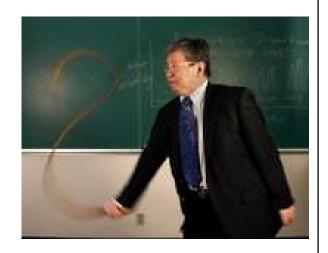


Bullwhip Effect

- Hau Lee investigate the 'Bullwhip Effect' after observing multi-echelon supply chain inventory problems (first described by Forrester in 1961)
- First documented the problem with Pampers
- Then found similar phenomenon in other industries, specifically HP printers.



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Magnification of orders

Magnification of orders as we move upstream in a supply chain from the customer



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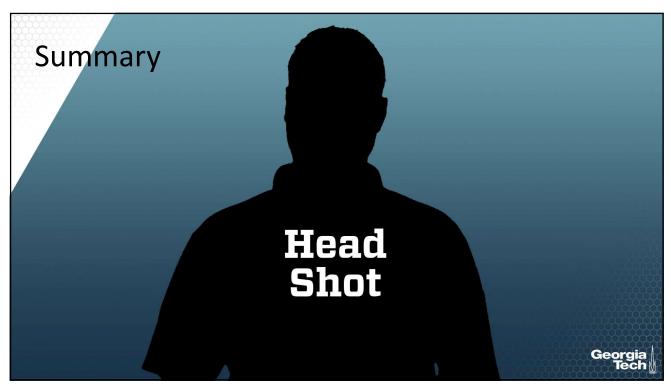
Causes

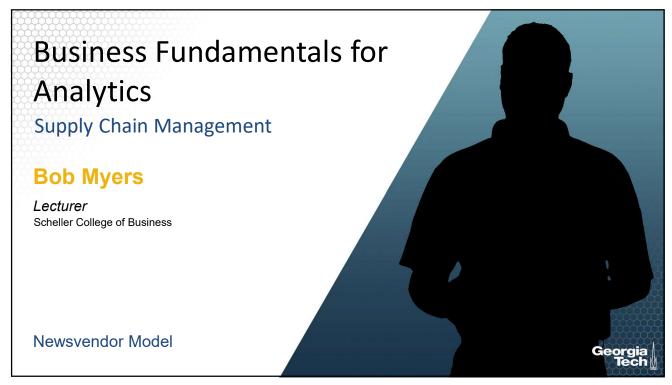
- Price Fluctuations (placing items on sale)
 - Sell out due to "artificial" demand, thus order more
 - Upstream perceives this as "actual" demand and ramps up production
- Order Batching
 - Upstream cannot distinguish change in batch size from change in demand
- Shortage Gaming
 - · Suppliers ration orders
 - Buyers overcompensate to ensure they have product
- Forecast Inaccuracies

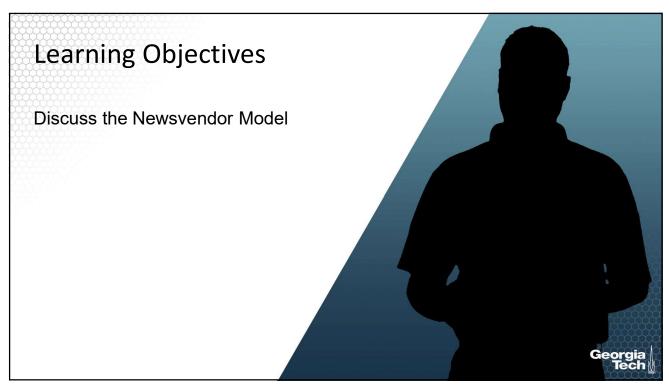
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Solutions/How to Mitigate Increase information sharing of data thru the supply chain. Ex: share POS data upstream. Reduce order costs (reduces desire to order in larger batches) Eliminate discounts and promotions (reduces "artificial" demand)







How many newspapers should he get today?

He buys for \$.80 a paper

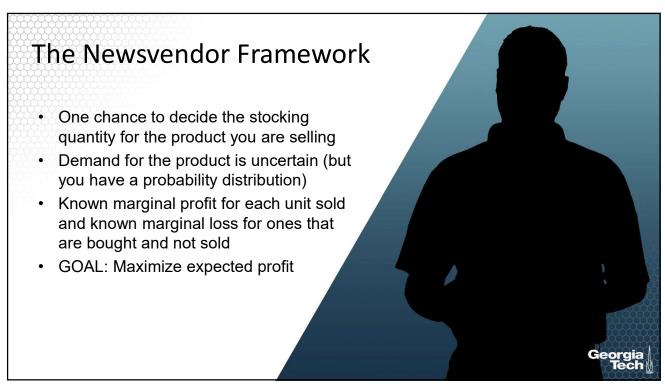


He sells for \$1.00 a paper

Too few papers and some customers will not be able to purchase a paper, and profits associated with these potential sales are lost.

Too many papers and the price paid for papers that were not sold during the day will be wasted, lowering profit.

