

DSPIC HW4

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1.

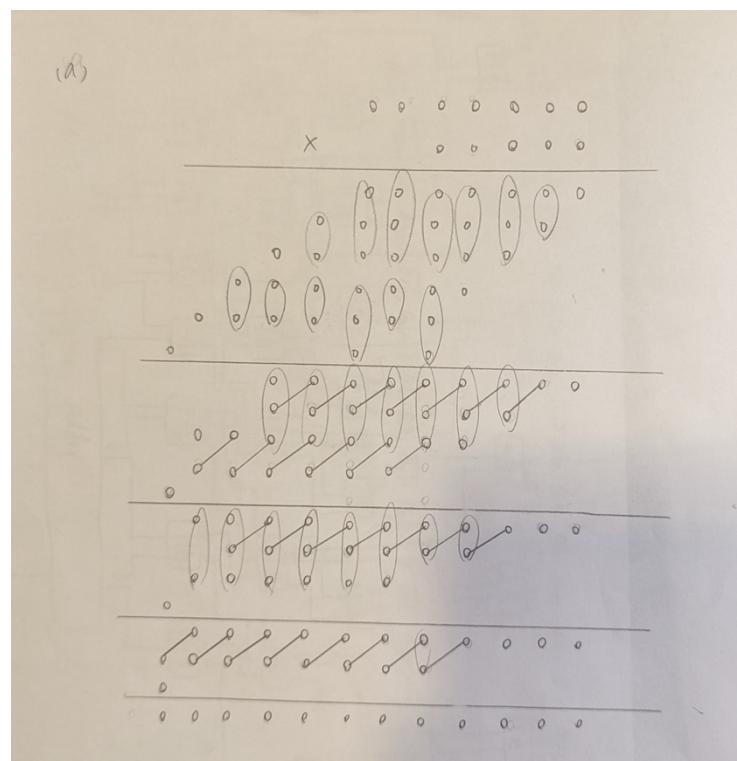
(a)

112064535 周易
 DSPIC HW4
 1. (d) $m=7 \quad n=5$

b_1	b_2	b_3	b_4	b_5	b_6	b_7	b_8	b_9	b_{10}
a_5	a_4	a_3	a_2	a_1	a_0				
$\overline{a_0 b_6}$	$\overline{a_0 b_5}$	$\overline{a_0 b_4}$	$\overline{a_0 b_3}$	$\overline{a_0 b_2}$	$\overline{a_0 b_1}$	$\overline{a_0 b_0}$			
$\overline{a_1 b_6}$	$\overline{a_1 b_5}$	$\overline{a_1 b_4}$	$\overline{a_1 b_3}$	$\overline{a_1 b_2}$	$\overline{a_1 b_1}$	$\overline{a_1 b_0}$			
$\overline{a_2 b_6}$	$\overline{a_2 b_5}$	$\overline{a_2 b_4}$	$\overline{a_2 b_3}$	$\overline{a_2 b_2}$	$\overline{a_2 b_1}$	$\overline{a_2 b_0}$			
$\overline{a_3 b_6}$	$\overline{a_3 b_5}$	$\overline{a_3 b_4}$	$\overline{a_3 b_3}$	$\overline{a_3 b_2}$	$\overline{a_3 b_1}$	$\overline{a_3 b_0}$			
$\overline{a_4 b_6}$	$\overline{a_4 b_5}$	$\overline{a_4 b_4}$	$\overline{a_4 b_3}$	$\overline{a_4 b_2}$	$\overline{a_4 b_1}$	$\overline{a_4 b_0}$			
$\overline{a_5 b_6}$	$\overline{a_5 b_5}$	$\overline{a_5 b_4}$	$\overline{a_5 b_3}$	$\overline{a_5 b_2}$	$\overline{a_5 b_1}$	$\overline{a_5 b_0}$			
$\overline{a_6 b_6}$	$\overline{a_6 b_5}$	$\overline{a_6 b_4}$	$\overline{a_6 b_3}$	$\overline{a_6 b_2}$	$\overline{a_6 b_1}$	$\overline{a_6 b_0}$			
$\overline{a_7 b_6}$	$\overline{a_7 b_5}$	$\overline{a_7 b_4}$	$\overline{a_7 b_3}$	$\overline{a_7 b_2}$	$\overline{a_7 b_1}$	$\overline{a_7 b_0}$			
$\overline{a_8 b_6}$	$\overline{a_8 b_5}$	$\overline{a_8 b_4}$	$\overline{a_8 b_3}$	$\overline{a_8 b_2}$	$\overline{a_8 b_1}$	$\overline{a_8 b_0}$			
$\overline{a_9 b_6}$	$\overline{a_9 b_5}$	$\overline{a_9 b_4}$	$\overline{a_9 b_3}$	$\overline{a_9 b_2}$	$\overline{a_9 b_1}$	$\overline{a_9 b_0}$			
$\overline{a_{10} b_6}$	$\overline{a_{10} b_5}$	$\overline{a_{10} b_4}$	$\overline{a_{10} b_3}$	$\overline{a_{10} b_2}$	$\overline{a_{10} b_1}$	$\overline{a_{10} b_0}$			

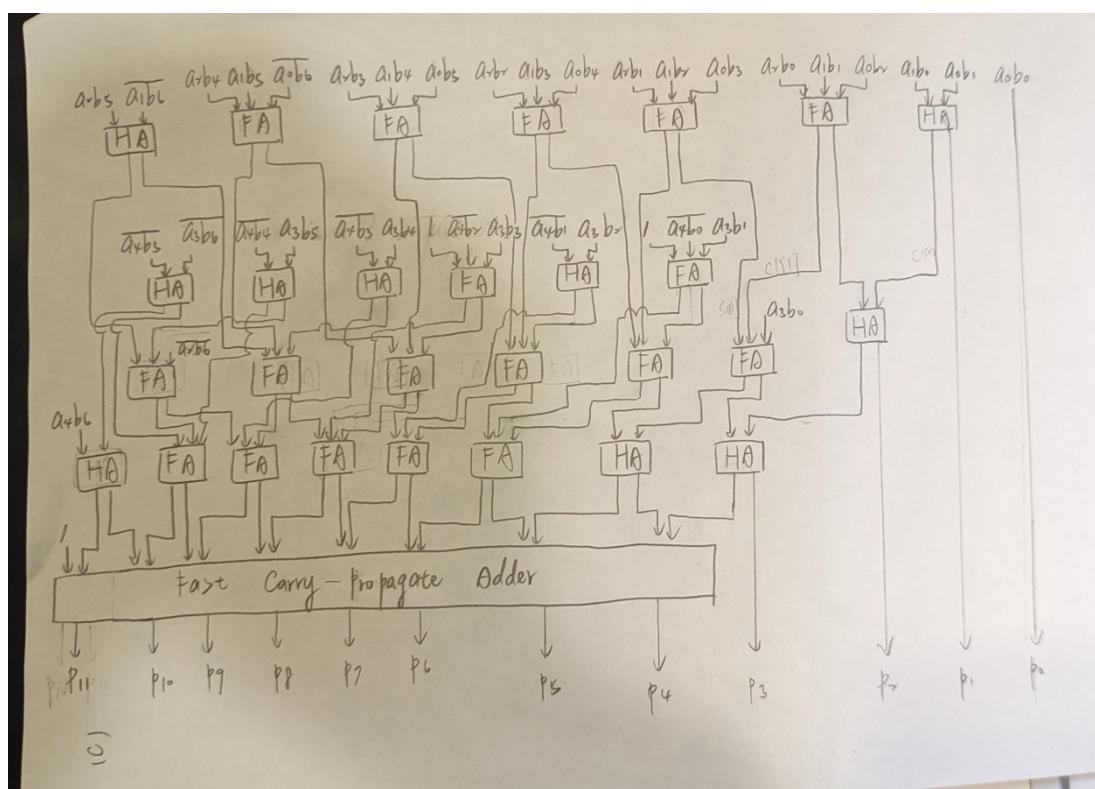
$f_1 \quad f_2 \quad f_3 \quad f_4 \quad f_5 \quad f_6 \quad f_7 \quad f_8 \quad f_9 \quad f_{10} \quad f_{11}$

(圖一) 7×5 乘法器運算流程



(圖二) 運作流程(包含 18 個 FA 及 11 個 HA)

(b)

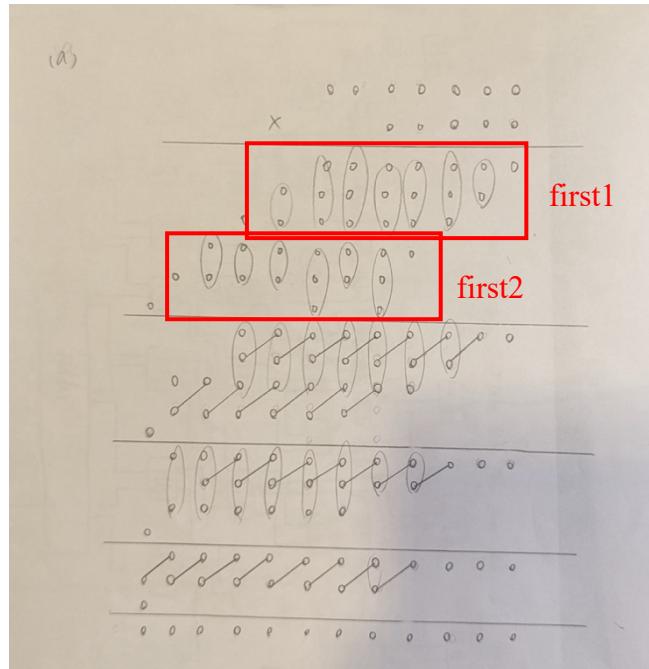


(圖三) Wallance-Tree 結構

(c)

