

Boosting



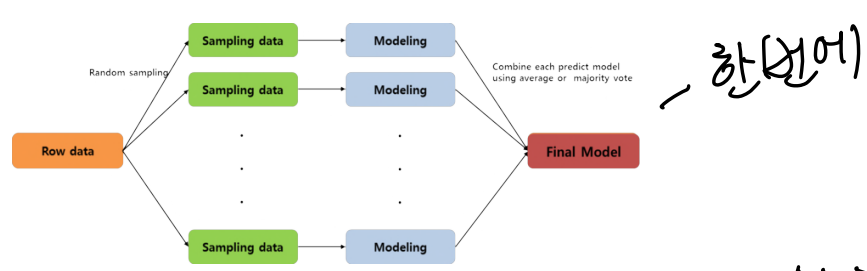
Gradient Boosting Algorithm

Bagging - 여러 Bootstrap 자료 결합하여 예측

∴ Bootstrap 자료를 산포 복원임의추출법

복원 샘플링으로 분산 줄이고 예측력 향상

과대적합, 분산이 크고 편향이 작은 모형 사용 결합



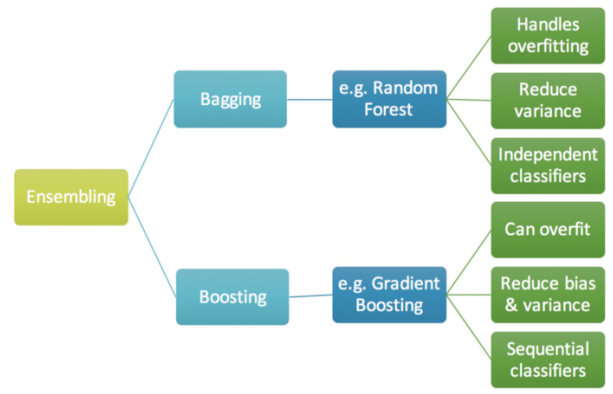
순차적으로

Boosting - 잘못 분류된 개체에 관심

약한 예측 모형 결합 → 강한 예측 모형

∴ 오분류에 높은 가중치

예측 모형 정확도 향상



비교	Bagging	Boosting
특징	병렬 앙상블 모델 (각 모델은 서로 독립적)	연속 앙상블 (이전 모델의 오류를 고려)
목적	Variance 감소	Bias 감소
적합한 상황	복잡한 모델 (High Variance, Low Bias)	Low Variance, High Bias 모델
대표 알고리즘	Random Forest	Gradient Boosting, AdaBoost
Sampling	Random Sampling	Random Sampling with weight on error

참고 : <https://www.slideshare.net/freepsw/boosting-bagging-vs-boosting>

Boosting - Gradient, adaptive

약한 분류기 $\xrightarrow{\text{순차적}} \text{강한 분류기}$

GBM 이해 - Residual fitting

Input: training set $\{(x_i, y_i)\}_{i=1}^n$, a differentiable loss function $L(y, F(x))$, number of iterations M .

Algorithm:

1. Initialize model with a constant value:

$$F_0(x) = \arg \min_{\gamma} \sum_{i=1}^n L(y_i, \gamma). \rightarrow \text{Baseline model}$$

2. For $m = 1$ to M :

1. Compute so-called *pseudo-residuals*:

$$r_{im} = - \left(\frac{\partial L(y_i, F(x_i))}{\partial F(x_i)} \right)_{F(x) = F_{m-1}(x)} \quad \text{for } i = 1, \dots, n.$$

\rightarrow negative gradient = pseudo-residual

2. Fit a base learner (e.g. tree) $h_m(x)$ to pseudo-residuals, i.e. train it using the training set $\{(x_i, r_{im})\}_{i=1}^n$.

3. Compute multiplier γ_m by solving the following one-dimensional optimization problem:

$$\gamma_m = \arg \min_{\gamma} \sum_{i=1}^n L(y_i, F_{m-1}(x_i) + \gamma h_m(x_i)).$$

