class

- Homework problems
  - Turn in JFLAP files
  - OR turn in on paper, check answers in JFLAP
- Recreate examples from class
- Work additional problems
  - Receive immediate feedback

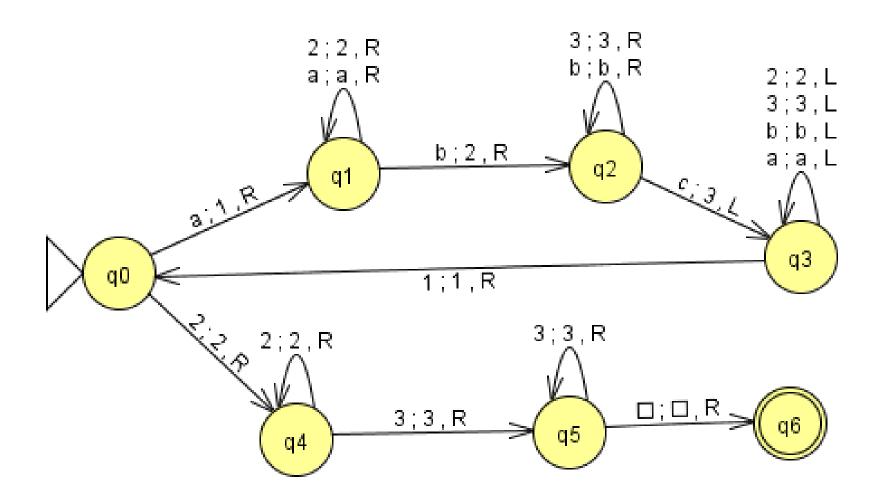
## Ordering of Problems in Homework

- Order questions so they are incremental in the usage of JFLAP
  - 1. Load a DFA. What is the language? Students only enter input strings.
  - 2. Load a DFA that is not correct. What is wrong? Fix it.
    - Students only modifying a small part.
  - 3. Build a DFA for a specific language. *Last, students build from scratch.*

#### Is this a TM for anbncn?



#### Here is the correct TM for anbnch



## Why study finite automata?

- Application: Compiler
- Compiler identifies your syntax errors
- Can write a big DFA to identify all words in a Java program
  - integers, doubles, boolean
  - keywords, variable names
  - arithmetic operators, punctuation symbols
- Example LR Parser...

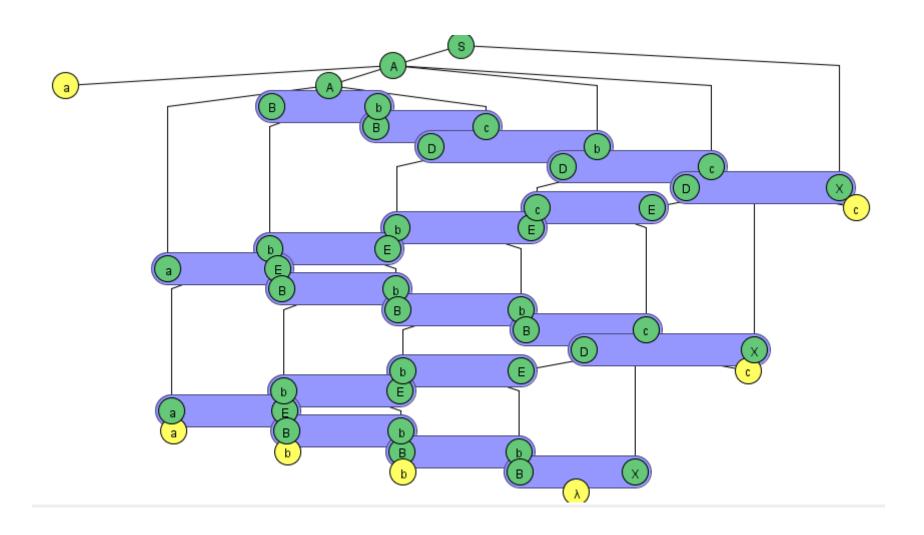
#### Lsystems

- Another type of grammar
  - Show a simple L-System
  - Show a tree
  - Show a fractal

