

# Artificial Life Summer 2025

## Evolutionary Algorithms 3

Master Computer Science [MA-INF 4201]

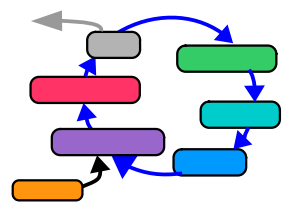
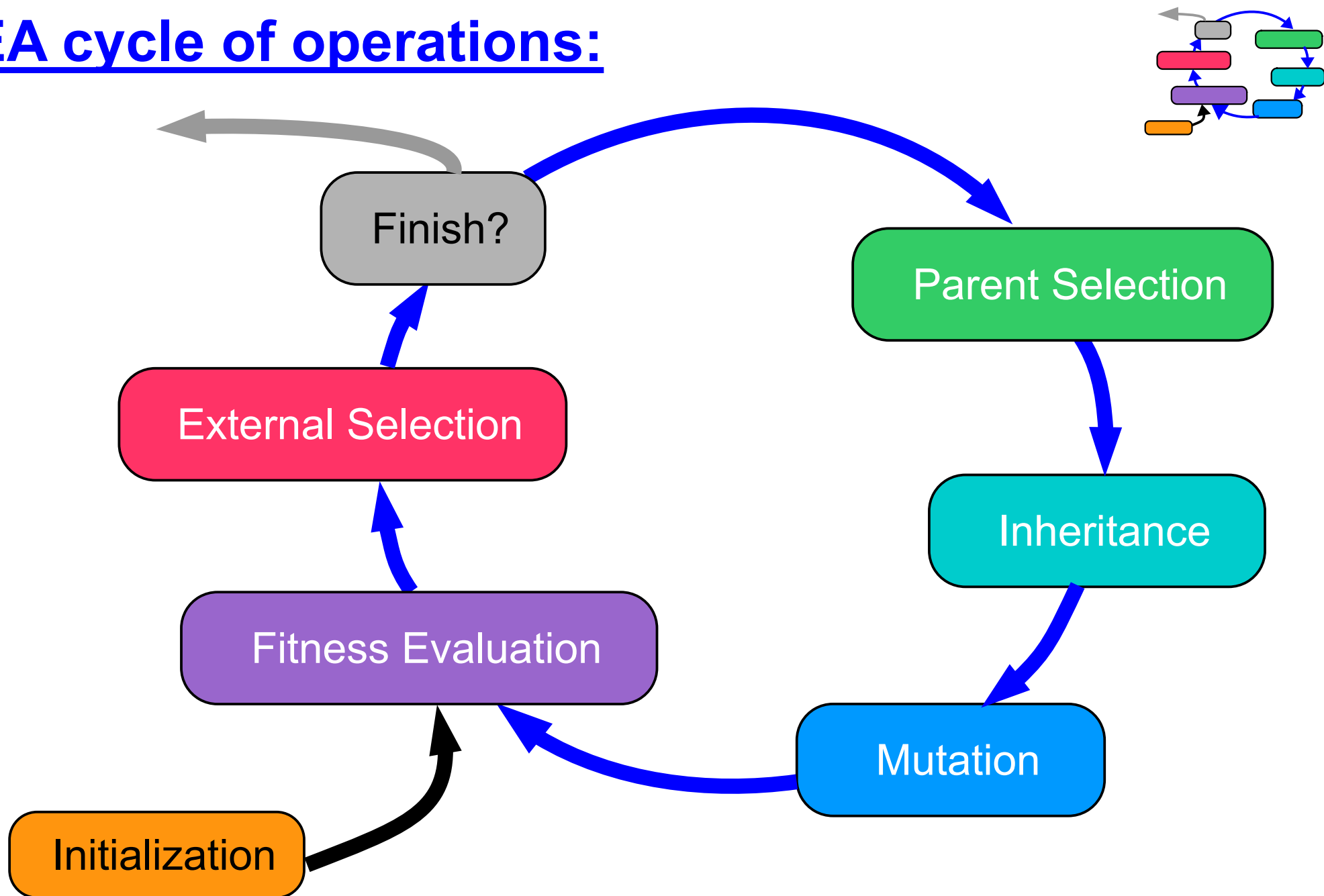
Mon 14:15 – 15:45, HSZ, HS-2

Dr. Nils Goerke, Autonomous Intelligent Systems,  
Department of Computer Science, University of Bonn

# Overview:

- Genome structure
- Example: 8 queens
- Super-individuals
- External-selection and parent-selection combined
- Probabilistic parent-selection
  - Wheel of fortune
  - Softmax selection
  - Tournament selection
- Genetic programming
- Co-evolution

# EA cycle of operations:



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**EA:**

## Genome Structure

**Naive structuring** of the genome:

**“Normal” structuring** of the genome:

**Sophisticated structuring** of the genome:

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**Pro:** easy to implement, only few knowledge necessary.

**Con:** large search space, a lot of local maxima possible,  
may be hard or impossible to find a good solution.

**“Normal” structuring** of the genome:

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**Pro:** still easy to implement, some knowledge necessary, wide variety to implement inheritance and mutation.

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**Sophisticated structuring** of the genome:

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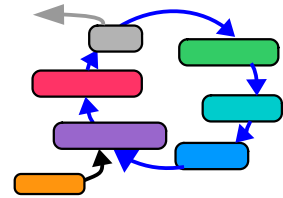
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**Sophisticated structuring** of the genome:

**Pro:** only legal, or good genomes are to be investigated.

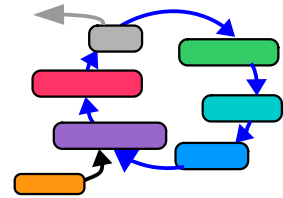
**Con:** profound knowledge about the process and of the kind of possible solutions is required, can become computational expensive to implement inheritance and mutation.



**EA:****Example: TSP****Objective:**

find the shortest route visiting each point from a set of given points (cities) exactly once (Traveling Salesman Problem).

**Genome:****Fitness Function:**

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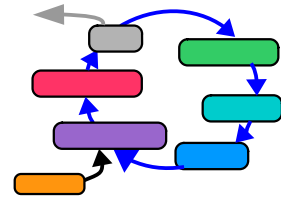
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**Genome:**

an ordered set of points (cities,  $C_i$ ), sequence of cities to be visited, containing each city exactly once.

$$g = \{ C_3, C_{17}, C_i, C_{42}, \dots \}$$

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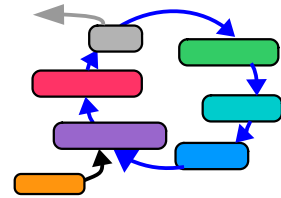
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**Fitness Function:**

$f(g)$  is the sum of all distances  $d(C_i, C_{i+1})$  between subsequent cities in the list (genome). Of course all distances  $d(C_i, C_j)$  between the cities  $i$  and  $j$  is required; either by a distance matrix or by a calculation from the coordinates.

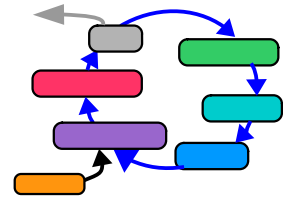
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**Example: TSP**



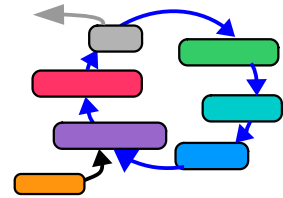
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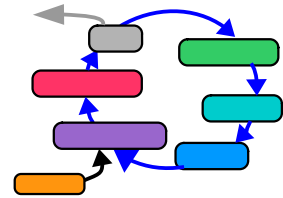
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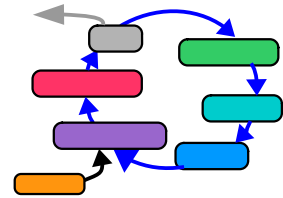
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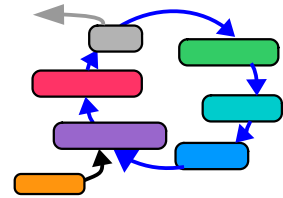
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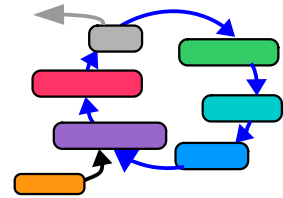
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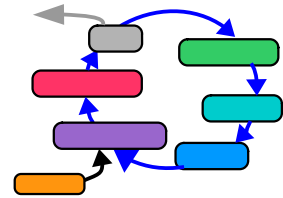
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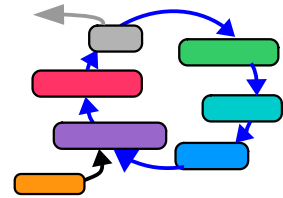
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A more sophisticated inheritance operator would have to guarantee that the offspring still represent legal genomes,

- routes that visit each city exactly once - .

This may cause high computational effort, which might be larger than the potential benefit.

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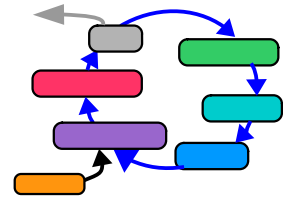
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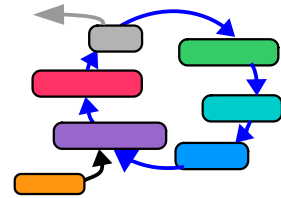
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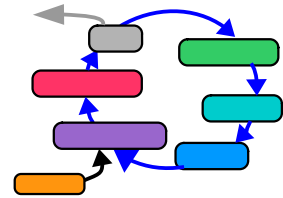
How do you know?

Either by theory (if available), or by a heuristics.

EA:

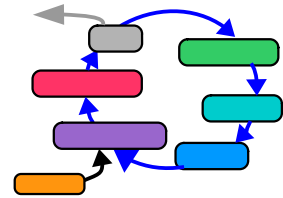
## Example: 8 Queens



EA:**Example: 8 Queens**

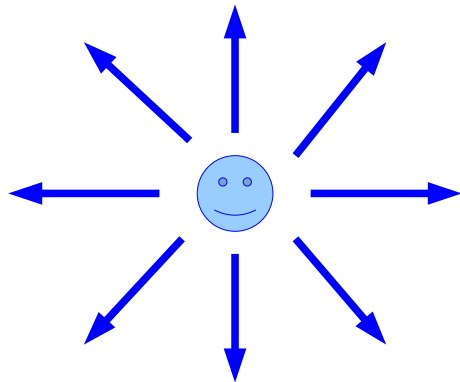
The 8 queens puzzle with an evolutionary algorithm:

The task of the 8 queens puzzle is to place 8 queens on a chess board (8x8) so that they can not reach each other.

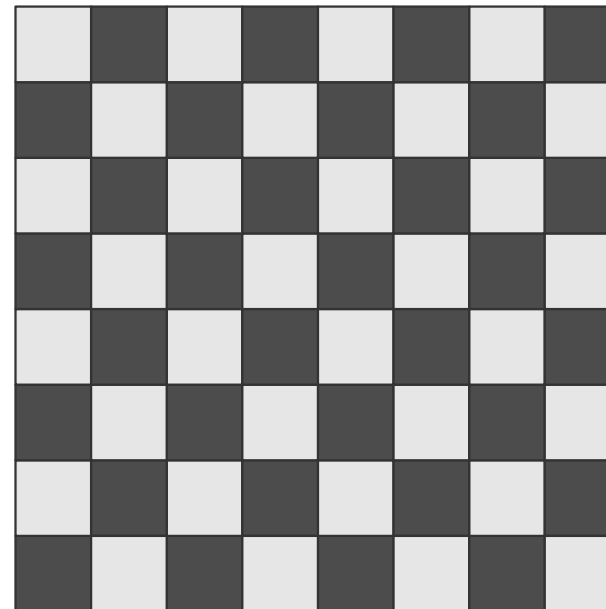
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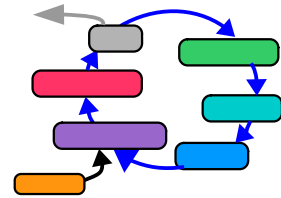


allowed moves  
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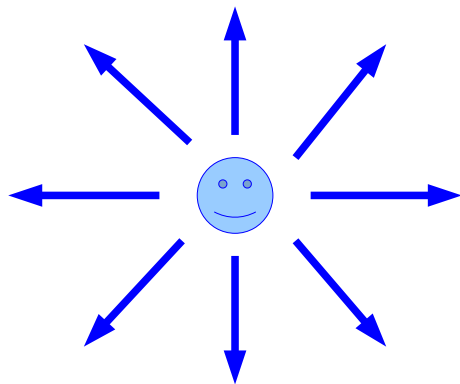
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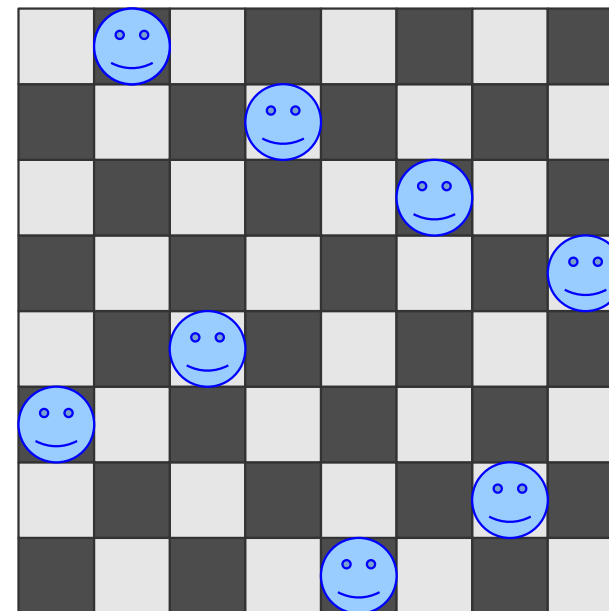
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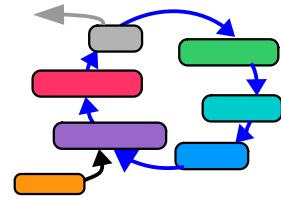


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One of  
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solutions

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EA:**Example: 8 Queens**

**Very naive** implementation of the genome:

a 64 bit binary vector; queen is 1, no queen is 0;  
more than 8 queens are possible.

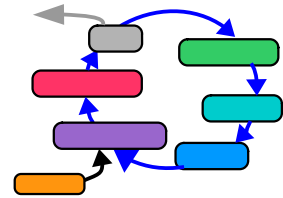
This very naive implementation is generating an extremely large search space with  $2^{64}$  possible genomes. This is beyond any computing power to be investigated in total.



**Semi naive** implementation of the genome:

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exactly 8 queens == 8 bits set are possible.

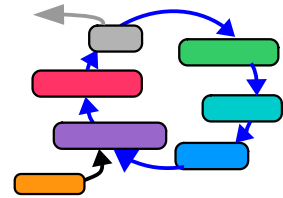
Still the resulting search space is very large.

EA:**Example: 8 Queens**

**Normal/Sophisticated** implementation of the genome:

8 rows of 8 bit binary vectors; queen is 1, no queen is 0;  
each row contains exactly one queen.

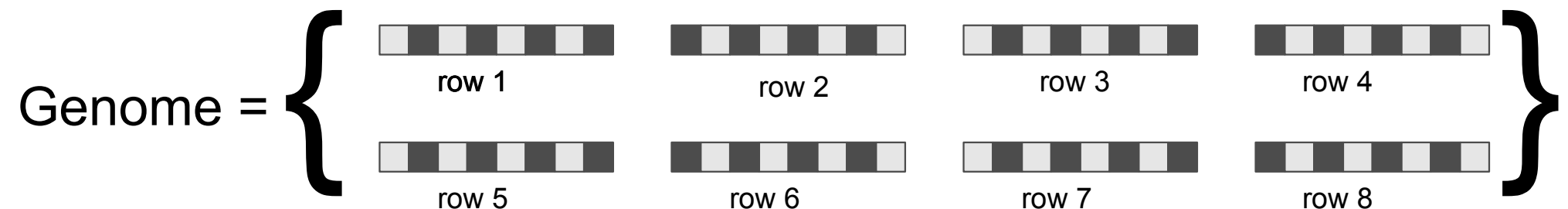
This is reducing the search space to  $8^8 = 16777216$   
possibilities, (which can be managed by brute-force).

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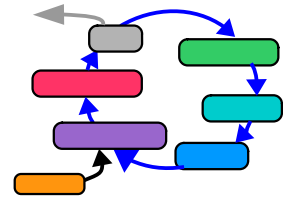
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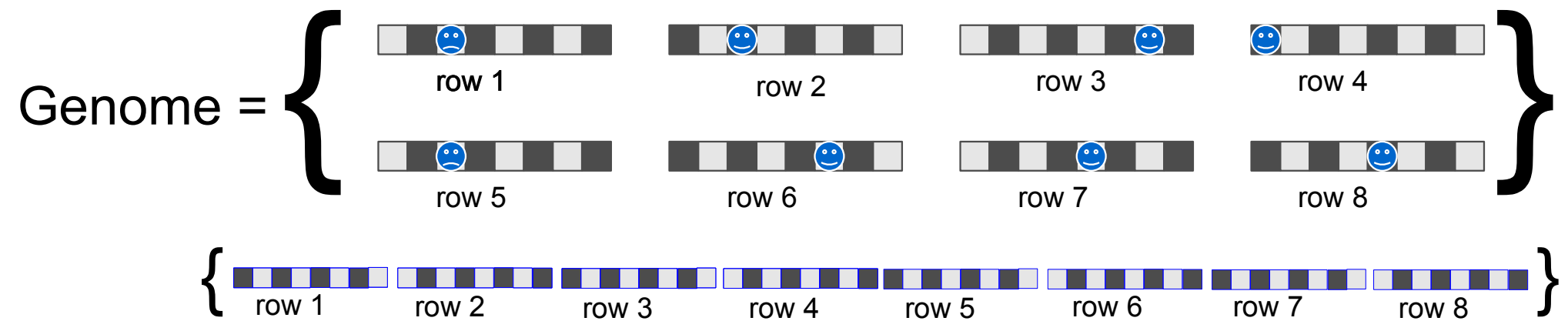
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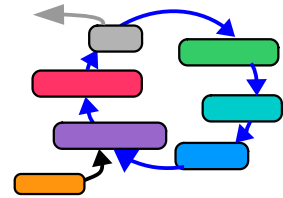


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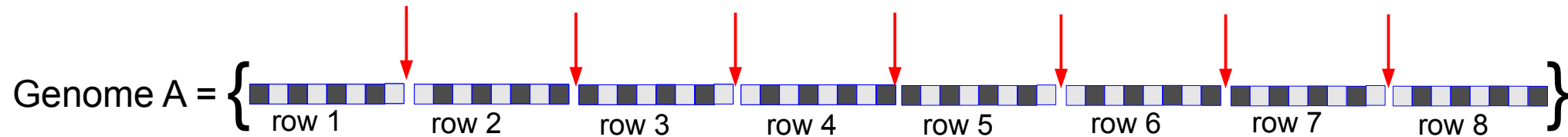
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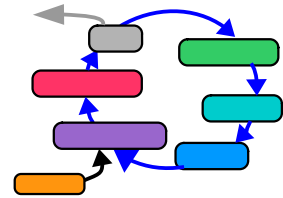
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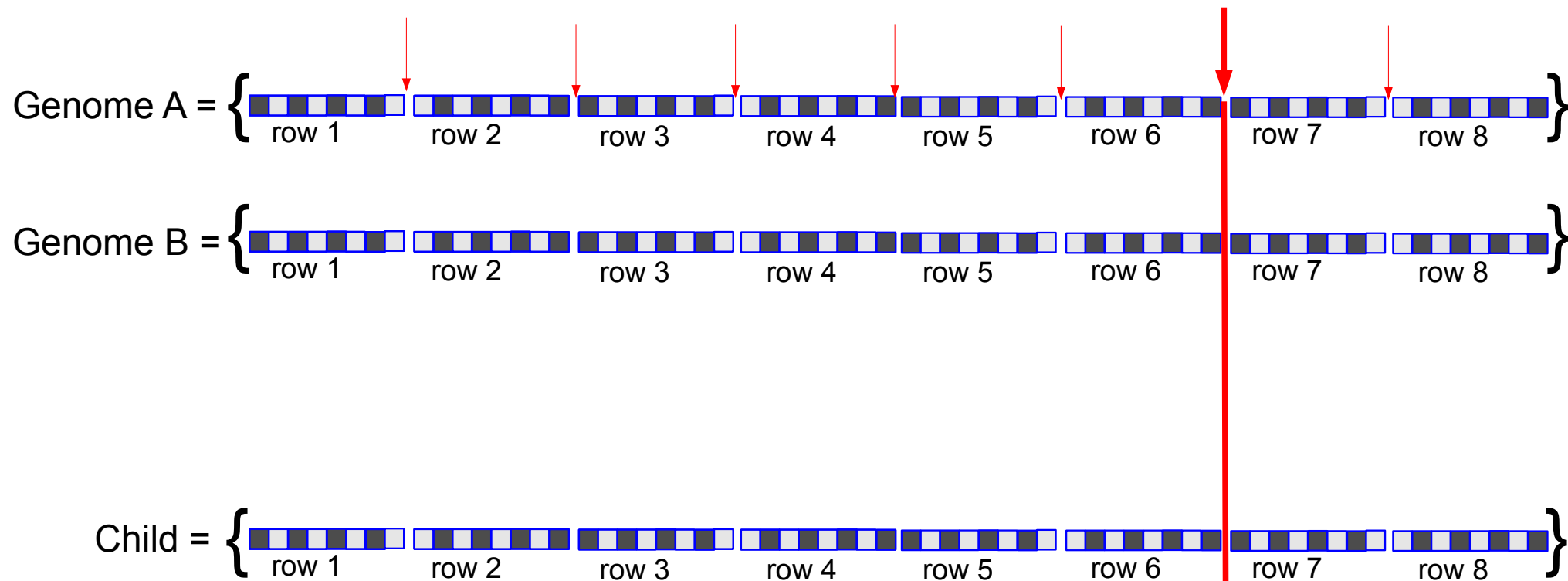
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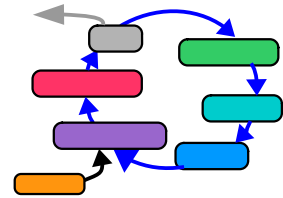
Inheritance, recombination, 1 point cross over  
cross-over points only between the rows




EA:**Example: 8 Queens**

Inheritance, recombination, 1 point cross over  
cross-over points only between the rows



EA:**Example: 8 Queens**

Mutation only the position of the queen **within** the row is altered

Genome A = {  }

Chose a random row **r** (1, ..., 8):  
and pick a new random position (1, ..., 8) for the queen 😞

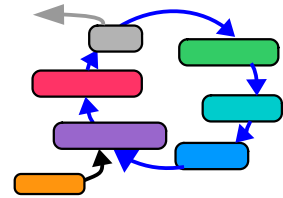
before mutation



after mutation





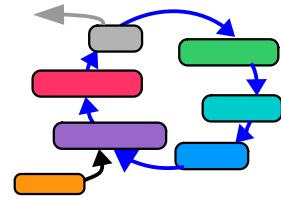
EA:**Example: 8 Queens**

A more sophisticated implementation of the genome:

If you have an even more sophisticated idea for structuring the genome, don't forget to shape the inheritance and mutation operators and the fitness function accordingly.

Go ahead,

feel free to do experiments

EA:**Example: 8 Queens**

The objective, is to find a placement of the 8 queens so that they can't reach each other.

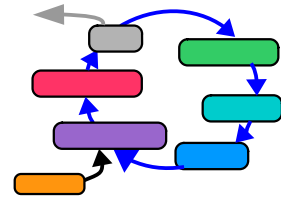
The fitness function for the EA should reflect this:

a large value of **f** if the placement is o.k. **I**  
a small value of **f** if the placement is not o.k. **O**

A fitness function that yields a binary value (**O**,**I**) is not a good idea for an evolutionary algorithm.

The resulting fitness surface is flat (**O**), with only a few isolated peaks (**I**).

The value of this kind of fitness function is not reflecting, that a genome can be close to a possible solution.

EA:**Example: 8 Queens**

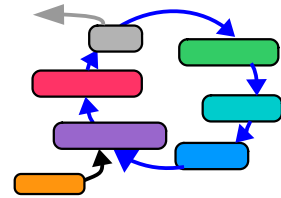
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An appropriate fitness function for an EA must be shaped accordingly;

In addition, the fitness function  $f$  value should implement, that genomes  $g$ , close to an optimal solution should yield a larger fitness value  $f(g)$  than those far away.

The optimal would be, to have a fitness function  $f(g)$  that is proportional to the distance between the genome  $g$  to an optimal genome  $g^*$ .

Unfortunately this is not possible in general.

EA:**Example: 8 Queens**

The objective, is to find a placement of the 8 queens so that they can't reach each other.

A proposal for a fitness function for the 8 queens problem:

Each possibility that one queen can attack another queen is counted as **-1**

The fitness value  **$f(g)$**  is the sum of all attack possibilities.

This yields a graded response as required, with a maximal value  **$f(g^*) = 0.0$**  when no attack is possible.

**Caution:**

This fitness function is only appropriate if the number of queens is fixed to 8 (*0 queens  $\Rightarrow$  0 attack possibilities*)

**EA:****Example:**

Implementing a task using an Evolutionary Algorithm, a series of structuring decision will be necessary.

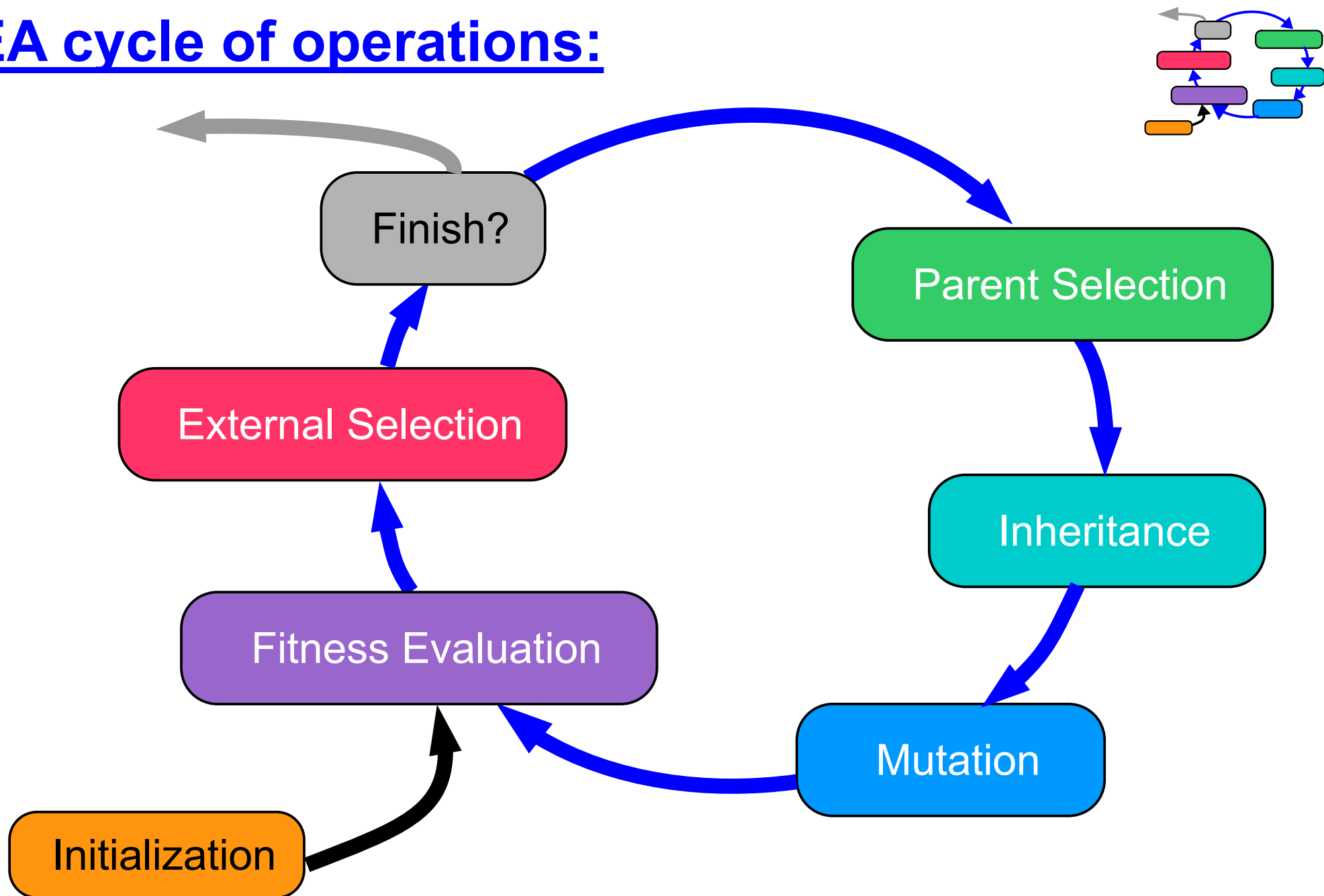
*The sequence below is not common theory, but just my personal choice of doing it.*

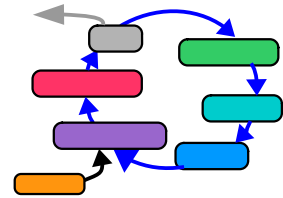
- |                            |  |
|----------------------------|--|
| <b>Objective:</b>          | specify the objective                  |
| <b>Genome:</b>             | structure the genome                   |
| <b>Fitness Function:</b>   | define an appropriate fitness function |
| <b>Inheritance:</b>        | layout the inheritance process         |
| <b>Mutation:</b>           | layout the mutation process            |
| <b>Selection Strategy:</b> | specify the selection strategy         |

# Overview:

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- **Super-individuals**
- External-selection and parent-selection combined
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  - Wheel of fortune
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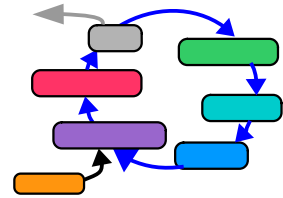
# EA cycle of operations:



