

Reconstructing External Force on the Circumferential Body of Continuum Robot with Embedded Proprioceptive Sensors

Qingxiang Zhao, Jiewen Lai, Henry K. Chu, *Member IEEE*

Abstract—The compliance of continuum robot poses difficulty in designing the controller, as the robot does not have position encoder and could be subject to uncertain external force (UEF). The former can be resolved through external sensors, while the latter issue still needs further investigation. This work presents a novel robot design that embeds eGaN sensors into the soft material, and the elongation in the robot chamber can lead to different changes in resistance values. The sensors act as a proprioceptive mechanism to sense the presence of the UEF. To locate the UEF, the robot surface is divided into multiple regions, and the column and row positions with the force can be solved using Hidden Markov Model and regularization algorithm. Through the virtual work principle, the force magnitude can be also evaluated. Experimental results confirm that, with possible four columns and five rows, the accuracy of finding the actual column and row positions are respectively 97% and 98.5%. The mean error in evaluating the tip position and the force magnitude is about 4mm and 0.23N. This work offers a new approach to obtain the information of the UEF, allowing continuum robots to work in a constrained environment.

Index Terms—Continuum robot; External force reconstruction; Embedded flexible sensors; Hidden Markov Model; Regularization; Virtual work principle

I. INTRODUCTION

The emergence of continuum robot has endowed robotics with a novel research branch. Some obvious merits, such as hyper redundancy, high compliance, and cost effectiveness over rigid robot arms, make it widely applied in surgery [1], [2], search and rescue [3], [4], and pick-place tasks [5]. Research on continuum robots in recent decades includes versatile actuation mechanisms [6], [7], advanced sensors, mechanical design and control models [5]. However, continuum robot also comes with challenges. Specifically, it is difficult to pinpoint the location and estimate the magnitude of an external force (EF) acting on a continuum robot in a constrained environment. The lack of information about the uncertain external force (UEF) can cause different degrees of changes on the shape of a soft manipulator, posing difficulty to design a proper control scheme for the robot.

Finding the location of the force can help users (e.g. surgeons) to better interact with the ambient environment,

Corresponding author: Henry K. Chu, phone: 2766-6662.

Qingxiang Zhao, Jiewen Lai and Henry K. Chu are with the Department of Mechanical Engineering, Hong Kong Polytechnic University, Hong Kong, China (email: qingxiang.zhao@connect.polyu.hk; jw.lai@connect.polyu.hk; henry.chu@polyu.edu.hk).

and adjust the actuation inputs accordingly to compensate the load effect. To this end, sensors are indispensable. Externally located camera [8] is a good option to directly monitor the robot as well as the surrounding obstacles, but occlusion could be a problem in some scenarios. Therefore, research towards proprioceptive sensing has been developed. Examples of existing works include employing Fiber Bragg Grating (FBG) [9], Electromagnetic (EM) [10], Hall effect [11], stretchable optical waveguides [12], and color-related sensors [13] to achieve shape sensing and force sensing for soft robots, where the signal outputs correspond to the change in the robot shape. Similarly, there are some limitations in these sensing mechanisms. For example, FBG is not cost-friendly and has limited bending flexibility. EM and Hall-effect sensors are sensitive to the surrounding magnetic field presented in the environment. Optical waveguides and color sensors need complicated fabrication procedures for sensor integration and are not feasible for small-sized robots. Recently, intrinsic properties of the robot have also been used for self-sensing. The shape of a dielectric actuated elastomer [14] is related to its capacitance values, and measuring the voltage and the current value can help to derive external force from the change in the shape accordingly. The signals provided to the pneumatic chamber is another useful information, acoustic or pressure signal can be collected to estimate the robot shape [15], [16]. While the overall shape is known, the effect from the external force is hard to be evaluated separately from the actuation inputs. In recent decades, the development of flexible electronics paves a way of compact and soft internal sensors for soft robots. Flexible and conductive materials, like eGaN (eutectic gallium indium, a liquid alloy) [17], [18] and ionic solution [19], can be integrated into soft non-conductive silicone to form compliant skin sensors, which are employed to sense the stress in Minimally Invasive Surgery (MIS) [20], strain [21], and shape [22] for robots.

In addition to sensors, establishing a proper model of the continuum robot is also essential for control and force estimation. Piecewise constant curvature (PCC) approximation [23] regards the shape of a single continuum robot as an arch, which is determined by the length of each actuation chamber, but the direction angle and the bending angle of the PCC model are jointly affected by actuators and the external forces. The other stream of modelling is to assume a flexible manipulator as an Euler-Bernoulli beam [24] or a Kirchhoff elastic rod [4]. Therefore, the kinematics can be obtained by solving the displacement of robot's backbone with all the acting forces,

but an UEF can act at any position and any direction. In the velocity domain, Jacobian matrix maps between the velocities of actuators and the end effector [25], so that in a short interval, the position change of the tip can be solved using the change of actuation configuration. Analytical models are problematic in an unstructured environment due to the uncertainty of the UEF. Thus, models considering the environmental information are likely to achieve higher precision so that machine learning [26] and fuzzy control models [27] were investigated. Building machine learning models is time-consuming and the environmental information in model training is often static, which is not consistent with dynamic UEF, and fuzzy control methods aim to bring the robot tip to a desired position which may not be attainable in some applications. Thereby, accurately estimating the UEF faced by soft robots not only benefits handlers but also contributes to building better control schemes. For instance, in [14], a feedback control scheme was proposed based on the estimated force. The shape of an elastomer was modelled by the actuation force and the external force, so that the system can intelligently avoid obstacles and adjust the controller outputs. In [28], contact detection was realized along a pneumatic-driven flexible manipulator. Similar to kinematics, estimating the UEF can be an inverse process when the manipulator is assumed as a Cosserat Rod [29], where the actuation configuration and the robot shape were both known. Nevertheless, existing works only considered the force applied at the tip, or sense the deformation type of the robot caused by an EF [30]. The essential difficulty of estimating the UEF has twofold: 1) UEF can fall into any position along the manipulator, and 2) the direction of the UEF at an action point has three components (x, y, z), thus, its magnitude varies irregularly. To find the location of the force acting arbitrarily on the body, *Qiao et al.* [31] and *Venkiteswaran et al.* [32] combined FBG signals with Cosserat model and Pseudo Rigid Body model, respectively, to solve the position information. However, these approaches are computationally intensive. Alternatively, an array of force sensors can be wrapped along the surface of the continuum robot. This method, however, requires many sensors in order to cover the entire surface. The prevalence of Deep Learning provides a novel method [33]; for example, in [34], [35], a *Deep-Table* frame and RNN model were respectively applied to estimate loads of a robot arm and to estimate hard inclusions of soft tissue. Most of existing works just focused on some specific small areas of the elastomer in estimating the UEF, or only the posture of the soft robot [36], and the motion of the robot is only two-dimension [37].

