```
In [ ]: # imports
        from machine_learning_functions import *
In []: (X := np.array([0.5, 1.0, 10.0, -5.0, -0.1, 0.0, -1.0, -0.3, 0.6, 0.4]))
Out[]: array([ 0.5, 1., 10., -5., -0.1, 0., -1., -0.3, 0.6, 0.4])
In [ ]: sigmoid = Sigmoid()
In [ ]: | sigmoid(X)
Out[]: array([0.04843825, 0.03301454, 0.00490444, -0.01170297, 0.11024104,
               0.09090909, -0.12063188, 0.19182462, 0.04429912, 0.05343058
In [ ]: sigmoid.dX(X)
                                     , 0.
Out[]: array([[ 0.04609199, 0.
                                                                 0.
                                                     0.
                         , 0.
                                      , 0.
                                                                 0.
                                                                           ],
               [ 0.
                         , 0.03192458, 0.
                                                     0.
                                                                  0.
                          , 0. , 0.
                                                                 0.
                                                                           ],
               [ 0.
                                      , 0.00488039,
                             0.
                                                     0.
                                                                 0.
                          ,
                          , 0.
                                      , 0.
                                                               , 0.
                0.
                                                     0.
                                                                           ],
                         , 0.
                                                 , -0.01183993, 0.
               [ 0.
                                      , 0.
                          , 0.
                                      , 0.
                                                  , 0.
                                                              , 0.
                0.
                                                                           ],
                                     , 0.
                                                                 0.09808796,
               [ 0.
                            0.
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                          , 0.
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                                                              , 0.
                0.
                                     , 0.
                                                                           ],
                         , 0.
                                      , 0.
                                                 , 0.
                                                                 0.
                                      , 0.
                0.08264463, 0.
                                                  , 0.
                                                               , 0.
                                                                           ],
                                                 , 0.
               [ 0.
                        , 0.
                                        0.
                                                              , 0.
                         , -0.13518393, 0.
                                                 , 0.
                                                             , 0.
                0.
                                                   , 0.
               [ 0.
                                                               , 0.
                                      , 0.15502793,
                          , 0.
                                                              , 0.
                0.
                                                     0.
                                     , 0.
                         , 0.
                                                 , 0.
                                                              , 0.
               Γ0.
                                                 , 0.04233671, 0.
                          , 0.
                                     , 0.
                0.
