HERAFitter

Open Source QCD Fit Project

HERAFitter team

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interfaces to external software packages which are also de- 37 and then use these PDFs for predicting other processes. scribed here.

18 Keywords PDFs · QCD · Fit

19 1 Introduction

signals of new physics at the LHC it is crucial to have accalculate the SM cross sections for such reactions is to use collinear factorisation in perturbative QCD (pQCD):

$$\begin{split} \sigma^{pp\to H+X}(\alpha_s,\mu_r,\mu_f) &= \sum_{\substack{a,b \ 0}} \int\limits_0^1 dx_1 \int\limits_0^1 dx_2 \, f_a(x_1,\alpha_s,\mu_F) f_b(x_2,\alpha_s,\mu_F) \\ &\times \hat{\sigma}^{ab\to H+X}(x_1,x_2;\alpha_s,\mu_R,\mu_F). \end{split}$$

Here the cross section $\sigma^{pp\to H+X}$ for inclusive Higgs pro- 55 is schematically illustrated in Fig. 1 and consists of four parts: duction is expressed as a convolution of Parton Distribution 56

Abstract We present the HERAFitter project which pro- 22 Functions (PDF) f_a and f_b with the partonic cross section vides a framework for Quantum Chronodynamics (QCD) 23 $\hat{\sigma}^{ab\to H+X}$. The PDFs describe the probability of finding a analyses related to the proton structure in the context of $\frac{1}{24}$ specific parton a(b) in the first (second) proton carrying a multi-processes and multi-experiments. Based on the con- z_2 fraction x_1 (x_2) of its momentum. The sum over indices a 5 cept of the factorisable nature of the cross sections into uni- $\frac{1}{26}$ and b in Eq. 1 indicates the various kinds of partons, i.e. versal Parton Distribution Functions (PDFs) and process de- 27 gluons, quarks and antiquarks of different flavours, that are pendent partonic scattering cross sections, HERAFitter al- 28 considered as the constituents of the proton. Both the PDFs 8 lows determination of PDFs from the various hard scatter- 29 and the partonic cross section depend on the strong coupling ing measurements. The main processes and data sets that are α_s constant α_s , and the factorisation and renormalisation scales, currently included are Deep-Inelastic-Scattering in ep colli- μ_F and μ_R , respectively. The partonic cross sections are calsions at HERA and Drell Yan, jet and top quark production 32 culable in pQCD, but the PDFs cannot yet be predicted in in $pp(p\bar{p})$ collisions at the LHC (Tevatron). HERAFitter 33 QCD, they must rather be determined from measurement. provides a comprehensive choice in the treatment of the ex- 34 They are assumed to be universal such that different scatperimental uncertainties. A large number of theoretical and 35 tering reactions can be used to constrain them; in particular methodological options is available within HERAFitter via 36 one can use specific reaction data for determining the PDFs

The inclusive Neutral Current (NC) and Charged Current (CC) data in Deep-Inelastic-Scattering (DIS) at ep col-40 lider HERA provide crucial information for determining the 41 PDFs. For instance, the gluon density relevant for calcu-42 lating the dominant gluon-gluon fusion contribution to the 43 Higgs production at the LHC can be accurately determined In the era of the Higgs discovery and extensive searches for 44 from the HERA data alone. Specific data from the Tevatron $p\bar{p}$ and the LHC pp collider can help to further constrain the curate Standard Model (SM) predictions for hard scatter- 46 PDFs. The most sensitive processes at the hadron colliders ing processes at the LHC. The most common approach to 47 are Drell Yan (DY) production, W and Z asymmetries, associated production of W or Z boson and heavy quarks, top 49 quark production and jet production.

> HERAFitter represents a QCD analysis framework that aims at determining precise PDFs by integrating all the PDF 52 sensitive information from HERA, Tevatron and LHC. The (1) 53 processes that are currently included in HERAFitter framework are listed in Tab. 1. The functionality of HERAFitter

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Data	Туре	Reaction	Theory calculation
	I	l	Carcalation
HERA	DIS NC	$ep \rightarrow ep$	QCDNUM [1], RT [2–5],
			ACOT [6]
HERA	DIS CC	$ep \rightarrow v_e p$	QCDNUM [1], RT [2–5],
TILICI	Disce	cp , vep	ACOT [6]
HERA	DIS jets	v.v	FastNLO (NLOJet++ [7, 8])
	3	$ep \rightarrow eX$	
HERA	DIS heavy	$ep \rightarrow ep$	ZM (QCDNUM [1]),
	quarks		RT [2–5], ACOT [6],
			FFNS (ABM [9, 10],
			QCDNUM [1])
Fixed Target	DIS NC	$ ep \rightarrow ep$	ZM (QCDNUM [1]),
Timed Tanget	DISTIC	P P	RT [2–5], ACOT [6]
		l	KI [2-5], ACOI [0]
Tevatron, LHC	Drell Yan	$pp(\bar{p})$	APPLGRID (MCFM [11-13])
Tevatron, LHC	W charge asym	$pp(\bar{p})$	APPLGRID (MCFM [11–13])
Tevatron, LHC	top	$pp(\bar{p})$	APPLGRID (MCFM [11–13]),
Tevation, Erro	top .	PP(P)	HATHOR [14]
Tevatron, LHC	jets	$pp(\bar{p})$	APPLGRID (NLOJet++ [7, 8])
Teration, Life	jets	PP(P)	FastNLO (NLOJet++ [7, 8])
* ***	DV.	(-)	
LHC	DY + heavy	$pp(\bar{p})$	APPLGRID (MCFM [11–13])
	quarks		RT [2–5], ACOT [6],

Table 1 The list of processes available in the HERAFitter package. The APLLGRID [15] and FastNLO [16–18] techniques for the fast interface to theory calculations are described in section 3.

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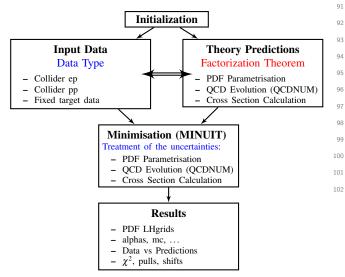


Fig. 1 Schematic structure of the HERAFitter program.

Input data: All relevant cross section measurements from the various reactions are stored internally in HERAFitter with the full information on their uncorrelated and correlated uncertainties. HERA I data sets are the basis of any proton PDF extraction, and they are used by all global PDF groups [5, 19–22]. Additional measurements provide constraints to the sea flavour decompositon (such as the new results from the LHC), as well as constraints to PDFs in the corners of the kinematic phase-space not covered precisely by HERA I, such as the high *x* region for the gluon and valence distributions.

