COMP1521 24T2 — Bitwise Operators

https://www.cse.unsw.edu.au/~cs1521/24T2/

Bitwise Operators

- CPUs typically provide instructions which operate on individual bits of values.
 - MIPS provides 13 bit manipulation instructions
 - · other CPUs can provide more
- C provides 6 operators which operate on individual bits of values

```
x & y // bitwise and
x | y // bitwise or
x ^ y // bitwise exclusive-or (XOR)
~ x // bitwise not
x << n // left shift
x >> n // right shift
```

Bitwise AND: &

The & operator

- takes two values (1,2,4,8 bytes), treats as sequence of bits
- performs logical AND on each corresponding pair of bits
- \cdot result contains same number of bits as inputs

	00100111	ΑN	D	П	0	1
ઠ	11100011			۱-		
			0	L	0	0
	00100011		1	Ī	0	1

- Useful for:
 - · checking whether a particular bit is set
 - setting particular bit(s) to 0

Code Example: Checking for Odd Numbers with &

the obvious way to check for odd numbers in C

```
int is_odd(int n) {
    return n % 2 != 0;
}
```

• we *could* use **&** to achieve the same thing:

```
int is_odd(int n) {
    return n & 1;
}
```

- but should we?
 - · no write obvious readable code
 - · rely on compiler to generate fastest assembler
 - if andi instruction is faster than rem, compiler will generate it

Bitwise OR: |

The | operator

- \cdot takes two values (1,2,4,8 bytes), treats as sequence of bits
- performs logical OR on each corresponding pair of bits
- result contains same number of bits as inputs

	00100111	OR		0	1
1	11100011		۱-		
		Θ	l	0	1
	11100111	1	ı	1	1

- Useful for:
 - setting particular bit(s) to 1

Bitwise NEG: ~

The ~ operator

- takes a single value (1,2,4,8 bytes), treats as sequence of bits
- performs logical negation of each bit
- · result contains same number of bits as input

- Useful for:
 - · creating particular bit patterns

Bitwise XOR: ^

The ^ operator

- takes two values (1,2,4,8 bytes), treats as sequence of bits
- performs logical XOR on each corresponding pair of bits
- result contains same number of bits as inputs

```
00100111 XOR | 0 1

`11100011 ---|----

----- 0 | 0 1

11000100 1 | 1 0
```

- Useful for:
 - generating hashes
 - cryptography
 - · graphics operations

Left Shift: <<

The << operator

- takes a single value (1,2,4,8 bytes), treats as sequence of bits
- also takes a small positive integer x
- moves (shifts) each bit x positions to the left
- left-end bit vanishes; right-end bit replaced by zero

```
00100111 << 2 00100111 << 8 ------ 10011100 00000000
```

- Useful for:
 - creating particular bit patterns
 - · multiplying by power of two

Right Shift: >>

The >> operator

- takes a single value (1,2,4,8 bytes), treats as sequence of bits
- also takes a small positive integer x
- moves (shifts) each bit x positions to the right
- right-end bit vanishes; left-end bit replaced by zero(*)
- shifts involving negative values are not portable (implementation defined)
- · common source of bugs in COMP1521 and elsewhere
- always use unsigned values/variables to be safe/portable.

- - Useful for:
 - · loops which need to process one bit at a time
 - · dividing by power of two

MIPS - Bit Manipulation Instructions

assembly	meaning	bit pattern
and r_d, r_s, r_t	r_d = r_s & r_t	000000ssssstttttddddd00000100100
or r_d , r_s , r_t	r_d = r_s l r_t	000000ssssstttttdddddd0000100101
$\mathbf{xor}\ r_d, r_s, r_t$	r_d = r_s ^ r_t	000000ssssstttttdddddd00000100110
$\operatorname{nor} r_d, r_s, r_t$	$r_d = {\scriptscriptstyle \sim} \left(r_s \mid r_t\right)$	000000ssssstttttdddddd00000100111
$andi\ r_t, r_s, \mathtt{I}$	r_t = r_s & I	001100ssssstttttIIIIIIIIIIIIII
$\mathtt{ori}\ r_t, r_s, \mathtt{I}$	r_t = r_s l I	001101ssssstttttIIIIIIIIIIIIII
$\mathbf{xori}\; r_t, r_s, \mathbf{I}$	r_t = r_s ^ I	001110ssssstttttIIIIIIIIIIIII
$ \cot r_d, r_s $	r_d = ~ r_s	pseudo-instruction

