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1  |----- MODULE TCS -----|
2  | See DISC'2018: Multi-Shot Distributed Transaction Commit |
3  |-----|
4  |
5  | EXTENDS Naturals, Integers, FiniteSets, Sequences, Functions, TLC,
6  |         FiniteSetsExt
7  |-----|
8  | CONSTANTS
9  |   Key,      the set of keys, ranged over by  $k \in Key$ 
10 |   Tid,       the set of transaction identifiers, ranged over by  $t \in Tid$ 
11 |   RSet,      RSet[ $t$ ]: the read set of  $t \in Tid$ 
12 |   WSet,      WSet[ $t$ ]: the write set of  $t \in Tid$ 
13 |   CVer,      CVer[ $t$ ]: the commit version of  $t \in Tid$ 
14 |   Shard,     the set of shards, ranged over by  $s \in Shard$ 
15 |   Coord,     Coord[ $t$ ]: the coordinator of  $t \in Tid$ 
16 |   KeySharding KeySharding[ $k$ ]: the shard that holds  $k \in Key$ 
17 |
18 | NotTid  $\triangleq$  CHOOSE  $t : t \notin Tid$ 
19 |
20 | Ver  $\triangleq$  0 .. Cardinality(Tid) with a distinguished minimum version 0
21 | Slot  $\triangleq$  0 .. Cardinality(Tid) - 1
22 |
23 | TKey( $t$ )  $\triangleq$  WSet[ $t$ ]  $\cup$  { $kv[1] : kv \in RSet[t]$ }
24 | TSharding( $t$ )  $\triangleq$  {KeySharding[ $k$ ] :  $k \in TKey(t)$ }
25 |
26 | ASSUME
27 |    $\wedge RSet \in [Tid \rightarrow SUBSET (Key \times Ver)]$ 
28 |    $\wedge \forall t \in Tid: RSet[t] \setminus * TODO: \text{one version per object}$ 
29 |    $\wedge WSet \in [Tid \rightarrow SUBSET Key]$ 
30 |    $\wedge \setminus * TODO: \text{"no blind update" assumption}$ 
31 |    $\wedge CVer \in [Tid \rightarrow Ver]$ 
32 |    $\wedge \setminus * TODO: \text{higher than any of the versions read}$ 
33 |    $\wedge Coord \in [Tid \rightarrow Shard]$ 
34 |    $\wedge KeySharding \in [Key \rightarrow Shard]$ 
35 |-----|
36 | VARIABLES
37 |   next,      next[ $s$ ]  $\in Z$  points to the last filled slot
38 |   txn,       txn[ $s$ ][ $i$ ] is the transaction (identifier) to certify in the  $i$ -th slot
39 |   vote,      vote[ $s$ ][ $i$ ] is the vote for txn[ $s$ ][ $i$ ]
40 |   dec,       dec[ $s$ ][ $i$ ] is the decision for txn[ $s$ ][ $i$ ]
41 |   phase,     phase[ $s$ ][ $i$ ] is the phase for txn[ $s$ ][ $i$ ]
42 |   msg,       the set of messages in transit
43 |   submitted the set of  $t \in Tid$  that have been submitted to TCS
44 |
45 | sVars  $\triangleq$   $\langle next, txn, vote, dec, phase \rangle$ 
46 | vars  $\triangleq$   $\langle next, txn, vote, dec, phase, msg, submitted \rangle$ 
47 |-----|

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52 Message  $\triangleq$  [type : { "PREPARE" }, t : Tid, s : Shard]
53    $\cup$  [type : { "PREPARE_ACK" }, s : Shard, n : Int, t : Tid, v : { "COMMIT", "ABORT" }]
54    $\cup$  [type : { "DECISION" }, p : Int, d : { "COMMIT", "ABORT" }, s : Shard]

56 Send(m)  $\triangleq$  msg' = msg  $\cup$  m
57 Delete(m)  $\triangleq$  msg' = msg  $\setminus$  m
58 SendAndDelete(sm, dm)  $\triangleq$  msg' = (msg  $\cup$  sm)  $\setminus$  dm

