Scheduling Mixed-Parallel Applications with Advance Reservations

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ABSTRACT

This paper investigates the scheduling of mixed-parallel applications, which exhibit both task and data parallelism, in advance reservations settings. Both the problem of minimizing application turn-around time and that of meeting a deadline are studied. For each several scheduling algorithms are proposed, some of which borrow ideas from previously published work in non-reservation settings. Algorithms are compared in simulation over a wide range of application and reservation scenarios. The main finding is that schedules computed using the previously published CPA algorithm can be adapted to advance reservation settings, notably resulting in low resource consumption and thus high efficiency.

Categories and Subject Descriptors

D.4 [Operating Systems]: Process Management—Scheduling; C.4 [Performance of Systems]: Modeling Techniques

General Terms

Algorithms, Performance

Keywords

Scheduling, Advance Reservation, Mixed Parallelism

1. INTRODUCTION

An effective way to extract the most performance and scalability out of a parallel application is to exploit both task parallelism and data parallelism. With this approach, which is typically termed *mixed parallelism* [22, 19, 39], an application consists of tasks organized in a Directed Acyclic Graph (DAG) in which each edge corresponds to a precedence relation between two tasks, implying

possible data communication. Mixed-parallel applications arise for instance in image processing applications that consist of a worklow of image filters, where some of these filters can be themselves implemented as data-parallel applications [23]. See [13] for a description of the benefits of mixed parallelism and for other examples of mixed-parallel application. Each task is itself a data-parallel task that exhibits loop parallelism, meaning that iterations can be executed, at least conceptually, in a Single Instruction Multiple Data (SIMD) fashion on various numbers of processors. (Mixed-parallel applications are also referred to as "malleable tasks with precedence constraints" in the literature.) Prime candidates for mixedparallel implementations are scientific workflows, as seen in existing workflow systems that support mixed parallelism [45, 27, 25]. In this work we focus on the problem of mixed-parallel application scheduling, and like most previous works in this area we restrict our study to applications that are fully specified at the onset of their execution (e.g., static non-data-dependent workflows).

Typical platforms for executing mixed-parallel applications range from single homogeneous commodity clusters to heterogeneous multi-site grid platforms. A key question for the use of these platforms, regardless of the application at hand, is: How do applications get access to compute resources? Batch schedulers are the most common resource management systems used in production today [5, 1, 2, 3, 4]. Batch schedulers accept requests for compute resources, place these requests in queues, and grant access to resources based on various policies [18]. The main advantage of batch schedulers is that they can be configured to maximize resource utilization. The main drawback is that there is often a disconnect between the desires of application users (low turn-around time, fairness) and the schedules computed by batch schedulers [42, 28]. In particular, it is often difficult for a user to estimate when a job may complete, sometimes motivating creative strategies to mitigate this uncertainty [35, 10]. In many production scenarios such use of batch schedulers is inappropriate, for instance when applications must execute within deadlines. Instead, users need guaranteed access to resources within fixed time-frames. Consequently, most modern batch schedulers provide advance reservation capabilities [1, 4, 9] or can support reservations thanks to plug-in modules [3, 33]; and several production platforms have enabled the use of reservations for years [18].

In this paper we consider the problem of scheduling mixed parallel applications with advance reservations, that is on a platform that supports advance reservations and that is subject to advance reservations from competing applications/users. We consider two scheduling problems: minimizing turnaround time and meeting a deadline. We restrict our study to the case of a single homogeneous computing platform such as a cluster, and leave the study of heterogeneous and/or multi-cluster platforms for future work. To the best

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of our knowledge, no previous work has studied the scheduling of mixed-parallel applications with advance reservations.

This paper is organized as follows. Section 2 discusses related work. Section 3 describes our application, platform, and resource management models, and gives formal problem definitions. Section 4 and Section 5 present algorithms and experimental results for both our scheduling problems. Section 6 summarizes our contributions and outlines future directions.

2. RELATED WORK

Our work is related to ones in two distinct areas: (i) scheduling of mixed-parallel applications on dedicated systems; (ii) scheduling of task-parallel applications, and in particular task-parallel workflows, with advance reservations. We review work in both these areas below, focusing solely on works that target homogeneous platforms.

2.1 Mixed-parallel Scheduling

On the theoretical side of mixed-parallel application scheduling the main contribution is the guaranteed algorithm in [29], which was later improved in [26]. Many non-guaranteed algorithms that generate good schedules in practice have been proposed [7, 37, 40, 41]. All these algorithms use two phases: a first phase in which the algorithm decides how many processors should be allocated to each task; and a second phase in which tasks are scheduled in time and space. Most notable is the CPA (Critical Path and Area-based scheduling) algorithm [37], which has low computational complexity and was shown to lead to good results when compared to its competitors. One drawback of CPA is that, for some application and platform characteristics, it may result in allocations that are too large and hinder task parallelism. The MCPA algorithm addresses this drawback in the case of layered task graphs [7]. In the general case, this drawback was also addressed in [34] via a more stringent stopping criterion for CPA's first phase, thus better limiting task allocations.

