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Find all subsets of a set (Power Set)

IN ALGORITHM, BIT MANIPULATION, INTERVIEWS, JAVA - ON 13:26:00 - NO COMMENTS

Visit us:

Print power set of any given set OR Print all subsets of a set OR Find all subsets of a set OR Print all subset of an array.

Given a set of numbers, print all the possible subsets of it including empty set.

What is Power Set?

In mathematics, the power set (or powerset) of any set S, written P(S), is the set of all subsets of S, including the empty set and S itself.

Let's understand it with help of example.

Case 1:

Input: Set(S) = [1,2]

Output: PowerSet P(S) = [[], [2], [1], [2, 1]]

Case 2:

Input: Set(S) = [a,b,c]

Output: PowerSet P(S) = [[], [a], [b], [c], [a,b], [a, c], [b, c], [a,

b, c]]

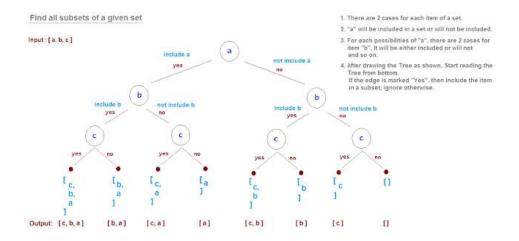
Solution

There can be many approach to solve this problem, here we will look at 2 simple approaches.

- 1. Using Tree representation approach.
- 2. Using Bit manipulation approach.

Tree Representation Approach

In this approach, we will draw a Tree like shown below,



There are 2 possibilities for each item of a set, It will be either included in a subset or not included.

Based on this fact, Lets draw a Tree for given Set [a, b, c]. Visit us:

There are 2 possibilities of "a". It will be either included in a subset or not included.

Similarly, For each possibilities of "a", again there are 2 possibilities for "b".

"b" will be included for each possibilities of "a" or not included.

Similarly, For each possibilities of "b", again there are 2 possibilities for "c".

Again, For "c", there are 2 possibilities either it will be considered or will be ignored in a subset.

Stop as there are no more items in a set remaining. Our Tree is complete and will look as shown in image above.

Lets understand our example and draw a Tree for it.

Set [a, b, c].

"a" is included.

- 1. "b" will be included in a subset.
 - 2. "c" will be included in a subset. END- No more element in Set.
 - 2. "c" will not be included in a subset. END- No more element in Set.
- 1. "b" will not be included in a subset.
 - 2. "c" will be included in a subset. END- No more element in Set.
 - 2. "c" will not be included in a subset. END- No more element in Set.

"a" is not included.

- 1. "b" will be included in a subset.
 - **2.** "c" will be included in a subset. END- No more element in Set.
 - 2. "c" will not be included in a subset. END- No more element in Set.
- 1. "b" will not be included in a subset.
 - 2. "c" will be included in a subset. END- No more element in Set.
 - 2. "c" will not be included in a subset. END- No more element in Set.

Now, read the Tree from Bottom to Root. Wherever there is Yes, include the item in a subset, ignore otherwise.

"a" is included.

- 1. "b" will be included in a subset.
 - 2. "c" will be included in a subset. END- No more element in Set. = [c, b, a]
 - 2. "c" will not be included in a subset. END- No more element in Set. = [b, a]

```
    "b" will not be included in a subset.
    "c" will be included in a subset.
    "c" will not be included in a subset.
    "c" will not be included in a subset.
    "b" will be included in a subset.
    "c" will be included in a subset.
    "c" will not be included in a subset.
    "c" will be included in a subset.
    "c" will not be included in a subset.
    "c" will
```

Understanding Program

Set S = [a, b, c]

Algorithm we will use for printing subset of a set is,

Step 1. Collect empty subset ([]) first because empty subset will be subset of any set including null set.

- Step 2. Now, For each item of a Set, Iterate subsets already found and
 - 1. Include a item in each subset and
 - 2. Not include a item in each subset.

```
Add empty set to subset list first.
Subsets - [ [] ]
1 - a, b, c
For a,
         Subsets = []
Include "a" in [].
Not include "a" in []
                                                                                       Subsets = [ [], [a] ]
         For b,
Subsets = [], [a]
Include "b" in [].
Not include "b" in []
                                                           ([b])
                                                           ([])
                 Include "b" in [a].
Not include "b" in [a]
                                                           ([b, a])
([a])
                                                                               Subsets = [ [b], [], [b, a], [a] ]
        ([c, b])
([b])
                 Include "c" in [].
Not include "c" in []
                 Include "c" in [b,a].
Not include "c" in [b,a]
                                                          ([c, b, a])
([b, a])
                 Include "c" in [a].
Not include "c" in [a]
                                                          ([c, a])
([a])
Subsets = [ [c, b], [b], [c], [], [c, b, a], [b, a], [c, a], [a] ]
```

