Package 'hdcate'

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Description This package uses a two-step procedure to estimate the conditional average treatment effects (CATE) with potentially high-dimensional covariate(s). In the first stage, the nuisance functions necessary for identifying CATE are estimated by machine learning methods, allowing the number of covariates to be comparable to or larger than the sample size. The second stage consists of a low-dimensional local linear regression, reducing CATE to a function of the covariate(s) of interest. The CATE estimator implemented in this package not only allows for high-dimensional data, but also has the "double robustness" property: either the model for the propensity score or the models for the conditional means of the potential outcomes are allowed to be misspecified (but not both). This package is based on the paper by Fan et al., ``Estimation of Conditional Average Treatment Effects With High-Dimensional Data" (2022), Journal of Business & Economic Statistics <doi:10.1080 07350015.2020.1811102="">.</doi:10.1080>
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Description

Use a two-step procedure to estimate the conditional average treatment effects (CATE) with potentially high-dimensional covariate(s).

Usage

```
HDCATE(data, y_name, d_name, x_formula)
```

Arguments

data data frame of the observed data y_n name variable name of the observed outcomes d_n name variable name of the treatment indicators x_f ormula formula of the covariates

Value

An initialized HDCATE model (object), ready for estimation.

```
# get simulation data
n_obs <- 500 # Num of observations
n_var <- 100 # Num of observed variables
n_rel_var <- 4 # Num of relevant variables</pre>
data <- HDCATE.get_sim_data(n_obs, n_var, n_rel_var)</pre>
# conditional expectation model is misspecified
x_{\text{formula}} \leftarrow \text{paste}(\text{paste}('X', c(2:n_{\text{var}})), collapse ='+')
# for example, and alternatively, the propensity score model is misspecified
# x_formula <- paste(paste0('X', c(1:(n_var-1))), collapse ='+')</pre>
# Example 1: full-sample estimator
# create a new HDCATE model
model <- HDCATE(data=data, y_name='Y', d_name='D', x_formula=x_formula)</pre>
# estimate HDCATE function, inference, and plot
HDCATE.set_condition_var(model, 'X2', min=-1, max=1, step=0.01)
HDCATE.fit(model)
HDCATE.inference(model)
HDCATE.plot(model)
```

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```
# Example 2: cross-fitting estimator
# change above estimator to cross-fitting mode, 5 folds, for example.
HDCATE.use_cross_fitting(model, k_fold=5)

# estimate HDCATE function, inference, and plot
HDCATE.set_condition_var(model, 'X2', min=-1, max=1, step=0.01)
HDCATE.fit(model)
HDCATE.inference(model)
HDCATE.plot(model)
```

HDCATE.fit

Fit the HDCATE function

Description

Fit the HDCATE function

Usage

```
HDCATE.fit(HDCATE_model)
```

Arguments

HDCATE_model an object created via HDCATE

Value

None. The HDCATE_model is fitted.

```
# get simulation data
n_obs <- 500  # Num of observations
n_var <- 100  # Num of observed variables
n_rel_var <- 4  # Num of relevant variables
data <- HDCATE.get_sim_data(n_obs, n_var, n_rel_var)
# conditional expectation model is misspecified
x_formula <- paste(paste0('X', c(2:n_var)), collapse ='+')
# propensity score model is misspecified
# x_formula <- paste(paste0('X', c(1:(n_var-1))), collapse ='+')
# create a new HDCATE model
model <- HDCATE(data=data, y_name='Y', d_name='D', x_formula=x_formula)
HDCATE.set_condition_var(model, 'X2', min=-1, max=1, step=0.01)
HDCATE.fit(model)</pre>
```

HDCATE.get_sim_data Get simulation data

Description

Get simulation data

Usage

```
HDCATE.get_sim_data(
    n_obs = 500,
    n_var = 100,
    n_rel_var = 4,
    sig_strength_propensity = 0.5,
    sig_strength_outcome = 1,
    intercept = 10
)
```

Arguments

n_obs Num of observations

n_var Num of covariates

n_rel_var Num of relevant variables, only the first n_rel_var covariates are actually present in the expectation function of potential outcome, and only the last n_rel_var covariates are present in the propensity score function.

sig_strength_propensity signal strength in propensity score functions

sig_strength_outcome signal strength in outcome functions

intercept value of intercept in outcome functions

Value

a data.frame, which is the simulated observed data.