In addition to the above two-step algorithms, one-step algorithms have also been proposed [8, 46]. In particular, the iCASLB algorithm was shown to lead to better performance than some two-step algorithms, including CPA, while maintaining reasonable complexity [46]. This algorithm performs allocation and mapping simultaneously by iteratively increasing the allocations of tasks on the critical path, with a look-ahead mechanism to avoid being trapped in local minima and a backfilling approach to improve the schedule.

In this work we reuse some of the ideas of the CPA algorithm to schedule mixed-parallel applications in the presence of advance reservations.

2.2 Scheduling with Reservation

One can classify works that have studied scheduling in advance reservation scenarios in two cases, depending on whether they target independent jobs or a single job that consists of dependent subjobs. In the first case, the goal is to find for each job a reservation that allows that job to meet a particular deadline [17, 24, 12, 11]. In the second case, reservations for sub-jobs must be made in a coordinated manner to ensure that the last sub-job meets a global application deadline [31, 47, 15]. Our work falls in this second case, but considers sub-jobs that are themselves data-parallel applications, which to the best of our knowledge has not been studied before.

3. MODELS AND PROBLEM STATEMENT

We use simulation to evaluate our algorithms because it allows for repeatable results (in real system the workload is dynamic), because it is cheap (we do not need to burn enormous amounts of allocated CPU hours on real-world parallel platforms), and because it is fast (we can explore a wide range of scenarios and run statistically significant numbers of experiments).

3.1 Application and Platform Model

We model an application as a Directed Acyclic Graph (DAG) in which each vertex represents a data-parallel task, and each edge represents a precedence relation between tasks. We consider the execution of such an application on a homogeneous distributed-memory parallel computing platform, e.g., a homogeneous cluster, that comprises *p* processors. We use the term "processor" to refer to an individually schedulable unit: a user can ask the batch scheduler for a given number of processors starting at some fixed date and for a given duration. With this terminology, a "processor" may in fact be a physical compute node that is a multi-processor and/or multi-core computer.

More formally, we model an application as a DAG (V, E), where V is a set of vertices, or tasks, T_i , i = 1, ..., n, and E is a set of directed edges. If there is an edge from task T_i to task T_j , then task T_j cannot begin executing until task T_i has completed. We call task T_i a successor of task T_i , which is a predecessor of task T_i . Without loss of generality, we assume that the DAG has a single entry task and a single exit task. In addition to the number of tasks, we use 4 parameters used in previous work to define the shape of the DAG: width, regularity, density, and jumps [34]. The width determines the maximum parallelism in the DAG, that is the number of tasks in the largest level. A small value leads to "chain" graphs and a large value leads to "fork-join" graphs. The regularity denotes the uniformity of the number of tasks in each level. A low value means that levels contain very dissimilar numbers of tasks, while a high value means that all levels contain similar numbers of tasks. The density denotes the number of edges between two levels of the DAG, with a low value leading to few edges and a large value leading to many edges. These three parameters take values between 0 and 1. Finally, we add random "jumps edges" that go from level lto level l + jump, for jump = 1, 2, 3, 4. The case jump = 1 corresponds to no jumping over any level, resulting in a so-called layered DAG [7]. We refer the reader to the DAG generation program and its documentation for more details [14].

While the above generates the DAG's structure, we still have to model the execution time of tasks. We assume that each task T_i is a data-parallel task that can be executed on any number of processors between 1 and p. Like most previous works we model task execution time based on Amdahl's law: a fraction α_i of the task execution is not parallelizable. Each task execution time is then fully specified simply by its sequential execution time, t_i , and by α_i . In our simulations we pick values for α_i randomly selected between 0 and a value α using a uniform probability distribution. We pick t_i randomly between 1 minute and 10 hours. The parameters of our application models and the ranges of values we use in our experiments are shown in Table 1, which also indicates default values whenever we fix a parameter.

We do not model any communication network or any data transfer between application tasks, with the following rationale. Due to the presence of advanced reservations different sets of processors are unavailable at different times. It would be egregiously inefficient to schedule the application across a continuous period of time, i.e., with a single reservation during which all application tasks can execute. Indeed, such a reservation would have a late start time due to other reservations, or would be limited to using only a few processors. We conclude that it is better to schedule the application using multiple reservations and we simply use one reservation

Table 1: Application model parameter values or value ranges. Default values when keeping a parameter fixed are shown in boldface.

Parameter	Values
Number of tasks	10, 25, 50 , 75, 100
α	.05, .10, .15, .20
width	.1, .2, .3, .4, .5 , .6, .7, .8, .9
density	.1, .2, .3, .4, .5 , .6, .7, .8, .9
regularity	.1, .2, .3, .4, .5 , .6, .7, .8, .9
jump	1, 2, 3, 4

per application task. In this multiple reservation scenario, a task could complete well ahead of the start time of one of its successors, thus precluding the use of network communication between the two tasks. One then must use disk I/O and implement task communication via files. The associated overhead is comprised in our model of task execution times.

Finally, note that the above model assumes that we have perfect knowledge of the data-parallel task execution times for various numbers of processors. This is a common assumption in the area of mixed-parallel application scheduling: this knowledge can be gathered via benchmarking or via precise performance models. If, however, only imprecise knowledge is available then reservations would be made using pessimistic estimates of task execution times (which most users typically employ for batch job submissions [32]). More pessimistic estimates lead to task reservations later in the future (due to fewer opportunities to fill small "holes" early in the reservation schedule) and thus to longer application execution time. We leave a study of the impact of pessimistic estimates for future work but do not anticipate that the results in this paper would be changed (all algorithms should be impacted similarly).