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Let's Define Some Variables

c: Cost of each item

p: Retail selling price for each item

s: Salvage value for unsold items

MP: Marginal profit from selling a stocked item = p-c

ML: Marginal loss from not selling a stocked item = c-s

x: Number of items you buy

P(x): Probability that the xth item is not sold



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Critical Fractile

Underage cost = opportunity cost of underestimating demand

Overage cost = cost of overestimating demand

 c_u = Underage cost = p - c (retail price minus cost)

 c_o = Overage cost = c - s (cost minus salvage value)

$$F(Q) = P(D \le Q) \le \frac{c_u}{c_u + c_o}$$

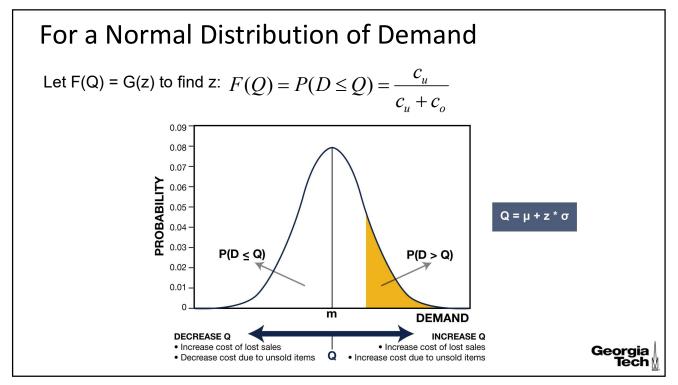
Where: D = demand

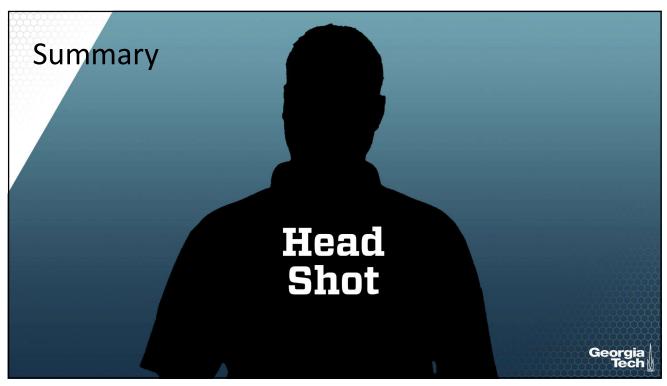
Q = quantity ordered

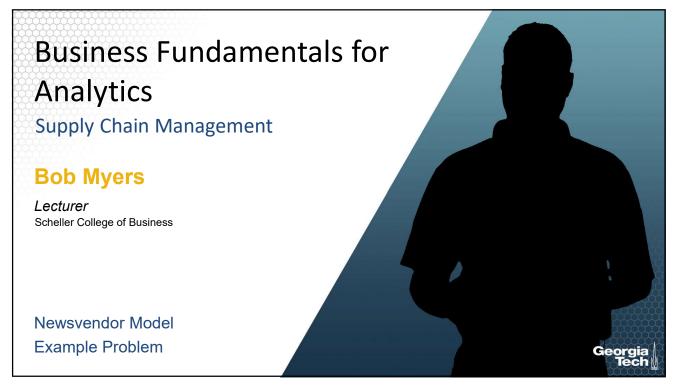


For a Normal Distribution of Demand 0.09 0.08 0.07 PROBABILITY 0.06 0.05 $F(Q) = P(D \le Q) \le \frac{c_u}{c_u + c_o}$ 0.04 0.03 $P(D \leq Q)$ P(D > Q)0.02 0.01 m **DEMAND** Solution with continuous distribution: Choose Q such that $P(D \le Q)$ = critical fractile

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Merchandise Buyer

- You work for the University Bookstore.
- Georgia Tech Football is going to play in the Sun Bowl.
- You need to decide on a T-shirt order from your supplier.
- · Order too many and costs go up.
- Order too few and miss out on sales.



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Data

- T-shirt vendor charges \$6.50 per shirt.
- You sell t-shirts for \$8.95 each.
- After the bowl game, demand will go away but Big Lots will buy any leftover tshirts for \$1.00 each.
- From past orders, you estimate demand to be normally distributed with a mean of 20,000 t-shirts and a standard deviation of 1,000.

How many t-shirts should you order?

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Solution

$$p = \$8.95$$
, $c = \$6.50$, $s = \$1.00$

$$c_u = \$8.95 - \$6.50 = \$2.45$$

$$c_o = \$6.50 - \$1.00 = \$5.50$$

$$m = 20,000, s = 1,000$$

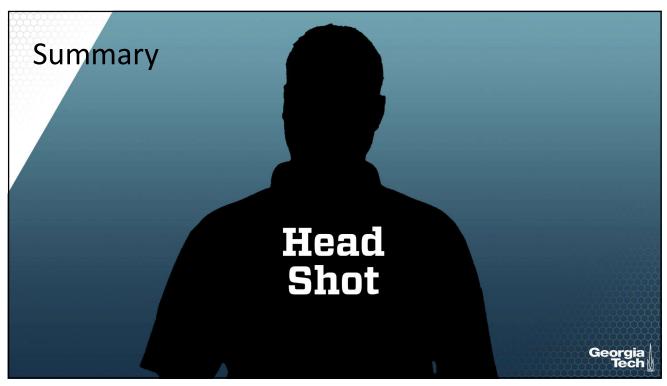
$$F(Q) = (P(D \le Q) = \frac{c_u}{c_u + c_o} = \frac{2.45}{2.45 + 5.50} = .308$$