**EA:****Super-Individual**

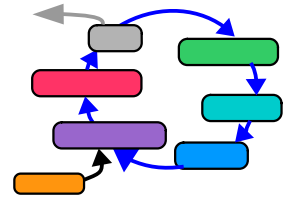
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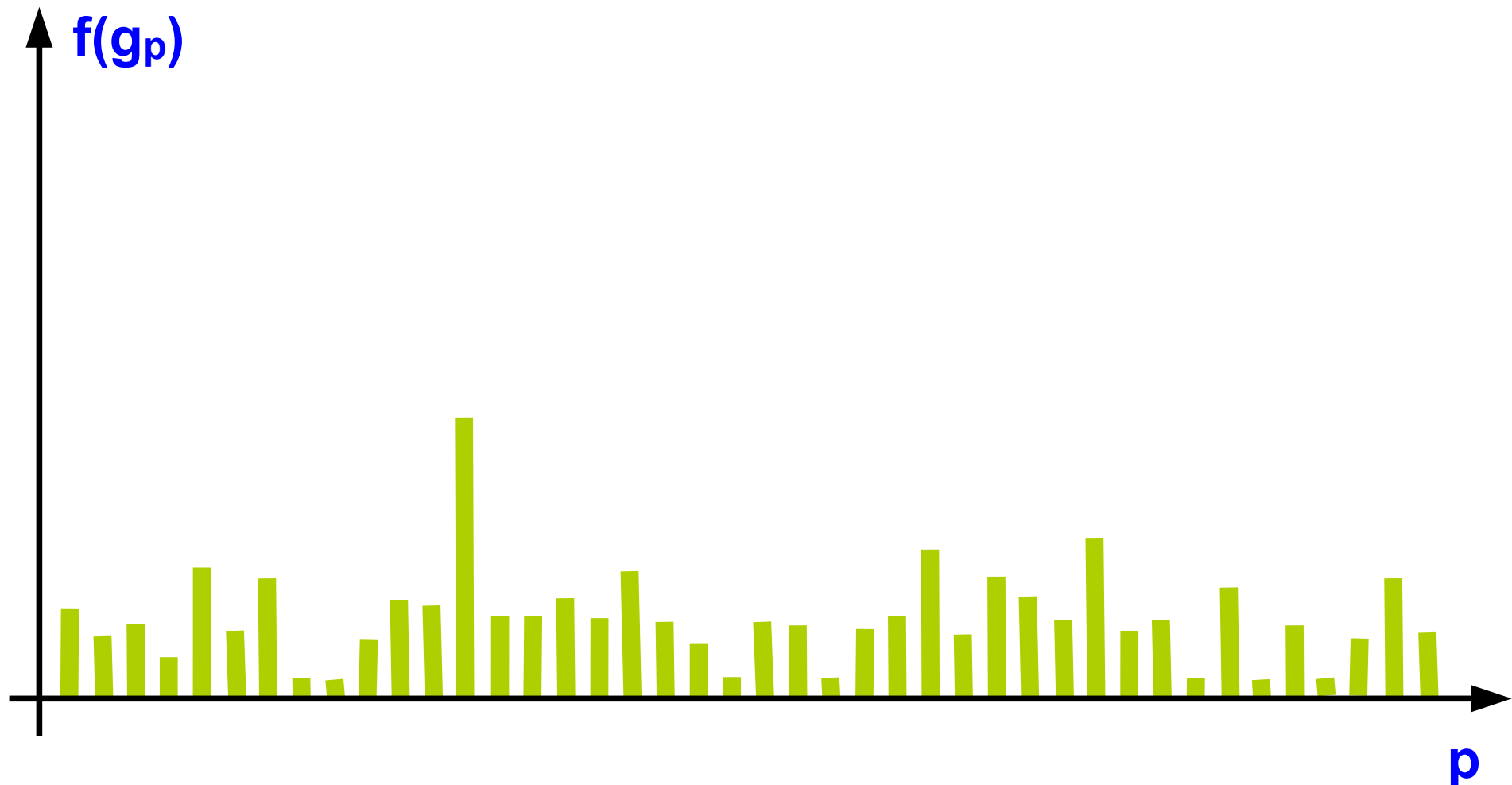
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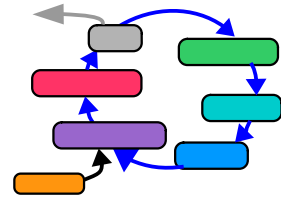
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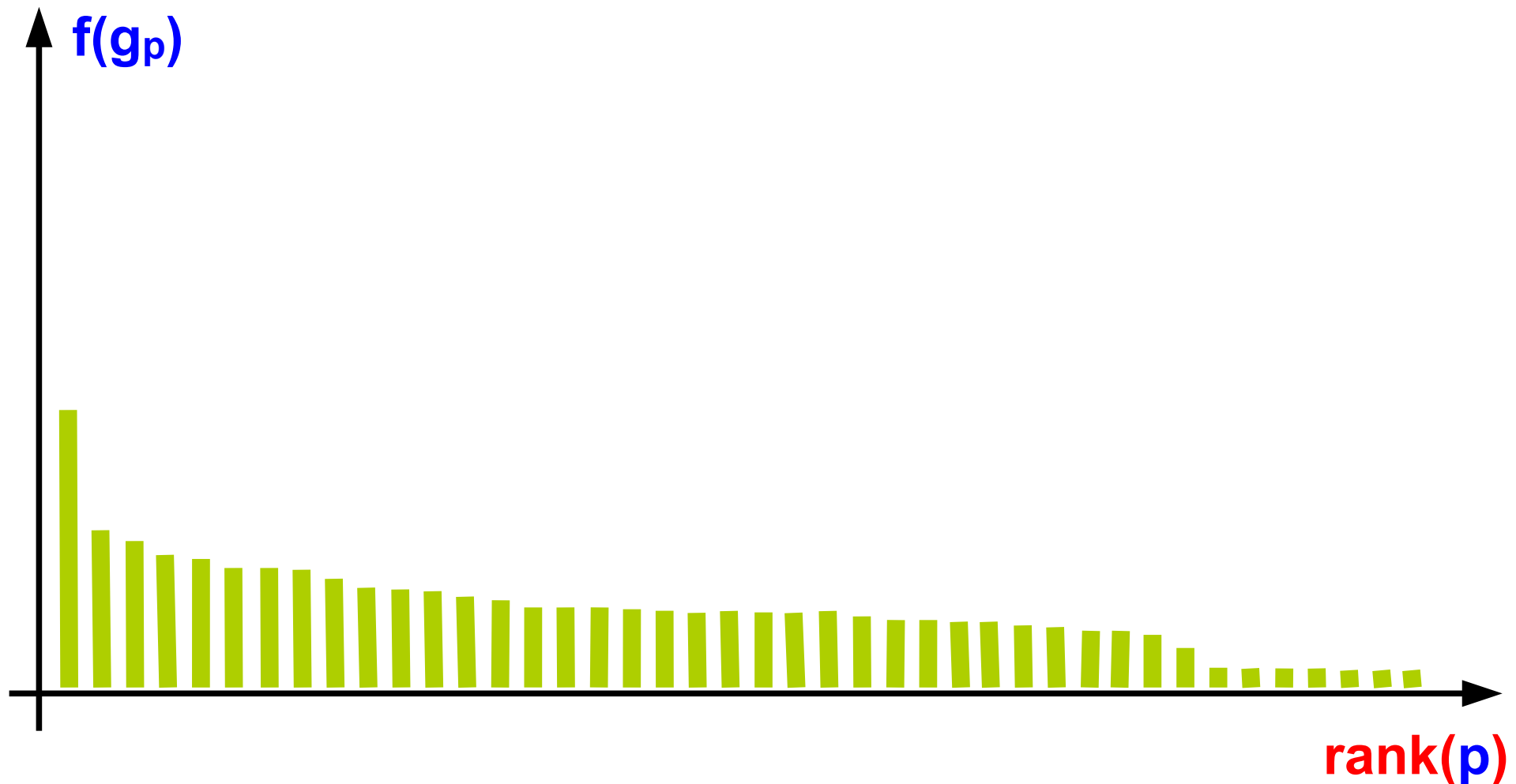
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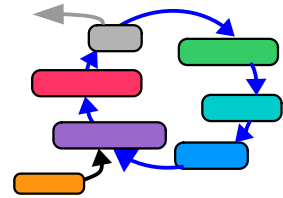
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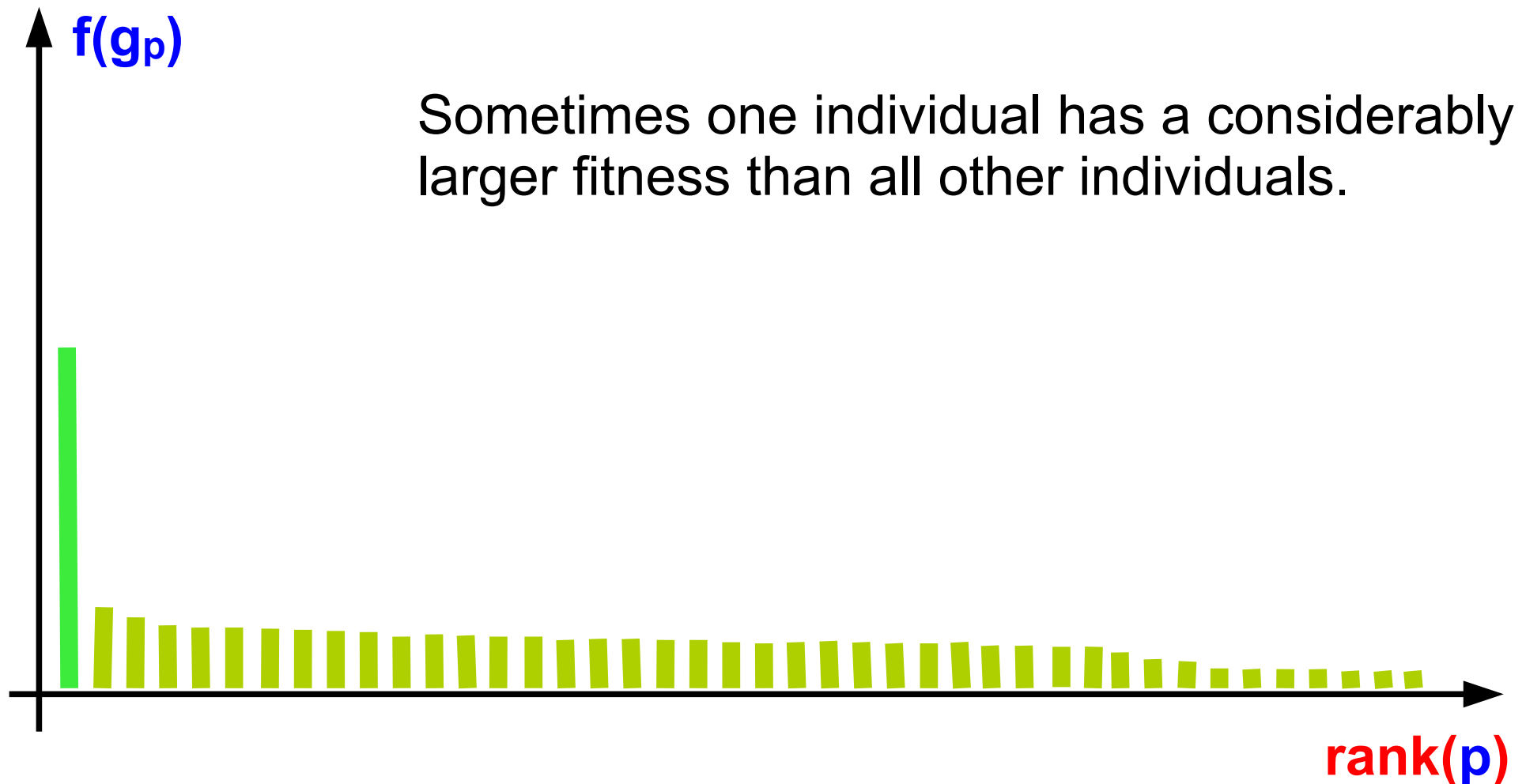
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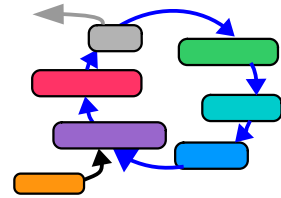
Sorted fitness values.



EA:**Super-Individual**

Sorted fitness values.



**EA:****Super-Individual**

Sometimes, the combination of **selection** and **inheritance** is producing a so called: **Super-Individual**.

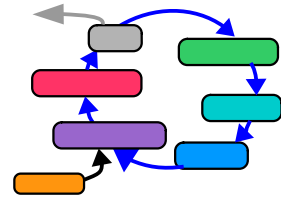
The fitness values throughout the population will typically vary.

In the case, that one individual has a considerably larger fitness than all other individuals, it can happen that this individual is selected more often

(e.g. fitness proportional selection,  $\mu \ll \lambda$  , ...).

## EA:

### Super-Individual



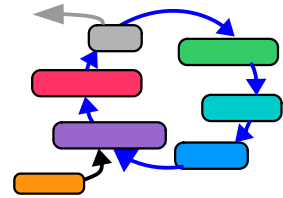
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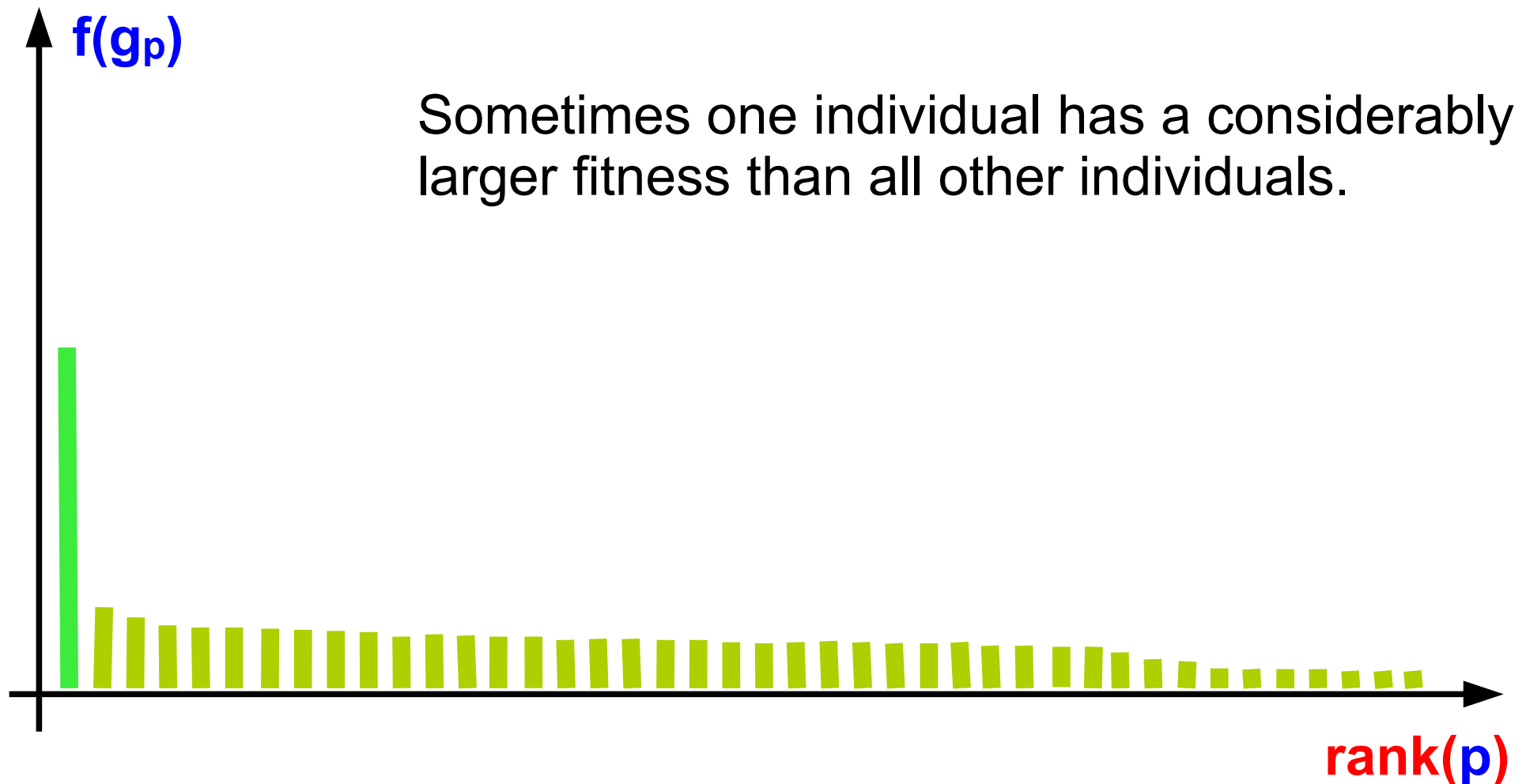
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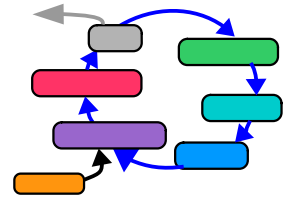
(e.g. fitness proportional selection,  $\mu \ll \lambda$ , ...).

Thus, it will produce more offspring than other individuals, increasing the number of individuals with a high fitness; which is explicitly intended by the principle of inheritance.

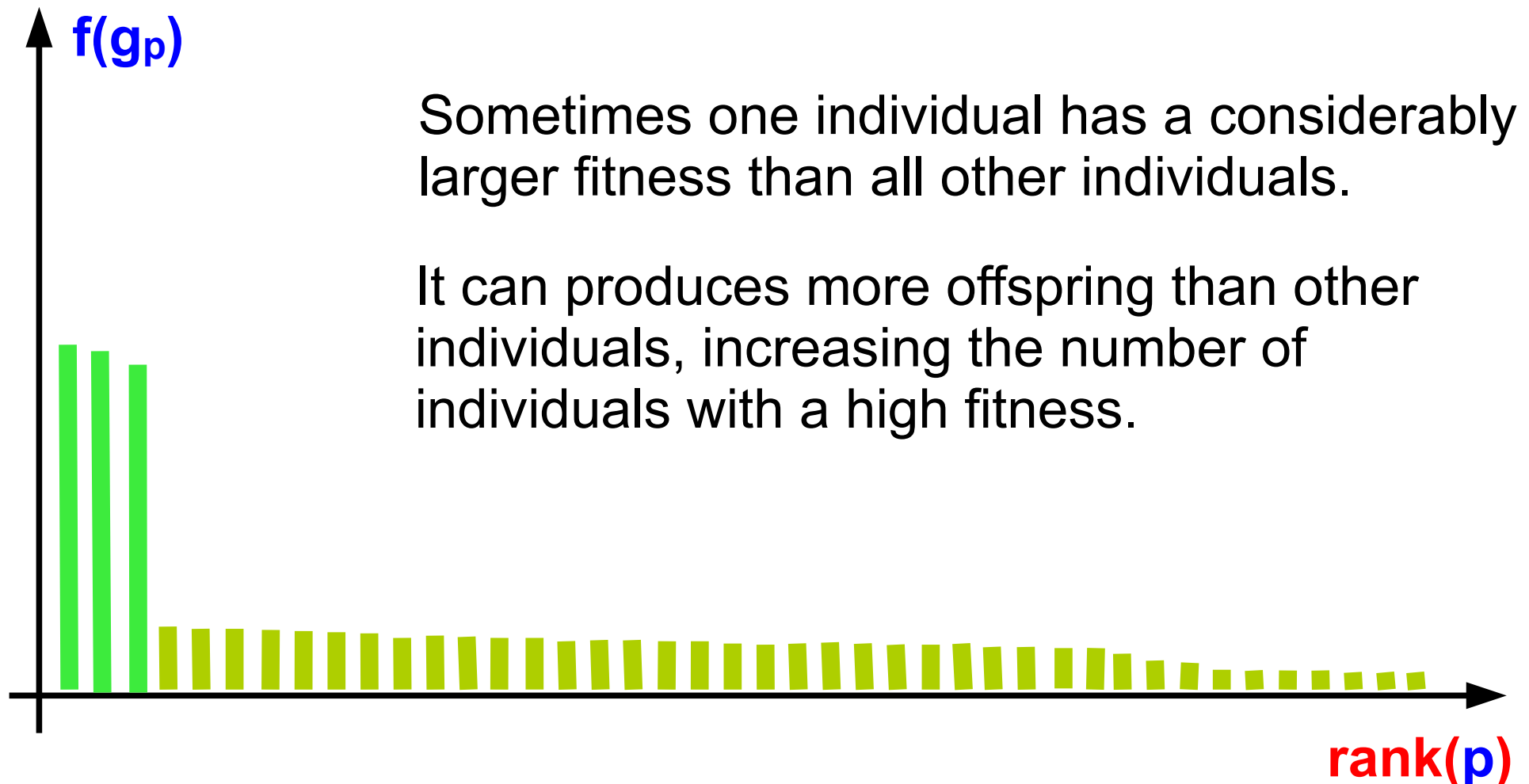
EA:**Super-Individual**

Sorted fitness values.

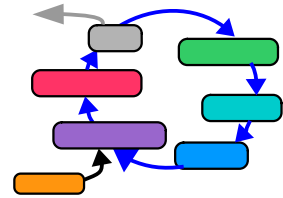


EA:**Super-Individual**

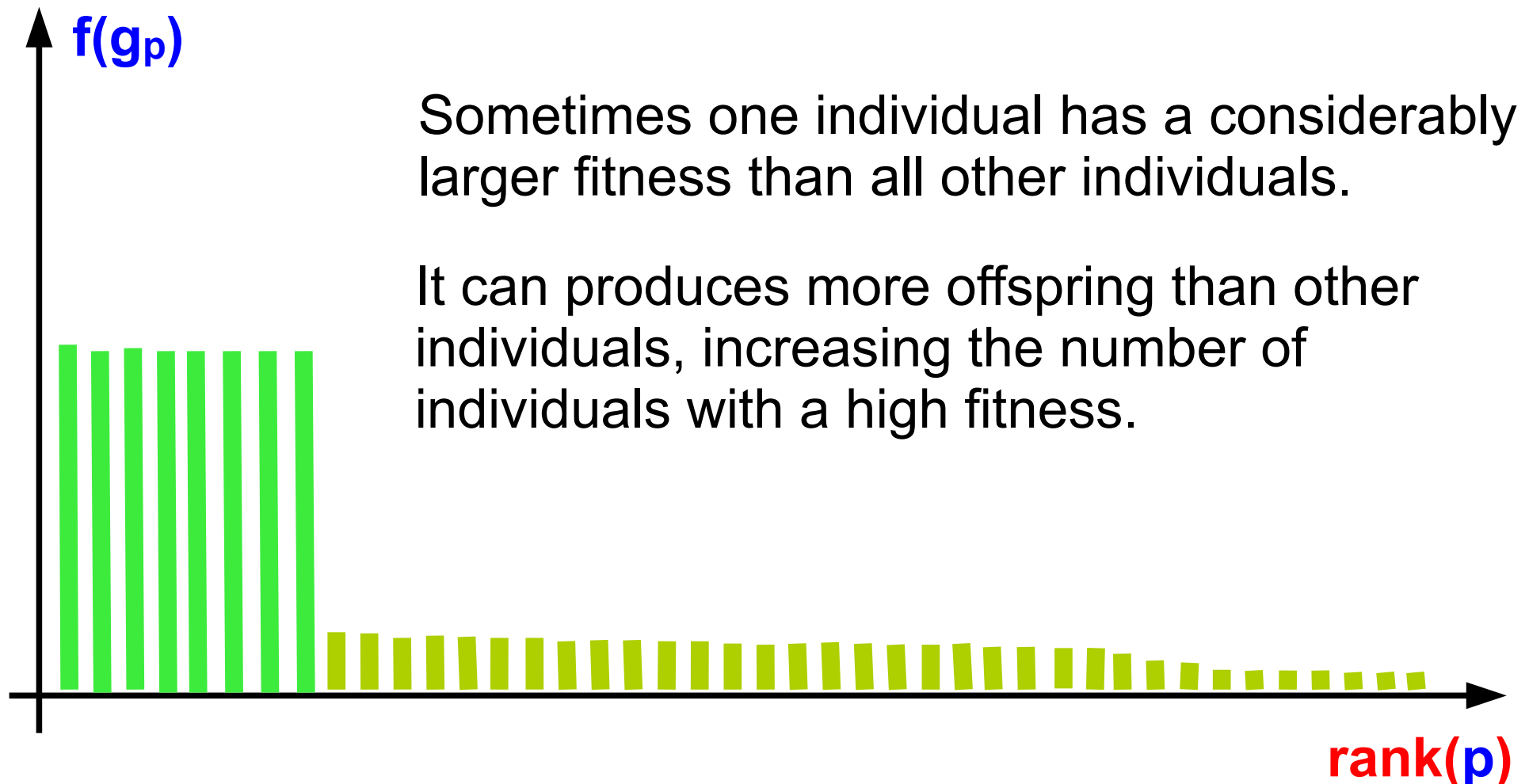
Sorted fitness values.

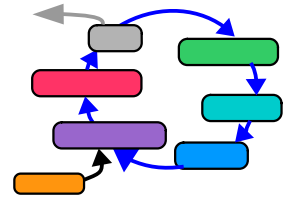




EA:**Super-Individual**

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**EA:****Super-Individual**

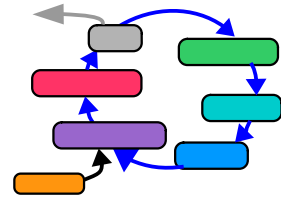
Sometimes, the combination of **selection** and **inheritance** is producing a so called: **Super-Individual**.

It can happen, that an individual with a rather high fitness is generating so much offspring, that they **dominate** the entire population.

Which means, that a large percentage of the population has identical (or almost identical) genomes.

## EA:

### Super-Individual



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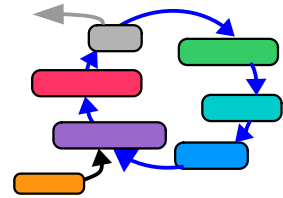
Which means, that a large percentage of the population has identical (or almost identical) genomes.

On one hand, a **Super-Individual** with a large fitness is good for the overall performance of the population,

on the other hand, if a large percentage of the population has identical genomes the **diversity** throughout the population is lost.

EA:

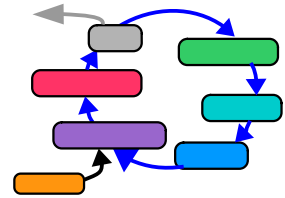
## Super-Individual



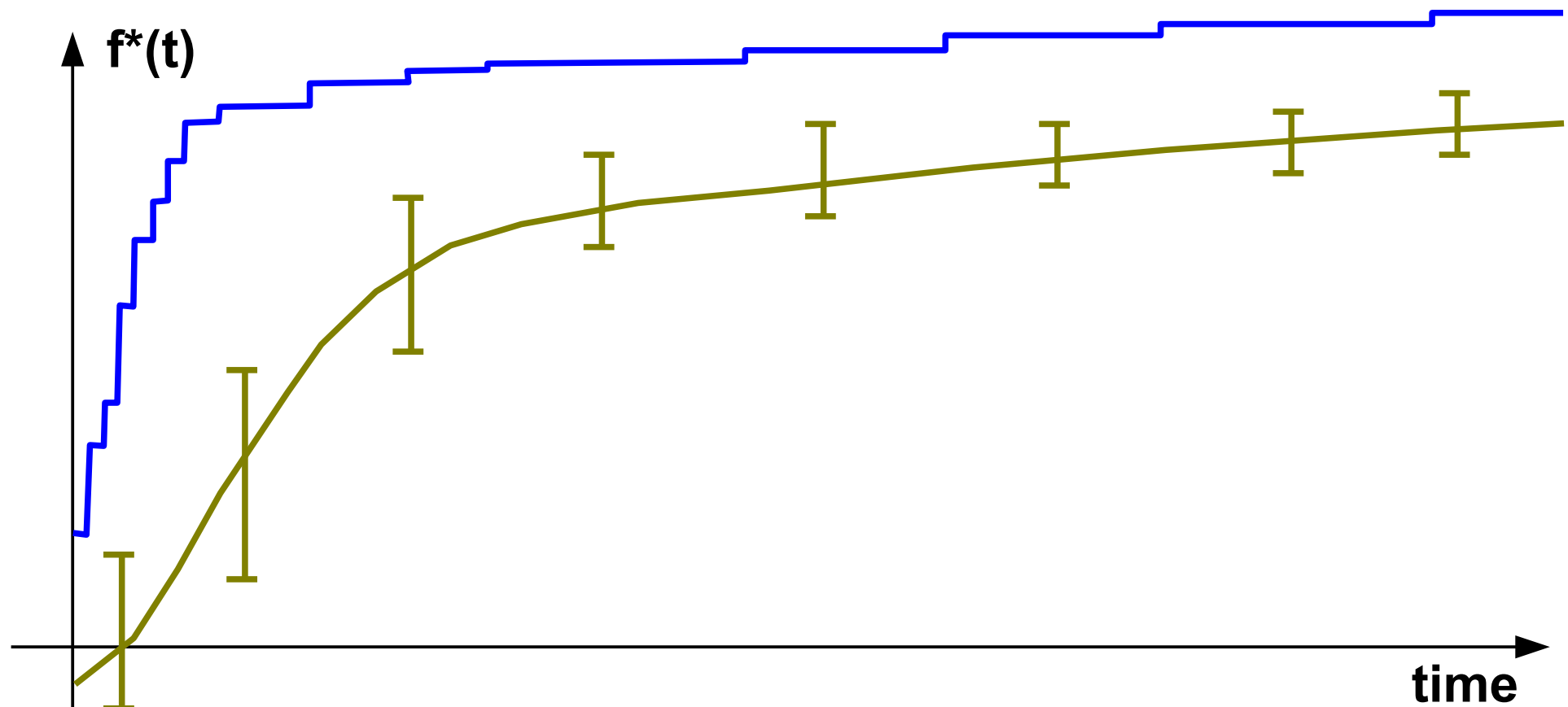
Generally speaking, the occurrence of a **super-individual** should be **avoided** to maintain the necessary diversity within the population (EAs are multi hypothesis approaches).

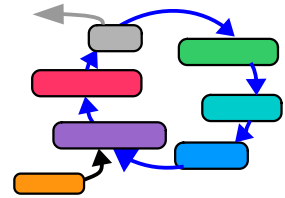
The detection of a super-individual can be really hard.  
A hint for the occurrence is a shrinking variance of fitness values in the parent population.

A close investigation of the performance graph is helpful.