3.2 Advance Reservation Model

We need to model (i) the existing reservations in the system at the time of application scheduling; and (ii) the way in which one interacts with the reservation system to schedule the application.

3.2.1 Modeling Reservation Schedules

Advanced reservation is a key feature of batch schedulers in production today and is expected to be used increasingly frequently by users. Unfortunately, little information is publicly available regarding actual *reservation schedules*, i.e., the list of ongoing and future resource reservations at a given time, where each reservation is defined as a start time, a finish time, and a number of processors. Ideally, one would obtain and analyze logs of batch schedulers running for long periods of time with detailed information both about jobs submitted to batch queues and about jobs that used advance reservations. While such logs are available for batch jobs, to the best of our knowledge there are only few public sources of logs that provide information on advance reservation jobs [6]. Therefore, very few works use real-world advance reservation logs (we are only aware of [30]), and reservation schedule modeling is an open issue.

In the face of this lack of data, the approach used in previous work is to modify available logs of batch jobs by randomly tagging some fraction of the jobs as "reserved" and removing all other jobs, thus resulting in a reservation schedule [43, 44]. We use this approach with four logs from the Parallel Workloads Archive [36] for four parallel platforms (see Table 2). For each log we select a fraction ϕ of the jobs from the log using a uniform probability dis-

tribution. In our experiments we use $\phi = 10$, 20, or 50 to study more or less sparse reservation schedules. We then pick a random time in the log, T, at which our application scheduling decisions take place. One problem with this method is that the resulting reservation schedule is stationary: the average number of reservations per time unit is approximately constant throughout time. Instead, one would expect that, starting at time T, the number of reservations decreases with time. Accordingly, we modify the reservation schedule using one of the three following methods:

- linear We add and remove reservations in the reservation schedule at time T so that the average number of reservation jobs per day decreases approximately linearly throughout time (and so that no reservations are present after time T+7 days).
- expo Same as above, but leading to an approximately exponential decrease.
- *real* We remove reservations in the reservation schedule at time *T* for jobs submitted to the batch queue after time *T*.

By using these three methods we not only increase the chance that at least one of the methods is more representative of the real world than those used in previous work, but more importantly we can quantify the sensitivity of our results to changes in the reservation schedule patterns.

In a preliminary attempt at validating the above approach we have obtained reservation logs for the Grid'5000 platform [21, 6]. These logs span a period of 2.5 years. We compute two simple metrics for the Grid'5000 log and our four supercomputer logs: (i) job execution times and (ii) times between job/reservation submission and job/reservation start time. For each log we compute averages and coefficient of variations for these metrics. The goal is to find whether these metrics have significantly different values for the Grid'5000 log. Results are shown in Table 3. We see that coefficients of variation are low, under 4%, and that average metric values for Grid'5000 are comparable to those for the four other logs. We also compute correlations between reservation schedules (i.e., number of reserved processors throughout time starting at random points in the log) from the Grid'5000 log and for synthetic reservation schedules generated from our 4 other logs using the linear, expo, and real methods described above for three values of φ. On average, the linear, expo and real methods lead to correlation coefficients of 0.27, 0.54, and 0.44, respectively. This seems to indicate that the expo method leads to reservation schedules that are the most correlated to those of the real-world Grid'5000 reservation schedule. However, we found that the real method leads to better correlations than the expo methods when used for some of our supercomputer logs.

A fully validated reservation schedule model is outside the scope of this paper (and would require more than one real-world data set!). We believe that our method for generating synthetic reservation schedules is reasonable, at least for our purpose. And indeed, as we will see later in the paper, we do not find significant discrepancies between simulation results obtained using our (plentiful) synthetic data or our (scarce) real-world data.

3.2.2 Modeling the Reservation Process

To model the interaction between the application scheduler and the batch scheduler we make two simplifying assumptions. First, we assume that application scheduling and submission of reservation requests are instantaneous. Therefore, the reservation schedule does not change while the application is being scheduled. Second, we assume that the application scheduler has full knowledge of the

Table 2: Four batch job logs used for simulation experiments.

Name	Institution	Year	Duration	Architecture	#CPUs	Avg. Utilization	
CTC_SP2	CTC	Jun/1996-May/1997	11 [mon]	IBM SP2	430	65.8 [%]	
OSC_Cluster	OSC	Jan/2000-Nov/2001	22	linux cluster	57	38.5	
SDSC_BLUE	SDSC	Apr/2000-Jan/2003	32	IBM SP	1152	75.7	
SDSC_DS*	SDSC	Mar/2004-Apr/2005	13	IBM eServer p690	224	27.3	

^{*} only for jobs submitted to partition 3.

Table 3: Statistics for the Grid'5000 reservation log and four non-reservation batch logs.

