

# Regression Analysis

## Regression Analysis in Practice

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Predicting Churn Values of  
Customers: Regression &  
Variable Selection



## About This Lesson



# Logistic Regression

## ## Create full model

```
full.model <- glm(Churn.Value~., family = "binomial", data = train)
```

```
summary(full.model)
```

## ## Finding insignificant variables

```
which(summary(full.model)$coeff[,4]>0.05)
```

## ## The overall regression seems to have explanatory power

## ## Model Assessment: Multicollinearity

```
vifs <- vif(full.model)
```

## Not statistically significant in the full model:

Gender, Senior Citizen, Phone Service, Multiple Lines, Internet Service, Online Security, Online Backup, Device Protection, Tech Support, Streaming TV, Streaming Movies, Payment Method, Monthly Charges

# Logistic Regression (cont'd)

## ## Create full model

```
full.model <- glm(Churn.Value~., family = "binomial", data = train)
```

```
summary(full.model)
```

## ## Finding insignificant variables

```
which(summary(full.model)$coeff[,4]>0.05)
```

## ## The overall regression seems to have explanatory power

## ## Model Assessment: Multicollinearity

```
vifs <- vif(full.model)
```

	GVIF	Df	GVIF^(1/(2*Df))
Gender	1.003414	1	1.001705
Senior Citizen	1.112401	1	1.054704
Partner	1.248636	1	1.117424
Dependents	1.098666	1	1.048173
Tenure Months	15.612548	1	3.951272
Phone Service	35.526189	1	5.960385
Multiple Lines	7.434935	1	2.726708
Internet Service	382.924211	2	4.423624
Online Security	5.158636	1	2.271263
Online Backup	6.520493	1	2.553526
Device Protection	6.611606	1	2.571304
Tech Support	5.409603	1	2.325855
Streaming TV	25.075402	1	5.007534
Streaming Movies	25.317771	1	5.031677
Contract	1.625406	2	1.129121
Paperless Billing	1.128532	1	1.062324
Payment Method	1.413278	3	1.059346
Monthly Charges	694.903171	1	26.361016
Total Charges	20.166529	1	4.490716

# Variable Selection

## Reduce the number of factors in the model

1. Overfitting
  - Model with large # of factors can fit too closely, cause random effects
  - It can cause bad estimates
2. Simplicity
  - Less chance of insignificant factors
  - Easier to interpret



# Variable Selection (cont'd)

- Forward-Backward Stepwise Regression

**# Create minimum model including an intercept**

```
min.model <- glm(Churn.Value~ 1, family = "binomial", data = train)
```

**# Perform stepwise regression**

```
step.model <- step(min.model, scope = list(lower = min.model, upper = full.model),
  direction = "both", trace = FALSE)
```

- **Not selected:** Gender, Senior Citizen, Online Backup, Device Protection, Monthly Charges
- **Not statistically significant:** Payment Method by Mailed check and by Credit Card



# Variable Selection (cont'd)

- LASSO Regression

**# Set predictors and response to correct format**

```
x.train <- model.matrix(Churn.Value ~ ., train)[-1]
```

```
y.train <- train$Churn.Value
```

**# Use cross validation to find optimal lambda**

```
cv.lasso <- cv.glmnet(x.train, y.train, alpha = 1, family = "binomial")
```

**# Train Lasso and display coefficients with optimal lambda**

```
lasso.model <- glmnet(x.train, y.train, alpha = 1, family = "binomial")
```

```
coef(lasso.model, cv.lasso$lambda.min)
```

- Not selected for both models:  
Monthly Charges

- Elastic Net Regression

**# Use cross validation to find optimal lambda**

```
cv.elnet <- cv.glmnet(x.train, y.train, alpha = 0.5, family = "binomial")
```

**# Train Elastic Net and display coefficients with optimal lambda**

```
elnet.model <- glmnet(x.train, y.train, alpha = 0.5, family = "binomial")
```

```
coef(elnet.model, cv.elnet$lambda.min)
```

# Summary

