Bitmasks

ICS312 Machine-Level and Systems Programming

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Boolean Bitwise Operations

- There are assembly bitwise instructions for all standard boolean operations: AND, OR, XOR, and NOT
- Bits are computed individually (i.e., "bitwise")
- Examples:

AND	1 0 1 1 0 0 0 0								∩R	1	1	0	0	0	1	0	1
	1	1	0	1	1	0	1	1	- -	0	1	1	0	1	1	1	0
=	1	0	0	1	0	0	0	0	=	1	1	1	0	1	1	1	1

Boolean Bitwise Instructions

mov ax, 0C123h

and ax, 082F6h; ax = C123 **AND** 82F6 = 8022

or ax, 0E34Fh; ax = 8022 **OR** E34F = E36F

xor ax, 036E9h; ax = E36F **XOR** 36E9 = D586

not ax; ax = NOT D586 = 2A79

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The test Instruction

- The test instruction performs an AND, but does not store the result
- It only sets the FLAG bits
 - Just like cmp does a subtraction but never stores its result
- Note that all boolean bitwise instructions do set the FLAG bits, BUT for the not operation, which doesn't
- Example:

```
mov al, 0FFh
test al, 000h
jz foo ; branches jz foo ; may not branch
```

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Uses of Bitwise operations

- Bitwise operations are used to modify particular bits in data
- This is done via bit masks, i.e., constant (or "immediate") quantities with carefully chosen bits
- Example:
 - Say you want to "turn on" bit 3 of a 2-byte value (counting from the right, with bit 0 being the least significant bit)
 - An easy way to do this is to OR the value with 00000000000001000, which is 8 in decimal
 - Say the value is stored in ax
 - You can simply execute the instruction:

```
or ax, 8; turns on bit 3 in ax
```

- Easy to generalize
 - To turn on bits: use OR (with appropriate 1's in the bit mask)
 - □ To turn off bits: use AND (with appropriate 0's in the bit mask)
 - To flip bits: use XOR (with appropriate 1's in the bit mask)

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Bit Mask Operations Examples

mov eax, 04F346BA2h

or ax, 0F000h; turns on 4 leftmost bits of ax

; eax = 4F34FBA2

xor eax, 000400000h ; flips bit 22 of EAX

; eax = 4F74FBA2

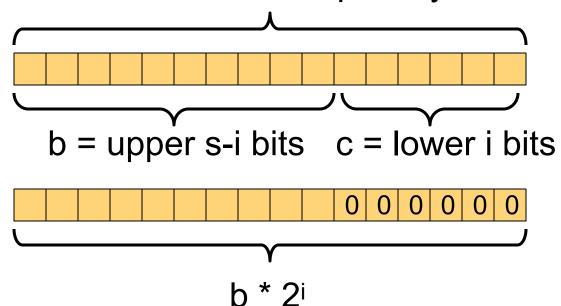
xor ax, 0FFFFh ; 1's complement of ax

; eax = 4F74045D

; (same as doing "not")

Remainder of a Division by 2i

- To find the remainder of a division of an operand by 2ⁱ, just AND the operand by 2ⁱ-1
- Why does this work? a = s-bit quantity

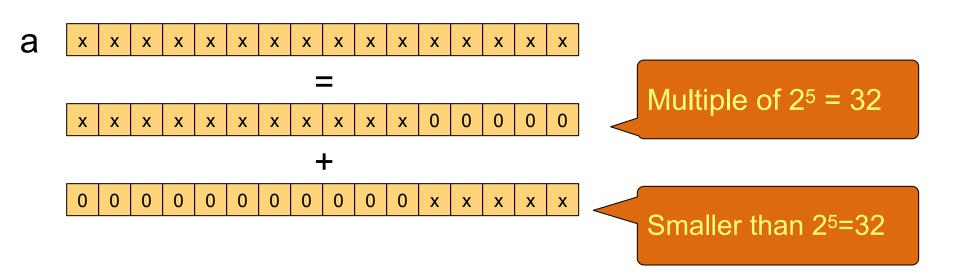


Therefore, $a = b * 2^i + c$, an c is the remainder! The remainder is simply the lowest i bits!

