Key Establishment Protocols

SEC 501 Introduction to Cryptography and Security Protocols

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Key Management Problem

- Security of the keys
  - Even if the cryptographic algorithms & protocols are cryptographically ultra-secure, a possible compromise of secret keys or part of them will have grave consequences.
- How two (or more) parties will exchange (agree on) keys for secret communication if they are unable to meet.
- Main problem is to share secret information for symmetric cryptography.
  - Public key cryptography keys may be stored on public databases.

Key Agreement Protocols

- Protocols whereby a secret key is established by exchanging information between two or more parties.
- Each party derives the secret key from the exchanged information.
- Key exchange is best done using public key cryptography.
- Diffie-Hellman protocol establishes a key with transfer of two messages.
- However, DH does not provide <u>authentication</u>.
- Station-to-Station protocol is an authenticated version of DH protocol.

DH Key Exchange

- Large prime p.
- A generator $\alpha \bmod p$

Alice

1. Picks a random a
2. Computes $p_A = \alpha^a \bmod p$
3. Publishes p_A
4. Computes k_{AB}
   $R_{BA} = {p_B}^a \bmod p$
   $R_{BA} = \alpha^{ba} \bmod p$

Bob

1. Picks a random b
2. Computes $p_B = \alpha^b \bmod p$
3. Publishes p_B
4. Computes k_{BA}
   $R_{AB} = {p_A}^b \bmod p$
   $R_{AB} = \alpha^{ab} \bmod p$

$$R = R_{AB} = R_{BA} = \alpha^{ab} \bmod p$$

$$K = \mathtt{Hash}(R||param) \qquad \text{(key derivation)}$$

The Intruder-in-the-Middle Attack

Alice	Eve		Bob
a	e		b
$p_A = \alpha^a$	$p_E = \alpha^e$		$p_B = \alpha^b$
$p_A \dashrightarrow$	p_A	p_B	$\dashleftarrow p_B$
$p_E \dashleftarrow$	p_E	p_E	$\dashrightarrow p_E$
${p_E}^a = \alpha^{ea}$			${p_E}^b = \alpha^{eb}$
	$K_1 = {p_A}^e = \alpha^{ae}$	$K_2 = {p_B}^e = \alpha^{be}$	

Station-to-Station Protocol 1/2

- Authenticated key agreement protocol.
- Alice and Bob use their private keys to sign the exchanged messages.
- Sign function : $\texttt{Sign}_{sk}()$
- Verify function : $\texttt{Verify}_{pk}()$
- Public keys are obtained from a public trusted database

Alice	Bob	
a	b	private keys
$p_A = \alpha^a \bmod p$	$p_B = \alpha^b \bmod p$	public keys

Station-to-Station Protocol 2/2

Alice

$R_A = \alpha^x \bmod p$

$T = \alpha^{yx} \bmod p$

$K = \texttt{Hash}(T||param)$

Bob

$R_B = \alpha^y \bmod p$

$T = \alpha^{xy} \bmod p$

$K = \texttt{Hash}(T||param)$

$E_K(\texttt{Sign}_b(R_B, R_A))$

$D_K(\texttt{Sign}_b(R_B, R_A)) =$

$\texttt{Sign}_b(R_B, R_A)$

$\texttt{Verify}_{p_B}(\texttt{Sign}_b(R_B, R_A))$

$E_K(\texttt{Sign}_a(R_B, R_A)))$

$D_K(\texttt{Sign}_a R_B, R_A)) =$

$\texttt{Sign}_a(R_B, R_A)$

$\texttt{Verify}_{p_A}(\texttt{Sign}_a(R_B, R_A))$

Forward Secrecy

- **Definition:**
  - A secure communication protocol is said to have forward secrecy if the compromise of long-term keys does not compromise past session keys
  - Attacker can store all past communications
- Station-to-Station Protocol provides forward secrecy
  - Bob sends $E_K(\mathtt{Sign}_b(R_B, R_A))$ to Alice
  - Assume that Bob's private key b is compromised at a later date.
  - This is not going to disclose the session key y chosen by Bob in a previous session of the station-to-station protocol

Conference Keying 1/2

- Problem statement
  - A group of t users wants to agree on a key
    - U_i where $i = 0, 1, \ldots, t-1$
  - each user contributes to the agreed key
- Setup
  - Large prime p and a generator α in $\mathbb{Z}_p^*$.
- Partial key generation
  1. User U_i selects a random integer $r_i, 1 < r_i < p-2$,
  2. computes $z_i = \alpha^{r_i} \mod p$
  3. sends z_i to $U_{i-1 \mod t}$ and $U_{i+1 \mod t}$

Conference Keying 2/2

- Computation of key
  - Each user U_i, after receiving z_{i-1} and z_{i+1} computes

$$x_i = \left(\frac{z_{i+1}}{z_{i-1}}\right)^{r_i} \bmod p = \alpha^{r_{i+1}r_i - r_{i-1}r_i} \bmod p$$

  - and broadcasts x_i
  - After receiving x_j for $1 \le j \le t$ and $j \ne i$, U_i computes $K = K_i = (z_{i-1})^{tr_i} x_i^{t-1} x_{i+1}^{t-2} \cdots x_{i+(t-3)}^{2} x_{i+(t-2)}^{1} \bmod p$

Example: Conference Keying 1/2

- Four users U_0, U_1, U_2 and U_3
- They select r_0, r_1, r_2 and r_3 at random
- They compute
  - $z_0 = \alpha^{r_0} \mod p$
  - $z_1 = \alpha^{r_1} \mod p$
  - $z_2 = \alpha^{r_2} \mod p$
  - $z_3 = \alpha^{r_3} \mod p$
- User U_i sends z_i to U_{i-1} and U_{i+1} for $i = 0, 1, 2, 3$

Example: Conference Keying 2/2

- Upon receiving, each user computes corresponding values
  - $U_0 : x_0 = \alpha^{r_1 r_0 - r_3 r_0} \mod p$
  - $U_1 : x_1 = \alpha^{r_2 r_1 - r_0 r_1} \mod p$
  - $U_2 : x_2 = \alpha^{r_3 r_2 - r_1 r_2} \mod p$
  - $U_3 : x_3 = \alpha^{r_0 r_3 - r_2 r_3} \mod p$

$$K_0 = (z_3)^{4r_0} {x_0}^3 {x_1}^2 {x_2}^1 \mod p = \alpha^{r_3 r_0 + r_1 r_0 + r_2 r_1 + r_3 r_2}$$
$$K_1 = (z_0)^{4r_1} {x_1}^3 {x_2}^2 {x_3}^1 \mod p = \alpha^{r_1 r_0 + r_2 r_1 + r_3 r_2 + r_3 r_0}$$
$$K_2 = (z_1)^{4r_2} {x_2}^3 {x_3}^2 {x_0}^1 \mod p = \alpha^{r_1 r_2 + r_3 r_2 + r_3 r_0 + r_0 r_1}$$

Kerberos

- Kerberos originated from a larger project in M.I.T., called Athena.
  - Athena was originally designed for connecting a huge network of workstations so that students can securely access their files from anywhere in the net.
  - Uses only secret (symmetric) key cryptography
    - In Version V, DES in CBC mode is used
- Kerberos provides <u>security</u> and <u>authentication</u> in key exchange (or establishment) between users in a network.
  - Users could be programs as well as individuals
  - Supports both <u>entity authentication</u> and <u>key establishment</u>.

Kerberos

- Based on a client-server architecture.
  - A client is either a user or a software that has some tasks to accomplish.
    - Sends an e-mail, print documents, mount devices, etc.
  - Servers are larger entities whose function is to provide services to the clients.
- The basic Kerberos model has the following participants
  1. Cliff: a client
  2. Simon: a server
  3. Trent: trusted authority (a.k.a. authentication server)
  4. Grant: ticket-granting server.

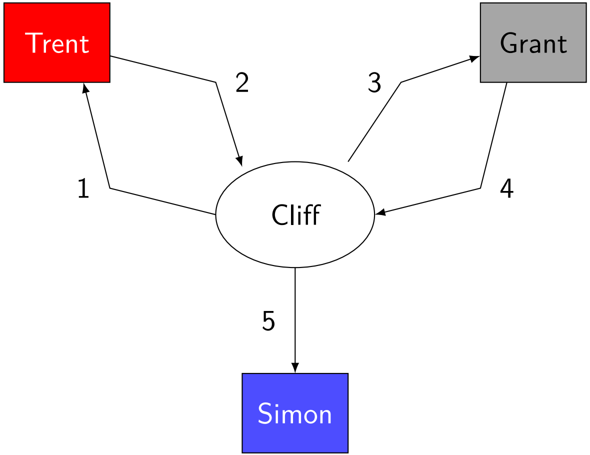
Kerberos: Roles

- Cliff requests a service from Simon,
  - But, they do not have any shared secret
  - Kerberos give them a secret information securely so that they can interact secretly.
- Trent
  - Authentication server
  - shares secret information (e.g., a password) with each user in the system
  - issues credentials to Cliff when he first logins.
    - with this credential Cliff can authenticate himself

Kerberos: Roles

- Grant
  - ticket granting server
  - After Cliff logins to the system, Grant issues him a ticket to use any particular service
  - Cliff presents his credentials (issued by Trent) to Grant to get this new ticket
  - Ticket contains information, from which Cliff and Simon generates a shared key
- Simon
  - service provider
  - receives Cliff's ticket and fulfills Cliff's service request

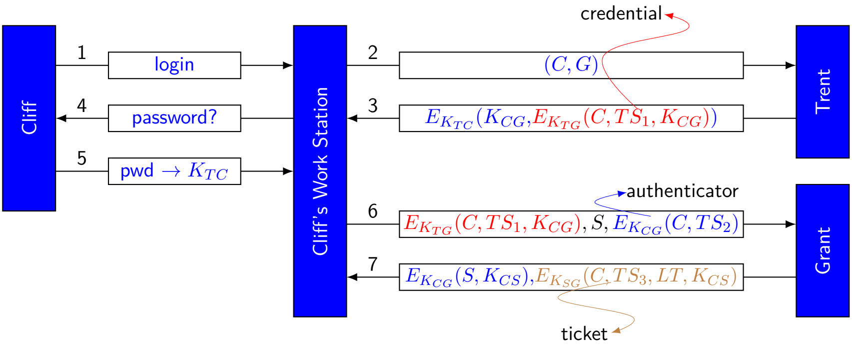
Overview of Kerberos Protocol



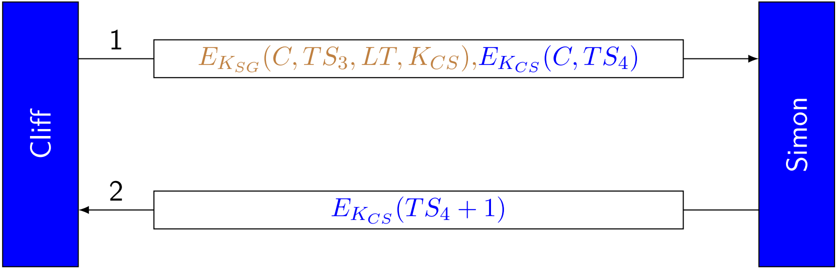
Kerberos: Notation

- K_{AB}: key that entity A and entity B share
  - K_{TG}: key Grant and Trent share
  - K_{TS}: key Simon and Trent share
- TS_i: timestamp
- LT: Validity period of the ticket (lifetime)
- $E_{K_{AB}}()$: encryption under key K_{AB}
- Credential: $E_{K_{TG}}(C, TS_1, K_{CG})$
- Authenticator: $E_{K_{CG}}(C, TS_2)$

Kerberos: Authentication



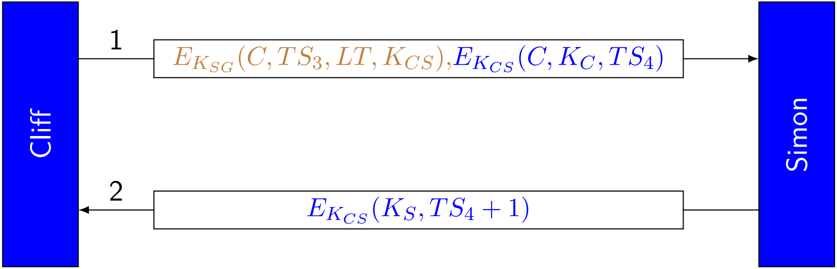
Kerberos: Use of Service



Security and Options in Kerberos

- Timestamps are used
  - Hosts must provide both secure and synchronized clocks.
- Security of Kerberos
  - If the shared key between Trent and Cliff are passwords, the protocol is no more secure than the strength of the password.
- Reuse of tickets
  - The lifetime of a ticket allows reuse of the ticket for multiple interactions with no additional interactions with Grant.
- Optional keys
  - K_C and K_S allow Cliff and Simon to combine these keys to derive another key, $F(K_C, K_S)$.

Optional Keys



Public Key Infrastructure (PKI)

- PKI is an infrastructure that keeps track of public keys
- A framework consisting of
  - policies defining the rules under which the cryptographic systems operate, and
  - procedures for generating and publishing keys and certificates.
- All PKIs consists of
  - certification
    - binding a public key to an entity
  - validation
    - guarantees that certificates are valid

Certificates

- A certificate contains information signed by its publisher, who is commonly referred as the Certification Authority (CA).
- There are different types of certificates
  1. Identity certificates contains entity's identity information such as e-mail address, and a list of public keys for the entity.
  2. Credential certificates contain information describing access rights.
- Data in certificates is signed by the CA
  - If Alice knows the public key of the CA, she can extract with assurance Bob's identity and his public keys from his certificate issued by the CA.

Trust in PKI

- Alice might not trust Bob,
- She might trust the CA, publisher of Bob's certificate
- PKI consists of many CAs.
- A CA can certify another CA if the former is more trusted.
- Different levels of trust
  - Alice and Bob may have different CAs
  - Alice's CA may only trust Bob's CA to certify Bob and but not certify others.
- Trust relationships become very elaborate.
  - It may be difficult to determine how much Alice can trust a certificate she receives.

X.509 Certificates

- X.509 is an international standard by ITU-T
  - designed to provide authentication services on large computer networks.
  - Initially issued in 1988
  - X.509 specifies public-key certificate format.
  - X.509 certificates are used in Visa and Mastercard's SET standard, in S/MIME, IP Security, and SSL/TLS.

X.509 Certificate Format

Version
Serial no.
Signature Algorithm Identifier
Issuer name
Validity period
Subject name
Subject's public key info
Issuer unique identifier
Subject unique identifier
Extension
Signature

- X.509 certificates contain fields describing trust policies.
- It is possible to designate that a public key is suitable for secure e-mail, but not suitable for e-commerce applications.
- <u>Notation</u>
  - `CA<<A>>` : the certificate of user `A` issued by certification authority `CA`.
  - $\mathtt{CA{<}{<}A{>}{>}\ =\ CA\{V,SN,AI,CA,T_A,A,Ap\}}$

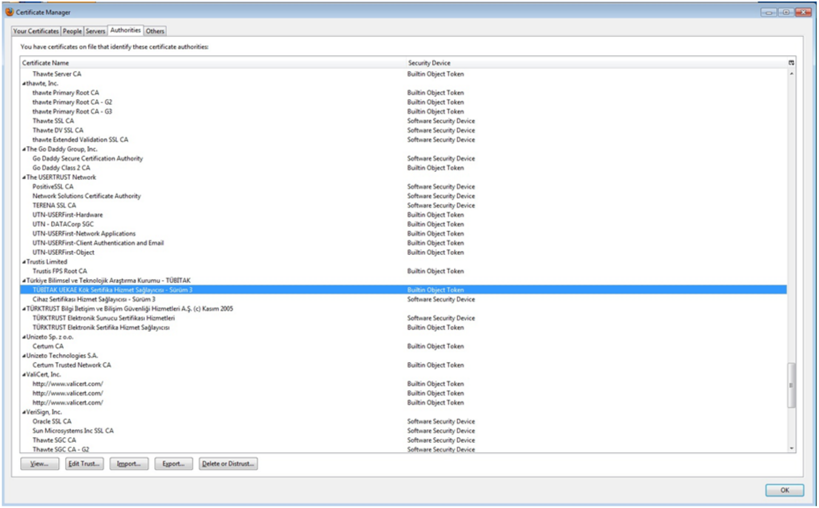
Sample Certificate

```
Certificate:
    Data:
        Version:  1 (0x0)
        Serial Number:  7829 (0x1e95)
        Signature Algorithm:  md5WithRSAEncryption
        Issuer:  C=ZA, ST=Western Cape, L=Cape Town, O=Thawte Consulting cc,
                 OU=Certification Services Division,
                 CN=Thawte Server CA/Email=server-certs@thawte.com
        Validity
            Not Before:  Jul 9 16:04:02 1998 GMT
            Not After :  Jul 9 16:04:02 1999 GMT
        Subject:  C=US, ST=Maryland, L=Pasadena, O=Brent Baccala,
                  OU=FreeSoft, CN=www.freesoft.org/Email=baccala@freesoft.org
        Subject Public Key Info:
            Public Key Algorithm:  rsaEncryption
            RSA Public Key:  (1024 bit)
                Modulus (1024 bit):
                    00:b4:31:98:0a:c4:bc:62:c1:88:aa:dc:b0:c8:bb:
                ...
                Exponent:
                    65537 (0x10001)
    Signature Algorithm:  md5WithRSAEncryption
        93:5f:8f:5f:c5:af:bf:0a:ab:a5:6d:fb:24:5f:b6:59:5d:9d:
        ...
```

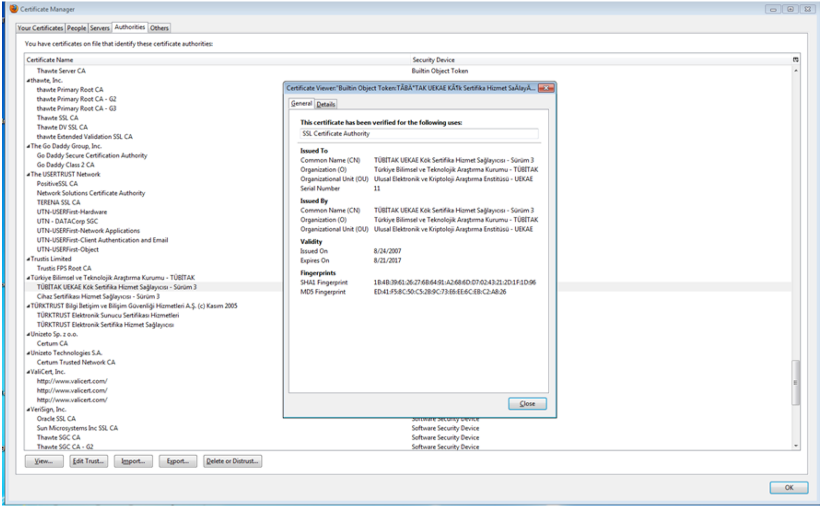
Self-Signed Certificate

```
Certificate:
    Data:
        Version:  3 (0x2)
        Serial Number:  1 (0x1)
        Signature Algorithm:  md5WithRSAEncryption
        Issuer:  C=ZA, ST=Western Cape, L=Cape Town, O=Thawte Consulting cc,
                 OU=Certification Services Division,
                 CN=Thawte Server CA/Email=server-certs@thawte.com
        Validity
            Not Before:  Aug 1 00:00:00 1996 GMT
            Not After :  Dec 31 23:59:59 2020 GMT
        Subject:  C=ZA, ST=Western Cape, L=Cape Town, O=Thawte Consulting cc,
                  OU=Certification Services Division,
                  CN=Thawte Server CA/Email=server-certs@thawte.com
        Subject Public Key Info:
            Public Key Algorithm:  rsaEncryption
            RSA Public Key:  (1024 bit)
                Modulus (1024 bit):
                    00:d3:a4:50:6e:c8:ff:56:6b:e6:cf:5d:b6:ea:0c:
                    ...
                Exponent:  65537 (0x10001)
        X509v3 extensions:
            X509v3 Basic Constraints:  critical
                CA:TRUE
    Signature Algorithm:  md5WithRSAEncryption
        07:fa:4c:69:5c:fb:95:cc:46:ee:85:83:4d:21:30:8e:ca:d9:
        ...
```

Certificates from My Computer



Certificates from My Computer



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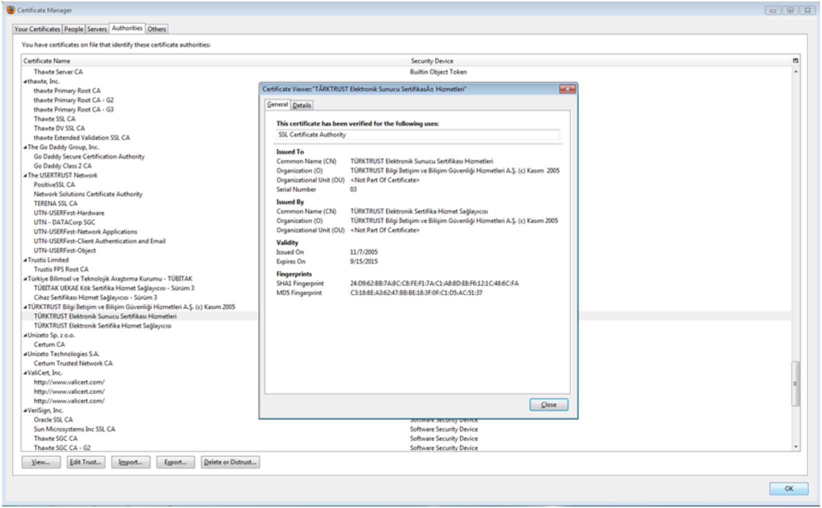
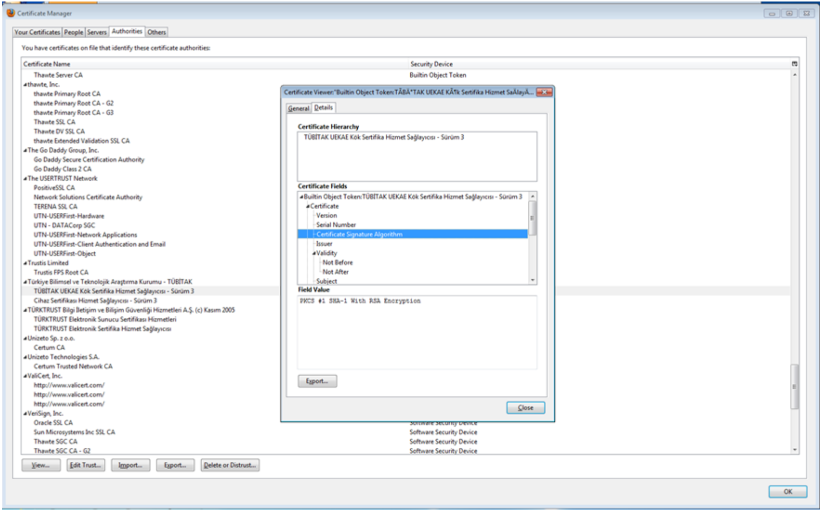
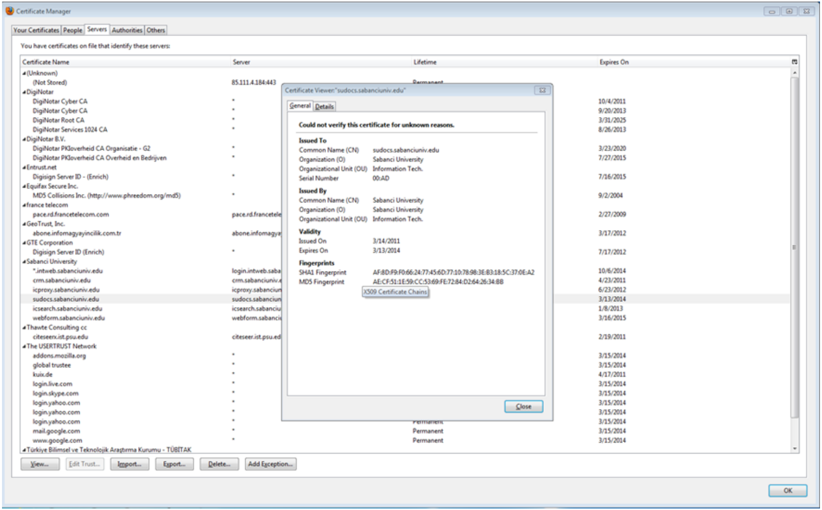