Theory predictions: Predictions are obtained relying on the factorisation approach (Eq. 1). PDFs are parametrised at a starting scale Q_0^2 by a chosen functional form with a set of free parameters **p**. They are then evolved from Q_0^2 to the scale of the measurement using the Dokshitzer-

Gribov-Lipatov-Altarelli-Parisi (DGLAP) [23–27] evolution equations as implemented in QCDNUM [1], and then convoluted (Eq. 1) with the hard parton cross sections calculated by a specific theory program (as listed in Tab. 1).

Minimization: PDFs are extracted from a least square fit by constructing a χ^2 from the input data and the theory prediction. The χ^2 is minimized iteratively with respect to the PDF parameters using the MINUIT[28] program. Various choices of accounting for the experimental uncertainties are employed in HERAFitter, either using nuisance parameter method for accounting of the correlated systematic uncertainties, or covariance matrix method. In addition, HERAFitter allows analysers to study different statistics assumptions for the distributions of the systematic uncertainties (i.e. Gauss or lognormal) [29].

Results: The fitted parameters **p** and their estimated uncertainties are produced. The resulting PDFs are provided in a format ready to be used by the LHAPDF library [30, 31]. Drawing tools are supplied which allow the PDFs to be graphically displayed at arbitrary scales with their one sigma uncertainty bands. A first set of PDFs extracted by HERAFitter is HERAPDF1.0 [32] which is based on HERA I data, a default data set in HERAFitter. This is illustrated in the Fig. 2. Since then, more sets were produced within the HERA and LHC collaborations, respectively. In addition to PDF display, to demonstrate the fit consistency, plots which compare the input data to the fitted theory predictions can be made using tools supplied with the package.

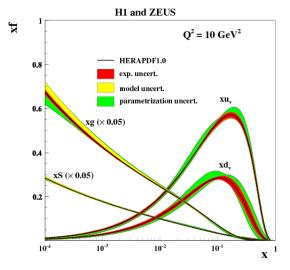


Fig. 2 Summary plots of valence, total sea (scaled) and gluon densities(scaled) with their experimental, model and parametrisation uncertainties at the scale of $Q^2 = 10 \text{ Gev}^2$ of the HERAPDF1.0 PDF set at NLO [32].

data and the theory prediction, the pull information (de- 143 and s is the centre-of-mass energy. fined as the difference between data and prediction di- 144 The NC cross section can be expressed in terms of structure vided by the uncorrelated uncertaintly of the data) is dis- 145 functions: played in units of sigma shifts for each given data bin.

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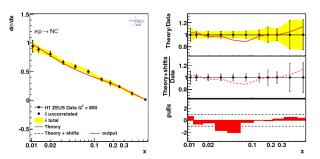


Fig. 3 An illustration of the HERAFitter drawing tools comparing the measurements (in this case HERA I) to the predictions of the fit. In addition, ratio plots are also provided together with the pull distribution (right panel).

Therefore, this project represents an ideal environment for benchmarking studies and a unique platform for the QCD interpretation of analyses within the LHC experiments, as already demonstrated by several publicly available results using the HERAFitter framework [33-39].

The outline of this paper is as follows. Section 2 discusses the various processes and corresponding theoretical calculations performed in the DGLAP [23-27] formalism that are available in HERAFitter. Alternative approaches to the DGLAP formalism are presented in section 5. In section 3 various different choices made in the theory calculations are described. Section 4 elucidates the methodology of determining PDFs through fits based on various χ^2 definitions used in the minimisation procedure. Specific applications of the package are given in section 6.

2 Theoretical Input

In this section the theoretical formalism for various processes available in HERAFitter are described.

2.1 Deep Inelastic Scattering Formalism and Schemes

Deep Inelastic Scattering (DIS) data provide the backbone 180 of any PDF fit. The formalism relating DIS measurements to 181

pQCD and the PDFs has been described in detail in many ex-Fig. 3 shows a comparison of inclusive NC data from the 136 tensive reviews [40] and will only be briefly recapped here. HERA I running period with predictions based on HER- 137 DIS is lepton scattering off the constituents of the proton by APDF1.0. It also illustrates the comparison to the theory 138 a virtual exchange of a neutral (NC) or charged (CC) vector predictions which are adjusted by the systematic uncer- 139 boson and, as a result, a scattered lepton and a multihadronic tainty shifts when using nuisance parameter method of 140 final state are produced. The DIS kinematic variables are the accounting for correlated systematic uncertainties (see 141 negative squared four-momentum of the exchange boson, section 4.2). As an additional consistency check between $_{142}$ Q^2 , the Bjorken x, and the inelasticity y, where $y = Q^2/sx$

$$\frac{d^2 \sigma_{NC}^{e^{\pm} p}}{dx dO^2} = \frac{2\pi \alpha^2}{x O^4} \left[Y_+ \tilde{F}_2^{\pm} \mp Y_- x \tilde{F}_3^{\pm} - y^2 \tilde{F}_L^{\pm} \right],\tag{2}$$

where $Y_{\pm} = 1 \pm (1 - y)^2$. The structure function \tilde{F}_2 is the dominant contribution to the cross section, $x\tilde{F}_3$ is important 148 at high Q^2 and \tilde{F}_L is sizable only at high y. In the framework of perturbative QCD the structure functions are directly related to the parton distribution functions, i.e. in leading order (LO) F_2 is the weighted momentum sum of quark and anti-quark distributions, $F_2 \approx x \sum e_q^2 (q + \overline{q})$, and xF_3 is related to their difference, $xF_3 \approx x \sum_{q} 2e_q a_q (q - \overline{q})$ (where a_q is the axial-vecor quark coupling). At higher orders, terms related to the gluon density distribution ($\alpha_s g$) appear, in particular F_L is strongly related to the low-x gluon.

The inclusive CC *ep* cross section can be expressed in terms of another set of structure functions and in LO the e^+p and e^-p cross sections are sensitive to different quark flavour 160 densities:

$$e^{+}: \ \tilde{\sigma}_{CC}^{e^{+}p} = x[\overline{u}] + (1-y)^{2}x[d] e^{-}: \ \tilde{\sigma}_{CC}^{e^{-}p} = x[u] + (1-y)^{2}x[\overline{d}].$$
(3)

Here u and d denote the sum over up- and down-type quarks; the latter include also strange and beauty quarks and the former charm quarks. Beyond LO, the QCD predictions for the DIS structure functions are obtained by convoluting the PDFs with the respective coefficient functions (hard process matrix elements). The treatment of heavy charm and beauty quark production is a crucial point in these calculations and several schemes exist:

In the Fixed Flavour Number (FFN) scheme [41–43] only the gluon and the light quarks are considered as partons within the proton and massive quarks are produced perturbatively in the final state. The lowest order process is the fusion of a gluon in the proton with a boson from the electron to produce a heavy quark and an antiquark.

