evaluation

October 7, 2024

1 Evaluation

1.1 Machine specs

The evaluation was performed on a machine with the following specs: - 12th Gen Intel(R) Core(TM) i7-1255U 1.70 GHz - 16 GB of RAM - Windows 11

The evaluation of MAFIA was performed using GPUMAFIA, which was installed on a virtual machine using VirtualBox. The virtual machine was configured with 4 CPUs and 4 GB of RAM. The operating system was Ubuntu 24.04.1 LTS.

CLIQUE and SUBCLU were evaluated on the host machine using ELKI.

1.2 Scalability with data size

- $\bullet\,$ Tested on a 20-dimensional data set containing 5 clusters in 5 different subspaces.
- 10% of the data was added as noise records.
- CLIQUE stopped working after 7mio records and SUBCLU stopped working after 200,000 records. MAFIA was able to handle at least 15mio records.

1.2.1 Settings

CLIQUE: - xsi: 25 - tau: 0.08

SUBCLU: - epsilon 0.02 - minpts: 250 (for 10k points). Doubled for each step, so 500 minpts for 20k, 1000 minpts for 40k, etc.

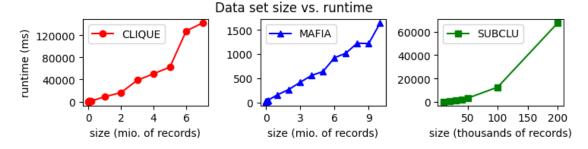
MAFIA: -a 1.4 -b 0.35 -M 20 -n 1000 -V -timing

1.2.2 Plot

```
[1]: import matplotlib.pyplot as plt import matplotlib.ticker as ticker

# Data
size = [10000, 20000, 30000, 40000, 50000, 100000, 2000000, 1000000, 2000000, 3000000, 4000000, 5000000, 6000000, 7000000, 8000000, 9000000, 10000000, 15000000]
clique = [62 , 119 , 155 , 203 , 235 , 533 , 1255 , 8795 , 16290 , 38581 , 50392 , 62348 , 127730 , 142005]
```

```
[15 , 25 , 17
                            , 22 , 27 , 31 , 45
mafia =
         , 556 , 637
                        , 922
                                  , 1016 , 1225
                                                    , 1215
 414
subclu = [137 , 477 , 984 , 1751 , 3055 , 12490 , 67603]
# Figure with 3 subplots
fig, axs = plt.subplots(1, 3, figsize=(7.5, 2))
# CLIQUE (size in millions)
axs[0].plot([s / 1_000_000 for s in size[:len(clique)]], clique, 'ro-', []
 →label='CLIQUE')
axs[0].set_xlabel('size (mio. of records)')
axs[0].set ylabel('runtime (ms)')
axs[0].xaxis.set_major_locator(ticker.MaxNLocator(5))
axs[0].yaxis.set_major_locator(ticker.MaxNLocator(5))
axs[0].legend()
# MAFIA (size in millions)
axs[1].plot([s / 1_000_000 for s in size[:len(mafia)]], mafia, 'b^-',__
 →label='MAFIA')
axs[1].set_xlabel('size (mio. of records)')
axs[1].xaxis.set_major_locator(ticker.MaxNLocator(4))
axs[1].yaxis.set_major_locator(ticker.MaxNLocator(4))
axs[1].legend()
# SUBCLU (size in thousands)
axs[2].plot([s / 1000 for s in size[:len(subclu)]], subclu, 'gs-', __
⇔label='SUBCLU')
axs[2].set_xlabel('size (thousands of records)')
axs[2].xaxis.set_major_locator(ticker.MaxNLocator(5))
axs[2].yaxis.set_major_locator(ticker.MaxNLocator(4))
axs[2].legend()
# Show plots
plt.suptitle('Data set size vs. runtime')
plt.tight_layout(rect=[0, 0, 1, 1.1])
plt.show()
```



1.3 Accuracy

Tested on a 10-dimensional data set containing 100,000 points for testing CLIQUE and MAFIA, however, SUBCLU was not able to handle this amount of data, so it was tested on a similar distribution of points with 20,000 points. 10% of the data was added as noise records.