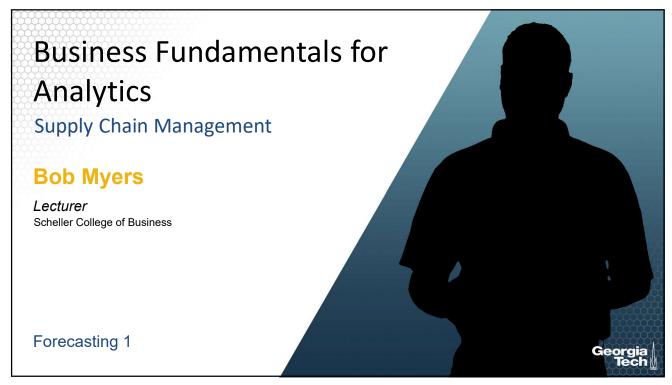
Look at the standard normal table and find the z that corresponds to F(Q): z = -0.5

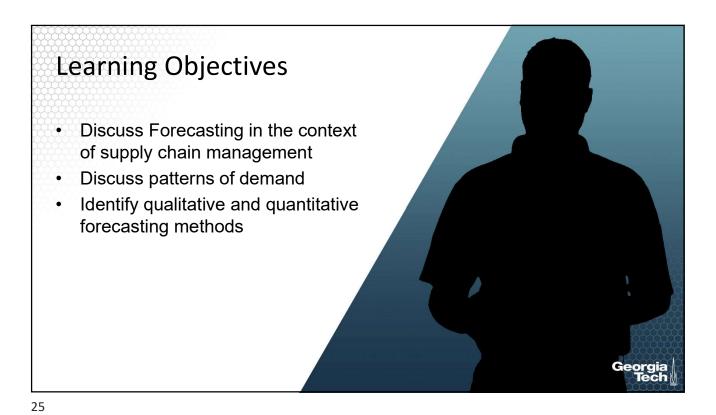
$$Q = \mu + z\sigma = 20,000 - .5 * 1,000 = 19,500 t - shirts$$

Since the overage costs were more than the underage costs, you order fewer than the expected demand

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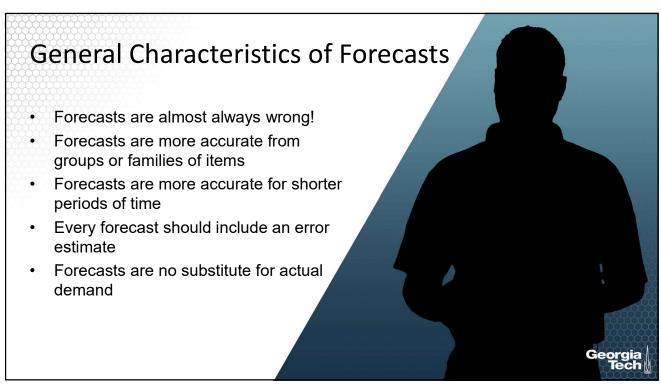
What is Forecasting?

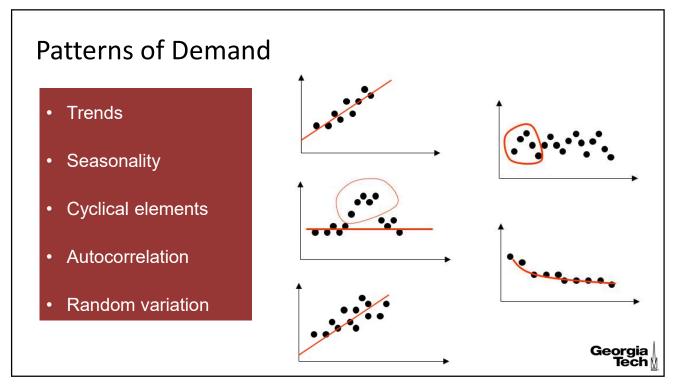
Forecasting – prediction of future events used for planning purposes.

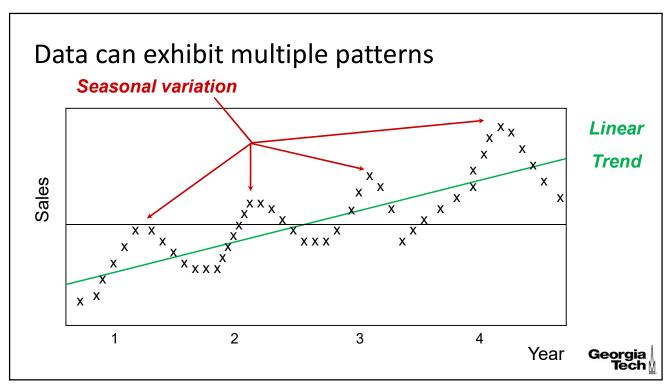
Used for:

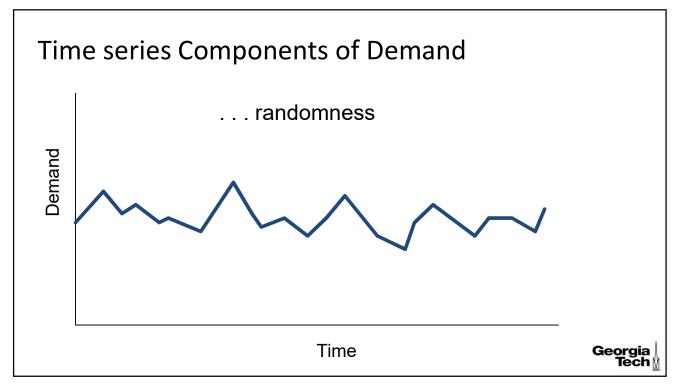
- Strategic planning (long term capacity decisions)
- Finance and Accounting (budgeting and cost control)
- Marketing (future sales trends, new product introduction)
- Production and Operations (staffing and supplier relations)