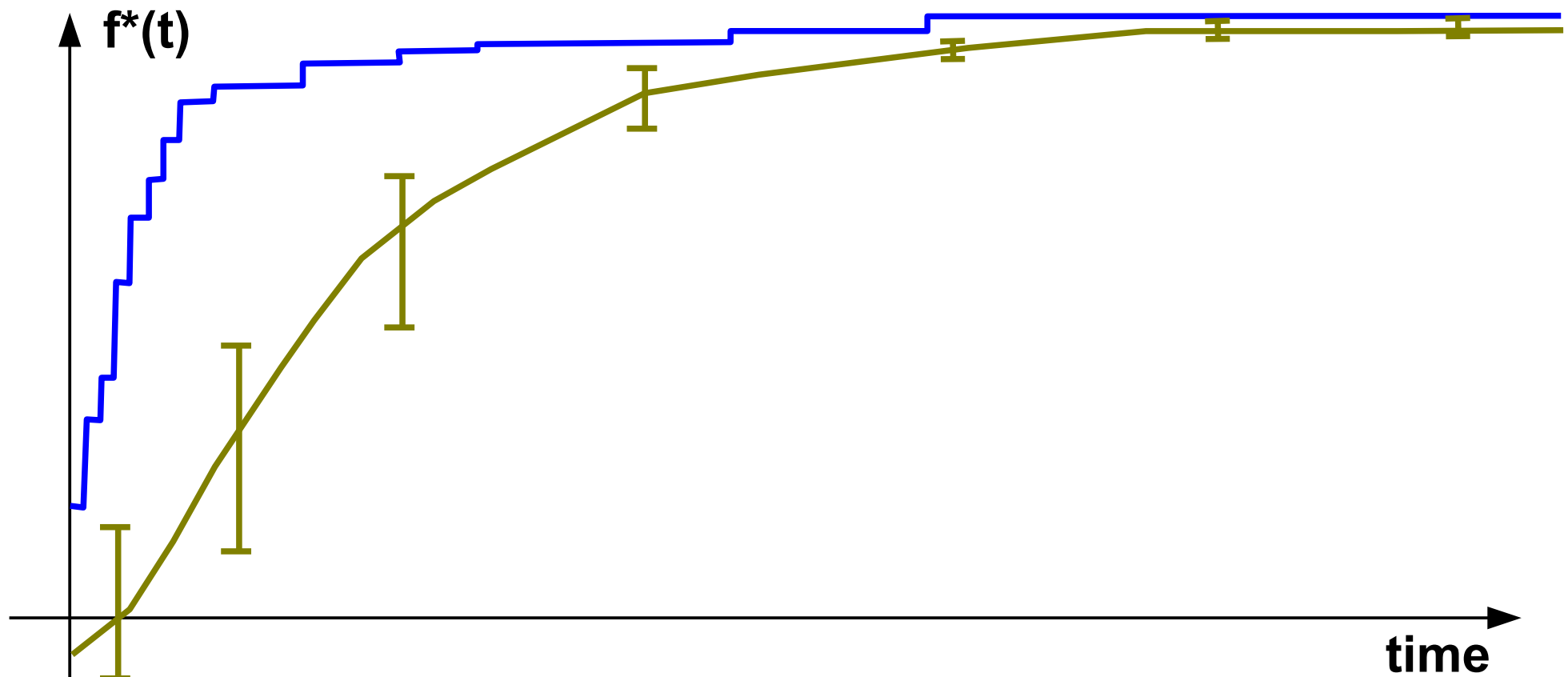
EA:**Super-Individual**

The performance graph is showing the development of the fitness  $f^*(t)$  of the best individual and the average fitness in each generation with respect to time.



EA:**Super-Individual**

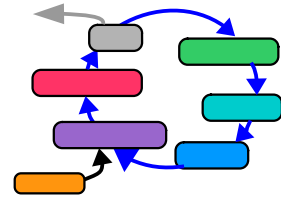
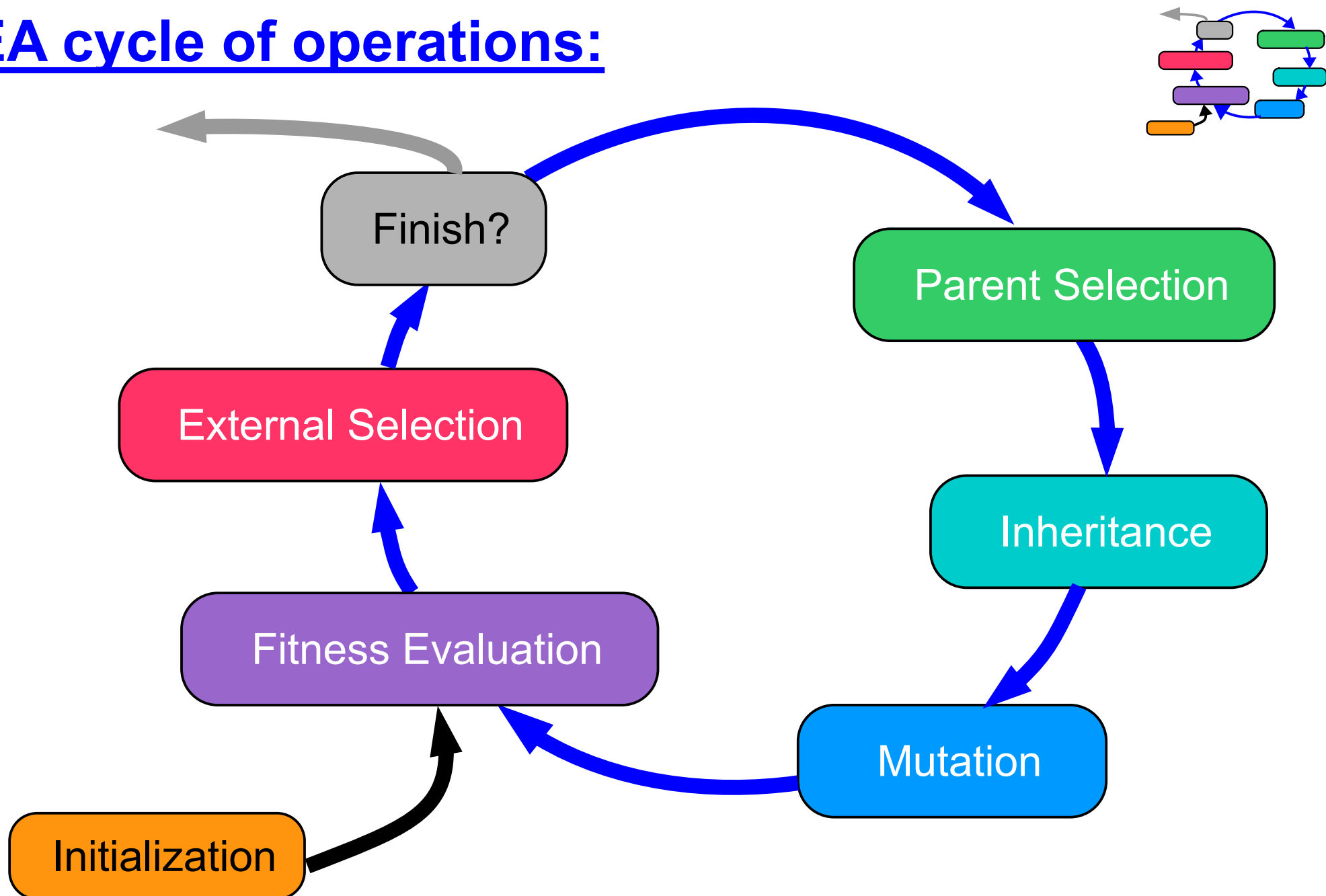
The performance graph might me an **indicator** for the occurrence of a **super-individual** dominating the population.



# Overview

- Genome structure
- Example: 8 queens
- Super-individuals
- **External-selection and parent-selection combined**
- Probabilistic parent-selection
  - Wheel of fortune
  - Softmax selection
  - Tournament selection
- Genetic programming
- Co-evolution

# EA cycle of operations:

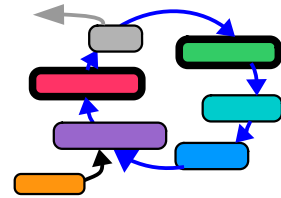




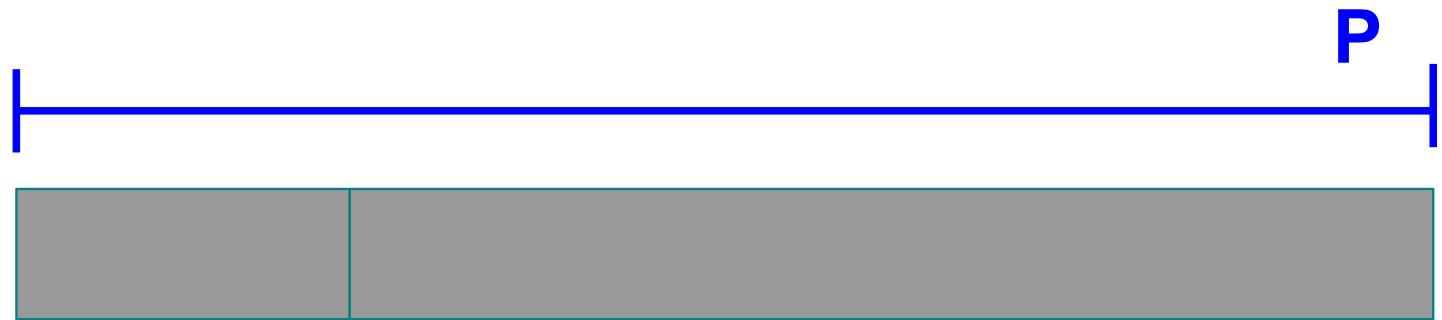
EA:

External Selection

Parent Selection



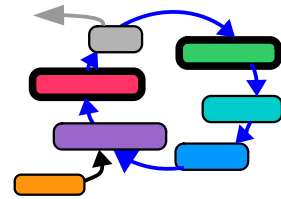
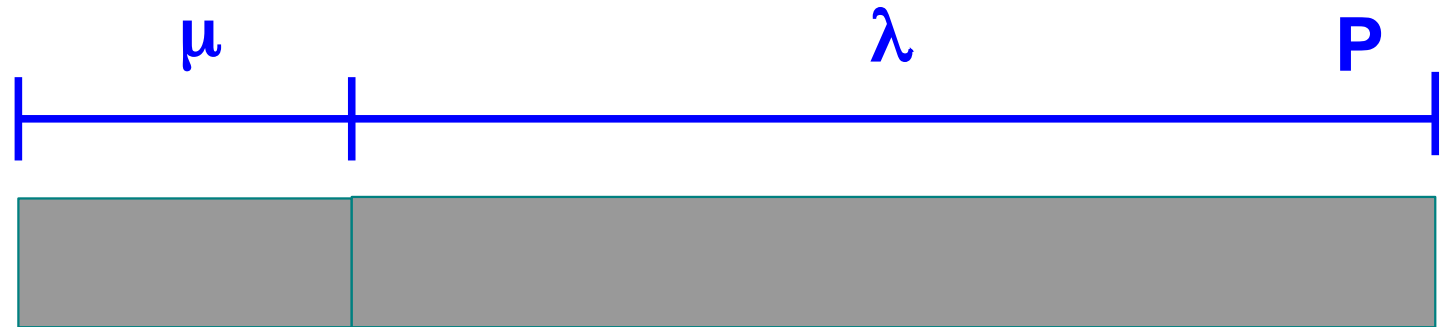
Have  $P$ , keep  $\mu$ , generate  $\lambda$  offspring



EA:

External Selection

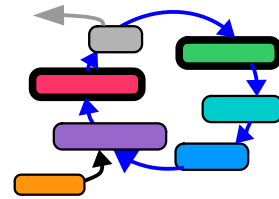
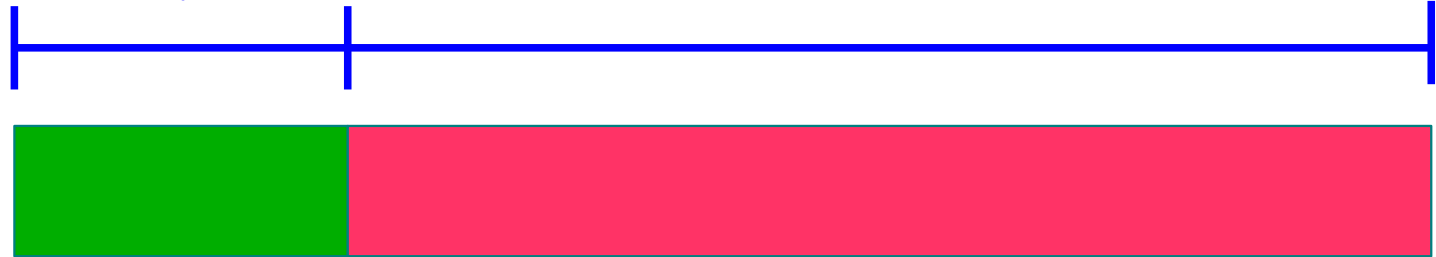
Parent Selection

Have **P**, keep  $\mu$ , generate  $\lambda$  offspring

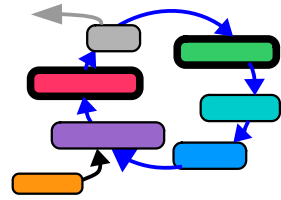
EA:

External Selection

Parent Selection

Have **P**, keep  $\mu$ , generate  $\lambda$  offspring $\mu$  $\lambda$ **P**external  
selection

# Parent Selection



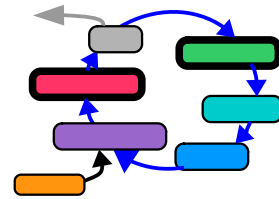
P

The diagram illustrates a 1D array partitioning. A horizontal line is divided into two segments. The left segment is green and labeled "keep". The right segment is pink and labeled "discard".

EA:

External Selection

Parent Selection



Have **P**, keep  $\mu$ , generate  $\lambda$  offspring

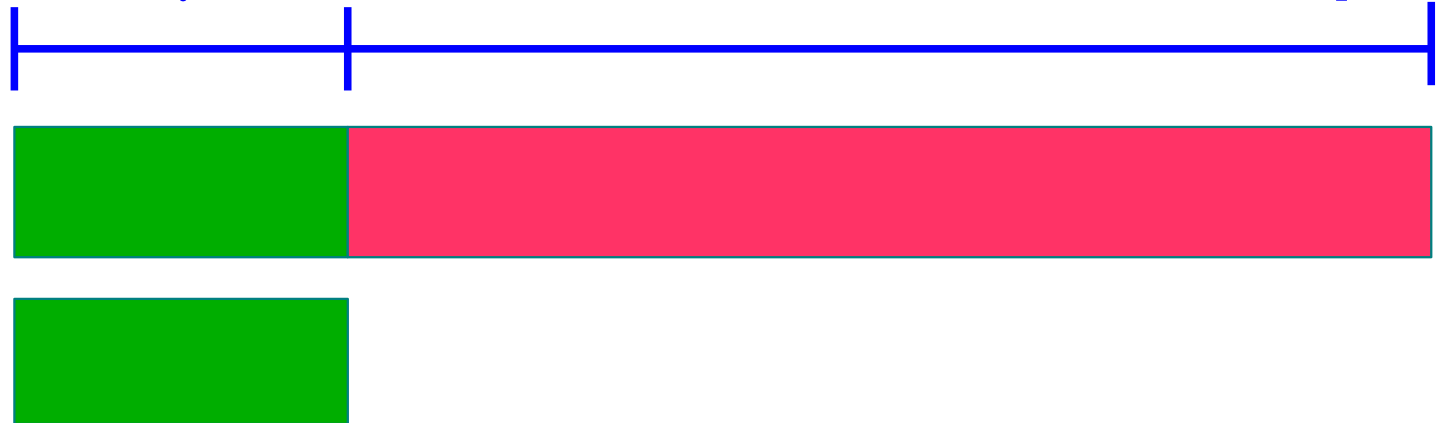
$\mu$

$\lambda$

**P**

external  
selection

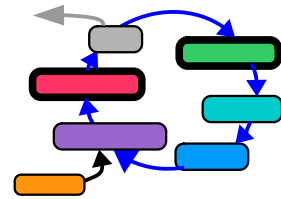
$\mu$  parents



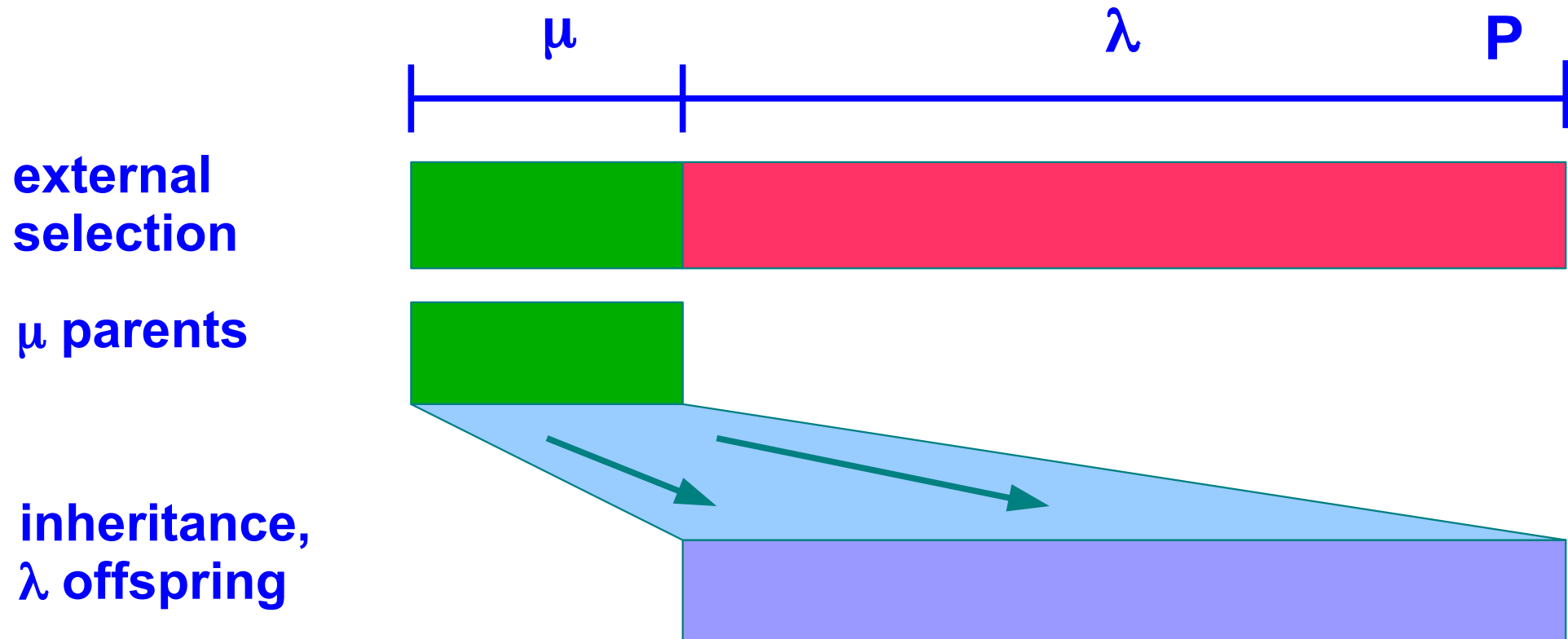
EA:

External Selection

Parent Selection



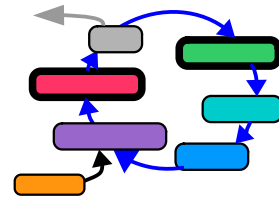
Have  $P$ , keep  $\mu$ , generate  $\lambda$  offspring



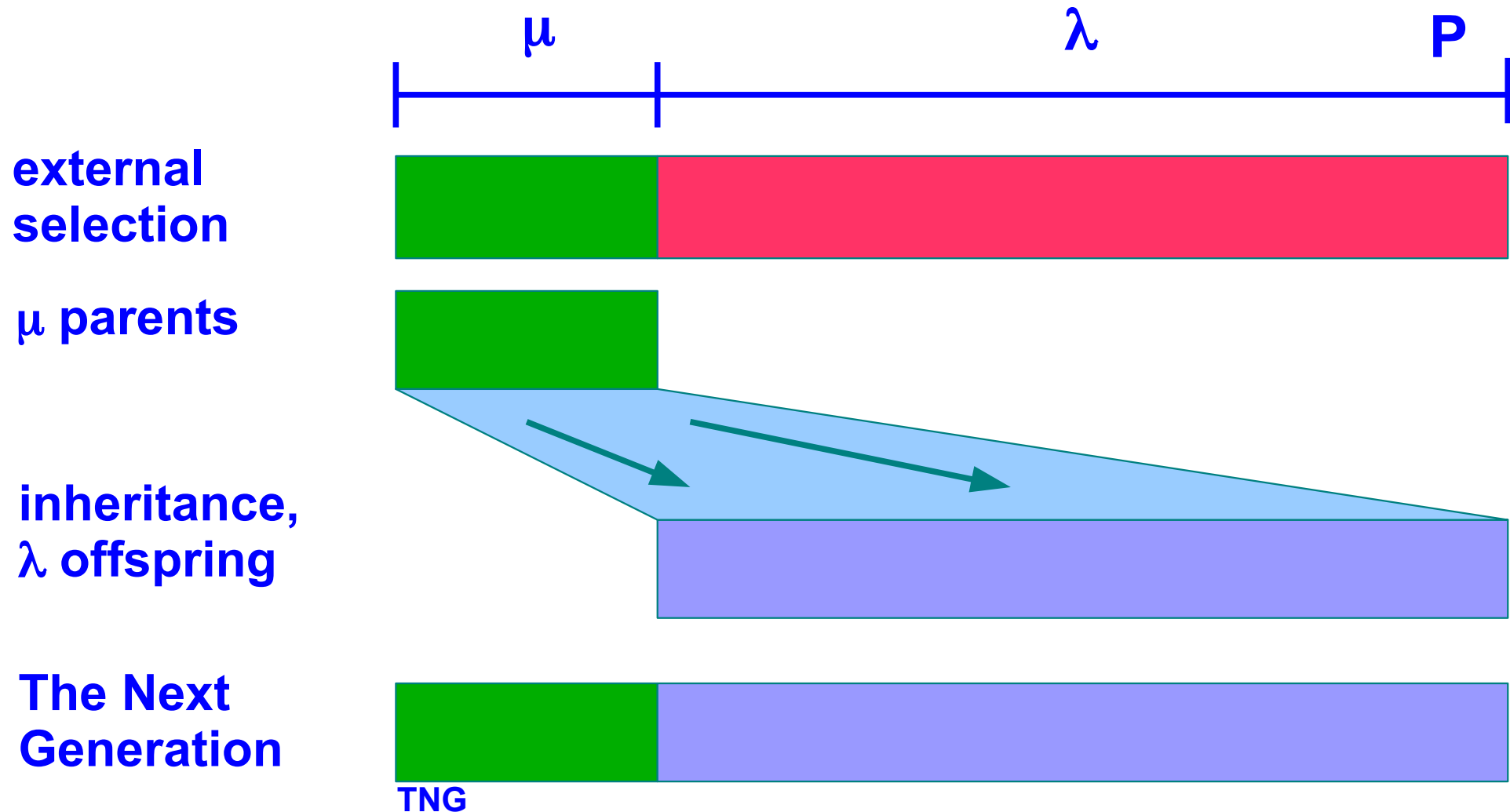
EA:

External Selection

Parent Selection



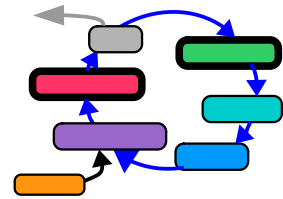
Have  $P$ , keep  $\mu$ , generate  $\lambda$  offspring



EA:

External Selection

Parent Selection



(  $1 + 1$  ):  $\mu=1$  one parent,  $\lambda=1$  one child,  
inheritance by copying, only mutation  
rank based, deterministic external selection

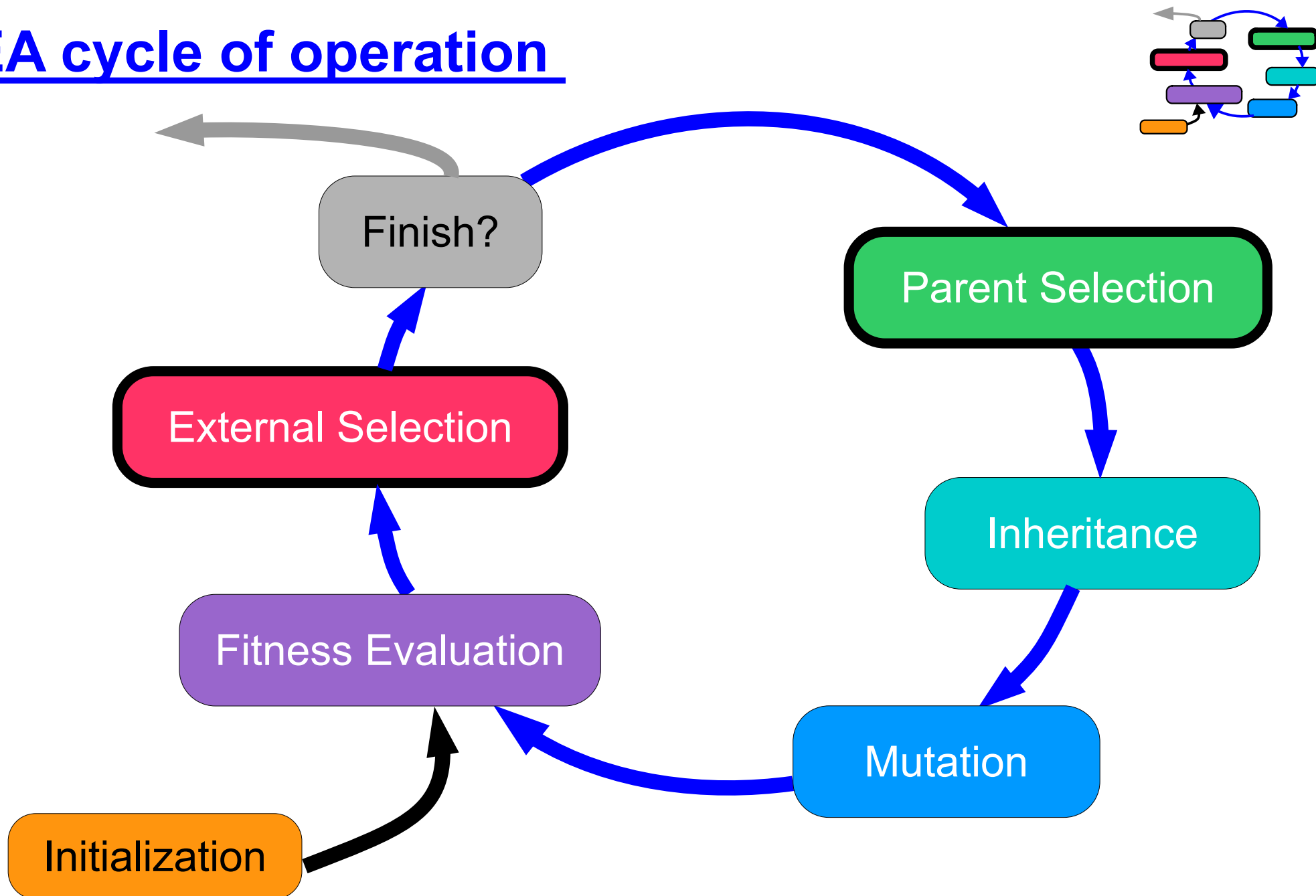
(  $1 + \lambda$  ):  $\mu=1$  one parent,  $\lambda$  children, offspring,  
inheritance by copying, only mutation  
rank based, deterministic external selection

(  $\mu + \lambda$  ):  $\mu$  parents,  $\lambda$  offspring, parents survive  
recombination, mutation, external selection.

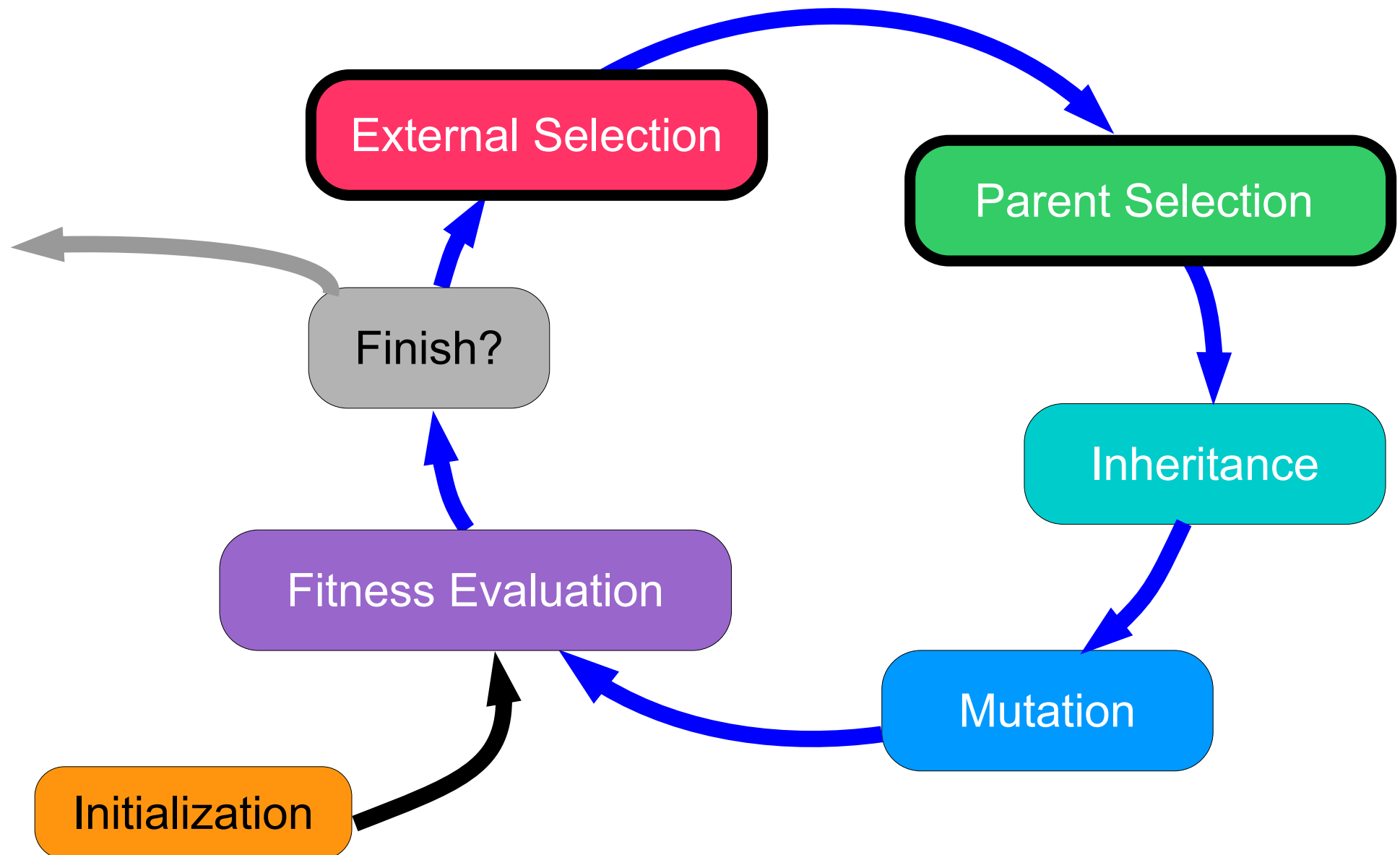
(  $\mu, \lambda$  ):  $\mu$  parents,  $\lambda$  offspring,  
recombination, mutation, external selection,  
parents are discarded.