mipsy translates not r_d , r_s to nor r_d , r_s , \$0

MIPS - Shift Instructions

assembly	meaning	bit pattern
$\overline{\operatorname{sllv} r_d, r_t, r_s}$	r_d = $r_t \ll r_s$	000000ssssstttttddddd00000000100
$\operatorname{srlv} r_d, r_t, r_s$	r_d = $r_t \gg r_s$	000000ssssstttttdddddd0000000110
$\operatorname{\mathtt{srav}} r_d, r_t, r_s$	r_d = $r_t \gg r_s$	000000ssssstttttdddddd0000000111
sll r_d , r_t , I	r_d = r_t « I	00000000000ttttdddddIIII1000000
$\mathtt{srl}\ r_d, r_t, \mathtt{I}$	r_d = r_t » I	00000000000tttttdddddIIII
$\operatorname{sra} r_d, r_t, \operatorname{I}$	r_d = r_t » I	00000000000tttttdddddIIIII000011

- srl and srlv shift zeros into most-significant bit
 - this matches shift in C of **unsigned** value
- sra and srav propagate most-significant bit
 - this ensure shifting a negative number divides by 2
- mipsy provides rol and ror pseudo-instructions which rotate bits
 - real instructions on some MIPS versions
 - no simple C equivalent

bitwise.c: showing results of bitwise operation

```
$ dcc bitwise.c print bits.c -o bitwise
$ ./bitwise
Enter a: 23032
Enter b: 12345
Enter c: 3
     a = 01011001111111000 = 0x59f8 = 23032
     b = 0011000000111001 = 0x3039 = 12345
    \sim a = 1010011000000111 = 0xa607 = 42503
 a & b = 00010000000111000 = 0x1038 = 4152
     b = 01111001111111001 = 0x79f9 = 31225
 a ^{\circ} b = 0110100111000001 = 0x69c1 = 27073
a >> c = 0000101100111111 = 0x0b3f = 2879
a \ll c = 11001111111000000 = 0xcfc0 = 53184
```

source code for bitwise.

course code for print, bits a course code for print, bits b

bitwise.c: code uint16 t a = 0;

```
printf("Enter a: ");
scanf("%hd". &a):
uint16 t b = 0:
printf("Enter b: ");
scanf("%hd", &b);
printf("Enter c: ");
int c = 0:
scanf("%d", &c);
print bits hex(" a = ". a);
print_bits_hex(" b = ", b);
print_bits_hex(" ~a = ", ~a);
print bits hex(" a & b = ", a & b);
print bits hex(" a | b = ". a | b):
print bits hex(" a ^ b = ", a ^ b);
print bits hex("a >> c = ".a >> c):
print bits hex("a << c = ".a << c):
```

```
$ dcc shift as multiply.c print bits.c -o shift as multiply
$ ./shift as multiply 4
2 to the power of 4 is 16
$ ./shift as multiply 20
2 to the power of 20 is 1048576
In binary it is: 000000000010000000000000000000
$ ./shift as multiply 31
2 to the power of 31 is 2147483648
```

```
int n = strtol(argv[1], NULL, 0);
uint32 t power of two;
int n bits = 8 * sizeof power of two;
if (n >= n bits) {
    fprintf(stderr, "n is too large\n");
    return 1;
power of two = 1:
power of two = power of two << n;
printf("2 to the power of %d is %u\n". n. power of two):
printf("In binary it is: "):
print bits(power of two, n bits);
printf("\n");
```

source code for shift as multiply c

set_low_bits.c: using << and - to set low n bits</pre>

```
$ dcc set low bits.c print bits.c -o n ones
$ ./set_low_bits 3
The bottom 3 bits of 7 are ones:
000000000000000000000000000000111
$ ./set low bits 19
The bottom 19 bits of 524287 are ones:
000000000000111111111111111111111
$ ./set low bits 29
The bottom 29 bits of 536870911 are ones:
```

```
int n = strtol(argv[1], NULL, 0);
uint32 t mask:
int n bits = 8 * sizeof mask;
assert(n \ge 0 \& n < n \text{ bits});
mask = 1;
mask = mask - 1;
printf("The bottom %d bits of %u are ones:\n", n, mask);
print bits(mask, n bits);
printf("\n");
source code for set low bits c
```

```
$ dcc set_bit_range.c print_bits.c -o set_bit_range
$ ./set bit range 0 7
Bits 0 to 7 of 255 are ones:
000000000000000000000000011111111
$ ./set bit range 8 15
Bits 8 to 15 of 65280 are ones:
000000000000000011111111100000000
$ ./set bit range 8 23
Bits 8 to 23 of 16776960 are ones:
0000000011111111111111111100000000
$ ./set bit range 1 30
Bits 1 to 30 of 2147483646 are ones:
```