Verilog code:

(1) 把加法器分成四層，第一層有兩個部分：



first1.v:

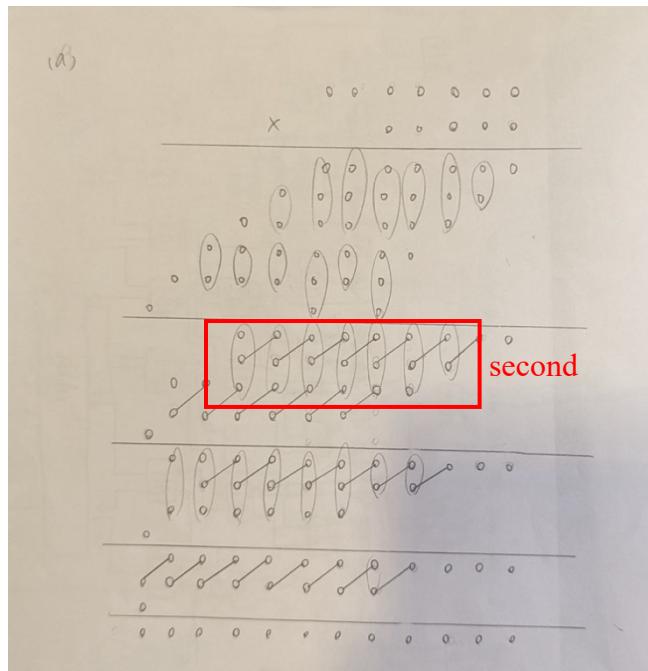
```
first1.v
1 `include "fulladd.v"
2 `include "halfadder.v"
3
4 module first1(
5   input [5:0] a, //a有6個 a0b1~a0b6
6   input [6:0] b, //a1b0~a1b6
7   input [5:0] cin, // a2b0~a2b5
8   output [6:0] cout, //7個adder
9   output [6:0] sum //同上
10 );
11
12
13 half_add add1[
14   .A(a[0]),
15   .B(b[0]),
16   .sum(sum[0]), //p1
17   .cout(cout[0])
18 ];
19
20 Full_Adder add2(
21   .A(a[1]),
22   .B(b[1]),
23   .Cin(cin[0]),
24   .Cout(cout[1]),
25   .Sum(sum[1])
26 );
27
```

```
27
28     Full_Adder add3(
29         .A(a[2]),
30         .B(b[2]),
31         .Cin(cin[1]),
32         .Cout(cout[2]),
33         .Sum(sum[2])
34     );
35
36     Full_Adder add4(
37         .A(a[3]),
38         .B(b[3]),
39         .Cin(cin[2]),
40         .Cout(cout[3]),
41         .Sum(sum[3])
42     );
43
44     Full_Adder add5(
45         .A(a[4]),
46         .B(b[4]),
47         .Cin(cin[3]),
48         .Cout(cout[4]),
49         .Sum(sum[4])
50     );
51
52     Full_Adder add6(
53         .A(a[5]),
54         .B(b[5]),
55         .Cin(cin[4]),
56         .Cout(cout[5]),
57         .Sum(sum[5])
58     );
59
60     half_add add7(
61         .A(b[6]),
62         .B(cin[5]),
63         .sum(sum[6]),
64         .cout(cout[6])
65     );
66
67
68 endmodule
```

first2.v:

```
≡ first2.v
 1 // `include "fulladd.v"
 2 // `include "halfadder.v"
 3
 4 module first2[
 5     input [5:0] a, //a有6個 a3b1~a3b6
 6     input [5:0] b, //a4b0~a4b5
 7     //cin都是1 不需要設輸入
 8     output [5:0] cout, //7個adder
 9     output [5:0] sum //同上
10 ];
11
12
13     Full_Adder add1(
14         .A(a[0]),
15         .B(b[0]),
16         .Cin(1'b1),
17         .Sum(sum[0]),
18         .Cout(cout[0])
19 );
20
21     half_add add2(
22         .A(a[1]),
23         .B(b[1]),
24         .cout(cout[1]),
25         .sum(sum[1])
26 );
27
28     Full_Adder add3(
29         .A(a[2]),
30         .B(b[2]),
31         .Cin(1'b1),
32         .Cout(cout[2]),
33         .Sum(sum[2])
34 );
35
36     half_add add4(
37         .A(a[3]),
38         .B(b[3]),
39         .cout(cout[3]),
40         .sum(sum[3])
41 );
42
43     half_add add5(
44         .A(a[4]),
45         .B(b[4]),
46         .cout(cout[4]),
47         .sum(sum[4])
48 );
49
50     half_add add6(
51         .A(a[5]),
52         .B(b[5]),
53         .cout(cout[5]),
54         .sum(sum[5])
55 );
56
57
58 endmodule
```

(2) 第二層:



second.v:

```

second.v
1 // `include "fulladd.v"
2 // `include "halfadder.v"
3
4 module second(
5     input [6:0] a, //a有6個 從first1的第一個ha到a2b6
6     input [6:0] b,
7     input [5:0] cin,
8     output [6:0] cout, //7個adder
9     output [6:0] sum //同上
10 );
11
12
13 half_add add1(
14     .A(a[0]),
15     .B(b[0]),
16     .sum(sum[0]), //p2
17     .cout(cout[0])
18 );
19
20 Full_Adder add2(
21     .A(a[1]),
22     .B(b[1]),
23     .Cin(cin[0]), //a3b0
24     .Cout(cout[1]),
25     .Sum(sum[1])
26 );
27
28 Full_Adder add3(
29     .A(a[2]),
30     .B(b[2]),
31     .Cin(cin[1]),
32     .Cout(cout[2]),
33     .Sum(sum[2])
34 );

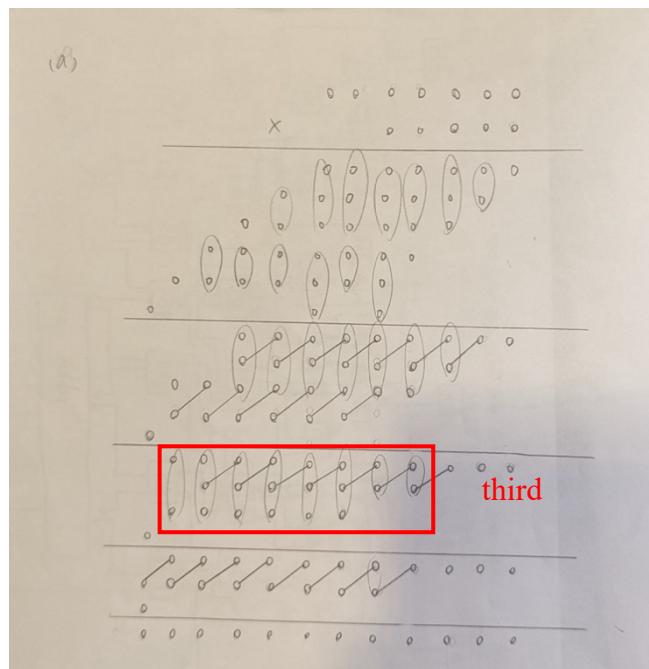
```

```

36     Full_Adder add4(
37         .A(a[3]),
38         .B(b[3]),
39         .Cin(cin[2]),
40         .Cout(cout[3]),
41         .Sum(sum[3])
42     );
43
44     Full_Adder add5(
45         .A(a[4]),
46         .B(b[4]),
47         .Cin(cin[3]),
48         .Cout(cout[4]),
49         .Sum(sum[4])
50     );
51
52     Full_Adder add6(
53         .A(a[5]),
54         .B(b[5]),
55         .Cin(cin[4]),
56         .Cout(cout[5]),
57         .Sum(sum[5])
58     );
59
60     Full_Adder add7(
61         .A(a[6]),
62         .B(b[6]),
63         .Cin(cin[5]),
64         .Cout(cout[6]),
65         .Sum(sum[6])
66     );
67
68
69     endmodule

```

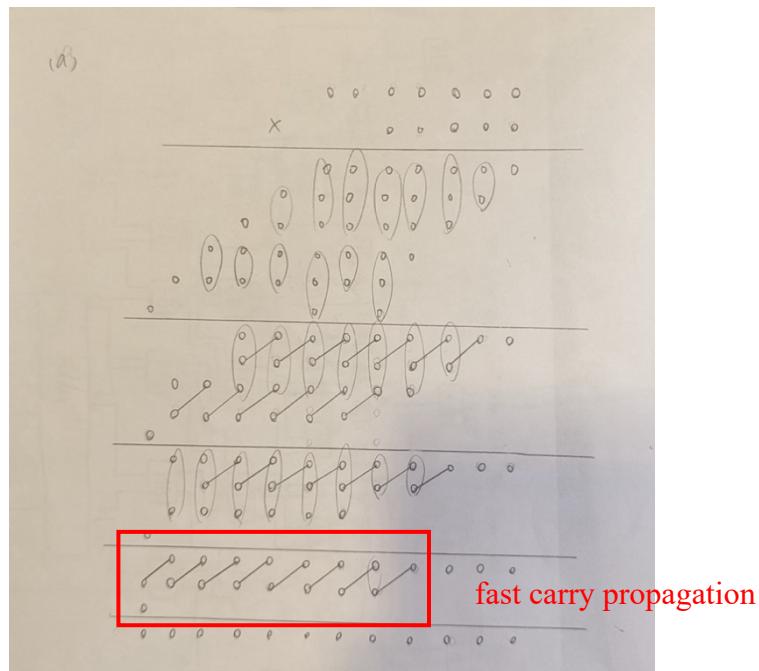
(3) 第三層:



third.v:

```
4  module third(
5      input [7:0] a, //a有8個 每一個adder的第一的輸入
6      input [7:0] b, //同上
7      input [4:0] cin, // 每個adder的最後一個輸入
8      output [7:0] cout, //8個adder
9      output [7:0] sum //同上
10 );
11
12
13 half_add add1(
14     .A(a[0]),
15     .B(b[0]),
16     .sum(sum[0]), //p3
17     .cout(cout[0])
18 );
19
20 half_add add2(
21     .A(a[1]),
22     .B(b[1]),
23     .cout(cout[1]),
24     .sum(sum[1])
25 );
26
27 Full_Adder add3(
28     .A(a[2]),
29     .B(b[2]),
30     .Cin(cin[0]),
31     .Cout(cout[2]),
32     .Sum(sum[2])
33 );
34
35 Full_Adder add4(
36     .A(a[3]),
37     .B(b[3]),
38     .Cin(cin[1]),
39     .Cout(cout[3]),
40     .Sum(sum[3])
41 );
42
43 Full_Adder add5(
44     .A(a[4]),
45     .B(b[4]),
46     .Cin(cin[2]),
47     .Cout(cout[4]),
48     .Sum(sum[4])
49 );
50
51 Full_Adder add6(
52     .A(a[5]),
53     .B(b[5]),
54     .Cin(cin[3]),
55     .Cout(cout[5]),
56     .Sum(sum[5])
57 );
58
59 Full_Adder add7(
60     .A(a[6]),
61     .B(b[6]),
62     .Cin(cin[4]),
63     .Cout(cout[6]),
64     .Sum(sum[6])
65 );
66
67 half_add add8(
68     .A(a[7]),
69     .B(b[7]),
70     .sum(sum[7]),
71     .cout(cout[7])
72 );
73
74
75 endmodule
```

(4) 第四層:



fast_carry_prop.v:

```

4  module fast( //變成一般的carry propagate 一個ha 七個fa
5    input [7:0] a,
6    input [7:0] b, //a[0]~a[6]
7    // input [5:0] cin, // 每個人的carryin來自前一級就不用加了
8    output cout, //最後不輸出p12
9    output [7:0] sum //p4-p11
10 );
11
12 wire [6:0] w; //每一級的carryout 除了cout
13
14 half_add add1(
15   .A(a[0]),
16   .B(b[0]),
17   .sum(sum[0]), //p3
18   .cout(w[0]) //下一級的carryin
19 );
20
21 Full_Adder add2(
22   .A(a[1]),
23   .B(b[1]),
24   .Cin(w[1]),
25   .Cout(w[1]),
26   .Sum(sum[1])
27 );
28
29 Full_Adder add3(
30   .A(a[2]),
31   .B(b[2]),
32   .Cin(w[2]),
33   .Cout(w[2]),
34   .Sum(sum[2])
35 );
36
37 Full_Adder add4(
38   .A(a[3]),
39   .B(b[3]),
40   .Cin(w[2]),
41   .Cout(w[3]),
42   .Sum(sum[3])
43 );

```

```

45     Full_Adder add5(
46       .A(a[4]),
47       .B(b[4]),
48       .Cin(w[3]),
49       .Cout(w[4]),
50       .Sum(sum[4])
51   );
52
53     Full_Adder add6(
54       .A(a[5]),
55       .B(b[5]),
56       .Cin(w[4]),
57       .Cout(w[5]),
58       .Sum(sum[5])
59   );
60
61     Full_Adder add7(
62       .A(a[6]),
63       .B(b[6]),
64       .Cin(w[5]),
65       .Sum(sum[6]),
66       .Cout(w[6])
67   );
68
69     Full_Adder add8(
70       .A(a[7]),
71       .B(b[7]),
72       .Cin(w[6]),
73       .Sum(sum[7]),
74       .Cout(cout)
75   );
76
77
78
79   endmodule

```

(5) 在 top module 裡將所有 input a 跟 b 乘好再運算:

baugh_wooley.v:

```

9  module baughwooley(a,b,p);
10
11  input [4:0] a;
12  input [6:0] b;
13
14  output [11:0] p;
15
16  wire [4:0] a;
17  wire [6:0] b;
18
19  wand [4:0][6:0]ab;
20
21  wire [6:0] c1;
22  wire [6:0] s1;// 給first1輸出
23  wire [5:0] c2;
24  wire [5:0] s2;// 給first2輸出
25
26  wire [6:0] a2; //第二層的輸入a
27  wire [5:0] b2; //第二層的輸入carryin
28
29  wire [6:0] c3;
30  wire [6:0] s3; //second的輸出
31
32  wire [7:0] a3; //third的輸入
33  wire [7:0] b3; //同上
34
35  wire [7:0] c4;
36  wire [7:0] s4; //third輸出

```

(圖四) 定義輸入及輸出

```

38  wire [7:0] a4; //最後一級carry propagate輸入
39  |
40  wire cout;
41
42  genvar i,j;
43  generate
44    for(i=0;i<4;i=i+1) begin
45      for(j=0;j<6;j=j+1) begin
46        assign ab[i][j]=a[i]&b[j];
47      end
48    end
49  endgenerate
50
51  generate
52    // genvar i;
53    for(i=0;i<4;i=i+1) begin
54      assign ab[i][6]=~(a[i]&b[6]);
55    end
56  endgenerate
57
58  generate
59    // genvar j;
60    for(j=0;j<6;j=j+1)begin
61      assign ab[4][j]=~(a[4]&b[j]);
62    end
63  endgenerate
64
65  assign ab[4][6]=a[4]&b[6];
66
67  first1 adder1(
68    .a(ab[8][6:1]),
69    .b(ab[1][6:0]),
70    .cin(ab[2][5:0]),
71    .cout(c1),
72    .sum(s1)
73  );

```

(圖五) 配置所有的 ab 對

```

75  assign a2[5:0]=s1[6:1];
76  assign a2[6]=ab[2][6]; //定義second的輸入
77
78  first2 adder2(
79    .a(ab[3][6:1]),
80    .b(ab[4][5:0]),
81    .cout(c2),
82    .sum(s2)
83  );
84  assign b2[5:1]=s2[4:0];
85  assign b2[6]=ab[3][6];//定義second的輸入 等等不行就把assign拿掉
86
87  second adder3(
88    .a(a2), //a2b6+s1[6:1]
89    .b(c1),
90    .cin(b2), //s2[4:0]+a3b0
91    .cout(c3),
92    .sum(s3)
93  );
94
95  assign a3[7]=ab[4][6];
96  assign a3[6]=s2[5];
97  assign a3[5:0]=s3[6:1];
98
99  assign b3[7]=c1[5];
100 assign b3[6:0]=c3[6:0];
101
102 third adder4(
103   .a(a3), // a4b6+s2[5]+s3[6:1]
104   .b(b3), // c2[5]+c3[6:0]
105   .cin(c2[4:0]), //c2[4:0]
106   .cout(c4),
107   .sum(s4)
108 );
109
110 assign a4[7]=1'b1;
111 assign a4[6:0]=s4[7:1];
112 fast adder5(
113   .a(a4), // 1'b1+s4[7:1]
114   .b(c4), //c4[7:0]
115   .cout(cout),
116   .sum(p[11:4])
117 );

```

```

119      assign p[0]=ab[0][0];
120      assign p[1]=s1[0];
121      assign p[2]=s3[0];
122      assign p[3]=s4[0];
123
124  endmodule

```

(圖六)(圖七) 運算後決定輸出

(6) test bench 輸入及輸出結果:

```

24 initial
25 begin
26 $dumpfile("baugh_tb.vcd");
27 $dumpvars;
28 #10
29 a=5'b01101; //13
30 b=7'b1110100; //-12
31 #10
32 a=5'b10100; //-13
33 b=7'b0001101; //12
34 #10
35 a=5'b10100; //-12
36 b=7'b1110011; //-13
37 #10
38 a=5'b10011; //-13
39 b=7'b1110100; //-12
40 #10
41 a=5'b00110; //6
42 b=7'b1111000; //-8
43 #10
44 a=5'b10110;
45 b=7'b0100001;
46 #10
47 a=5'b10000;
48 b=7'b1100011;
49 #10
50 a=5'b10111;
51 b=7'b1110110;
52 #10
53 a=5'b01101;
54 b=7'b1110100; //13
55 #10
56 a=5'b10010;
57 b=7'b1011101;
58 #10
59 a=5'b10100;
60 b=7'b1110000;
61 #10
62 a=5'b11111;
63 b=7'b1110100;
64 #10
65 a=5'b01110;
66 b=7'b1001010;
67 #10
68 a=5'b11010;
69 b=7'b0101101;

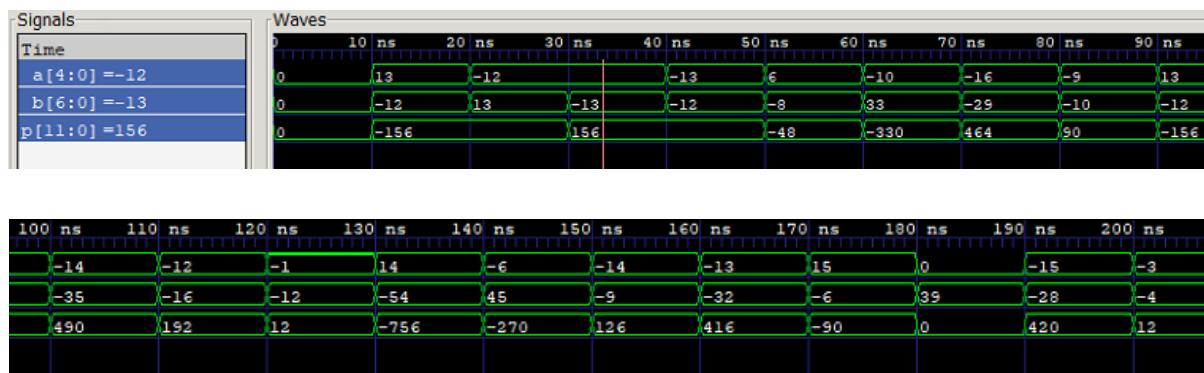
70 #10
71 a=5'b10010;
72 b=7'b1110111;
73 #10
74 a=5'b10011;
75 b=7'b1100000;
76 #10
77 a=5'b01111;
78 b=7'b1111010;