59 |-----|
60 TypeOK  $\triangleq$ 
61    $\wedge$  next  $\in$  [Shard  $\rightarrow$  Int]
62    $\wedge$  txn  $\in$  [Shard  $\rightarrow$  [Slot  $\rightarrow$  Tid  $\cup$  { NotTid }]]
63    $\wedge$  vote  $\in$  [Shard  $\rightarrow$  [Slot  $\rightarrow$  { "COMMIT", "ABORT", "NULL" }]]
64    $\wedge$  dec  $\in$  [Shard  $\rightarrow$  [Slot  $\rightarrow$  { "COMMIT", "ABORT", "NULL" }]]
65    $\wedge$  phase  $\in$  [Shard  $\rightarrow$  [Slot  $\rightarrow$  { "START", "PREPARED", "DECIDED" }]]
66    $\wedge$  msg  $\subseteq$  Message
67    $\wedge$  submitted  $\subseteq$  Tid

68 |-----|
69 Init  $\triangleq$ 
70    $\wedge$  next = [s  $\in$  Shard  $\mapsto$  -1]
71    $\wedge$  txn = [s  $\in$  Shard  $\mapsto$  [i  $\in$  Slot  $\mapsto$  NotTid]]
72    $\wedge$  vote = [s  $\in$  Shard  $\mapsto$  [i  $\in$  Slot  $\mapsto$  "NULL"]]
73    $\wedge$  dec = [s  $\in$  Shard  $\mapsto$  [i  $\in$  Slot  $\mapsto$  "NULL"]]
74    $\wedge$  phase = [s  $\in$  Shard  $\mapsto$  [i  $\in$  Slot  $\mapsto$  "START"]]
75    $\wedge$  msg = {}
76    $\wedge$  submitted = {}

77 |-----|
78 KeyOnShard(s)  $\triangleq$  { k  $\in$  Key : KeySharding[k] = s }

80 ComputeVote(t, s, n)  $\triangleq$ 
81   LET cs  $\triangleq$  { k  $\in$  Slot : committed slots before position n }
82    $\wedge$  k < n
83    $\wedge$  phase[s][k] = "DECIDED"
84    $\wedge$  dec[s][k] = "COMMIT" }
85   ct  $\triangleq$  { txn[s][k] : k  $\in$  cs } committed transactions
86   fv  $\triangleq$  IF  $\forall k \in \text{KeyOnShard}(s), v \in \text{Ver} :$ 
87      $\langle k, v \rangle \in \text{RSet}[t] \Rightarrow (\forall c \in ct : k \in \text{WSet}[c] \Rightarrow \text{CVer}[c] \leq v)$ 
88     THEN "COMMIT" ELSE "ABORT"
89   ps  $\triangleq$  { k  $\in$  Slot : "prepared to commit" slots before position n }
90    $\wedge$  k < n
91    $\wedge$  phase[s][k] = "PREPARED"
92    $\wedge$  vote[s][k] = "COMMIT" }
93   pt  $\triangleq$  { txn[s][k] : k  $\in$  ps } "prepared to commit" transactions

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94       $gv \triangleq$  "ABORT"
95       $gv \triangleq$  IF  $\forall k \in \text{KeyOnShard}(s), v \in \text{Ver}:$ 
96           $\wedge \langle k, v \rangle \in \text{RSet}[t] \Rightarrow (\forall p \in \text{pt} : k \notin \text{WSet}[p])$ 
97           $\wedge k \in \text{WSet}[t] \Rightarrow (\forall p \in \text{pt} : \langle k, v \rangle \notin \text{RSet}[p])$ 
98          THEN "COMMIT" ELSE "ABORT"
99      IN IF  $fv = \text{"COMMIT"} \wedge gv = \text{"COMMIT"}$  THEN "COMMIT" ELSE "ABORT"

101  $\text{ComputeDecision}(vs) \triangleq$ 
102     IF  $\forall v \in vs : v = \text{"COMMIT"}$  THEN "COMMIT" ELSE "ABORT"
103 |-----|
104  $\text{Certify}(t) \triangleq$  Certify  $t \in \text{Tid}$ 
105      $\wedge t \in \text{Tid} \setminus \text{submitted}$ 
106      $\wedge \text{Send}([\text{type} : \{\text{"PREPARE"}\}, t : \{t\}, s : \text{TSharding}(t))]$ 
107      $\wedge \text{submitted}' = \text{submitted} \cup \{t\}$ 
108      $\wedge \text{UNCHANGED } s\text{Vars}$ 