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In the Zero-Mass Variable Flavour Number (ZM-VFN) scheme[44] the heavy quark densities are included in the proton for Q^2 values above a threshold $\sim m_h^2$ and are treated as massless in both the initial and final states. The lowest order process is the scattering of a heavy quark in the proton with the electron via (electroweak) boson

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exchange. This scheme is expected to be reliable only in 234 the region $Q^2 >> m_h^2$.

In the general mass Variable-Flavour number (GM-VFN) 236 scheme [45] heavy quark production is treated for $Q^2 \le 237$ m_h^2 in the FFN scheme and for $Q^2>>m_h^2$ in the ZM- 238 VFN scheme with a suitable interpolation in between. 239 This scheme is very popular and numerous variants ex- 240

All three schemes are available in HERAFitter . In the following the implemented variants are briefly discussed.

FFN schemes: In HERAFitter this scheme can be accessed via the QCDNUM implementation or through the interface to the open-source code OPENOCDRAD (as implemented by the ABM group) [9]. The latter implementation also includes the running mass definition of the heavy quark mass [10]. The running mass scheme has the advantage of reducing the sensitivity of the DIS cross sections to higher order corrections, and improving the theoretical precision of the mass definition. In QCDNUM, the calculation of the heavy quark contributions to DIS structure functions are available at Nextto-Leading-Order (NLO) and only electromagnetic exchange contributions are taken into account. In the ABM implementation, both CC and NC contributions are avail- 255 2.2 Drell Yan processes in pp or $p\bar{p}$ collisions able at NLO and the Next-to-Next-to Leading Order (NNLO) QCD corrections to the massive Wilson coefficients, which The Drell Yan (DY) process provides further valuable inis currently best known approximation [46].

treated as infinitely massive below scale in vicinity of heavy quark mass, and massless above this threshold. Thi prescription has been used for many years by global 261 PDF groups, however it is only suited for quantitative 262 analyses for scales $Q^2 >> m_h^2$, for which the terms of ²⁶³ order $\mathcal{O}(m_h^2/Q^2)$ can be neglected.

GM-VFN Thorne-Roberts scheme: The Thorne-Roberts 265 (TR) scheme provides a smooth transition from the mas- 266 are two different variants of the TR schemes: TR stan-269 dard (as used in MSTW PDF sets [2, 3, 5]) and TR op- 270 age and described below: timal [4], with a smoother transition across the heavy quark threshold region. Both of these variants are accessible within the HERAFitter package at NLO and NNLO.

GM-VFN ACOT scheme: olaf remark: I find the following paragraph information on the CTEQ scheme a bit difficult to digest/appreciate. The Aivazis-Collins-Olness-Tung scheme belongs to the group of VFN factorisation schemes that use the renormalization method of Collins-Wilczek-Zee (CWZ) [6]. This scheme involves a mixture of the \overline{MS} scheme for light and heavy (when the factorisation scale is larger than the heavy quark mass) partons and the zero-momentum subtraction renormalisation scheme for graphs with heavy quark lines (if the factorisation scale is smaller than the mass of the heavy quark threshold).

Within the ACOT package, different variants of the ACOT scheme are available: ACOT-Full, S-ACOT-χ, ACOT-ZM, MS at LO and NLO. For the longitudinal structure function higher order calculations are also available. The ACOT-Full implementation takes into account the quark masses and it reduces to ZM MS scheme in the limit of masses going to zero, but it has the disadvantage of being quite slow.

Calculations of higher-order electroweak corrections to 247 DIS scattering at HERA are available in HERAFitter performed in the on-shell scheme where the gauge bosons masses $_{249}$ M_W and M_Z are treated symmetrically as basic parameters 250 together with the top, Higgs and fermion masses. These electroweak corrections are based on the EPRC package [47]. $_{\text{252}}$ The code provides the running of α using the most recent parametrisation of the hadronic contribution to Δ_{α} [48], as well as an older version from Burkhard [49].

formation about PDFs. In pp and $p\bar{p}$ scattering, the Z/γ and ZM-VFN schemes: In this scheme, the heavy quarks are 258 W production probe bi-linear combinations of quarks. Complementary information on the different quark densities can be obtained from W asymmetry (d, u and their ratio), the ratio of the W and Z cross sections (sensitive to the flavor composition of the quark sea, in particular to the s density), associated W and Z production with heavy quarks (sensitive $_{264}$ to s and c quark densities).

Presently, the predictions for Drell-Yan and W and Z production are known NNLO and W,Z +heavy flavour are sive FFN scheme at low scales $Q^2 < m_h^2$ to the mass- 267 know to NLO. There are several possibilities for obtaining less ZM-VFNS scheme at high scales $Q^2 >> m_h^2$. There 268 the theoretical predictions for DY production in HERAFitten the theoretical predictions for DY production in HERAFitter . At LO an analytic calculation is available within the pack-

> The leading order DY triple differential cross section in invariant mass M, boson rapidity v and CMS lepton scattering angle $\cos \theta$, for the neutral current, can be written as [50, 51]:

$$\frac{d^3\sigma}{dMdyd\cos\theta} = \frac{\pi\alpha^2}{3MS} \sum_q P_q \left[F_q(x_1, Q^2) F_{\bar{q}}(x_2, Q^2) + (q \leftrightarrow \bar{q}) \right], \tag{4}$$

where *S* is the squared CMS beam energy, $x_{1,2} = \frac{M}{\sqrt{S}} \exp(\pm y)$, $F_q(x_1, Q^2)$ is the parton number density, and P_q is a partonic cross section.

The expression for charged current scattering has a simpler 311 3 Computational Techniques form.

$$\frac{d^{3}\sigma}{dMdyd\cos\theta} = \frac{\pi\alpha^{2}}{48S\sin^{4}\theta_{W}} \frac{M^{3}(1-\cos\theta)^{2}}{(M^{2}-M_{W}^{2}) + \Gamma_{W}^{2}M_{W}^{2}}$$
$$\sum_{q_{1},q_{2}} V_{q_{1}q_{2}}^{2} F_{q_{1}}(x_{1},Q^{2}) F_{q_{2}}(x_{2},Q^{2}), \tag{5}$$

where $V_{q_1q_2}$ is the CKM quark mixing matrix and M_W and Γ_W are W boson mass and decay width.

The simple form of these expressions allows the calculation of integrated cross sections without utilization of Monte-Carlo techniques which often introduce statistical fluctuations. In both neutral and charged current expressions the parton distribution functions factorise as functions dependent only on boson rapidity y and invariant mass M and the integral in $\cos \theta$ can be computed analytically.

