

RSA

$$p=5; q=7$$

$$n=pq=35$$

$$\varphi(p,q) = 4 \cdot 6 = 24$$

$$gg^T(e,4)=1$$

$$e=11$$

$$\rightarrow S_0 = (11, 35)$$

$$gg^T(5,7)=1 = 3 \cdot 5 - 2 \cdot 7$$

$$7 = 1 \cdot 5 + 2 \quad 2 = 7 - 1 \cdot 5$$

$$5 = 2 \cdot 2 + 1 \quad 1 = 5 - 2 \cdot 2$$

$$2 = 2 \cdot 1 + 0$$

$$5 - 2 \cdot 2 = 5 - 2(7 - 1 \cdot 5) = 5 - 2 \cdot 7 + 2 \cdot 5 = 3 \cdot 5 - 2 \cdot 7$$

$$gg^T(4,5)=gg^T(24,11)$$

$$24 = 2 \cdot 11 + 2$$

$$2 = 24 - 2 \cdot 11$$

$$11 = 5 \cdot 2 + 1$$

$$1 = 11 - 5 \cdot 2$$

$$11 - 5 \cdot 2 = 11 - 5(24 - 2 \cdot 11) = 11 - 24 \cdot 5 + 10 \cdot 11 = 11 \cdot 11 - 24 \cdot 5$$

$$2 = 2 \cdot 1 + 0$$

$$\rightarrow gg^T(24,11) = 1 = -5 \cdot 24 + 11 \cdot 11 = 11 \cdot 11$$

$$\rightarrow S_p = (11, 35)$$

$$\begin{array}{r} 8 \cdot 35 \\ 40 \\ \hline 60 \\ 100 \\ \hline 160 \\ 240 \end{array}$$

$$4=2$$

$$C = 4^e = 2^{11} = 2 \cdot 2^8 = 2 \cdot 4^4 = 2 \cdot 4 \cdot 4^3 = 8 \cdot 256$$

$$= 8 \cdot 11 = 88$$

$$= 8 \cdot 16$$

$$C^d = 16^8 = 16 \cdot (16)^7 = 16 \cdot 16 \cdot 16 \cdot 16 \cdot 16 \cdot 16 \cdot 16 \cdot 16$$

$$= 16 \cdot 16 \cdot 16 \cdot 16 \cdot 16 \cdot 16 \cdot 16 \cdot 16$$

$$= 2^{11}$$