                                                                           ],
                                                  , 0.
                          , 0.
                                      , 0.
               [ 0.
                                                              , 0.
                0.
                            0.
                                         0.
                                                     0.
                                                                 0.05057576]])
In [ ]: sigmoid.dX(X).shape
Out[]: (10, 10)
In [ ]: # activation = RELU()
        activation = Leaky_RELU(0.2)
In [ ]: activation(X)
\label{eq:out} {\tt Out[\ ]:\ array([\ 0.5\ ,\ 1.\ \ ,\ 10.\ \ ,\ -1.\ \ ,\ -0.02,\ 0.\ \ ,\ -0.2\ ,\ -0.06,\ 0.6\ ,}
               0.4\ ])
In [ ]: activation.vectorised derivative(X)
Out[]: array([1., 1., 1., 0.2, 0.2, 1., 0.2, 0.2, 1., 1.])
In [ ]: activation.dX(X)
```

```
Out[]: array([[1.,0.,0.,0.,0.,0.,0.,0.,0.,0.,0.,0.],
              [0., 1., 0., 0., 0., 0., 0., 0., 0., 0.],
              [ 0. \ , \ 0. \ , \ 1. \ , \ 0. \ , \ 0. \ , \ 0. \ , \ 0. \ , \ 0. \ , \ 0. \ , \ 0. \ ],
              [0.,0.,0.,0.2,0.,0.,0.,0.,0.,0.],
              [0., 0., 0., 0., 0., 1., 0., 0., 0., 0., 0.]
              [0., 0., 0., 0., 0., 0., 0.2, 0., 0., 0.]
              [0.,0.,0.,0.,0.,0.,0.,0.,0.2,0.,0.],
              [0., 0., 0., 0., 0., 0., 0., 0., 0., 1., 0.]
              Test the layer class
In [ ]: layer = Layer Transformation(4, 2, RELU())
In [ ]: layer.weights
Out[]: array([[-0.09064785, -0.79155874],
              [-0.44657293, -0.2488978],
              [-0.51476828, 0.60746217],
              [ 0.5473846 , -0.99528016]])
In [ ]: layer.bias
Out[]: array([0.5, 0.5, 0.5, 0.5])
In [ ]: layer.get_activations(
           np.array([0,0])
Out[]: array([0.5, 0.5, 0.5, 0.5])
In [ ]: layer.get_activations(
          np.array([1,1])
Out[]: array([-0.
                                    0.59269389, 0.05210445])
                       , -0.
In [ ]: layer.get_activations(
           np.array([0.34,0.81])
                       , 0.14655799, 0.81702314, -0.
Out[]: array([-0.
                                                          1)
In [ ]: layer.weighted sums
Out[]: array([-0.17198285, 0.14655799, 0.81702314, -0.12006616])
In [ ]: layer.activations
Out[]: array([-0.
                   , 0.14655799, 0.81702314, -0.
                                                          1)
In [ ]: (
           layer.dAdZ(),
           layer.dZdW(),
           layer.dZdAp()
```

```
Out[]: (array([[0., 0., 0., 0.],
                [0., 1., 0., 0.],
                [0., 0., 1., 0.],
                [0., 0., 0., 0.]]),
         array([0.34, 0.81]),
         array([[-0.09064785, -0.79155874],
                [-0.44657293, -0.2488978],
                [-0.51476828, 0.60746217],
                [ 0.5473846 , -0.99528016]]))
In [ ]: cost_func = MSE()
        cost_func(
           layer.activations,
            np.array([0, 0, 1, 0])
Out[]: 0.013739943763856552
In [ ]:
            (dAdZ := layer.dAdZ()),
            (dcdA := cost_func.dP()),
            (dcdZ := dAdZ @ dcdA)
Out[]: (array([[0., 0., 0., 0.],
                [0., 1., 0., 0.],
                [0., 0., 1., 0.],
                [0., 0., 0., 0.]]),
         array([-0. , 0.07327899, -0.09148843, -0.
                                                                ]),
                          , 0.07327899, -0.09148843, 0.
         array([ 0.
                                                                ]))
In [ ]: # here I will use outer product rather than transverses
           dcdZ,
           (dZdW := layer.dZdW()),
            (dcdW := np.outer(dcdZ, dZdW))
Out[]: (array([ 0.
                           , 0.07327899, -0.09148843, 0.
                                                                ]),
         array([0.34, 0.81]),
         array([[ 0. , 0.
                [ 0.02491486, 0.05935599],
                [-0.03110607, -0.07410563],
                       , 0.
                                   11))
In [ ]: # (
             (dZdB := layer.dZdB()),
        #
             dcdZ,
              (dcdB := dZdB @ dcdZ)
        # )
            dcdZ,
            (dcdB := dcdZ)
Out[]: (array([ 0.
                       , 0.07327899, -0.09148843, 0.
                                                                ]),
