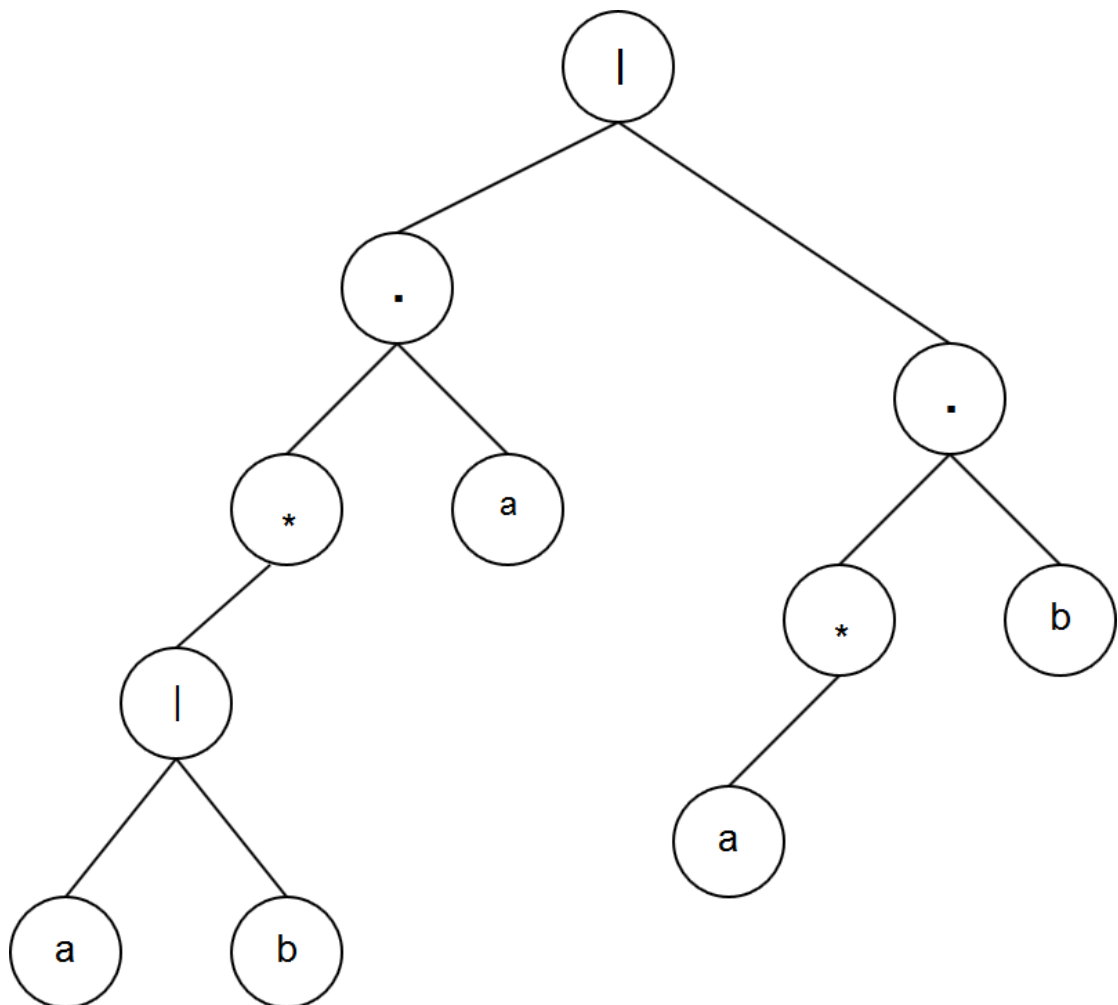


## Assignment 3

### Automatic Conversion from Regular Expressions to Finite Automata

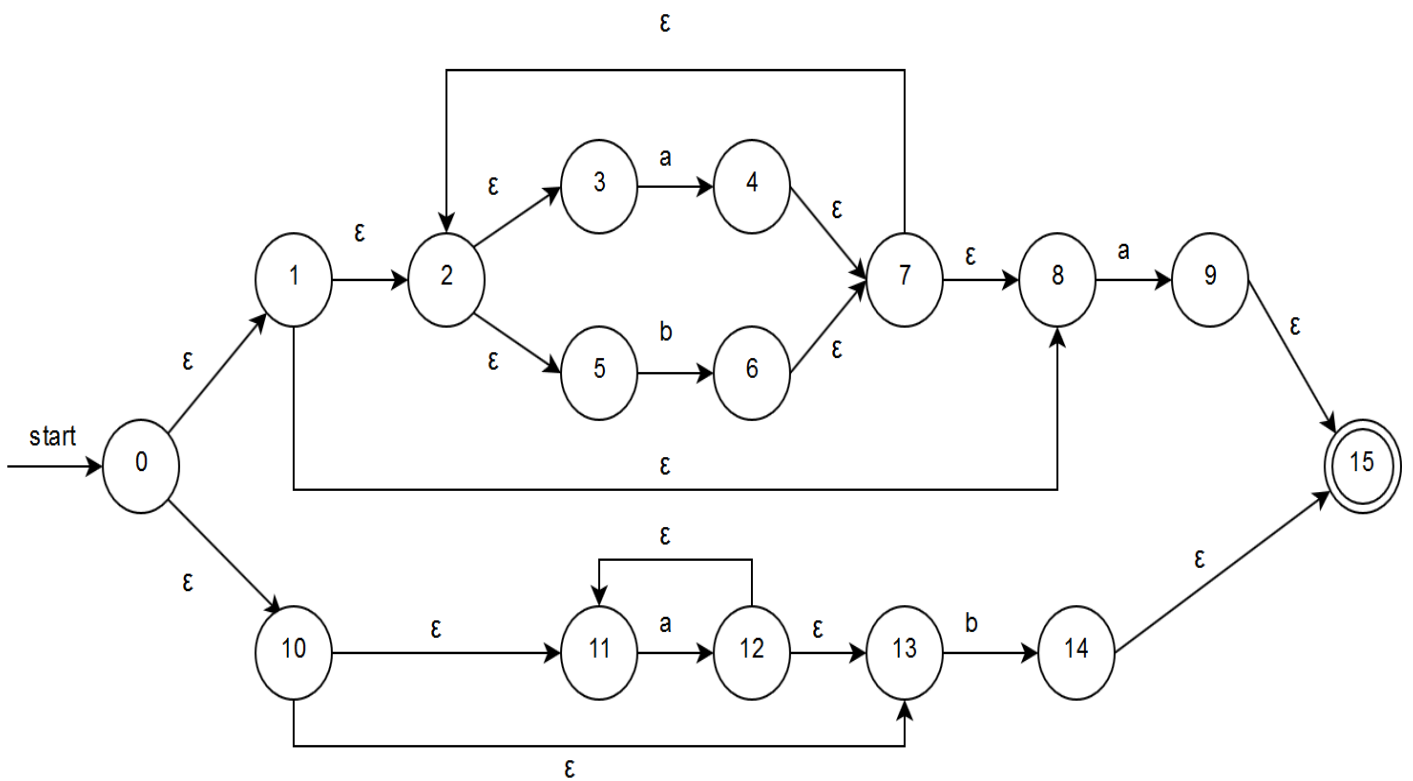
1.

(10%) Construct the expression tree for the following regular expression  $(a \mid b)^* a \mid a^* b$



2.

(40%) Construct a nondeterministic finite automaton (NFA) for the regular expression using the Thompson's construction algorithm



3.

(50%) Convert the NFA into a deterministic finite automaton (DFA) using the subset construction algorithm

$$\varepsilon\text{-closure}(\{0\}) = \{0,1,2,3,5,8,10,11,13\} = \mathbf{A}$$

$$\begin{aligned}\varepsilon\text{-closure}(\text{move}(\mathbf{A}, a)) &= \varepsilon\text{-closure}(\{4,9,12\}) \\ &= \{2,3,4,5,7,8,9,11,12,13,15\} = \mathbf{B}\end{aligned}$$

$$\varepsilon\text{-closure}(\text{move}(\mathbf{A}, b)) = \varepsilon\text{-closure}(\{6,14\}) = \{2,3,5,6,7,8,14,15\} = \mathbf{C}$$

$$\varepsilon\text{-closure}(\text{move}(\mathbf{B}, a)) = \varepsilon\text{-closure}(\{4,9,12\}) = \mathbf{B}$$