In contrast, this work aims to find the external force acting on the circumferential body of a soft manipulator, including the acting position and the magnitude. That is a relatively bigger area and the information of the estimated EF is more complete. The contribution includes:

- 1) A model-free approach is proposed to determine the presence of an EF using the signals from embedded soft sensors.
- 2) The surface of the robot is considered as a 2D map with multiple grids, and a probability approach is used to find the likelihood of the column position. After this, the row position and the corresponding magnitude are estimated by virtual work

principle.

The rest of this work is organized as follows. Section II described how we fabricated an eGaIn sensor and integrated it into the soft robot arm. In Section III, we detailed the methodology to estimate a single external force. Experiments were conducted to validate the proposed method, as detailed in Section IV. Finally, Section V concluded this work.

II. SYSTEM SETUP AND CONFIGURATION

Silicone molding technology was employed to fabricate a soft manipulator, and the fabrication procedures are illustrated in Fig. 1 (a). Silicone rubber (E605, Hong Yejie, Shenzhen, China) was poured into a 3D-printed mold (Fig. 1 (a)-(I)) to form the inner component of the manipulator, which was then wrapped by a Nylon thread to limit the radial expansion once the chambers are pressurized. Two helical grooves were designed in the mold, preventing the wrapped threads from slipping during the operation (Fig. 1 (a)-(II)). Next, the inner component was secured by two disks at the two ends, and three insulated thin silicone tubes (OD:1mm, ID:0.5mm), which serve as the channels for eGaIn, were connected to the two disks (Fig. 1 (a)-(III)). Then, the entire component was placed into another mold to form the outer layer (Fig. 1 (a)-(IV)). After demolding, an outer layer surface consisting of twenty concave faces (4 columns and 5 rows) along the manipulator were obtained. Then, eGaIn was injected into the three thin tubes (Fig. 1 (a)-(V)), where the elongation of the tube will simultaneously decrease its cross-sectional area, such that the electronic-resistance change of eGaIn sensors ($R = \rho \frac{L}{S}$) can reflect the deformation of the manipulator. The three sensors are connected in series and a constant current power source of 1A is then supplied, as Fig. 1 (c) shows. The voltage difference across each sensor is measured via an oscilloscope (Tektronik TBS 1064), which converts the resistance change into voltage signal. Finally, three supporting steel bars (marked in blue in Fig. 1 (a)) that are located 120° apart were removed, providing the space as the chambers for actuation. Two rings were then glued at the two ends, allowing a marker to be placed at the top for tip position evaluation and mounting at the bottom (Fig. 1 (a)-(V)). The region that an UEF is likely to present along the circumferential body can be indexed by the column and the row numbers radially. A schematic view of the circumferential surface is shown in Fig. 1 (d)-(right), and the problem lies in accurately finding the two positions to pinpoint the external force and then to estimate its magnitude, with an assumption that the UEF is always pointing towards the backbone of the manipulator.

To actuate this soft manipulator, the three chambers were connected to three pneumatic pressure regulators (ITV-0030, SMC), and the pressurized air can be controlled with an accuracy of 0.01 bar. The manipulator was mounted vertically in an aluminium frame, and a calibrated RGB-D camera (Realsense D415, Intel) was set up at the top of the frame to sample the true position at the tip, as illustrated in Fig. 1 (b). A single-axis force sensor (ZNLBS-VII, Zhongnuochuanli, Bengbu, Anhui, China, range: $[-5, 5]N$) was placed next to the manipulator, providing the true external force magnitude for

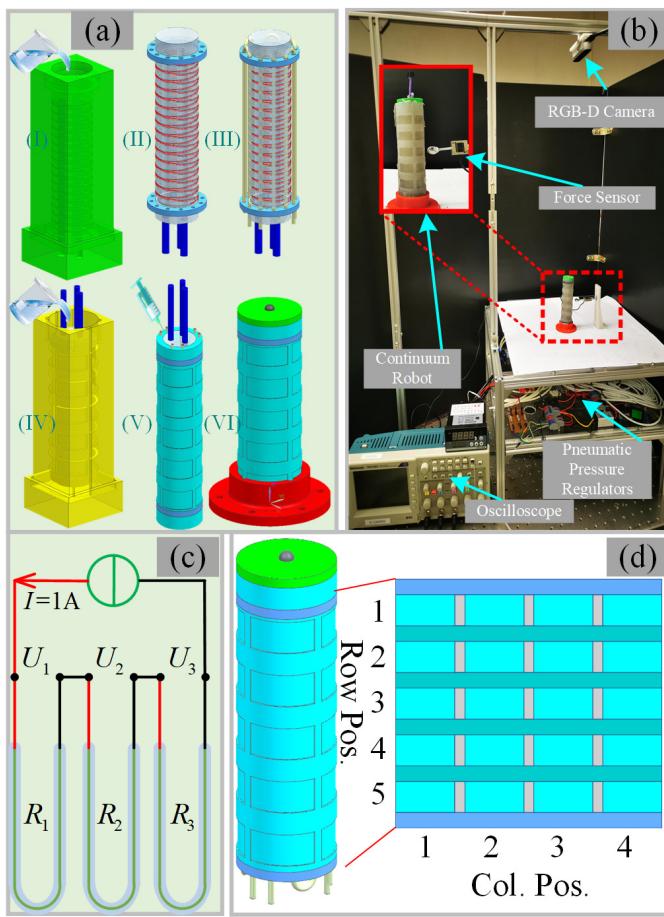


Fig. 1. (a) Fabrication of the manipulator. (b) System setup. (c) Circuit of electronic resistance measurement. (d) Schematic view of the circumferential view of the soft manipulator.

validation. A control interface was developed using MATLAB 2019.