Log	Avg. job exec. time	CV job exec. time	Avg. time to exec.	CV time to exec.
Grid'5000	1.84 [hour]	3.54 [%]	3.24 [hour]	2.52 [%]
CTC_SP2	3.20	1.41	7.49	0.61
OSC_Cluster	9.33	2.84	3.02	1.63
SDSC_BLUE	1.18	0.77	8.90	0.69
SDSC_DS*	1.52	2.75	4.41	2.48

reservation schedule. Some schedulers do expose this information as part of their interface (e.g., PBSpro [4], Maui [3], Plus [33]), but system administrators may not be willing to enable this feature. In this case, the application schedule would have to be determined via (a bounded number of) trial-and-error reservation requests for each application task.

3.3 Scheduling Problems

We consider two different scheduling problems, instantiated for a mixed-parallel application on a homogeneous cluster with p processors and with a given reservation schedule at application scheduling time:

- RESSCHED: compute a schedule that minimizes application turn-around-time, i.e., the time between schedule computation and application completion.
- RESSCHEDDL: determine whether the application can complete before a given deadline K (and produce the schedule if possible).

In the next two sections we discuss the complexity of both problems, propose algorithms to solve them, and evaluate these algorithms in simulation.

4. MINIMIZING TURN-AROUND TIME

4.1 Computational Complexity

In [16] the authors study the problem of application turn-around time minimization for independent sequential tasks in the presence of future reservations, which they term RESASCHEDULING. This problem is a simpler special case of problem RESSCHED due to the fact that tasks are independent and sequential. The authors prove that RESASCHEDULING is strongly NP-hard via reduction to 3-PARTITION [20]. Furthermore, they prove that the problem is inapproximable in the general case. We conclude that RESSCHED is NP-hard, and inapproximable. They describe guaranteed algorithms for two special cases. The first special case requires that the number of reserved processors be monotonically decreasing with time, which does not hold in practice. The second special case requires that a subset of the processors be un-reservable, which may be desirable in practice. However, is is not known whether the performance guarantee holds when there are dependencies among tasks and when tasks are data-parallel. Furthermore, mixed-parallel

application scheduling with no reservations is also NP-hard. Guaranteed algorithms are available [29, 26] but here it is not known whether these guarantees hold in the presence of reservations.

It is very likely that the aforementioned performance guarantee do not hold in our case. We leave the development of (most likely elusive) new guaranteed algorithms for solving RESSCHED outside the scope of this paper. Instead, we resort to developing non-guaranteed heuristics.

4.2 Algorithms

Perhaps the most natural approach for scheduling a task-parallel DAG with advance reservations is to adapt popular list-scheduling heuristics so that they account for existing advance reservations [31, 47, 15]. In the case of problem RESSCHED, the added challenge is that the application is mixed-parallel.

A well-known and simple algorithm for scheduling mixed-parallel applications is CPA [38]. This algorithm uses two phases: (i) an allocation phase in which it decides how many processors should be allocated to each task; and (ii) a mapping phase in which tasks are scheduled in decreasing order of their bottom levels, which is a standard list scheduling approach. Recall that the bottom level of a task is the maximum length of the paths from this task to the end task in the DAG, expressed as a sum of task execution times, and easily computed recursively. In its first phase, CPA starts by allocating one processor to each task. Then, CPA iteratively increases the allocation of one task by one processor. This task is chosen at each step as the task on the critical path whose execution time would be reduced the most (relatively) when given an extra processor. The algorithm uses a stopping criterion for the allocation phase, trying to achieve the best compromise between the length of the critical path and the average processor utilization. This criterion was later modified in [34], where it is shown empirically that the modified criterion leads to better schedule (lower makespan, higher efficiency). When we refer to CPA hereafter we mean this improved version of the algorithm.

A natural approach would then be to adapt the CPA algorithm to an advance reservation scenario. A major difficulty here is that task allocations are computed disregarding the reservation schedule, meaning that task start times could be delayed significantly. Instead, we propose an algorithm that proceeds in the following two simple phases:

- Compute a bottom level value for each task and sort the tasks in decreasing order of their bottom levels;
- 2. For each task, in order, determine the best feasible task al-

location, i.e., a number of processors and a start time, that allows the task to achieve the earliest completion time, accounting for competing reservations.

The above, albeit simple, makes it possible to increase or reduce task allocations while considering the time at which the task would execute, and thus also considering existing advance reservations at that time. Two questions arise:

- 1. How should bottom levels be computed?
- 2. Should task allocations be bounded?

Let us discuss these two questions and propose several approaches, whose combinations result in a number of candidate algorithms for solving RESSCHED.

Computing task bottom levels requires that all task execution times be known. The execution time of a task must be computed for a given number of processors. We consider four options:

- BL_1 task execution times are computed assuming that each task is allocated a single processors.
- BL_ALL Task execution times are computed assuming that each task is allocated p processors.
- BL_CPA Task execution times are computed using the task allocations computed by the first phase of the CPA algorithm when considering that up to p processors, i.e., all processors, can be used.
- 4. BL_CPAR Task execution times are computed using the task allocations computed by the first phase of the CPA algorithm when considering that up to q ≤ p processors are available. q is the historical average number of available processors for the platform (computed based on the past reservation schedule and assuming that the number of available processors is stationary).

