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1 |----- MODULE CCTest -----|
  | Test of CC Module |
5 | EXTENDS CC |
6 |-----|
  | Test case: The following histories are from Figure 2 of the POPL'2017 paper. |
  | Naming Conventions: |
  |   - ha: history of Figure 2(a) |
  |   - hasa: session a of history ha |
  | TODO: |
  | - to add more test cases |
  | - to automatically generate test cases that do or do not satisfy the specs |
20 hasa  $\triangleq$   $\langle W(\text{"x"}, 1, 1), R(\text{"x"}, 2, 2) \rangle$ 
21 hasb  $\triangleq$   $\langle W(\text{"x"}, 2, 3), R(\text{"x"}, 1, 4) \rangle$ 
22 ha  $\triangleq$   $\{hasa, hasb\}$  CM but not CCv
24 hbsa  $\triangleq$   $\langle W(\text{"z"}, 1, 1), W(\text{"x"}, 1, 2), W(\text{"y"}, 1, 3) \rangle$ 
25 hbsb  $\triangleq$   $\langle W(\text{"x"}, 2, 4), R(\text{"z"}, 0, 5), R(\text{"y"}, 1, 6), R(\text{"x"}, 2, 7) \rangle$ 
26 hb  $\triangleq$   $\{hbsa, hbsb\}$  CCv but not CM
28 hcsa  $\triangleq$   $\langle W(\text{"x"}, 1, 1) \rangle$ 
29 hcsb  $\triangleq$   $\langle W(\text{"x"}, 2, 2), R(\text{"x"}, 1, 3), R(\text{"x"}, 2, 4) \rangle$ 
30 hc  $\triangleq$   $\{hcsa, hcsb\}$  CC but not CM nor CCv
32 hdsa  $\triangleq$   $\langle W(\text{"x"}, 1, 1), R(\text{"y"}, 0, 2), W(\text{"y"}, 1, 3), R(\text{"x"}, 1, 4) \rangle$ 
33 hdsb  $\triangleq$   $\langle W(\text{"x"}, 2, 5), R(\text{"y"}, 0, 6), W(\text{"y"}, 2, 7), R(\text{"x"}, 2, 8) \rangle$ 
34 hd  $\triangleq$   $\{hdsa, hdsb\}$  CC, CM, and CCv but no SC
36 hesa  $\triangleq$   $\langle W(\text{"x"}, 1, 1), W(\text{"y"}, 1, 2) \rangle$ 
37 hesb  $\triangleq$   $\langle R(\text{"y"}, 1, 3), W(\text{"x"}, 2, 4) \rangle$ 
38 hesc  $\triangleq$   $\langle R(\text{"x"}, 2, 5), R(\text{"x"}, 1, 6) \rangle$ 
39 he  $\triangleq$   $\{hesa, hesb, hesc\}$  not CC (nor CM, nor CCv)
41 all  $\triangleq$   $\{ha, hb, hc, hd, he\}$ 
42 |-----|
43 THEOREM WellFormedTheorem  $\triangleq$  test of well-formedness of histories
44  $\forall h \in all : WellFormed(h)$ 
45 |-----|
  | Test of program order |
49 CardOfProgramOrderOfHistory(h)  $\triangleq$ 
50 LET CardOfProgramOrderOfSession(s)  $\triangleq$ 
51 IF Len(s)  $\leq 1$  THEN 0 ELSE Sum(1 .. Len(s) - 1)
52 IN ReduceSet(LAMBDA s, x : CardOfProgramOrderOfSession(s) + x, h, 0)
54 THEOREM ProgramOrderCardinalityTheorem  $\triangleq$ 
55  $\forall h \in \{ha, hb, hc, hd, he\} :$ 

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56      Cardinality(ProgramOrder(h)) = CardOfProgramOrderOfHistory(h)

58  THEOREM POPastTest  $\triangleq$ 
59       $\wedge POPast(ha, R("x", 2, 2)) = \{W("x", 1, 1)\}$ 
60       $\wedge POPast(hb, R("y", 1, 6)) = \{W("x", 2, 4), R("z", 0, 5)\}$ 
61       $\wedge POPast(hc, W("x", 2, 2)) = \{\}$ 
62       $\wedge POPast(hd, R("x", 1, 4)) = \{W("x", 1, 1), R("y", 0, 2), W("y", 1, 3)\}$ 
63       $\wedge POPast(he, W("x", 2, 4)) = \{R("y", 1, 3)\}$ 
64  |-----|
65      Test of axioms
66  |-----|
67      Test of the definitions of causal consistency
68  |-----|
72  CCvTest  $\triangleq$ 
73       $\wedge PrintT(\neg CCv(ha))$  4
74       $\wedge CCv(hb) \setminus$  * 7
75       $\wedge PrintT(\neg CCv(hc))$  4
76       $\wedge CCv(hd) \setminus$  * 8
77       $\wedge PrintT(\neg CCv(he))$  6
78      LET sat  $\triangleq$  {hb, hd}
79      IN  $\wedge \forall h \in$  sat: CCv(h)
80       $\wedge \forall h \in$  all  $\setminus$  sat:  $\neg CCv(h)$ 
81  |-----|

\ * Modification History
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