III. UEF LOCALIZATION AND MAGNITUDE ESTIMATION

The tip position is the combined result from the actuation inputs and the external force, as shown in Fig. 2 (a), where the shape of the manipulator at step k can be deemed as an arch defined by three parameters: the direction angle ψ_k , the bending angle θ_k and the bending radius R_k . All of them can be solved using (A1) (equation in Appendix) if the tip position $P_k(x_k, y_k, z_k)$ can be obtained. Since the three eGaN sensors are mounted adjacent to the three chambers respectively, the sensor readings directly correlate with the chamber length, so that the real-time tip position both in load-free and load conditions can be computed based on the sensor readings S_k . Namely, the true tip position P_k can be mapped via S_k .

In load-free condition, the tip position can be regarded as solely depending on actuation inputs A_k , which means that tip position $P_k|_{free}$ can be solved just using A_k . In contrast, as Fig. 2 (b) shows, an external force $F_{e,k}$ causes the true tip position P_k to deviate from the theoretical load-free value $P_k|_{free}$. When the external load is present, the position deviation $\Delta P_k = P_k - P_k|_{free}$ in the tip position is large due

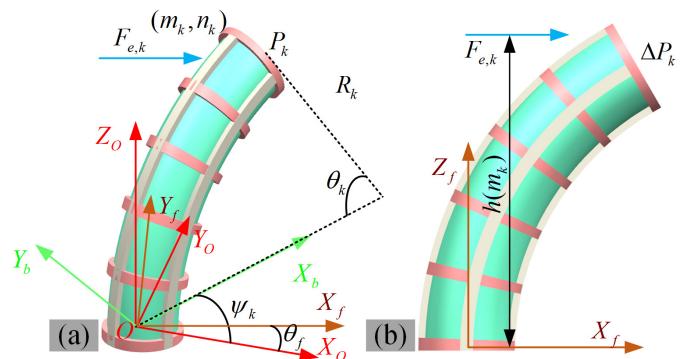


Fig. 2. Illustration of deformed flexible arm. (a) Coordinate frames. (b) Tip position in $X_f O Z_f$ only due to an external force.

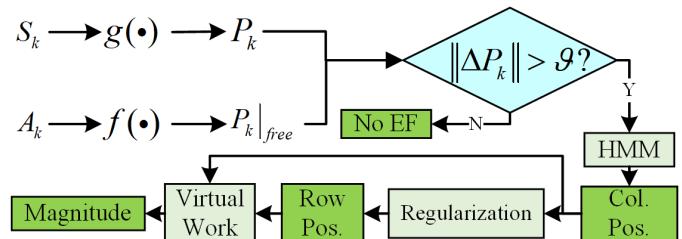


Fig. 3. Flowchart of external force estimation.

to $F_{e,k}$. Therefore, by knowing the current actuation inputs A_k , the deviation can imply whether or not $F_{e,k}$ is present.

The evaluation method consists of three parts. First, the models to find $P_k|_{free}$ and P_k are constructed using Neural Network. Then, the column position of an UEF is estimated with HMM. Finally, the row position and the magnitude are calculated using the principle of virtual work. The overall framework is illustrated in Fig. 3.

A. Tip position prediction

Sensor readings are highly and directly related to the shape and the tip position, such that a mapping $g(\cdot)$ between P_k and S_k : $P_k(x_k, y_k, z_k) = g(S_k)$ can be built to form a proprioceptive sensing mechanism, both in load and load-free conditions. Fabrication imperfection and uncertainty of the EF increase the difficulty to find an analytical mapping, so using data-driven method to build Neural Network model provides a feasible alternative. Similarly, $P_k|_{free}$ is also solved, which is $P_k|_{free} = f(A_k)$. Since the input data and the position data do not vary significantly over time, an embedded dimension d is considered to estimate the position using last d records of data, and the two mappings are updated as:

$$\begin{cases} P_k|_{free} = f(A_{k-d:k}) \\ P_k(x_k, y_k, z_k) = g(S_{k-d:k}) \end{cases} \quad (1)$$

Two Multilayer Perceptron (MLP) Neural Networks are respectively constructed to find $f(\cdot)$ and $g(\cdot)$. We set the embedded dimension $d = 5$. The output layer and input layer of the two models has 3 and 15 nodes, respectively, and the activation functions in hidden layer and output layer

are 'Sigmoid' ($y = \frac{1}{1+e^{-x}}$) and 'ReLU' ($y = \max(0, x)$), respectively. A threshold ϑ is set to account for model error. Through comparing between ΔP_k and ϑ , UEF is detected as:

$$\begin{cases} \text{UEF} & \|\Delta P_k\| \geq \vartheta \\ \text{Load Free} & \text{else} \end{cases} \quad (2)$$

B. Column position estimation towards UEF via HMM

After identifying the existence of an UEF, its position can be estimated based on the tip position deviation ΔP_k . As Fig. 2 (b) and Fig. 1 (d) illustrate, there are 20 regions where an UEF is likely to present, one of which is denoted by (m, n) ($m \in [1, 5], n \in [1, 4]$ are row position and column position, respectively). We firstly solve n_k because it is involved in the deviation direction of the tip, and the row position m_k as well as the magnitude affects deviation degree (i.e. bending angle). In the robot system, only A_k , ΔP_k , and S_k are known, which refers to observation data, and the column position n_k is hidden. Because of the uncertainty of the EF and slow motion of the robot, the state is only mapped with the current observation data. This satisfies the property of HMM, inspiring us to estimate the hidden state n_k by it. The observation sequence $O = (o_1, \dots, o_k)$ and a well learned HMM λ are employed to find the column position:

$$\hat{n}_k = \arg \max_{1 \leq i \leq 5} \Pr(n_k = i | \lambda, O) \quad (3)$$

where $\hat{n}_k = 5$ means no UEF, and the observation data o_k depends on the actuation inputs and the position deviation: $o_k^{1 \times 6} = \{A_k^{1 \times 3}, \Delta P_k^{1 \times 3}\}$. To reduce the unit discrepancy, the actuation inputs are normalized with $[0, 1]$ and further expressed as:

$$o_k(l) = \begin{cases} -1 & A_k(l) \in [0.0, 0.33] \\ 0 & A_k(l) \in [0.34, 0.66] \\ 1 & A_k(l) \in [0.67, 1] \end{cases} \quad (4)$$