# EA cycle of operation



# EA cycle of operation



EA:

## Parent Selection

## External Selection

An alternative scheme to operate the evolutionary algorithm is to **separate** parent selection from external selection.

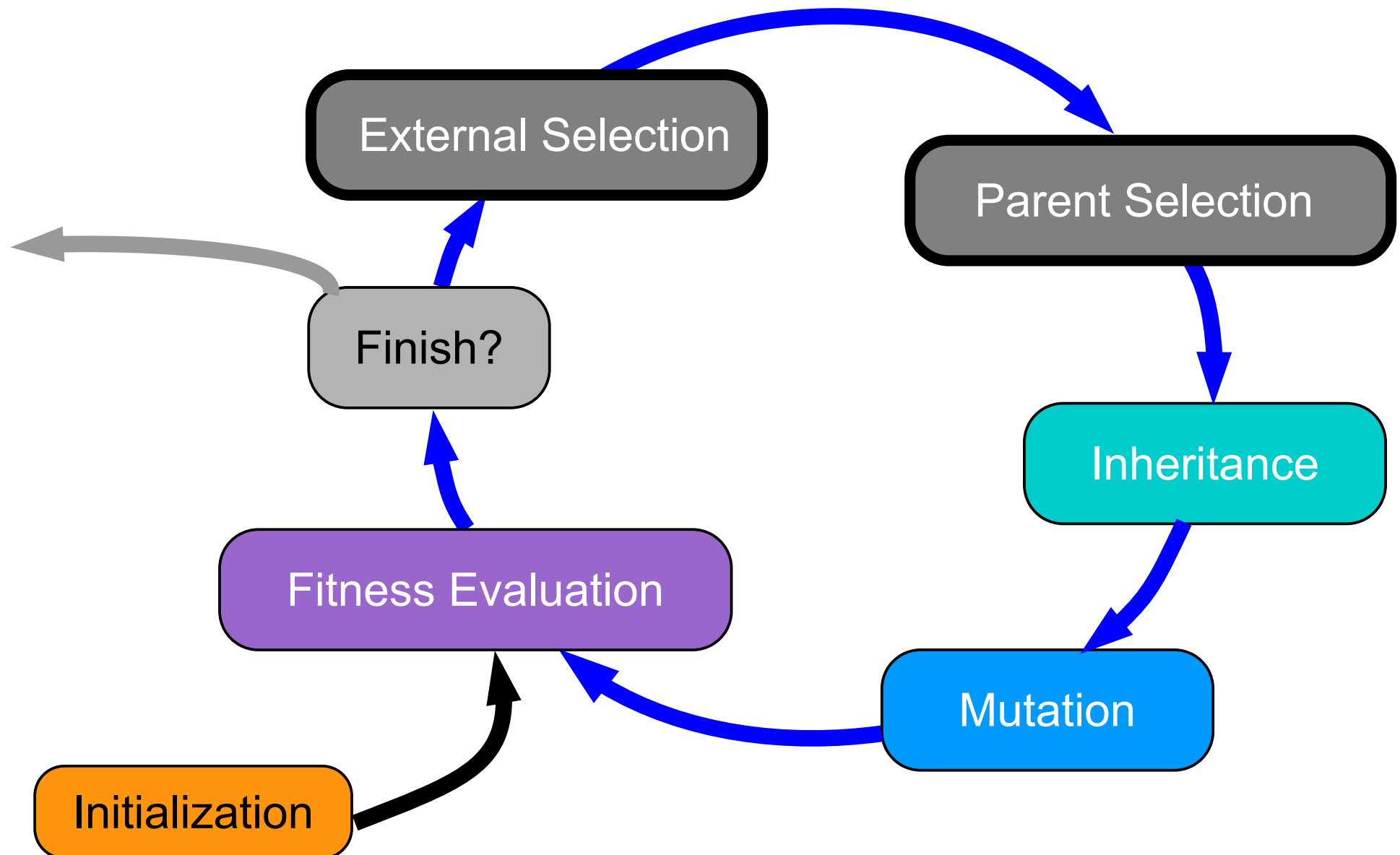
Then, within **external selection**, the  $\mu$  individuals to survive, are selected from the complete population of  $P$  individuals, and  $\lambda$  individuals are discarded .

And, within **parent selection** the parents are selected from the complete population as well, building the pool of parents for subsequent inheritance.

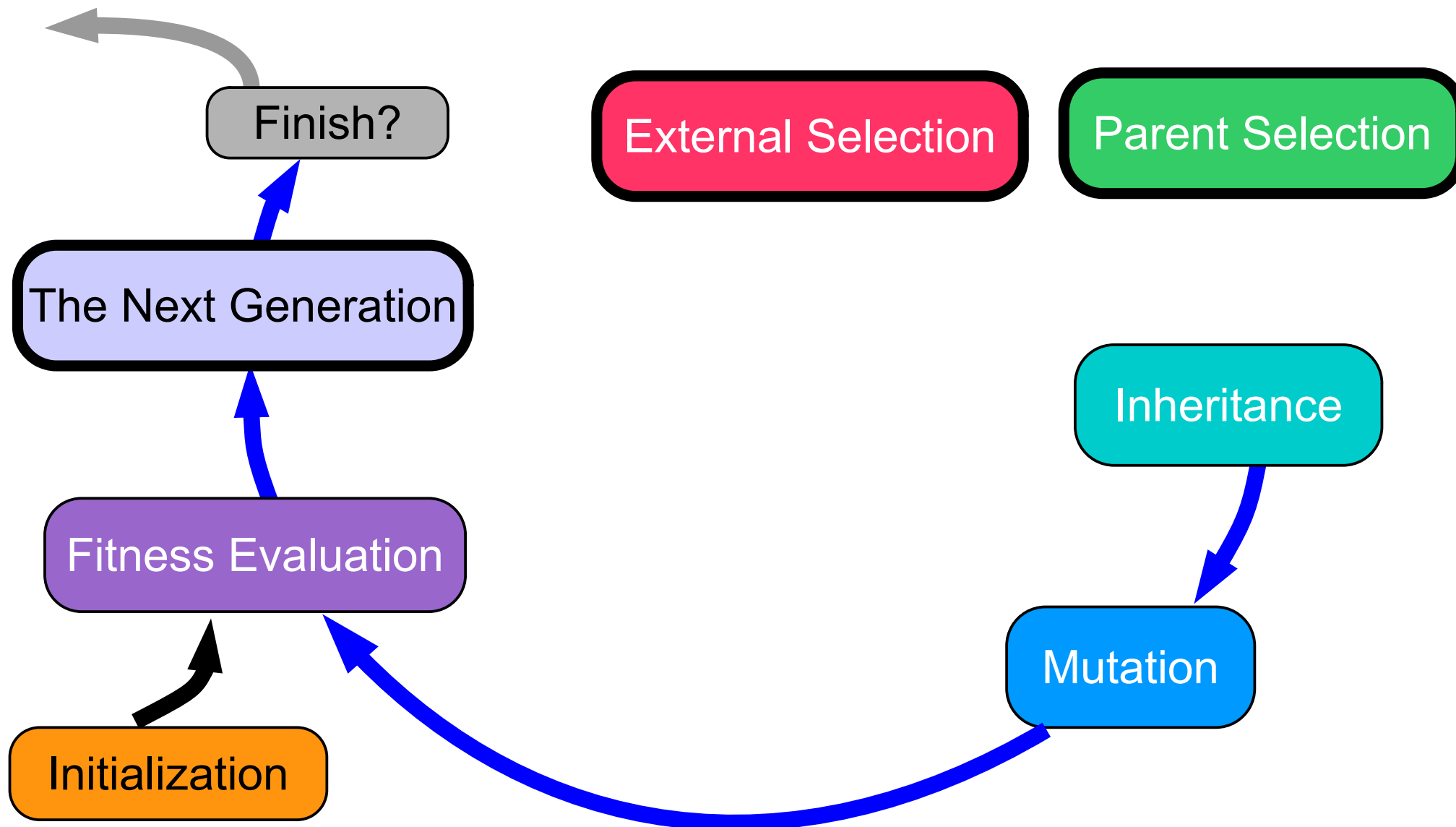
The **inheritance step** generates  $\lambda$  new individuals, from the pool of parents; the pool of parents is erased afterwards.

The Next Generation is build by combining the  $\mu$  survivors with the  $\lambda$  offspring ( $\mu + \lambda = P$ ).

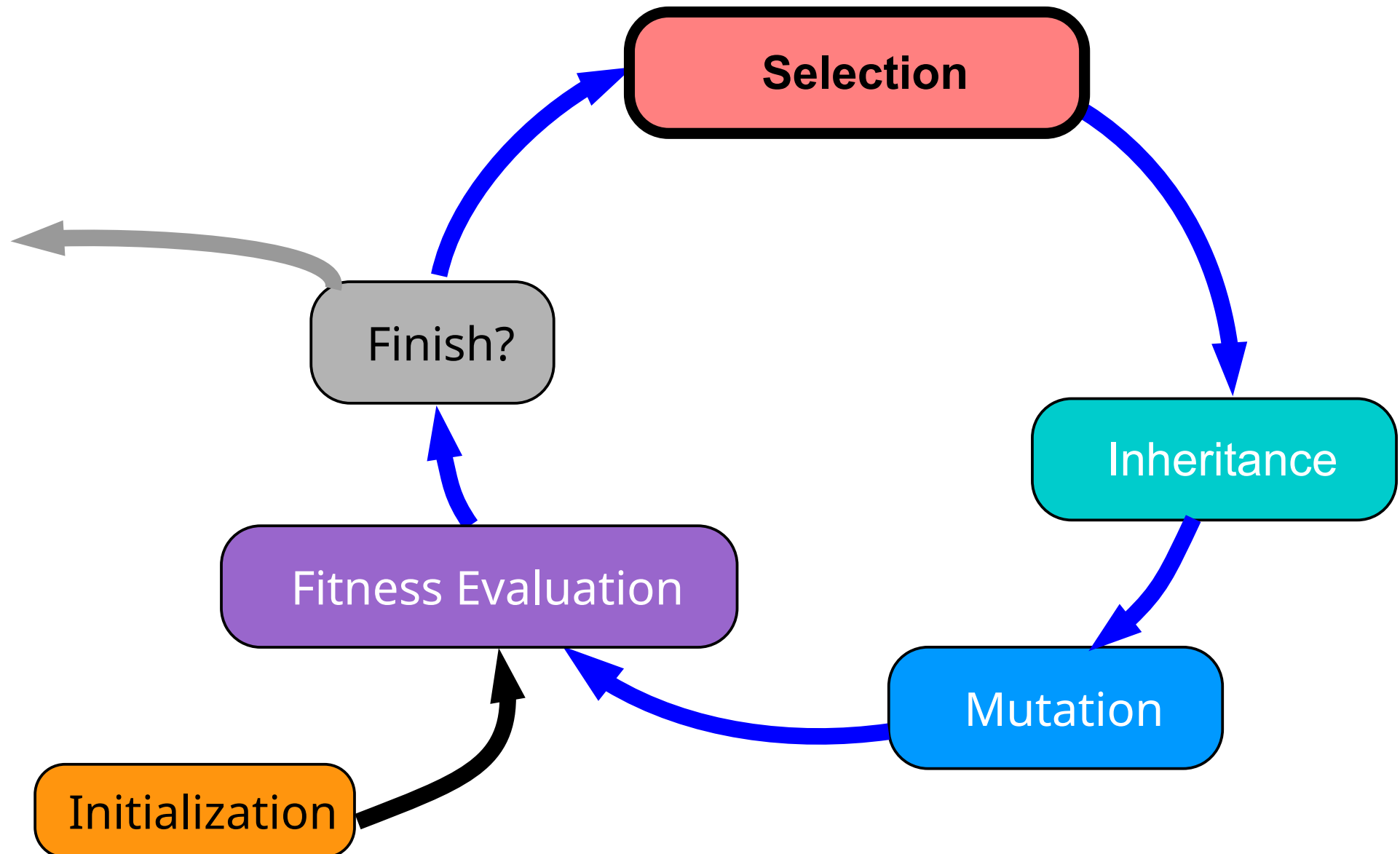
# EA cycle of operation



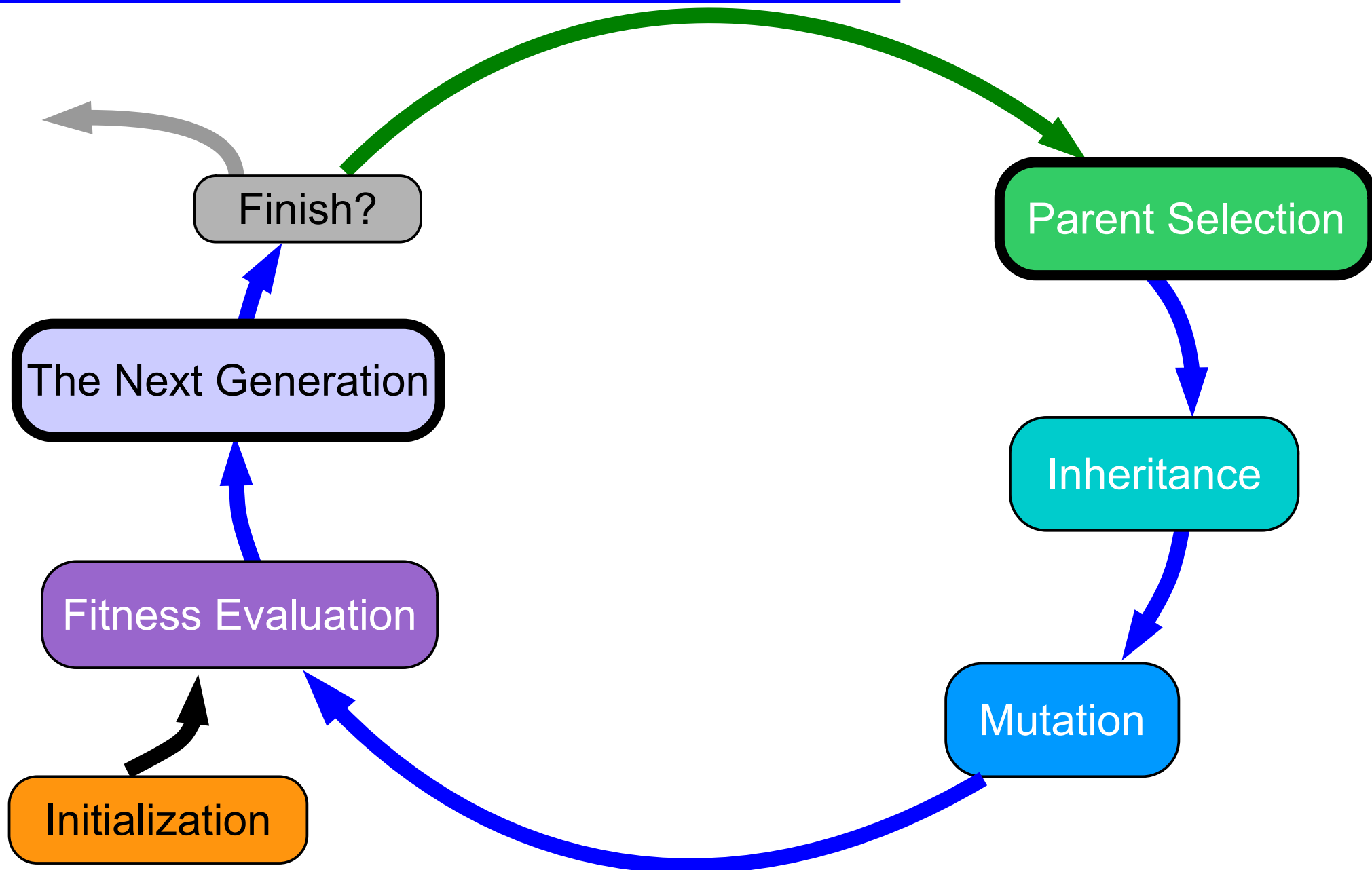
# EA alternative cycle of operation



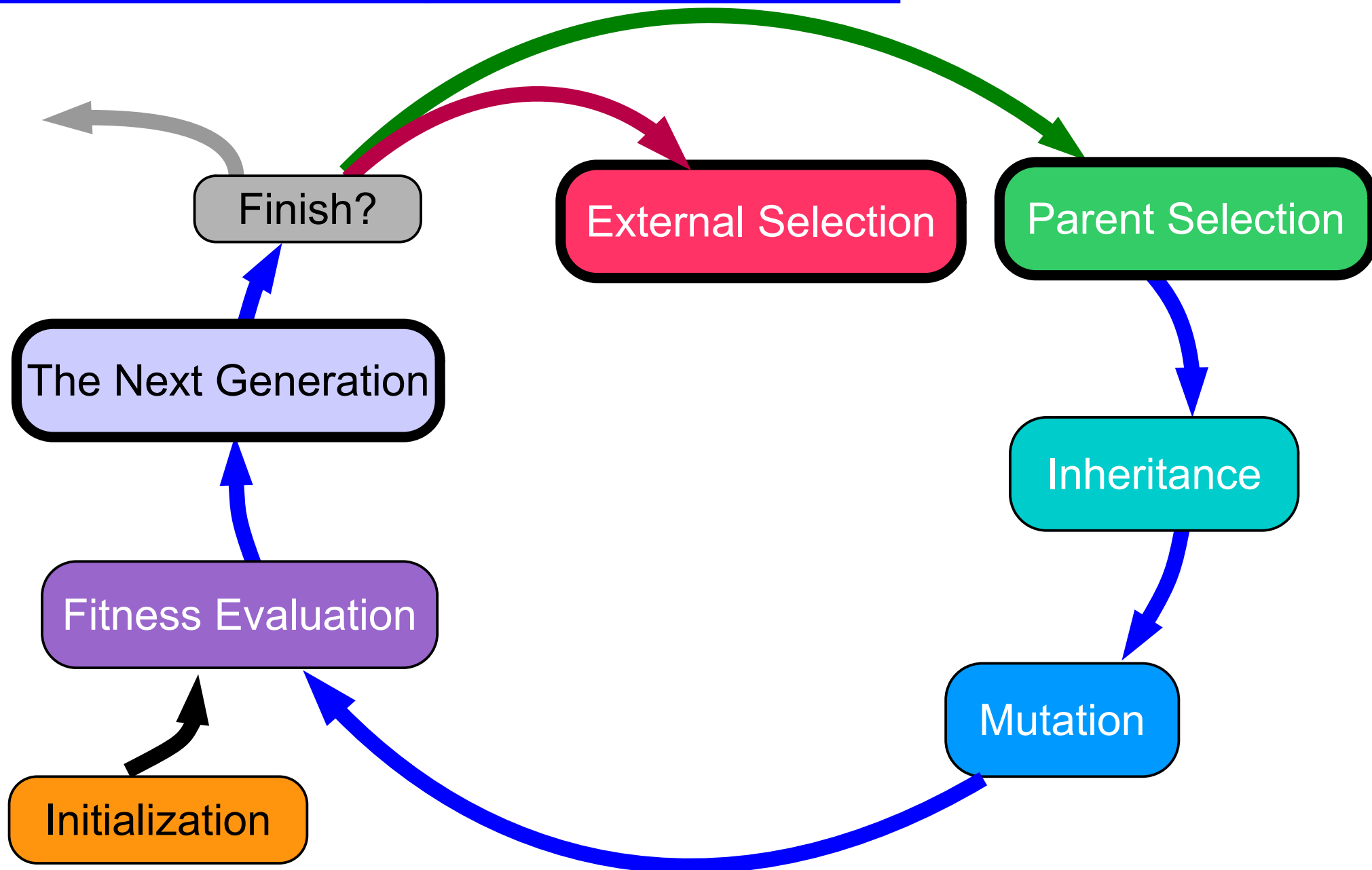
# EA cycle of operation



# EA alternative cycle of operation

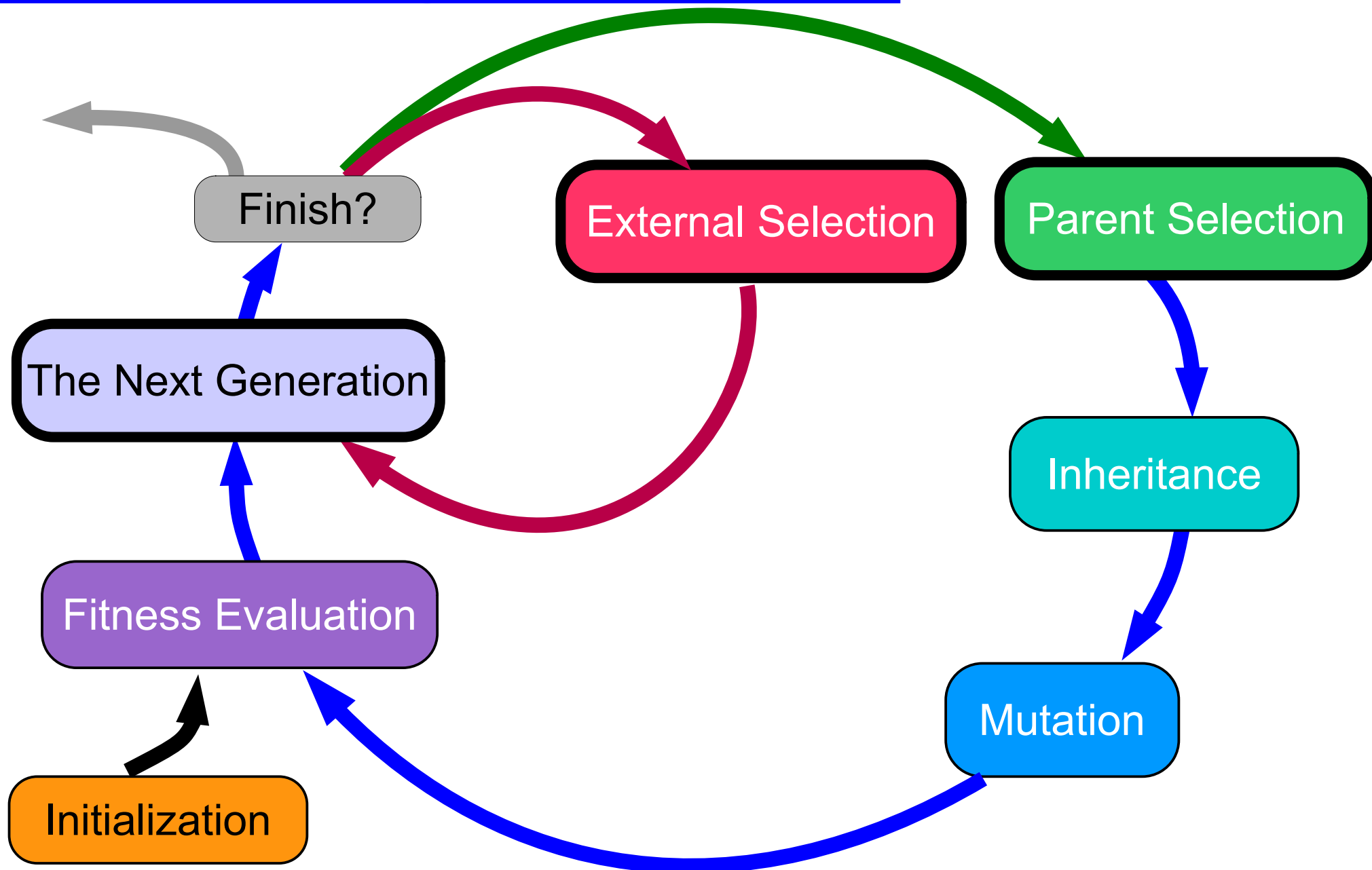


# EA alternative cycle of operation





# EA alternative cycle of operation

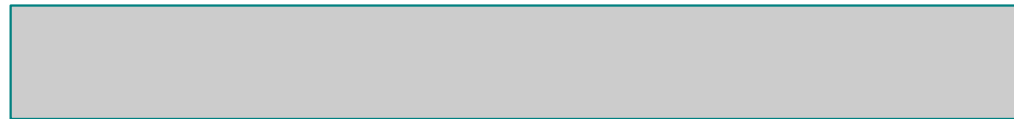


EA:

Parent Selection

External Selection

Have  $P$ , keep  $\mu$ , generate  $\lambda$  offspring

 $P$ 

EA:

Parent Selection

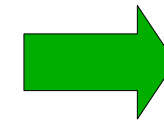
External Selection

Have  $P$ , keep  $\mu$ , generate  $\lambda$  offspringparent  
selection $P$

EA:

Parent Selection

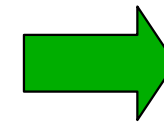
External Selection

Have  $P$ , keep  $\mu$ , generate  $\lambda$  offspringparent  
selection $P$ pool of  
parents

EA:

Parent Selection

External Selection

Have  $P$ , keep  $\mu$ , generate  $\lambda$  offspringparent  
selection $P$ pool of  
parentsexternal  
selection

EA:

Parent Selection

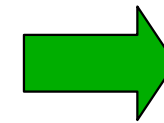
External Selection

Have  $P$ , keep  $\mu$ , generate  $\lambda$  offspring

parent  
selection



$P$



pool of  
parents



external  
selection



EA:

Parent Selection

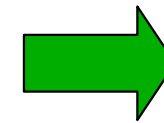
External Selection

Have  $P$ , keep  $\mu$ , generate  $\lambda$  offspring

parent  
selection



$P$

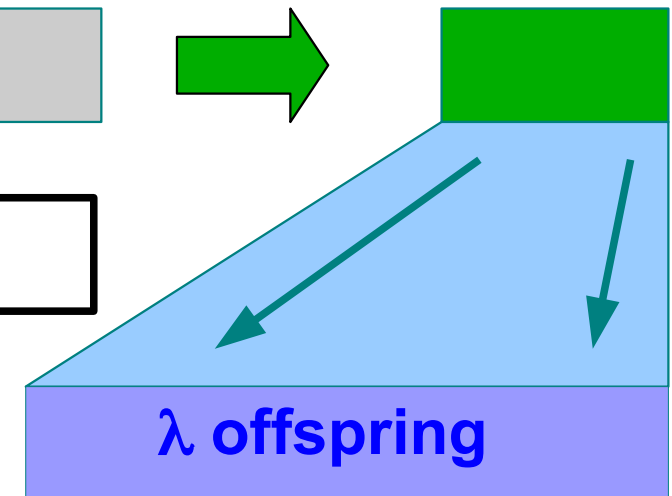


pool of  
parents

external  
selection



inheritance,  
 $\lambda$  offspring



$\lambda$  offspring

EA:

Parent Selection

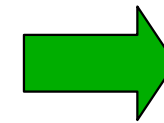
External Selection

Have  $P$ , keep  $\mu$ , generate  $\lambda$  offspring

parent  
selection



$P$

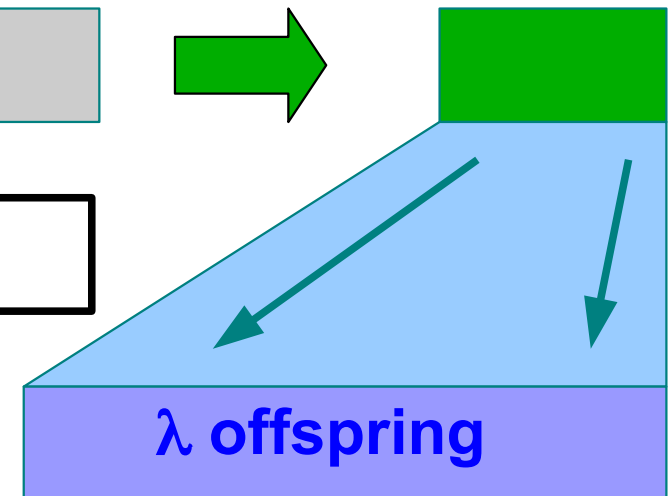


pool of  
parents

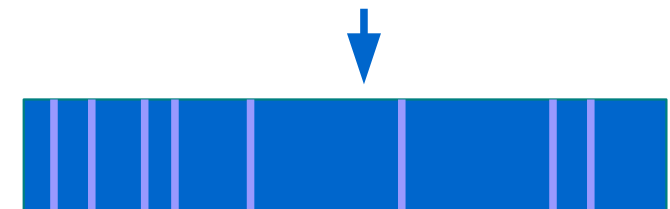
external  
selection



inheritance,  
 $\lambda$  offspring



mutation



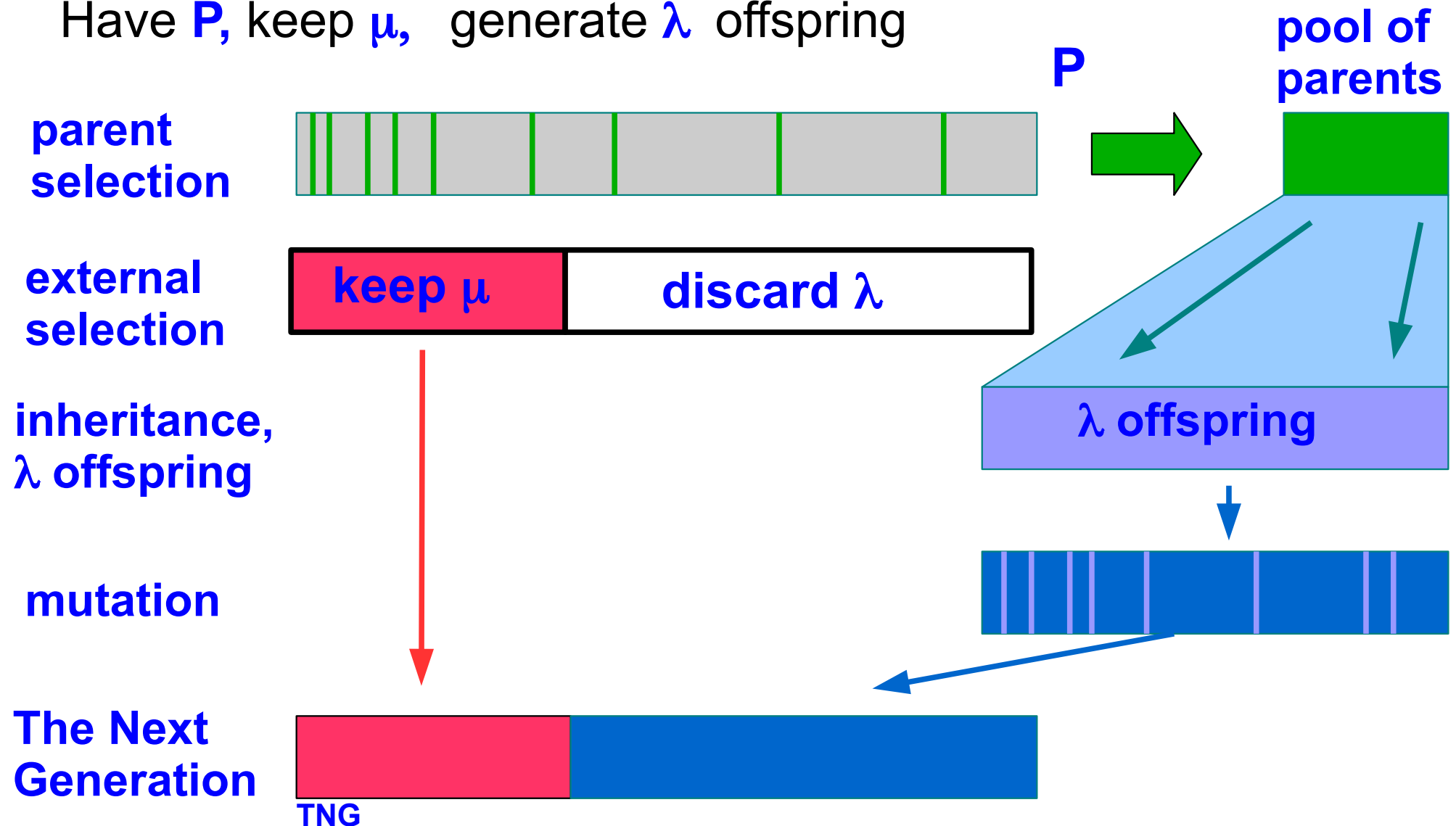


EA:

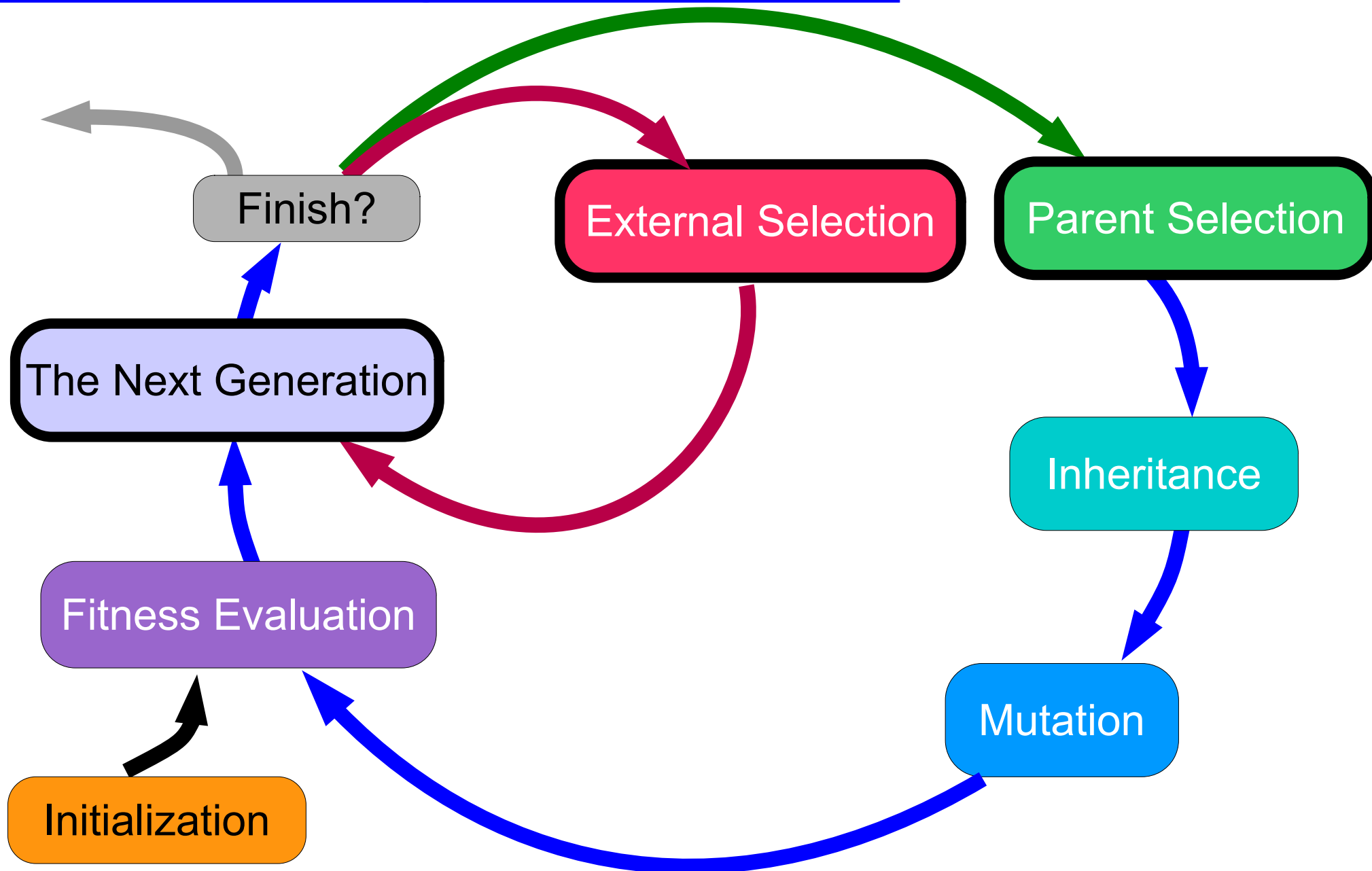
Parent Selection

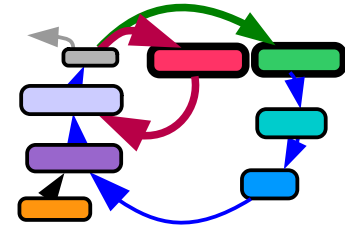
External Selection

Have  $P$ , keep  $\mu$ , generate  $\lambda$  offspring



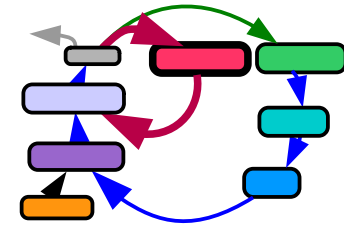
# EA alternative cycle of operation



EA:**Selection**

Common strategies for the **selection** are:

- random choice
- schedule based, e.g. round robin
- fitness based elitism:
  - fitness proportional choice
  - rank proportional choice
- fitness based stochastic:
  - fitness proportionate, probabilistic choice
  - rank proportionate, probabilistic choice
- combinations of the above

EA:**External Selection**

**Elitism** is a way to design the selection, and inheritance steps to shape the next generation following the principle of **Exploitation**.

Using elitism a subset of the population is surviving (excluding mutation), and will be part of the next generation.

Typically the  $\mu$  best individuals are chosen to survive.

The  $(\mu + \lambda)$  deterministic, rank dependent strategy, with taking the  $\mu$  best individuals as parents is a common implementation of elitism.

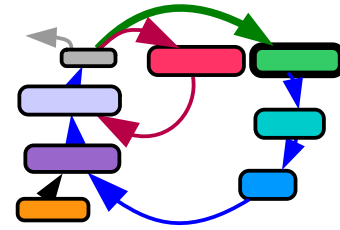
But the pool of parents, and the elite of  $\mu$  surviving individuals can be **different**.

# Overview

- Genome structure
- Example: 8 queens
- Super-individuals
- External-selection and parent-selection combined
- **Probabilistic parent-selection**
  - Wheel of fortune
  - Tournament selection
- Genetic programming
- Co-evolution

EA:

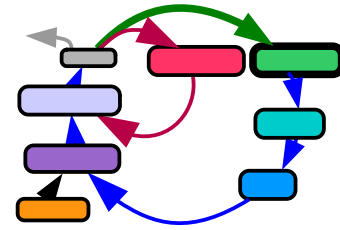
## Parent Selection



Within parent selection one has to try to obey the two principles of **Exploration** and **Exploitation** at the same time.

EA:

## Parent Selection

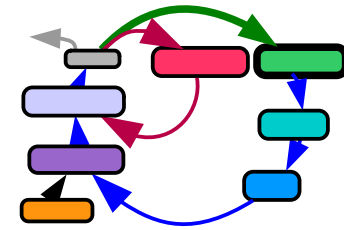


Within parent selection one has to try to obey the two principles of **Exploration** and **Exploitation** at the same time.

Of course, one is trying to use the acquired knowledge as good as possible, while maintaining the diversity within the population.

EA:

## Parent Selection



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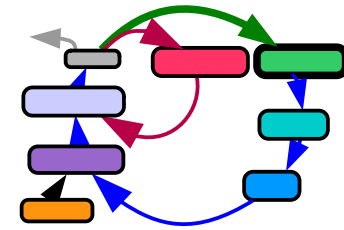
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Therefore it is a good idea to build up the pool of parents with a lot of the best individuals and explicitly take some individuals with a lower performance.



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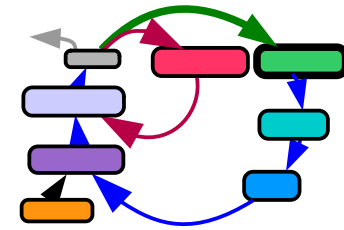
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A common way to implement this is to make the probability of being chosen for the pool of parents depending on the achieved fitness  **$f(g)$** :

EA:

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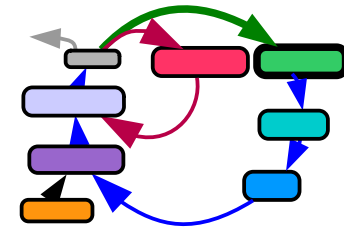
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**fitness proportional** or **rank proportional**

EA:

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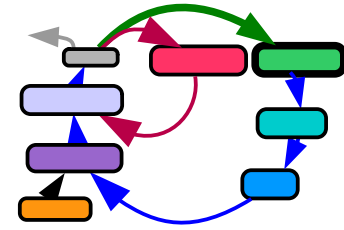
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EA:

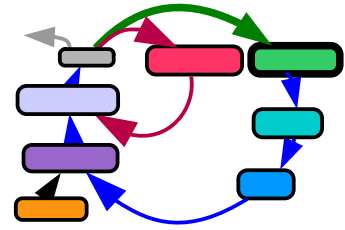
## Parent Selection



It showed to be feasible to make up the set of parents with those individuals, that have shown a good fitness  $f(g)$ , and explicitly include additional individuals that have not performed as good.

EA:

## Parent Selection

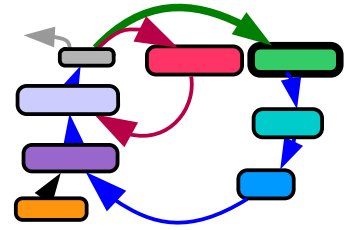


It showed to be feasible to make up the set of parents with those individuals, that have shown a good fitness  $f(g)$ , and explicitly include additional individuals that have not performed as good.

A **probabilistic parent selection**, depending on the reached fitness values  $f(g)$  is a common way to implement this.

EA:

## Parent Selection



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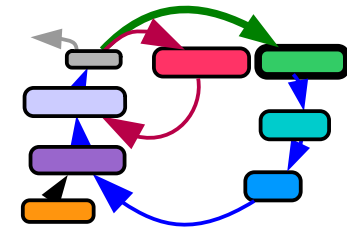
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Common probabilistic, fitness based parent selection:

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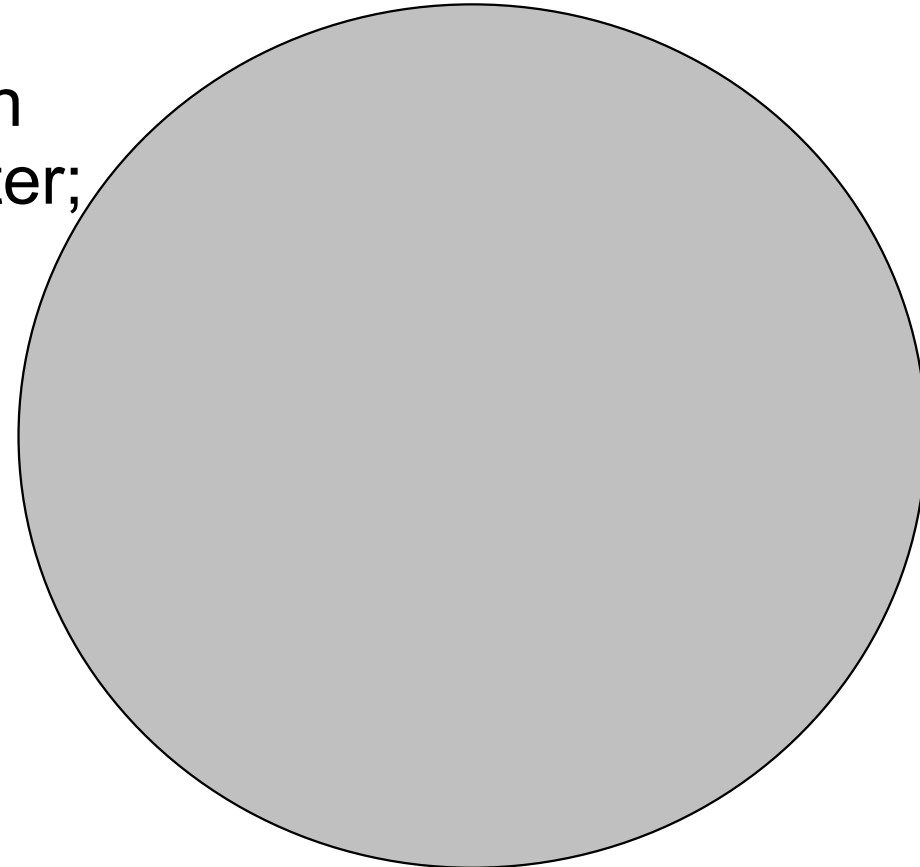
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EA:**Parent Selection**

A widely used way to implement a probabilistic, rank proportionate parent selection is the **wheel of fortune**,

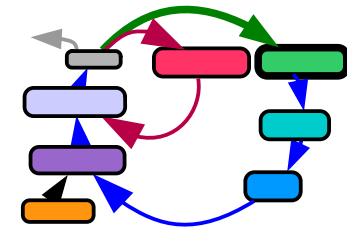
Where the probability  $\omega$  to be chosen is larger, when the fitness  $f(g)$  is better; is larger, when the rank  $r(f(g))$  of the individual is smaller.





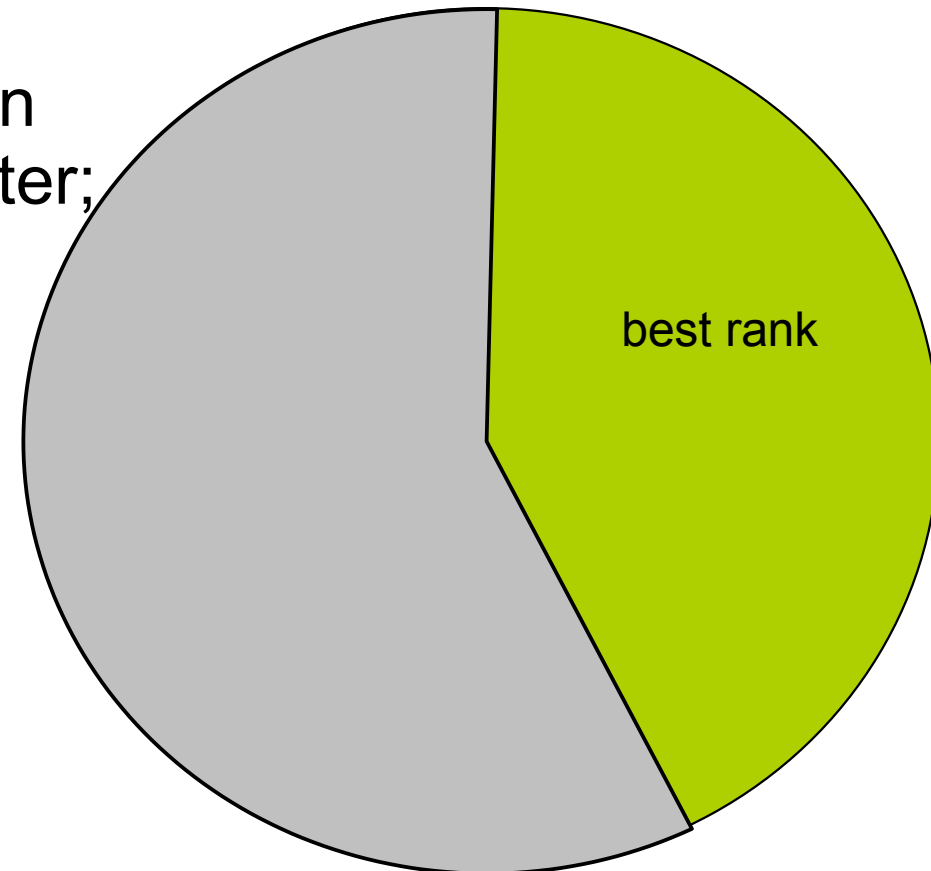
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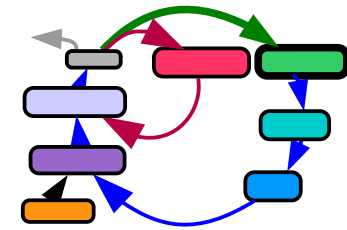
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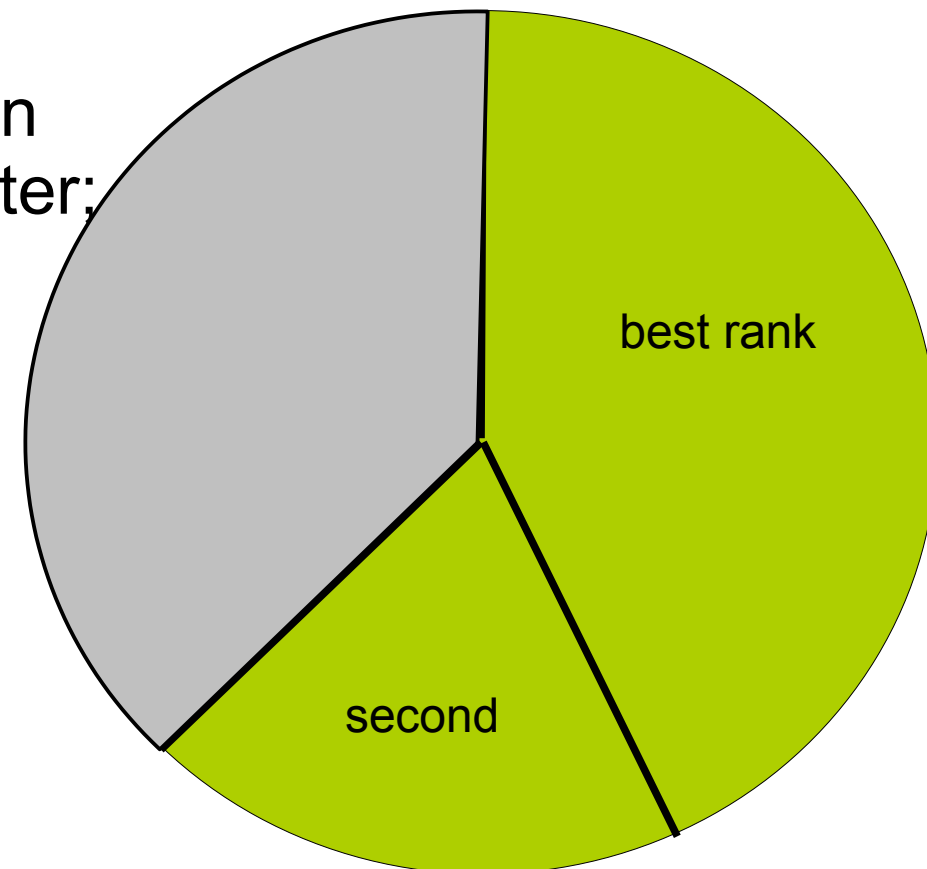
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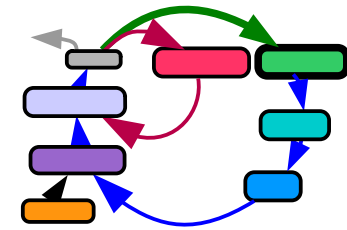
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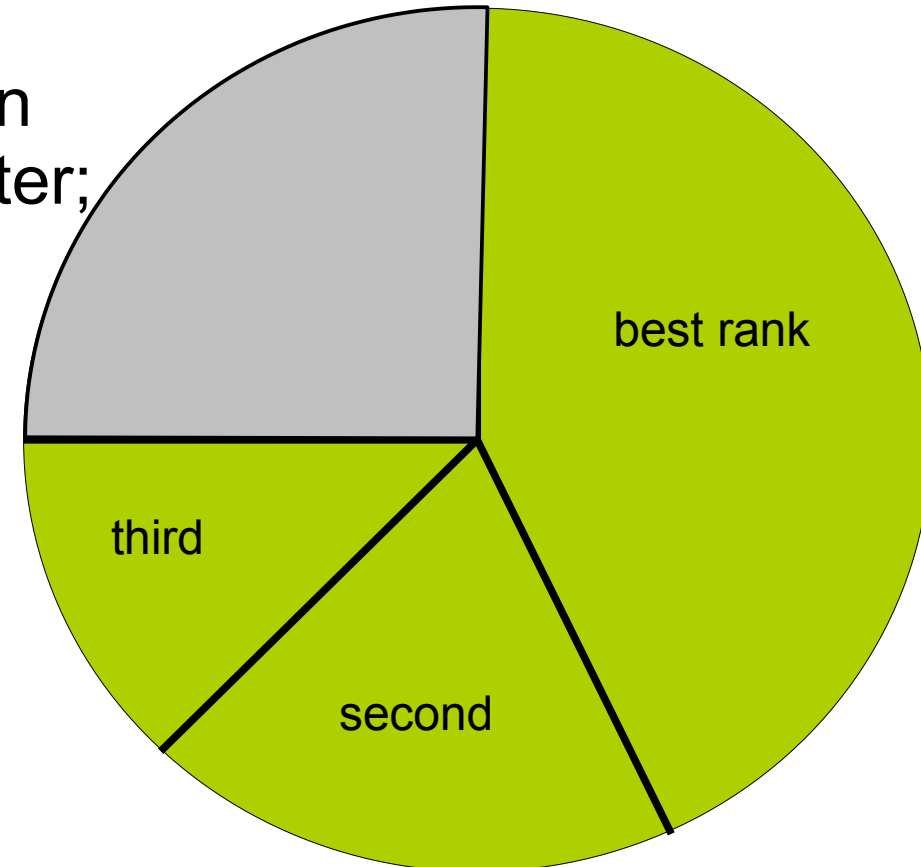
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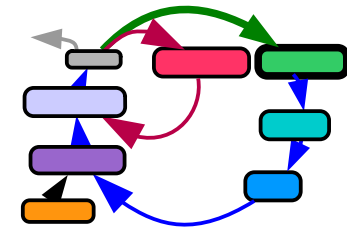
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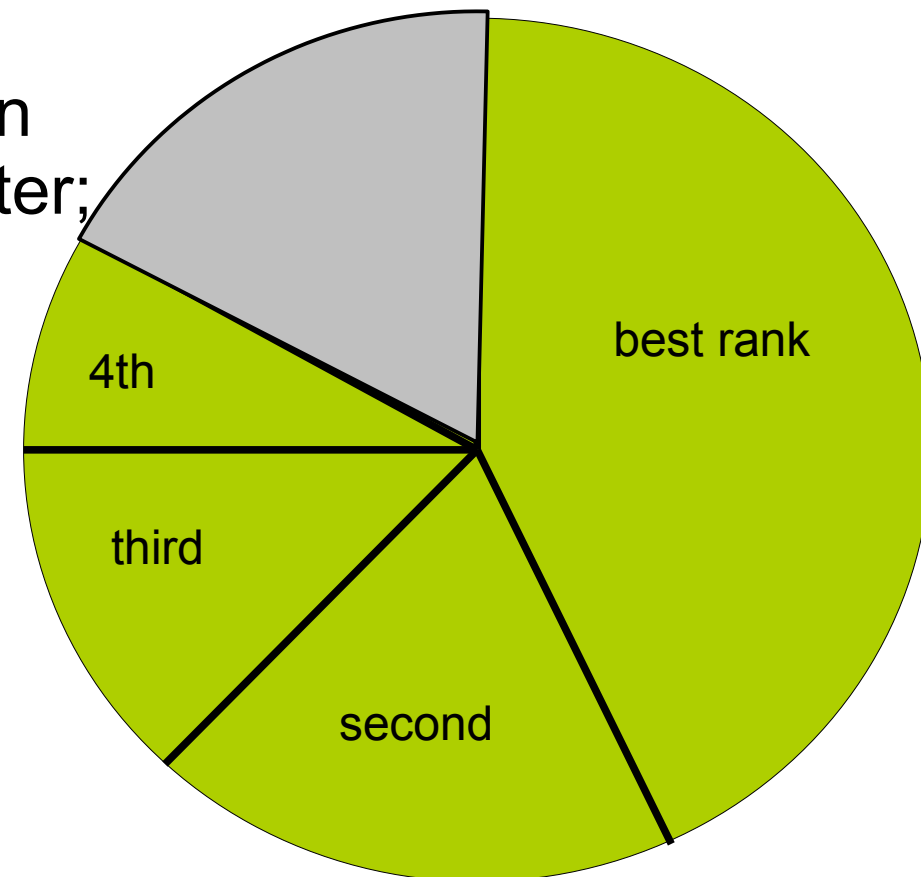
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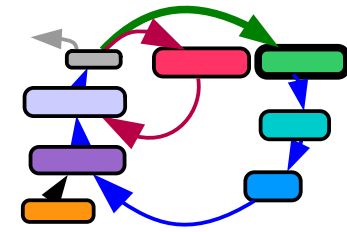
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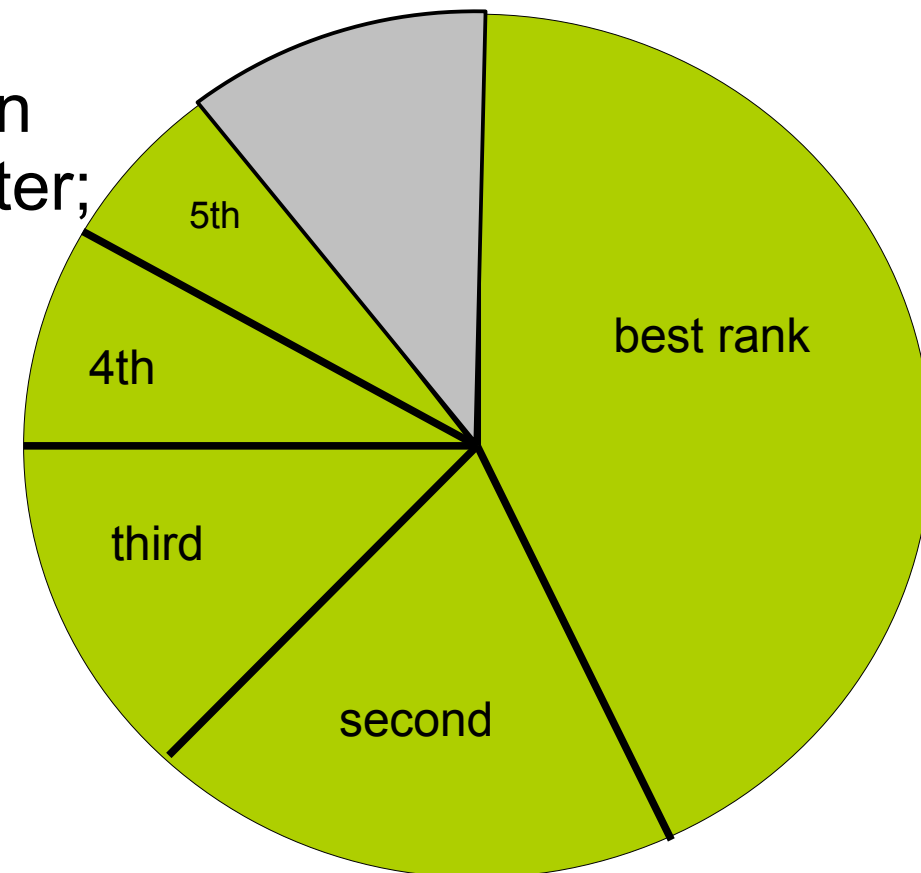
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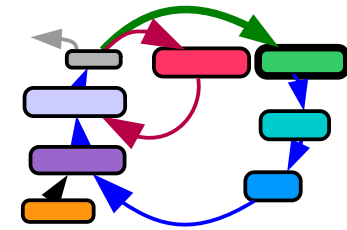
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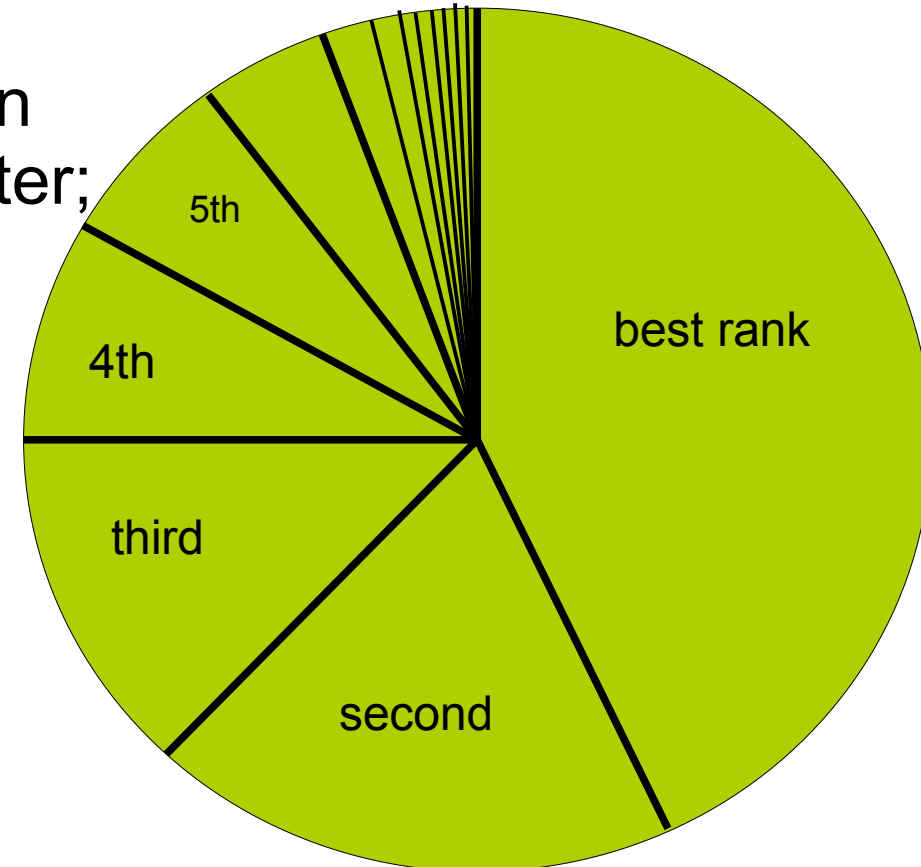
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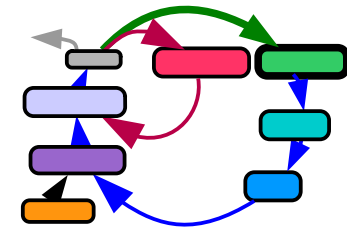
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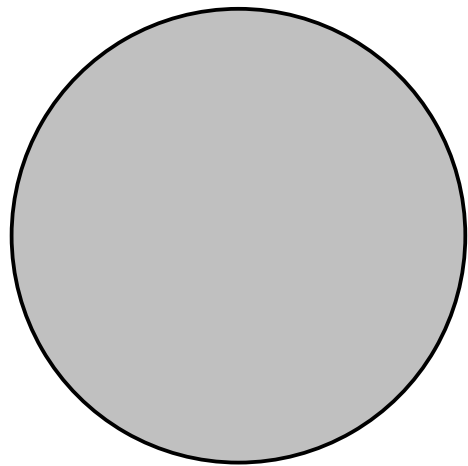
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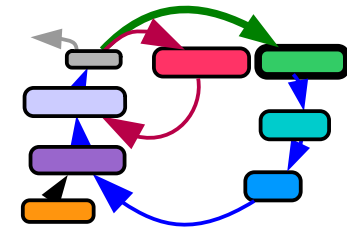
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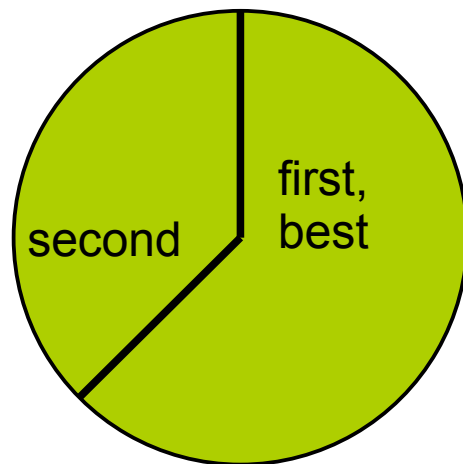
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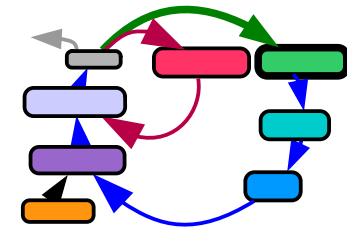