Java Program for printing Subsets of set using Tree representation approach.

```
package string;
 1
     import java.util.ArrayList;
import java.util.Iterator;
 3
 4
     import java.util.List;
 6
 7
     public class FindAllSubsetOfSet {
 8
 9
      public static void main(String[] args) {
10
       System.out.println("\n"+createSubsetUsingTree("A"));
11
12
13
      private static List<String> createSubsetUsingTree(String str){
```

```
15
              List<String> result = new ArrayList<String>(); // take set if you want unique res
     16
              result.add("[]");
     17
     18
               //If str is not null, then process further otherwise return empty set.
              if(str!=null && str.length()>0){
     19
     20
                //Iterate each element of a set
     21
     22
                for (int i = 0; i < str.length(); i++) {</pre>
     23
     24
                 //Working on str.charAt(i);
     25
                 //Store the result of subset of str.charAt(i) in tempList.
     26
                 List<String> tempList = new ArrayList<String>();
     27
     28
                 //Add str.charAt(i) in each item of result.
     29
                 Iterator<String> iter = result.iterator();
     30
                 while(iter.hasNext()){
     31
                  String val = iter.next();
     32
                  // If val is [], it means str.charAt(i) is not included, So include it in rest
if(val.equals("[]")){
  tempList.add("[" + str.charAt(i) + "]");
     33
     34
     35
     36
                  }else{
     37
                    //For each item, there will be 2 subset, one including it and one without inc
//If val is not [], it means it already contain some subset without str.char/
tempList.add("[" + val.substring(1,val.length()-1) + ", " + str.char/At(i) + '
     38
     39
Visit 405:
     43
     44
                 //Add all subsets present in tempList to final result.
     45
                 result.addAll(tempList);
     47
              return result;
```

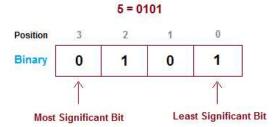
Bit Manipulation Approach

In this approach we will use Bits Manipulation for printing Subset of a set.

Before going ahead, first lets understand how to check any bit is set in a byte.

Binary representation of a number 1 = 0001, 2 = 0010,, 5 = 0101,

How to identify whether LSB, that is bit at position 0 is set in 5(0101)? Solution:



Do a Logical AND of 1 and 5 that is (0001 & 0101).

If the result is greater than 0, then LSB, that is bit at position 0 is set in value 5.

How to identify whether bit at position 1 is set in 5(0101)? Solution:

Do a Logical AND of 2 and 5 that is (0010 & 0101).

If the result is greater than 0, then bit at position 1 is set

So, to generalize it, if we want to check nth bit is set in a number,

- Step 1. We will first take binary representation of 1 (0001),
- Step 2. Move the LSB in binary representation of 1 to nth position.

Eg: If we want to check whether bit at position 2 is set, then move 1 two times on right side,

- = 1 << 2
- = 0001 << 2
- = 0100

Step 3. Once the LSB of binary 1 is moved to nth position, which we want to check,

just do logical AND of binary representation of 1 with the number,

If the result is greater than 0, then the bit is set, not otherwise.

If we want to find subset of 3 characters [a, b, c], then how many total subset can be made out of it?

If you observe, the number of subsets equals to 2 to the power of the number of elements in the set.

Number of subsets that can be made from set of 3 characters [a, b, c] is $2^3 = 8$ subsets.

Number of subsets that can be made from set of 4 characters [a, b, c, d] is $2^4 = 16$ subsets.

Visit us: there are n characters [a, b, c.... n] in a set, then there will be 2ⁿ total subsets.

How to find total number of subsets possible using bit manipulation?

By shifting the bit representation of the number 1 by n, we will get 2^n.

Thus, if we shift the bit string of 1 by the number of elements in the given set, we'll get the number of subsets for that set.

For example, if we have S = [a, b, c], length of set here is 3,

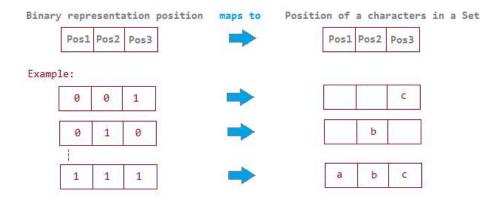
So, for finding total subsets, we have to shift binary 1, 3 times,

 $1 << 3 = (0001 << 3) = (1000) = 2^3 = 8$ subsets of set S.

If we compare subset of [a, b, c] to binaries representation of numbers from 0 to 7, we can find a relation with the bit sets in each number to subsets of [a, b, c].