Another Way to Look at it

Example with i=5

Another Way to Look at it



- Therefore, a = <some multiple of 32> + <some number smaller than 32>
- By definition, that smaller than 32 number is the remainder of the division of a by 32 It is just the low $log_2(32)=5$ bits of a!!!

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Remainder of a Division by 2ⁱ

Let's compute the remainder of the integer division of 123d by 2⁵=32d (unsigned) by doing an AND with 2⁵-1

```
mov ax, 123
mov bx, 0001Fh
and bx, ax
```

```
0 0 0 0 0 0 0 0 1 1 1 1 0 1 1 ax

0 0 0 0 0 0 0 0 0 0 1 1 1 1 1 1 bx

0 0 0 0 0 0 0 0 0 0 0 1 1 1 1 1 bx
```

- The remainder when dividing 123 by 32 is 11011b = 27d
- Often one says "I masked out the 11 high bits of ax" (using bx as the bitmask)

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Turning on a specific bit

- Say you want to turn on a specific bit in some data, but that you don't know which one before you run the program
 - the index of the bit to turn on is contained in a register
 - we need to build the bit mask "on the fly"
- Assuming that the index of the bit is initially in bl, and that we wish to turn on a bit in eax

```
mov cl, bl ; must have the bit index in cl
mov ebx, 1 ; create a number 0...01
shl ebx, cl ; shift it left cl times
or eax, ebx ; turn on the desired bit using
```

; ebx as a mask!

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Turning off a specific bit

- Turning a bit off requires one more instruction, to generate a bit mask that looks like 1...101..1
- Assuming that the index of the bit is initially in bl, and that we which to turn on a bit in eax

```
mov cl, bl ; must have the bit index in cl mov ebx, 1 ; create a number 0...01 shl ebx, cl ; shift it left cl times not ebx; ; take the complement! and eax, ebx ; turn off the desired bit using : ebx as a mask!
```

An odd xor

- One often sees the following instruction:
 - xor eax, eax ; eax = 0
- This is a simple way to set eax to 0
- It is useful because its machine code is smaller than that of, for instance, "mov eax, 0"
- Therefore one saves a few bits in the text segment, meaning that when the program runs it will load fewer bits less from memory, saving perhaps a few cycles
- Message: One could do everything with high-level operations, but the good (assembly) programmer (and definitely the good compiler) will use bit operations to save memory and/or time
- Let's go through the example in Section 3.3, which is a good example of bit operation "craziness"

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Avoiding Conditional Branches

- Section 3.3 is all about a trick to avoid conditional branches
- Conditional branches kill performance
 - Essentially, one key to making processors go fast is to allow them to know what's coming up next
 - With conditional branches, the processor doesn't know in advance whether the branch will be taken or not
- In many cases, one cannot avoid using conditional branches
 - It's just in the nature of the computation
 - □ For instance, in a foor loop
- But in some cases it's possible, with some cleverness
- Let's just look at an example that illustrates some of the coolness/craziness of bitwise operations

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SETxx Instructions

- The x86 assembly provides a set of instructions that set the value of a byte register (e.g., al) or of a byte memory location to 0 or 1 based on a flag
- Say you want to set al to 0 if bx > cx or to 1 otherwise (all signed)
- With the setg instruction you can save a conditional branch:

```
; without setg
mov al, 1 ; al = 1
cmp bx, cx ; compare
jng next ; jump if bx <= cx
mov al, 0 ; al = 0
next:</pre>
```

```
; with setg
cmp bx, cx
setg al, 0
```