The NLO and NNLO calculations are highly demanding 325 in terms of the computing power and time, and k-factor or fast grid techniques need to be used (see section 3 for details). The programme MCFM [11–13] is available for NLO $\,^{\scriptscriptstyle 328}$ calculations and the programmes FEWZ [52] and DYNNLO [53] for NLO and NNLO.

2.3 Jet production in ep and pp collisions

Jet production at high transverse momentum is sensitive to the high-x gluon PDF (see e.g. [5]) and can thus increase 336 the precision of the gluon PDF determination, which is particularly important for Higgs production and searches for 338 new physics. Jet production cross sections are only currently 339 known to NLO, although NNLO calculations are now quite 340 advanced [54, 55]. Within HERAFitter the programmes 341 MCFM and NLOJET++ [7, 8] may be used for the calcula- 342 tion of jet production. Similarly to DY case, the calculation 343 is very demanding in terms of computing power. Therefore, 344 to allow the possibility to include the ep, pp or $p\bar{p}$ jet cross 345 section measurements in QCD fits to extract PDF and α_s fits 346 fast grid techniques are used (see section 3).

2.4 Cross Sections for $t\bar{t}$ production in pp or $p\bar{p}$ collisions

Top-quark pairs $(t\bar{t})$ are produced at hadron colliders dominantly via gg fusion and $q\bar{q}$ annihilation. This provides the 353 possibility to use top production to constrain the gluon den- 354 sity in the proton. Calculations are available to NLO in MCFM₅₅ and to approximate NNLO in the program HATHOR [14]. 356 These are both available within HERAFitter Version 1.3 of 357 HATHOR includes the exact NNLO for $q\bar{q} \rightarrow t\bar{t}$ [56] as well 358 as a new high-energy constraint on the approximate NNLO 359 calculation obtained from soft-gluon resummation [57]. The 360 use of these programmes also needs fast grid techniques.

With increased precision of data, the calculations must also progress to higher accuracy, involving an increased number of diagrams with each additional order, and this translates (5) 315 into computationally demanding calculations even for the DIS processes. Such calculations are too slow to be used iteratively in a fit. There are several methods available which allow fast PDF extractions. Two such techniques are implemented into HERAFitter : the k-factor approximation from lower (LO) to higher order (NLO) and the fast grid techniques using interfaces to the packages FastNLO and APPLGRID. These techniques are briefly described below.

k-factor technique:

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A k-factor is a ratio of the prediction between a highorder (slow) pQCD calculation and the lowest-order (fast) calculation. These "k-factors" are evaluated as a function of the kinematic variables relevant to the measurement for a fixed PDF (for example the first iteration of the fit) and stored in tables. They can then be applied 'on the fly' to each subsequent fit iteration which will use the fast prediction multiplied by this "k-factor". Having determined a PDF this way the output PDF fit should then be used to recalculate the k-factors and the fit repeated until input and output k-factors have converged.

- For the DIS process, the heavy flavour schemes provide accurate but computationally slow calculations. In HERAFitter "FAST" schemes were implemented such that the k-factor used can be the ratio between same order calculations but massless vs massive (i.e. NLO (ZM-VFNS)/NLO (ACOT), or the ratio between LO (massless)/NLO (massive). The kfactors are only calculated for the PDF parameters at the first fit iteration and hence, the FAST heavy flavour schemes should only be used for quick checks and the full scheme is recommended. The method was employed in the QCD fits to the HERA data when ACOT scheme was used as a cross check of the central results [32], as shown in Fig. 4.
- In the case of the DY processes the LO calculation described in section 2.2 is such that the PDF functions factorise, allowing high speed calculations when performing parameter fits over lepton rapidity data. In this case the factorised part of the expression which is independent of PDFs can be calculated only once for all minimisation iterations. The leading order code in HERAFitter package implements this optimisation and uses fast convolution routines provided by QCDNUM. Currently the full width LO calculations are optimised for lepton pseudorapidity and boson rapidity distributions with the possibility to apply lepton p_{\perp} cuts. This flexibility allows the cal-

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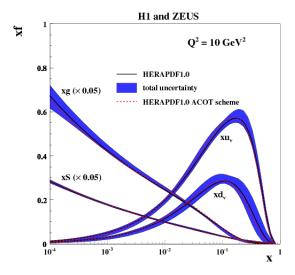


Fig. 4 Summary plots of valence, total sea (scaled) and gluon (scaled)densities with their total model uncertainties at the scale of $Q^2 = 10~{\rm Gev}^2$ obatined using ACOT scheme with k-factor method (red) compared to the HERAPDF1.0 PDF set at NLO using RT scheme.

culations to be performed within the phase space corresponding to the available measurement.

The calculated leading order cross sections are multiplied by k-factors to obtain predictions at NLO. ³⁹⁴ This method was used by the ATLAS collaboration ³⁹⁵ in determining the strange quark density of the proton from W and Z cross sections [33]. An illustration ³⁹⁷ of ATLAS PDF extracted using k-factor method ³⁹⁸ is illustrated in Fig. 5, shown in comparison with ³⁹⁹ global PDF sets such as CT10[19] and NNPDF2.3[20]^{4,00}

Fast Grid Techniques:

- The APPLGRID [15] package allows the fast com- 403 putation of NLO cross sections for particular pro- 404 cesses for arbitrary sets of proton parton distribution 405 functions. The package implements calculations of 406 DY production as well as jet production in $pp(\bar{p})$ 407 collisions and DIS processes. The approach is based on storing the perturbative 409 coefficients of NLO QCD calculations of final-state 410 observables measured in hadron colliders in look-up 411 tables. The PDFs and the strong couplings are in- 412 cluded during the final calculations, e.g. during PDF 413 fitting. The method allows variation of factorization 414 and renormalization scales in calculations. The look-up tables (grids) can be generated with mod-416 ified versions of the MCFM parton level generator 417 for DY [11–13] or NLOjet++ [7, 8] code for NLO jet 418 production. The model input parameters are pre-set 419 as usual for MCFM, while binning and definitions 420

of the cross section observables are set in the AP- 421

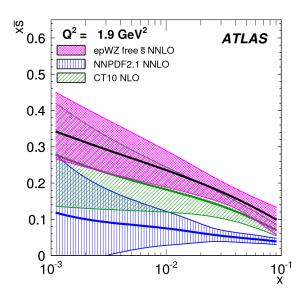


Fig. 5 The strange anti-quark density versus x for the ATLAS epWZ free sbar NNLO fit (magenta band) compared to predictions from NNPDF2.1 (blue hatched) and CT10 (green hatched) at $Q^2 = 1.9$ GeV².