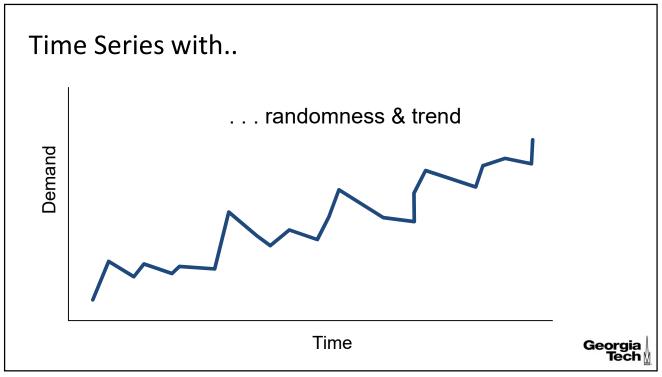


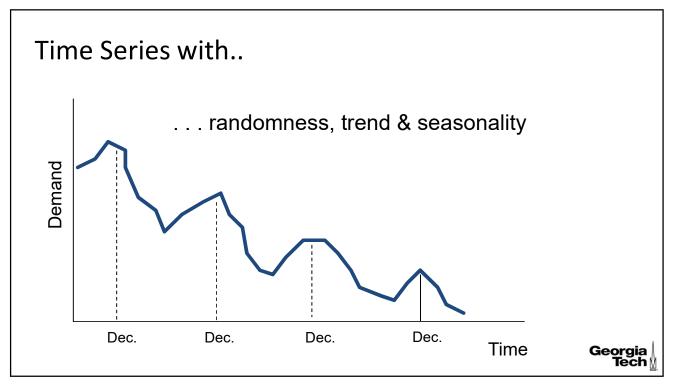












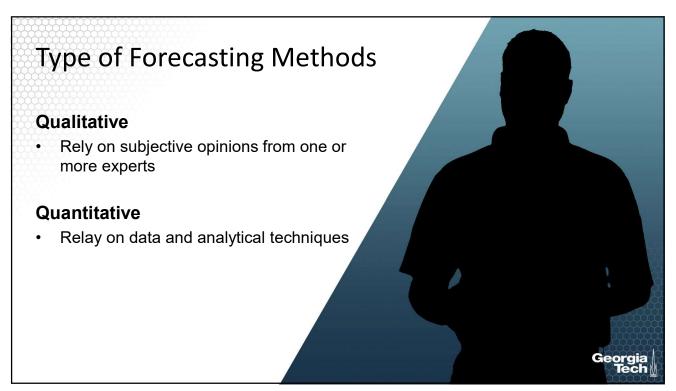
Some Important Questions

- What is the purpose of the forecast?
- · Which systems will use the forecast?
- How important is the past in predicting the future?

Answers will help determine the time horizons, techniques, and level of detail in the forecast.



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Quantitative Forecasting Methods

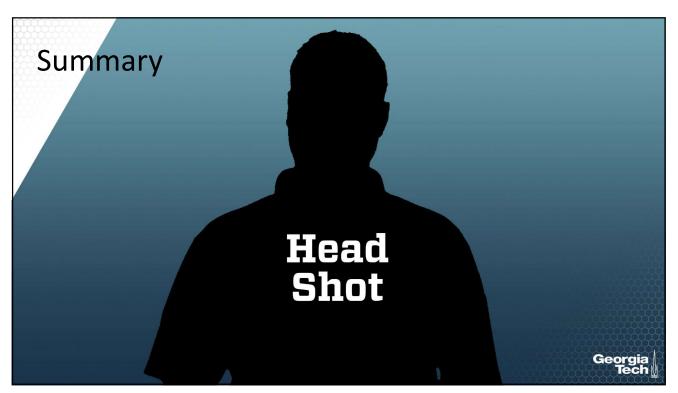
Time Series: models that predict future demand based on past history trends

Casual Relationships: models that use statistical techniques to establish relationships between various items and demand (Ex: Linear Regression)

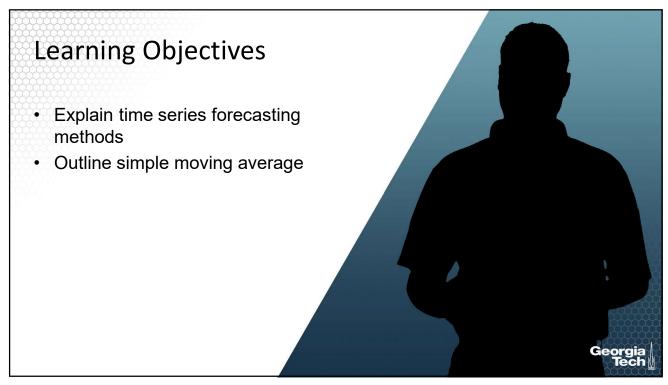
Simulation: models that can incorporate some randomness and non-linear effects



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Time Series: Moving Average

- The moving average model uses the last n periods in order to predict demand in period t+1.
- There are two types of moving average models: simple moving average and weighted moving average.
- The moving average model assumption is that the most accurate prediction of future demand is a simple (linear) combination of past demand.



