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1 |----- MODULE CCTest -----|
  | Test of CC Module |
5 | EXTENDS CC |
6 |-----|
  | Test case: The following histories are from Figure 2 of the POPL'2017 paper.
  | Naming Conventions:
  |   - ha: history of Figure 2(a)
  |   - hasa: session a of history ha
  | TODO:
  | - to add more test cases
  | - to automatically generate test cases that do or do not satisfy the specs
  |   - consider Section 3.2 of POPL'2017
  |   - ref: the MonkeyDB paper
23 hasa  $\triangleq \langle W(\text{"x"}, 1, 1), R(\text{"x"}, 2, 2) \rangle$ 
24 hasb  $\triangleq \langle W(\text{"x"}, 2, 3), R(\text{"x"}, 1, 4) \rangle$ 
25 ha  $\triangleq \{hasa, hasb\}$  CM but not CCv
27 hbsa  $\triangleq \langle W(\text{"z"}, 1, 1), W(\text{"x"}, 1, 2), W(\text{"y"}, 1, 3) \rangle$ 
28 hbsb  $\triangleq \langle W(\text{"x"}, 2, 4), R(\text{"z"}, 0, 5), R(\text{"y"}, 1, 6), R(\text{"x"}, 2, 7) \rangle$ 
29 hb  $\triangleq \{hbsa, hbsb\}$  CCv but not CM
31 hcsa  $\triangleq \langle W(\text{"x"}, 1, 1) \rangle$ 
32 hcsb  $\triangleq \langle W(\text{"x"}, 2, 2), R(\text{"x"}, 1, 3), R(\text{"x"}, 2, 4) \rangle$ 
33 hc  $\triangleq \{hcsa, hcsb\}$  CC but not CM nor CCv
35 hdsa  $\triangleq \langle W(\text{"x"}, 1, 1), R(\text{"y"}, 0, 2), W(\text{"y"}, 1, 3), R(\text{"x"}, 1, 4) \rangle$ 
36 hdsb  $\triangleq \langle W(\text{"x"}, 2, 5), R(\text{"y"}, 0, 6), W(\text{"y"}, 2, 7), R(\text{"x"}, 2, 8) \rangle$ 
37 hd  $\triangleq \{hdsa, hdsb\}$  CC, CM, and CCv but no SC
39 hesa  $\triangleq \langle W(\text{"x"}, 1, 1), W(\text{"y"}, 1, 2) \rangle$ 
40 hesb  $\triangleq \langle R(\text{"y"}, 1, 3), W(\text{"x"}, 2, 4) \rangle$ 
41 hesc  $\triangleq \langle R(\text{"x"}, 2, 5), R(\text{"x"}, 1, 6) \rangle$ 
42 he  $\triangleq \{hesa, hesb, hesc\}$  not CC (nor CM, nor CCv)
44 all  $\triangleq \{ha, hb, hc, hd, he\}$ 
45 |-----|
46 THEOREM WellFormedTheorem  $\triangleq$  test of well-formedness of histories
47  $\forall h \in all : WellFormed(h)$ 
48 |-----|
  | Test of the auxiliary definitions for the axioms
52 CardOfProgramOrderOfHistory(h)  $\triangleq$ 
53 LET CardOfProgramOrderOfSession(s)  $\triangleq$ 
54 IF Len(s)  $\leq 1$  THEN 0 ELSE Sum(1 .. Len(s) - 1)
55 IN ReduceSet(LAMBDA s, x : CardOfProgramOrderOfSession(s) + x, h, 0)

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57 THEOREM ProgramOrderCardinalityTheorem  $\triangleq$  test of PO(h)
58    $\forall h \in \{ha, hb, hc, hd, he\} :$ 
59     Cardinality(PO(h)) = CardOfProgramOrderOfHistory(h)

61 THEOREM POPastTest  $\triangleq$  test of POPast(h, o)
62    $\wedge POPast(ha, R("x", 2, 2)) = \{W("x", 1, 1)\}$ 
63    $\wedge POPast(hb, R("y", 1, 6)) = \{W("x", 2, 4), R("z", 0, 5)\}$ 
64    $\wedge POPast(hc, W("x", 2, 2)) = \{\}$ 
65    $\wedge POPast(hd, R("x", 1, 4)) = \{W("x", 1, 1), R("y", 0, 2), W("y", 1, 3)\}$ 
66    $\wedge POPast(he, W("x", 2, 4)) = \{R("y", 1, 3)\}$ 

