

# Receiver Operator Characteristics (ROC)

and Area Under the Curve (AUC)

# Why?

- The Receiver Operator Characteristics let's us evaluate classifiers on biased datasets.
- Example: Cancer prediction. A classifier that always predicts 'no cancer' has 99.9% accuracy because only a small percentage of the population has cancer.

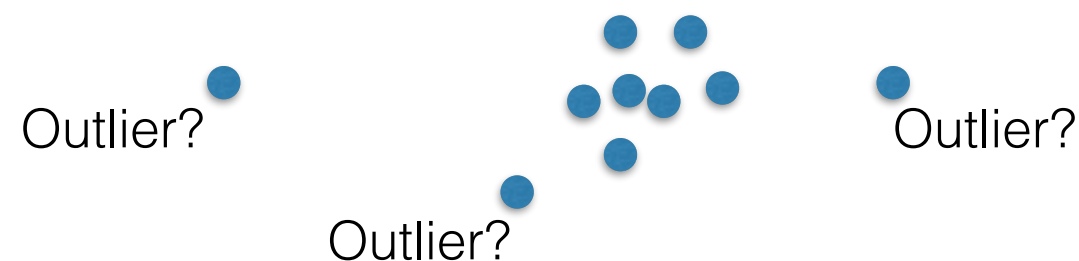
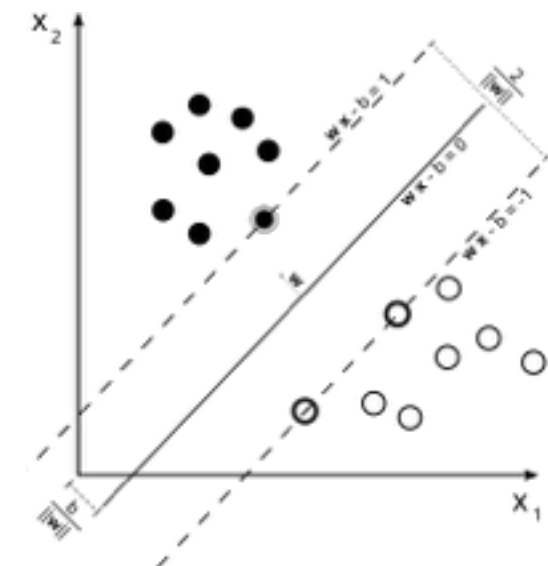
# Binary Classification Confusion Matrix

		Classifier Output		
		Predicted condition		
Label	Total population	Predicted Condition positive	Predicted Condition negative	Prevalence $= \frac{\Sigma \text{Condition positive}}{\Sigma \text{Total population}}$
	condition positive	True positive	False Negative (Type II error)	True positive rate (TPR), Sensitivity, Recall $= \frac{\Sigma \text{True positive}}{\Sigma \text{Condition positive}}$
	True condition condition negative	False Positive (Type I error)	True negative	False positive rate (FPR), Fall-out $= \frac{\Sigma \text{False positive}}{\Sigma \text{Condition negative}}$

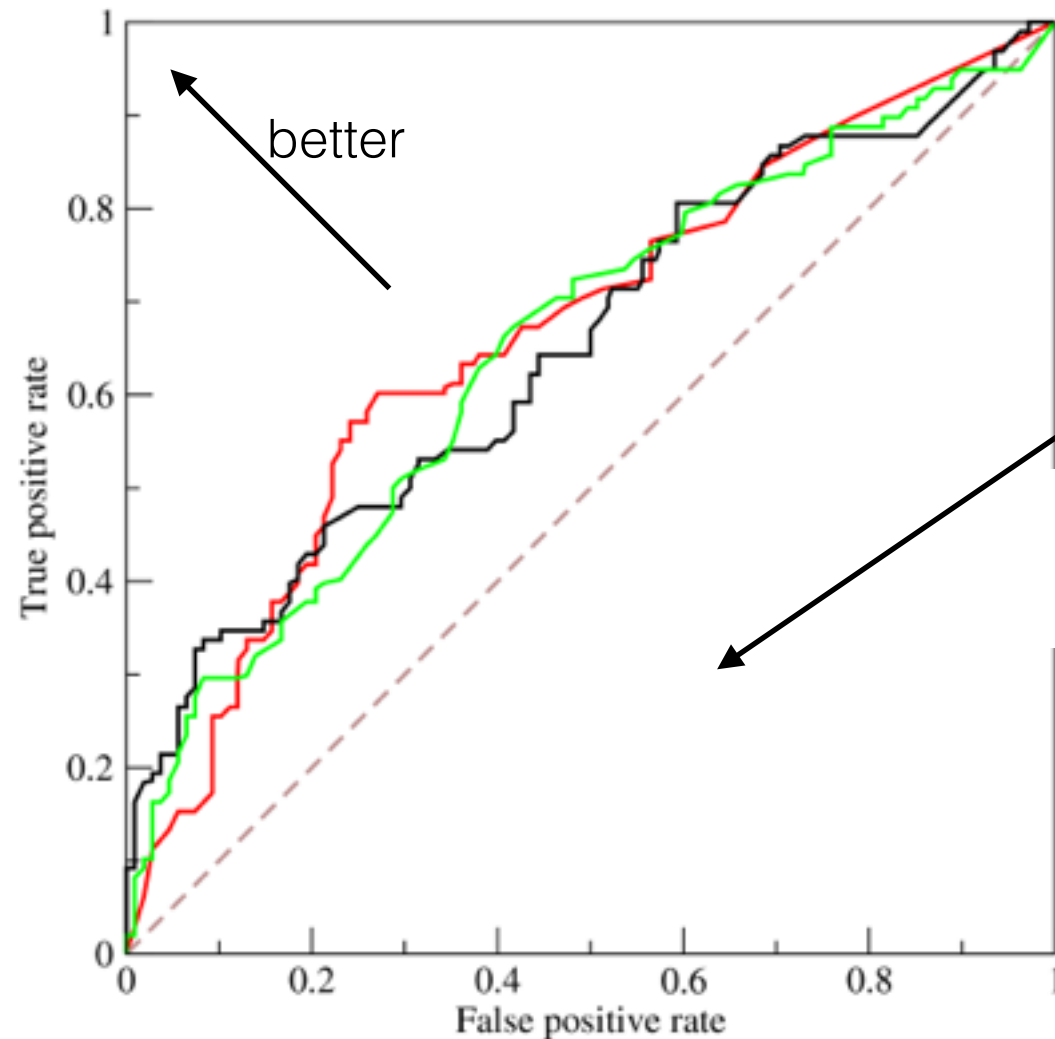
In binary classification we have some sort of bias parameter

- SVM: Bias parameter that moves our hyperplane orthogonal to it
- Outlier detection: From which distance on should we call a point outlier?

Different bias parameters give different FPR/TPR pairs! We plot these in the Receiver Operator Characteristics (ROC).



# Example ROC (Curve)



## Area Under the Curve (AUC)

Different ways to measure:  
We use trapezoidal rule, i.e. the area that we get from combining (0,0), all (FPR, TPR) points, (1,1), to (0, 0).

This is initially a scatter plot (FPR/TPR points). The points were then linked to create a nicer figure.