Our rationale for the last two options above is that, as we will see below, one of our goals is to achieve a schedule that is inspired by the CPA algorithm. Therefore, one may surmise that using CPA-computed allocations to compute the bottom-level may ultimately lead to better schedules (although there is no guarantee). The rationale for the BL_CPAR approach is that the CPA-computed allocations will in the end be bounded by some maximum number of *available* processors. A coarse approximation for this number is the historical average number of available processors.

For phase two, we consider three ways in which task allocations can be bounded:

- 1. **BD_ALL** Task allocations are simply bounded by *p*, meaning that all options are considered for each task when picking the allocation that achieves the earliest completion time.
- 2. **BD_CPA** Task allocations are bounded by the CPA-computed allocations assuming that *p* processors are available.
- 3. **BD_CPAR** Task allocations are bounded by the CPA-computed allocations assuming that *q* processors are available, where *q* is the historical average number of available processors.

One of the insights behind CPA is that it bounds task allocations to foster task parallelism in addition to enabling data parallelism. Therefore, bounding task allocations based on CPA-computed allocations should be beneficial both in terms of application turnaround-time and in terms of parallel efficiency.

The above defines $4\times 3=12$ algorithms for solving the RESS-CHED problem, each named BL_x_BD_y, where $x\in\{1, ALL, CPA, CPAR\}$ and $y\in\{ALL, CPA, CPAR\}$. Note that if the reservation schedule is empty, then the BL_CPA_BD_CPA algorithm is simply the CPA algorithm.

4.3 Experimental Evaluation

4.3.1 Computing Bottom Levels

We first determine which of the techniques for computing task bottom levels is the most effective. We compare the algorithms in simulation, with a simulator that implements the models described in Section 3. We run simulations for applications generated with the parameter values in Table 1 by fixing five of the six parameters to their default values but for one parameter. For each of the resulting 5+4+9+9+9+4=40 applications specifications we generate 20 sample random application instances. We use the job submission logs described in Table 2. For each log we tag $\phi = 10\%$, 20%, or 50% of the jobs as reservations, and we then use the linear, expo, and real methods described in Section 3.2.1, leading to $4 \times 3 \times 3 = 36$ reservation schedule specifications. For each specification we generate 50 random reservation schedule instances as follows. We pick 10 different start times in each trace, i.e., the time at which the application is being scheduled. For each start time we generate 5 sample random taggings of jobs as reservation jobs. Overall, we have $40 \times 36 = 1,440$ experimental scenarios, and for each scenario we have $20 \times 50 = 1,000$ random instances. In all that follows we discuss average results over the 1,000 random instances for each scenario and omit the word "average" for brevity.

For each experimental scenario we schedule the application using all 12 algorithms described in the previous section. For each experimental scenario and for each allocation bounding method, we compute the improvement of the turn-around-time when using the BL_ALL, BL_CPA, and BL_CPAR bottom-level computation method relative to using the BL_1 method.

Over all our experiments the relative turn-around-time improvement over using the BL_1 method is between -3.46% and +5.69%, with negative values denoting that the BL_1 methods leads to better performance. This result quantifies the (obviously moderate) sensitivity of application scheduling to bottom-level computations. Looking at the results in more details, we found that the BL_CPA and the BL_CPAR methods together lead to the best turn-around-time in 78.4% of the cases. The BL_CPAR method is better than the BL_CPA method for more than two thirds of these cases. When it is worse than BL_CPA, its relative performance when compared to the BL_1 method is better than that of BL_CPA by at most 0.3 points. The BL_1 method is best in 13.7% of the cases, and the BL_ALL method in 7.9% of the cases. Finally, we found no particular trends regarding the 6 parameters defined in Table 1, or with the method used to generate reservations (*linear*, *expo*, or *real*).

We conclude that BL_CPAR is the best method (but only marginally better than BL_CPA). It is important to note that this result holds *regardless* of the method used for bounding allocations. We hypothesize that this is because task allocations in the final schedule most resemble those produced by the CPA algorithm when using the number of available processors (rather than, e.g., 1-processor allocations). This intuition is partially confirmed via a more thorough examination of our results. Indeed, we found not only that the BL_1 method leads to the worst results, but also that the gap between the BL_1 method and the other three methods decreases when the total number of processors in the platform decreases or when the number of reservations increases.

The above observations are confirmed in similar experiments

conducted with 50 reservation schedules extracted from the Grid'5000 log at 50 random start times. For the remainder of this paper we exclusively use the BL_CPAR method for computing task bottom

4.3.2 Bounding Allocations

Using the same experimental methodology as in the previous section we schedule our application instances on our platform instances using the three allocation bounding methods: BD_ALL, BD_CPA, BD_CPAR. We also use another method that arbitrarily bounds allocations to half of the total number of processors: BD_HALF. We include this method to evaluate whether sophisticated allocation bounding based on the CPA algorithm is truly necessary or whether a simple bounding technique would be sufficient.

We use two metrics to evaluate the schedule: (i) the application turn-around-time; and (ii) the CPU-hour consumption. While the objective when solving RESSCHED is to minimize application turn-around-time, it is still interesting to observe how efficient the schedule is. Ideally, one would like to find an algorithm that leads to the best turn-around-times with the lowest resource consumption.