```

```

79      #10
80      a=5'b00000;
81      b=7'b0100111;
82      #10
83      a=5'b10001;
84      b=7'b1100100;
85      #10
86      a=5'b11101;
87      b=7'b1111100;
88      #10
89      $finish;
90      end
91
92      endmodule

```



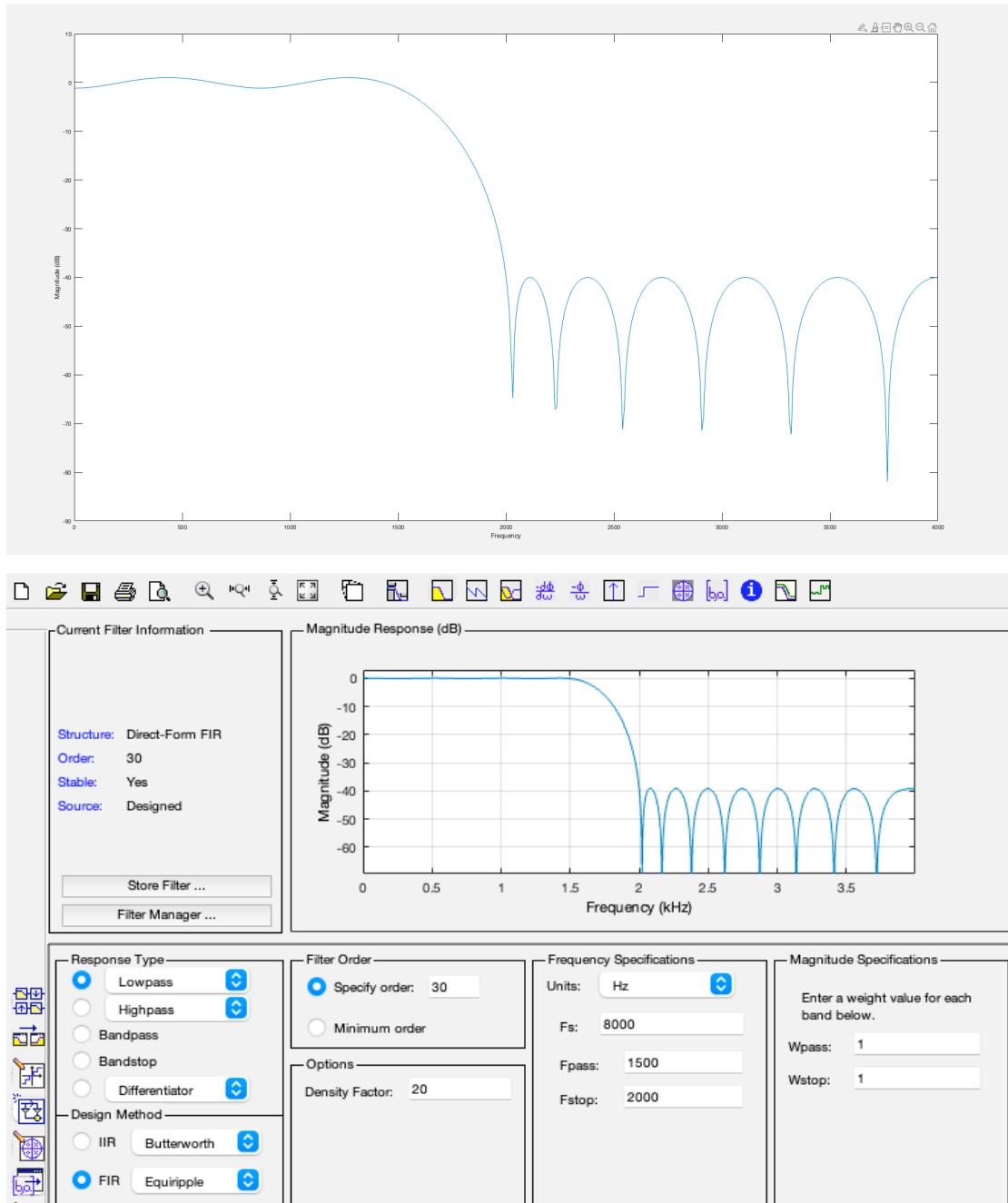
2.

(a)

(i) 利用 matlab 產生 21 個 tap 的 filter coefficient，以符合規定的 filter constrains，coefficient 為：

-0.0105963997986059
-0.0380214361435444
-0.0365217681824527
0.00336388262116807
0.0454851577619937
0.0194242970434525
-0.0610882554173864
-0.0752620124582160
0.0734976427892512
0.307268070442418
0.421992848704956
0.307268070442418
0.0734976427892512
-0.0752620124582160
-0.0610882554173864
0.0194242970434525
0.0454851577619937
0.00336388262116807
-0.0365217681824527
-0.0380214361435444
-0.0105963997986059

(ii) 21 tap 的 FIR low pass filter 頻率響應為：



可以看到 tap 數更高的 filter 在 transition band 上更加 sharp

(b)

(i) c program:

```
1 #include <stdio.h>
2 #include <time.h>
3 #include <stdlib.h>
4 #include <math.h>
5
6 #define NUM_SAMPLES 512
7
8 #define M 21 // 濾波器阶数
9
10
11 float generateRandomFloat() {
12     // 生成随机整数
13     int randomInt = rand();
14
15     // 映射到浮点数范围 [0, 10] 要取範圍多少隨意
16     float randomFloat = ((float)randomInt /RAND_MAX) ; //RAND_MAX
17
18     // 生成带符号的随机浮点数
19     return (rand() % 2 == 0) ? randomFloat : -randomFloat;
20 }
```

(圖八)生成亂數之副函式

```
25 int main() {
26     float inputSignal[NUM_SAMPLES]; // 输入信号
27     float outputSignal[NUM_SAMPLES]; // 输出信号
28     float filterCoeff[M] = {-0.0105963997986059, -0.0380214361435444, -0.0365217681824527, 0.00336388262116807, 0.0454851577619937, 0.0
29     srand(time(NULL));
30
31     // 设置随机种子
32     srand((unsigned int)time(NULL));
33
34     // 生成随机浮点数
35     float randomSignal[NUM_SAMPLES];
36     float sumOfSquares = 0;
37
38
39     for (int i = 0; i < NUM_SAMPLES; i++) {
40         randomSignal[i] = generateRandomFloat(); // -1~1之間的floating point
41         sumOfSquares += randomSignal[i] * randomSignal[i];
42     }
43
44     // 调整幅度，使得平均功率为1
45     float scaleFactor = 1 / sqrt(sumOfSquares);
46
47     for (int i = 0; i < NUM_SAMPLES; i++) {
48         randomSignal[i] *= scaleFactor;
49         inputSignal[i]=randomSignal[i]*sqrt(NUM_SAMPLES);
50         // printf("inputsignal = %f\n", randomSignal[i]);
51     }
52
53     // 执行 FIR 低通滤波器
54     firLowPassFilter(inputSignal, outputSignal, filterCoeff, NUM_SAMPLES, M);
55
56     // 计算平均功率
57     float averagePower = 0;
58     for (int i = 0; i < NUM_SAMPLES; i++) {
59         averagePower += inputSignal[i] * inputSignal[i];
60     }
```

```

61     averagePower /= NUM_SAMPLES;
62     printf("Generated signal with average power = %f\n", averagePower);
63
64     // 打印输入和输出信号
65     printf("Input Signal: ");
66     for (int i = 0; i < NUM_SAMPLES; i++) {
67         printf("%f ", inputSignal[i]);
68     }
69
70     printf("\nOutput Signal (FIR Low Pass Filtered): ");
71     for (int i = 0; i < NUM_SAMPLES; i++) {
72         printf("%f ", outputSignal[i]);
73     }
74     // printf("%f ", outputSignal[0]);
75
76     return 0;
77 }
```

(圖九)(圖十)將隨機生成的 512 筆資料 scaling 成 power 為 1 的 input

```

79 // FIR 低通濾波器的實現
80 void firLowPassFilter(float input[], float output[], float filterCoeff[], int inputLength, int filterLength) {
81     for (int n = 0; n < inputLength; n++) {
82         output[n] = 0.0;
83         for (int k = 0; k < filterLength; k++) {
84             if (n - k >= 0) {
85                 output[n] += filterCoeff[k] * input[n - k]; //convolution
86             }
87         }
88     }
89 }
```