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Time Series: Simple Moving Average (Cont'd)

In the simple moving average models the forecast value is

$$F_{t+1} = \frac{A_t + A_{t-1} + \dots + A_{t-n+1}}{n}$$

t is the current period

Ft+1 is the forecast for the next period

n is the number of periods

A is the Actual demand for a given period



Example: 4 Period Simple Moving Average

Week	Demand
1	650
2	678
3	720
4	785
5	859
6	920
7	850
8	758
9	892
10	920
11	789
12	844

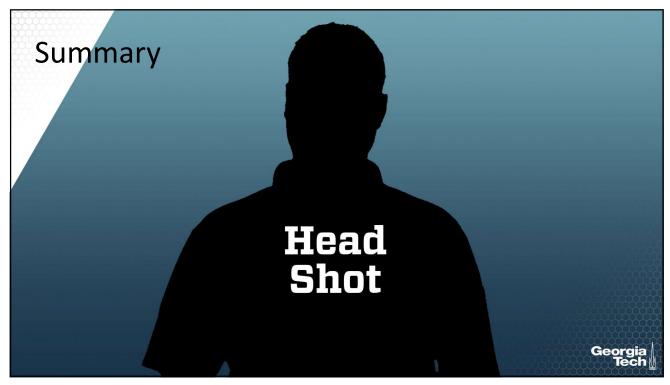
What is the Forecast for Week 13 using a 4 period Simple Moving Average?

$$F_{13} = \frac{A_t + A_{t-1} + \dots + A_{t-n+1}}{n} = \frac{A_{12} + A_{11} + A_{10} + A_9}{4}$$

$$F_{13} = \frac{844 + 789 + 920 + 892}{4} = 861.25$$

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Time Series: Weighted Moving Average (WMA)

We may want to give more importance to some of the data...

$$F_{t+1} = w_1 A_t + w_{t-1} A_{t-1} + \dots + w_{t-n} A_{t-n}$$
$$w_t + w_{t-1} + \dots + w_{t-n} = 1$$

t is the current period

Ft+1 is the forecast for the next period

n is the number of periods

A is the Actual demand for a given period

w is the importance (weight) for a given period



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Example: 3 Period Weighted Moving Average

Week	Demand
1	650
2	678
3	720
4	785
5	859
6	920
7	850
8	758
9	892
10	920
11	789
12	844

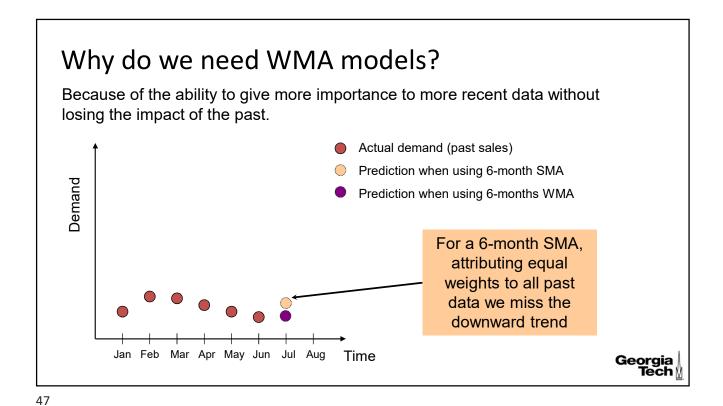
What is the Forecast for Week 110 using a 3 period Weighted Moving Average with weights .7,.2,.1?

$$F_{t+1} = W_t A_t + W_{t-1} A_{t-1} + \dots + W_{t-n+1} A_{t-n+1}$$

$$F_{10}$$
=.7 A_9 +.2 A_8 +.1 A_7

$$F_{10} = .7 * 892 + .2 * 758 + .1 * 850 = 861$$

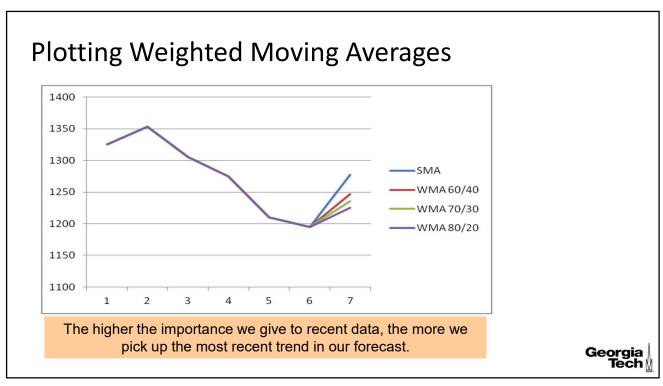


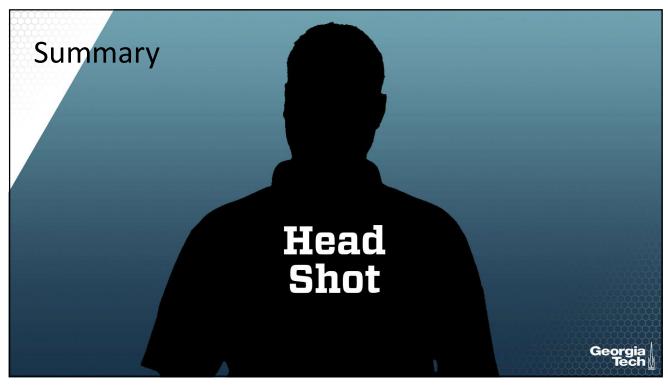


How Do We Choose the Weights?