```
HDCATE.get_sim_data()
HDCATE.get_sim_data(n_obs=50, n_var=4, n_rel_var=2)
```

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HDCATE.inference

Construct uniform confidence bands

Description

Construct uniform confidence bands

Usage

```
HDCATE.inference(HDCATE_model, sig_level = 0.01, n_rep_boot = 1000)
```

Arguments

```
HDCATE_model an object created via HDCATE

sig_level a (vector of) significant level, such as 0.01, or c(0.01, 0.05, 0.10)

n_rep_boot repeat n times for bootstrap, the default is 1000.
```

Value

None. The HDCATE confidence bands are constructed.

Examples

```
# get simulation data
n_obs <- 500  # Num of observations
n_var <- 100  # Num of observed variables
n_rel_var <- 4  # Num of relevant variables
data <- HDCATE.get_sim_data(n_obs, n_var, n_rel_var)
# conditional expectation model is misspecified
x_formula <- paste(paste0('X', c(2:n_var)), collapse ='+')
# propensity score model is misspecified
# x_formula <- paste(paste0('X', c(1:(n_var-1))), collapse ='+')
# create a new HDCATE model
model <- HDCATE(data=data, y_name='Y', d_name='D', x_formula=x_formula)
HDCATE.set_condition_var(model, 'X2', min=-1, max=1, step=0.01)
HDCATE.fit(model)
HDCATE.inference(model)</pre>
```

HDCATE.plot

Plot HDCATE function and the uniform confidence bands

Description

Plot HDCATE function and the uniform confidence bands

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Usage

```
HDCATE.plot(
  HDCATE_model,
  output_pdf = FALSE,
  pdf_name = "hdcate_plot.pdf",
  include_band = TRUE,
  test_side = "both",
  y_axis_min = "auto",
  y_axis_max = "auto",
  display.hdcate = "HDCATEF",
  display.ate = "ATE",
  display.siglevel = "sig_level"
)
```

Arguments

HDCATE_model an object created via HDCATE output_pdf if TRUE, the plot will be saved as a PDF file, the default is FALSE pdf_name file name when output_pdf=TRUE include_band if TRUE, plot the uniform confidence bands (need: HDCATE.inference was called before) test_side 'both', 'left' or 'right', i.e. 2-side test or one-side test minimum value of the Y axis to plot in the graph, the default is auto y_axis_min maximum value of the Y axis to plot in the graph, the default is auto y_axis_max display.hdcate the name of HDCATE function in the legend, the default is 'HDCATEF' display.ate the name of average treatment effect in the legend, the default is 'ATE' display.siglevel the name of the significant level for confidence bands in the legend, the default is 'sig_level'

Value

None. A plot will be shown or saved as PDF.

```
# get simulation data
n_obs <- 500  # Num of observations
n_var <- 100  # Num of observed variables
n_rel_var <- 4  # Num of relevant variables
data <- HDCATE.get_sim_data(n_obs, n_var, n_rel_var)
# conditional expectation model is misspecified
x_formula <- paste(paste0('X', c(2:n_var)), collapse ='+')
# propensity score model is misspecified
# x_formula <- paste(paste0('X', c(1:(n_var-1))), collapse ='+')
# create a new HDCATE model
model <- HDCATE(data=data, y_name='Y', d_name='D', x_formula=x_formula)
HDCATE.set_condition_var(model, 'X2', min=-1, max=1, step=0.01)
HDCATE.fit(model)</pre>
```

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```
HDCATE.inference(model)
HDCATE.plot(model)
```

HDCATE.set_bw

Set bandwidth

Description

Set user-defined bandwidth.