$$o_k(l) = \begin{cases} 0 & \|\Delta P_k(l-3)\| \leq \xi \\ \text{sgn}(\Delta P_k(l-3)) & \text{else} \end{cases}$$

where $\xi = 3$ mm is a threshold considering the measurement error. The hidden state of our HMM is the column position n_k and the state transition probability between two continuous steps i and j is: $a_{ij} = \Pr(n_{k+1} = j | n_k = i)$. In addition, the emission probability is defined as: $b_j(o_k) = \Pr(o_k | n_k = j)$. As a result, there are possibly in total $N = 3^6$ different observation data, which is difficult to manifest their corresponding emission probability. This issue was previously tackled by multivariate Gaussian distribution [38], requiring a large amount of data to find the mean value and variance. Therefore, K-means algorithm is employed to reduce the dimension of the observation data, and the observation data is classified into one hundred categories (input one observation data with 6 dimensions to get one dimension). The observation data o_k is updated to v_k : $v_k^{1 \times 1} \leftarrow K\text{means}(o_k^{1 \times 6})$, and the observation sequence O is: $\{v_1, \dots, v_k\}$.

Initially, the state transition probability is assumed as an uniform distribution, so that the initial probability for each

hidden state is $\pi_i = \frac{1}{5}$. Now, this HMM is defined as: $\lambda = \{\pi, a_{ij}, b_j(v_k)\}$. With Bayesian's rule, (3) is updated to:

$$\hat{n}_k = \arg \max_{1 \leq i \leq 5} \frac{\Pr(n_k = i, O | \lambda)}{\Pr(O | \lambda)} \quad (5)$$

In order to calculate $\Pr(O | \lambda)$, forward and backward probability are defined as:

$$\begin{aligned} \alpha_k(i) &= \Pr(v_1, \dots, v_k, n_k = i | \lambda) \\ \beta_k(i) &= \Pr(v_k, \dots, v_T | n_k = i, \lambda) \end{aligned} \quad (6)$$

so $\Pr(O | \lambda)$ can be further calculated by:

$$\Pr(O | \lambda) = \sum_{i=1}^5 \sum_{j=1}^5 \alpha_k(i) a_{ij} b_j(v_{t+1}) \beta_{t+1}(j) \quad (7)$$

Let $\gamma_k(i)$ denotes the probability of hidden state i with knowing λ and O at step k , and $\xi_k(i, j)$ represents the probability of hidden state j at step $(k+1)$ if the hidden state is i at step k , both of which are then denoted as:

$$\begin{aligned} \gamma_k(i) &= \Pr(n_k = i | O, \lambda) = \frac{\alpha_k(i) \beta_k(j)}{\sum_{j=1}^5 \alpha_k(i) \beta_k(j)} \\ \xi_k(i, j) &= \Pr(n_k = i, n_{k+1} = j | O, \lambda) \\ &= \frac{\alpha_k(i) a_{ij} b_j(o_{k+1}) \beta_{k+1}(j)}{\sum_{i=1}^5 \sum_{j=1}^5 \alpha_k(i) a_{ij} b_j(o_{k+1}) \beta_{k+1}(j)} \end{aligned} \quad (8)$$

To obtain a well-learned HMM model, T sets of data including the observation data and the column position are collected, and the Baum-Welch algorithm is employed. Finally, the parameters of λ are learned via:

$$a_{ij}^{n+1} = \frac{\sum_{k=1}^{T-1} \xi_k(i, j)}{\sum_{k=1}^{T-1} \gamma_k(i, j)}, b_j(k)^{n+1} = \frac{\sum_{k=1, o_k=v_k}^T \gamma_k(j)}{\sum_{k=1}^T \gamma_k(j)} \quad (9)$$

The initial probability is $\pi_i^{n+1} = \gamma_1(j)$. After iterations, we can get: $\lambda^{(n+1)} = \{\pi^{(n+1)}, a_{ij}^{(n+1)}, b_j^{(n+1)}(n_k)\}$, so the estimated column position at step k is:

$$\hat{n}_k = \arg \max_{1 \leq i \leq 5} [\gamma_k(i)] \quad (10)$$

C. Row position and magnitude estimation

After estimating the column position of a single EF ($\hat{n}_k \neq 5$), the algorithm still needs to find the row position m_k , which is related to the moment that the robot is experiencing. The robot can reach a static equilibrium with a tip position after all the acting forces are in balance, and the equilibrium can be established by virtual work principle as:

$$\delta W = \delta W_g + \delta W_{el} + \delta W_{ac} + \delta W_e = 0 \quad (11)$$

where δW_g , δW_{el} , δW_{ac} and δW_e respectively denote the virtual work of gravity, elastic force from the robot itself, the actuators, and the external force. The centroid C_k locates at the center of the robot backbone, as calculated using (A3) in Appendix, so $\delta W_g = G \cdot \delta C_k(3)$. The length of each chamber is solved using (A2) and the elongation of each chamber is: $\Delta l_{k,i} = l_{k,i} - l$. Therefore, δW_{el} can

be calculated by: $\delta W_{el} = \sum_{i=1}^3 \frac{1}{3} EI \Delta l_{k,i}^2$, where E is the Young's Modulus and I is the inertial moment. Similarly, the virtual work of the actuators is the accumulation of the three chambers: $\delta W_{ac} = \sum_{i=1}^3 A_k(i) \pi r_c^2 \Delta l_{k,i}$ (r_c is the radius of the chamber). All virtual work can be expressed as functions in term of bending angle θ_k . The external force can be present in any position of the 20 areas, so $\delta W_e = F_e \delta_e$, where δ_e is involved in $\delta \theta_k$ and the row position m_k . Although all of them can be solved, (11) includes both the magnitude and the row position of an external force. It would be difficult to evaluate them simultaneously. Considering that the tip position deviation is purely caused by the external force, we can use ΔP_k to establish another mapping: $\Delta P_k \leftarrow (F_{e,k}, m_k)$.