110  $\text{Prepare}(t, s) \triangleq$  Prepare  $t \in \text{Tid}$  on  $s \in \text{Shard}$  when receive "PREPARE( $t$ )" message
111      $\wedge \exists m \in \text{msg} :$ 
112          $\wedge m = [\text{type} \mapsto \text{"PREPARE"}, t \mapsto t, s \mapsto s]$ 
113          $\wedge \text{next}' = [\text{next} \text{ EXCEPT } ![s] = @ + 1]$ 
114          $\wedge \text{txn}' = [\text{txn} \text{ EXCEPT } ![s][\text{next}'[s]] = t]$ 
115          $\wedge \text{vote}' = [\text{vote} \text{ EXCEPT } ![s][\text{next}'[s]] = \text{ComputeVote}(t, s, \text{next}'[s])]$ 
116          $\wedge \text{phase}' = [\text{phase} \text{ EXCEPT } ![s][\text{next}'[s]] = \text{"PREPARED"}]$ 
117          $\wedge \text{SendAndDelete}(\{[\text{type} \mapsto \text{"PREPARE\_ACK"},$ 
118              $s \mapsto s,$ 
119              $n \mapsto \text{next}'[s],$ 
120              $t \mapsto t,$ 
121              $v \mapsto \text{vote}'[s][\text{next}'[s]]\},$ 
122              $\{m\})$ 
123          $\wedge \text{UNCHANGED } \langle \text{dec}, \text{submitted} \rangle$ 

125  $\text{PrepareAck}(t, s) \triangleq$  PrepareAck for  $t \in \text{Tid}$  on shard  $s \in \text{Shard}$  when receive all "PREPARE_ACK" messages for  $t$ 
126      $\wedge s = \text{Coord}[t]$ 
127      $\wedge \text{LET } ms \triangleq \{m \in \text{msg} : m.\text{type} = \text{"PREPARE\_ACK"} \wedge m.t = t\}$ 
128          $vs \triangleq \{m.v : m \in ms\}$ 
129          $ss \triangleq \{m.s : m \in ms\}$ 
130     IN  $\wedge ss = \text{TSharding}(t)$ 
131          $\wedge \text{SendAndDelete}(\{[\text{type} \mapsto \text{"DECISION"},$ 
132              $p \mapsto \text{ChooseUnique}(ms, \text{LAMBDA } m : m.s = \text{shard}).n,$ 
133              $d \mapsto \text{ComputeDecision}(vs),$ 
134              $s \mapsto \text{shard}] : \text{shard} \in ss\},$ 
135              $ms)$ 
136      $\wedge \text{UNCHANGED } \langle s\text{Vars}, \text{submitted} \rangle$ 

138  $\text{Decision}(s) \triangleq$  Decide on shard  $s \in \text{Shard}$  when receive a "DECISION" message
139      $\wedge \exists m \in \text{msg} :$ 

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140       $\wedge m.type = \text{"DECISION"}$ 
141       $\wedge m.s = s$ 
142       $\wedge dec' = [dec \text{ EXCEPT } ![s][m.p] = m.d]$ 
143       $\wedge phase' = [phase \text{ EXCEPT } ![s][m.p] = \text{"DECIDED"}]$ 
144       $\wedge Delete(\{m\})$ 
145       $\wedge \text{UNCHANGED } \langle next, txn, vote, submitted \rangle$ 
146 |-----|
147   $Next \triangleq$ 
148       $\vee \exists t \in Tid : Certify(t)$ 
149       $\vee \exists t \in Tid, s \in Shard :$ 
150           $\vee Prepare(t, s)$ 
151           $\vee PrepareAck(t, s)$ 
152       $\vee \exists s \in Shard :$ 
153           $\vee Decision(s)$ 
155   $Spec \triangleq Init \wedge \Box [Next]_{vars}$ 
156 |-----|
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  \ * Last modified Sun Jun 13 18:09:18 CST 2021 by hengxin
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