#### Unrestricted Grammar - anbncn

S	$\rightarrow$	AX
A	$\rightarrow$	aAbc
A	$\rightarrow$	aBbc
Bb	$\rightarrow$	bВ
Вс	$\rightarrow$	D
De	$\rightarrow$	сD
Db	$\rightarrow$	bD
DX	$\rightarrow$	EXc
BX	$\rightarrow$	λ
сE	$\rightarrow$	Ec
bЕ	$\rightarrow$	Eb
аE	$\rightarrow$	aВ

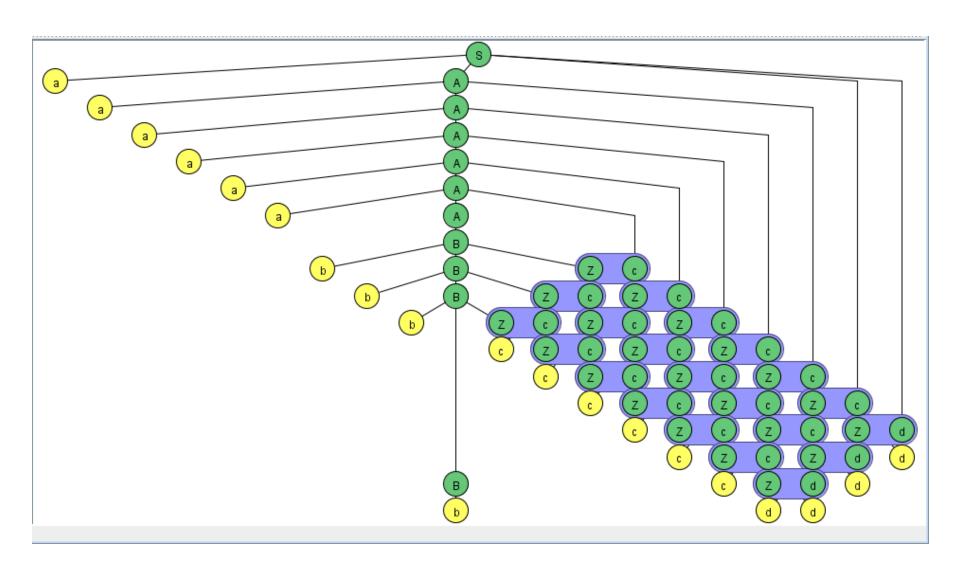
#### Trace aabbcc



# Example - Unrestricted Grammar anbmcndm

S	$\rightarrow$	aAcd
Α	$\rightarrow$	aAc
Α	$\rightarrow$	В
В	$\rightarrow$	bBZ
В	$\rightarrow$	b
Zc	$\rightarrow$	cZ
Zd	$\rightarrow$	dd

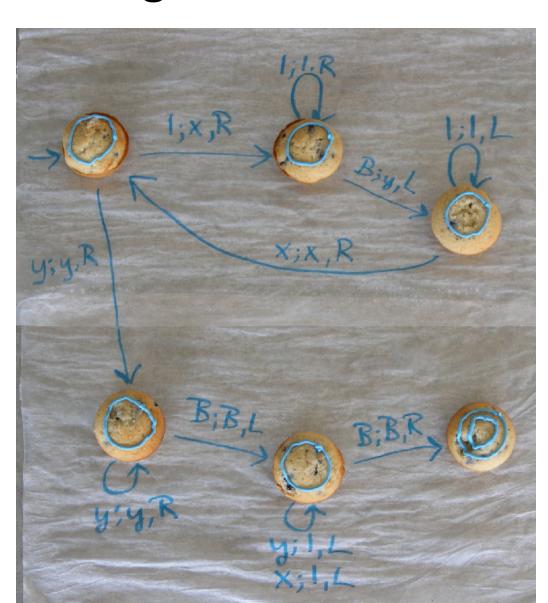
#### Example – Unrestricted Grammar (cont)



# There are other ways to get interaction in this course besides software...

# Interaction in Class – Props Edible Turing Machine

- TM for f(x)=2x where x is unary
- TM is not correct, can you fix it? Then eat it!
- States are blueberry muffins



# Students building DFA with cookies and icing