• Trial and error
• Depends upon:
• Importance we feel past data has on future data
• Known seasonality

***Note that Simple Moving Average is actually WMA with all weights the same



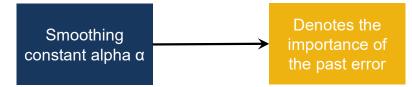






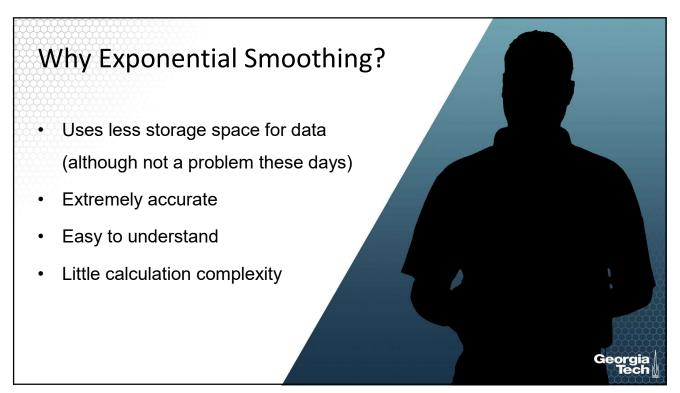
Time Series: Exponential Smoothing

The Prediction of the future depends mostly on the most recent observation and on the error for the latest forecast



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Exponential Smoothing (ES)

Assume that we are currently in period t. We calculated the forecast for the last period (Ft-1) and we know the actual demand last period (A_{t-1}) ...

$$F_{t+1} = F_t + \propto (A_t - F_t)$$
where $0 < \propto < 1$

The smoothing constant a expresses how much our forecast will react to observed differences..

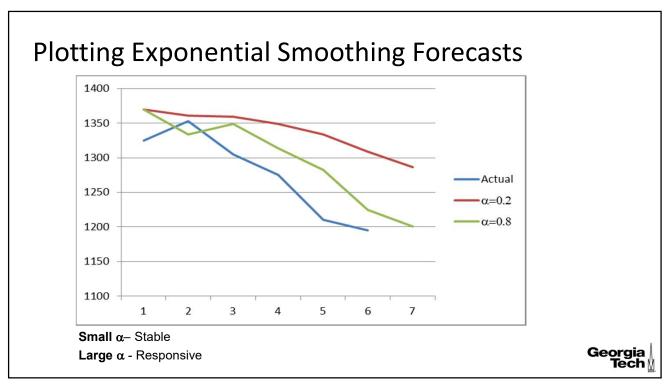
- If a is low, there is little reaction to difference
- If a is high, there is a lot of reaction to differences

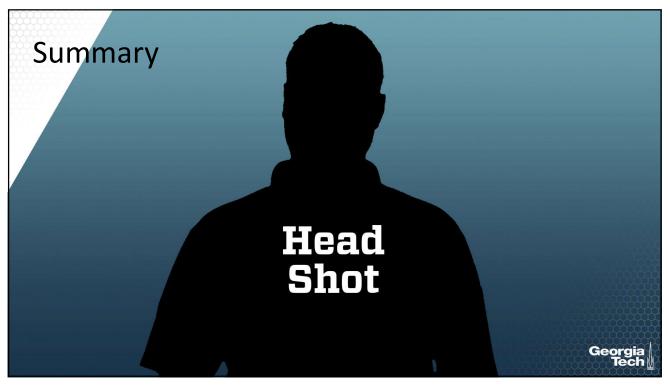


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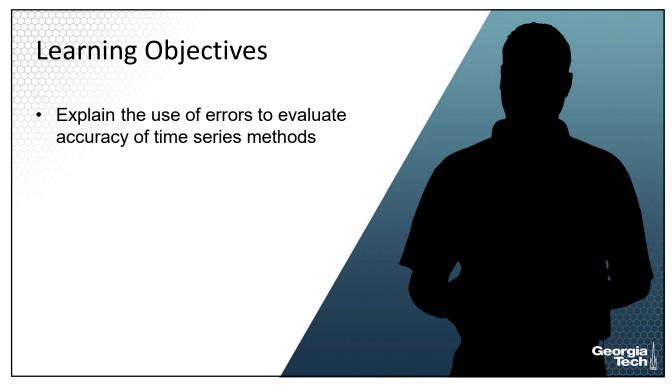
Example

Week	Demand	Forecast
1	820	820
2	775	820 🗸
3	680	811
4	655	785 🖌
5	750	759
6	802	757
7	798	766
8	689	772
9	775	756
10		760









How can we compare/evaluate different methods?



