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# IndPrinciples: Induction Principles(IndPrinciples.v)

## **Keywords**

# **Key Ideas**

#### General rule for t\_ind:

- The type declaration t gives several constructors; each corresponds to one clause of the induction principle.
- Each constructor c takes argument types a1 ... an.
- Each ai can be either t (the datatype we are defining) or some other type s.
- The corresponding case of the induction principle says:
  - "For all values x1 ... xn of types a1 ... an, if P holds for each of the inductive arguments (each xi of type t), then P holds for c x1 ... xn ".

## **Tactics**

- apply nat\_ind. We do not introduce n into the context before applying nat\_ind.
- ``

#### **Definitions and Theorems**

#### **Basics**

- Theorem  $mult_0_r'$  : forall n : nat, n \* 0 = 0.
- Theorem plus\_one\_r' : forall n : nat, n + 1 = S n.
- Inductive yesno : Type := | yes | no.
- Inductive rgb : Type := | red | green | blue.

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```
• Inductive natlist : Type := | nnil | ncons (n : nat) (l : natlist).
```

- Inductive byntree : Type := | bempty | bleaf (yn : yesno) | nbranch (yn : yesno) (t1 t2 : byntree).
- Inductive ExSet : Type :=

#### **Polymorphism**

- Inductive list (X:Type) : Type := | nil : list X | cons : X → list X → list X.
- Inductive tree (X:Type) : Type := | leaf (x : X) | node (t1 t2 : tree X).

#### **Induction Hypotheses**

### **Problems**

Inductive foo (X : Type) (Y : Type) := | bar (x : X) | baz (y : Y) | quux (f1 : nat -> foo X Y). Check foo\_ind.
 如何生成 quux 对应的归纳原理 (Induction Principle)?

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