(圖十一)convolution

```

Generated signal with average power = 1.000000
Input Signal: -1.340897 1.251119 -0.844923 0.247925 -0.887348 1.179609 1.643725 1.056794 0.463018 1.432070 -0.197500 0.112583 -1.533250 -0.043409 0.106639 0.108163 -1.586210
1.347913 1.323558 0.431794 1.172345 -0.515141 1.021076 0.263678 -0.314157 -0.538758 0.094643 -0.265915 -0.357032 -0.65119 0.902878 0.689262 -1.020968 -1.624012 0.167142
602684 -0.129730 0.124132 0.109984 0.843797 -0.1647025 0.1151055 0.886590 -1.342705 1.683588 1.378432 -0.100818 0.521633 0.966550 -1.304256 -0.848987 -1.
210588 -1.295377 -0.784651 1.523307 1.197323 0.069293 0.277943 1.322774 0.179314 -0.639313 1.301270 1.006320 0.131201 -1.072033 -1.458300 -1.393583 -1.287966 1.654029 1.
031796 0.459251 0.709825 -0.495572 -1.013503 1.284369 0.487221 -0.135029 1.630933 -1.263616 -0.456713 -1.318913 -0.642574 1.247319 -0.045994 -1.654899 1.018750 -0.576685 0.
806087 1.023628 1.622964 0.538919 0.396396 1.253896 -1.186585 1.701861 0.243519 1.002769 0.292317 1.683487 -0.896294 -0.315223 0.217478 0.589907 1.513118 0.888889 -0.347308
1.042679 -1.243427 1.205611 -0.767853 -0.546861 -1.260231 1.574324 0.515154 0.838330 -1.586359 0.978542 -1.505648 0.043469 -0.219778 0.327659 -0.669412 -1.154548
729453 -1.118269 0.797789 -0.243855 -1.406766 1.379433 0.95821 -0.438654 0.349278 0.540543 -0.063598 -1.025652 1.166448 -0.2150657 -0.175825 0.461356 0.707910 0.710856 1.
122321 0.331916 -0.555407 1.506046 1.310367 0.214565 -0.100055 0.270378 -0.871462 -0.323179 -0.656657 0.321151 1.272916 -0.429397 -0.769408 0.374498 -0.692499 0.535040 -0.
347352 1.218868 0.270214 -1.446353 0.813023 -1.036573 1.346200 0.805085 1.572404 1.506537 -1.363393 1.070001 -1.304227 1.003981 1.118510 -0.874578 -0.074350 -1.508233 -0.
786311 -0.117208 0.265272 1.688133 1.231945 0.794815 -0.185625 0.662328 0.030310 1.19164 0.464438 0.436112 0.680750 0.683377 0.4333673 -0.455476 -1.096529 0.421859 -1.
300582 0.051459 0.489514 1.110717 0.802032 0.4080650 -0.848933 -1.073314 0.035361 1.691488 0.076417 1.486871 -0.886303 0.888352 1.389575 -0.439747 -0.246087 0.
878957 0.149962 -0.701663 0.317623 1.226954 1.691433 -1.508875 -1.595899 -0.717852 -1.207786 -0.746344 -0.303710 -1.177820 0.601206 -0.718670 -0.444709 0.420421 0.885413 1.
579721 1.147457 1.147457 -0.762154 0.243855 -1.406766 0.349278 0.540543 -0.063598 -1.025652 1.166448 -0.2150657 -0.175825 0.461356 0.707910 0.710856 1.
971718 1.142534 1.237153 -1.381915 0.101342 -0.225249 -0.539530 1.028218 -0.311826 0.822631 -0.630101 -1.697802 -0.021755 1.058503 0.493556 1.234631 1.463369 0.853483 -0.
178545 0.792765 -0.031971 -0.105141 -0.11859 0.120227 1.198454 -0.652974 -1.570851 0.254738 1.411017 0.139449 0.094071 0.381414 -0.204774 0.377686 -1.188925 -0.035571 0.678128 -0.
777231 -1.444828 1.128361 -0.1023729 -0.392280 1.189454 -0.652974 -1.570851 0.254738 1.411017 0.139449 0.094071 0.381414 -0.204774 0.377686 -1.188925 -0.035571 0.678128 -0.
751288 0.052117 0.064686 0.129652 -0.457165 1.165515 0.597363 -0.939691 0.923338 -0.743501 1.461609 0.2038473 1.273540 0.370664 0.238374 -0.256175 1.584688 0.117873 -0.983342 0.
984006 1.1598323 -1.399669 0.136657 0.109671 0.157500 0.647044 0.466729 0.4414388 -0.142248 -1.087245 -1.211816 -0.025378 0.564874 -0.308952 1.283474 0.333115 -0.485276 1.
013431 -1.362159 -0.708468 1.701466 0.401974 1.484921 1.289550 1.447402 1.612840 0.207678 1.335994 1.069628 0.754519 -0.889249 0.567537 1.207764 -0.964886 0.139459 1.103148
534875 0.139326 1.208357 0.496276 -0.067648 -0.372740 -0.107402 1.240512 0.240512 -0.453589 -0.585208 -1.91093 0.1052118 1.288926 -1.021865 0.185635 -1.384366 0.
949067 0.901188 0.725849 1.070175 -1.129866 0.125629 1.655649 1.235942 1.165515 0.109671 0.157500 0.647044 0.466729 0.4414388 -0.142248 -1.087245 -1.211816 -0.025378 0.564874 -0.308952 1.283474 0.333115 -0.485276 1.
563799 0.012575 1.4840426 -1.222558 -0.875585 1.399528 -1.3141829 1.216661 0.8465795 1.204774 1.362686 -0.466707 -1.430351 -1.463795 -1.314664 1.179940 0.933675 -1.538265 0.
060832 -0.466715 -1.672655 1.655649 1.370606 0.280486 0.378476 0.746996 0.855341 -0.273796 -0.864933 -1.705111 0.149167 1.406473 1.273540 0.370664 0.238374 -0.256175 1.584688 0.117873 -0.983342 0.
184651 0.189641 0.140220 -0.058941 -0.280826 -0.290199 -0.033306 0.245452 0.150249 -0.356195 -0.895385 -0.984360 -0.512349 0.547937 0.467161 0.040052 -0.
359783 -0.494419 -0.354972 -0.063170 0.343116 0.777056 0.991753 0.653626 -0.148074 -0.880992 -1.170599 -1.169616 -1.233250 -1.328704 -0.108942 -0.331242 0.549171 1.056058 1.
058225 0.715660 0.361486 0.208486 0.378476 0.746996 0.855341 -0.273796 -0.864933 -1.705111 0.149167 1.406473 1.273540 0.370664 0.238374 -0.256175 1.584688 0.117873 -0.983342 0.
318256 0.0901126 0.9300272 0.294585 -0.628571 -1.174482 -0.963300 -0.255457 0.209885 0.43916 -0.393353 -0.532649 -0.668651 0.695343 1.213670 1.243087 0.940244 0.552653 0.
304368 0.2467334 0.369199 0.669711 0.919506 0.862875 0.487420 -0.213896 -0.413264 0.064521 0.866594 0.1217446 0.812029 0.906364 -0.182445 0.135000 0.412366 0.093712 -0.619608
-0.912888 -0.393285 0.510302 0.925788 0.481618 -0.291058 -0.744547 -0.541528 -0.085665 0.058731 -0.194077 -0.545236 -0.0868470 -0.044295 -0.151648 -0.
146233 0.036943 0.2156804 0.226591 0.125742 0.042811 0.031033 -0.067348 -0.296579 -0.469011 -0.34788 0.266135 0.834398 0.959666 0.642635 0.302565 0.359017 0.727226 1.084922
0.806559 0.226387 -0.393318 -0.627322 -0.177470 0.298745 0.428149 -0.117139 -0.388385 0.495012 0.116399 -0.361923 -0.546638 0.495012 0.116399 -0.361923 -0.546638 0.
434086 0.721438 0.1472669 0.5123863 0.818472 -0.086293 -0.466919 -0.126743 0.464619 0.602095 0.484666 -0.808884 -1.311198 -0.1073168 -0.208627 0.728581 1.282115 1.247836 0.
799918 0.330833 0.077375 0.132998 0.341286 -0.420322 -0.466919 -0.126743 0.464619 0.602095 0.484666 -0.808884 -1.311198 -0.1073168 -0.208627 0.728581 1.282115 1.247836 0.
007484 -0.824801 -0.749596 0.155783 1.029678 0.1727344 0.328858 -0.241403 -0.135701 0.377955 0.746438 0.688071 0.321827 -0.069498 -0.227508 0.036991 0.654748 1.088997 0.
605799 -0.437677 -0.1358787 -0.568958 -1.175666 -0.711129 -0.532649 -0.465296 -0.340534 -0.898890 0.338179 0.962157 1.481947 1.614052 1.206001 0.452966 -0.351184 -0.
824848 -0.945772 -0.717065 -0.341336 -0.153294 -0.369288 -0.924093 -0.1332667 -1.197826 -0.544526 0.119580 0.420943 0.528728 0.668051 0.843365 0.099501 -0.500060 -0.
556275 0.584278 0.214529 -0.368675 -0.844277 -1.002522 -0.575373 -0.4490025 -0.340304 -0.898890 0.338179 0.962157 1.481947 1.614052 1.206001 0.452966 -0.351184 -0.
537745 0.081644 0.494986 0.483165 0.206143 0.143306 0.568379 0.128940 0.853041 0.127451 -0.520148 -0.445546 0.138108 0.498336 0.332856 -0.121654 -0.379700 0.298703 0.009931
0.538920 1.166881 1.469526 0.953878 -0.313576 -1.495346 -1.639706 -0.677579 0.474905 0.721022 -0.040133 -0.984035 -1.100891 -0.188927 0.093568 1.262572 0.522872 -0.706246 -1.
538800 -0.677854 -1.336545 -0.839218 -0.289312 0.218063 0.627438 0.714954 0.523496 0.247499 0.066411 0.013285 -0.018524 -0.113510 -0.389685 -0.846827 -1.324968 -1.611519 -1.
510087 -0.1058377 -0.559270 -0.388291 -0.685363 -1.198161 -0.472197 -1.354713 -0.947553 -0.492738 -0.082012 0.286122 0.533557 0.655005 0.703819 0.879198 1.077217 0.975083 0.
366068 0.501289 -0.106008 -0.959809 0.124828 0.041804 -0.389319 -0.639808 -0.467271 0.039126 0.550069 0.774728 0.549039 -0.060467 -0.649927 -0.825356 -0.490612 -0.
948489 -0.046865 -0.175699 0.006762 0.508280 0.857992 0.670294 0.238668
[Done] exited with code=0 in 2.464 seconds