Table 4 shows a summary of the results over our 1,440 experimental scenarios for each algorithm in terms of turn-around-time and CPU-hour usage. For each metric we show the average degradation from best. For an experimental scenario, the degradation from best for an algorithm is computed as the average relative difference between the metric for this algorithm and the metric for best-performing algorithm. We then take the average over all scenarios. A value close to 0 means that the algorithm is on average close to the best performing algorithm. For each metric we also show the number of times the algorithm is best across all the scenarios. Note that the total number of "wins" is slightly higher than 1,440 due to ties.

The average degradation from best shows that the BD_CPAR algorithm is the best algorithm both in terms of turn-around-time and in terms of CPU-hour usage. The BD_CPA algorithm is a close runner-up in terms of turn-around-time but uses more CPU-hours. This demonstrates that using the historical average number of available processors to compute CPA allocations leads to some benefit. The BD_ALL algorithm exhibits the worst performance overall. Since it does not bound allocations at all, it harms task parallelism and, in turn, turn-around time. Also, this algorithm wastes compute resources due to the diminishing returns of Amdahl's law and its use of large allocations. The BD_HALF algorithm also leads to poor results, showing that arbitrary bounding of task allocation is likely not a good approach and that application characteristics must be taken into account for the bounding. Interestingly, BD_CPA has more "wins" than DB CPAR but these wins are very slight. By contrast, when BD_CPA loses to BD_CPAR it loses by a larger margin because it uses allocations that are too large relatively to the number of processors that are actually available.

While several of the parameters defining our experimental scenarios do not have any effect on our results we nevertheless observe a few trends:

• When DAG width is low the BD_ALL algorithm leads to the best turn-around-times. In this case the DAG is essentially a chain and the best turn-around-time is achieved when using allocations that are as large as possible. In fact, all 36 wins by BD_ALL in Table 4 are for a DAG width of 0.1 (and in these cases BD_ALL leads to turn-around-times at most 0.5% shorter than those obtained by BD_CPAR). For large DAG widths, the gap between the BD_ALL and BD_HALF algorithms and the BD_CPA and BD_CPAR algorithm in-

- creases, due to these last two algorithms' ability to capitalize on task parallelism.
- As the number of competing reservations in the reservation schedule increases the gap between the BD_ALL algorithm and the other algorithms decreases (but their ranking is preserved). This is easily explained: with fewer available processors the allocations computed by BD_ALL are not as large and thus do not preclude task parallelism as drastically. For the same reason, the gap between the BD_ALL algorithm and the other algorithms decreases for smaller platforms and for more utilized platforms.

Table 5 shows a summary of the results obtained by conducting similar experiments for our 40 application scenarios, but with 50 reservation schedules extracted at 50 random times from the Grid'5000 log. We see that the results are similar to those in Table 4 for our synthetic reservation schedules (with actually more turn-around time "wins" for BD_CPAR than for BD_CPA).

We conclude that among our candidate algorithms for solving RESSCHED the best approach, which in addition leads to low resource consumption, is to use the BL_CPAR method to compute task bottom-levels and the BD_CPAR method to bound task allocations. Note however that the improvement over the BL_CPA and BD_CPA methods are not drastic.

5. MEETING A DEADLINE

5.1 Computational Complexity

RESSCHEDDL is essentially the decision problem associated the RESSCHED optimization problem, and we have seen the NP-hardness of RESSCHED in Section 4.1. Here again we do not develop guaranteed algorithms but instead propose several non-guaranteed heuristics.

5.2 Algorithms

The most natural idea is to use the same scheduling approach as for solving RESSCHED, but "backwards", i.e., scheduling tasks in order of increasing bottom-levels and scheduling them backward in time starting from the deadline, K. We use the BL_CPAR method for computing bottom-levels because it proved the best for solving RESSCHED. For each task t to be scheduled, its successors have already been scheduled (because they have lower bottom-levels). Therefore, one must schedule t so that it finishes no later than the minimum of the start times of its successors (or than K if t is the first task being scheduled). Each task scheduling decision becomes a deadline scheduling decision, where each task has a different deadline. This decision boils down to picking a number of processors for task t and find a reservation (for this number of processors and for the corresponding task execution time) that is as late as possible. The reservation should be as late as possible to leave as much time as possible between the time at which the application is being scheduled (which we term "now") and t's start time, thus making it easier to schedule all tasks with a higher bottom-level than task t.

In the above scheme, for each task scheduling decision there are typically several possible numbers of processors. Each of these numbers of processors would lead to a different start time for task *t*. Therefore we must pick one of several <number of processors, start time > pairs. The question is: which one should be picked?

5.2.1 Aggressive Algorithms

We can use the same three approaches as for bounding task allocations when solving the RESSCHED problem: BD_ALL, BD_CPA,

Table 4: Result summary for turn-around time minimization (with synthetic reservation schedules).

Algorithm	Turn-arou	nd-time	CPU-hours		
	Ave. deg. from best Number of wins		Ave. deg. from best	Number of wins	
BD_ALL	33.75 [%] 36		42.48 [%]	0	
BD_HALF	28.38	3	37.83	1	
BD_CPA	0.29 1026		0.75	6	
BD_CPAR	0.21	386	0.00	1,434	

Table 5: Result summary for turn-around time minimization (with Grid'5000 reservation schedules).