The flexible manipulator is assumed as a system and the tip position P_k reflects its system response influenced by the external force and the actuation inputs, which is expressed as:

$$P_k = H(A_k)A_k + H_e(m_k)F_{e,k} + Q \quad (12)$$

where $H(A_k) \in R^{3 \times 3}$ is a system matrix relating between the tip position (system response) and the actuator inputs (i.e. $f(\cdot)$), and $H_e(m_k)$ is a matrix involved in the position of the external force $F_{e,k}$. The tip position change caused by an UEF at a certain row position, namely $H_e(m_k)F_{e,k}$, is calculated using (A4). Since we have found the column position in the previous section, only m_k and $F_{e,k}$ are unknown in this equation. Q is the Gaussian white noise indicating the systematic error. $H(A_k)A_k$ denotes the pure systematic response from the actuators, so (12) is updated as:

$$\Delta P_k = H_e(m_k)F_{e,k} + Q \quad (13)$$

ΔP_k is the pure systematic response due to $F_{e,k}$. Therefore, the row position of $F_{e,k}$ can be solved by:

$$\hat{m}_k = \arg \min_{m_k} \|\Delta P_k - H_e(m_k)F_{e,k}\|_2^2 \quad (14)$$

However, finding the optimal solution is not easy with many local minima. Since the equation may not yield to the global minima due to the noise and local minima, a regularization factor is also added to the equation to ensure convergence:

$$\arg \min_{m_k} (\sqrt{\|\Delta P_k - H_e(m_k)F_{e,k}\|_2^2} + \chi \sqrt{\|F_{e,k}\|_2^2}) \quad (15)$$

where χ is a regularization parameter. After finding the row position m_k , the magnitude of the external force can be accordingly solved via (13). However, the value of χ is really important for the results, and setting a proper χ requires delicate calculation. We employ gradient descent algorithm to set different values of χ to address the issue. In virtual work principle, the ideal value of δW is close to zero, but an improper χ may lead to a large error in $\delta W(\chi)$. As a result, an iteration process was employed to update χ such that $\delta W(\chi)$ can converge to an value within an user-defined threshold ς : $\tilde{\chi} = \chi - \eta \delta W(\chi)$, where η is the learning rate. When the algorithm finds the most possible position of the external force with different χ , the magnitude can also be calculated via (13).

IV. EXPERIMENTAL VALIDATION

Experiments were conducted to test the performance of the sensors and each module of the algorithm.

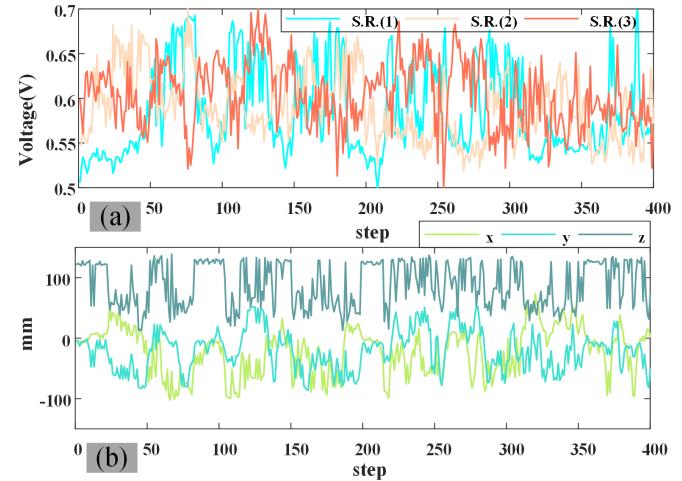


Fig. 4. Fundamental test about the experimental setup. (a) Sensor readings. (b) (x, y, z) of the tip position in task space.

A. Sensor performance

Robot was commanded to explore its task space by randomly setting the air pressure of each chamber for 2000 times in load-free condition, where the pressure was increased or decreased 0.05 bar, or kept unchanged between steps, and the tip varied continuously. After the robot became stable after each step, the sensor readings were collected ten times to store their mean value. Fig. 4 shows 400 sets of data, indicating the sensors are capable of outputting different values based on the shape of the robot. The data was also used to train the two tip position sensing models. The sensors are further examined about robustness and temperature-resistance ability.

1) Robustness

First, only one chamber was actuated in load-free state for ten times using same actuation inputs: varied from 0 to 0.6 bar with an increment of 0.05 bar (13 actuation inputs in total, in room temperature $25^\circ C$), and the eGaN sensor beside the chamber directly detected the length change. Fig. 5 shows the variation of the sensor reading, from which the maximum variance with 0.016 V appears at 0.4 bar. This indicates the robustness of the sensor and can clearly map the shape change of the robot.

2) Performance in different temperatures

In addition, the manipulator was heat in an oven with $45^\circ C$ for one hour, and re-mount back to the platform for another testing. Using the same actuation inputs, we obtained similar sensor readings data, as shown in Fig. 5. The data is almost similar to that obtained in $25^\circ C$, showing the eGaN can work robustly in common temperature range.

B. Results of tip position proprioceptive mechanism

The position deviation ΔP_k is one important input data for HMM, so its accuracy is highly involved in the UEF estimation result. To train $f(\cdot)$, the data collected in Section-IV-A (load-free condition) was used. To mimic the robot operation under a load (i.e. with EF), a weight with 20g was

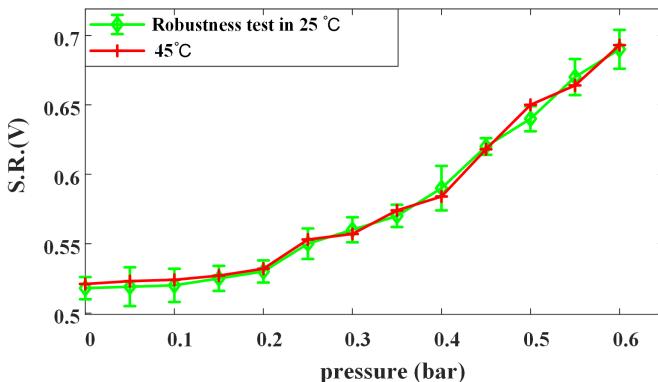


Fig. 5. Performance of robustness and in different temperature.

hung at the robot tip and at the middle part, and random actuation inputs were commanded to robot to reach another 1000 new positions, respectively. The true tip position was collected using the RGB-D camera. The data for training and testing the two models is listed in TABLE I. In training, the maximum iteration in each model was set to 1000, and the learning rate was 0.1.

TABLE I. Data and results for the tip position sensing models ('Y': use the data, and 'N': not use.)