set bit range.c: using << and - to set a range of bits

```
int low_bit = strtol(argv[1], NULL, 0);
int high bit = strtol(argv[2], NULL, 0);
uint32_t mask;
int n bits = 8 * sizeof mask:
int mask_size = high_bit - low_bit + 1;
mask = 1:
mask = mask << mask size;</pre>
mask = mask - 1;
mask = mask << low bit:</pre>
printf("Bits %d to %d of %u are ones:\n", low bit, high bit, mask);
print bits(mask, n bits);
printf("\n");
```

```
$ dcc extract bit range.c print bits.c -o extract bit range
$ ./extract bit range 4 7 42
Value 42 in binary is:
Bits 4 to 7 of 42 are:
0010
$ ./extract bit range 10 20 123456789
Value 123456789 in binary is:
00000111010110111100110100010101
Bits 10 to 20 of 123456789 are:
11011110011
```

extract_bit_range.c: extracting a range of bits

```
int mask_size = high bit_- low bit_+ 1:
mask = 1:
mask = mask << mask size:</pre>
mask = mask - 1:
mask = mask << low bit:</pre>
uint32 t extracted bits = value & mask:
extracted bits = extracted bits >> low bit:
printf("Value %u in binary is:\n". value):
print bits(value, n bits);
printf("\n"):
printf("Bits %d to %d of %u are:\n", low_bit, high_bit, value);
print bits(extracted bits, mask size);
printf("\n");
```

```
// print the bottom how many bits bits of value
void print bits(uint64 t value, int how many bits) {
    // print bits from most significant to least significant
    for (int i = how_many_bits - 1; i >= 0; i--) {
        int bit = get nth bit(value, i);
        printf("%d". bit);
// extract the nth bit from a value
int get_nth_bit(uint64_t value, int n) {
    uint64_t shifted_value = value >> n;
    int bit = shifted value & 1:
    return bit;
```

print bits.c: extracting the n-th bit of a valued

print_int_in_hex.c: print an integer in hexadecimal

· write C to print an integer in hexadecimal instead of using:

```
printf("%x", n)
$ dcc print int in hex.c -o print int in hex
$ ./print_int_in_hex
Enter a positive int: 42
42 = 0 \times 00000002A
$ ./print int in hex
Enter a positive int: 65535
65535 = 0 \times 0000  FFFF
$ ./print int in hex
Enter a positive int: 3735928559
3735928559 = 0xDEADBEEF
```

source code for print int in hexic

```
int main(void) {
   uint32 t a = 0:
    printf("Enter a positive int: ");
    scanf("%u", &a);
    printf("%u = 0x", a);
   print hex(a);
   printf("\n");
    return 0;
```

```
print int in hex.c: print_hex - extracting digit
int n hex digits = 2 * (sizeof n);
// print hex digits from most significant to least significant
for (int which digit = n hex digits - 1; which digit >= 0; which digit--) {
    // shift value across so hex digit we want
    // is in bottom 4 bits
    int bit shift = 4 * which digit;
    uint32 t shifted value = n >> bit shift:
    int hex_digit = shifted_value & 0xF;
    int hex digit ascii = "0123456789ABCDEF"[hex digit];
    putchar(hex_digit_ascii);
```

int_to_hex_string.c: convert int to a string of hex digits

· Write C to convert an integer to a string containing its hexadecimal digits.