```

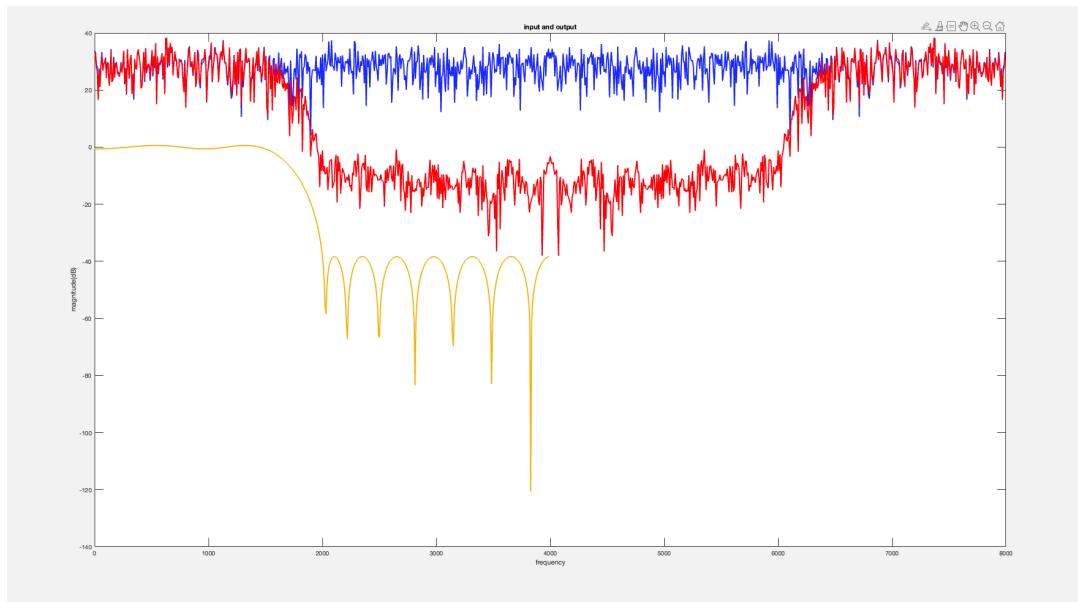
(圖十二)輸出結果

```
>> mean(abs(c_input).^2)
```

```
ans =
```

```
1.0000
```

在 matlab 中驗證 c 產生的 input average power 為 1



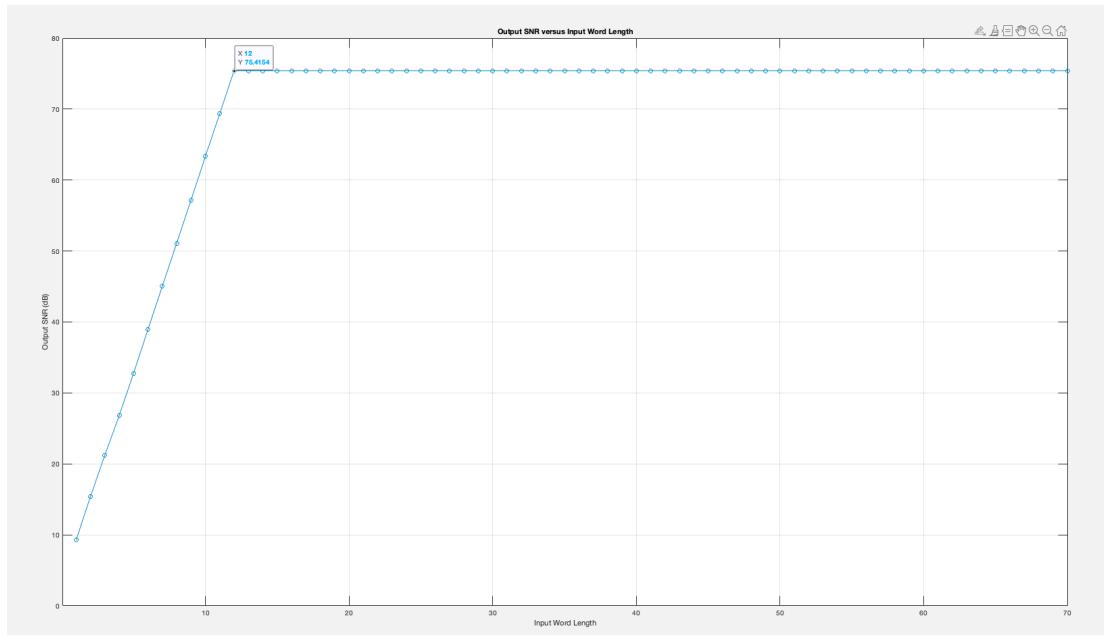
(圖十三)輸入與輸出頻譜對比

(ii)

- (1) 先將 input word-length quantize 為 fix point，整數為 4bits，小數為 12bits，共 16bits，再把 fix point input 跟 floating point input 比較：

```
>> inputWordLengths = 1:70;
% 初始化存储 SNR 的数组
outputSNR = zeros(size(inputWordLengths));
% 模拟不同输入字长下的 FIR 滤波器输出，并计算输出 SNR
for i = 1:length(inputWordLengths)
    inputWordLength = inputWordLengths(i);
    % 在这里模拟 FIR 滤波器的输出，得到outputSignal
    % 计算输出 SNR
    % 在这里计算 SNR，假设有变量 powerOfFloatingPointResult 表示浮点结果的功率
    % 以及变量 powerOfDifference 表示浮点和定点结果之间的差异的功率
    INSig=fi(quatizeinput,1,inputWordLength+4 ,inputWordLength,'RoundMode', 'floor');
    IN=double(INSig);
    OUTSig=filter(b,a,IN);
    powerOfDifference= sum(abs(output-OUTSig).^2);
    outputSNR(i) = 10 * log10(Pfloat / powerOfDifference);
end
% 绘制 SNR 与输入字长的关系图
figure;
plot(inputWordLengths, outputSNR, '-o');
xlabel('Input Word Length');
ylabel('Output SNR (dB)');
title('Output SNR versus Input Word Length');
grid on;
```

小數點位數



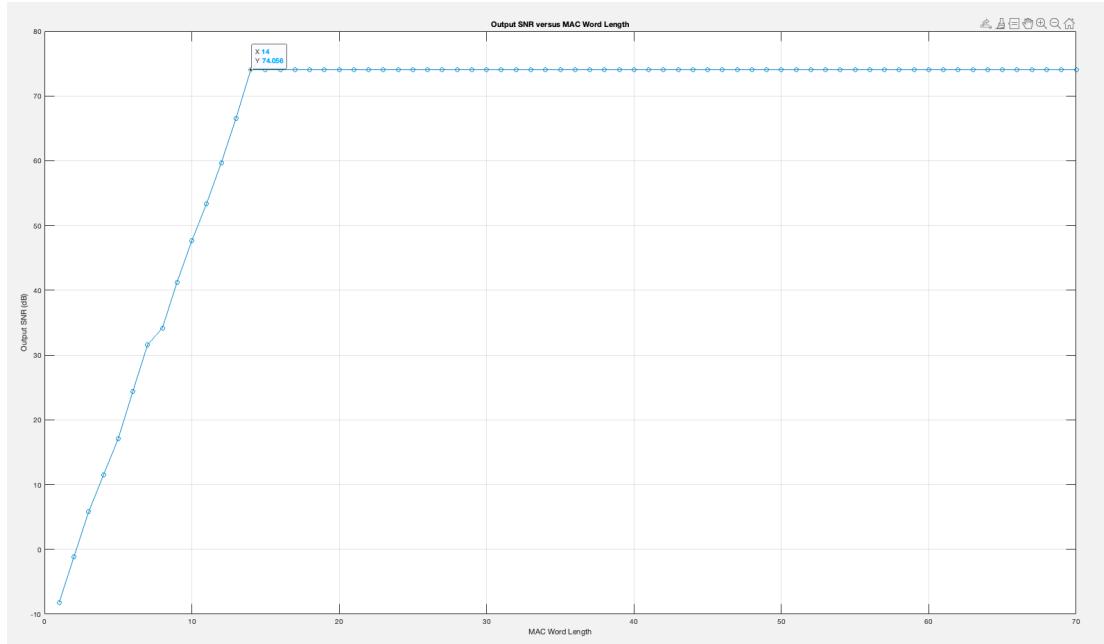
發現在小數點為 12bits 時開始 saturate，因此決定 fix point word-length 為 16bits，小數為 12bits

- (2) 將 filter coefficient quantize 為 16bits word-length 的 fix point，小數位為 14bits，跟 floating point 的 filter coefficient 比較：

```

>> macWordLengths = 1:70;      % 例如：MAC字長的範圍
snrResultsMAC = zeros(size(macWordLengths));
for i = 1:length(macWordLengths)
    macWordLength = macWordLengths(i);
    % 模擬具有當前MAC字長的FIR濾波器
    Qcoeff=fi(quantizecoeff,1,macWordLength+3,macWordLength,'RoundMode','floor'); ...
    Qfilt=double(Qcoeff); ...
    outputSignal = filter(Qfilt, 1, input); % X是您的輸入數據 小數點位數
    powerOfDifference2=sum(abs(output-outputSignal).^2); ...
    snrResultsMAC(i) = 10*log10(Pfloat/powerOfDifference2);
end
% 繪制 SNR 与输入字长的关系图
figure;
plot(macWordLengths, snrResultsMAC, '-o');
xlabel('MAC Word Length');
ylabel('Output SNR (dB)');
title('Output SNR versus MAC Word Length');
grid on;

```



發現在小數點為 14bits 時開始 saturate，因此決定 MAC word-length 為 16bits，小數為 14bits

(c)

(i) Verilog code:

(1) fir.sv:

先將每個 coefficient 存在 reg tap 裡，coefficient 的形式根據上一題的結果，先將所有小數換成整數，例如：0.307250976562500 換成十進制(包含 sign bit)是 00.01001110101010，將小數點去掉後十六進制為 13AA。每個 tap 相乘完的結果兩兩相加，最後到 output 總共有 37bits，其中小數位為 26 bits(input 12bits+coefficient 14bits)，再將輸出結果設為 26bits 小數。

```
1 `timescale 1ns / 10ps
2
3 module FIR( //使用AXI stream interface
4     input fir_clk,
5     input signed [15:0] input_signal, //切成4bits 12bits
6     output reg signed [36:0] filtered_signal //fir輸出
7 );
8
9 //21-tap FIR
10 reg signed [15:0] buff0, buff1, buff2, buff3, buff4, buff5, buff6, buff7, buff8, buff9, buff10, buff11, buff12, buff13, buff14, buff15, buff16, buff17, buff18, buff19, buff20;
11 wire signed [15:0] tap0, tap1, tap2, tap3, tap4, tap5, tap6, tap7, tap8, tap9, tap10, tap11, tap12, tap13, tap14, tap15, tap16, tap17, tap18, tap19, tap20;
12 reg signed [31:0] acc0, acc1, acc2, acc3, acc4, acc5, acc6, acc7, acc8, acc9, acc10, acc11, acc12, acc13, acc14, acc15, acc16, acc17, acc18, acc19, acc20 ;
13 reg signed [32:0] sum_0 [0:10];
14 reg signed [33:0] sum_1 [0:5];
15 reg signed [34:0] sum_2 [0:2];
16 reg signed [35:0] sum_3 [0:1];
17
18
19
20
21
22
23 //乘2^14 整數兩位 共16位
24 /* Taps for LPF running @ IMSPs with a cutoff freq of 400kHz */
25 assign tap0 = 16'hFF52; // -0.0106201171875000
26 assign tap1 = 16'hFD91; // -0.0380249023437500
27 assign tap2 = 16'hFDA9; // -0.0365600585937500
28 assign tap3 = 16'h0037; // 0.00335693359375000
29 assign tap4 = 16'h02E9; // 0.0454711914062500
30 assign tap5 = 16'h013E; // 0.0194091796875000
31 assign tap6 = 16'hFC17; // -0.0610961914062500
32 assign tap7 = 16'hFB2E; // -0.0753173828125000
33 assign tap8 = 16'h04B4; // 0.0734863281250000
34 assign tap9 = 16'h13AA; // 0.307250976562500
35 assign tap10 = 16'h1B01; // 0.421936035156250
36 assign tap11 = 16'h13AA; // 0.307250976562500
37 assign tap12 = 16'h04B4; // 0.0734863281250000
38 assign tap13 = 16'hFB2E; // -0.0753173828125000
39 assign tap14 = 16'hFC17; // -0.0610961914062500
40 assign tap15 = 16'h013E; // 0.0194091796875000
41 assign tap16 = 16'h02E9; // 0.0454711914062500
42 assign tap17 = 16'h0037; // 0.00335693359375000
43 assign tap18 = 16'hFDA9; // -0.0365600585937500
44 assign tap19 = 16'hFD91; // -0.0380249023437500
45 assign tap20 = 16'hFF52; // -0.0106201171875000
```

```

53      always @ (posedge fir_clk)
54          begin
55              buff0 <= input_signal;
56              buff1 <= buff0;
57              buff2 <= buff1;
58              buff3 <= buff2;
59              buff4 <= buff3;
60              buff5 <= buff4;
61              buff6 <= buff5;
62              buff7 <= buff6;
63              buff8 <= buff7;
64              buff9 <= buff8;
65              buff10 <= buff9;
66              buff11 <= buff10;
67              buff12 <= buff11;
68              buff13 <= buff12;
69              buff14 <= buff13;
70              buff15 <= buff14;
71              buff16 <= buff15;
72              buff17 <= buff16;
73              buff18 <= buff17;
74              buff19 <= buff18;
75              buff20 <= buff19;
76      end

```

每一級 tap 的 delay

```

81      always @ (posedge fir_clk)
82          begin
83
84              acc0 <= tap0 * buff0;
85              acc1 <= tap1 * buff1;
86              acc2 <= tap2 * buff2;
87              acc3 <= tap3 * buff3;
88              acc4 <= tap4 * buff4;
89              acc5 <= tap5 * buff5;
90              acc6 <= tap6 * buff6;
91              acc7 <= tap7 * buff7;
92              acc8 <= tap8 * buff8;
93              acc9 <= tap9 * buff9;
94              acc10 <= tap10 * buff10;
95              acc11 <= tap11 * buff11;
96              acc12 <= tap12 * buff12;
97              acc13 <= tap13 * buff13;
98              acc14 <= tap14 * buff14;
99              acc15 <= tap15 * buff15;
100             acc16 <= tap16 * buff16;
101             acc17 <= tap17 * buff17;
102             acc18 <= tap18 * buff18;
103             acc19 <= tap19 * buff19;
104             acc20 <= tap20 * buff20;
105         end

```

```

107     always @ (posedge fir_clk)
108         begin
109             sum_0[0] <= acc0 + acc1;
110             sum_0[1] <= acc2 + acc3;
111             sum_0[2] <= acc4 + acc5;
112             sum_0[3] <= acc6 + acc7;
113             sum_0[4] <= acc8 + acc9;
114             sum_0[5] <= acc10 + acc11;
115             sum_0[6] <= acc12 + acc13;
116             sum_0[7] <= acc14 + acc15;
117             sum_0[8] <= acc16 + acc17;
118             sum_0[9] <= acc18 + acc19;
119             sum_0[10] <= acc20;
120         end
121
122     always @ (posedge fir_clk)
123         begin
124             sum_1[0] <= sum_0[0] + sum_0[1];
125             sum_1[1] <= sum_0[2] + sum_0[3];
126             sum_1[2] <= sum_0[4] + sum_0[5];
127             sum_1[3] <= sum_0[6] + sum_0[7];
128             sum_1[4] <= sum_0[8] + sum_0[9];
129             sum_1[5] <= sum_0[10];
130         end
131
132     always @ (posedge fir_clk)
133         begin
134             sum_2[0] <= sum_1[0] + sum_1[1];
135             sum_2[1] <= sum_1[2] + sum_1[3];
136             sum_2[2] <= sum_1[4] + sum_1[5];
137         end

```

tap 的輸出兩兩相加

```

139     always @ (posedge fir_clk)
140         begin
141             sum_3[0] <= sum_2[0] + sum_2[1];
142             sum_3[1] <= sum_2[2];
143         end
144
145
146     /* Accumulate stage of FIR */
147     always @ (posedge fir_clk)
148         begin
149             // filtered_signal <= acc0 + acc1 + acc2 + acc3 + acc4 + acc5 + acc6 + acc7 ;
150             // filtered_signal <= sum_4;
151             filtered_signal <= sum_3[0] + sum_3[1];
152
153         end
154
155     endmodule

```

(2) fir_tb.v:

在這裡使用 cordic IP 產生兩個分別為 1kHz 及 2kHz 的 sine wave，
cordic clock 為 50MHz，取樣頻率 8kHz，input 用兩個 sine wave 相
加表示，sine wave 為 15 bits，因此 input 最多可以用 16 bits 表示。

```
1  `timescale 1ns / 10ps
2
3  module tb_FIR;
4
5      localparam CORDIC_CLK_PERIOD = 20; // To create 50 MHz CORDIC sampling clock
6      localparam FIR_CLK_PERIOD = 1250; // To create 100 MHz FIR lowpass filter sampling clock
7      localparam FIR_CLK_PERIOD = 125000; // To create 8kHz FIR lowpass filter sampling clock
8      localparam signed [15:0] PI_POS = 16'h5488; // +pi in fixed-point 1.2.13
9      localparam signed [15:0] PI_NEG = 16'h9B78; // -pi in fixed-point 1.2.13
10     localparam PHASE_INC_1KHZ = 1; // Phase jump for 1kHz sine wave synthesis
11     //localparam PHASE_INC_2KHZ = 3; // Phase jump for 2kHz sine wave synthesis 下降10倍
12     localparam PHASE_INC_2KHZ = 2; // Phase jump for 2kHz sine wave synthesis 下降10倍
13     reg cordic_clk = 1'b0;
14     reg fir_clk = 1'b0;
15     reg phase_tvalid = 1'b0;
16     reg signed [15:0] phase_1KHz = 0; // 1kHz phase sweep, 1.2.13
17     reg signed [15:0] phase_2KHz = 0; // 2kHz phase sweep, 1.2.13
18     wire sincos_1KHz_tvalid;
19     wire signed [15:0] sin_1KHz, cos_1KHz; // 1.1.14 1kHz sine/cosine
20     wire sincos_2KHz_tvalid;
21     wire signed [15:0] sin_2KHz, cos_2KHz; // 2.1.24 2kHz sine/cosine
22
23     reg signed [15:0] input_signal = 0; // Resampled 1kHz sine + 2kHz sine, 1.1.14
24     wire signed [36:0] filtered_signal; // Filtered signal output from FIR lowpass filter
25
26     //Synthesize 1KHz sinc
27     cordic_0 cordic_inst_0(
28         .aclk          (cordic_clk),
29         .s_axis_phase_tvalid (phase_tvalid),
30         .s_axis_phase_tdata (phase_1KHz),
31         .m_axis_dout_tvalid (sincos_1KHz_tvalid),
32         .m_axis_dout_tdata ({sin_1KHz, cos_1KHz})
33     );
34     //Synthesize 2KHz sinc
35     cordic_0 cordic_inst_1(
36         .aclk          (cordic_clk),
37         .s_axis_phase_tvalid (phase_tvalid),
38         .s_axis_phase_tdata (phase_2KHz),
39         .m_axis_dout_tvalid (sincos_2KHz_tvalid),
40         .m_axis_dout_tdata ({sin_2KHz, cos_2KHz})
41     );
42
43     //Phase sweep
44     always @(posedge cordic_clk)
45     begin
46         phase_tvalid <= 1'b1;
47         // Sweep phase to synthesize 1kHz sine
48         if (phase_1KHz + PHASE_INC_1KHZ < PI_POS) begin
49             phase_1KHz <= phase_1KHz + PHASE_INC_1KHZ;
50         end
51         else
52             begin
53                 phase_1KHz <= PI_NEG + (phase_1KHz+PHASE_INC_1KHZ - PI_POS);
54             end
55     end
```