The first case, has two clusters embedded in a different 4 dimensional subspace. Second case, has 4 clusters embedded in a different 4 dimensional subspace.

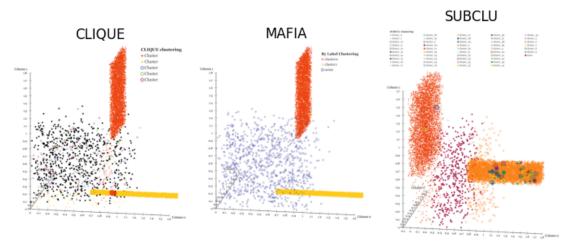
MAFIA reports the correct clusters in both cases with proper use of parameters. However, CLIQUE reports...

1.3.1 2 clusters

```
Settings SUBCLU: - epsilon: 0.05 - minpts: 850 CLIQUE: - xsi: 20 - tau: 0.41 - prune: false MAFIA: -a 3 -b 0.6 -M 20 -n 1000 -V -p -timing
```

```
[2]: import matplotlib.pyplot as plt
    import matplotlib.image as mpimg
    # Load images
    clique_img = mpimg.imread('data-generator/datasets/mdcgen/accuracy/2clusters/
     mafia_img = mpimg.imread('data-generator/datasets/mdcgen/accuracy/2clusters/
     subclu_img = mpimg.imread('data-generator/datasets/mdcgen/accuracy/2clusters/
     ⇔20k/subclu/3d_plot.png')
    # Figure with subplots
    fig, axs = plt.subplots(1, 3, figsize=(7, 4))
    # Plot images
    axs[0].imshow(clique_img)
    axs[0].axis('off')
    axs[0].set_title('CLIQUE')
    axs[1].imshow(mafia_img)
    axs[1].axis('off')
    axs[1].set_title('MAFIA')
    axs[2].imshow(subclu_img)
    axs[2].axis('off')
    axs[2].set_title('SUBCLU')
```

Accuracy for 2 clusters in a 10-dimensional (3 dimensions shown) data set



1.3.2 4 clusters

Settings SUBCLU: - epsilon: 0.02 - minpts: 500

CLIQUE: - xsi: 35 - tau: 0.2

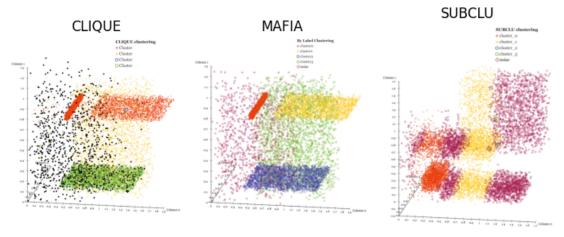
MAFIA: -a 3 -b 0.6 -M 100 -n 1000 -V -p -timing

```
# Figure with subplots
fig, axs = plt.subplots(1, 3, figsize=(7, 4))
# Plot images
axs[0].imshow(clique_img)
axs[0].axis('off')
axs[0].set_title('CLIQUE')
axs[1].imshow(mafia_img)
axs[1].axis('off')
axs[1].set_title('MAFIA')
axs[2].imshow(subclu_img)
axs[2].axis('off')
axs[2].set_title('SUBCLU')
# Title
plt.suptitle('Accuracy for 4 clusters in a 10-dimensional (3 dimensions shown)

data set¹)

# Show plot
plt.tight_layout(rect=[0, 0, 1, 1.15])
plt.show()
```

