

## Sheet G02 - Bézier Curves and TPS

Solutions for the theoretical and practical part via eCampus by Mo, 27.10.2025, 10:00.

### Practical Part

Please download the zip file `framework_g02.zip` from eCampus and unzip them into the framework's folder. Configure the project like last time.

**Submit this exercise by uploading the complete source file (`source.cpp`) onto eCampus!**

### Assignment 1) Tensor Product Surfaces

(3Pts)

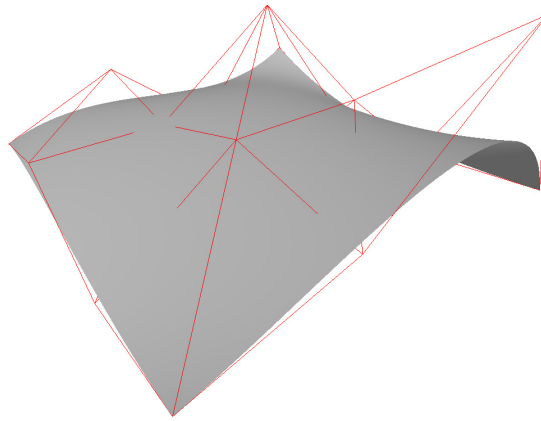


Figure 1: A Tensor Product Surface.

In the file `exercises/exercise02Surface/source.cpp` you will find the exercise for this assignment.

- In the function `getBezierCoefficients(...)`, implement the Bézier Coefficients for a degree 3 Bezier Curve.
- In the function `calculate_surface(...)`, implement the computation of the points on the tensor product surface according to

$$\mathbf{q}(u, v) = \sum_{i=0}^m \sum_{j=0}^n c_{ij} F_i^m(u) \cdot G_j^n(v)$$

where  $F_i^m = G_i^n = B_i^n$  are the Bernstein polynomials of degree  $n = 3$ .

After a correct implementation, the result should look like Figure 1.

## Theoretical Part

Please hand in a sheet-G02-*lastname*.pdf sheet written in L<sup>A</sup>T<sub>E</sub>X via eCampus!

### Assignment 2) B-spline Basis Functions

(4Pts)

- a) Compute and plot all basis functions up to degree 2 for knot vector  $U = \{0, 1, 2, 3, 4\}$ .
- b) Compute and plot all basis functions up to degree 2 for knot vector  $U = \{0, 1, 2, 3, 3, 3, 4, 5, 6\}$ .
- c) Verify the following propositions with convincing arguments:
  - $N_{i,p}(u)$  is a degree  $p$  polynomial.
  - For all  $i, p$  and  $u$ ,  $N_{i,p}(u)$  is non-negative.
- d) Given knot sequences  $U_1 = \{0, 0, 1, 1\}$  and  $U_2 = \{0, 0, 0, 1, 1, 1\}$ , use hand calculation to verify that the B-spline basis functions on  $U_1$  and  $U_2$  are identical to the Bézier basis functions.

**Good luck!**