4. Update the model:

$$F_m(x) = F_{m-1}(x) + \gamma_m h_m(x).$$

3. Output $F_M(x)$.

다익 쿼리

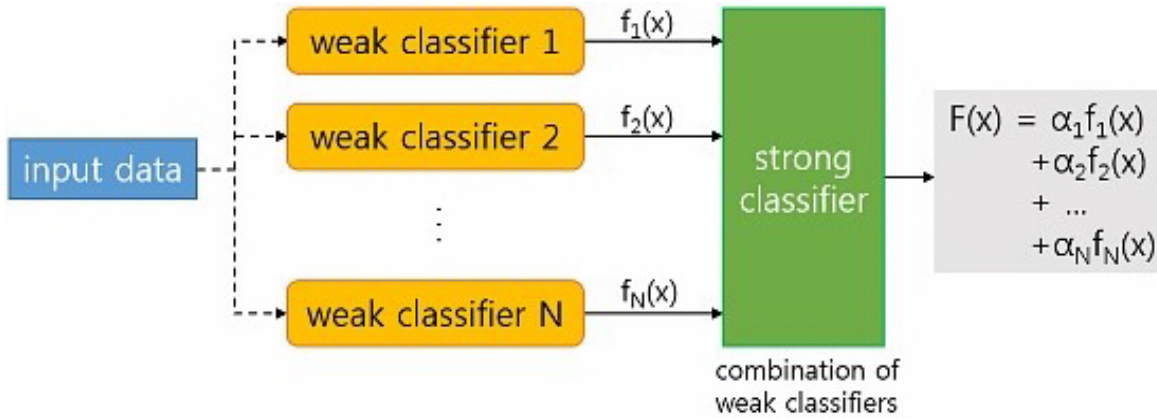
1. x Gradient p_x

2. $x+1$ Gradient update p_{x+1}

3. $x+2$ " p_{x+2}

$$Hx = \sum_{i=1}^n \alpha_i f_i$$

약한 분류기 조합하여 강분류기 만들기



AdaBoost is an algorithm for constructing a "strong" classifier as linear combination

$$f(x) = \sum_{t=1}^T \alpha_t h_t(x)$$

of "simple" "weak" classifiers $h_t(x)$.

$h_t(x)$... "weak" or basis classifier, hypothesis, "feature"

$H(x) = \text{sign}(f(x))$... "strong" or final classifier/hypothesis

Adaboost - adaptive + boosting · 상호보완, 순차적

· 앞서 분류기가 잘못 분류한 결과를 다음 분류기 학습에 사용

How it works?

$$\hookrightarrow \text{아마 } w_{n+1} = w_n - \frac{\partial L}{\partial w}$$

1. 모든 feature에 대해 성능평가, 각 feature마다 weight error 계산
2. 분류 성능 가장 좋은 feature을 해당 round의 weak classifier
3. 해당 weak classifier의 weight를 극대화. - 예러가 작으면 중요도 ↑
4. training sample의 weight를 업데이트
잘못분류된 sample의 weight 증가 → 해당 샘플 중요도 증가
5. t+1 반복

→ 다음에 잘못분류된 영향 신경쓰고

최종 output $H(x) = \alpha_1 h_1(x) + \alpha_2 h_2(x) + \dots + \alpha_T h_T(x) = \sum_{t=1}^T \alpha_t h_t(x)$

weight

Given: $(x_1, y_1), \dots, (x_m, y_m)$ where $x_i \in \mathcal{X}$, $y_i \in \{-1, +1\}$. training sample target label (no, yes)
Initialize: $D_1(i) = 1/m$ for $i = 1, \dots, m$. D : weight of training samples (the probability of being selected for training the component classifier)
For $t = 1, \dots, T$: T : iteration round

- Train weak learner using distribution D_t .
- Get weak hypothesis $h_t: \mathcal{X} \rightarrow \{-1, +1\}$.
- Aim: select h_t with low weighted error:

$$\sum_{i: h_t(x_i) \neq y_i} D_t(i) \quad \leftarrow \quad \varepsilon_t = \Pr_{i \sim D_t} [h_t(x_i) \neq y_i] \begin{cases} 1 & \text{if misclassified,} \\ 0 & \text{if properly classified} \end{cases}$$

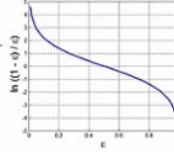
ε : error rate of weak classifier

- Choose $\alpha_t = \frac{1}{2} \ln \left(\frac{1 - \varepsilon_t}{\varepsilon_t} \right)$. α : weight (importance) of weak classifier

- Update, for $i = 1, \dots, m$:

update weights of training samples

$$D_{t+1}(i) = \frac{D_t(i) \exp(-\alpha_t y_i h_t(x_i))}{Z_t}$$



where Z_t is a normalization factor (chosen so that D_{t+1} will be a distribution).

Output the final hypothesis:

H : strong classifier

$$H(x) = \text{sign} \left(\sum_{t=1}^T \alpha_t h_t(x) \right)$$

$$\sum_i D_{t+1}(i) = 1$$