         array([ 0.
                         , 0.07327899, -0.09148843, 0.
                                                                ]))
```

```
In [ ]:
            (dZdAp := layer.dZdAp()),
            dcdZ,
            (dcdAp := dZdAp.T @ dcdZ)
Out[]: (array([[-0.09064785, -0.79155874],
                [-0.44657293, -0.2488978],
                [-0.51476828, 0.60746217],
                [0.5473846, -0.99528016]]),
         array([ 0. , 0.07327899, -0.09148843, 0.
                                                                 ]),
         array([ 0.01437093, -0.07381474]))
In [ ]: model = FFN(
            [2,4,2],
            [RELU() for _ in range(2)],
            MSE()
In [ ]: (
            model.tranformation_layers[0].weights,
            model.tranformation_layers[0].bias,
            model.tranformation_layers[1].weights,
            model.tranformation_layers[1].bias
Out[]: (array([[-0.55816015, 0.2858176],
                [-0.21456866, -0.57383174],
                [-0.43776862, -0.84339484],
                [ 0.80917179, 0.88996469]]),
         array([0.5, 0.5, 0.5, 0.5]),
         array([[-0.35003769, 0.9576626, -0.8890226, 0.16348804],
                [-0.20132945, 0.35412975, 0.50686099, 0.80956816]]),
         array([0.5, 0.5]))
In [ ]: model.foreward propagate(
           np.array([0, 0]),
            np.array([1, 1])
Out[]: (array([0.44104518, 1.23461473]), 0.18373728297811864)
In [ ]: model.back_propogate(
            np.array([0, 0]),
            np.array([1, 1])
Out[]: {'W2': array([[-0.27947741, -0.27947741, -0.27947741],
                [0.11730736, 0.11730736, 0.11730736, 0.11730736]]),
         'B2': array([-0.55895482, 0.23461473]),
         'W1': array([[ 0., 0.],
                [-0., -0.],
                [ 0., 0.],
                [ 0., 0.]]),
         'B1': array([ 0.1484204 , -0.45220608, 0.61584053, 0.09855418])}
In [ ]: from random import uniform
```

```
In [ ]: # # create random function to learn
        \# degree = 1
        # coefficients = [uniform(-1, 1) for _ in range(degree+1)]
        # def polynomial_function(x):
              return sum(coefficients[i] * x**i for i in range(degree+1))
        def linear function(x): return 2*x+5
In [ ]: num_data_items = 1000
        X_data = [uniform(-100, 100) for _ in range(num_data_items)]
        Y_data = [linear_function(X_data[i]) for i in range(num_data_items)]
        X_data, Y_data = np.array(X_data), np.array(Y_data)
In [ ]: function_emulator_model = FFN(
            [1, 1],
            [Linear_Activation_Funcion()],
            MSE()
In [ ]:
            function_emulator_model.tranformation_layers[0].weights,
            function_emulator_model.tranformation_layers[0].bias,
Out[]: (array([[0.51662746]]), array([0.5]))
In [ ]: # function_emulator_model.transformation_layers[0].weights = np.array([[2.0]])
        # function_emulator_model.transformation_layers[0].bias = np.array([5.0])
In [ ]:
        # function_emulator_model.transformation_layers[0].weights = np.array([[1.2]])
        # function emulator model.transformation layers[0].bias = np.array([3.0])
        function_emulator_model.foreward_propagate(2, 2*2+5)
In [ ]:
Out[]: (array([1.53325493]), 55.75228194202673)
In [ ]:
        function_emulator_model.back_propogate(2, 2*2+5)
Out[]: {'W1': array([[-29.86698028]]), 'B1': array([-14.93349014])}
In [ ]:
        function_emulator_model.foreward_propagate(-3, (-3)*2+5)
        (array([-1.04988239]), 0.0024882533143272354)
Out[]:
In [ ]: function_emulator_model.back_propagate(-3, (-3)*2+5)
Out[]: {'W1': array([[0.29929437]]), 'B1': array([-0.09976479])}
In [ ]: training_manager = Model(
            FFN=function_emulator_model,
            data_set=(X_data, Y_data)
```

```
In [ ]: training_manager.train_and_evaluate(
            learning_rate=0.0001,
            epochs=10,
            batch_size=50
Out[]: 14.35824670325447
In [ ]: (
            function_emulator_model.tranformation_layers[0].weights,
            function emulator model.tranformation layers[0].bias,
Out[]: (array([[1.99942258]]), array([1.21192484]))
In [ ]: for _ in range(10):
            x = uniform(-1, 1)
            y = linear_function(x)
            p, c = training_manager.FFN.foreward_propagate(
                np.array([x,]), np.array([y,])
