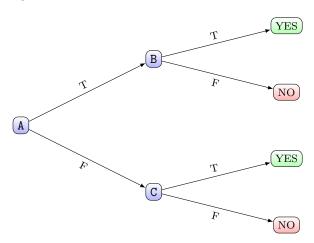
1. On the first round, we must consider all the attribute choices. We thus have:

$$\begin{split} ENT(A,d) &= ENT(a,d) + ENT(\bar{a},d) \\ &= Pr(a) \Big[- Pr(d|a) \cdot \log_2(Pr(d|a)) - Pr(d|a) \cdot \log_2(Pr(d|a)) \Big] \\ &+ Pr(\bar{a}) \Big[- Pr(d|\bar{a}) \cdot \log_2(Pr(d|\bar{a})) - Pr(d|\bar{a}) \cdot \log_2(Pr(d|\bar{a})) \Big] \\ &= \frac{12}{23} \left[-\frac{3}{12} \log_2\left(\frac{3}{12}\right) - \frac{9}{12} \log_2\left(\frac{9}{12}\right) \right] + \frac{11}{23} \left[-\frac{7}{11} \log_2\left(\frac{7}{11}\right) - \frac{4}{11} \log_2\left(\frac{4}{11}\right) \right] \\ &\approx 0.876 \\ ENT(B,d) &= ENT(b,d) + ENT(\bar{b},d) \\ &= Pr(b) \Big[- Pr(d|b) \cdot \log_2(Pr(d|b)) - Pr(d|b) \cdot \log_2(Pr(d|b)) \Big] \\ &+ Pr(\bar{b}) \Big[- Pr(d|\bar{b}) \cdot \log_2(Pr(d|\bar{b})) - Pr(d|\bar{b}) \cdot \log_2(Pr(d|\bar{b})) \Big] \\ &= \frac{9}{23} \left[-\frac{2}{9} \log_2\left(\frac{2}{9}\right) - \frac{7}{9} \log_2\left(\frac{7}{9}\right) \right] + \frac{14}{23} \left[-\frac{8}{14} \log_2\left(\frac{8}{14}\right) - \frac{6}{14} \log_2\left(\frac{6}{14}\right) \right] \\ &\approx 0.899 \\ ENT(C,d) &= ENT(c,d) + ENT(\bar{c},d) \\ &= Pr(c) \Big[- Pr(d|c) \cdot \log_2(Pr(d|c)) - Pr(d|c) \cdot \log_2(Pr(d|c)) \Big] \\ &+ Pr(\bar{c}) \Big[- Pr(d|\bar{c}) \cdot \log_2(Pr(d|\bar{c})) - Pr(d|\bar{c}) \cdot \log_2(Pr(d|\bar{c})) \Big] \\ &= \frac{16}{23} \left[-\frac{6}{16} \log_2\left(\frac{6}{16}\right) - \frac{10}{16} \log_2\left(\frac{10}{16}\right) \right] + \frac{7}{23} \left[-\frac{4}{7} \log_2\left(\frac{4}{7}\right) - \frac{3}{7} \log_2\left(\frac{3}{7}\right) \right] \\ &\approx 0.964 \end{split}$$

Since splitting on A results in the lowest entropy and thus greatest information gain, we split on that first. This results in

$$\left\{ \begin{array}{l} \{+x_5, +x_7, -x_6, -x_8\}, & \text{for } A = F \\ \{+x_1, +x_2, -x_3, -x_4\}, & \text{for } A = T \end{array} \right\}$$

At this point we have completed our search, since $ENT(C|\bar{a}) = ENT(B|a) = 0$. Therefore, our resulting tree is:



2. We assume that all nodes utilize the step function with threshold t as labeled on the node. These are therefore of the form

$$g(I) = \left\{ \begin{array}{ll} 1, & \text{for } I \geq t \\ 0, & \text{for } I < t \end{array} \right\}$$

Numbers appearing directly above or below an edge are weights. Thus our network is:

