

## CHAPTER 6 – PROBLEMS (Part 2)

**Problem 1.** Consider the following sequence of operations on an initially empty search tree:

Insert 10  
 Insert 100  
 Insert 30  
 Insert 80  
 Insert 50  
 Remove 10  
 Insert 60  
 Insert 70  
 Insert 40  
 Remove 80  
 Insert 90  
 Insert 20  
 Remove 30  
 Remove 70

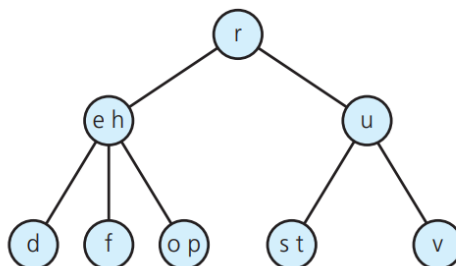
What does the tree look like after these operations execute if the tree is:

- A binary search tree?
- An AVL tree?
- A Red-black tree?
- A 2-3 tree?
- A 2-3-4 tree?

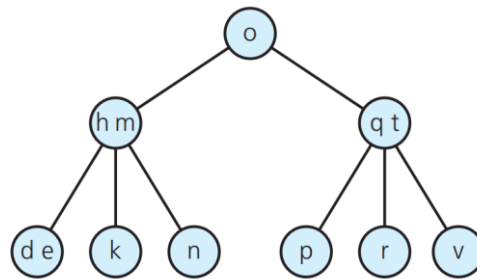
**Problem 2.** Draw a Red-Black Tree that is not an AVL tree structure. Explain your answer.

**Problem 3.** Is it possible to have all black nodes in a Red-Black tree? Give an example for your answer.

**Problem 4.** Given the following 2-3 tree. Draw the tree that results after inserting  $k$ ,  $b$ ,  $c$ ,  $y$ , and  $w$  into the tree.



**Problem 5.** Given the following 2-3 tree. Draw the tree that results after removing  $t$ ,  $e$ ,  $k$ , and  $d$  from the tree.



**Problem 6.** Draw the 2-3-4 tree that results from inserting  $o$ ,  $d$ ,  $j$ ,  $h$ ,  $s$ ,  $g$ , and  $a$ , in the order given, into a 2-3-4 tree that contains a single node whose value is  $n$ .

**Problem 7.** Show all legal B-trees of minimum degree 2 that store the keys 1, 2, 3, 4, 5.

**Problem 8.** Insert the following keys to an empty 5-way B-tree: 3, 7, 9, 23, 45, 1, 5, 14, 25, 24, 13, 11, 8, 19, 4, 31, 35, 56. Draw the result tree after each insertion.

**Problem 9.** Show the results of deleting C, P, and V, in order, from the following B-tree with  $m = 5$ :