Training data		
load free 2000 sets	20g weight at tip 1000 sets	20g weight at mid. 1000 sets
$f(\cdot)$ Y	N	N
$g(\cdot)$ Y	Y	Y
Testing data (max. err./ mean err. unit: mm)		
load free 100 sets	dual 20g weight (tip. and mid.) 100 sets	30g weight at tip 100 sets
$f(\cdot)$ Y (3.98/3.19)	N	N
$g(\cdot)$ Y (3.87/3.26)	Y (3.94/3.31)	Y (4.13/3.45)

In terms of validation, one hundred new data of random actuation inputs were commanded to the robot in load-free condition, covering almost the entire task space of the tip. The ground truth was also collected by the RGB-D camera for comparison. Fig. 6 (a) shows the comparison between the actual tip position and the values predicted by $f(\cdot)$ in load-free condition. The maximum error between the predicted and the actual values in all the 100 steps is 3.98mm, while the mean position error is 3.19mm.

To test the performance of $g(\cdot)$, in addition to the new 100 data for $f(\cdot)$, 100 sets of data with two 20g loads at the tip and in the middle, and 100 sets of data with a 30g weight at the tip were considered, as listed in TABLE I-Testing data. The multi-load case was not included in the training data, and the results demonstrate the predicted tip position is generally accurate compared with the ground truth. The position value on each axis for the 100 data (two 20g weights) is plotted in Fig. 6. As Fig. 6 (a) shows, $f(\cdot)$ can properly predict the tip in load-free scenario, and no significant error was observed as compared with the measurement from RGB-D. Similarly, even with the unseen multiple loads, $g(\cdot)$ can also properly predict the tip, as shown in Fig. 6 (b). To ensure that ΔP_k can effectively detect the presence of UEF in all three scenarios: no load, load

TABLE II. Predicted tip position under the same actuation inputs (up: $P_k|_{free}$, mid: P_k , bottom: ΔP_k , unit: mm).

Act. Inputs (bar)	load free	dual 20g weights	30g weight at tip.
(0.1,0.2,0.5)	(19.7,-2.9,150.7) (20.8,-3.4,151.6)	(19.7,-2.9,150.7) (40.4,92.2,83.5)	(19.7,-2.9,150.7) (34.5,-84.1,100.2)
1.5	118.3	96.8	
(0.4,0.4,0)	(-45.4,29.9,88.5) (-46.6,30.2,89.2)	(-45.4,29.9,88.5) (-74.1,-35.5,132.6)	(-45.4,29.9,88.5) (-64.7,16.5,147.8)
1.4	83.9	63.8	
(0.6,0.2,0.3)	(-101.8,42.8,102.7) (-102.3,43.6,104.8)	(-101.8,42.8,102.7) (-108.4,-58.7,56.6)	(-101.8,42.75,102.7) (-122.2,21.1,167.2)
2.4	111.6	46.3	

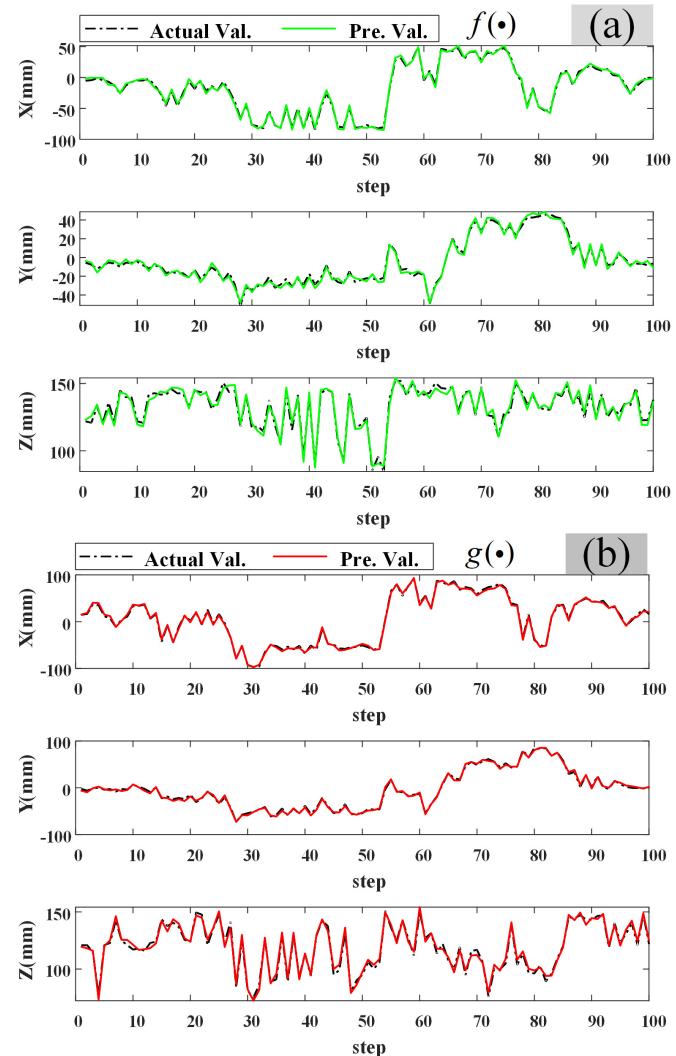


Fig. 6. Validation towards $f(\cdot)$ and $g(\cdot)$. (a) load-free testing. (b) load (dual 20g weights added at the tip and middle area) condition testing.

at the tip, and multiple loads, three random actuation inputs were selected and the predicted from $f(\cdot)$ and $g(\cdot)$ under the three scenarios are summarized in TABLE II. Results confirm that ΔP_k is small when there is no load and is large in the presence of loads. Based on the results, the threshold ϑ used to determine the force for ΔP_k was set to 5mm.