Usage

```
HDCATE.set_bw(model, bandwidth = "default")
```

Arguments

model an object created via HDCATE

bandwidth the value of bandwidth

Value

None.

```
# get simulation data
n_obs <- 500  # Num of observations
n_var <- 100  # Num of observed variables
n_rel_var <- 4  # Num of relevant variables
data <- HDCATE.get_sim_data(n_obs, n_var, n_rel_var)
# conditional expectation model is misspecified
x_formula <- paste(paste0('X', c(2:n_var)), collapse ='+')
# propensity score model is misspecified
# x_formula <- paste(paste0('X', c(1:(n_var-1))), collapse ='+')
# create a new HDCATE model
model <- HDCATE(data=data, y_name='Y', d_name='D', x_formula=x_formula)
# Set user-defined bandwidth, e.g., 0.15.
HDCATE.set_bw(model, 0.15)</pre>
```

```
HDCATE.set_condition_var
```

Set the conditional variable in CATE

Description

Set the conditional variable in CATE

Usage

```
HDCATE.set_condition_var(
  HDCATE_model,
  name = NA,
  min = NA,
  max = NA,
  step = NA
)
```

Arguments

HDCATE_model an object created via HDCATE

name name of the conditional variable

min minimum value of the conditional variable for evaluation

max maximum value of the conditional variable for evaluation

step minimum distance between two evaluation points

Value

None. The HDCATE_model is ready to fit.

```
# get simulation data
n_obs <- 500  # Num of observations
n_var <- 100  # Num of observed variables
n_rel_var <- 4  # Num of relevant variables
data <- HDCATE.get_sim_data(n_obs, n_var, n_rel_var)
# conditional expectation model is misspecified
x_formula <- paste(paste0('X', c(2:n_var)), collapse ='+')
# propensity score model is misspecified
# x_formula <- paste(paste0('X', c(1:(n_var-1))), collapse ='+')
# create a new HDCATE model
model <- HDCATE(data=data, y_name='Y', d_name='D', x_formula=x_formula)
HDCATE.set_condition_var(model, 'X2', min=-1, max=1, step=0.01)</pre>
```

```
HDCATE.set_first_stage
```

Set user-defined first-stage estimating methods

Description

Set user-defined ML methods (such as random forests, elastic-net, boosting) to run the first-stage estimation.

Usage

```
HDCATE.set_first_stage(
  model,
  fit.treated,
  fit.untreated,
  fit.propensity,
  predict.treated,
  predict.untreated,
  predict.propensity
)
```

Arguments

model an object created via HDCATE

fit.treated function that accepts a data.frame as the only argument, fits the treated expectation function, and returns a fitted object

fit.untreated function that accepts a data.frame as the only argument, fits the untreated expectation function, and returns a fitted object

fit.propensity function that accepts a data.frame as the only argument, fits the propensity function, and return a fitted object

predict.treated function that accepts the returned object of fit.treated and a data.frame as arguments, and returns the predicted vector of that data.frame

predict.untreated function that accepts the returned object of fit.untreated and a data.frame as

function that accepts the returned object of fit.untreated and a data.frame arguments, and returns the predicted vector that data.frame

predict.propensity

function that accepts the returned object of fit.propensity and a data.frame as arguments, and returns the predicted vector that data.frame

Value

None.

```
# get simulation data
n_obs <- 500 # Num of observations
n_var <- 100 # Num of observed variables
n_rel_var <- 4 # Num of relevant variables</pre>
```

```
data <- HDCATE.get_sim_data(n_obs, n_var, n_rel_var)</pre>
# conditional expectation model is misspecified
x_formula <- paste(paste0('X', c(2:n_var)), collapse ='+')</pre>
# propensity score model is misspecified
# x_formula <- paste(paste0('X', c(1:(n_var-1))), collapse ='+')</pre>
# create a new HDCATE model
model <- HDCATE(data=data, y_name='Y', d_name='D', x_formula=x_formula)</pre>
# manually define a lasso method
my_lasso_fit_exp <- function(df) {</pre>
  hdm::rlasso(as.formula(paste0('Y', "~", x_formula)), df)
my_lasso_predict_exp <- function(fitted_model, df) {</pre>
  predict(fitted_model, df)
}
my_lasso_fit_ps <- function(df) {</pre>
 hdm::rlassologit(as.formula(paste0('D', "~", x_formula)), df)
}
my_lasso_predict_ps <- function(fitted_model, df) {</pre>
 predict(fitted_model, df, type="response")
# Apply the "my-lasso" apporach to the first stage
HDCATE.set_first_stage(
  model,
  my_lasso_fit_exp,
  my_lasso_fit_exp,
 my_lasso_fit_ps,
 my_lasso_predict_exp,
 my_lasso_predict_exp,
  my_lasso_predict_ps
```