Accuracy for 4 clusters in a 10-dimensional (3 dimensions shown) data set



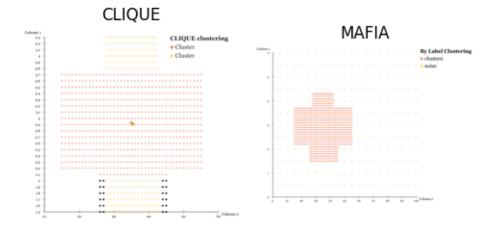
1.3.3 Plus shape

Settings CLIQUE: - xsi: 10 - tau: 0.2

```
[4]: import matplotlib.pyplot as plt
     import matplotlib.image as mpimg
     # Load images
     clique img = mpimg.imread('data-generator/datasets/home made/accuracy/
      ⇔plus_shape/clique/plot.png')
     mafia_img = mpimg.imread('data-generator/datasets/home_made/accuracy/plus_shape/

¬mafia/plot.png')
     # Figure with subplots
     fig, axs = plt.subplots(1, 2, figsize=(5, 4))
     # Plot images
     axs[0].imshow(clique_img)
     axs[0].axis('off')
     axs[0].set_title('CLIQUE')
     axs[1].imshow(mafia_img)
     axs[1].axis('off')
     axs[1].set_title('MAFIA')
     # Title
     plt.suptitle('Accuracy for a plus-shaped cluster in a 2-dimensional data set')
     # Show plot
     plt.tight_layout(rect=[0, 0, 1, 1.25])
     plt.show()
```

Accuracy for a plus-shaped cluster in a 2-dimensional data set

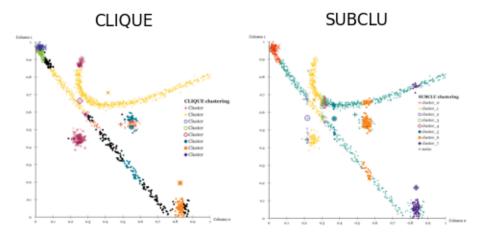


1.3.4 Bezier curve

```
Settings SUBCLU: - epsilon: 0.005 - minpts: 20 CLIQUE: - xsi: 20 - tau: 0.06
```

```
[5]: import matplotlib.pyplot as plt
     import matplotlib.image as mpimg
     # Load images
     clique_img = mpimg.imread('data-generator/datasets/artificalCluster/accuracy/
     ⇔bezier/clique/plot.png')
     subclu_img = mpimg.imread('data-generator/datasets/artificalCluster/accuracy/
      ⇔bezier/subclu/plot.png')
     # Figure with subplots
     fig, axs = plt.subplots(1, 2, figsize=(5, 4))
     # Plot images
     axs[0].imshow(clique_img)
     axs[0].axis('off')
     axs[0].set_title('CLIQUE')
     axs[1].imshow(subclu_img)
     axs[1].axis('off')
     axs[1].set_title('SUBCLU')
     # Title
     plt.suptitle('Accuracy for a bezier-shaped cluster in a 2-dimensional data set')
     # Show plot
     plt.tight_layout(rect=[0, 0, 1, 1.25])
     plt.show()
```

Accuracy for a bezier-shaped cluster in a 2-dimensional data set



1.4 Cluster dimensionality

1.4.1 Settings

CLIQUE: - xsi: 30 - tau: 0.25

MAFIA: -a 2.2 -b 0.35 -M 40 -n 1000 -p -V -timing

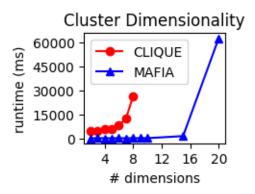
1.4.2 Plot

```
[6]: import matplotlib.pyplot as plt
    import matplotlib.ticker as ticker
    # Data
    dims =
             [2, 3, 4, 5, 6, 7, 8, 9, 10, 15, 20]
    mafia = [45 , 63 , 55 , 45 , 63 , 55 , 60 , 79, 86, 1387, 62607]
    clique = [4440, 4347, 6017, 5740, 8093, 12532, 26373]
    # Figure size
    plt.figure(figsize=(2.5, 2.1))
    # Plot both in same figure
    plt.plot(dims[:len(clique)], clique, 'ro-', label='CLIQUE')
    plt.plot(dims, mafia, 'b^-', label='MAFIA')
    # Set number of x-ticks
    plt.gca().xaxis.set_major_locator(ticker.MaxNLocator(6))
    plt.gca().yaxis.set_major_locator(ticker.MaxNLocator(6))
    # Add labels and title
```

```
plt.xlabel('# dimensions')
plt.ylabel('runtime (ms)')
plt.title('Cluster Dimensionality')

# Add legend
plt.legend()

# Show plot
plt.tight_layout()
plt.show()
```



1.5 Data dimensionality

MAFIA and CLIQUE was on a $100~\mathrm{k}$ dataset.