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SETxx Instructions

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mov al, 1; al = 1
cmp bx, cx; compare
jng next; jump if bx <= cx
mov al, 0; al = 0
next:
```

```
; with setg
cmp bx, cx
setg al, 0
```

The second operand is added to al "after" al is set to 0 or 1. In this case we don't want to add anything, so we use "0"

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Example: max(a,b)

- Say we want to store into ecx the maximum of two (signed) numbers, one stored in eax and the other one in [num]
- Here is a simple code to do this

```
cmp eax, [num]
jge next ; conditional branch
mov ecx, [num]
jmp end
next:
mov ecx, eax
end:
```

- Let's rewrite this without a conditional branch!
- Just follow along... this won't strike you as intuitive but you should be able to understand that it works
 - Even though you wouldn't have been able to do it from scratch on your own, most likely

Example: max(a,b)

- To avoid the conditional branch, one needs a SETxx instruction and clever bit masks
- We use a helper register, ebx, which we set to all zeros

```
xor ebx, ebx ; ebx = 0
```

We compare the two numbers

```
cmp eax, [num]; compare eax to [num]
```

We set the value of bl to 0 or 1 depending on the result of the comparison

```
setg bl ; set bl to 0 or 1

If eax > [num], ebx = 1 = 0...01b

If eax <= [num], ebx = 0 = 0...00b
```

■ We negate ebx (i.e., take 1's complement and add 1)

```
neg ebxIf eax > [num], ebx = FFFFFFFhIf eax <= [num], ebx = 0000000000h</li>
```

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Example: max(a,b)

- We now have:
 - eax contains one number, [num] contains the other
 - □ If eax > [num], ebx = FFFFFFFF (we want to "return" eax)
 - If eax <= [num], ebx = 0000000000h (we want to "return" [num])</p>
- If eax is the maximum and we AND eax and ebx, we get eax, otherwise we get zero
- If [num] is the maximum and we AND [num] and NOT(ebx), we get [num], otherwise we get zero
- So if we compute ((eax AND ebx) OR ([num] AND NOT(ebx))) we get the maximum!
 - □ If eax is the maximum (ebx = FFFFFFFh):
 - ((eax AND ebx) OR ([num] AND NOT(ebx))) = eax OR 0...0 = eax
 - □ If [num] is the maximum (ebx = 00000000h):
 - ((eax AND ebx) OR ([num] AND NOT(ebx))) = 0...0 OR [num] = [num]
- Now we just need to compute ((eax AND ebx) OR ([num] AND NOT(ebx)))

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Example: max(a,b)

ecx, ebx

or

Computing ((eax AND ebx) OR ([num] AND NOT(ebx))): ecx, ebx mov and ecx, eax : ecx = eax AND ebx not ebx ebx, [num] ; ebx = [num] AND NOT(ebx) and ecx, ebx ; voila! or Whole program: ebx, ebx; ebx = 0xor eax, [num] ; compare eax and [num] cmp setg ; bl = 1 if eax > [num], 0 otherwise bl ebx ; take one's complement + 1 neg ecx, ebx mov and ; ecx = eax AND ebx ecx, eax not ebx ebx, [num] and ; ebx = [num] AND NOT(ebx)

; voila!

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Predicates

- The technique we have used to remove a conditional branch is often called "predicates"
- Essentially, you replace conditional branches with Boolean computations that "work out"
- Predicates are (or should be) used extensively when programming for the GPU
 - For performance reasons
- Whether the previous example leads to performance gains is unclear:
 - Version #1: we have a "bad" branch instruction
 - Version #2: we have a lot of computation
- But if we have a lot of maximum computations to perform in a row, Version #2 is almost certainly faster

Bitwise Operations in High-Level Languages

- Although in this course we focus on assembly programming, let's discuss highlevel languages a little bit
- All high-level languages provide bitwise operations
- Let's look at the typical bitwise operators...

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Operators in C/C++/Java/...

- Boolean Operations:
 - □ AND: &&
 - □ OR: ||
 - □ XOR: XXX
 - □ NOT: !
- Bitwise Operations:
 - □ AND: &
 - □ OR: |
 - □ XOR: ^
 - □ NOT: ~
- Shift Operations:
 - □ Left Shift: <<
 - □ Right Shift: >>
 - Logical if operand is unsigned (not in Java)
 - Arithmetic is operand is signed

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Example Operations: C/C++