PLGRID code. The grid parameters, Q^2 binning and interpolation orders are also defined in the code. APPLGRID constructs the grid tables in two steps: (i) exploration of the phase space in order to optimize the memory storage and (ii) actual grid construction in the phase space corresponding to the requested observables. The NLO cross sections are restored from the grids using externally provided PDFs, α_S , factorization and renormalization scales. For NNLO predictions k-factors can be applied.

- The FastNLO project [16–18] uses multi-dimensional interpolation techniques to convert the convolutions of perturbative coefficients with parton distribution functions and the strong coupling into simple products. The perturbative coefficients are calculated by the NLOJET++ program [8] where, in addition to the jet production processes available in MCFM, calculations for jet-production in DIS [58] are available as well as calculations for hadron-hadron collisions [7, 59] which include threshold-corrections at 𝒪(NNLO) for inclusive jet cross sections [60].

The fastNLO libraries are included in the HERAFitter package. In order to include a new measurement into the PDF fit, the fastNLO tables have to be specified. These tables include all necessary information about the perturbative coefficients and the calculated process for all bins of a certain dataset. The fastNLO tables were originally calculated for multiple factors of the factorization scale, and a renormalization scale factor could be chosen freely. More recently, some

of the fastNLO tables allow for the free choice [18] 464 of the renormalization and the factorization scale as a 465 function of two pre-defined observables. The evaluation of the strong coupling constant, which enters the cross section calculation, is taken consistently from the QCDNUM evolution code.

4 Fit Methodology

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There are considerable number of choices available when 467 performing a QCD fit analysis which require careful inves- 468 tigation (i.e. functional parametrisation form, heavy quarks 469 masses, alternative theoretical calculations, method of min- 470 imisation, interpretation of uncertaintes etc.). It is desirable 471 to be able to discriminate or quantify the effect of the chosen ansatz, ideally within a common framework and HERAFitter,73 is optimally designed for such tests. The methodology em- 474 ployed by HERAFitter relies on a flexible and modular 475 framework that allows for independent integration of the 476 state-of-the-art techniques, either related to the inclusion of 477 a new theoretical calculation, or to new approaches to treat uncertainties.

In this section we briefly describe the available options in HERAFitter ranging from the functional form used to parametrise PDFs and the choice of the form of the χ^2 function, to different methods to assess the experimental uncer- 478 tainties on extracted PDFs.

In addition, as an alternative approach to a complete QCD 480 fit, the reweighting method, which is also available in the 481 HERAFitter is described in this section. 482

4.1 Functional Forms for PDF parametrisation

The PDFs are parametrised at a starting scale which is chosen by the user. Various functional forms can be tested using free parameters to be extracted from the fit:

Standard Polynomials: The term standard is understood 490 to refer to a simple polynomial that interpolates between 491 the low and high x regions:

$$xf(x) = Ax^{B}(1-x)^{C}P_{i}(x),$$
 (6) 494

Standard forms are commonly used by PDF groups. The parametrised PDFs at HERA are the valence distributions xu_v and xd_v , the gluon distribution xg, and the u- 496 4.2 χ^2 representation type and d-type sea $x\bar{U}$, $x\bar{D}$, where $x\bar{U} = x\bar{u}$, $x\bar{D} = x\bar{d} + \bar{d}$

A for the valence and gluon distributions. The sum-rules can be evaluated analytically.

Log-Normal Distributions: A bi-log-normal distribution to parametrise the x dependence of the PDFs is also available in HERAFitter . This parametrisation is motivated by multiparticle statistics [29]. The following functional form can be used:

$$xf(x) = x^{p-b\log(x)}(1-x)^{q-\log(1-x)}.$$
 (7)

This function can be regarded as a generalisation of the standard functional form described above. In order to satisfy the QCD sum rules this parametric form requires numerical integration.

Chebyshev Polynomials:

A flexible Chebyshev polynomial based parametrisation can be used for the gluon and sea densities. The polynomials use $\log x$ as an argument to emphasize the low x behavior. The parametrisation is valid for $x > x_{min} =$ 1.7×10^{-5} . The PDFs are multiplied by 1 - x to ensure that they vanish as $x \to 1$. The resulting parametric form

$$xg(x) = A_g(1-x) \sum_{i=0}^{N_g-1} A_{g_i} T_i \left(-\frac{2\log x - \log x_{min}}{\log x_{min}} \right), (8)$$

$$xS(x) = (1-x) \sum_{i=0}^{N_S-1} A_{S_i} T_i \left(-\frac{2\log x - \log x_{min}}{\log x_{min}} \right).$$
 (9)

Here the sum over *i* runs up to $N_{g,S} = 15$ order Chebyshev polynomials of the first type T_i for the gluon, g, and sea-quark, S, density, respectively. The normalisation A_{ρ} is given by the momentum sum rule. The advantages of this parametrisation are that the momentum sum rule can be evaluated analytically and that for $N \ge 5$ the fit quality is already similar to the standard Regge-inspired parametrisation with a similar number of parameters.

External PDFs: HERAFitter also provides the possibility to access external PDF sets, which can be used to construct theoretical predictions for the various processes implemented in HERAFitter. This is possible via an interface to LHAPDF [30, 31] which provides access to the global PDF sets available at LO, NLO or NNLO evolved either locally through the HERAFitter or taken as provided by the LHAPDF grids. Figure 6 is produced with the drawing tools available in HERAFitter and illustrates the PDFs accessed from LHAPDF.

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 $x\bar{s}$. The $P_i(x)$ for the HERAPDF [32] style takes the sim- 497 The PDF parameters are extracted from a χ^2 minimization ple Regge-inpsired form $(1 + \varepsilon \sqrt{x} + Dx + Ex^2)$ with ad- 498 process. For experimental uncertainties there are various forms ditional constraints relating to the flavour decomposi- 499 to represent the χ^2 function, e.g. using a covariance mation of the light sea. For the CTEQ style, $P_i(x)$ takes the 500 trix or representing them by nuisance parameters. In addiform $e^{a_3x}(1+e^{a_4}x+e^{a_5}x^2)$. QCD number and momen- 501 tion, there are various methods to deal with correlated systum sum-rules are used to determine the normalisations 502 tematic (or statistical) uncertainties (e.g. different scaling

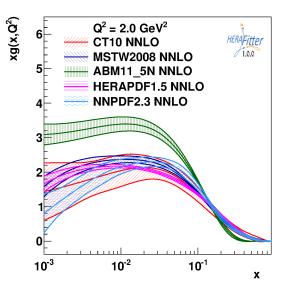


Fig. 6 Gluon density as extracted by various PDF groups at the scale of $Q^2=2~{\rm GeV^2}$, plotted using the drawing tools from HERAFitter .

options, etc.). Here we summarise the options available in HERAFitter .