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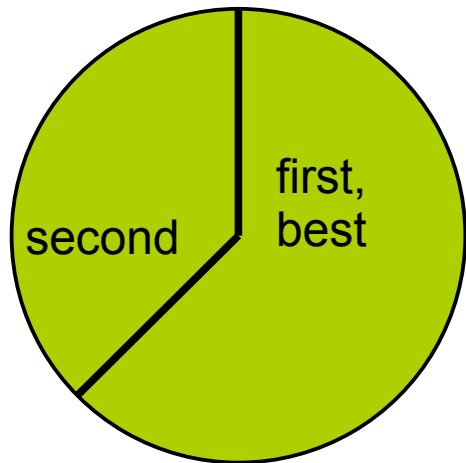
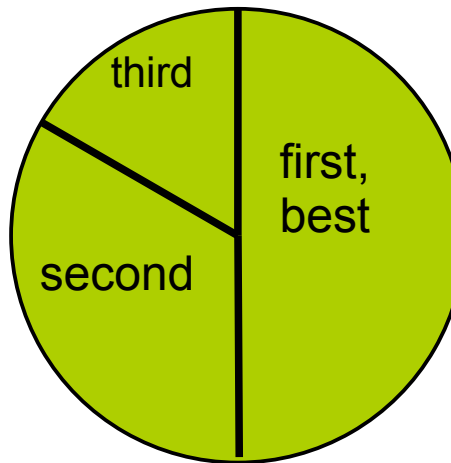
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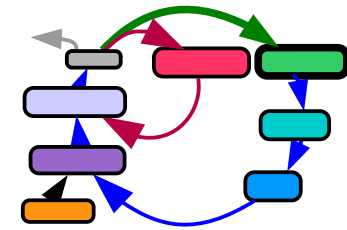
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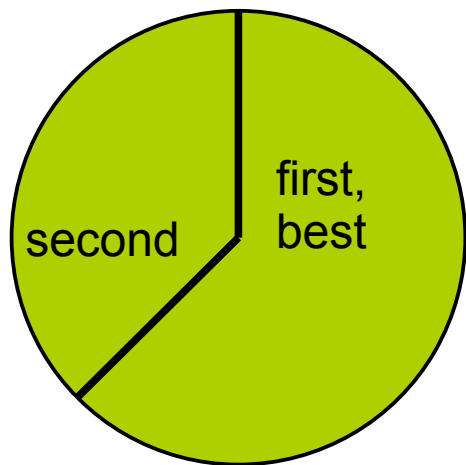
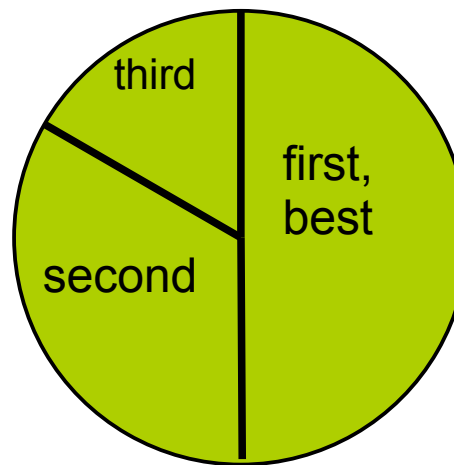
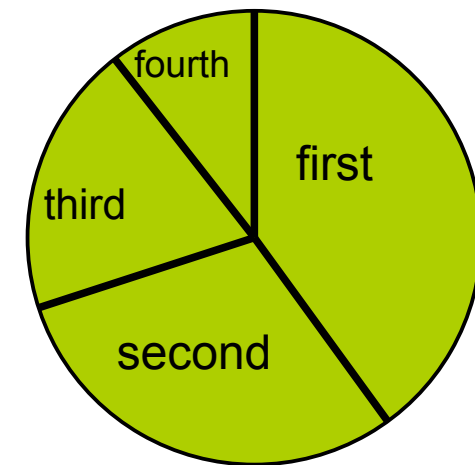
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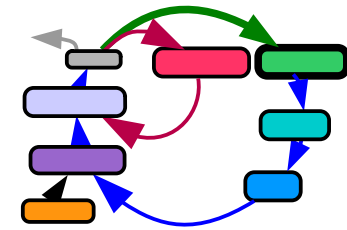
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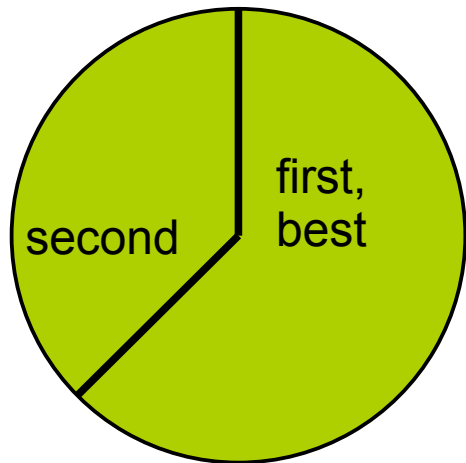
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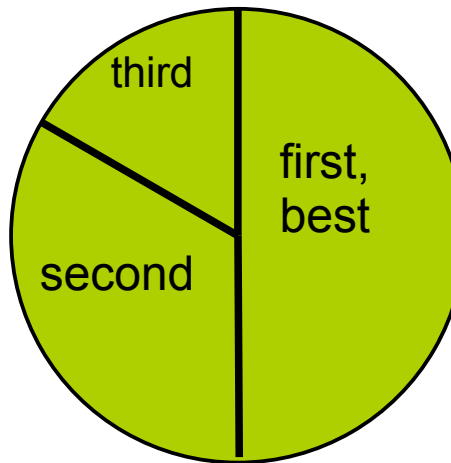
**P=2:****P=3:****P=4:**

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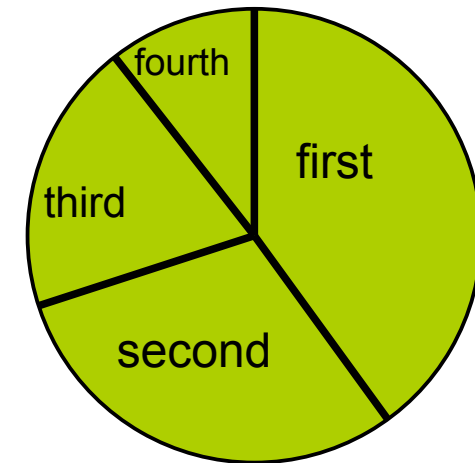
The chance, or the probability  $\omega$  to be chosen is larger with smaller fitness dependent rank  $r(f(g))$  of the individual.

**P=2:**

$$2/3 + 1/3 = 1.0$$

**P=3:**

$$3/6 + 2/6 + 1/6 = 1.0$$

**P=4:**

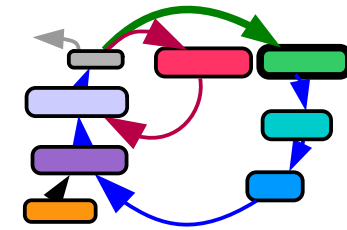
$$4/10 + 3/10 + 2/10 + 1/10 = 1.0$$

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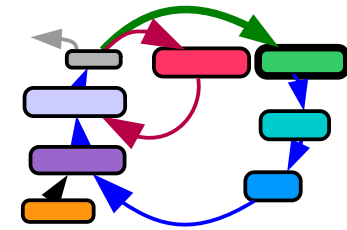
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Common probabilistic, fitness based parent selection:

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EA:

## Parent Selection



Another common way to implement the parent selection, is using the **softmax function** for probabilistic selection.

The parents are taken randomly from the population.

The probability  $\omega_p$  to be taken is determined by the fitness  $f(p)$  of the individual  $p$ .

$$\omega_p = \frac{e^{f(p)/\tau}}{\sum_{q=1}^P e^{f(q)/\tau}}$$

The positive parameter  $\tau$  is called a temperature. Large value of  $\tau$  generates a (nearly) equiprobable distribution.

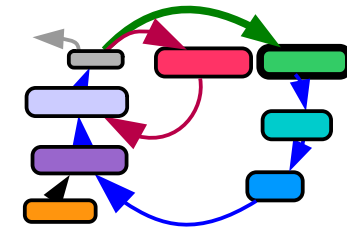
Easy to implement, easy to control the selection pressure.

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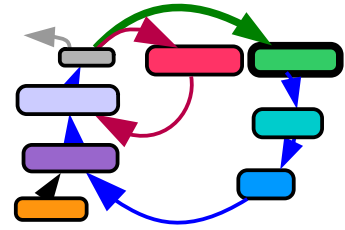
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Some individuals are taken randomly from the population, and compared pairwise (randomly chosen) in a form of **tournament**, the winner of each tournament is now eligible for the pool of parents.

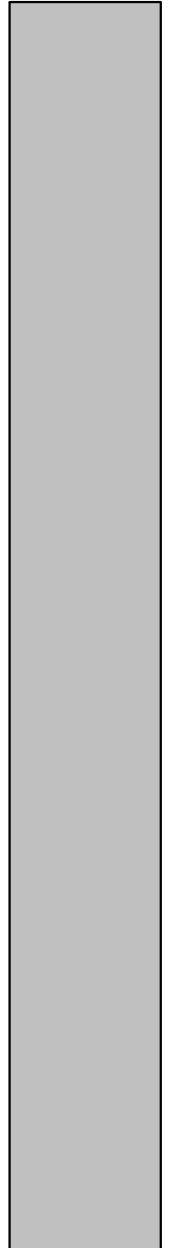
To further increase the fitness of the pool of parents, the winning individuals can now undergo further stages of tournaments among each other.

Easy to implement, easy to control the selection pressure.

**EA:**

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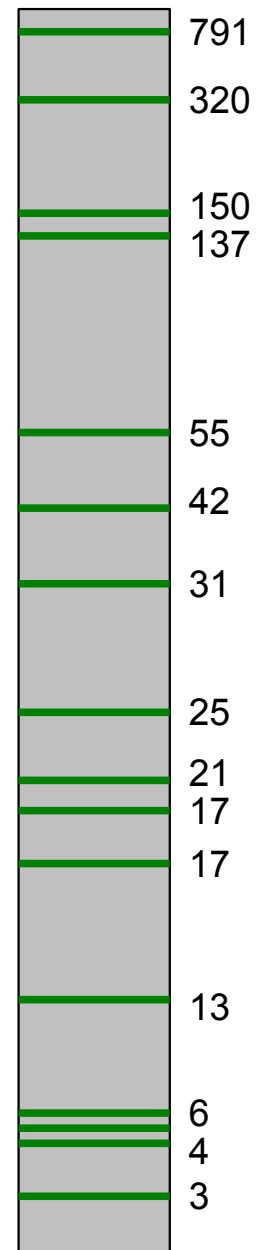
**Tournament selection**



EA:

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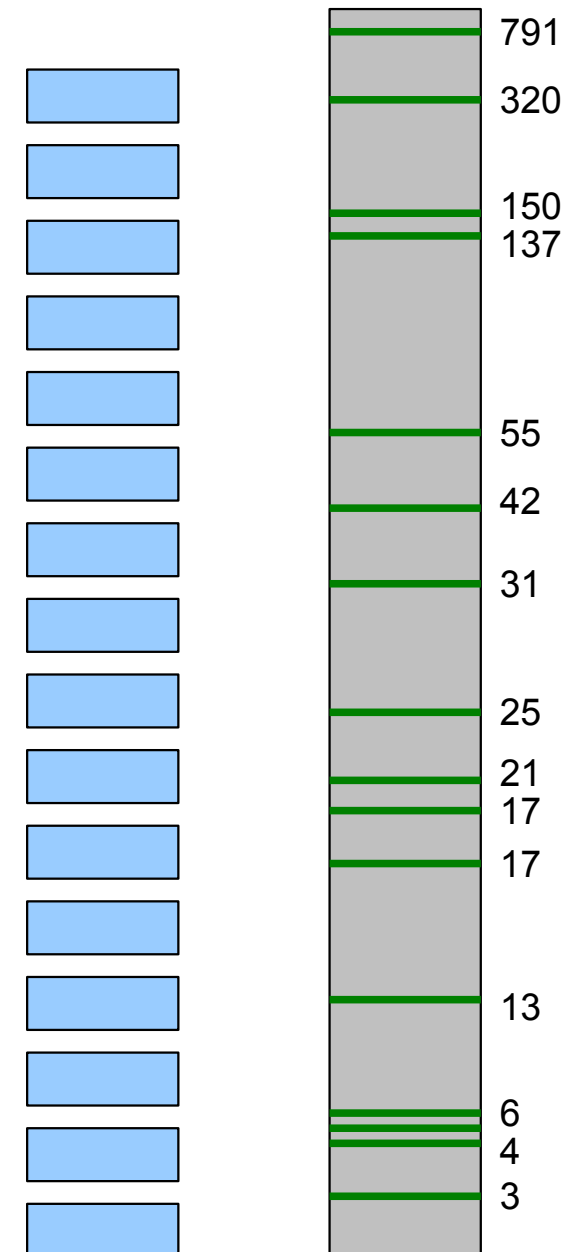
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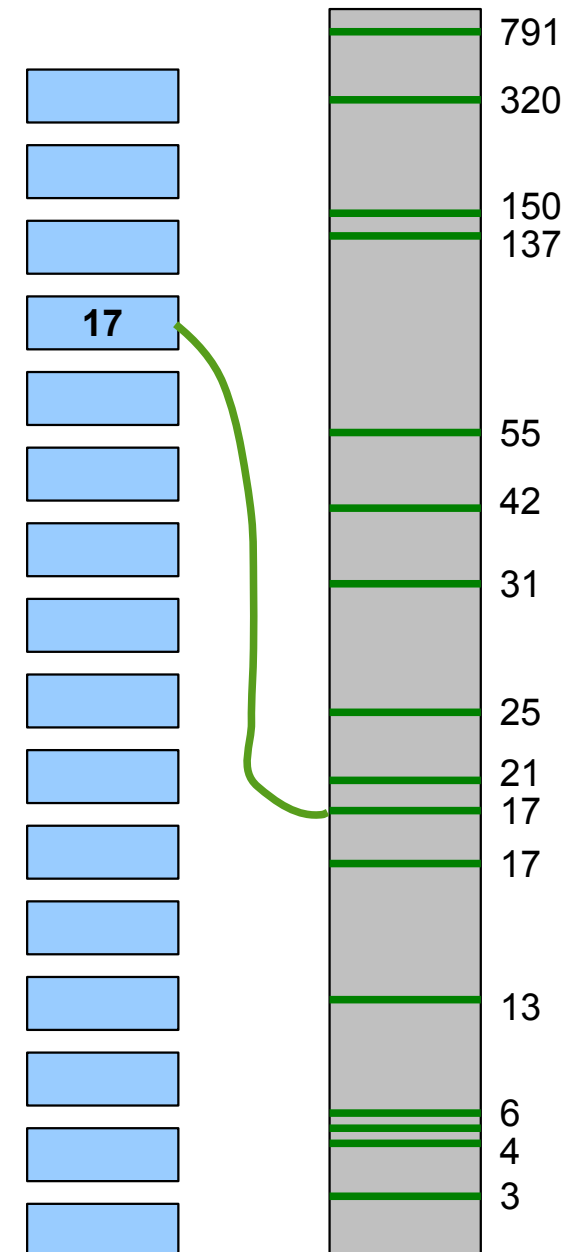
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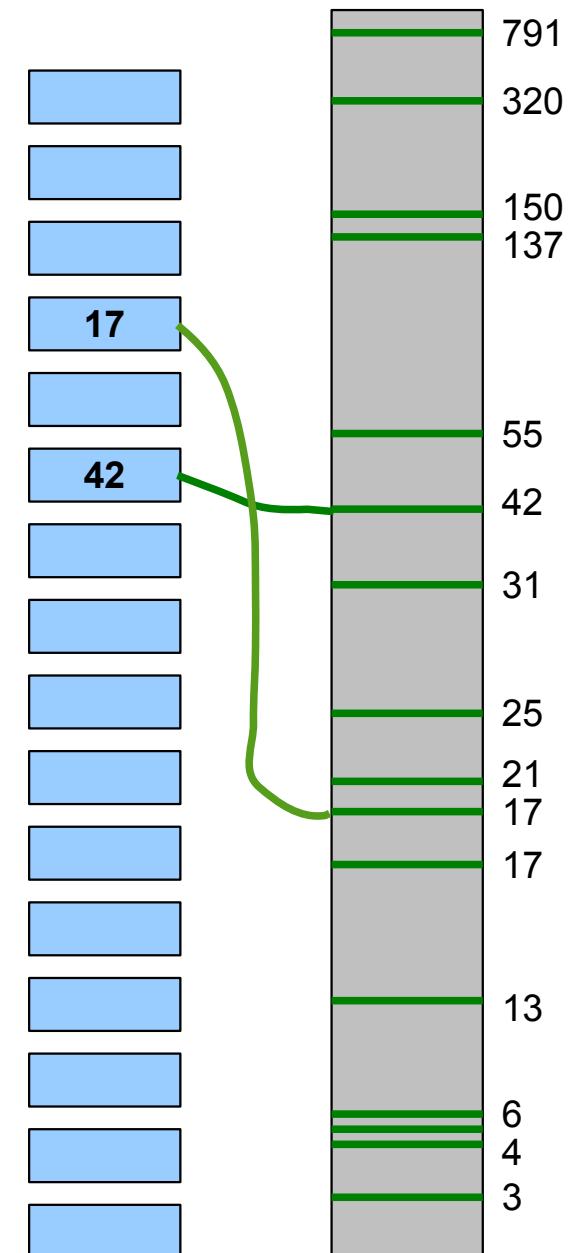
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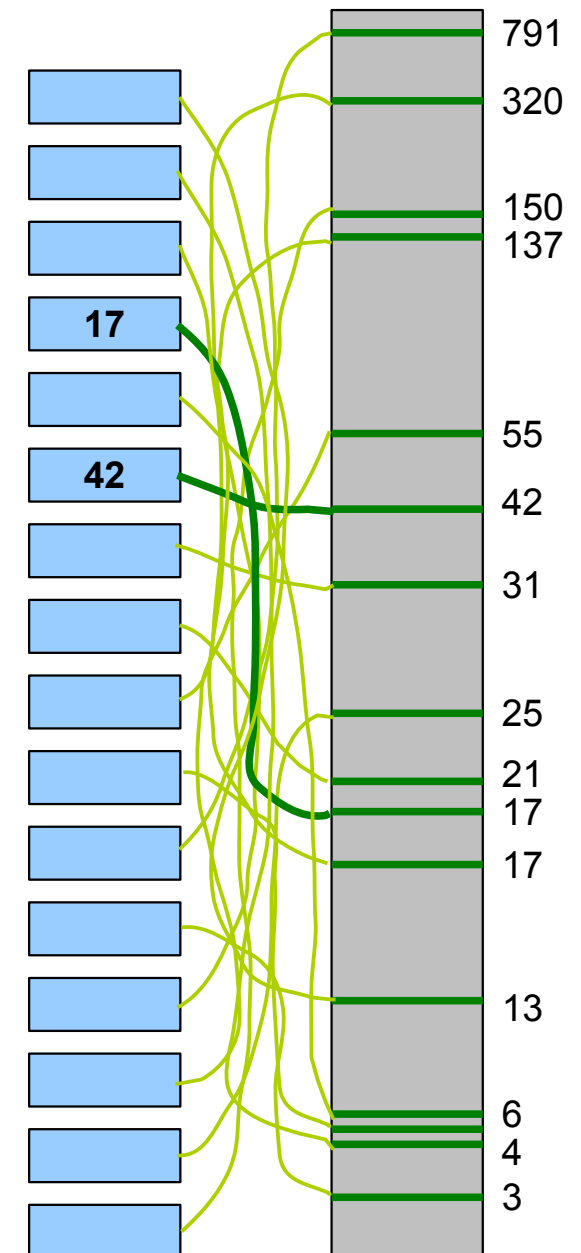
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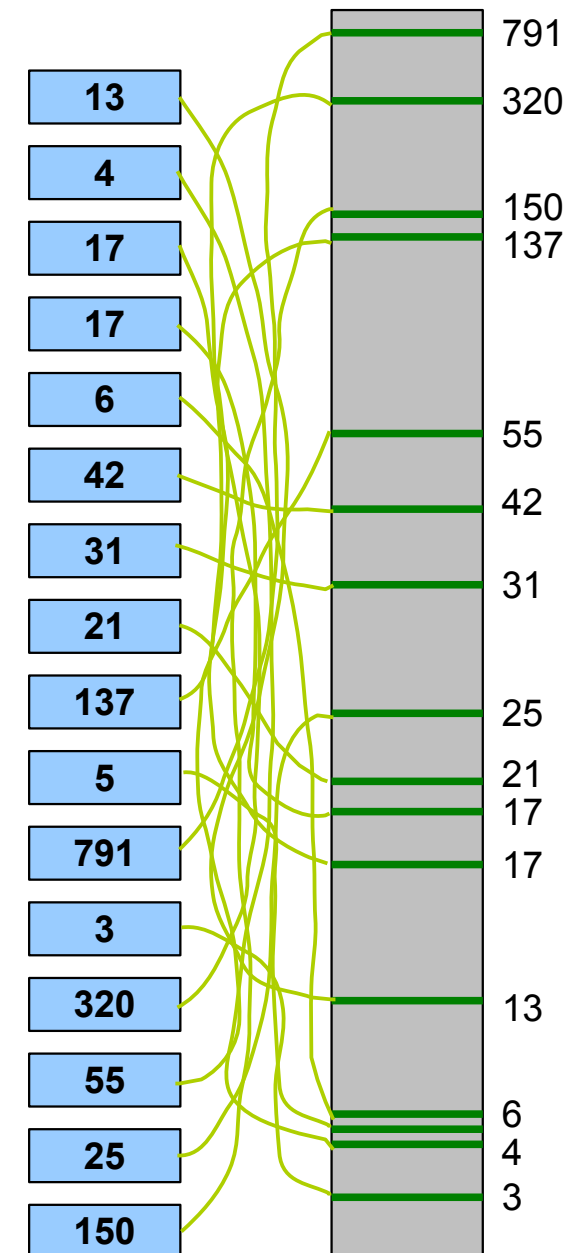
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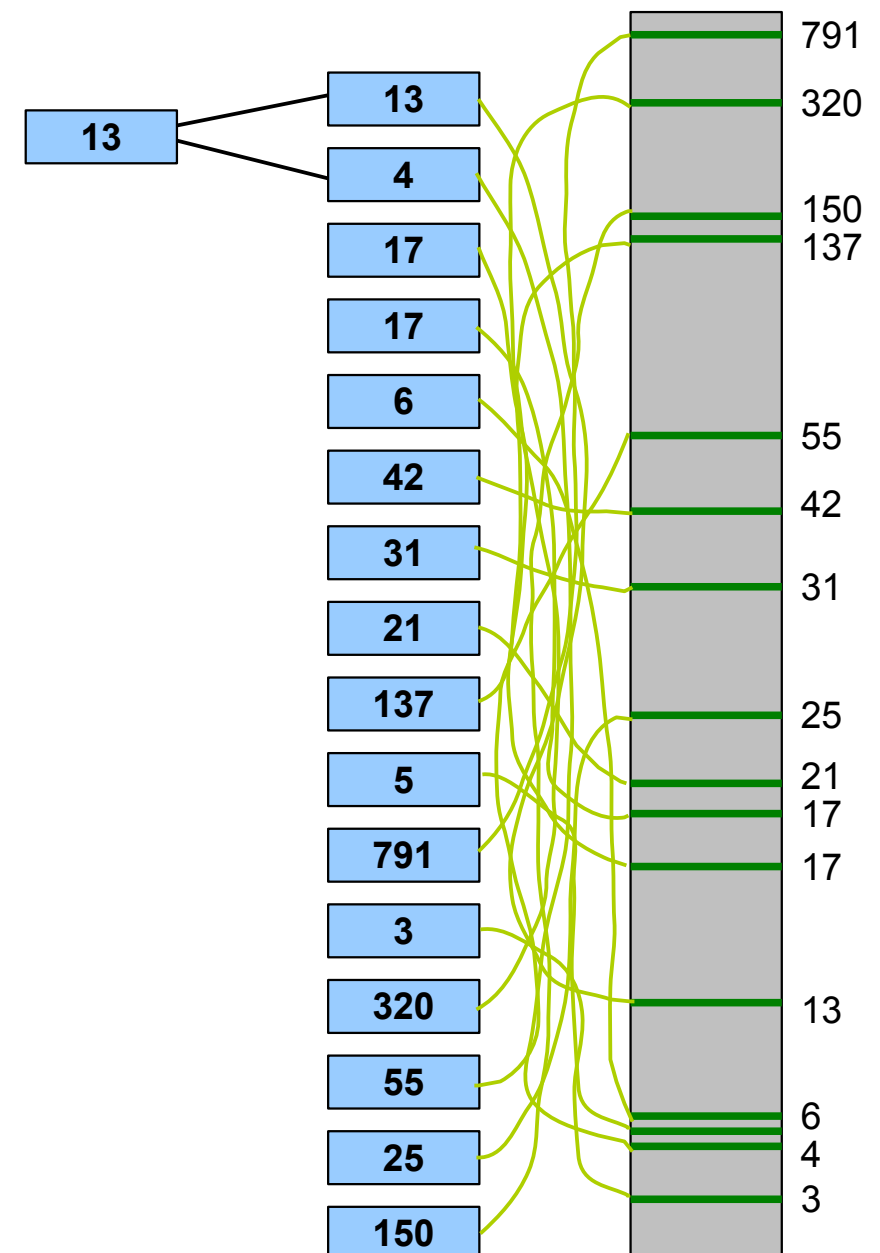




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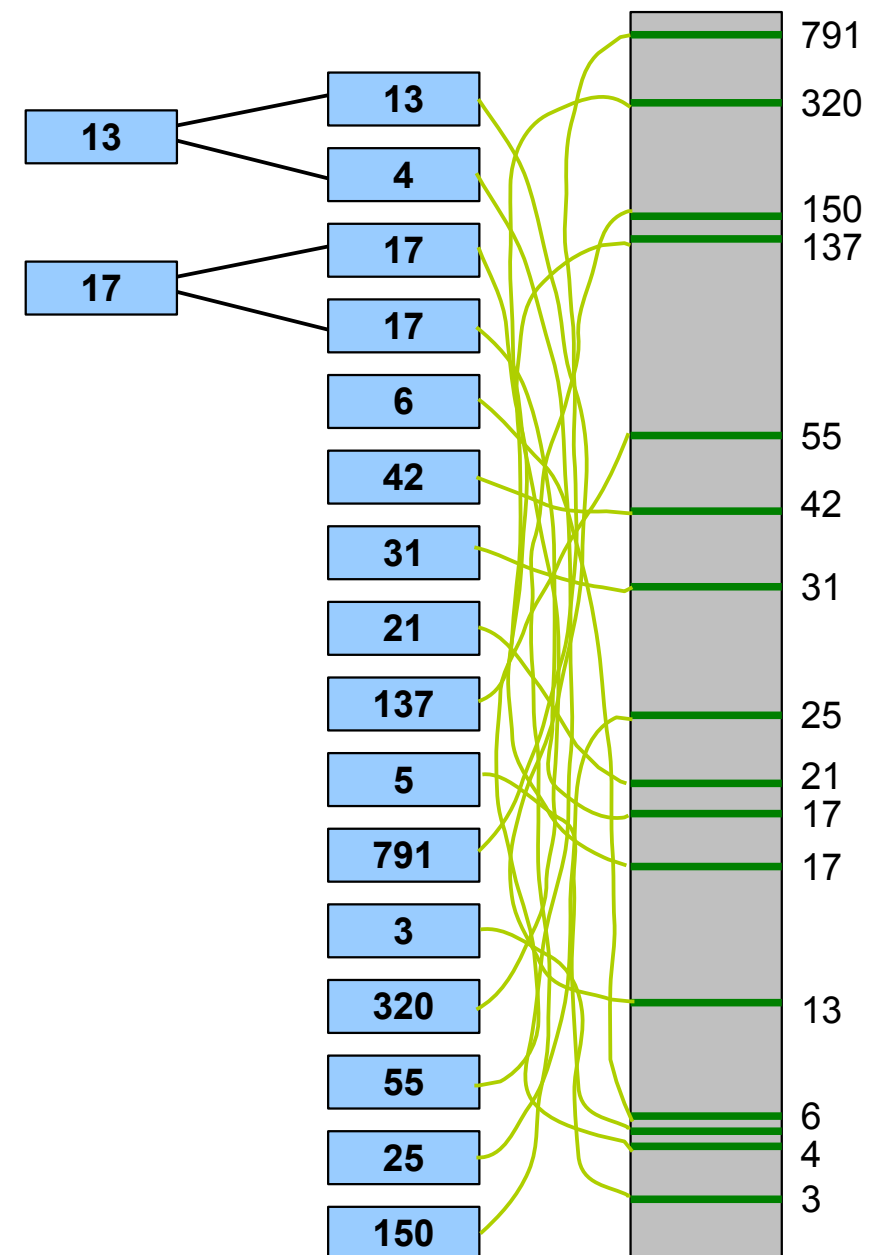
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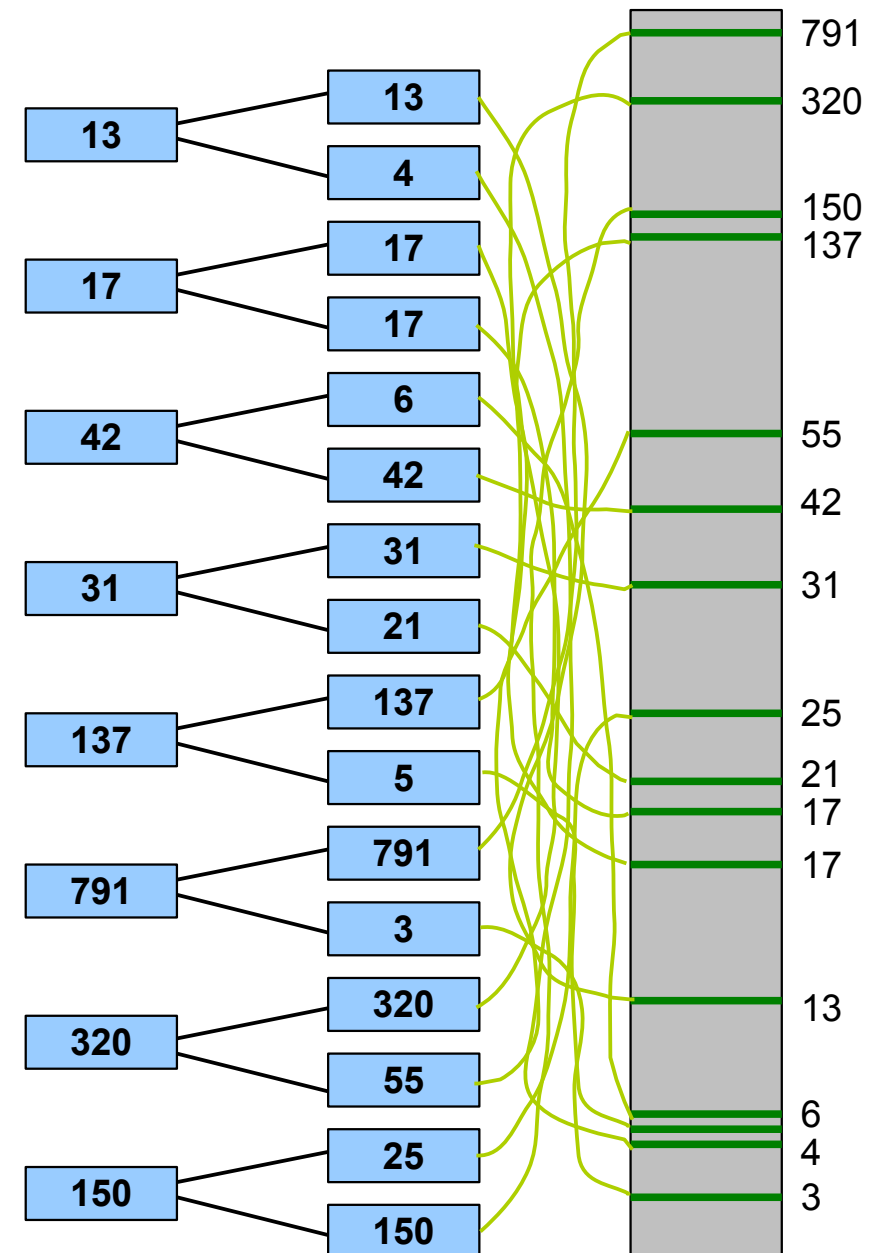
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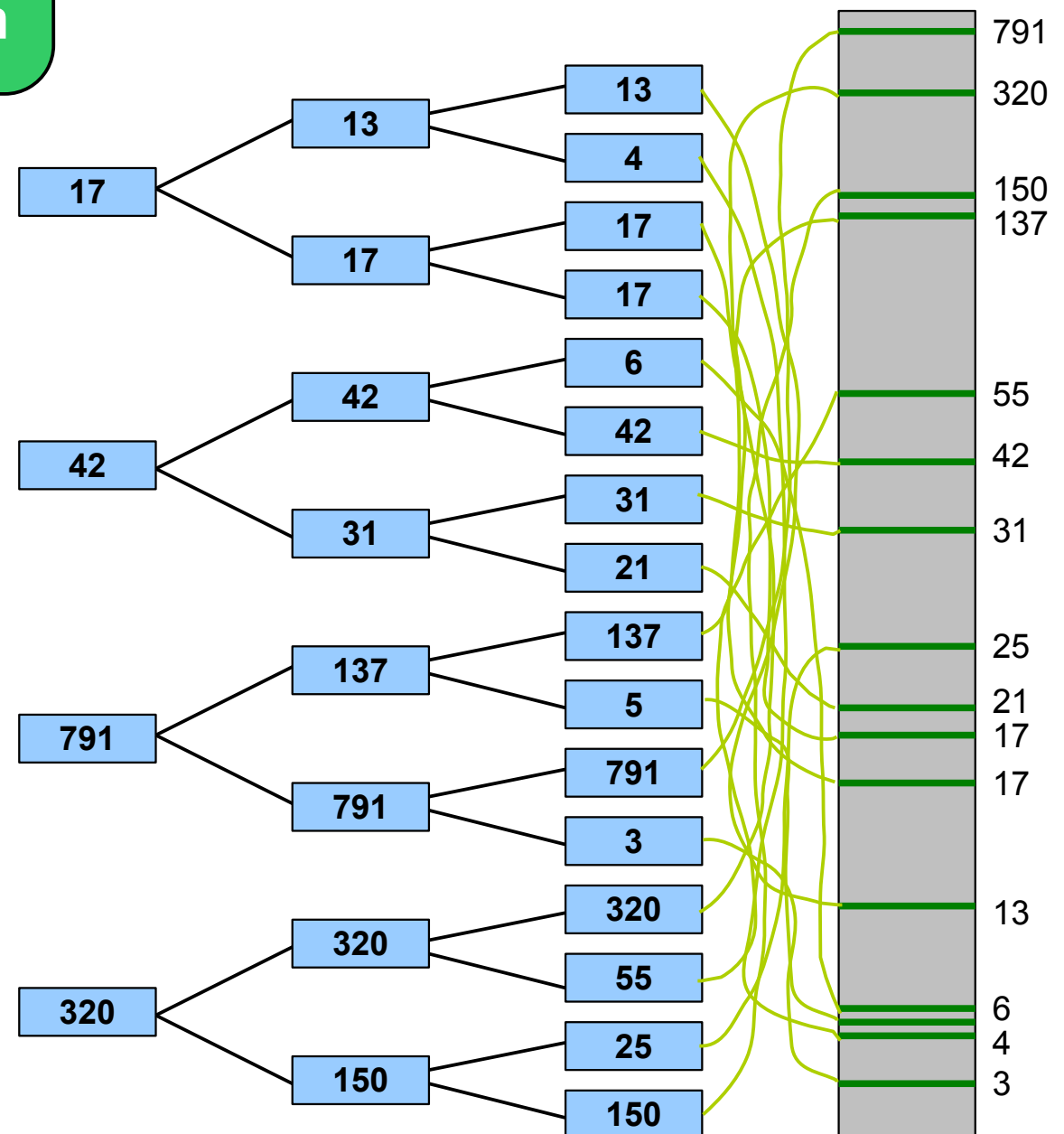
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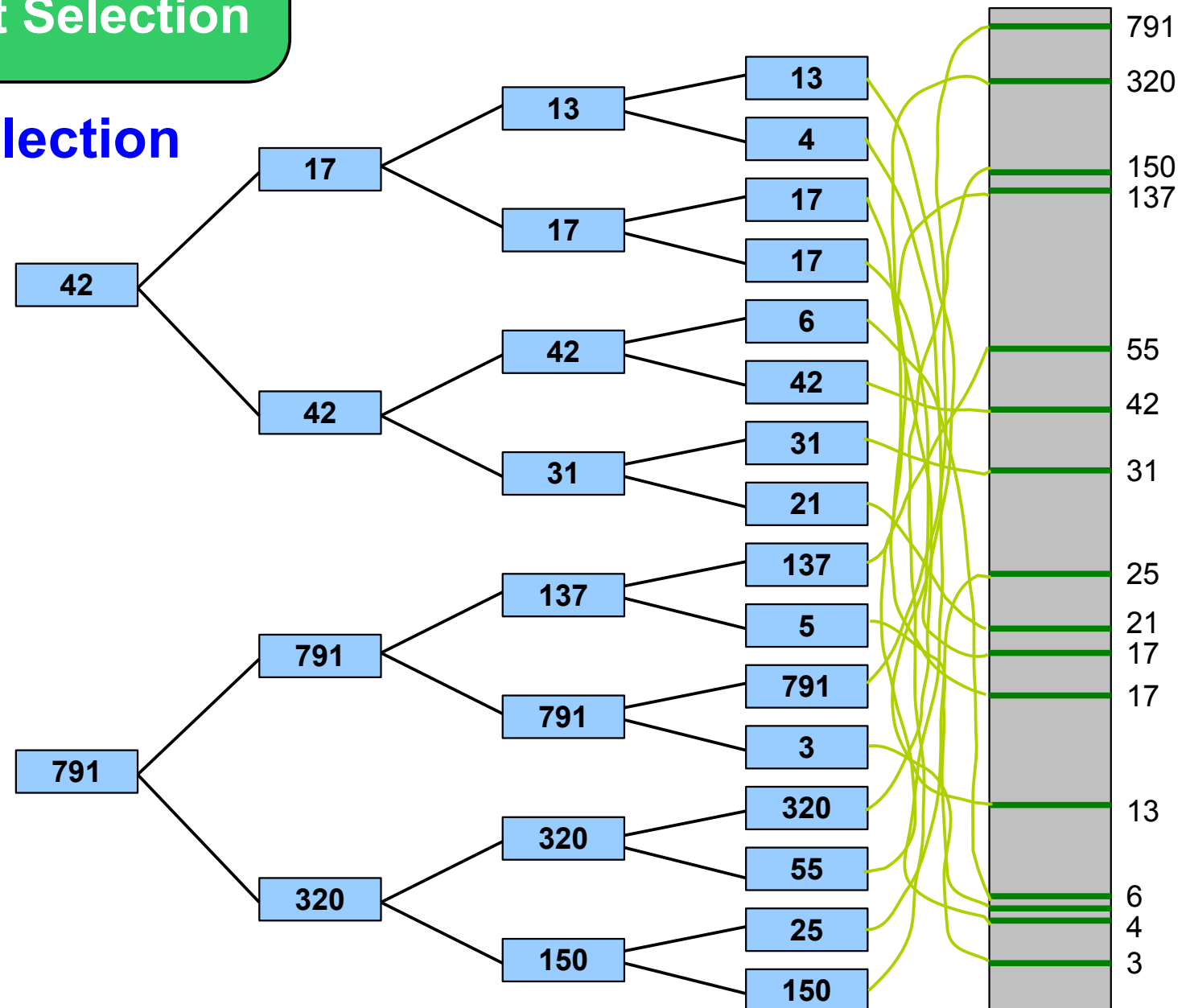
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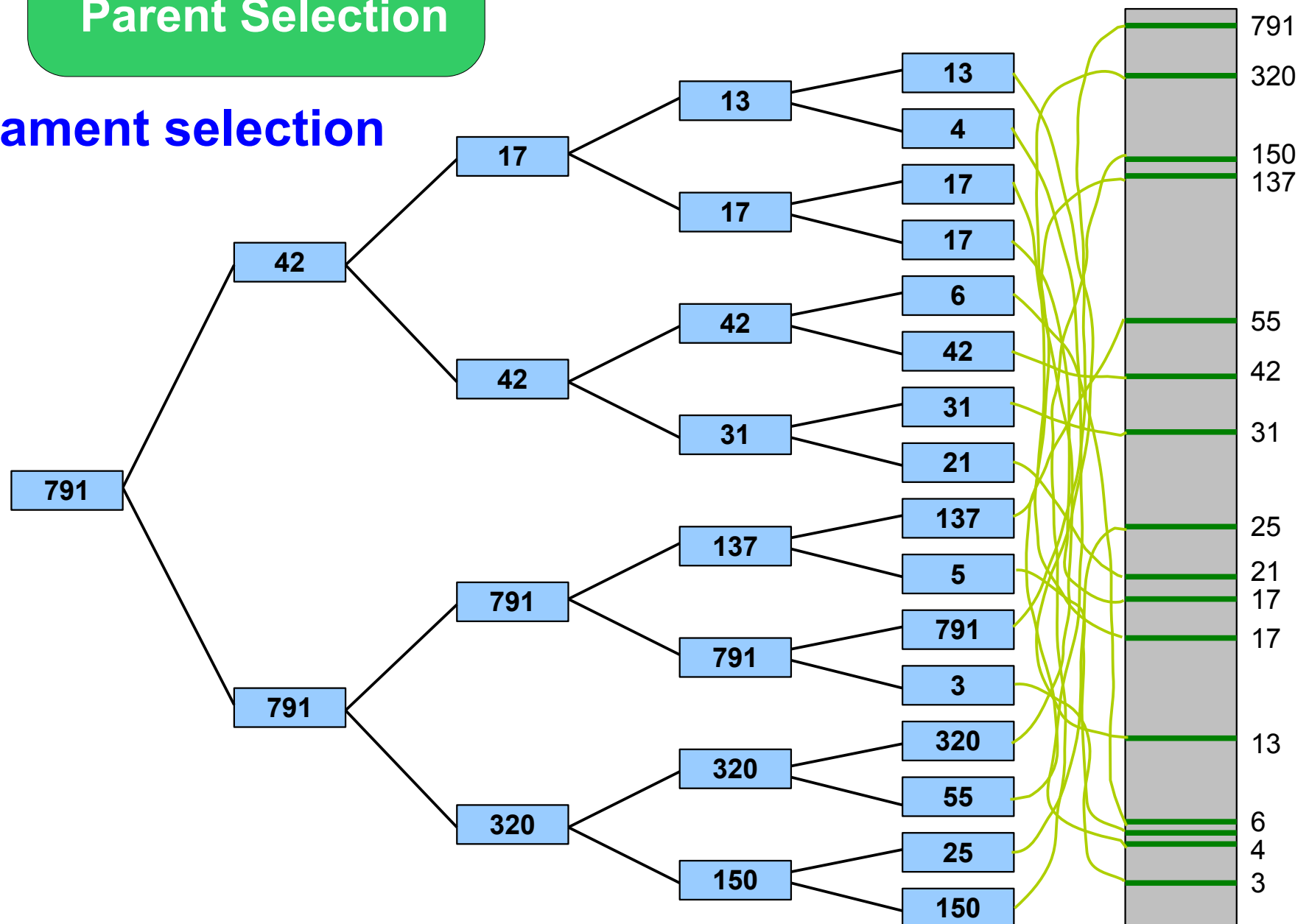
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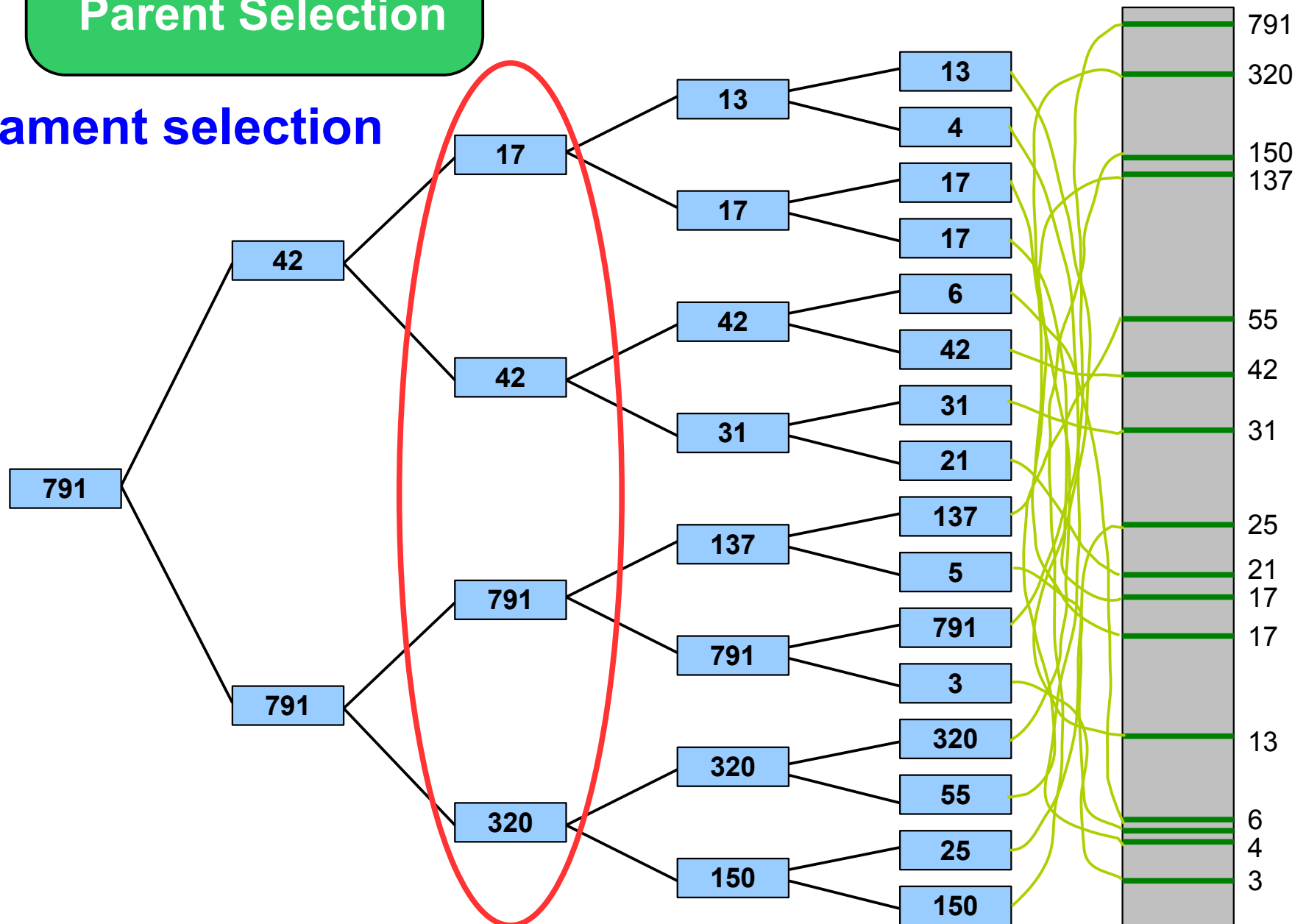
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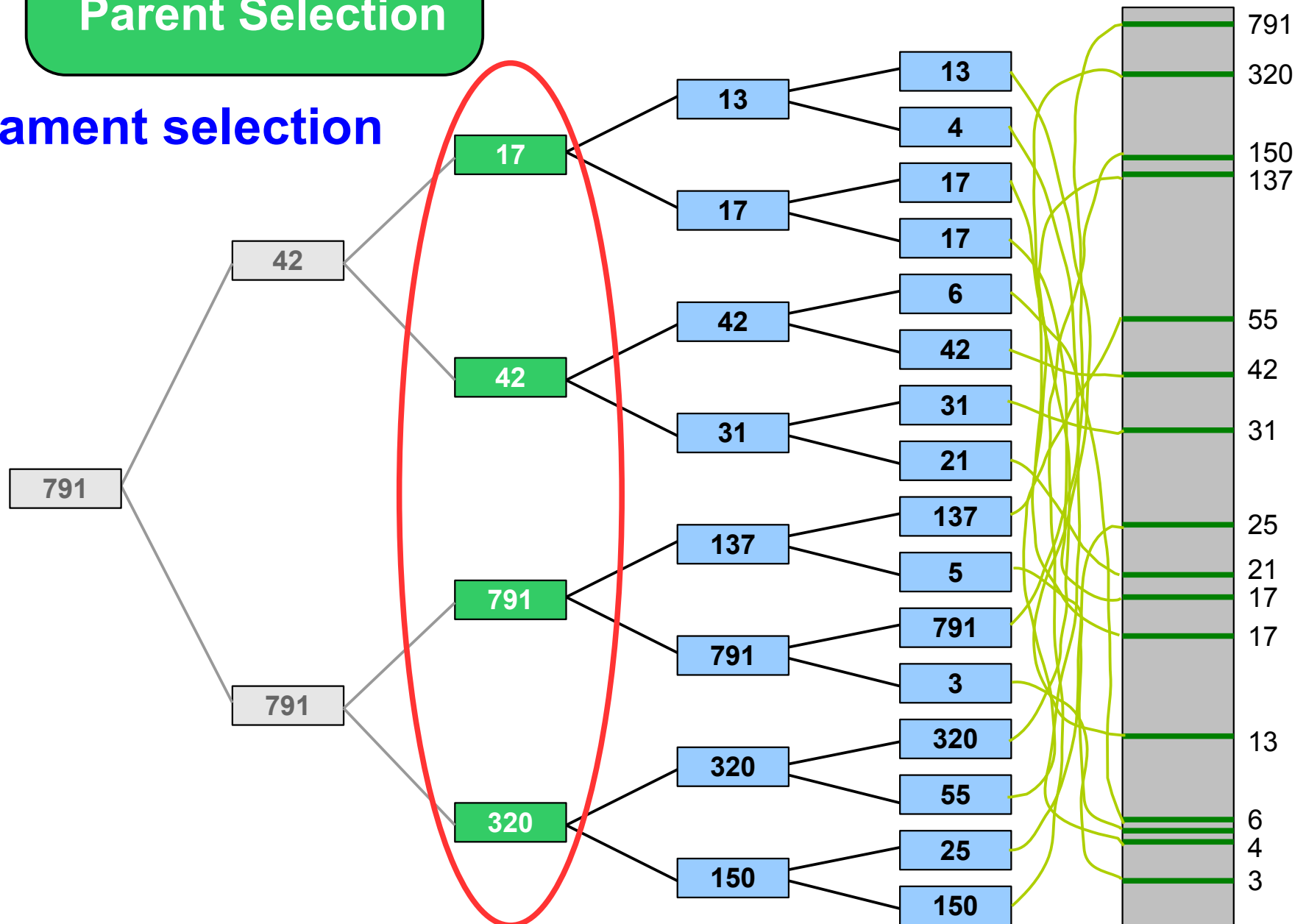
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# Parent Selection





EA:

## Parent Selection

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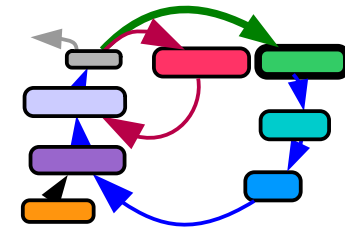
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# Historic Remarks, Different Approaches

## Evolutionary Computation (EC)

Swarm Behavior / Swarm Intelligence

- Ant Algorithm
- Ant Colony Optimization
- Particle Swarm Optimization

Evolutionary Algorithms (EA)

- Genetic Algorithms (GA)
- **Genetic Programming (GP)**
- Evolutionary Strategies (ES)
- **Evolutionary Programming (EP)**

# Historic Remarks, Different Approaches

## Evolutionary Computation (EC)

### Evolutionary Algorithms (EA)

- Genetic Algorithms (GA)  
John Henry Holland (1975)
- Evolutionary Strategies (ES)  
Ingo Rechenberg (1965), Hans-Paul Schwefel (1970)
- **Evolutionary Programming (EP)**  
Lawrence J. Fogel (1964)
- **Genetic Programming (GP)**  
N.A.Barricelli (1954), R.M.Friedberg (1958)

**EA:**

## Genetic & Evolutionary Programming

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Although proposed as an alternative approach to “normal computer programming”, the subject of **Genetic or Evolutionary Programming** refers to EA applications where the genome is regarded as a sequence of commands (a program).

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### Genetic & Evolutionary Programming

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The fitness  $f(g)$  of the genome  $g$  is the quality the program achieves within the given application.



## EA:

### Genetic & Evolutionary Programming

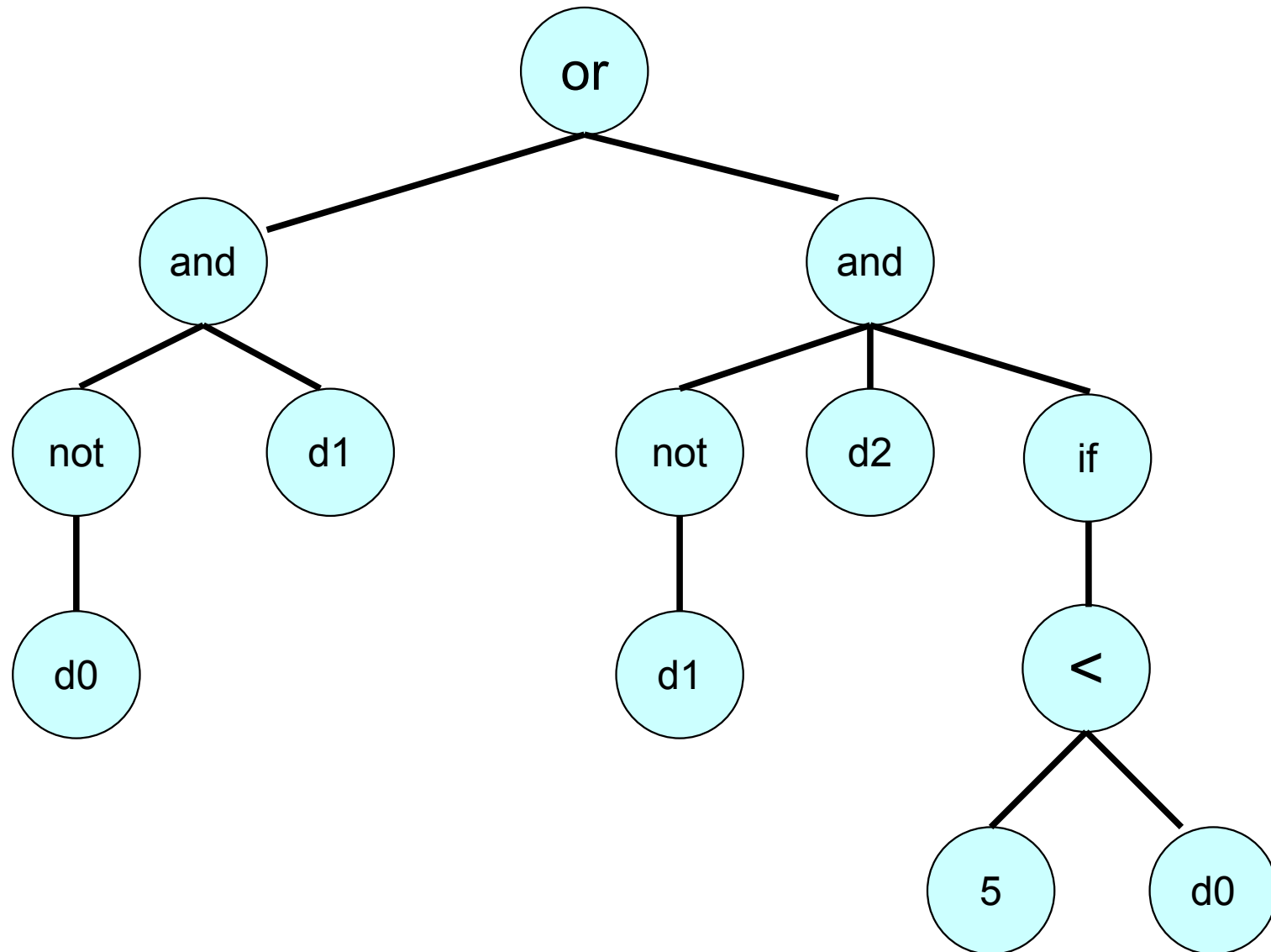
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The fitness  $f(g)$  of the genome  $g$  is the quality the program achieves within the given application.

The basis for **genetic programming** is typically not the source code level, but a genome that is representing a formal description of the code (syntax graph, prefix notation of functions, ...).

EA:

## Genetic & Evolutionary Programming



not **d0** AND **d1** OR not **d1** AND **d2** AND if(**5**<**d0**)

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The population is not evaluated against a static fitness function, but against a changing other population.

The performance of one population is the fitness for the others population.



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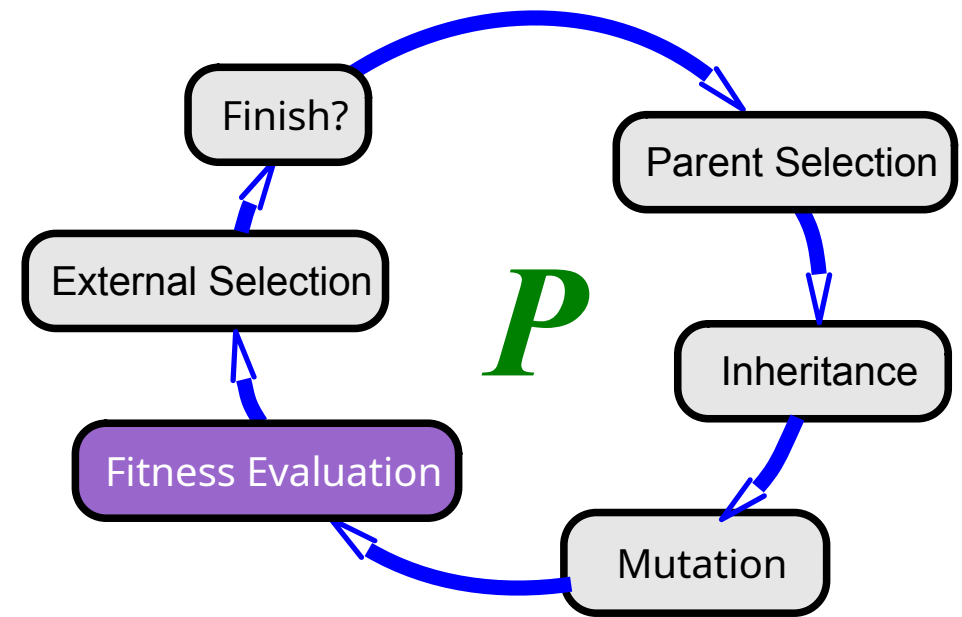
*Q**P*

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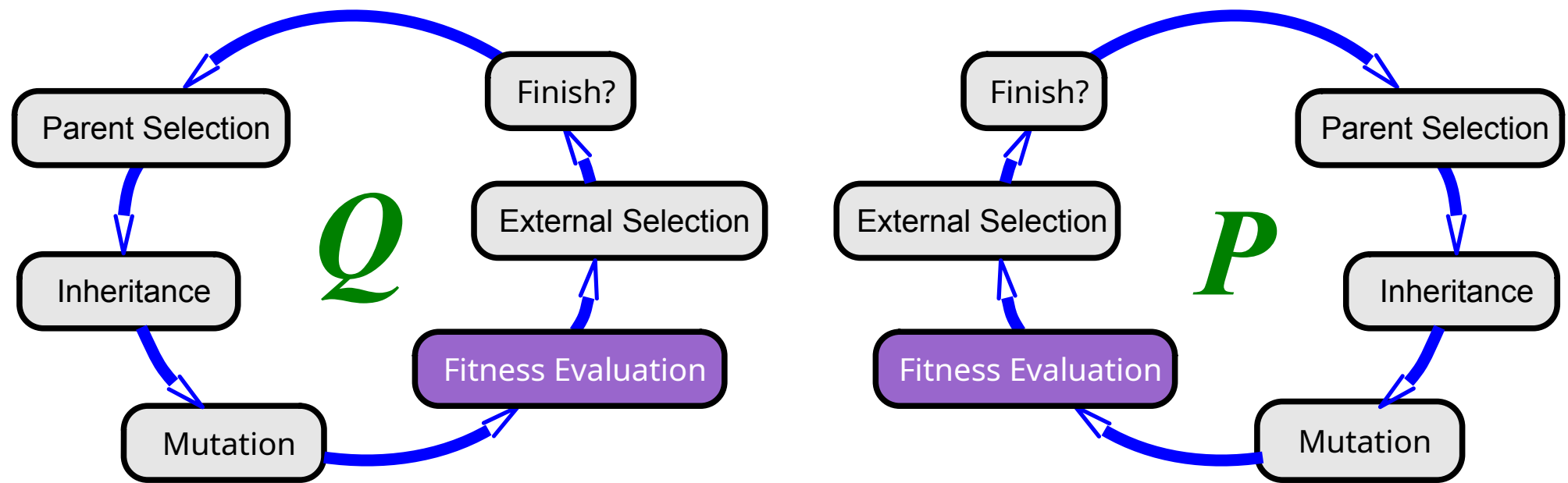
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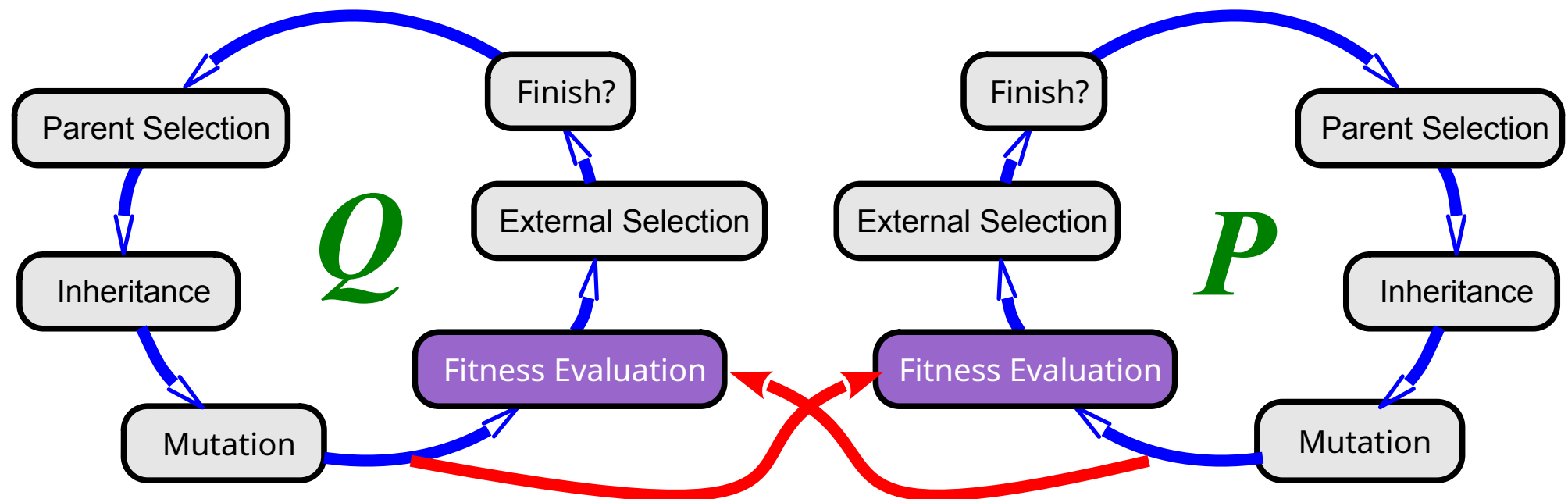


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**EA:****Co Evolution**

Co evolution can be used to simulate the development of two species interacting:

e.g. a predator-prey system  
or two agents, or two players in games, ...

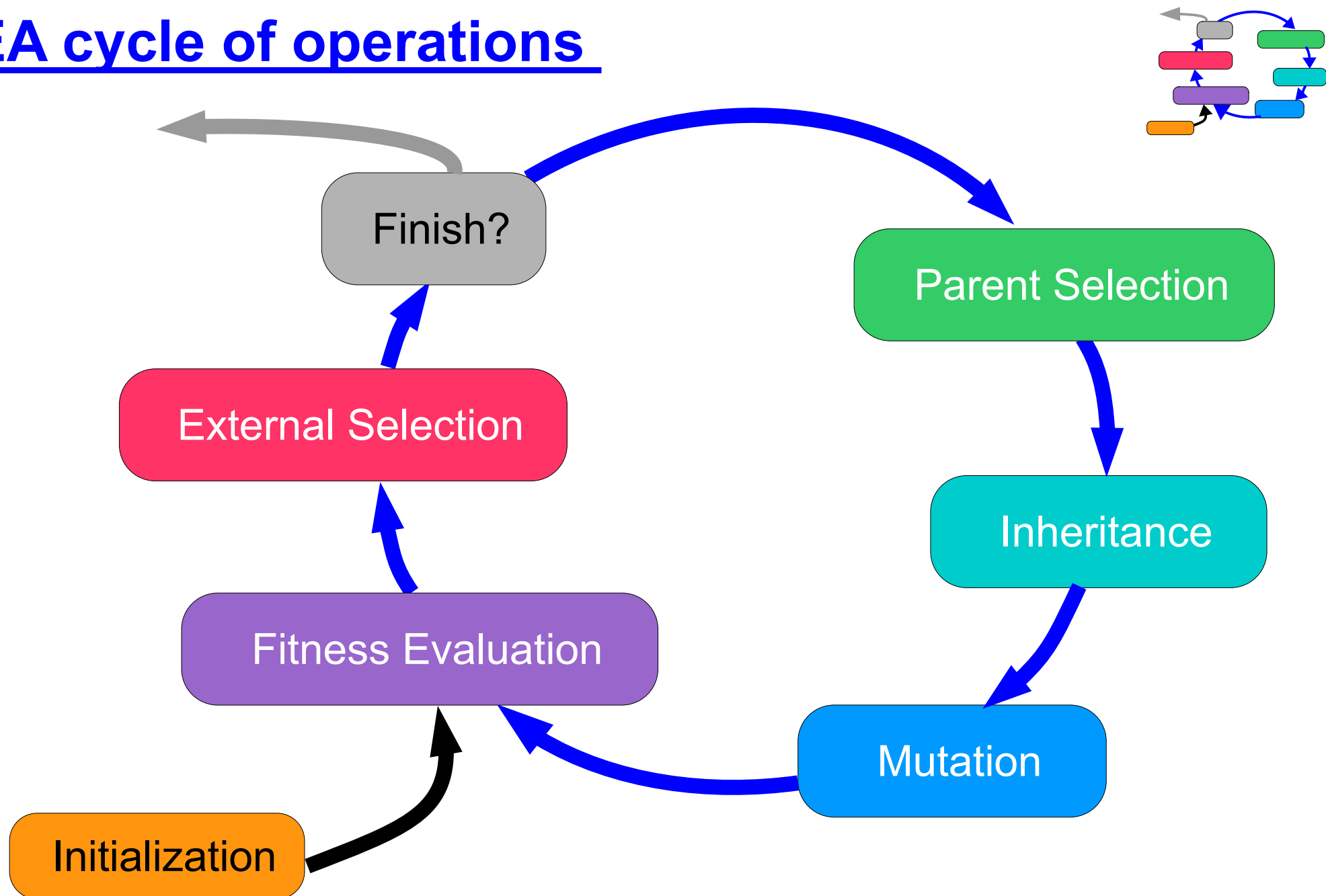
Since both fitness functions, are not static but changing over time, a final objective is sometimes hard to determine.

The achieved results in co evolution for one population is only use-able in interaction with the other population.

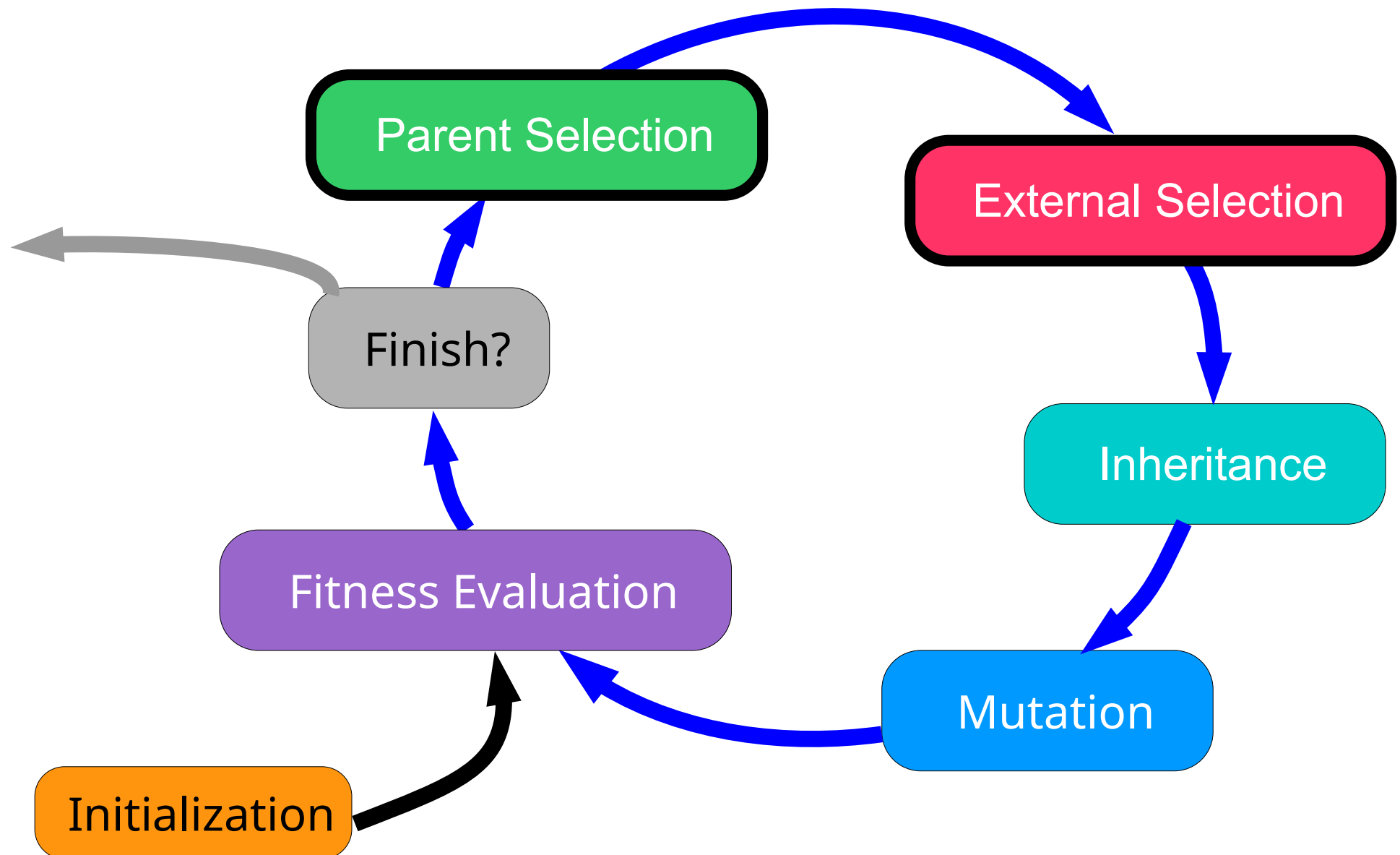
# Overview

- Genome structure
- Example: 8 queens
- Super-individuals
- External-selection and parent-selection combined
- Probabilistic parent-selection
  - Wheel of fortune
  - Softmax selection
  - Tournament selection
- Genetic programming
- Co-evolution

# EA cycle of operations

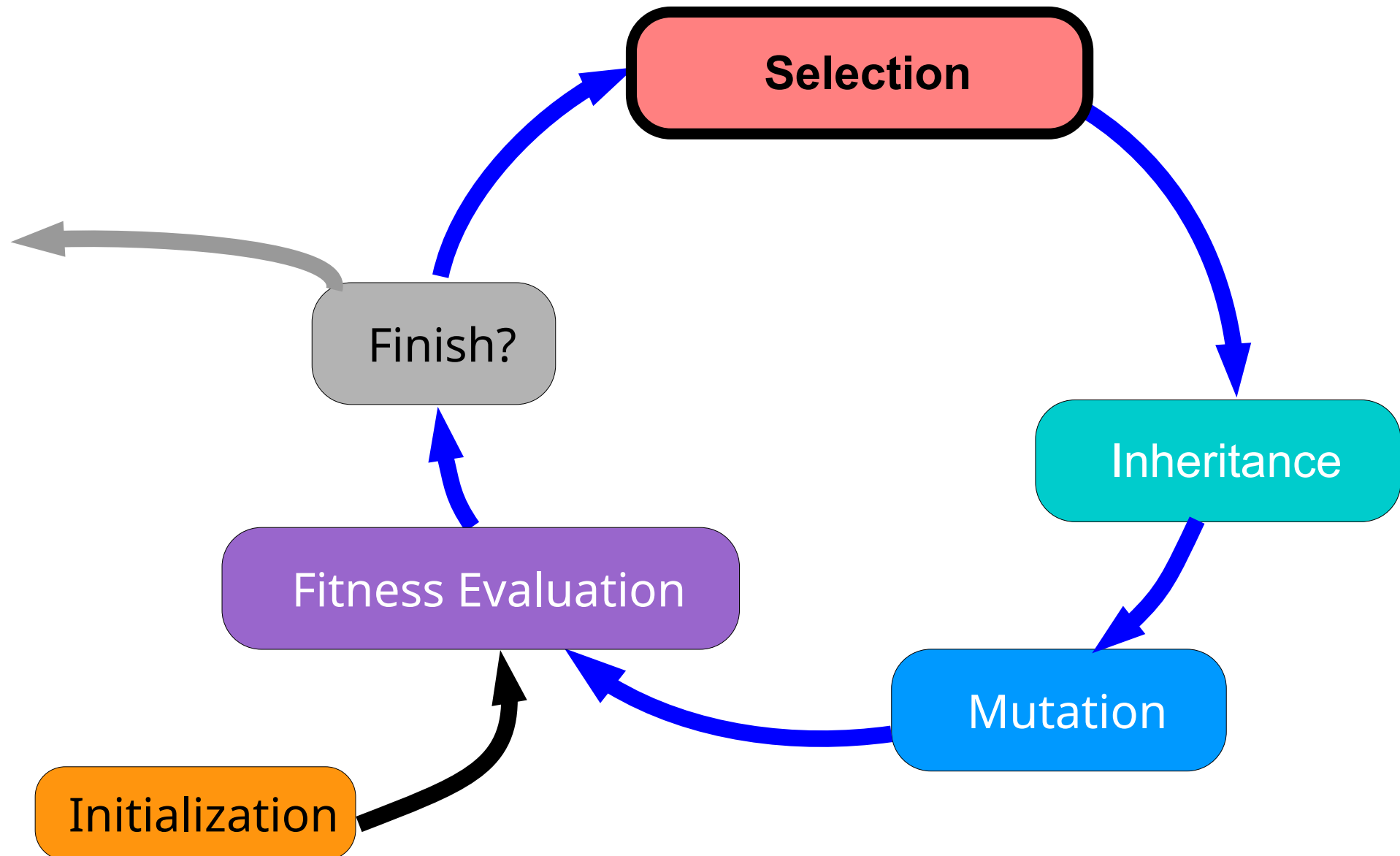


# EA cycle of operation

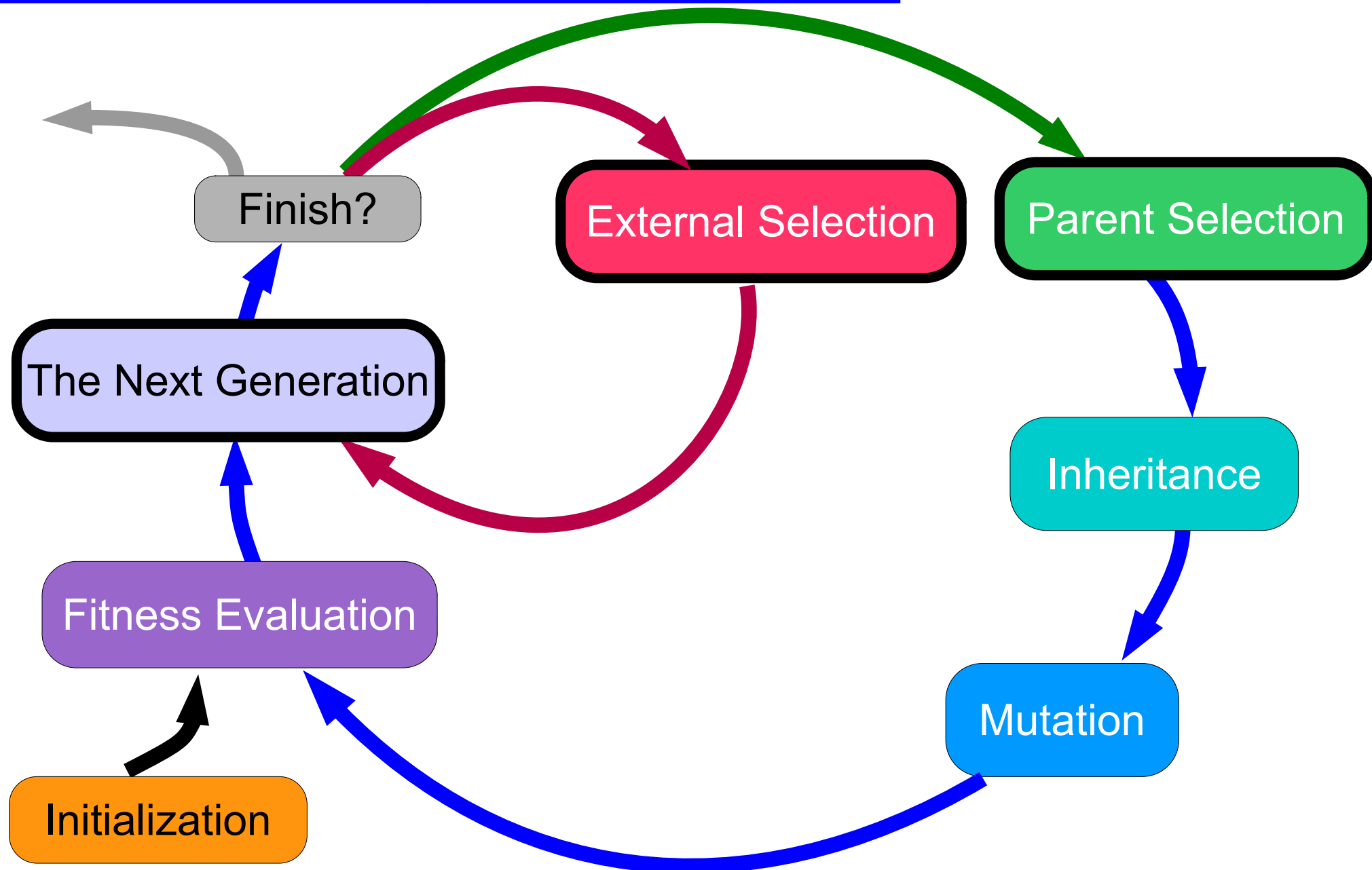




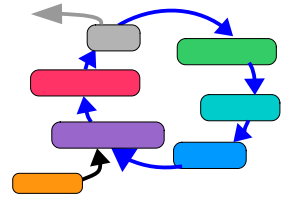
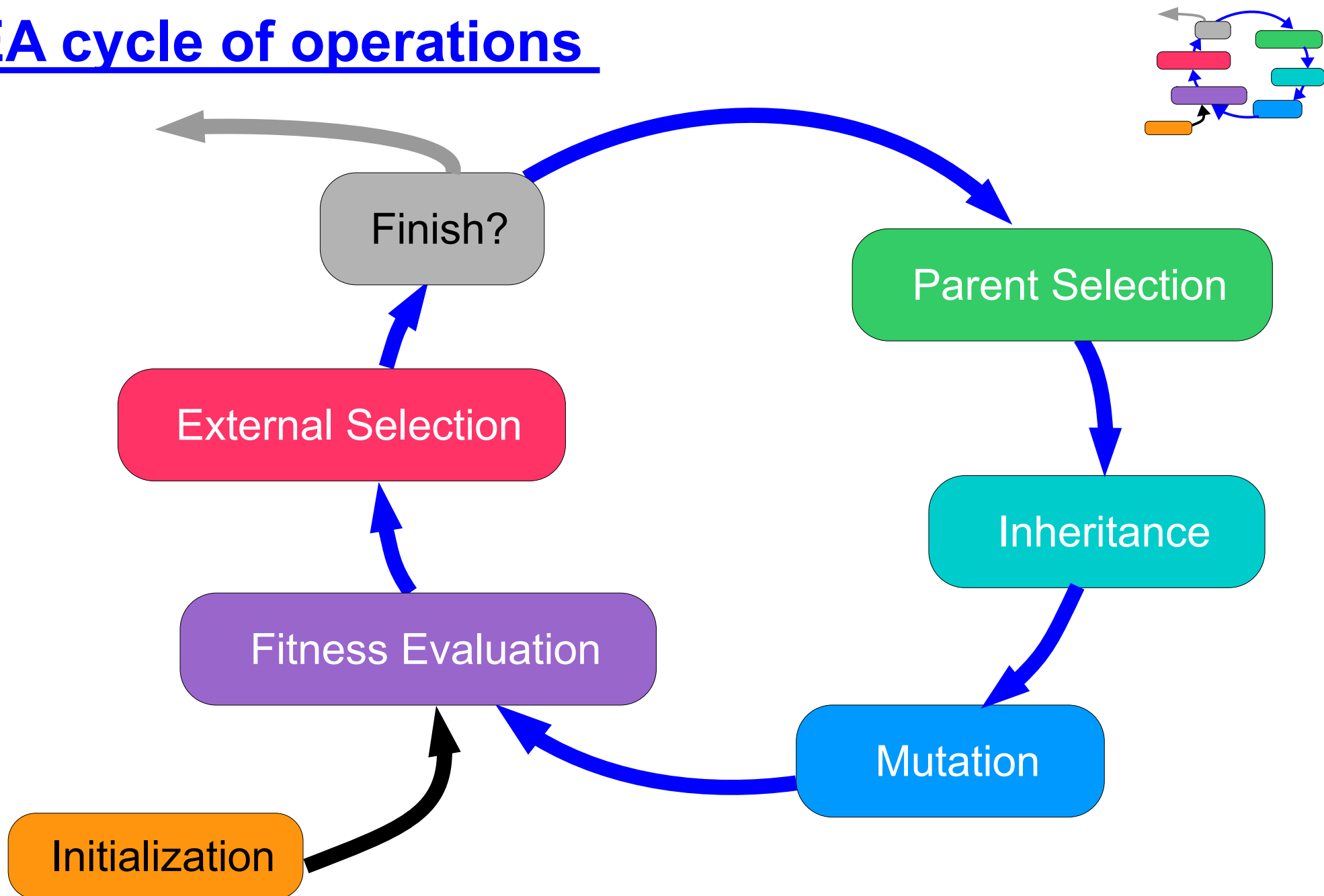
# EA cycle of operation



# EA alternative cycle of operation



# EA cycle of operations



## Some important dates

Wed 14.5.25: **Dies Academicus** , special talks, no regular teaching

Thu 29.5.25 : **Ascension Day** , no lectures, no exercises, ...

Sun 8.6. - 9.6.25 : **Pentecost, Whitsun, Pfingsten**, Public holiday

Tue 10.6.25 – Fri 13.6.25 : **Excursion week**, no lectures, exercises, ...

Thu 19.6.25 : **Feast of Corpus Christi**, no lectures, exercises, ...

# Programming Assignment PA-E

Write a Python Programm, that implements an evolutionary algorithm to **maximize the length** of a route going **twice** through a given set of  $N$  points (cities) in 2-dimensions.

Starting, and ending point are open to be determined by the algorithm; each point (city) must be visited **exactly twice**.

The  $N$  points  $X_n = (x_1, x_2)_n$  shall be read in from the text-file Positions\_PA-E.txt

This list are the positions of European Capitals w.r.t. a map:  
[http://upload.wikimedia.org/wikipedia/commons/6/64/Europe\\_capitals\\_map\\_de.png](http://upload.wikimedia.org/wikipedia/commons/6/64/Europe_capitals_map_de.png)

There is an additional new file: Positions2\_PA-E.txt  
augmented with the names of the European Capitals.

# Programming Assignment PA-E

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There is an additional new file: Positions2\_PA-E.txt  
augmented with the names of the European Capitals.

```
#Artificial_Life_Lecture_SS25_Programming_Assignment_PA_E_List_of_46_Positions_of_European_Capitals_in_2D
#Positions_are_according_to_map_http://upload.wikimedia.org/wikipedia/commons/6/64/Europe_capitals_map_de.png
1    446  621    #Amsterdam
2    328  913    #Andorra_la_Vella
3    1062 966    #Ankara
4    857  1071  #Athens
5    755  884    #Belgrade
6    606  627    #Berlin
7    477  798    #Bern
8    684  764    #Bratislava
9    430  671    #Brussels
10   889  857    #Bucharest
11   720  786    #Budapest
12   927  780    #Chisinau
13   592  535    #Copenhagen
14   249  548    #Dublin
15   788  383    #Helsinki
16   940  667    #Kiew
17    51  960    #Lisbon
18   627  831    #Ljubljana
19   ....  ....  .....
```



[http://upload.wikimedia.org/wikipedia/commons/6/64/Europe\\_capitals\\_map\\_de.png](http://upload.wikimedia.org/wikipedia/commons/6/64/Europe_capitals_map_de.png)

# Artificial Life Summer 2025

## Evolutionary Algorithms 3

Master Computer Science [MA-INF 4201]

Mon 14:15 – 15:45, HSZ, HS-2

Dr. Nils Goerke, Autonomous Intelligent Systems,  
Department of Computer Science, University of Bonn



# Artificial Life Summer 2025

## Evolutionary Algorithms 3

**Thank you for your patience**

Dr. Nils Goerke, Autonomous Intelligent Systems,  
Department of Computer Science, University of Bonn