68 THEOREM CausalPastTest  $\triangleq$  TODO: test of CausalPast(co, o)
69   FALSE

71 THEOREM CausalHistTest  $\triangleq$  TODO: test of CausalHist(co, o)
72   FALSE

74 THEOREM CausalArbTest  $\triangleq$  TODO: test of CausalArb(co, ar, o)
75   FALSE

76 |-----|
    | Test of axioms
    | TODO: test of AxCausalValue, AxCausalArb, etc
    |-----|

82 THEOREM RWRegSemanticsTest  $\triangleq$  Test of RWRegSemanticsTest(seq, o)
83   seq =  $\langle \rangle$ 
84    $\wedge RWRegSemantics(\langle \rangle, R("x", InitVal, 1))$ 
85    $\wedge RWRegSemantics(\langle \rangle, W("x", 1, 1))$ 
86    $\wedge \neg RWRegSemantics(\langle \rangle, R("x", 2, 1))$ 
87   no W("x", -, -) in seq
88    $\wedge RWRegSemantics(\langle W("y", 1, 1), W("z", 1, 2), W("y", 1, 3) \rangle, R("x", InitVal, 4))$ 
89    $\wedge RWRegSemantics(\langle W("y", 1, 1), W("z", 1, 2), W("y", 1, 3) \rangle, W("x", 1, 4))$ 
90    $\wedge \neg RWRegSemantics(\langle W("y", 1, 1), W("z", 1, 2), W("y", 1, 3) \rangle, R("x", 1, 4))$ 
91   contains W("x", -, -) in seq
92    $\wedge RWRegSemantics(\langle W("x", 1, 1), W("y", 1, 2), W("x", 2, 3), W("z", 1, 4) \rangle, R("x", 2, 5))$ 
93    $\wedge \neg RWRegSemantics(\langle W("x", 1, 1), W("y", 1, 2), W("x", 2, 3), W("z", 1, 4) \rangle, R("x", 1, 5))$ 
94 |-----|
    | Test of the definitions of causal consistency
    | ha: 4; hb: 7; hc: 4; hd: 8; he: 6
    |-----|

100 CCDefTest  $\triangleq$ 
101    $\wedge PrintT(CC(ha))$ 
102    $\wedge PrintT(CC(hc))$ 
103    $\wedge PrintT(\neg CC(he))$ 
104    $\wedge LET sat \triangleq \{ha, hb, hc, hd\}$ 
105     IN  $\wedge \forall h \in sat : CC(h)$ 
106      $\wedge \forall h \in all \setminus sat : \neg CC(h)$ 

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108  $CCvDefTest \triangleq$ 
109    $\wedge PrintT(\neg CCv(ha))$ 
110    $\wedge CCv(hb)$ 
111    $\wedge PrintT(\neg CCv(hc))$ 
112    $\wedge CCv(hd)$ 
113    $\wedge PrintT(\neg CCv(he))$ 

115   LET  $sat \triangleq \{hb, hd\}$ 
116   IN    $\wedge \forall h \in sat: CCv(h)$ 
117        $\wedge \forall h \in all \setminus sat: \neg CCv(h)$ 

118 |-----|
    | Test of the checking algorithms for causal consistency |
122  $CCAlgTest \triangleq$  | Test of the checking algorithm for  $CC$  (Causal Consistency)
123   LET  $sat \triangleq \{ha, hb, hc, hd\}$ 
124   IN    $\wedge \forall h \in sat :$ 
125        $\wedge PrintT(ToString(h) \circ " \text{ is differentiated: } " \circ ToString(IsDifferentiated(h)))$ 
126        $\wedge CCAlg(h)$ 
127        $\wedge \forall h \in all \setminus sat :$ 
128        $\wedge PrintT(ToString(h) \circ " \text{ is differentiated: } " \circ ToString(IsDifferentiated(h)))$ 
129        $\wedge \neg CCAlg(h)$ 
130 |-----|

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