Covariance Matrix Representation: For a data point μ_i with a corresponding theory prediction m_i , the χ^2 function for the case when experimental uncertainties are given as a covariance matrix $C_{i,j}$ over data bins i and j, can be expressed in the following form:

$$\chi^{2}(m) = \sum_{i,j} (m_{i} - \mu_{i}) C_{ij}^{-1}(m_{j} - \mu_{j}).$$
 (10)

The covariance matrix can be decomposed in statistical, uncorrelated and correlated systematic contributions:

$$C_{ij} = C_{ij}^{stat} + C_{ij}^{uncor} + C_{ij}^{sys}. \tag{11}$$

This representation can not single out the effect of a particular source of systematic uncertainty.

Nuisance Parameters Representation:

$$\chi^{2}(m,b) = \sum_{i} \frac{\left[m^{i} - \sum_{j} \gamma_{j}^{i} m^{i} b_{j} - \mu^{i}\right]^{2}}{\delta_{i,\text{stat}}^{2} \mu^{i} \left(m^{i} - \sum_{j} \gamma_{j}^{i} m^{i} b_{j}\right) + \left(\delta_{i,\text{uncor}} m^{i}\right)^{2}}$$

$$+ \sum_{i} b_{j}^{2}.$$
(12)

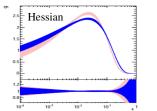
Here μ^i is the measured central value at a point i with 553 relative statistical $\delta_{i,stat}$ and relative uncorrelated systematic uncertainty $\delta_{i,unc}$. Further, γ^i_j quantifies the sensitivity of the measurement μ^i at the point i to the correlated systematic source j. The function χ^2 depends in 357 addition on the set of systematic nuisance parameters b_j . 558 This definition of the χ^2 function assumes that systemsatic uncertainties are proportional to the central prediction values (multiplicative errors), whereas the statistical 561

errors scale with the square root of the expected number of events.

Mixed Form: It can happen that various parts of the systematic and statistical uncertainties are stored in different forms. A situation can be envisaged when the correlated systematic experimental uncertainties are provided as nuisance parameters, but the statistical bin-to-bin correlations are given in the form of a covariance matrix. HERAFitter offers the possibility to include such information, when provided, as well as any other mixed form of treating statistical, uncorrelated and correlated systematic uncertainties.

4.3 Treatment of the Experimental Uncertainties

HERAFitter provides three methods for assessing the experimental uncertainties on PDFs: the Hessian, Offset, and Monte Carlo methods, which are described below. Figure 7 illustrates the difference between the Hessian and Monte-Carlo methods both of which can be applied and plotted with HERAFitter.



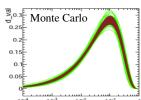


Fig. 7 Differences in the experimental uncertainties on the gluon (left) and d-valence quark (right) densities extracted through different methods in HERAFitter: Hessian(left) versus Monte Carlo (right).

Hessian method: The technique developed by [61] presents an estimate of PDF uncertainties reflecting the experimental precision of data used in the QCD fit by examining the behaviour of χ^2 with the nuisance parameter representation (see section 4.2) in the neighborhood of the minimum. The systematic shift nuisance parameters b_j (Eq. 12) as well as the PDF parameters are free parameters of the fit. Thus the fit determines the best fit to the data taking into account correlated systematic shifts of the data. This is known as Hessian or error matrix method. The Hessian matrix is build by the second derivatives of χ^2 at the minimum. The PDF eigenvectors are obtained through an iterative procedure used to diagonalise the Hessian matrix and rescale the eigenvectors to adapt the step sizes to their natural scale.

Offset method:

There is another method to propagate the correlated systematic experimental uncertainties from the measurements to PDFs [62], which has the practical advantage that

covariance matrix. It uses also the χ^2 function for the 610 eigenvectors provided by most PDF groups. central fit for which only uncorrelated uncertainties are 611 resulting deviations of each of these fits from the central 621 random fluctuations around the central PDF set. PDF parameters are added in quadrature.

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In most cases, the uncertainties estimated through the offset method are larger than those from the Hessian method, as the offset method does not use the information on correlated systematic uncertainties optimally.

Monte Carlo method: The PDF uncertainties can be estimated using a Monte Carlo technique [63, 64]. The method consists in preparing replicas of data sets by allowing the central values of the cross sections to fluctuate within their systematic and statistical uncertainties taking into account all point-to-point correlations. The preparation of the data is repeated for a large N > 100times) and for each of these replicas a NLO QCD fit is performed to extract the PDF set. The PDF central values and uncertainties are estimated using the mean values and RMS over the replicas.

4.4 Treatment of the Theoretical Input Parameters

The results of a QCD fit depends not only on the input data but also on the input theoretical ansatz, which is also uncertain. Nowadays, modern PDFs try to address the impact of the choices of theoretical parameters by providing alternative PDFs with different choices of the mass of charm m_c , mass of the bottom quarks m_b and the value of $\alpha_S(M_Z)$, etc. (633) The above mentioned features make HERAFitter a powerfor the PDFs at the starting scale and indeed the value of the 635 starting scale itself. HERAFitter provides a platform in framework.

4.5 Reweighting Techniques

method (Bayesian Reweighting) is available in the HERAFitter tions, fast evolution kernels, and usage of the openMP (Open Because no fit is performed, the method provides a fast esti- 645 Multi-Processing) interface which allows parallel applicamate of the impact of new data. It was originally developed 646 tions of some of the heavy flavour scheme theory predictions by the NNPDF collaboration [65, 66] and later extended [67] 647 in DIS.

does not require the inversion of a large measurement 600 to work not only on the NNPDF replicas, but also on the

The Bayesian Reweighting technique uses the PDF probtaken into account to get the best PDF parameters. The 612 ability distributions which are modified with weights to acgoodness of fit can no longer be judged from the χ^2 since 613 count for the difference between theory prediction and new correlated uncertainties are ignored. The correlated sys- 614 data. In the NNPDF method the PDFs are constructed as tematic uncertainties of the data are then used to esti- $_{615}$ ensembles of N_{rep} parton distribution functions and observmate the errors on the PDF parameters as follows. The $_{616}$ ables $\mathcal{O}(PDF)$ are conventionally calculated from the avercross section is varied by one sigma shift from the cen- $_{617}$ age of the predictions obtained from the ensemble $\langle \mathcal{O}(\text{PDF}) \rangle =$ tral value for each systematic source and the fit is per- $_{618}$ $\frac{1}{N_{\text{rep}}} \sum_{k=1}^{N_{\text{rep}}} \mathcal{O}(\text{PDF}_k)$. In the case of PDF uncertainties proformed. This is done for both postive and negative one $_{619}$ vided by standard Hessian eigenvector error sets, this can be sigma shifts. After this has been done for all sources the $\frac{1}{620}$ achieved by creating the k-th random replica by introducing