- Bias when a consistent mistake is made
- Random errors that are not explained by the model being used



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Measure of Forecast Accuracy

$$E_t = A_t - F_t$$

- Et can be positive or negative
- Positive E_t means the forecast was too low
- Negative E_t means the forecast was too high



Measures of Forecast Error

• RSFE – Running Sum of Forecast Error
$$RSFE = \sum (A_i - F_i)$$

• MFE – Mean Forecast Error (Bias)
$$MFE = \frac{\sum (A_i - F_i)}{N} = \frac{RSFE}{N}$$

• MAD – Mean Absolute Deviation
$$MFE = \frac{\sum |A_i - F_i|}{N}$$

• TS – Tracking Signal
$$TS = \frac{RSFE}{MAD}$$

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Computing Forecast Error

$$RSFE = \sum (A_i - F_i) = 200$$

Bias = MFE =
$$\frac{\sum (A_i - F_i)}{N} = \frac{200}{10} = 20$$

Mean Absolute Deviation (MAD) =

$$\frac{\sum |A_i - F_i|}{N} = \frac{1600}{10} = 160$$

PD	Forecast	Actual Sales	(Sales – Forecast)	Absolute Error
1	1,000	1,200	200	200
2	1,000	1,000	0	0
3	1,000	800	-200	200
4	1,000	900	-100	100
5	1,000	1,400	400	400
6	1,000	1,200	200	200
7	1,000	1,100	100	100
8	1,000	700	-300	300
9	1,000	1,000	0	0
10	1,000	900	-100	100
	10,000	10,200	200	1,600

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Measuring Accuracy: Tracking Signal

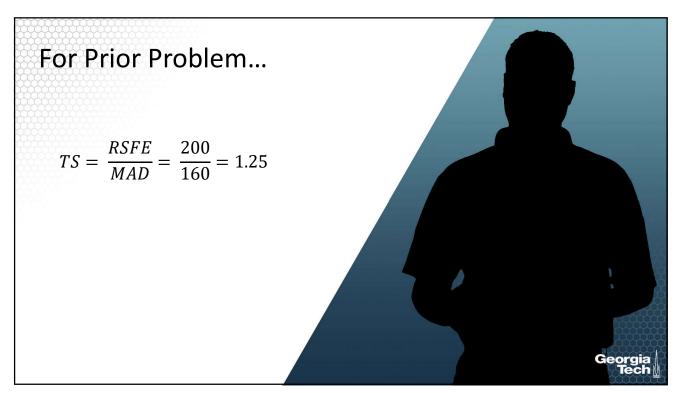
- TS = Tracking Signal
- Measure of how often our estimations have been above or below the actual value. It is used to decide when to re-evaluate the model

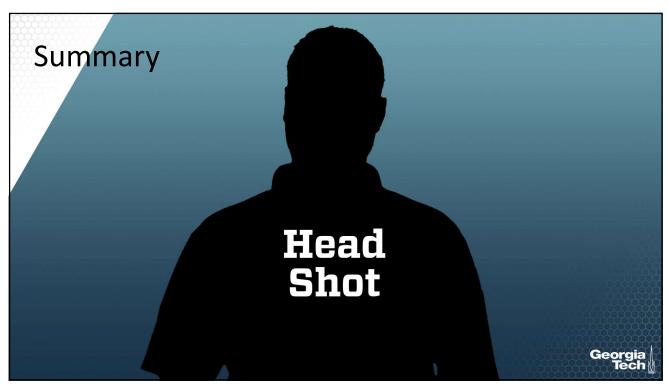
$$TS = \frac{RSFE}{MAD}$$

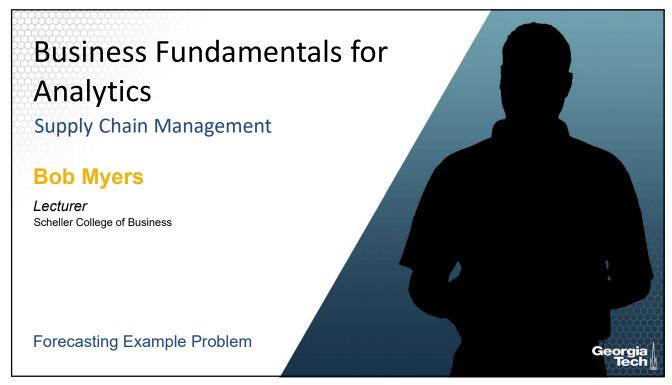
- Positive tracking signal most of the time, the actual values are above the forecasted values.
- Negative tracking signal most of the time, the actual values are below the forecasted values.
- If TS < -4 or TS > 4, investigate!

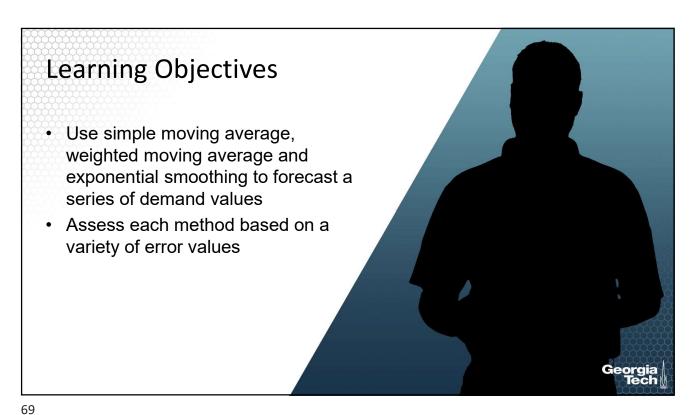
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Example

Harrys Hardware has the following demand data for a new multipurpose hammer:

	Demand
1	289
2	296
3	354
4	287
5	301
6	281
7	294
8	318

Evaluate the following models:

- 1. SMA (2 period, 3 period, 4 period)
- 2. WMA (.5,.3,.2 and .7,.2.1)
- 3. ES (alpha = .9 and alpha = .2. for both take F₁=289)

Using these Error methods:

- 1. RSFE
- 2. MSE
- 3. MAD
- 4. TS



Use Excel and when done, continue on..