Could use the C library function **snprintf** to do this.

```
$ dcc int to hex string.c -o int to hex string
$ ./int to hex string
$ ./int to hex string
Enter a positive int: 42
42 = 0 \times 00000002A
$ ./int to hex string
Enter a positive int: 65535
65535 = 0 \times 00000 FFFF
$ ./int to hex string
Enter a positive int: 3735928559
3735928559 = 0xDEADBEEF
```

source code for int_to_hex_string.c

```
int main(void) {
   uint32 t a = 0:
    printf("Enter a positive int: ");
    scanf("%u", &a);
    char *hex_string = int_to_hex_string(a);
    printf("%u = 0x%s\n", a, hex_string);
    free(hex_string);
    return 0;
```

source code for int to hex string c

int to hex string.c: convert int to a string of hex digits

```
int n hex digits = 2 * (sizeof n);
char *string = malloc(n hex digits + 1):
for (int which_digit = 0; which_digit < n_hex_digits; which_digit++) {</pre>
    // shift value across so hex digit we want
    int bit shift = 4 * which digit:
    uint32 t shifted value = n >> bit shift:
    int hex_digit = shifted_value & 0xF;
    int hex_digit_ascii = "0123456789ABCDEF"[hex_digit];
    int string position = n hex digits - which digit - 1:
    string[string position] = hex digit ascii:
string[n hex digits] = 0:
return string;
```

hex_string_to_int.c: convert hex digit string to int

• As an exercise write C to convert an integer to a string containing its hexadecimal digits.

Could use the C library function **strtol** to do this.

```
$ dcc hex_string_to_int.c -o hex_string_to_int
$ dcc hex_string_to_int.c -o hex_string_to_int
$ ./hex_string_to_int 2A
2A hexadecimal is 42 base 10
$ ./hex_string_to_int FFFF
FFFF hexadecimal is 65535 base 10
$ ./hex_string_to_int DEADBEEF
DEADBEEF hexadecimal is 3735928559 base 10
$
```

source code for hex string to int.c

```
int main(int argc, char *argv[]) {
    if (argc != 2) {
        fprintf(stderr, "Usage: %s <hexadecimal-number>\n", argv[0]);
        return 1;
    char *hex string = argv[1];
    uint32_t u = hex_string_to_int(hex_string);
    printf("%s hexadecimal is %u base 10\n", hex string, u);
    return 0;
```

source code for hex_string_to_int.c

```
uint32_t hex_string_to_int(char *hex_string) {
    uint32 t value = 0:
    for (int i = 0; hex string[i] != 0; i++) {
        int ascii hex digit = hex string[i];
        int digit_as_int = hex_digit_to_int(ascii_hex_digit);
        value = value << 4:</pre>
        value = value | digit as int;
    return value;
```

source code for hex_string_to_int.c

hex_string_to_int.c: convert single hex digit to int

```
int hex digit to int(int ascii digit) {
   if (ascii digit >= '0' && ascii digit <= '9') {
        // the ASCII characters '0' .. '9' are contiguous
        // so subtract the ASCII value for '0' yields the corresponding integer
        return ascii digit - '0':
    if (ascii digit >= 'A' && ascii digit <= 'F') {
        return 10 + (ascii digit - 'A');
    fprintf(stderr. "Bad digit '%c'\n". ascii digit):
    exit(1);
```

shift_bug.c: bugs to avoid

```
// below operations are undefined for a signed type
int16 t i:
i = i >> 1: // undefined - shift of a negative value
printf("%d\n", i);
i = i << 1; // undefined - shift of a negative value
printf("%d\n". i):
i = 32767:
i = i << 1: // undefined - left shift produces a negative value
uint64 t j;
j = 1 << 33; // undefined - constant 1 is an int</pre>
j = ((uint64 t)1) << 33; // ok
```

source code for shift_bug.c

xor.c: fun with xor

```
int xor value = strtol(argv[1], NULL, 0);
if (xor value < 0 || xor value > 255) {
    fprintf(stderr, "Usage: %s <xor-value>\n", argv[0]);
    return 1;
int c;
while ((c = getchar()) != EOF) {
    int xor_c = c ^ xor_value;
    putchar(xor_c);
```

xor.c: fun with xor

```
$ echo Hello Andrew|xor 42
bOFFE
kDNXO] $ echo Hello Andrew|xor 42|cat -A
bOFFE$
kDNXO] $
$ echo Hello |xor 42
bOFFE $ echo -n 'bOFFE 'lxor 42
Hello
$ echo Hello|xor 123|xor 123
Hello
```