> As a next step, the initial PDF probability distributions are updated by applying weights w_k , calculated as:

$$w_k = \frac{(\chi_k^2)^{\frac{1}{2}(N_{\text{data}} - 1)} \exp^{-\frac{1}{2}\chi_k^2}}{\frac{1}{N_{\text{rep}}} \sum_{k=1}^{N_{\text{rep}}} (\chi_k^2)^{\frac{1}{2}(N_{\text{data}} - 1)} \exp^{-\frac{1}{2}\chi_k^2}},$$
(13)

where $N_{\rm data}$ is the number of new data points, k denotes the specific replica for which the weight is calculated and χ_k^2 is a difference between a given data point y_i and its theoretical prediction obtained with the k-th PDF replica:

$$\chi^{2}(y, PDF_{k}) = \sum_{i,j=0}^{N_{\text{data}}} (y_{i} - y_{i}(PDF_{k})) \sigma_{ij}^{-1}(y_{j} - y_{j}(PDF_{k}))$$
(14)

The new, reweighted PDFs commonly are chosen to be based upon a smaller number of PDF sets compared to the input because replicas that are incompatible with the data are discarded in order to create a more stream-lined PDF set.

4.6 Performance Optimisation

Another important input is the choice of the functional form 634 ful project that encapsulates state of the art developments to debates on reaching the ultimate experimental precision.

An important factor for a feasible QCD fit which is perwhich such choices can readily be varied within a common $_{637}$ formed by iterative χ^2 minimisation, is performance in terms 638 of how long a calculation takes for each given data point. The performance of the HERAFitter code is greatly im-640 proved with several special built-in options including the k-factor techniques (see section 3) and the grid techniques 642 for the fast calculation of cross sections of particular pro-As an alternative to a complete QCD fit, the reweighting 643 cesses for arbitrary sets of PDFs. There are also cache op-

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5 Alternative to DGLAP formalisms

Different approaches that are alternative to the DGLAP formalism can be used to analyse DIS data in HERAFitter . These include several different dipole models and the use of transverse momentum dependent, or unintegrated PDFs, 691 uPDFs. These approaches are discussed below.

5.1 DIPOLE models

The dipole picture provides an alternative approach to virtual photon-proton scattering at low x which allows the description of both inclusive and diffractive processes. In this approach, the virtual photon fluctuates into a $q\bar{q}$ (or $q\bar{q}g$) dipole which interacts with the proton [68]. The dipoles can be viewed as quasi-stable quantum mechanical states, which have very long life time $\propto 1/m_p x$ and a size which is not changed by scattering. The dynamics of the interaction are embedded in the dipole scattering amplitude.

Several dipole models which assume different behavior of the dipole-proton cross sections are implemented in HERAFitter: the Golec-Biernat-Wüsthoff (GBW) dipole saturation model [69], the colour glass condensate approach to the high parton density regime called the Iancu-Itakura-Munier (IIM) dipole model [70] and a modified GBW model which takes into account the effects of DGLAP evolution called the Bartels-Golec-Kowalski (BGK) dipole model [71].

GBW model: In the GBW model the dipole-proton cross section $\sigma_{\rm dip}$ is given by

$$\sigma_{\text{dip}}(x, r^2) = \sigma_0 \left(1 - \exp\left[-\frac{r^2}{4R_0^2(x)} \right] \right), \tag{15}$$

here r corresponds to the transverse separation between the quark and the antiquark, and R_0^2 is an x-dependent scale parameter which represents the spacing of the gluons in the proton. $R_0^2(x) = (x/x_0)^{\lambda}$ is called the saturation radius. The fitted parameters are the cross-section normalisation σ_0 and x_0 and λ . This model gives exact Bjorken scaling when the dipole size r is small.

IIM model: The IIM model assumes an improved expression for the dipole cross section which is based on the Balitsky-Kovchegov equation [72]. The explicit formula for σ_{dip} can be found in [70]. The fitted parameters are an alternative scale parameter \tilde{R} , x_0 and λ .

BGK model: The BGK model modifies the GBW model by taking into account the DGLAP evolution of the gluon density. The dipole cross section is given by

$$\sigma_{\rm dip}(x, r^2) = \sigma_0 \left(1 - \exp\left[-\frac{\pi^2 r^2 \alpha_{\rm s}(\mu^2) x g(x, \mu^2)}{3\sigma_0} \right] \right).$$
 (16) 715

that the spacing R_0 is inverse to the gluon density. The gluon density parametrized at some starting scale Q_0^2 by $xg(x) = A_g x^{-\lambda_g} (1-x)^{C_g}$ is evolved to larger scales using LO or NLO DGLAP evolution. The fitted parameters for this model are σ_0 , μ_0^2 and three parameters for the gluon density: A_g , λ_g , C_g . The parameter C_{bgk} is kept fixed: $C_{bgk} = 4.0.$

BGK model with valence quarks:

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The dipole models are valid in the low-x region only, where the valence quark contribution is small, of the order of 5%. The new HERA F_2 data have a precision which is better than 2 %. Therefore, in HERAFitter the contribution of the valence quarks is taken from the PDF fits and added to the original BGK model, this is uniquely possible within the HERAFitter framework.

5.2 Transverse Momentum Dependent (unintegrated) PDFs with CCFM

Here another alternative approach to collinear DGLAP evolution is presented. In high energy factorization [73] the measured cross section is written as a convolution of the partonic cross section $\hat{\sigma}(k_t)$, which depends on the transverse momentum k_t of the incoming parton, with the k_t -dependent parton distribution function $\mathcal{A}(x, k_t, p)$ (transverse momentum dependent (TMD) or unintegrated uPDF):

$$\sigma = \int \frac{dz}{z} d^2k_t \hat{\sigma}(\frac{x}{z}, k_t) \tilde{\mathscr{A}}(x, k_t, p)$$
 (17)

would probably be good to explain how the unintegrated 704 relates to the integrated here Generally, the evolution of 705 $\tilde{\mathscr{A}}(x,k_t,p)$ can proceed via the BFKL**you need a BFKL** reference, DGLAP or via the CCFM evolution equations. 707 In HERAFitter an extension of the CCFM [74-77] evo-108 lution has been implemented. Since the evolution cannot be easily obtained in a closed form, first a kernel $\tilde{\mathscr{A}}(x'',k_t,p)$ is determined from the MC solution of the CCFM evolution equation, and is then folded with a non-perturbative starting distribution $\mathcal{A}_0(x)$ [78]:

$$x\mathscr{A}(x,k_{t},p) = x \int dx' \int dx'' \mathscr{A}_{0}(x) \widetilde{\mathscr{A}}(x'',k_{t},p) \,\delta(x' \cdot x'' - x)$$

$$= \int dx' \int dx'' \mathscr{A}_{0}(x) \widetilde{\mathscr{A}}(x'',k_{t},p) \,\frac{x}{x'} \delta(x'' - \frac{x}{x'})$$

$$= \int dx' \mathscr{A}_{0}(x') \cdot \frac{x}{x'} \widetilde{\mathscr{A}}(\frac{x}{x'},k_{t},p). \tag{18}$$

The kernel $\tilde{\mathscr{A}}$ includes all the dynamics of the evolution, Sudakov form factors and splitting functions and is determined in a grid of $50 \otimes 50 \otimes 50$ bins in x, k_t, p .