· Next slide will have solutions!

	RSFE	MFE	MAD	TS
2 month SMA				
3 month SMA				
4 month SMA				
ES aplha=.9				
ES aplha=.2				
WMA (.5,.3,.2)				
WMA (.7,.2,.1)				

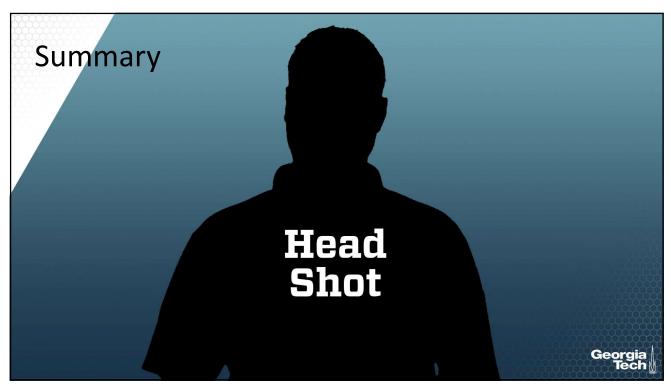


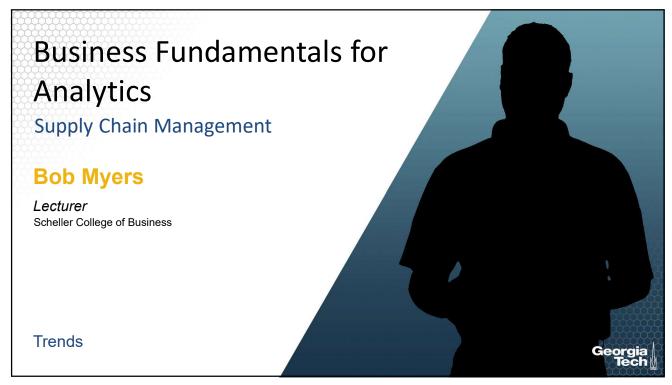
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Thoughts? Insights?

	RSFE	MFE	MAD	TS
2 month SMA	24.50	4.08	27.58	0.89
3 month SMA	-40.00	-8.00	20.13	-1.99
4 month SMA	-18.50	-4.63	18.25	-1.01
ES aplha=.9	29.43	4.20	27.16	1.08
ES aplha=.2	56.34	8.05	18.77	3.00
WMA (.5,.3,.2)	-38.60	-7.72	20.64	-1.87
WMA (.7,.2,.1)	-37.40	-7.48	21.20	-1.76











Artificial Intelligence



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Robotics



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Autonomous Vehicles





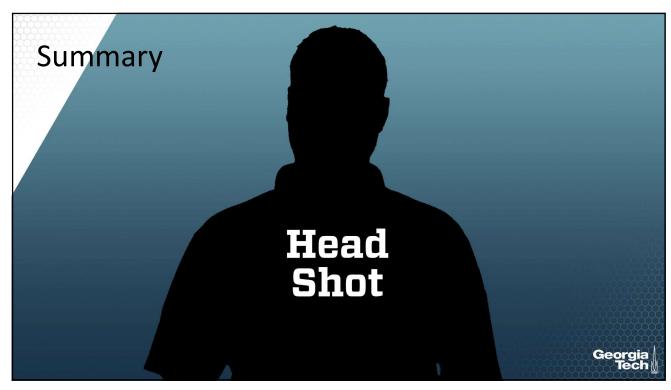
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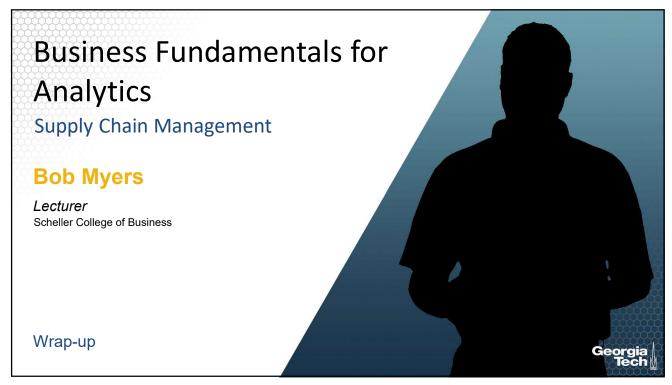
See Some Similarities?

 All of these have large amounts of data and calculations underlying them. Meaning the need for Analytics!

These will fundamentally, radically change how companies do business.







It is an Incredible Time for Operations and Supply Chain!

- Operations managers focus on how to develop capabilities to design, produce, and deliver products and services in a competitive market.
- Discipline going thru radical changes due to several maturing technologies.
- Data and Analytics will play a KEY role. Most new technology relies upon it.

