Modeling the cumulative incidence function of clustered competing risk data: a multinomial GLMM approach

master thesis defense



Henrique Laureano (.github.io)

April 7, 2021

- 1 Data
- 2 Modeling
- 3 Application
- 4 Model
- Gontributions & challenges
- 6 Template Model Builder
- Simulation stud

Results 2/22

Clustered competing risk data



Key terms:

- Clustered: groups with a dependence structure (e.g. families);
- Causes competing by something.

Something?

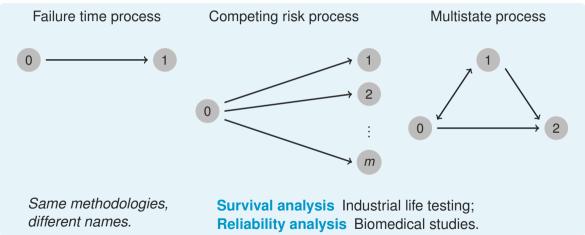
- Failure of an industrial or electronic component;
- Occurence or cure of a disease or some biological process;
- Progress of a patient clinic state.

Independent of the application, always the same framework

Cluster	ID	Cause 1	Cause 2	Censorship	Time	Feature
1	1	Yes	No	No	10	Α
1	2	No	No	Yes	8	Α
2	1	No	No	Yes	7	В
2	2	No	Yes	No	5	Α

Big picture: Failure time data





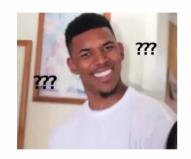


- Data
- 2 Modeling
- 3 Application
- 4 Model
- Gontributions & challenges
- 6 Template Model Builder
- Simulation stud

Results 5/22

Modeling clustered competing risks data









What? Why? How?

Failure time data → Survival models



First of all, we have to choose which scale we model the survival experience.

Usually, is in the

hazard (failure rate) scale :
$$\lambda(t \mid \text{features}) = \lambda_0(t) \times c(\text{features})$$
. (1)

We have a Equation 1 for each competing cause.

The cluster dependence is something actually not measured...

Not measured dependence \rightarrow random/latent effects \rightarrow Frailty models.

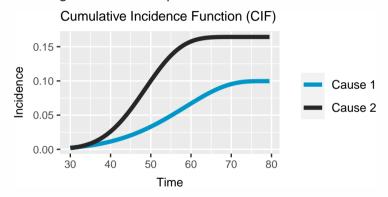
Full likelihood analysis with frailty models for competing risks data is generally complicated, when not impracticable.

• *Not* usually, the probability scale.

Clustered competing risks in the probability scale



for us, is more attractive possibility is to work on the probability scale, focusing on the cause-specific



i.e.

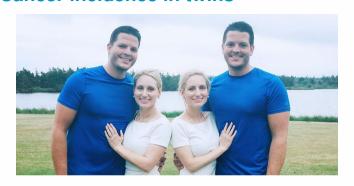
 $CIF = \mathbb{P}[\text{ failure time } \leq t, \text{ a given cause } | \text{ features }]$

- 1 Data
- 2 Modeling
- 3 Application
- 4 Model
- **(5)** Contributions & challenges
- Template Model Builder
- Simulation stud
- Results

9/22

Cancer incidence in twins





Clustered competing risks data

L Clusters? Families

Family studies

Twins data

Family studies ⇒ within-family dependence

That may reflect

- Disease heritability;
- The impact of shared environmental effects;
 - Parental effects: continuity of the phenotype across generations.

- Data
- 2 Modeling
- 3 Application
- 4 Model
- **(5)** Contributions & challenges
- 6 Template Model Builder
- Simulation stud

Results

Our contribution: a hierarchical approach



Thinking on two competing causes

... for the outcome y_{ijt} of a subject i, family j, in the time t, we have

$$y_{ijt} \mid \underbrace{\{u_{1j}, u_{2j}, \eta_{1j}, \eta_{2j}\}}_{\text{latent effects}} \sim \text{Multinomial}(p_{1ijt}, p_{2ijt}, p_{3ijt})$$

$$\begin{bmatrix} u_{1j} \\ u_{2j} \\ \eta_{1j} \\ \eta_{2j} \end{bmatrix} \sim \text{Multivariate} \begin{pmatrix} \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}, \begin{bmatrix} \sigma_{u_1}^2 & \sigma_{u_1, u_2} & \sigma_{u_1, \eta_1} & \sigma_{u_1, \eta_2} \\ \sigma_{u_2}^2 & \sigma_{u_2, \eta_1} & \sigma_{u_2, \eta_2} \\ \sigma_{\eta_1}^2 & \sigma_{\eta_1, \eta_2}^2 \end{bmatrix}$$

$$p_{kijt} = \frac{\partial \text{CIF}}{\partial t}$$

$$= \frac{\partial}{\partial t} \underbrace{\pi_k(X, u_1, u_2 \mid \beta)}_{\text{cluster-specific risk level}} \underbrace{\Phi[w_k g(t) - X^\top \gamma_k - \eta_k]}_{\text{cluster-specific failure time trajectory}}$$

k = 1, 2.

- Data
- 2 Modeling
- 3 Application
- 4 Model
- **5** Contributions & challenges
- 6 Template Model Builder
- Simulation stud

Results 13/22

Contributions & challenges



- A clear and simpler modeling structure;
- There is no free lunch
 Computational challenges overcame via an efficient implementation and estimation routines, the TMB;
- The data is very simple, we just know the outcome (yes or no);
- We have to be able to build the CIF curves;
- And accommodate the within-family dependence properly, that can happen in different manners;
- . . .

- Data
- 2 Modeling
- 3 Application
- 4 Model
- 6 Contributions & challenges
- **6** Template Model Builder
- Simulation stud

B Results

TMB: Template Model Builder



Quickly implement complex random effect models through simple C++ templates. The ${\tt R}$ package combines

- CppAD: C++ automatic differentiation;
- Eigen: templated matrix-vector library;
- CHOLMOD: sparse matrix routines available from R;

to obtain an efficient implementation of the applied Laplace approximation with exact derivatives.

Also, key features are

- automatic sparseness detection;
- parallelism through BLAS;
- parallel user templates.

- Data
- 2 Modeling
- 3 Application
- 4 Model
- Gontributions & challenges
- **6** Template Model Builder
- Simulation study

Results 17/22

- Data
- 2 Modeling
- 3 Application
- 4 Model
- 6 Contributions & challenges
- Template Model Builder
- Simulation stud
- 8 Results

- 1 Data
- 2 Modeling
- 3 Application
- 4 Model
- 6 Contributions & challenges
- Template Model Builder
- Simulation stud

Results 19/22

Thanks for watching and have a great day



Special thanks to



PPGMNE

Programa de Pós-Graduação em Métodos Numéricos em Engenharia





Joint work with

Wagner H. Bonat http://leg.ufpr.br/~wagner

Paulo Justiniano Ribeiro Jr. http://leg.ufpr.br/~pauloius



1 Data2 Modeling3 Application

- 6 Contributions & challenges
- Template Model Builder
- Simulation stud

B Results 21/22

References



Kalbfleisch, J. D., and R. L. Prentice. 2002. *The Statistical Analysis of Failure Time Data*. Second Edition. Hoboken, New Jersey: John Wiley & Sons, Inc.