Number	Binary representation	Subset
0	000	= Empty set
1	001	= C
2	010	= b
3	011	= bc
4	100	= a
5	101	= ac
4 5 6	110	= ab
7	111	= abc

Map 3 positions of Binary Representation to 3 characters of a set [a, b, c]



Understanding Program

```
length of a Set = 3

Total Subsets = 2<sup>3</sup> = 8 Subsets

i = 0 to 7

for 0 = 000
    check each bit at position 0, 1 and 2 in 000.

If bit at position 0 is set, then "a" will be part of subset.

If bit at position 1 is not set, then "b" will not be part of subset.

If bit at position 1 is not set, then "b" will not be part of subset.

If bit at position 1 is not set, then "b" will not be part of subset.

If bit at position 2 is set, then "c" will be part of subset.

If bit at position 2 is not set, then "c" will not be part of subset.

For 1 = 001
    check each bit at position 0, 1 and 2 in 001.

Bit at position 0 is set, NO, then "a" will not be part of subset.

Bit at position 2 is set, YES, then "c" will be part of subset.

For 7 = 111
    check each bit at position 0, 1 and 2 in 111.

Bit at position 1 is set, YES, then "a" will be part of subset.

Bit at position 1 is set, YES, then "a" will be part of subset.

Bit at position 1 is set, YES, then "a" will be part of subset.

Bit at position 1 is set, YES, then "a" will be part of subset.

Bit at position 1 is set, YES, then "b" will be part of subset.

Bit at position 2 is set, YES, then "b" will be part of subset.
```

Visit us:

Java Program for printing Subsets of set using Bit Manipulation approach.

```
package string;
     import java.util.ArrayList;
     import java.util.HashSet;
     import java.util.List;
import java.util.Set;
 7
     public class FindAllSubsetOfSet {
 8
 9
10
      public static void main(String[] args) {
11
       List<Object> list = new ArrayList<Object>();
       list.add("a");
list.add("b");
12
13
14
       list.add("c");
15
       System.out.println(getSubsetUsingBitMap(list));
16
17
18
19
      private static Set<Set<Object>> getSubsetUsingBitMap(List<Object> list){
20
21
       Set<Set<Object>> result = new HashSet<Set<Object>>();
22
23
       int numOfSubsets = 1 << list.size(); //OR Math.pow(2, list.size())</pre>
24
        // For i from 0 to 7 in case of [a, b, c]
25
26
        // we will pick \theta(0,0,0) and check each bits to see any bit is set,
27
        // If set then element at corresponding position in a given Set need to be include
28
       for(int i = 0; i < numOfSubsets; i++){</pre>
29
30
        Set<Object> subset = new HashSet<Object>();
31
        int mask = 1; // we will use this mask to check any bit is set in binary represe
32
33
34
        for(int k = 0; k < list.size(); k++){</pre>
35
         if((mask & i) != 0){ // If result is !=0 (or >0) then bit is set.
36
37
          subset.add(list.get(k)); // include the corresponding element from a given set
38
39
         // check next bit in i.
40
41
         mask = mask << 1;
42
43
44
         // add all subsets in final result.
45
        result.add(subset);
46
47
       return result;
48
      }
49
50
```

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Write a program to print all permutations of a given string without repetition. (Repetition of characters is not allowed).

Write a program to print all permutations of a given string with repetition. (Repetition of characters is allowed).

<u>Print all combinations/permutations of a string of length k that can be formed from a set of n</u> <u>characters</u>

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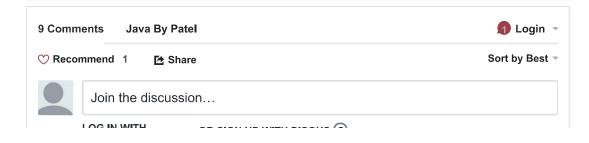
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AnOop PooNia • a year ago

best explanation ... god bless u brother



Vaibhavi • a year ago

Most thorough and original explanation of Power set!

Thank you for your efforts.



Ankita • a year ago

Thank you for the post !!

2 questions:

Visit us:

- 1) will the time complexity of tree method be O(2^N)
- 2) how to handle duplicates in both methods? I tried using bollean hashset but failed

Thanks in advance.



Venkat Pavan • a year ago

best explanation even a newbie like me understood the logic

∧ | ∨ . Reply . Share >



Jayesh Patel Mod → Venkat Pavan • a year ago

Thanks Venkat...

∧ | ∨ . Reply . Share >



dogbert82 • 2 years ago

Thanks for this very detailed explanation! I think this is the best ever explanation for subset problem I have ever seen! Once again thank you....I really enjoyed it..

∧ | ∨ . Reply . Share >



Jayesh Patel Mod → dogbert82 • 2 years ago

Thanks dogbert82....Your kind words means a lot to me and I am glad it helped...

∧ | ∨ . Reply . Share >



M.I. • 2 years ago

These lines are not very clear mate.

"If the result is greater than 0, then LSB, that is bit at position 0 is set in value 5."

and

"If the result is greater than 0, then bit at position 1 is set"

Thanks.



Jayesh Patel Mod → M.I. • 2 years ago

First of all sorry for late reply. I can understand, my words are confusing. I will rework on this and explain it in better way. Many thanks for feedback.

Matrix.

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I'm Jayesh Patel, author of "JavaByPatel".

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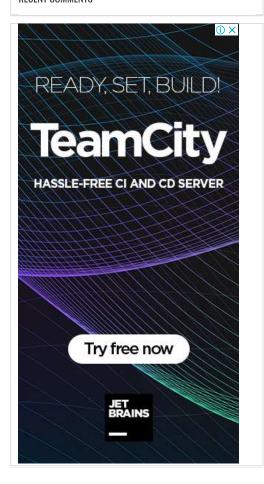
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