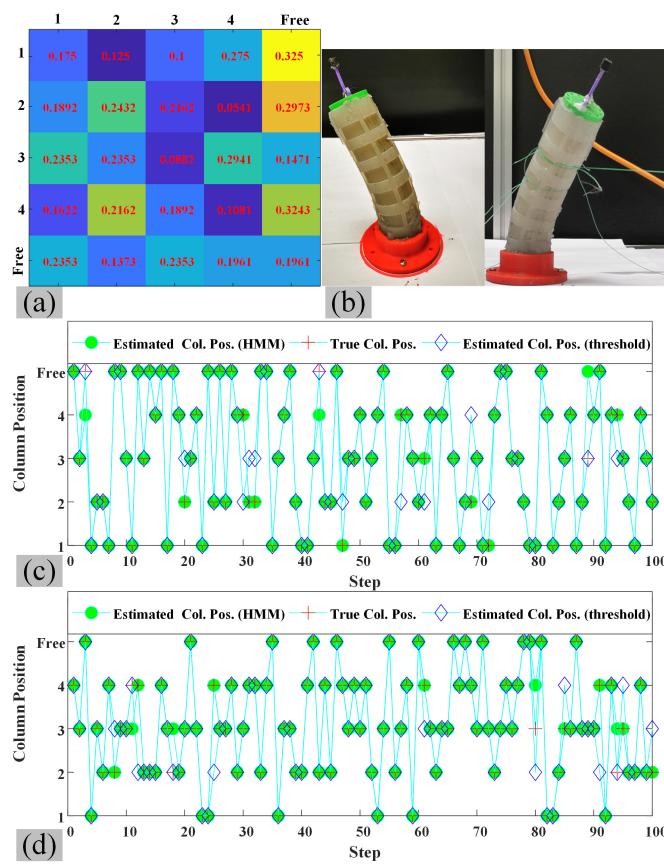


Fig. 7. (a) State transition probability. (b) Snapshots robot experiencing different EF. (c) and (d) Column position estimation results when robot was excited by a bar (pushing force) and thread (tension), respectively.

C. Testing on column position estimation

The above experiments validated the performance of the sensors and the mechanism to sense the presence of an UEF. Once the force is detected, HMM can be employed to find the column position accordingly. To examine the model, 500 sets of data were first prepared for training and another 100 sets were prepared for validation. The robot was randomly moved to a new location, and a metal bar was used to poke on the surface and exerted a force onto the robot. The location where the bar poked at (i.e. the column and row positions) was randomly selected. At some steps, no force was exerted onto the robot to also include the no-load case to the data. The learned state transition probability matrix is illustrated in Fig. 7 (a). Validation using the 100 sets of data is summarized in Fig. 7 (c). It can be observed that HMM can predict the column position properly and only three of the estimated results (the 4th, 42th and 88th) did not match, reaching an accuracy of 97%. To better show the accuracy of the model, a simpler prediction method, inspired by [39], to predict the force direction, which is based on the change in tip position (x, y) due to the force, was considered for comparison, and

TABLE III. Material properties

Property	Value	Property	Value
E Young's Modulus	2.7 MPa	r_c Chamber Radius	2 mm
ρ Density	1.07 (g/cm^3)	l Backbone Length	120 mm
r Distribution Radius	13 mm	G Gravity	0.86 N

the algorithm is listed as:

$$\hat{n}_k = \begin{cases} 1 & \Delta P_k(1) < 0, \Delta P_k(2) < 0 \\ 2 & \Delta P_k(1) > 0, \Delta P_k(2) < 0 \\ 3 & \Delta P_k(1) > 0, \Delta P_k(2) > 0 \\ 4 & \Delta P_k(1) < 0, \Delta P_k(2) > 0 \\ \text{free} & \|\Delta P_k\| < \vartheta \end{cases} \quad (16)$$

The results of this method is also shown in Fig. 7 (c)(threshold). While the column position can still be predicted, but the accuracy is only 90%. In addition, this simpler prediction method can only work with 4 quadrants, and the HMM method is needed for higher column resolution.

In addition to pushing force, tension was also considered to test the trained HMM. Four threads were secured to the surface of robot to generate pulling force at the four columns, as shown in Fig. 7 (b)-(Right). 100 sets of random actuation inputs and random pulling were prepared and the results are shown in Fig. 7 (d). Both HMM and the simpler prediction methods can still predict the column position, the accuracy using HMM (96%) remains higher than the simple method (91%). A video showing the estimation process of using HMM to find the column position for two different cases, is included in the supplementary material.

D. Estimating the row position and EF magnitude

TABLE III lists the material properties of the robot that are required for estimating the row position and the magnitude. Since the algorithm uses an iterative approach to find the optimal values and the model was built assuming the robot is in balance, the system starts to estimate the row position and magnitude 1s after setting an actuation input (robot is stable). The parameter χ is set to 1 and the maximum iteration epoch is 10 in (15). In addition, the mean value and the variance of the Gaussian white noise in (13) were set to 0 and 5, respectively. In testing, the two hundred sets of actuation inputs were commanded to robot and the bar always excited the robot ensuring $\|\Delta P_k\| \geq \vartheta$ (EF always acts). The final estimated row positions and the true ones are illustrated in Fig. 8 (a), proving that only 3 (67th, 148th, and 172th) estimated positions failed to meet with the true results, reaching an accuracy of 98.5%.

In terms of validating the magnitude estimation method, the force sensor was mounted at different positions, as Fig. 8 (c) shows, which means the position and magnitude of the external force were both known, and then robot was commanded to touch the force sensor, whose output was regarded as the ground truth for validation. The force sensor was fixed beside the four columns of the manipulator, and different actuation inputs were set to command the manipulator to contact the force sensor while the row position was also changed at each column position by manually adjusting the height of the force

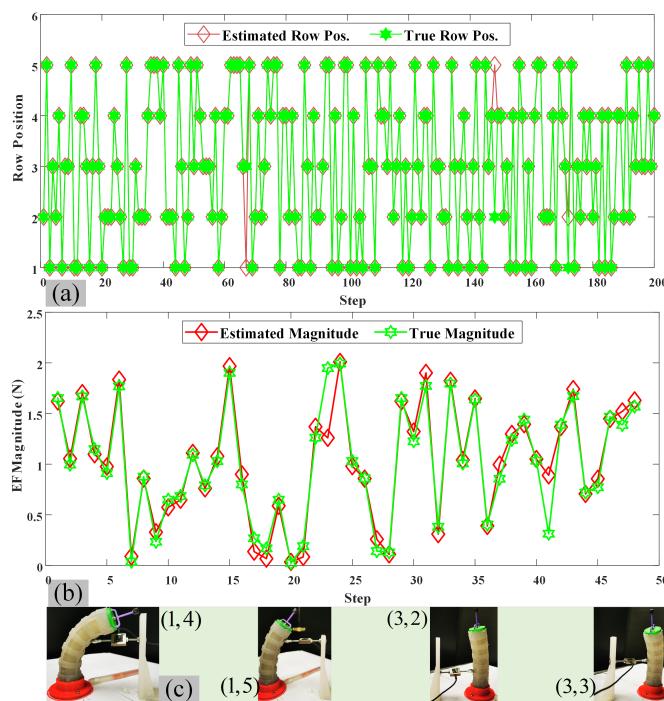


Fig. 8. (a) Row position estimation results. (b) True magnitude and the estimated value. (c) Snapshots of robot disturbed by the force sensor at different area (column position, row position).