            print(f"For the input \{x:.4f\} the network predicted \{p[0]:.4f\} and actual va
       For the input 0.8926 the network predicted 2.9967 and actual value was 6.7853 giv
       ing a cost of 14.3534
       For the input -0.8759 the network predicted -0.5393 and actual value was 3.2482 g
       iving a cost of 14.3457
       For the input -0.0286 the network predicted 1.1548 and actual value was 4.9428 gi
       ving a cost of 14.3494
       For the input -0.8426 the network predicted -0.4728 and actual value was 3.3147 g
       iving a cost of 14.3458
       For the input 0.8849 the network predicted 2.9812 and actual value was 6.7698 giv
       ing a cost of 14.3534
       For the input -0.6873 the network predicted -0.1622 and actual value was 3.6255 g
       iving a cost of 14.3465
       For the input 0.1227 the network predicted 1.4573 and actual value was 5.2455 giv
       ing a cost of 14.3501
       For the input 0.0584 the network predicted 1.3287 and actual value was 5.1168 giv
       ing a cost of 14.3498
       For the input 0.0623 the network predicted 1.3364 and actual value was 5.1245 giv
       ing a cost of 14.3498
       For the input -0.9207 the network predicted -0.6290 and actual value was 3.1585 g
       iving a cost of 14.3455
In [ ]: # create random function to learn
        degree = 1
        coefficients = [uniform(-1, 1) for _ in range(degree+1)]
        def polynomial function(x):
            return sum(coefficients[i] * x**i for i in range(degree+1))
In [ ]: coefficients
Out[]: [0.35074834378407993, -0.6476307797195384]
In [ ]: | num_data_items = 10000
        X_data = [uniform(-100, 100) for _ in range(num_data_items)]
        Y_data = [linear_function(X_data[i]) for i in range(num_data_items)]
```

```
X_data, Y_data = np.array(X_data), np.array(Y_data)
In [ ]: function_emulator_model = FFN(
            [1, 1, 1],
            [Leaky_RELU(0.01), Linear_Activation_Funcion()],
        )
        # function_emulator_model = FFN(
              [1, 1],
              [Linear_Activation_Funcion()],
        #
              MSE()
        # )
In [ ]:
            function_emulator_model.tranformation_layers[0].weights,
            function_emulator_model.tranformation_layers[0].bias,
Out[]: (array([[-0.33452972]]), array([0.5]))
In [ ]: training_manager = Model(
            FFN=function_emulator_model,
            data_set=(X_data, Y_data)
In [ ]: training_manager.train_and_evaluate(
            learning_rate=0.0001,
            epochs=10,
            batch_size=50
Out[]: 2849.3752604979236
In [ ]: (
            function emulator model.tranformation layers[0].weights,
            function emulator model.tranformation layers[0].bias,
            function_emulator_model.tranformation_layers[1].weights,
            function_emulator_model.tranformation_layers[1].bias,
Out[]: (array([[1.29304125]]),
          array([11.45175091]),
          array([[2.14321746]]),
          array([-51.47822236]))
In [ ]: for _ in range(10):
            x = uniform(-1, 1)
            y = linear_function(x)
            p, c = training manager.FFN.foreward propagate(
                 np.array([x,]), np.array([y,])
            print(f"For the input \{x:.4f\} the network predicted \{p[\emptyset]:.4f\} and actual va
```

For the input -0.8135 the network predicted -29.1891 and actual value was 3.3730 giving a cost of 1060.2882

For the input -0.7973 the network predicted -29.1441 and actual value was 3.4054 giving a cost of 1059.4733

For the input -0.1669 the network predicted -27.3971 and actual value was 4.6663 giving a cost of 1028.0572

For the input 0.2831 the network predicted -26.1502 and actual value was $5.5661~\mathrm{g}$ iving a cost of 1005.9251

For the input 0.7605 the network predicted -24.8272 and actual value was 6.5209 g iving a cost of 982.7036

For the input -0.5839 the network predicted -28.5528 and actual value was 3.8322 giving a cost of 1048.7863

For the input -0.4445 the network predicted -28.1665 and actual value was 4.1110 giving a cost of 1041.8343

For the input -0.1829 the network predicted -27.4416 and actual value was 4.6341 giving a cost of 1028.8516

For the input 0.9026 the network predicted -24.4332 and actual value was 6.8053 g iving a cost of 975.8413

For the input 0.2418 the network predicted -26.2646 and actual value was 5.4835 g iving a cost of 1007.9462

In []: