

Optical Pumping of Rb^{85} and Rb^{87}

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Abstract

Optical Pumping is a spectroscopical method that was developed in the 1950's and has been a very accurate method to determine spectroscopical properties of certain materials. In this experiment the following were determined: the individual g-factors, nuclear spins, cross sectional area and ratio of the periods. For Rb^{85} the g-factor and nuclear spin were found to be: 0.3260 ± 0.0005 and 2.571 respectively. For Rb^{87} they were found to be: 0.482 ± 0.001 and 1.576 respectively. The cross-sectional area and ratio of the periods were found to be: $1.8 \times 10^{-16} \pm 0.3 \times 10^{-16}$ and 1.44 ± 0.05 respectively.

I Introduction

Optical Pumping is a spectroscopical method developed in 1950 by Alfred Kastler, whom received the Nobel Prize in physics in 1966 for his discovery. This method is one in which photons are utilized to create population differences of electronic excited and ground states. So the meaning and general concept is in the name itself.

Under standard conditions the population difference required to carry out experiments is not possible because from statistical mechanics at thermal equilibrium we have an equal number of electrons that rise and fall from excitation levels. Due to this, they tend to cancel each others effects and no net population differences can be detected. This is also the basis of lasers where, a population difference needs to be created so that photons can be spontaneously emitted by the lasing medium.

For this experiment the equipment that is being used is provided by TeachSpin and consists of an Radio Frequency (RF) discharge lamp, Interference Filter, Polarizers, Quarter Wave plate, absorption cell, optical detector, three sets of magnetic coils in a Helmholtz configuration and a RF magnetic coil. The sample is a Rubidium glass bulb that contains neon gas with a pressure of approximately 0.04 atm pressure. The presence of the neon gas is important as its spherical symmetry will reduce the interactions between the Rubidium atoms and the outside environment. They will act as a buffer gas.

Optical Pumping is a process in which has had much applicability in solid state and liquid state physics. However, we will only be dealing with a gas since at the solid and liquid phases the interactions between the neighboring atoms increases thus broadening the energy levels [1].

II Theory

(i) Structure of alkali atoms

In the experiment described in this paper we will be studying the absorption and emission from Rubidium isotopes (85 and 87) which are alkali atoms. As such the electronic structure of Rubidium is as such,

$$1s^2 2s^2 2p^6 3s^2 3p^6 3d^1 4s^2 4p^6 5s$$

Where we can show the shorthand version as,

$$[Kr]5s$$



Figure 3: *Coupling of angular momentum in an electron [3].*

Where, the superscripts show the number of electrons contained in each of the electronic shells. Since the only valence electron is in the 5s shell we can consider the atom to be consisting of only one electron. This electron much like with other electrons can be described by means of the total angular momentum of the electron \vec{J} where it is made up of components \vec{S} and \vec{L} . Which, represent the spin angular momentum and orbital angular momentum respectively. The vectors are shown on figure 3

Since, these components are vectors we can represent the total angular momentum as such,

$$\vec{J} = \vec{S} + \vec{L} \quad (1)$$

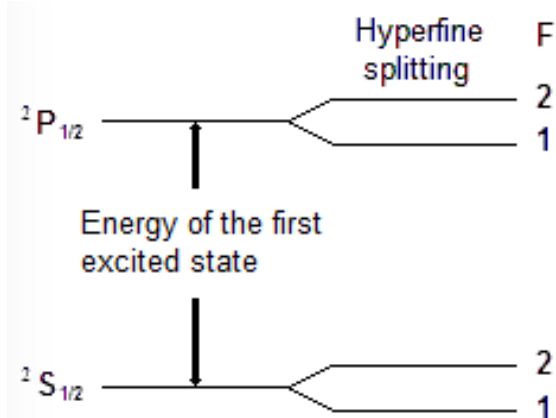


Figure 1: *Hyperfine splitting energy diagram for $I = 3/2$ particle [3]*

Where, for an alkali atom in the ground state the value of \vec{L} is zero from the quantum numbers associated with the orbital shell and the value of \vec{S} will be $1/2$. So, this gives rise to a total angular momentum of $1/2$.

As it will later become apparent, we will display some of the energy levels in the notation $^{2s+1}L_J$. Where, all of the values are those taken from equation 1. To represent the ground state of an alkali atom we can write it with the formatting $^2S_{1/2}$. Since the value of \vec{L} is zero by convention we write it as the letter S. Where it to be 1 we would write in P and so on.

If the electron were to be in a P state it would be able to have an angular momentum of $\vec{L} \pm \vec{S}$ and would take on the representations $^2P_{1/2}$ and $^2P_{3/2}$. Due to the difference in angular momentum the energy levels would have different energies. This arises due to the spin-orbit coupling of the angular momentum vectors [4].

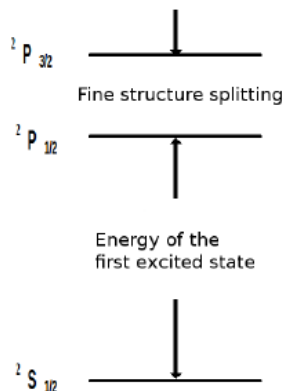


Figure 4: *Pictorial representation of the energy difference in the fine structure. Not to scale [3].*

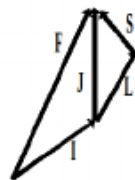


Figure 2: *Hyperfine coupling in an alkali atom [3]*

So far, we have been ignoring the effects of the nucleus to make the theory easier. However, this will not go on any longer. We will now consider the hyperfine splitting of the electron angular momenta. This arises from the spin-spin coupling where for the fine structure we had the spin-orbit coupling. The spin-spin coupling is due to the magnetic dipole moment of both the proton and electron. Now, it should be noted, that the magnetic dipole moment of the proton is much smaller than that compared to the electron. The dipole momenta can be given as the following.

$$\vec{\mu}_p = \frac{g_p e}{2m_p} \vec{S}_p \quad \vec{\mu}_e = -\frac{e}{m_e} \vec{S}_e [4] \quad (2)$$

Where, the p and e represent the proton and electron values respectively, g_p and g_e are the respective g-factors of value 5.59 and 2.00 and \vec{S} represents the respective angular spin. Using derivations outlined in reference [4] we can get to an expression for the difference in energy of the two states with different angular momenta. The equation is as such.

$$\Delta E = \frac{4g_p \hbar}{3m_p m_e^2 c^2 r^4} [4] \quad (3)$$

Where, c is the speed of light and r is the radius of the atom. In the reference they are making an example to a hydrogen atom with r equal to a (Bohr's atomic radius). This derivation can still be generalized to our use as we are dealing with an atom that can be approximated to be one that is like a hydrogen atom. Where we can also make the relation with the frequency as such.

$$\nu = \frac{\Delta E}{h} [4] \quad (4)$$

Where the Hamiltonian is as such.

$$H = h\vec{I} \cdot \vec{J} [3] \quad (5)$$

Usually the energy difference between these two levels is very small and one can cause transitions in the hyperfine structure with an RF wave. A pictorial representation of the coupling of the magnetic dipole moment spins is shown on figure 2. Where a rough energy separation schematic is given in figure 1. As is clearly seen the energy that is required to jump from one energy level to the next is much greater than that required to make the transition in the hyperfine structure. Later we will discuss the implications of this with respect to optical pumping.

However next we will show another form of splitting where all of the degenerate energy levels of the electronic energy level diagram are split.

(ii) Interaction of an alkali atom with a magnetic field

This interaction is better known as the Zeeman effect and the general premise behind this effect is that by applying a magnetic field to an atom we can further split the degenerate energy levels according to their angular momenta.

In the Zeeman effect there are three main regions that are to be considered: weak field, intermediate and Strong field effects. For the purposes of this experiment we will only deal with the weak field effect as the strong field can require magnetic fields around 10T which is only achievable with extremely expensive equipment.

The Zeeman effect is an effect which can break the spin-orbit coupling of an electron creating a difference in energy between the different orbitals of an atom. The weak field Zeeman effect is named as such because the energy splitting from the Zeeman effect is very small comparatively and as such the Hyperfine splittings dominate with the Zeeman effect becoming the perturbation [4]. The hamiltonian of this effect is as shown.

$$H = h\vec{I} \cdot \vec{J} - \frac{\mu_J}{J} \vec{J} \cdot \vec{B} - \frac{\mu_I}{I} \vec{I} \cdot \vec{B} [3] \quad (6)$$

Where, μ_J is the electronic dipole moment and μ_I is the nuclear magnetic dipole moment.

Figure 5 shows the energy levels from the weak field Zeeman effect. The energy levels are splitting into $2F + 1$ levels. Where F is the angular momentum of the atom, M is the projection of F onto the direction of the magnetic field. In figure 3 we show two levels for the ground state and the first excited

state. For this experiment we are only considering the first excited state $^2P_{1/2}$. The reason why we only consider this and not the $^2P_{3/2}$ is because at \vec{J} values of 1/2 we can calculate the energy levels in closed form from quantum mechanics with the Breit-Rabi equation.

Since the electron can be considered to be a moving charge with charge 1.6×10^{-19} Coulombs. This magnetic dipole moment has a value that is equal to the Bohr Magnetron, μ_B . Ignoring the effects of the nucleus we can then represent the magnetic energy as [3].

$$U = \frac{M(\vec{L} + 2\vec{S}) \cdot \vec{J}}{J^2} \mu_B B = g_J \mu_B M B [3] \quad (7)$$

Where, g_J is the Lande g-factor which describes the change in the magnetic moment of an electron bound in an atom, B is the magnetic field and M is the atomic spin component along the magnetic field direction. The g-factor is given by,

$$g_J = \frac{(\vec{L} + 2\vec{S}) \cdot \vec{J}}{J^2} \quad (8)$$

$$g_J = 1 + \frac{J(J+1) + S(S+1) - L(L+1)}{2J(J+1)} [3]$$

To show the interaction energy of an electron we simply need to add a negative sign to equation 7 from the negative charge of the electron. In the case of rubidium where we have a J and S value of 1/2 we find that the g-factor is equal to 2.00232 [3].

Now, if we were to include the interaction of the nucleus to find the interaction energy the equation could be represented as follows.

$$U = -g_F \mu_B M B [3] \quad (9)$$

Where, g_F can be shown to be the following.

$$g_F = g_J \frac{F(F+1) + J(J+1) - I(I-1)}{2F(F+1)} [3] \quad (10)$$

Where, F represents the total angular momentum of the atom, I is the total nuclear spin angular momentum and J is the total electronic angular momentum. This quantity is highly dependent on the atom that is being used and as such there is no one set value as with the Lande g-factor.

Where we can then show the transition frequency as.

$$\nu = \frac{g_F \mu_B B}{h} [3] \quad (11)$$

The above equations are only applicable when the interaction energy with the magnetic field is very

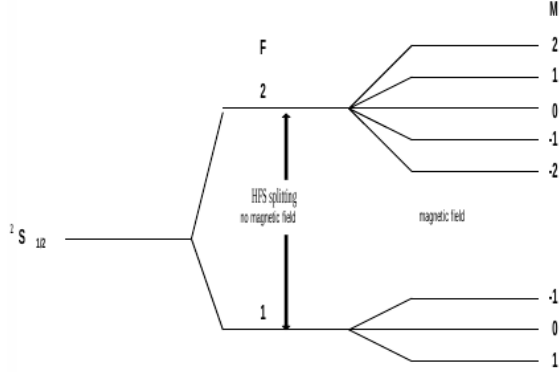


Figure 5: Energy levels of an alkali atom of the $2S_{1/2}$ state in a weak magnetic field [3]

small and depends linearly. If the dependence is quadratic, which will be studied in this experiment, we must apply the Breit-Rabi equation which can be derived by diagonalizing the Hamiltonian in equation 6 [3]. The result of such is the following.

$$W(F, M) = -\frac{\Delta W}{2(2I+1)} - \frac{\mu_I}{I} MB \pm \dots$$

$$\frac{\Delta W}{2} \left[1 + \frac{4M}{2I+1} x + x^2 \right]^{1/2} [3] \quad (12)$$

Where,

$$x = (g_J - g_I) \frac{\mu_B B}{\Delta W} [3] \quad (13)$$

$$g_I = -\frac{\mu_I}{I\mu_B} [3] \quad (14)$$

Where, W is the interaction energy and ΔW is the hyperfine splitting energy.

Figure 7 shows a plot of the Breit-Rabi equation. The three Zeeman levels for the magnetic field are as follows. Weak field is at an x value close to zero where the energy splitting varies linearly and the hyperfine interaction dominates where the Zeeman effect is the perturbation. The strong field region, also known as the Paschen-Back region is x values greater than 2 where the energy levels are linear once again and depends on the Zeeman effect where the hyperfine splitting is taken as the perturbation. The final region is the intermediate field region at values greater than zero but less than 2. In this region both the hyperfine splitting and the Zeeman effect contribute equally to the energy splitting of the electronic orbitals [4].

In this experiment we are only concerned with the weak field Zeeman effect.

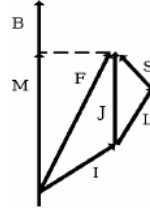


Figure 6: Zeeman effect in an alkali atom [3]

(iii) Photon absorption in an alkali atom

The lowest electronic state along with the first two excited states of the valence electron for a rubidium atom are the following: $2S_{1/2}$, $2P_{1/2}$ and $2P_{3/2}$. Where, we will mainly deal with the ground state and the first excited state for simplicity.

The transitions from the ground state to the excited state are governed by selection rules that are as follows: $\Delta L = 0, \pm 1$, $\Delta S = 0$ and $\Delta J = 0, \pm 1$. However, the value of L cannot go from 0 to 0 [3]. For this experiment we are interested in the amount of light that is absorbed or transmitted by the rubidium atoms in a given volume. For this purpose it can be useful to use the concept of a cross section of the atoms. In the limit of low density this can be represented as.

$$n = n_0 e^{-\sigma \rho l} [3] \quad (15)$$

Where, n and n_0 are the incoming and outgoing flux of electrons and ρ is the density of the gas.

A similar concept can be employed when talking about a flux of photons.

$$I = I_0 e^{-\sigma_0 \rho l} [3] \quad (16)$$

Where the cross section in this equation is actually the cross section at the resonance condition which is much lower than the expected value.

Now we must append to our selection rules for transitions to account for the selection rules for the hyperfine splitting which will add that $\Delta F = 0, \pm 1$. Additional splitting caused by the magnetic field adds that $\Delta M = 0, \pm 1$.

The selection rule for M can be somewhat different, because since angular momentum must always be conserved the absorption of light must be circularly

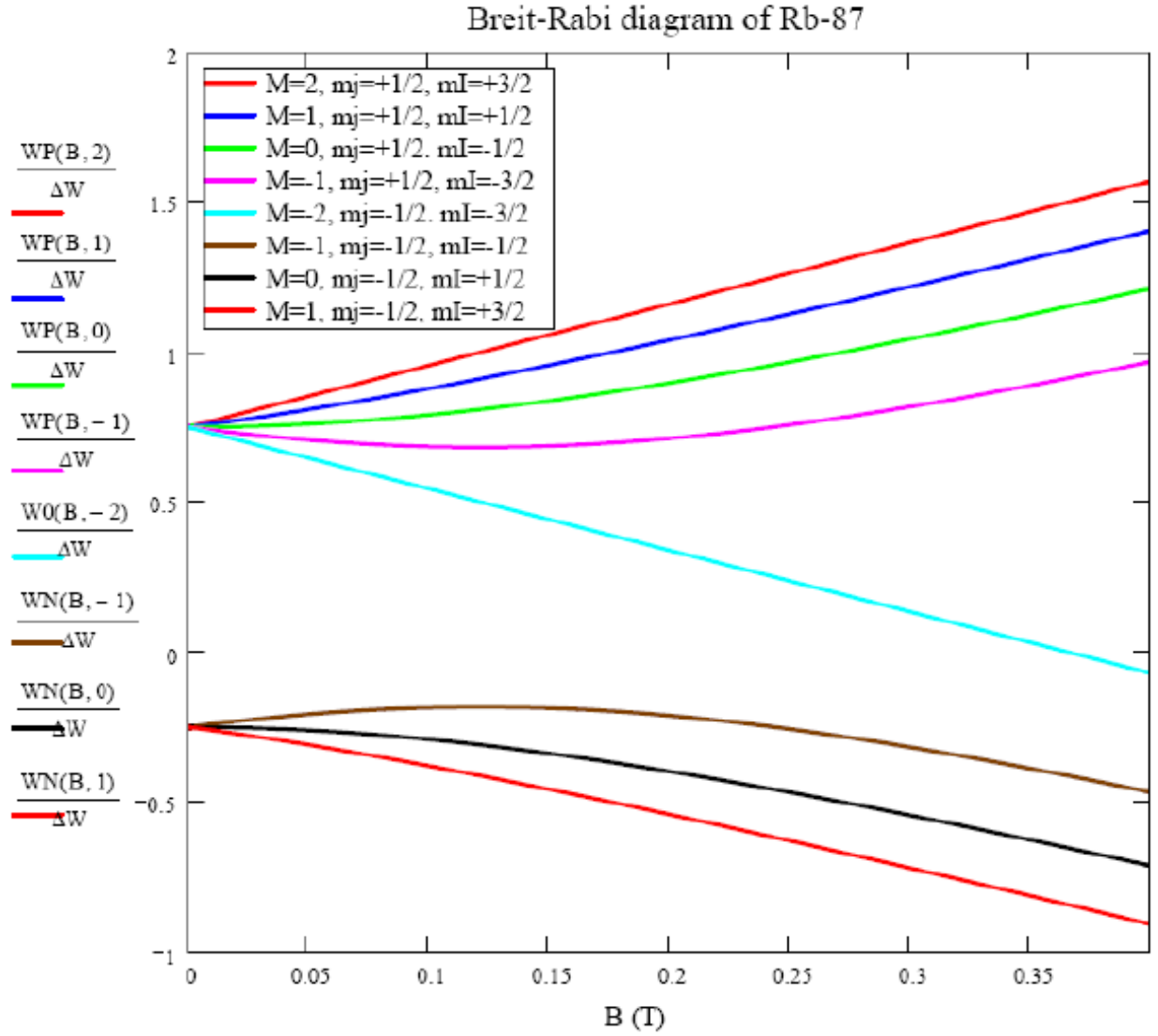


Figure 7: Breit-Rabi diagram of Rb^{87} in a magnetic field [3].

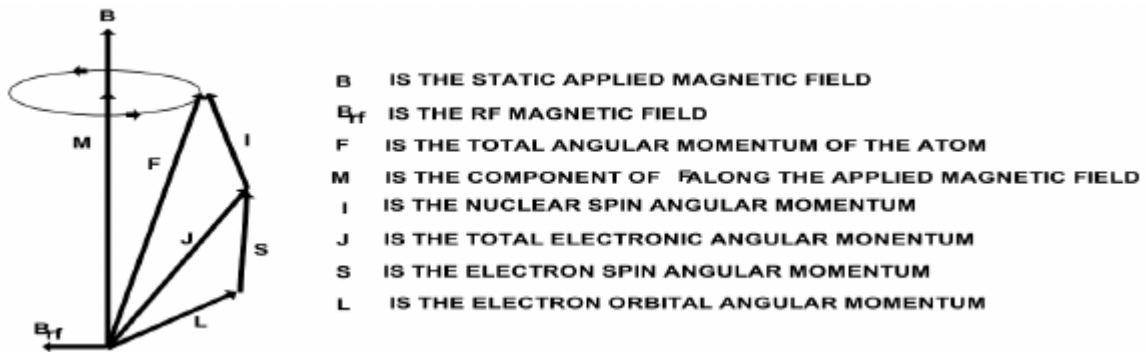


Figure 8: Magnetic fields and angular momenta involved in the experiment [3].

polarized. Of course, if light is circularly polarized we will be adding to the angular momentum. The question then becomes how does it change depending on the polarization.

It has already been established that only circularly polarized will change the angular momentum of the atom. So, depending on the polarization we will get addition or subtraction to the angular momentum. That is to say that we will have either a +1 or a -1 to the angular momentum, never both.

The lifetime of the transitions will be determined by collision processes. It is mentioned that the rubidium glass bulb is filled with a buffer gas that is there to decrease the collisions of the atoms with the walls of the container and lose its angular momentum. The neon gas disallows this from happening and since it is a very symmetric atom it will not contribute much to the decrease of the angular momentum of the atom [1].

(iv) Optical pumping in rubidium

In optical pumping we are trying to create a net population difference in one state relative to another. From statistical mechanics we know that electronic states can settle into a thermal equilibrium where there is no net population difference on one state. By making use of the hyperfine splitting and the Zeeman effect along with some clever applications of the incoming photons we can achieve this.

On figure 10 we see the types of transitions that are possible. On the left side of the figure we see that there is a large separation between the energy levels that corresponds to a transition energy of a 795 nm photon. Then there are smaller gaps that come from the hyperfine splitting and then the Zeeman levels.

In order to create this 795 nm photon an RF discharge lamp is used to create circularly polarized light at that wavelength. The RF discharge lamp along with a general schematic of the experiment is shown on figure 9. Inside the RF discharge there is some Rb^{87} gas along with some metal. When a current is passed through the gas it induces a transition to populate the first two excited states. By spontaneous emission it then emits two photons, one at 795 nm and one at 780 nm. We are only interested in the 795 nm line and can filter the 780 nm line by the interference filter [3].

There is also a linear polarizer that serves a very important purpose. Previously it was shown that the M levels can be increased by using circularly polarized light. Meaning, we are not interested in the

effects of the linearly polarized light on the transitions. Why is it important that we do this you may ask. the reason is because the $^2P_{1/2}$ state has the highest angular momentum when it has a value of $M = 2$. There is no $M = 3$ state meaning that once the electrons make the transition to the $M = 2$ state they will accumulate on that level until they can relax back to their ground configuration. By this method we create a population difference. Should always be noted that the Zeeman effect causes transitions within the atomic orbitals where the circularly polarized light causes the transitions between the different energy levels. Should also mention that this is not restricted to the positive values since it depends on the polarization direction of the light.

(v) Zero field transition

Before going further to talk about RF induced transitions we should mention the transitions that occur at values of zero magnetic field. The fundamental reason this happens is because the atoms are still being irradiated with the photons at the energy to excite the electrons. When the magnetic field is zero there are no effects from the hyperfine splitting or the Zeeman effect so there is, ideally, only two energy levels and have a completely degenerate system. Where, it becomes simple to populate one of them. This results in the lineshape that is shown on figure 11.

This can be used to tune the magnetic field of the apparatus and cancel off most if not all of the outside sources of magnetic fields. The equipment is extremely sensitive to tiny changes in magnetic field where a laptop being on or off can make a difference in the accuracy of the data.

One of the most prominent sources of outside magnetic field is the field that is produced by the Earth and must be cancelled by using a combination of the vertical, horizontal coils and lateral positioning of the apparatus.

(vi) Transient effects

Throughout this report we have been considering the optical pumping to happen only when the RF has been constantly on. Now we will consider the case when the RF signal is turned off and on at a certain frequency.

When we are at resonance the Larmor frequency for the weak field Zeeman effect is given by.

$$\omega_0 = 2\pi\nu_0 = g_F \frac{\mu_B}{\hbar} B_0 [3] \quad (17)$$

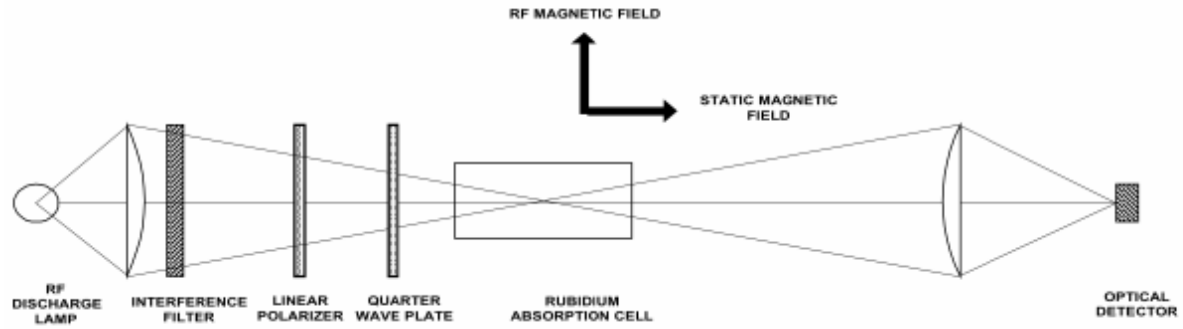


Figure 9: *Magnetic fields and angular momenta involved in the experiment [3].*

ENERGY LEVELS FOR Rb^{87} ($I = 3/2$) IN AN APPLIED MAGNETIC FIELD

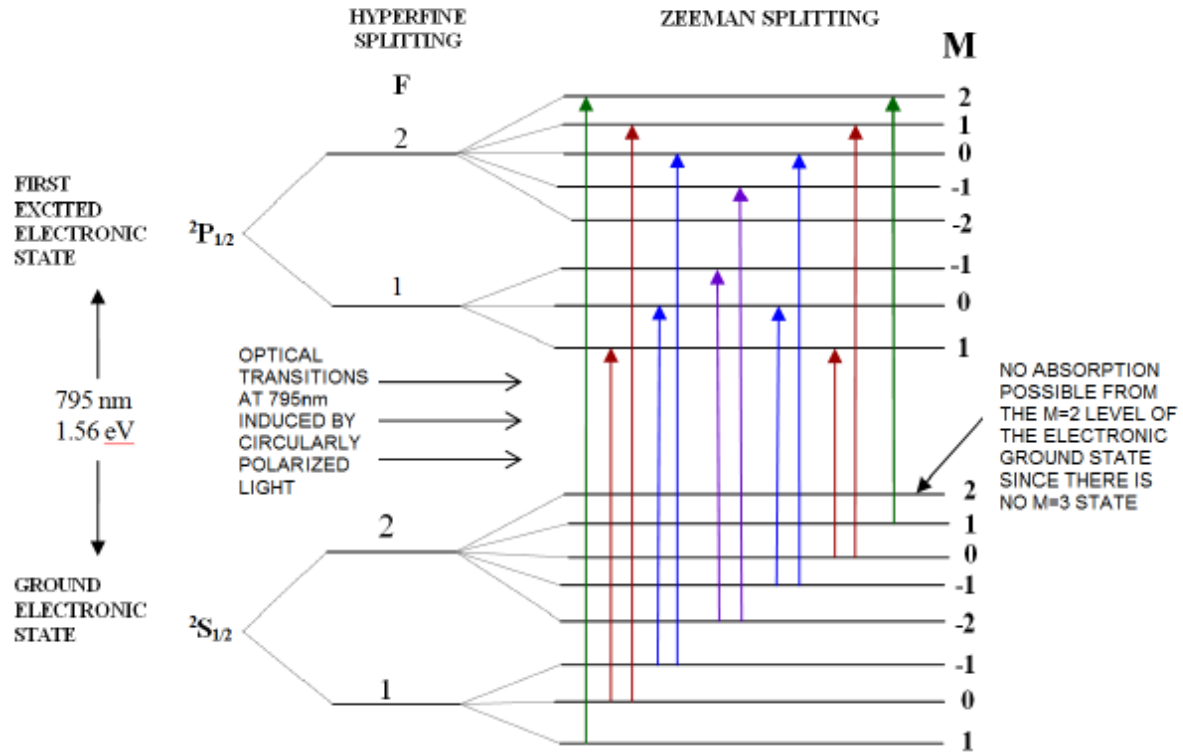


Figure 10: *Transitions involved in the optical pumping of Rb^{87} [3].*

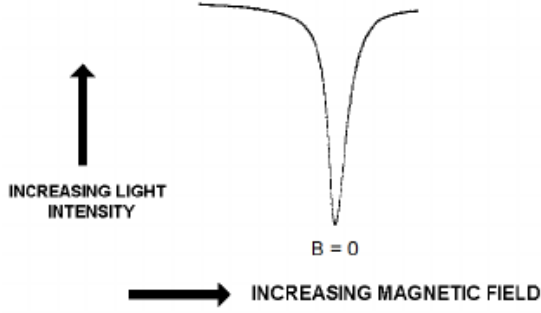


Figure 11: Zero field transition with no RF field [3].

Where, ν_0 is given by equation 11 and g_F by equation 10. We can then define the gyromagnetic ratio, γ , as.

$$\gamma = g_F \frac{\mu_B}{\hbar} [3] \quad (18)$$

We can then write the Larmor frequency as.

$$\omega_0 = \gamma B_0 [3] \quad (19)$$

The equations above are very similar to those employed in Nuclear Magnetic Resonance.

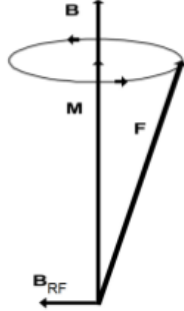


Figure 13: F vector and the precession about the magnetic field with perpendicular field B_{RF} [3].

Figure 13 shows how the total atomic angular momentum precesses about the magnetic field, B , when a perpendicular field tuned to the Larmor frequency, B_{RF} .

III Experimental Set-Up

For this experiment we are using a TeachSpin set-up that provides us access to the equipment that is necessary to be able to carry out the experiment without much difficulty or needing to set-up very complicated equipment.

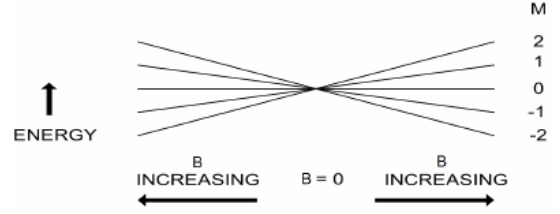


Figure 12: Energy levels near zero field with no RF field [3].

(i) Rubidium Discharge Lamp

The rubidium discharge lamp consists of an RF oscillator, oven and gas bulb. In the bulb there is a mixture of gas containing rubidium gas and a buffer gas. The buffer gas in the bulb is xenon. The remaining gas is a mixture of Rb^{85} and Rb^{87} with concentrations of about 36% and 64% respectively. The oven is set to a temperature of 115°C . The lamp takes 10 to 20 minutes in order to fully turn on and be able to equalize the temperature inside the gas bulb. It should be noted that the rubidium atoms emit light at the 795 nm range which is in the near infrared. One may be able to see some light coming from the lamp, but this light may be due to the xenon spectral line or higher lines of rubidium [3].

We are only interested in the 795 nm range line.

(ii) Detector

The detector is a PDB-C108 silicon photodiode from Photonic Detectors Inc. [3] With an active area of 0.25 inches in diameter and a spectral response in the 795 nm range of 0.6 A/W. Figure 14 gives a general schematic of the photodiode with some of the connections. The preamp is a current-to-voltage converter with three gain settings selectable by a switch on the detector itself.

The photodiode preamplifier has a voltage range of 0.0 V to 11.5 V and it should be kept in mind to avoid saturating the signal.

Gain Resistor (M Ω) \pm 5%	Low pass 3dB point (kHz) \pm 10%	Noise (μV_{pp})
1	12.0	20
3	8.0	40
10	5.0	100

Table 1: Photodiode preamplifier specifications [3]. The signal from the preamp is on a coaxial BNC

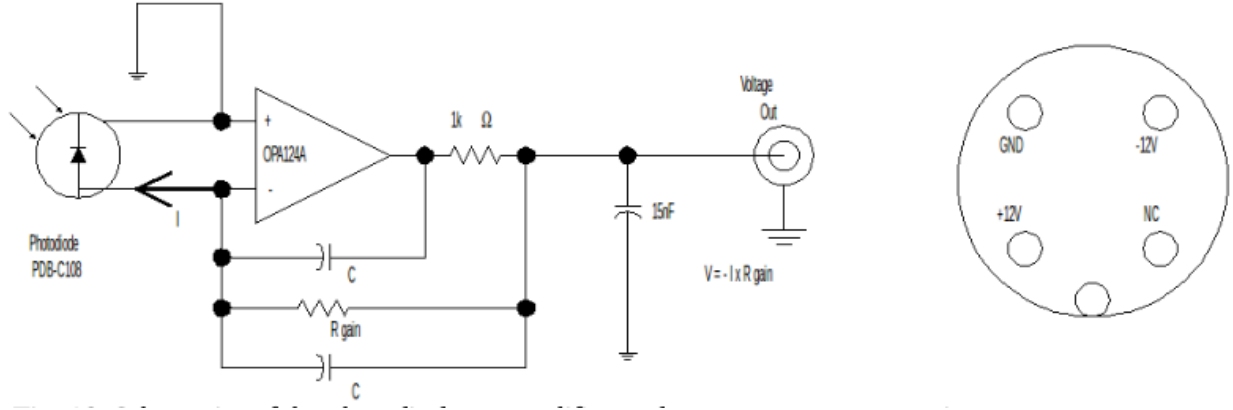


Figure 14: *General Schematic of the photodiode detector with preamplifier and preamp power connections [3].*

connector labeled Detector that feeds into the main housing for the analysis. This can be used to connect the cable directly to an oscilloscope and see what is being read.

The electronics houses the following sections that can help to adjust the signal from the detector [3].

- a). DC offset: 0-10 V DC Set by a ten turn potentiometer and fine control adjustment 0-20 mV set by a one turn potentiometer. At low gain settings the fine adjustment knob will not be very useful due to the scaling difference.
- b). Gain: 1,2,5 ... 100 Adjustable gain knob that will increase the signal gain. The maximum value is 1000.
- c). Low Pass filter: A two pole low pass filter with time constants: min., 1 ms, 10 ms, 100 ms, 1 s, 3s. When the min. value is selected, the frequency response is determined by the gain setting of the preamplifier.
- d). Meter: Displays the voltage reading from the detector output. The range is from -4 to +4 V with a multiplier toggle switch to increase to a range of -8 to +8 V.

(iii) Optics

In this section we will go into the optics that are used for this experiment. The optics that will be discussed are: plano-convex lenses, interference filter, polarizers, quarter wavelength plate.

- a). Two plano-convex lenses: Diameter 50 mm, focal length 50 mm.
- b). Interference filter: Diameter 50 mm. This filter is chosen since it has the ability to absorb

the 780 nm line that is emitted and still transmit the 795 nm line that is of interest in the experiment.

- c). Two linear polarizers on rotatable mounts: Diameter 50 mm. The linear polarizer will be used to filter out other polarizations of light so that they can be converted into circularly polarized light with the help of a quarter wavelength plate.
 - d). Quarter wavelength plate on rotatable mount: Diameter 50 mm, "optical thickness" 205 ± 5 nm. When properly oriented, the plate can convert linearly polarized light into circularly polarized light. The plate has different optical axes which have different indices of refraction that will slow down the light beam. To produce circularly polarized light, place the quarter wave plate at a 45° angle to the linear polarizer.
- Figure 15 gives the retardation about the different axial tilt. Tuning the optical thickness (retardation) can be accomplished by rotating the plates.