Algorithm	Turn-around-time		CPU-hours		
	Ave. deg. from best Number of wins		Ave. deg. from best	Number of wins	
BD_ALL	34.32 [%]	0	43.08 [%]	0	
BD_HALF	30.43 9		29.17	0	
BD_CPA	0.19	9	0.82	0	
BD_CPAR	0.15	30	0.00	40	

and BD_CPAR. We then obtain three algorithms (whose names start with "DL_" as in DeadLine):

- DL_BD_ALL For each task, in order of increasing bottomlevels, pick the <number of processors, start time> pair that leads to the latest task start time.
- 2. **DL_BD_CPA** Same as DL_BD_ALL, but bound the the number of processors by the CPA-computed allocation assuming that *q* = *p* processors are available.
- 3. **DL_BD_CPAR** Same as DL_BD_CPA, but with *q* equal to the historical average number of available processors.

Based on the results obtained with similar approaches for solving RESSCHED, we expect that algorithm DL_BD_CPAR would be the best of the three. We term these three algorithms "aggressive" because they do not attempt to use fewer processors when the deadline is looser.

5.2.2 Resource Conservative Algorithms

One problem with the previous three algorithms is that they do not adapt the number of processors they use to the tightness of the deadline. If the deadline is loose, then the application could be scheduled using very few processors per task and still meet the deadline. As a result the number of CPU-hours spent would be reduced, a useful feature since users typically have a limited CPU-hour budget. The goal is then to pick a <number of processors, start time> pair with the lowest number of processors that will not preclude meeting the deadline. The challenge is that it is difficult to reason about which task start time is late enough to ensure (with high probability) that the deadline will be met.

We propose one approach for addressing this challenge. Our insight, when scheduling a task t, is to use the CPA algorithm to compute a full schedule for all the application tasks that have not been scheduled yet. This full schedule, computed for some number of processors q, will then produce a particular start time for task t, say T. Provided that q is approximately equal to the number of processors available between "now" and t's deadline, T provides a good guideline for picking a start time for task t. A start time much earlier than T would most likely make it impossible to meet the deadline, while a start time much later than T would likely waste CPU-hours. Our basic strategy when scheduling task t is to first compute T and then pick the <number of processors, start time> pair with the lowest number of processors (to save resources) so that the start time is later than T (to still meet the deadline).

The above strategy results in two algorithms, each for a different values of *q*, as for DL_BD_CPA and DL_BD_CPAR above. The two algorithms are named DL_RC_CPA and DL_RC_CPAR, with RC standing for "Resource Conservative":

- 1. **DL_RC_CPA** For each task, in order of increasing bottom-level, pick the <number of processors, start time> pair that leads to the earliest task start time that is larger than the CPA-computed start time for q = p processor.
- 2. **DL_RC_CPAR** Same as DL_RC_CPA but with *q* equal to the historical average number of available processors.

5.3 Experimental Evaluation

We use two performance metrics. First, for each problem instance we determine the tightest deadline that each algorithm can achieve, with an earlier such deadline denoting better performance. This tightest deadline is determined via binary search. Second, we compute the number of CPU-hours consumed by the schedule produced by each algorithm for a deadline that is 50% as large as the latest tightest deadline across all the algorithms. This second deadline quantifies the resource consumption in a "loose deadline" scenario. We do not conduct experiments for absolute deadline values because whether a deadline is loose or tight strongly depends on the problem instance, i.e., on the application configuration and the reservation schedule.

We compare our five algorithms in simulation using the same experimental methodology as in Section 4.3. Due to the enormous number of experiments and to the fact that searching for the tightest deadline is time consuming, we show results obtained using only the SDSC_BLUE log out of our for logs, thus corresponding to 360 out of our total 1,440 synthetic experimental scenarios, with 1,000 random RESSCHEDDL instances for each. We also show results obtained for 50 reservation schedules extracted from the Grid'5000 logs at random start times.

Table 6 shows a summary of the results using percentage average degradation from best as in Section 4.3.2. For each metric we show four columns of results, one showing average results for each value of φ and one for the Grid'5000 reservation schedules. Recall that a higher φ means a less sparse reservation schedule. The first observation is that in all cases the resource conservative algorithms, DL_RC_CPA and DL_RC_CPAR, lead to dramatically lower resource consumption than the aggressive algorithms when given loose deadlines. The DL_BD_ALL aggressive algorithm leads to resource consumption that is orders of magnitude higher

Table 6: Result summary for meeting a deadline

Algorithm	Tightest deadline				CPU-hours for loose deadline				
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	(Average % degradation from best)			(Avei	(Average % degradation from best)				
	$\phi = 10$	$\phi = 10 \phi = 20 \phi = 50 Grid'5000$			$\phi = 10$	$\phi = 20$	$\phi = 50$	Grid'5000	
DL_BD_ALL	178.43	175.58	188.33	227.03	3556.70	3486.30	3769.20	2006.30	
DL_BD_CPA	6.11	6.16	6.26	8.00	252.30	251.36	275.05	185.58	
DL_BD_CPAR	6.52	6.44	6.91	8.38	231.01	236.97	243.60	179.35	
DL_RC_CPA	13.17	13.27	17.36	19.51	6.39	6.80	7.98	2.15	
DL_RC_CPAR	4.12	4.27	8.26	15.13	0.16	0.15	0.16	0.09	

than the other algorithms due to its use of overly large allocations. As expected also, the DL_BD_CPAR algorithm uses slightly fewer resources than the DL_BD_CPA algorithm because of its use of smaller allocations.

