Project #3B: Solving Systems of Linear Equations

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MA375
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Matrix Equation A:

Using the given matrices for matrix equation A and the gaussian elimination method created, I was able to achieve the solution:

 $[0 \ 1 \ 2 \ 3 \ 4]^T$

```
[henry@Henrys-MacBook-Pro project3 % python3 GaussianElimination.py
MA375 - Project #3B
Henry Song
1. Use matrix equation A from Project 3B
2. Use matrix equation B from Project 3B
3. Use custom matrix equation
4. Use randomly generated matrix
5. Quits program
Please select an option: 1
                                 -32 |
  14
        52
                -15
                36 -5
-5 47
16 49
  -9
                                 16 |
49 |
        -15
                -5
16
  3
        2
                                 79
  -5
        -32
  -15.0000 |
  -100.0000 |
  106.0000 |
  329.0000
463.0000
Option 1: x = | -0.0000 1.0000 2.0000 3.0000 4.0000 |
1. Use matrix equation A from Project 3B
2. Use matrix equation B from Project 3B
3. Use custom matrix equation
4. Use randomly generated matrix
5. Quits program
Please select an option:
```

Matrix Equation B:

Using the given matrices for matrix equation A and the gaussian elimination method created, I was able to achieve the solution:

 $[0 \ 1 \ 2 \ 3 \ 4]^T$

```
[henry@Henrys-MacBook-Pro project3 % python3 GaussianElimination.py
MA375 - Project #3B
Henry Song
1. Use matrix equation A from Project 3B
2. Use matrix equation B from Project 3B
3. Use custom matrix equation
4. Use randomly generated matrix
5. Quits program
Please select an option: 2
               2
              9
7
7
      6
7
9
3
                               4 |
                     8
                               2 |
  2
  0
                               2
  35.0000
  58.0000
  53.0000
  37.0000
39.0000
Option 2: x = | -0.0000 1.0000 2.0000 3.0000 4.0000 |
1. Use matrix equation A from Project 3B
2. Use matrix equation B from Project 3B
3. Use custom matrix equation
4. Use randomly generated matrix
5. Quits program
Please select an option:
```

Solving other matrices:

These matrices are generated using a manually entered size and filled with randomly generated integers. I apologize in advance for the tiny pictures, especially as the matrix gets larger. Normal resolution pictures are also included as stand-alone images in submission folder.

```
2x2 matrix:
                                                                               3x3 matrix:
1. Use matrix equation A from Project 3B
                                                               1. Use matrix equation A from Project 3B
2. Use matrix equation B from Project 3B
                                                               2. Use matrix equation B from Project 3B
3. Use custom matrix equation
                                                               3. Use custom matrix equation
                                                               4. Use randomly generated matrix
4. Use randomly generated matrix
                                                               5. Quits program
5. Quits program
                                                               Please select an option: 4
Please select an option: 4
                                                               Enter size of desired random matrix: 3
Enter size of desired random matrix: 2
                                                                A =
                                                                1 579
                                                                        345
                                                                                  430 I
  228
          743
                                                                  473
                                                                        863
                                                                                  215
  527
          174
                                                                        748
                                                                 398
                                                                                  723 I
B =
                                                               B =
                                                                  671.0000
  760.0000
                                                                 384.0000
  591.0000
                                                                 864.0000
Option 4: x = | 0.8721 0.7553 |
                                                                Option 4: x = | 0.4451 - 0.0480 0.9997
                  4x4 matrix:
                                                                               5x5 matrix:

    Use matrix equation A from Project 3B
    Use matrix equation B from Project 3B

    Use matrix equation A from Project 3B
    Use matrix equation B from Project 3B
    Use custom matrix equation

3. Use custom matrix equation
                                                           4. Use randomly generated matrix
4. Use randomly generated matrix
                                                           5. Quits program
5. Quits program
                                                           Please select an option: 4
Please select an option: 4
                                                            Enter size of desired random matrix: 5
Enter size of desired random matrix: 4
                                                             457
| 249
        299
                806
                         556 I
                                                             928
                                                                   839
                                                                           651
                                                                                  680
                                                                                          410
 586
        873
                272
                         907
                                                             675
                                                                   476
                                                                           593
                                                                                          498
  794
        158
                85
                         787
                                                             387
                                                                   465
                                                                           619
                                                                                          440
                                                             884
                                                                   831
                                                                                          188
                                                             901.0000
  574.0000
                                                             638.0000
912.0000
418.0000
  321.0000
  52.0000 |
  518.0000 |
                                                             554.0000
Option 4: x = | 0.0549 0.2315 0.6851 -0.1098
                                                            Option 4: x = | 2.4044 -2.6581 -0.9485 0.5566 2.1362
```

```
7x7 matrix:
                                               6x6 matrix:
  1. Use matrix equation A from Project 3B
                                                                                                                                         Use matrix equation A from Project 3B
                                                                                                                                    2. Use matrix equation B from Project 3B
  2. Use matrix equation B from Project 3B
                                                                                                                                    3. Use custom matrix equation
  3. Use custom matrix equation
                                                                                                                                    4. Use randomly generated matrix 5. Quits program
  4. Use randomly generated matrix
  5. Quits program
                                                                                                                                    Please select an option: 4
  Please select an option: 4
                                                                                                                                     Enter size of desired random matrix: 7
  Enter size of desired random matrix: 6
                                                                                                                                                                          791
653
                                                                                                                                        672
                                                                                                                                                              687
                                                                                                                                                                                                   372
                                                                                                                                                                                                                346
                              681
                                                                         90 |
     389
                217
                                             362
                                                           502
                                                                                                                                        413
                                                                                                                                                 251
                                                                                                                                                              457
                                                                                                                                                                                       268
                                                                                                                                                                                                   707
                                                                                                                                                                                                                916
                                                                                                                                                                          895
452
                                                                                                                                                                                                                445
548
                                                                                                                                                              615
     352
                559
                               941
                                             443
                                                           177
                                                                         482
                                                                                                                                        304
                                                                                                                                                 835
                                                                                                                                                                                       486
                                                                                                                                                                                                   933
                                                                                                                                        808
                                                                                                                                                                                       697
     540
                807
                               299
                                             233
                                                           787
                                                                         681
                                                                                                                                                 647
                                                                                                                                                              845
                                                                                                                                                                                                   273
                                                                                                                                        98
                                                                                                                                                              800
                                                                                                                                                                          329
                                                                                                                                                                                       289
                                                                                                                                                                                                   42
                                                                                                                                                                                                                536
                                             959
                                                           450
     709
                780
                              689
                                                                         526
                                                                                                                                        430
                                                                                                                                                 822
                                                                                                                                                              637
                                                                                                                                                                          847
                                                                                                                                                                                       560
                                                                                                                                                                                                   924
                                                                                                                                                                                                                633
                911
                               261
     183
                                             547
                                                           242
                                                                         511
                                                                                                                                        535
                                                                                                                                                 461
                                                                                                                                                              944
                                                                                                                                                                          643
                                                                                                                                                                                       371
                                                                                                                                                                                                    357
                                                                                                                                                                                                                619
      717
                               355
