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MODULE CCTest
      Test of CC Module
 5 EXTENDS CC
       Test case: The following histories are from Figure 2 of the POPL'2017 paper.
       Naming Conventions:
       -ha: history of Figure 2(a)
       - hasa: session a of history ha
       TODO: to automatically generate histories
     hasa \stackrel{\triangle}{=} \langle W(\text{"x"}, 1, 1), R(\text{"x"}, 2, 2) \rangle
     hasb \triangleq \langle W(\text{``x''}, 2, 3), R(\text{``x''}, 1, 4) \rangle
     ha \stackrel{\Delta}{=} \{hasa, hasb\} CM but not CCv
    hbsa \triangleq \langle W(\text{"z"}, 1, 1), W(\text{"x"}, 1, 2), W(\text{"y"}, 1, 3) \rangle
     hbsb \stackrel{\Delta}{=} \langle W("x", 2, 4), R("z", 0, 5), R("y", 1, 6), R("x", 2, 7) \rangle
    hb \stackrel{\Delta}{=} \{hbsa, hbsb\} CCv but not CM
    hcsa \stackrel{\triangle}{=} \langle W("x", 1, 1) \rangle
     hcsb \triangleq \langle W("x", 2, 2), R("x", 1, 3), R("x", 2, 4) \rangle
     hc \stackrel{\Delta}{=} \{hcsa, hcsb\}\ CC \text{ but not } CM \text{ nor } CCv
     hdsa \triangleq \langle W("x", 1, 1), R("y", 0, 2), W("y", 1, 3), R("x", 1, 4) \rangle
     hdsb \triangleq \langle W("x", 2, 5), R("y", 0, 6), W("y", 2, 7), R("x", 2, 8) \rangle
    hd \stackrel{\Delta}{=} \{hdsa, hdsb\}\ CC, CM, \text{ and } CCv \text{ but no } SC
     hesa \triangleq \langle W(\text{"x"}, 1, 1), W(\text{"y"}, 1, 2) \rangle
     hesb \triangleq \langle R("y", 1, 3), W("x", 2, 4) \rangle
     hesc \triangleq \langle R("x", 2, 5), R("x", 1, 6) \rangle
     he \stackrel{\triangle}{=} \{hesa, hesb, hesc\} \text{ not } CC \text{ (nor } CM, \text{ nor } CCv)
36
37
     THEOREM WellFormedTheorem \stackrel{\triangle}{=} test of well-formedness of histories
          \forall h \in \{ha, hb, hc, hd, he\} : WellFormed(h)
39
40 F
      Test of program order
     CardOfProgramOrderOfHistory(h) \stackrel{\Delta}{=}
44
          LET CardOfProgramOrderOfSession(s) \stackrel{\Delta}{=}
45
                  IF Len(s) \le 1 THEN 0 ELSE Sum(1 ... Len(s) - 1)
46
                  ReduceSet(LAMBDA\ s,\ x: CardOfProgramOrderOfSession(s) + x,\ h,\ 0)
47
          IN
     THEOREM Program Order Cardinality Theorem \stackrel{\triangle}{=}
49
          \forall h \in \{ha, hb, hc, hd, he\}:
50
              Cardinality(ProgramOrder(h)) = CardOfProgramOrderOfHistory(h)
51
     THEOREM POPastTest \triangleq
           \land POPast(ha, R("x", 2, 2)) = \{W("x", 1, 1)\}\
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