## **AVL Runtime Proof**

On Friday, we proved an upper-bound on the height of an AVL tree is  $2 \times lg(n)$  or O(lg(n)):

```
N(h) := Minimum # of nodes in an AVL tree of height h

N(h) = 1 + N(h-1) + N(h-2)

> 1 + 2^{h-1/2} + 2^{h-2/2}

> 2 \times 2^{h-2/2} = 2^{h-2/2+1} = 2^{h/2}
```

## Theorem #1:

**Every AVL** tree of height h has at least 2<sup>h/2</sup> nodes.