- e). Alignment: Throughout the experiment the optics may need to be aligned to be able to get the best results from the equipment. One way to do this is to maximize the signal gotten from the detector by moving the lenses until the signal reaches a maximum value. In theory this should work since the light incident to the lenses should be made to be linearly aligned and then re-focus into the detector to get the signal reading. If we do not get a maximum value there are two things that can be happening. The light that is coming from the

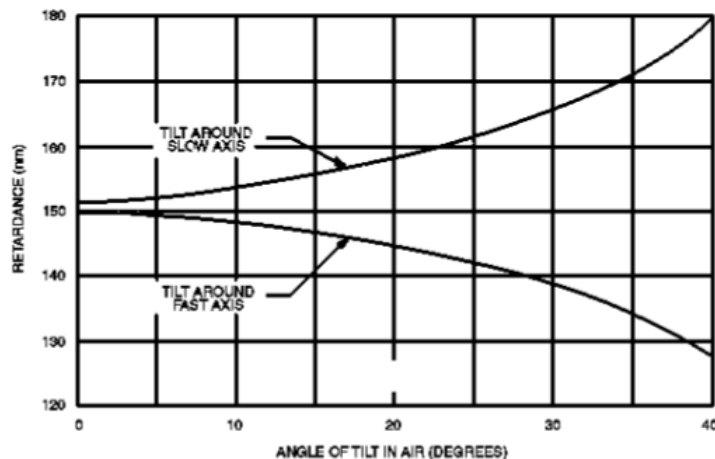


Figure 15: *Tilt tuning of the quarter wavelength plate [3].*

lamp is not being spread into a parallel beam correctly or the light that is going into the detector is not being refocused properly.

We shall look at the first problem. One possible way to troubleshoot the problem is to use a sheet of whitepaper and place it in front of the lens. Remember that the light that we are able to see with the slight purple color is the light that may be due to transitions in the xenon gas or higher energy excitations in the rubidium atoms. So, we cannot do this after the interference filter as we will not be able to see the light beam nor properly adjust the lens position. By moving the paper back and forth one should be able to see that the beam of light does not change in size which we will see as a circle. If it does diverge slightly change the lens position until it does not diverge anymore and the circle is at its maximum diameter.

Now we shall look at the second problem which will be at the detector. For this we can place the quarter wave plate and the linear polarizer in front of the discharge lamp. Due to the fact that the entire apparatus is bolted onto the rail and table we will not be able to use the same troubleshooting method as we did before, since we cannot see the light beam. What we must do is to read a signal either on the oscilloscope or a voltmeter and maximize the signal. To do this change the position of the lens on the rail and assuming that the first lens was set to its correct position the second should be in the correct position when the signal from the detector is at a maximum. This is because, the light beam that incident on the lens is supposedly parallel and constant so the lens should

refocus the light back into a single point and this point should be at the detector.

It is important to check the height of the optics which should be set to a height of approximately 3.5 inches.

(iv) Temperature regulation

The following components make up the cell temperature regulation system [3].

- a). Temperature regulator: Proportional, Integral, Derivative (PID) temperature controller with associated electronics. The settings for the PID are preset in the electronics box and cannot be changed without changing the inner electronics.
- b). Temperature probe: Type T (Copper - Constantan) Thermocouple ($5\text{ }\mu\text{m}$ wire). Constantan is magnetic, however, the wire was chosen to be so small so that the effect of its magnetic field on the magnetic field in the sample can be neglected.
- c). Oven: The oven consists of the following components.
 - 1). Rubidium cell: Glass bulb that contains the rubidium sample that is to be studied in the experiment.
 - 2). Cell holder: A foam insert that holds the sample.
 - 3). Heater: The heater is an open-ended glass heater that is wrapped with non-magnetic bifilar wound heater wire. The resistance is measured to be $50\text{ }\Omega$.

- 4). Insulation: Foam layer surrounding the heater.
 - 5). Oven casing: A Plexiglass cylinder. Has endcaps of 50 mm optical windows. Holes in the casing allow wires to be run into the oven.
- d). Operation: On the front face of the electronics box there is a controller window with three buttons that control the menu up and down respectively. To set a temperature one must press the menu button and cycle to SP (Set Point) and using the up and down buttons one can set the desired temperature in centigrade. To view the current temperature one can press the menu button again and press it again to show the PRoC on the display. By leaving it on this setting it will display the measured temperature.
- Do note that setting the temperature takes a very long time (20-30 minutes). So, the first thing that should be done when starting the lab should be to set the temperature and allow it to settle.
- The minimum temperature is ambient room temperature where the max is approximately 100° C.

(v) Magnetic Fields

All the DC magnetic fields are produced by magnetic coils that are placed in a Helmholtz configuration. There are three magnetic coils whose specs are known.

	Mean Radius (cm)	Turns/Side
Vertical Field	11.735	20
Horizontal Field	15.79	154
Sweep field	16.39	11

Table 2: Mean Radius and turns given values for the coils [3].

	Field/Amp ($T \times 10^{-4}/A$)	Max Field ($T \times 10^{-4}$)
Vertical Field	1.5	1.5
Horizontal Field	8.8	22.0
Sweep field	0.60	0.60

Table 3: Field/Amp and Maximum field specs for the coils. The Field/Amp specs are approximate [3].

IV Results and Discussion

(i) Absorption of *Rb* resonance radiation by atomic *Rb*

References

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