



Submit your solutions as `answers.pdf` to the repository.

**Exercise 1** (Explain in your own words, 1+1+1 points).

- Write down the Needham-Schroeder protocol and explain the weakness of the protocol in case of a stolen session key and a man-in-the-middle attack.
- Explain the two different types of secret sharing from the lecture.
- Explain the basic operation of a blockchain-based distributed ledger.

**Exercise 2** (Distributed Group Key Management, 2+1+2 points).

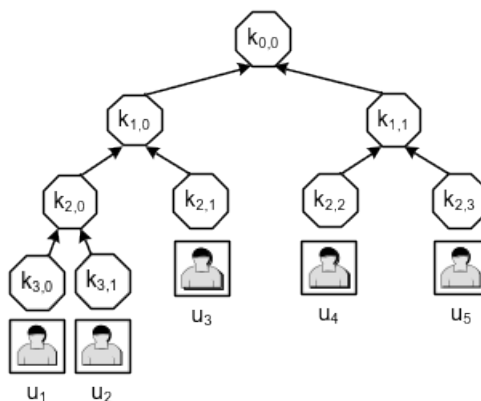


Figure 1: Key tree of the TGDH protocol

Given is the group  $\mathbb{Z}_{37}^*$  with generator  $g = 2$ . The users  $u_1, u_2, u_3, u_4$ , and  $u_5$  use the Tree-based Group Diffie-Hellman (TGDH) protocol with the key tree shown in Figure 1 for the group key establishment. Assuming that the following keys are stored in the leaves:  $k_{3,0} = 9$ ,  $k_{3,1} = 5$ ,  $k_{2,1} = 8$ ,  $k_{2,2} = 17$ ,  $k_{2,3} = 27$ .

- The user  $u_6$  with the key  $k = 19$  joins the group. Draw the modified tree.
- Write down the messages of the sponsor.
- Now the user  $u_5$  leaves the group. Hence, the user  $u_4$  alters his private key to 10. Calculate the new group key.

**Exercise 3** (Secret Sharing, 1+1 points).

- a) A one-time pad is the simplest 2-out-of-2 secret-sharing algorithm. Only the authorized set of users  $u_1$  and  $u_2$  can reconstruct the secret. Specify the algorithm and reconstruct the message from the shares  $s_1 := 0110000011$  and  $s_2 := 1011010111$ .
- b) Assuming five users  $u_i$ ,  $i = 1, 2, 3, 4, 5$  and a (3,5)-threshold sharing algorithm with the polynomial  $f(x) = 15x^2 + 14x + 6 \pmod{17}$ . Calculate a share for each user. Show that the secret can be restored by using the key shares of users  $u_1, u_2, u_3$ . (useful calculation rules:  $(-a) \pmod{b} = (kb - a) \pmod{b}$ , <https://de.planetcalc.com/8329/>).