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MODULE CCTest
      Test of CC Module
 5 EXTENDS CC
       Test case: The following histories are from Figure 2 of the POPL'2017 paper.
       Naming Conventions:
       -ha: history of Figure 2(a)
       - hasa: session a of history ha
       TODO:
       - to add more test cases
       - to automatically generate test cases that do or do not satisfy the specs
        - consider Section 3.2 of POPL'2017
        - ref: the MonkeyDB paper
    hasa \triangleq \langle W(\text{"x"}, 1, 1), R(\text{"x"}, 2, 2) \rangle
    hasb \triangleq \langle W("x", 2, 3), R("x", 1, 4) \rangle
     ha \stackrel{\triangle}{=} \{hasa, hasb\} CM but not CCv
    hbsa \triangleq \langle W("z", 1, 1), W("x", 1, 2), W("y", 1, 3) \rangle
     hbsb \triangleq \langle W("x", 2, 4), R("z", 0, 5), R("y", 1, 6), R("x", 2, 7) \rangle
     hb \stackrel{\triangle}{=} \{hbsa, hbsb\} CCv but not CM
    hcsa \stackrel{\triangle}{=} \langle W("x", 1, 1) \rangle
     hcsb \triangleq \langle W("x", 2, 2), R("x", 1, 3), R("x", 2, 4) \rangle
     hc \stackrel{\Delta}{=} \{hcsa, hcsb\} CC but not CM nor CCv
    hdsa \triangleq \langle W(\text{``x''}, 1, 1), R(\text{``y''}, 0, 2), W(\text{``y''}, 1, 3), R(\text{``x''}, 1, 4) \rangle
    hdsb \triangleq \langle W("x", 2, 5), R("y", 0, 6), W("y", 2, 7), R("x", 2, 8) \rangle
    hd \stackrel{\triangle}{=} \{hdsa, hdsb\}\ CC, CM, \text{ and } CCv \text{ but no } SC
     hesa \triangleq \langle W(\text{"x"}, 1, 1), W(\text{"y"}, 1, 2) \rangle
    hesb \stackrel{\triangle}{=} \langle R(\text{"y"}, 1, 3), W(\text{"x"}, 2, 4) \rangle
     hesc \triangleq \langle R("x", 2, 5), R("x", 1, 6) \rangle
     he \stackrel{\triangle}{=} \{hesa, hesb, hesc\} \text{ not } CC \text{ (nor } CM, \text{ nor } CCv)
     all \triangleq \{ha, hb, hc, hd, he\}
45
    THEOREM WellFormedTheorem \triangleq
                                                         test of well-formedness of histories
          \forall h \in all : WellFormed(h)
47
      Test of the auxiliary definitions for the axioms
     CardOfProgramOrderOfHistory(h) \stackrel{\Delta}{=}
52
          LET CardOfProgramOrderOfSession(s) \stackrel{\triangle}{=}
53
                  IF Len(s) < 1 THEN 0 ELSE Sum(1 ... Len(s) - 1)
54
                  ReduceSet(LAMBDA\ s,\ x: CardOfProgramOrderOfSession(s) + x,\ h,\ 0)
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55

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THEOREM ProgramOrderCardinalityTheorem \stackrel{\Delta}{=} test of <math>PO(h)
          \forall h \in \{ha, hb, hc, hd, he\}:
 58
             Cardinality(PO(h)) = CardOfProgramOrderOfHistory(h)
 59
     THEOREM POPastTest \stackrel{\triangle}{=} test of <math>POPast(h, o)
 61
          \land POPast(ha, R("x", 2, 2)) = \{W("x", 1, 1)\}\
 62
          \land POPast(hb, R("y", 1, 6)) = \{ W("x", 2, 4), R("z", 0, 5) \}
 63
          \land POPast(hc, W("x", 2, 2)) = \{\}
 64
          \land POPast(hd, R("x", 1, 4)) = \{ W("x", 1, 1), R("y", 0, 2), W("y", 1, 3) \}
 65
          \land POPast(he, W("x", 2, 4)) = \{R("y", 1, 3)\}\
 66
     THEOREM CausalPastTest \stackrel{\Delta}{=} TODO: test of CausalPast(co, o)
 68
          FALSE
 69
     THEOREM CausalHistTest \stackrel{\Delta}{=}
                                            TODO: test of CausalHist(co, o)
 71
         FALSE
 72
     THEOREM CausalArbTest \stackrel{\triangle}{=}
                                          TODO: test of CausalArb(co, ar, o)
 74
          FALSE
 75
 76 F
       Test of axioms
       TODO: test of AxCausalValue, AxCausalArb, etc
     THEOREM RWRegSemanticsTest \triangleq
                                                   Test of RWRegSemanticsTest(seq, o)
 82
 83
          \land RWRegSemantics(\langle \rangle, R("x", InitVal, 1))
 84
          \land RWRegSemantics(\langle \rangle, W("x", 1, 1))
 85
          \wedge \neg RWRegSemantics(\langle \rangle, R("x", 2, 1))
 86
           no W("x", \_, \_) in seq
 87
          \overline{\land RWRegSemantics}(\langle W("y", 1, 1), W("z", 1, 2), W("y", 1, 3) \rangle, R("x", InitVal, 4))
 88
          \land RWRegSemantics(\langle W("y", 1, 1), W("z", 1, 2), W("y", 1, 3) \rangle, W("x", 1, 4))
 89
          \land \neg RWRegSemantics(\langle W("y", 1, 1), W("z", 1, 2), W("y", 1, 3) \rangle, R("x", 1, 4))
 90
           contains W("x", \_, \_) in seq
 91
          \land RWRegSemantics((W("x", 1, 1), W("y", 1, 2), W("x", 2, 3), W("z", 1, 4)), R("x", 2, 5))
 92
          \land \neg RWRegSemantics(\langle W("x", 1, 1), W("y", 1, 2), W("x", 2, 3), W("z", 1, 4)\rangle, R("x", 1, 5))
 93
 94 |
      Test of the definitions of causal consistency
      ha: 4; hb: 7; hc: 4; hd: 8; he: 6
     CCTest \triangleq
100
          \wedge PrintT(CC(ha))
101
          \land PrintT(CC(hc))
102
          \wedge PrintT(\neg CC(he))
103
          \land Let sat \triangleq \{ha, hb, hc, hd\}
104
                     \land \forall h \in sat : CC(h)
105
106
                     \land \forall h \in all \setminus sat : \neg CC(h)
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CCvTest \triangleq
108
              \land \mathit{Print}T(\neg \mathit{CCv}(\mathit{ha}))
109
             \wedge \ CCv(hb)
110
              \wedge PrintT(\neg CCv(hc))
111
112
             \wedge \ CCv(hd)
             \land \mathit{PrintT}(\neg \mathit{CCv}(\mathit{he}))
113
            Let sat \stackrel{\Delta}{=} \{hb, hd\}
115
            IN \land \forall h \in sat: CCv(h)
116
117
                 \land \, \forall \, h \, \in \, all \, \backslash \, sat \colon \, \neg \, CCv(h)
118 L
        \setminus * \ \mathrm{Modification} \ \mathit{History}
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