sensor. In this way, sixteen regions on the manipulator surface were tested by the force sensor, and three actuation inputs were considered for each region to set different magnitudes. The row position calculation was based on the results from the column position estimation, which means θ_f can be obtained for further calculation. The estimated results are illustrated in Fig. 8 (b). During all the 48 steps, only two (23th and 41th) estimated positions were deviated from the true value, which mainly results from the inaccurate row position. As for the magnitude, a maximum force of $2N$ was applied for testing, and the maximum error happened on the inaccurate step is $0.71N$ which is caused by the inaccurate estimation of the row position. Other than that, the mean error of the estimated magnitude in other 46 steps is $0.23N$, showing this estimation method combining virtual work principle and regularization algorithm is effective.

The time consumption in estimating the presence of an EF (Machine Learning), finding the column position (HMM), and solving the row position and the magnitude (virtual work principle) are 0.078s, 0.008s, and 0.85s, respectively. The third item is more time-consuming due to the iteration process and the process started after the robot was stable, which would take a longer time. The first and the second items took less time and they can be evaluated in real-time. In addition, the probability model requires fewer data in training.

V. CONCLUSION

Finding the external force acting on a soft robot is important in the field. While majority of work focused on the effect at the

end-effector, this paper presents a new method to estimate an unknown force acting on the body of a continuum robot. The robot was fabricated with integrated eGaN sensors to provide useful information related to the shape of the robot. This proprioceptive sensing mechanism can eliminate the use of common external measurement devices, allowing the robot to operate in a confined and occluded environment. A model-free approach based on Artificial Neural Network was employed to predict the tip position based on the sensor information, and compared with the tip position under a load-free scenario so that the presence of an external force can then be determined. To find the exact location of the force, the circumferential body of the robot was represented by a 2D map, and the indices of the map were evaluated accordingly. HMM was employed to find the column position, and the principle of virtual work with a regularization term was used to find the row position and the magnitude. Experimental results confirmed that the model-free approach can predict the tip position with an error of about $4mm$. Different scenarios, including different weights of load, multiple loads, and load-free were examined to ensure the robustness of the prediction method. Random force was exerted onto the robot and this algorithm can achieve an accuracy of 97% and 98.5% in finding the column and row positions, respectively. The error in finding the force magnitude is $0.23N$. This proprioceptive sensing and evaluation algorithms enable the robot to easily sense the force information, allowing better interaction with the surrounding environment.

APPENDIX

The parameters ψ_k , θ_k and R_k under the tip position $P_k = (x_k, y_k, z_k)$ can be solved by:

$$\psi_k = \text{atan}2(y_k, x_k), \theta_k = 2\arccos\left(\frac{z_k}{\sqrt{x_k^2 + y_k^2 + z_k^2}}\right), R_k = l/\theta_k \quad (\text{A1})$$

The length of each chamber is:

$$\begin{aligned} l_{k,1} &= l(1 - (\theta_k/l)r \cos(\psi_k)) \\ l_{k,2} &= l(1 - (\theta_k/l)r \cos(\psi_k + \frac{2}{3}\pi)) \\ l_{k,3} &= l(1 - (\theta_k/l)r \cos(\psi_k + \frac{4}{3}\pi)) \end{aligned} \quad (\text{A2})$$

The centroid of the manipulator is:

$$C_k = \frac{l}{\theta_k} \left[(1 - \cos \frac{\theta_k}{2}) \cos \psi_k, (1 - \cos \frac{\theta_k}{2}) \sin \psi_k, \sin \frac{\theta_k}{2} \right]^T \quad (\text{A3})$$

The tip position change due to an UEF is calculated as:

$$\begin{aligned} H_e(m_k)F_{e,k} &= \text{rotz}(\theta_f) \begin{bmatrix} \frac{F_{e,k}h(m_k)^2(3l-h(m_k))}{6EI} \\ 0 \\ \frac{2EI}{F_{e,k}h(m_k)^2} \sin\left(\frac{F_{e,k}h(m_k)^2}{2EI}\right) \end{bmatrix} \\ \theta_f &= \frac{2\hat{n}_k-1}{4}\pi (\hat{n}_k \neq 5) \end{aligned} \quad (\text{A4})$$

where $\text{rotz}(\theta_f)$ denotes a rotation matrix around Z axis to θ_f , as shown in Fig. 2, and θ_f is involved in the estimated column position.

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Qingxiang Zhao received the B.Eng. degree and the M.S. degree in mechanical engineering from Sichuan University, Chengdu, China, in 2016 and 2019, respectively. He is currently pursuing his Ph.D. degree in mechanical engineering at The Hong Kong Polytechnic University, Hong Kong. His research interests include soft robotics, industrial automation, and artificial intelligence.



Henry K. Chu (M'12) received the B.S. degree in mechanical engineering from the University of Waterloo, Waterloo, ON, Canada, and the M.S. and Ph.D. degrees in mechanical and industrial engineering from the University of Toronto, Toronto, ON, Canada. He was a Post-Doctoral Fellow with the University of Toronto and the City University of Hong Kong, Hong Kong. He is currently an Assistant Professor with The Hong Kong Polytechnic University, Hong Kong. His research interests include robotic manipulation, vision-based control and automation, micro-system design, and tissue engineering.



Jiewen Lai (S'20) received the B.Eng. degree in metallurgical engineering from Wuhan University of Science and Technology, Wuhan, China, in 2016, and the M.Sc. degree in mechanical and automation engineering from The Chinese University of Hong Kong, Hong Kong, in 2017. He is currently working toward the Ph.D. degree in mechanical engineering with The Hong Kong Polytechnic University, Hong Kong. His research interests include soft/continuum robot and surgical robot system.