HDCATE.unset_first_stage

Clear the user-defined first-stage estimating methods

Description

Inverse operation of HDCATE.set_first_stage

Usage

```
HDCATE.unset_first_stage(model)
```

Arguments

model

an object created via HDCATE

Value

None.

Examples

```
# get simulation data
n_obs <- 500  # Num of observations
n_var <- 100  # Num of observed variables
n_rel_var <- 4  # Num of relevant variables
data <- HDCATE.get_sim_data(n_obs, n_var, n_rel_var)
# conditional expectation model is misspecified
x_formula <- paste(paste0('X', c(2:n_var)), collapse ='+')
# propensity score model is misspecified
# x_formula <- paste(paste0('X', c(1:(n_var-1))), collapse ='+')
# create a new HDCATE model
model <- HDCATE(data=data, y_name='Y', d_name='D', x_formula=x_formula)
# ... manually set user-defined first-stage estimating methods via `HDCATE.set_first_stage`
# Clear those user-defined methods and use the built-in method
HDCATE.unset_first_stage(model)</pre>
```

HDCATE.use_cross_fitting

Use k-fold cross-fitting estimator

Description

Use k-fold cross-fitting estimator

Usage

```
HDCATE.use_cross_fitting(model, k_fold = 5, folds = NULL)
```

Arguments

model an object created via HDCATE

k_fold number of folds

folds you can manually set the folds, should be a list of index vector

Value

None.

```
# get simulation data
n_obs <- 500  # Num of observations
n_var <- 100  # Num of observed variables
n_rel_var <- 4  # Num of relevant variables
data <- HDCATE.get_sim_data(n_obs, n_var, n_rel_var)
# conditional expectation model is misspecified
x_formula <- paste(paste0('X', c(2:n_var)), collapse ='+')
# propensity score model is misspecified
# x_formula <- paste(paste0('X', c(1:(n_var-1))), collapse ='+')</pre>
```

```
# create a new HDCATE model
model <- HDCATE(data=data, y_name='Y', d_name='D', x_formula=x_formula)

# for example, use 5-fold cross-fitting estimator
HDCATE.use_cross_fitting(model, k_fold=5)

# alternatively, pass a list of index vector to the third argument to set the folds manually, in this case, the second argument k_fold is auto detected, you can pass any value to it.
HDCATE.use_cross_fitting(model, k_fold=2, folds=list(c(1:250), c(251:500)))</pre>
```

```
HDCATE.use_full_sample
```

Use full-sample estimator

Description

This is the default mode when creating a model via HDCATE

Usage

```
HDCATE.use_full_sample(model)
```

Arguments

model

an object created via HDCATE

Value

None.

```
# get simulation data
n_obs <- 500  # Num of observations
n_var <- 100  # Num of observed variables
n_rel_var <- 4  # Num of relevant variables
data <- HDCATE.get_sim_data(n_obs, n_var, n_rel_var)
# conditional expectation model is misspecified
x_formula <- paste(paste0('X', c(2:n_var)), collapse ='+')
# propensity score model is misspecified
# x_formula <- paste(paste0('X', c(1:(n_var-1))), collapse ='+')
# create a new HDCATE model
model <- HDCATE(data=data, y_name='Y', d_name='D', x_formula=x_formula)
HDCATE.use_full_sample(model)</pre>
```

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