1.5.1 Settings

```
CLIQUE: - xsi: 30 - tau: 0.3 - prune: false MAFIA: -a 2.2 -b 0.35 -M 40 -n 1000 -p -V -timing
```

1.5.2 Plot

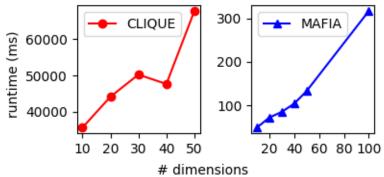
```
[7]: import matplotlib.pyplot as plt import matplotlib.ticker as ticker

# Data dims = [10 , 20 , 30 , 40 , 50 , 100] mafia_runtime = [49 , 72 , 85 , 104 , 133, 317] clique_runtime = [35688, 44180, 50275, 47682, 67772]

# CLIQUE: # 10d = 66 clusters found # 20d = 84
```

```
# 30d = 93
# 40d = 77
# 50d = 93
# 100d, not able to run.
# MAFIA:
# 10d = 3 clusters found
# 20d = 4 clusters found
# 30d = 3 clusters found
# 40d = 4 clusters found
# 50d = 3 clusters found
# 100d = 4 clusters found
# Figure with 2 subplots
fig, axs = plt.subplots(1, 2, figsize=(4, 2))
# CLIQUE
axs[0].plot(dims[:len(clique_runtime)], clique_runtime, 'ro-', label='CLIQUE')
axs[0].legend()
axs[0].xaxis.set_major_locator(ticker.MaxNLocator(5))
# MAFTA
axs[1].plot(dims, mafia_runtime, 'b^-', label='MAFIA')
axs[1].legend()
axs[1].xaxis.set_major_locator(ticker.MaxNLocator(5))
\# Common x and y labels
fig.text(0.5, -0.02, '# dimensions', ha='center')
fig.text(-0.01, 0.5, 'runtime (ms)', va='center', rotation='vertical')
# Show plot
plt.suptitle('Runtime vs. Data Dimensionality')
plt.tight_layout(rect=[0, 0, 1, 1.1])
plt.show()
```

Runtime vs. Data Dimensionality



1.6 Sensitivity of alpha

As observed in article. Alpha and beta controls the number of clusters and their quality.

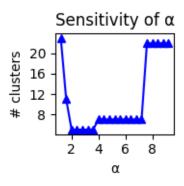
- 1,000,000 data points
- 20 dims
- 5 clusters
- 10% outliers
- noiseMatrix: 1 3 5 7 8

1.6.1 Settings

```
-b 0.35 -M 40 -n 1000
-a 0.8 -> 5.2 (step size: 0.4)
```

1.6.2 Plot

```
[8]: import matplotlib.pyplot as plt
     import numpy as np
     # Data
     alpha = np.arange(1.2, 9.6, 0.4)
     clusters_found = [23, 11, 5, 5, 5, 5, 5, 7, 7, 7, 7, 7, 7, 7, 7, 7, 22, 22, 22, 21
     ⇒22, 22]
     # Figure size
     plt.figure(figsize=(2, 2))
     # Plot
     plt.plot(alpha, clusters_found, 'b^-')
     # Set number of x- and y-ticks
     plt.gca().xaxis.set_major_locator(ticker.MaxNLocator(5))
     plt.gca().yaxis.set_major_locator(ticker.MaxNLocator(5))
     # Add labels and title
     plt.xlabel(' ')
     plt.ylabel('# clusters')
     plt.title('Sensitivity of ')
     # Show plot
     plt.tight_layout()
     plt.show()
```



2 Export to pdf

1. Install a LaTeX distribution.

• Windows: MikTeX

• Mac: MacTeX

• Linux: TeX Live

- 2. Install pandoc (https://pandoc.org/), make sure it can be found using pandoc --version. Otherwise, try to re-open terminal.
- 3. Convert to pdf by running the following command: jupyter nbconvert --to pdf evaluation.ipynb.