In terms of deadline tightness the DL_BD_ALL leads to very poor performance, again due to its use of overly large allocations that hinder task parallelism. More interestingly, for $\phi = 10$ and $\phi = 20$, DL RC CPAR leads to marginally tighter deadlines than the aggressive algorithms! This is because DL RC CPAR tries to match the CPA schedule as much as possible, which has the effect of both saving CPU-hours and leading to short turn-around times, and thus to possibly tighter deadlines. For $\phi = 50$, we see that the aggressive algorithm perform marginally better. With $\phi = 50$ the reservation schedule is less sparse and there are more chances for DL_RC_CPAR to be left in a bind, for instance after a large fraction of the DAG has been scheduled. With such reservation schedules, it is very difficult to match the CPA schedule as much as possible, and attempting to match it leads to missing tight deadlines. Instead, the aggressive algorithms are deadline conservative since they use more resources whenever possible. They are therefore less susceptible to missing a tight deadline. This phenomenon is amplified for the DL_RC_CPA, which leads to poorer results than DL_RC_CPAR and than the aggressive algorithms: it misses tight deadlines because it overestimates the number of available proces-

Our results indicate no particular trends with respect to most of the 6 application parameters defined in Table 1, or with the method used to generate reservations (linear, expo, or real). The only exception is the number of tasks. We witness the same trend when the number of task increases as when ϕ increases, meaning that the resource conservative algorithms do not achieve as tight deadlines as the aggressive algorithms. Here again it is because with more tasks in the application there are more opportunities for the resource conservative algorithms to be left in a bind when attempting to meet a tight deadline.

Note that the above weakness of the resource-conservative algorithms could be easily remedied by adding a parameter for tuning their resource conservativeness. As we have described them, for each task these algorithms pick the <number of processors, start time> pair with the lowest number of processors and with a task start time $\geqslant T$, where T is the CPA-computed task start time. Instead they could pick the pair with the lowest number of processors such that the task start time is $\geqslant \lambda \cdot T$, where λ is a tunable parameter > 1. The best λ could then be determined experimentally.

Finally, the results for the Grid'5000 reservation schedules are consistent with those for the synthetic reservation schedules, although the advantage of the resource-conservative algorithms are marginally lower in terms of deadline tightness and marginally higher in terms of CPU-hours.

We conclude that the BD_RC_CPAR algorithm is the best choice. In low reservation load conditions (i.e., $\phi=10$ or $\phi=20$) it leads

to deadlines tighter than or comparable to the deadlines achieved by its competitors. Even in high reservation load conditions (i.e., $\varphi=50$) it leads to deadlines that are at most 15% looser than the aggressive algorithms. More importantly, in all cases BD_RC_CPAR leads to resource consumption that is lower than that of BD_RC_CPA and orders of magnitude lower than that of the aggressive algorithms

6. CONCLUSION

We have studied the problem of scheduling mixed-parallel workflows using advance reservations on a parallel platform that is subject to advance reservations from competing users. We have defined two scheduling problems, RESSCHED and RESSCHEDDL, depending on whether the goal is to minimize application turnaround-time or to meet a deadline, respectively. For each problem we have proposed and evaluated a set of scheduling algorithms. These algorithms were compared for both their performance (i.e., turn-around-time and tightest deadline met) and their resource consumption. Some of these algorithms reuse and adapt some of the ideas developed in the CPA algorithm [37] to compute task-bottom levels, to bound task allocations, and to compute the most resourceconservative allocations. We found these algorithms to be the most effective when using a CPA-schedule computed with an approximation (albeit coarse) of the expected available number of processors. Most notably, CPA-inspired schedule can be used to drastically reduce CPU-hour consumption. Our simulator is publicly available¹.

This work can be extended in three main directions. To the best of our knowledge this paper is the first to propose scheduling algorithms for mixed-parallel applications in an advance reservation scenario. Therefore a first natural direction is to improve on the algorithms that we have proposed to solve our scheduling problems. For instance, it would be interesting to use the iCASLB algorithm [46] instead of CPA. In fact, iCASLB could perhaps be adapted directly to advance reservation scenarios. A second direction, this one on the practical side, would be to explore how the algorithms can be implement in real-world systems by removing some of our assumptions. Prime candidates for removal are our assumption that while the application is being scheduled the reservation schedule does not change, and our assumption that the scheduling algorithm has full knowledge of the reservation schedule. A broader question of course is to consider platforms beyond a single homogeneous cluster, such as heterogeneous multi-grid platforms. It would be interesting to see how mixed-scheduling algorithms for heterogeneous platforms [34] could be adapted to consider advance reservations.

¹http://navet.ics.hawaii.edu/~casanova/software/res_ simulator.tar.qz

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