pokemon.c: using an int to represent a set of values #define FIRE TYPE 0x0001 #define FIGHTING TYPE 0x0002 #define WATER TYPE 0x0004 #define FLYING TYPE 0x0008 #define POISON TYPE 0x0010 #define ELECTRIC TYPE 0x0020 #define GROUND TYPE 0x0040 #define PSYCHIC TYPE 0x0080 #define ROCK TYPE 0x0100 #define ICE TYPE 0x0200 #define BUG TYPE 0x0400 #define DRAGON TYPE 0x0800 #define GHOST TYPE 0x1000 #define DARK TYPE 0x2000 #define STEEL TYPE 0x4000 #define FAIRY TYPE 0x8000 37 / 47

pokemon.c: using an int to represent a set of values

- simple example of a single integer specifying a set of values
- · interacting with hardware often involves this sort of code

```
uint16_t our_pokemon = BUG_TYPE | POISON_TYPE | FAIRY_TYPE;

// example code to check if a pokemon is of a type:
if (our_pokemon & POISON_TYPE) {
    printf("Poisonous\n"); // prints
}
if (our_pokemon & GHOST_TYPE) {
    printf("Scary\n"); // does not print
}
```

source code for pokemon.c

```
our pokemon |= GHOST TYPE;
// example code to remove a type from a pokemon
our pokemon δ= ~ POISON TYPE;
printf(" our pokemon type (2)\n");
if (our pokemon & POISON TYPE) {
    printf("Poisonous\n"); // does not print
if (our pokemon & GHOST TYPE) {
    printf("Scary\n"); // prints
source code for pokemonic
```

```
$ dcc bitset.c print_bits.c -o bitset
$ ./bitset
Set members can be 0-63, negative number to finish
Enter set a: 1 2 4 8 16 32 -1
Enter set b: 5 4 3 33 -1
a = \{1.2.4.8.16.32\}
b = \{3.4.5.33\}
a union b = \{1,2,3,4,5,8,16,32,33\}
a intersection b = {4}
cardinality(a) = 6
is member(42, a) = 0
```

```
printf("Set members can be 0-%d, negative number to finish\n".
      MAX SET MEMBER):
set a = set read("Enter set a: ");
set b = set read("Enter set b: "):
print bits hex("a = ". a);
print bits hex("b = ", b);
set print("a = ", a);
set print("b = ", b);
set print("a union b = ". set union(a. b));
set print("a intersection b = ", set intersection(a, b));
printf("cardinality(a) = %d\n". set cardinality(a));
printf("is member(42, a) = %d\n", (int)set member(42, a));
```

source code for bitset.c

bitset.c: common set operations set set add(int x, set a) { return a | ((set)1 << x); set set union(set a, set b) { return a | b: set set intersection(set a, set b) { return a & b: int set_member(int x, set a) { assert(x >= 0 && \times < MAX SET MEMBER); return (a >> x) & 1;

```
// return size of set
int set_cardinality(set a) {
    int n_members = 0;
    while (a != 0) {
        n_members += a & 1;
        a >>= 1;
    }
    return n_members;
}
```

```
set set_read(char *prompt) {
    printf("%s", prompt);
    set a = EMPTY_SET;
    int x;
    while (scanf("%d", &x) == 1 && x >= 0) {
        a = set_add(x, a);
    }
    return a;
}
```

bitset.c: set output void set print(char *description, set a) { printf("%s", description); printf("{"): int n printed = 0: for (int i = 0; i < MAX_SET_MEMBER; i++) { if (set member(i, a)) { if (n_printed > 0) { printf(","); printf("%d", i); n printed++;

printf("}\n");

Exercise: Bitwise Operations

Given the following variable declarations:

```
// a signed 8-bit value
unsigned char x = 0x55;
unsigned char y = 0xAA;
```

What is the value of each of the following expressions:

- · (x & y) (x ^ y)
- \cdot (x << 1) (y << 1)
- (x >> 1) (y >> 1)

Exercise: Bit-manipulation

Assuming 8-bit quantities and writing answers as 8-bit bit-strings:

What are the values of the following:

- · 25, 65, ~0, ~~1, 0xFF, ~0xFF
- · (01010101 & 10101010), (01010101 | 10101010)
- · (x & ~x), (x | ~x)

How can we achieve each of the following:

- ensure that the 3rd bit from the RHS is set to 1
- ensure that the 3rd bit from the RHS is set to 0