                                             624
                                                           282
                                                                         903
  B =
                                                                                                                                        632.0000
     587.0000
                                                                                                                                       376.0000
834.0000
963.0000
     645.0000
     627.0000
     949.0000
                                                                                                                                       24.0000 |
692.0000
     111.0000
     306.0000
                                                                                                                                        230.0000
                                                                                                                                     Option 4: x = | 1.9965 -4.4272 -0.8400 3.0589 4.2427 1.1111 -3.1370
   Option 4: x = | 5.2366 3.3675 0.4267 -2.7490 -2.2463 -3.8731
                                               8x8 matrix:
                                                                                                                                                                                 9x9 matrix:
                                                                                                                               Enter size of desired random matrix: 9
Enter size of desired random matrix: 8
                                                                                                                                                      657
  102
           179
                       423
                                   47
                                               562
                                                           724
                                                                                                                                  395
997
672
749
389
397
703
                                                                                                                                          653
634
69
609
591
627
                                                                                                                                                      206
                                                                                                                                                                 233
                                                                                                                                                                            881
688
685
946
255
23
                                                                                                                                                                                       104
                                                                                                                                                                                                  559
208
174
791
705
73
817
                                                                                                                                                                                                              598
                                                                                                                                                                                                                         255
807
722
879
447
  767
67
           990
884
                                                                      308
127
                       274
                                   802
                                               293
                                                           944
                                                                                   147
                                                                                                                                                      383
399
503
276
                                                                                                                                                                 787
943
                                                                                                                                                                                       292
322
582
                                                                                                                                                                                                             329
312
                                   575
                                               422
                                                           375
                                                                                   443
                       675
                                                                      894
273
95
592
  847
           857
                       36
                                   972
                                               720
                                                           139
                                                                                   148
                                                                                                                                                                 484
568
                                                                                                                                                                                                              84
783
           95
945
                                               863
                                                           45
                                                                                   508
  764
                       927
                                   493
                                                                                                                                                                                       56
  43
                                               437
                                                                                   928
                       442
                                                           258
                                                                                                                                                                                                              697
455
                                   901
                                                                                                                                                      148
                                                                                                                                                                 407
                                                                                                                                                                                       499
                                                                                                                                                                                                                         192
                                                                                  209
  44
                                                           499
           525
                       375
                                   151
                                               518
                                                                                                                                                                 30
936
                                                                                                                                                                                                                         441
37 |
                                                                                                                                           666
                                                                                                                                                      568
                                                                                                                                                                            801
                                                                                                                                                                                       122
           436
                       363
  289
                                   179
                                               101
                                                           53
                                                                                   472
                                                                                                                                           527
                                                                                                                                                      827
                                                                                                                                  642.0000
615.0000
636.0000
544.0000
237.0000
610.0000
113.0000
  690.0000
116.0000
265.0000
  487.0000
  646.0000
  46.0000
  243.0000
                                                                                                                                   0.0000 |
  561.0000
                                                                                                                                  120.0000
Option 4: x = | -0.3081 -0.6327 0.9470 0.9693 -0.3999 -0.1071 0.7802 -0.5458
                                                                                                                               Option 4: x = | -0.6231 0.5739 -0.7194 0.7238 0.4995 -0.8009 -0.2375 0.1449 0.6086 |
                                            10x10 matrix:
                                                                                                                                                                              10x10 matrix:
Enter size of desired random matrix: 10
                                                                                                                                 Enter size of desired random matrix: 10
  420
237
688
180
969
238
131
482
316
                                                                              994
28
938
22
969
595
667
827
221
442
                                                                                        179
344
491
332
427
956
694
176
318
31
                                                                                                                                   989
127
724
12
753
341
531
335
472
305
         351
767
243
365
862
655
248
465
24
201
                             24
409
498
96
914
872
415
242
104
283
                                                           780
728
298
942
485
735
779
284
700
42
                                                                     101
182
648
899
358
740
406
386
663
908
                                                                                                                                           830
503
147
932
624
472
612
938
866
31
                                                                                                                                                     140
915
700
986
724
422
809
202
403
929
                                                                                                                                                              172
538
80
737
942
687
343
617
518
548
                                                                                                                                                                         978
333
300
759
934
424
541
851
844
23
                                                                                                                                                                                   164
794
724
226
429
7
48
622
                                                                                                                                                                                            153
557
463
237
79
326
688
950
                                                                                                                                                                                                      443
446
88
87
249
686
208
618
                                                                                                                                                                                                                686
539
801
784
224
278
760
319
                                                                                                                                                                                                                          685
293
764
237
465
573
491
211
833
961
                   105
20
989
235
867
996
630
359
234
                                       937
805
85
688
432
204
348
776
781
                                                 981
841
342
348
217
697
254
902
523
                                                                                                                                                                                   269
109
                                                                                                                                                                                            751
363
                                                                                                                                                                                                       891
915
                                                                                                                                                                                                                993
855
                                                                                                                                   3 =

915.0000

585.0000

518.0000

662.0000

423.0000

514.0000
  -
658.0000 |
777.0000 |
46.0000 |
671.0000 |
  442.0000
578.0000
                                                                                                                                   835.0000
376.0000
114.0000
571.0000
  226.0000
439.0000
  686.0000
946.0000
 Option 4: x = | -0.7291 -0.0566 0.3297 0.2538 1.3576 -0.7862 0.9592 0.0769 0.1921 -1.0571
                                                                                                                                 Option 4: x = | 6.2506 4.3139 -3.2894 5.7250 -9.3137 0.2945 -1.1414 -0.6807 5.2419 -5.0086
```

Source Code:

- Song_Henry_Project3.zip
 - o Project Report.pdf
 - o GaussianElimination.py
 - /matrix_calculation_images
 - 2x2.png
 - 3x3.png
 - 4x4.png
 - 5x5.png
 - 6x6.png
 - 7x7.png
 - 8x8.png
 - 9x9.png
 - 10x10_1.png
 - 10x10_2.png
- GitHub
 - o https://github.com/henrysong671/MA375-Project2