$$\varepsilon\text{-closure}(\text{move}(\mathbf{B}, b)) = \varepsilon\text{-closure}(\{6,14\}) = \mathbf{C}$$

$$\varepsilon\text{-closure}(\text{move}(\mathbf{C}, a)) = \varepsilon\text{-closure}(\{4,9\}) = \{2,3,4,5,7,8,9,15\} = \mathbf{D}$$

$$\varepsilon\text{-closure}(\text{move}(\mathbf{C}, b)) = \varepsilon\text{-closure}(\{6\}) = \{2,3,5,6,7,8\} = \mathbf{E}$$

$$\varepsilon\text{-closure}(\text{move}(\mathbf{D}, a)) = \varepsilon\text{-closure}(\{4,9\}) = \mathbf{D}$$

$$\varepsilon\text{-closure}(\text{move}(\mathbf{D}, b)) = \varepsilon\text{-closure}(\{6\}) = \mathbf{E}$$

$$\varepsilon\text{-closure}(\text{move}(\mathbf{E}, a)) = \varepsilon\text{-closure}(\{4,9\}) = \mathbf{D}$$

$$\varepsilon\text{-closure}(\text{move}(\mathbf{E}, b)) = \varepsilon\text{-closure}(\{6\}) = \mathbf{E}$$

State	Input Symbol	
	a	b
A = {0,1,2,3,5,8,10,11,13}	B	C
B = {2,3,4,5,7,8,9,12,13,15}	B	C
C = {2,3,5,6,7,8,14,15}	D	E
D = {2,3,4,5,7,8,9,15}	D	E
E = {2,3,5,6,7,8}	D	E