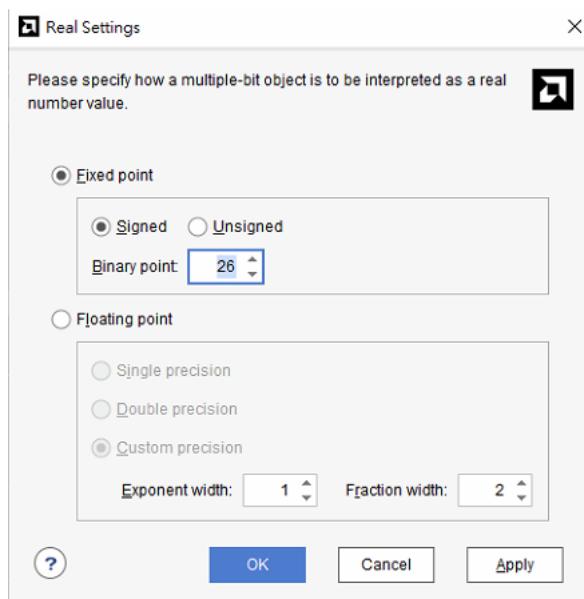
```

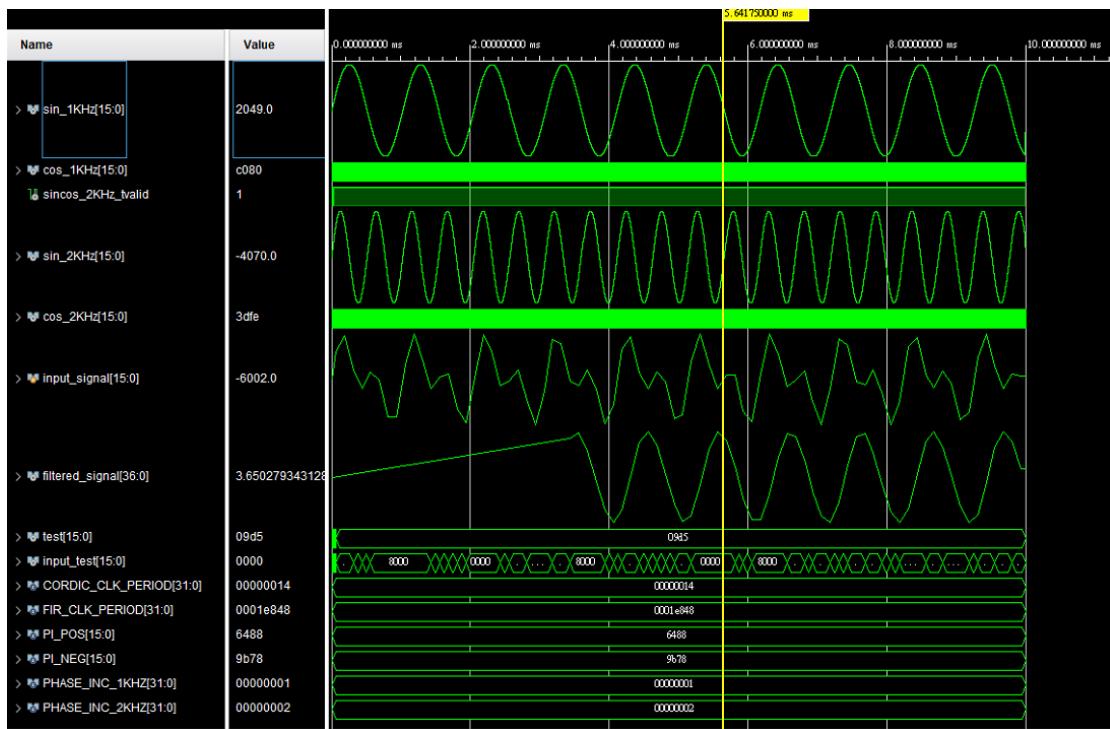
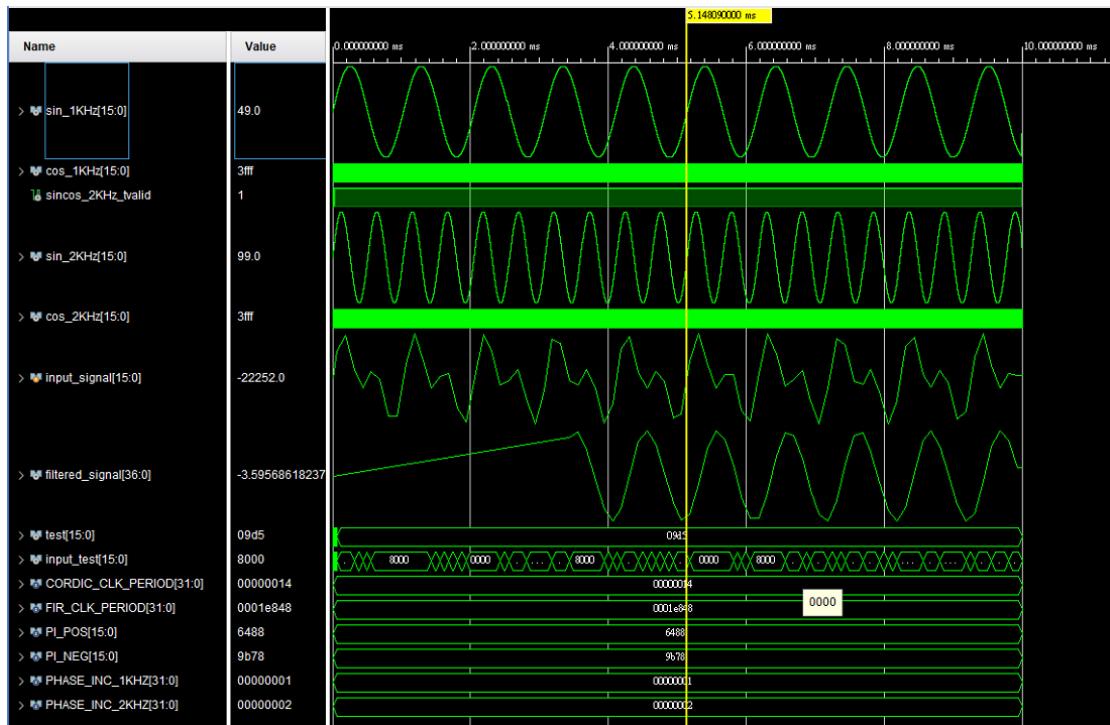
57      // Sweep phase to synthesize 2kHz sinc
58      if (phase_2kHz + PHASE_INC_2kHz <= PI_POS) begin
59          phase_2kHz <= phase_2kHz + PHASE_INC_2kHz;
60      end
61      else
62      begin
63          phase_2kHz <= PI_NEG + (phase_2kHz+PHASE_INC_2kHz - PI_POS);
64      end
65  end
66
67      // Create 50MHz Cordic clock 20ns
68  always begin
69      cordic_clk = #(CORDIC_CLK_PERIOD/2) ~cordic_clk;
70  end

75  always
76  begin
77      fir_clk = #(FIR_CLK_PERIOD/2) ~fir_clk;
78  end
79
80  always @(posedge fir_clk)
81  begin
82      // input_signal <= (sin_1kHz + sin_2kHz) / 2;
83      input_signal <= (sin_1kHz + sin_2kHz);
84  end
85
86      /* Instantiate FIR module to test. */
87      FIR FIR_i(
88          .clk(fir_clk),
89          .input_signal(input_signal), //input
90          .filtered_signal(filtered_signal));
91
92
93 endmodule

```

(3) output waveform:





(ii) circuit speed and resource number:

```

1 : create_clock -period 8.000 -name fir_clk -waveform {0.000 4.000} [get_ports fir_clk]
2 :

```

Utilization				Post-Synthesis	Post-Implementation	Power		Summary	On-Chip	
				Graph		Table				
Resource	Utilization	Available	Utilization %				Total On-Chip Power:	0.188 W		
LUT	213	53200	0.40				Junction Temperature:	27.2 °C		
LUTRAM	40	17400	0.23				Thermal Margin:	57.8 °C (4.8 W)		
FF	382	106400	0.36				Effective 9JA:	11.5 °C/W		
DSP	26	220	11.82				Power supplied to off-chip devices:	0 W		
IO	54	125	43.20				Confidence level:	Low		
BUFG	1	32	3.13				Implemented Power Report			

Design Timing Summary

Setup	Hold	Pulse Width
Worst Negative Slack (WNS): 4.011 ns	Worst Hold Slack (WHS): 0.047 ns	Worst Pulse Width Slack (WPWS): 3.020 ns
Total Negative Slack (TNS): 0.000 ns	Total Hold Slack (THS): 0.000 ns	Total Pulse Width Negative Slack (TPWS): 0.000 ns
Number of Failing Endpoints: 0	Number of Failing Endpoints: 0	Number of Failing Endpoints: 0
Total Number of Endpoints: 1826	Total Number of Endpoints: 1826	Total Number of Endpoints: 489

All user specified timing constraints are met.