```
short int
                            // 2-byte signed
                       S;
                            // 2-byte unsigned
short unsigned int
                       u;
                            // s = 0xFFFF
s = -1;
                            // u = 0x0064
u = 100;
                            // u = 0x0164
u = u \mid 0x0100;
s = s \& 0xFFF0;
                            // s = 0xFFF0
                            // s = 0xFE94
s = s \wedge u;
                            // u = 0x0B20
u = u << 3;
                            // s = 0xFFA5
s = s >> 2;
```

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Common Uses of Bit Operations

- One can use bit operations in high-level languages like in assembly
 - e.g., fast multiplications and divisions
- A very common use is for dealing with file permissions on UNIX systems
- The POSIX API, for dealing with files on all Linux systems, uses bits to encode file access permissions
- If you have to write code that needs to read/modify file permissions, then you need to use bitwise operations

Using chmod from C

- In a POSIX system, there is a C library function called chmod() that modifies permissions
- chmod() takes two arguments:
 - The file name
 - A 4-byte quantity that is interpreted as a bunch of individual bits, which describe the permission
- To make life easy, the user does not have to construct the bits by hand, but there are macros
- For instance: (p contains the file's permission bits) chmod("file", p | S_IRUSR)

Gives read permission to the owner of the file S_IRUSR has one of its bits turned on

- This makes it easy to do multiple things at once: chmod("file", p | S_IRUSR | S_IWUSR | S_IROTH) The user can read and write, all "other" users can read
- Simply use a bitwise OR to apply all permission settings

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Modifying Permissions

- Say you want to write a program that, given a file, removes write access to others and adds read access to the owner of the file
- First step: get the 4-byte permission data struct stat s; // data structure stat("file", &s); // get all file metadata unsigned int p; // 4-byte quantity p = s.st mode; // p = permission bits
- Second step: modify, keeping most bits unchanged chmod("file", (p & ~S_IWOTH) | S_IRUSR);

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Counting Bits

- Section 3.6 of the book shows methods for counting bits
- These methods are shown in C, but of course it's easy (if perhaps cumbersome) to implement them in assembly
- Let's look at Method #1
 - Make sure you look at the others on your own and that you understand them (some are quite creative)

```
unsigned char data; // 1 byte (book uses 4)
char count=0; // counter (only 1 byte necessary)
while (data) {
   data = data & (data -1);
   cnt++;
}
printf("number of 1 bits: %d\n",count);
```

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Counting Bits

```
while (data) {
  data = data & (data -1);
  cnt++;
Example: data = 01011010 (in binary)
   □ data = data & (data -1) = 01011010 & 01011001
                         = 01011000
   □ data = data & (data -1) = 01011000 & 01010111
                          = 01010000
   etc.
```

- At each step, we set the rightmost 1 bit to 0!
- When we have all zeros we stop
- The number of iterations is the number of 1 bits!!

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Detecting duplicates

- Inspired from the first exercise in the "Cracking the Coding Interview" book
- You have write a function that takes an ASCII character as input, and returns true is that function was called previously with that ASCII character
- Typical idea: maintain a set of "already seen" characters
 - e.g., a <char, boolean> map, an array of boolean
- But storing a boolean in a byte is super wasteful
 - You're wasting 7 out of 8 bits
- The book suggests using a "bit field" to save space
- Let's do it live... (could be bad;))



Next week we'll have an in-class practice quiz about this module

Let's look at Homework assignment #6