

**Chapter 3: Quadratic Functions.** Based on these sources, here is a comprehensive guide to help you prepare for your test on **Quadratic Functions**, including key concepts, essential equations, and a study checklist.

## Important Concepts and Key Ideas

- **Properties of Quadratic Functions:** These functions are of degree 2 and their graphs are parabolas. A parabola is symmetric about a vertical line called the **axis of symmetry**, which passes through the **vertex**.
- **Forms of the Quadratic Function:**
  - **Standard Form** ( $f(x) = ax^2 + bx + c$ ): Useful for identifying the y-intercept ( $c$ ).
  - **Factored Form** ( $f(x) = a(x - r)(x - s)$ ): Useful for identifying the x-intercepts or zeros ( $r$  and  $s$ ).
  - **Vertex Form** ( $f(x) = a(x - h)^2 + k$ ): Useful for identifying the vertex  $(h, k)$  and the axis of symmetry ( $x = h$ ).
- **Maximum and Minimum Values:** The y-coordinate of the vertex represents the maximum or minimum value of the function. If  $a > 0$ , the parabola opens up and has a minimum; if  $a < 0$ , it opens down and has a maximum.
- **The Inverse of a Quadratic Function:** The inverse of  $f(x) = x^2$  is not a function unless the domain of the original function is restricted (e.g.,  $x \geq 0$ ). Graphically, the inverse is a reflection across the line  $y = x$ .
- **Operations with Radicals:** An **entire radical** (e.g.,  $\sqrt{72}$ ) can be simplified into a **mixed radical** (e.g.,  $6\sqrt{2}$ ) by extracting perfect-square factors. You can only add or subtract **like radicals** (those with the same number under the radical sign).
- **The Discriminant** ( $b^2 - 4ac$ ): This value determines the number of zeros for a quadratic function:
  - $D > 0$ : Two distinct real zeros.
  - $D = 0$ : One real zero (the vertex sits on the x-axis).
  - $D < 0$ : No real zeros.
- **Families of Parabolas:** A “family” is a group of parabolas that share a common characteristic, such as the same vertex, the same zeros, or the same y-intercept.
- **Linear-Quadratic Systems:** A line can intersect a parabola at most at two points. Intersection points are found by setting the linear equation equal to the quadratic equation and solving the resulting quadratic.

## Important Equations, Laws, and Rules

Rule/Concept	Equation/Formula
<b>Quadratic Formula</b>	$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$
<b>Discriminant</b>	$D = b^2 - 4ac$
<b>Vertex (from zeros)</b>	$x = \frac{r+s}{2}$
<b>Radical Multiplication</b>	$\sqrt{a} \times \sqrt{b} = \sqrt{ab} \text{ (for } a, b \geq 0\text{)}$
<b>Radical Multiplication (Mixed)</b>	$(c\sqrt{a})(d\sqrt{b}) = cd\sqrt{ab}$
<b>Inverse Mapping</b>	Point $(x, y)$ becomes $(y, x)$
<b>Profit Function</b>	$P(x) = R(x) - C(x)$ (Revenue - Cost)

## Study Checklist

### 1. Properties and Graphing (3.1 - 3.2)

- Can you identify a quadratic function from a table of values using **second differences**?
- Can you convert between standard, factored, and vertex forms?
- Do you know how to **complete the square** to find the vertex?
- Can you solve real-world “max/min” problems (e.g., maximizing profit or area)?

### 2. Inverses and Radicals (3.3 - 3.4)

- Can you find the equation of an inverse by switching  $x$  and  $y$  and solving for  $y$ ?
- Do you know how to restrict the domain so the inverse is a function?
- Can you simplify radicals by finding the largest perfect-square factor?
- Can you multiply binomial radical expressions (e.g., using FOIL)?

### 3. Solving Equations and Systems (3.5, 3.6, 3.8)

- Can you solve quadratic equations using factoring and the **quadratic formula**?
- Do you know how to identify **inadmissible solutions** in word problems (e.g., negative time or width)?
- Can you use the **discriminant** to predict the number of zeros or intersection points?
- Can you solve a **linear-quadratic system** algebraically and state the points of intersection?

#### 4. Modeling and Families (3.7)

- Can you determine the equation of a parabola given its vertex and one other point?
- Can you determine the equation of a parabola given its zeros and one other point?
- Do you understand that changing ' $a$ ' in  $y = a(x - h)^2 + k$  creates a family of parabolas with the same vertex?