

## Counting Sort

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For Counting Sort, the input is  $n$  integers in some known range  $[0, k - 1]$ .

```
1 def CountingSort:
    C = [0]*k, B = [0] * n
3   for j in [1, n]:
        C[A[j]] += 1    # C = distribution
5   for i in [1, k]:
        C[i] = C[i-1] + C[i] # C = Cumulative distribution
7   for j in [n, 1]:
        B[C[A[j]]] = A[j]
        C[A[j]]--
9   return B
```

The algorithm calculates a cumulative frequency distribution for the numbers in the input array in the first 2 passes, so that  $C[i]$  is the number of elements less than or equal to  $i$ . In the final loop, the algorithm puts the last element from  $A$  into  $B$  based on its position within the cumulative distribution, then recurses (iteratively) on  $A[:-1]$ .

Counting sort has  $\Theta(n+k)$  runtime and space complexity and is a stable sort. For obvious reasons, it should only be preferred if  $k \ll n \lg n$ .