MODULE *CCTest*

Test of *CC* Module

EXTENDS *CC*

Test case: The following histories are from Figure 2 of the *POPL*'2017 paper.

Naming Conventions:

– *ha*: history of Figure 2(*a*)
– *hasa*: session a of history ha

TODO:

- to add more test cases
- to automatically generate test cases that do or do not satisfy the specs

- consider Section 3.2 of *POPL*'2017
– *ref*: the *MonkeyDB* paper

$hasa \triangleq \langle W(\text{“x”}, 1, 1),\ R(\text{“x”}, 2, 2)\rangle$
$hasb \triangleq \langle W(\text{“x”}, 2, 3),\ R(\text{“x”}, 1, 4)\rangle$
$ha \triangleq \{hasa, hasb\}$ *CM* but not *CCv*

$hbsa \triangleq \langle W(\text{“z”}, 1, 1),\ W(\text{“x”}, 1, 2),\ W(\text{“y”}, 1, 3)\rangle$
$hbsb \triangleq \langle W(\text{“x”}, 2, 4),\ R(\text{“z”}, 0, 5),\ R(\text{“y”}, 1, 6),\ R(\text{“x”}, 2, 7)\rangle$
$hb \triangleq \{hbsa, hbsb\}$ *CCv* but not *CM*

$hcsa \triangleq \langle W(\text{“x”}, 1, 1)\rangle$
$hcsb \triangleq \langle W(\text{“x”}, 2, 2),\ R(\text{“x”}, 1, 3),\ R(\text{“x”}, 2, 4)\rangle$
$hc \triangleq \{hcsa, hcsb\}$ *CC* but not *CM* nor *CCv*

$hdsa \triangleq \langle W(\text{“x”}, 1, 1),\ R(\text{“y”}, 0, 2),\ W(\text{“y”}, 1, 3),\ R(\text{“x”}, 1, 4)\rangle$
$hdsb \triangleq \langle W(\text{“x”}, 2, 5),\ R(\text{“y”}, 0, 6),\ W(\text{“y”}, 2, 7),\ R(\text{“x”}, 2, 8)\rangle$
$hd \triangleq \{hdsa, hdsb\}$ *CC*, *CM*, and *CCv* but no *SC*

$hesa \triangleq \langle W(\text{“x”}, 1, 1),\ W(\text{“y”}, 1, 2)\rangle$
$hesb \triangleq \langle R(\text{“y”}, 1, 3),\ W(\text{“x”}, 2, 4)\rangle$
$hesc \triangleq \langle R(\text{“x”}, 2, 5),\ R(\text{“x”}, 1, 6)\rangle$
$he \triangleq \{hesa, hesb, hesc\}$ not *CC* (nor *CM*, nor *CCv*)

$all \triangleq \{ha, hb, hc, hd, he\}$

THEOREM $WellFormedTheorem \triangleq$ test of well-formedness of histories
$\forall\, h \in all : WellFormed(h)$

Test of the auxiliary definitions for the axioms

$CardOfProgramOrderOfHistory(h) \triangleq$
LET $CardOfProgramOrderOfSession(s) \triangleq$
IF $Len(s) \leq 1$ THEN 0 ELSE $Sum(1\,..\,Len(s)-1)$
IN $ReduceSet(\text{LAMBDA } s, x : CardOfProgramOrderOfSession(s) + x,\ h,\ 0)$

```
THEOREM ProgramOrderCardinalityTheorem ≜  test of ProgramOrder(h)
    ∀ h ∈ {ha, hb, hc, hd, he} :
        Cardinality(ProgramOrder(h)) = CardOfProgramOrderOfHistory(h)

THEOREM POPastTest ≜  test of POPast(h, o)
    ∧ POPast(ha, R("x", 2, 2))  = {W("x", 1, 1)}
    ∧ POPast(hb, R("y", 1, 6))  = {W("x", 2, 4), R("z", 0, 5)}
    ∧ POPast(hc, W("x", 2, 2)) = {}
    ∧ POPast(hd, R("x", 1, 4))  = {W("x", 1, 1), R("y", 0, 2), W("y", 1, 3)}
    ∧ POPast(he, W("x", 2, 4)) = {R("y", 1, 3)}

THEOREM CausalPastTest ≜  TODO: test of CausalPast(co, o)
    FALSE

THEOREM CausalHistTest ≜  TODO: test of CausalHist(co, o)
    FALSE

THEOREM CausalArbTest ≜  TODO: test of CausalArb(co, ar, o)
    FALSE
```

Test of axioms

TODO: test of *AxCausalValue*, *AxCausalArb*, etc

```
THEOREM RWRegSemanticsTest ≜  Test of RWRegSemanticsTest(seq, o)
     seq = ⟨⟩
    ∧ RWRegSemantics(⟨⟩, R("x", InitVal, 1))
    ∧ RWRegSemantics(⟨⟩, W("x", 1, 1))
    ∧ ¬RWRegSemantics(⟨⟩, R("x", 2, 1))
     no W("x", _, _) in seq
    ∧ RWRegSemantics(⟨W("y", 1, 1), W("z", 1, 2), W("y", 1, 3)⟩, R("x", InitVal, 4))
    ∧ RWRegSemantics(⟨W("y", 1, 1), W("z", 1, 2), W("y", 1, 3)⟩, W("x", 1, 4))
    ∧ ¬RWRegSemantics(⟨W("y", 1, 1), W("z", 1, 2), W("y", 1, 3)⟩, R("x", 1, 4))
     contains W("x", _, _) in seq
    ∧ RWRegSemantics(⟨W("x", 1, 1), W("y", 1, 2), W("x", 2, 3), W("z", 1, 4)⟩, R("x", 2, 5))
    ∧ ¬RWRegSemantics(⟨W("x", 1, 1), W("y", 1, 2), W("x", 2, 3), W("z", 1, 4)⟩, R("x", 1, 5))
```

Test of the definitions of causal consistency

ha: 4; *hb*: 7; *hc*: 4; *hd*: 8; he: 6

```
CCTest ≜
    ∧  PrintT(CC(ha))
    ∧  PrintT(CC(hc))
    ∧  PrintT(¬CC(he))
    ∧  LET sat ≜ {ha, hb, hc, hd}
       IN   ∧ ∀ h ∈ sat : CC(h)
            ∧ ∀ h ∈ all \ sat : ¬CC(h)
```

```
CCvTest ≜
    ∧ PrintT(¬CCv(ha))
  ∧ CCv(hb)
    ∧ PrintT(¬CCv(hc))
  ∧ CCv(hd)
  ∧ PrintT(¬CCv(he))

  LET sat ≜ {hb, hd}
  IN   ∧ ∀ h ∈ sat: CCv(h)
       ∧ ∀ h ∈ all \ sat: ¬CCv(h)
```

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