The calculation of the cross section according to Eq.(17)The factorization scale μ^2 has the form $\mu^2 = C_{bgk}/r^2 + \pi \pi$ involves a multidimensional Monte Carlo integration which μ_0^2 . This model relates to the GBW model using the idea 718 is time consuming and suffers from numerical fluctuations,

(22)

and therefore cannot be used directly in a fit procedure. In-⁷²⁰ stead the following procedure is applied:

$$\sigma_r(x, Q^2) = \int_x^1 dx_g \mathscr{A}(x_g, k_t, p) \hat{\sigma}(x, x_g, Q^2)$$

$$= \int_x^1 dx' \mathscr{A}_0(x') \cdot \tilde{\sigma}(x/x', Q^2). \tag{19}$$

The kernel $\tilde{\mathscr{A}}$ has to be provided separately and is not 760 calculable within the program. A starting distribution \mathcal{A}_0 , at 761 the starting scale Q_0 , of the following form is used:

$$x\mathcal{A}_0(x, k_t) = Nx^{-B_g} \cdot (1 - x)^{C_g} (1 - D_g x)$$
(20)

with free parameters N, B_g, C_g, D_g .

The calculation of the ep cross section follows eq.(17), 764 6 Application of HERAFitter with the off-shell matrix element including quark masses taken from [73] in its implementation in CASCADE [79]. In 765 HERAFitter has been successfully integrated in the high addition to the boson gluon fusion process, valence quark 766 energy community as a much needed means to provide uninitiated $\gamma q o q$ processes are included, with the valence 767 derstanding and interpretation of new measurements in the quarks taken from [80].

5.3 Diffractive PDFs

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(DPDFs) can be derived from QCD fits to diffractive cross 774 perimental and theoretical uncertainties. The results are also sections. At HERA about 10% of deep inelastic interactions 775 output to PDF grids that can be used to study predictions for are diffractive leading to events in which the interacting pro- 776 SM or beyond SM processes, as well as for the study of the ton stays intact $(ep \rightarrow eXp)$. In the diffractive process the $_{777}$ impact of future collider measurements (using pseudo-data). proton appears well separated from the rest of the hadronic 778 than W and the same net quantum numbers as the exchanged $_{782}$ PDF sets [82]). photon. For such processes, the proton vertex factorisation 783 approach is assumed where diffractive DIS is mediated by 784 platform include the follwing SM processes studied at the the exchange of hard Pomeron or a secondary Reggeon. The 785 LHC: inclusive Drell-Yan and Wand Z production [33, 35, factorisable pomeron picture has proved remarkably suc- 786 36]; inclusive jets [34, 37] production. At HERA, the recessful in the description of most of these data.

sider the squared four-momentum transfer t (the undetected ₇₈₉ nation of charm production measurements in DIS [39]. The momentum transfer to the proton system) and the mass $M_{X_{790}}$ HERAFitter framework also provides an unique possibilof the diffractively produced final state. In practice, the vari- $_{791}$ ity to make impact studies for future colliders as illustrated able M_X is often replaced by $\beta = \frac{Q^2}{M_X^2 + Q^2 - t}$. In models based $_{792}$ by the QCD studies that have been performed to explore the on a factorisable Pomeron, β may be viewed as the fraction 793 potential of the LHeC data [83]. of the pomeron longitudinal momentum which is carried by 794 the struck parton, $x = \beta x_{IP}$.

For the inclusive case, the diffractive cross-section can be expressed as:

$$\frac{d\sigma}{d\beta \, dO^2 dx_{IP} \, dt} = \frac{2\pi\alpha^2}{\beta \, Q^4} \, \left(1 + (1 - y)^2 \right) \overline{\sigma}^{D(4)}(\beta, Q^2, x_{IP}, t) \quad (21)$$

where the "reduced cross-section", $\overline{\sigma}$, is defined as

$$\overline{\sigma}^{D(4)} = F_2^{D(4)} - \tfrac{y^2}{1+(1-y)^2} \, F_L^{D(4)} = F_T^{D(4)} + \tfrac{2(1-y)}{1+(1-y)^2} \, F_L^{D(4)}.$$

With $x = x_{IP}\beta$ we can relate this to the standard DIS formula. The diffractive structure functions can be expressed as convolutions of the calculable coefficient functions with diffractive quark and gluon distribution functions, which in general depend on all of x_{IP} , Q^2 , β , t.

The diffractive PDFs in HERAFitter are implemented following the prescription of ZEUS publication [81] and can ⁷⁶³ be used to reproduce the main results.

768 context of QCD theory, a field limited by the precision of 769 the PDFs. The HERAFitter platform not only allows the extraction of PDFs but also of theory parameters such as 771 the strong coupling and heavy quark masses. The parameters and distributions are outut with a quantitative asssess-Similarly to standard DIS, diffractive parton distributions 773 ment of the fit quality with fully detailed information on ex-

So far the HERAFitter platform has been used to profinal state by a large rapidity gap and this is interpreted as 779 duce grids from the QCD analyses performed at HERA (HERthe diffractive dissociation of the exchanged virtual photon 780 APDF series [32]), and their extension to the LHC using to produce a hadronic system X with mass much smaller 781 measurements from ATLAS [33, 34] (the first ever ATLAS

New results that have been based on the HERAFitter 787 sults of QCD analyses using HERAFitter are published In addition to the usual variables x, Q^2 , one must con- $_{788}$ for inclusive H1 measurements [38] and the recent combi-

> this section reads a bit like it could be married with 795 the summary

796 7 Summary

797 The HERAFitter project is a unique platform for QCD analyses to study the structure of the proton. It incorporates 799 not only the crucial data on Deep Inelastic Scattering from 800 HERA but also data from the hadron colliders which are date theory calculations are available for each process at LO, 852 NLO and NNLO when possible. HERAFitter has flexible 853 modular structure and contains many different useful tools 854 for PDF interpretation. HERAFitter is the first open source platform which is optimal for benchmarking studies.

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