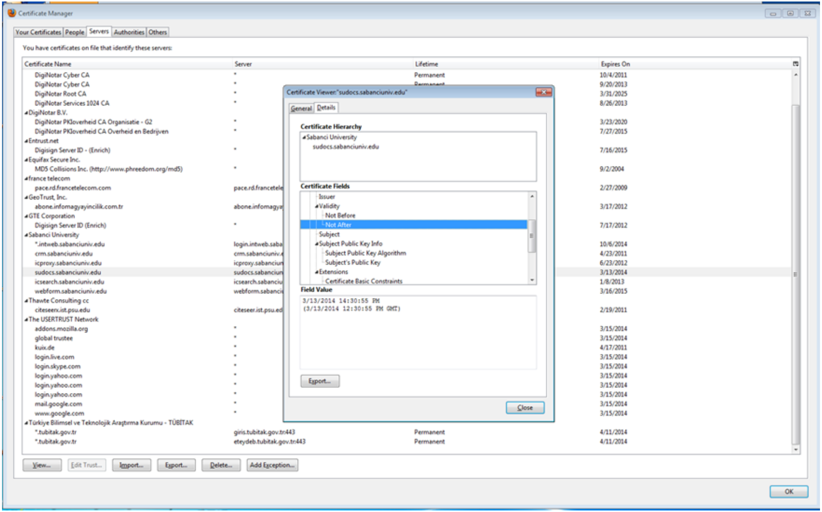
Certificates from My Computer



Certificates for SuDocs



Certificates for SuDocs

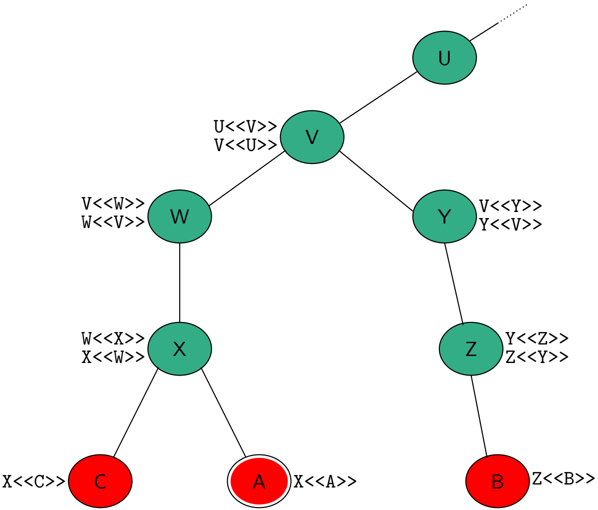


Chain of Certificates

Alice		Bob
$pk_{\texttt{CA1}}$		$pk_{\texttt{CA2}}$
CA1<<Alice>>	$\xleftarrow{\texttt{CA2<<Bob>>}}$	CA2<<Bob>>

Alice		CA2
$pk_{\texttt{CA1}}$	$\xrightarrow{\texttt{RQST(CA1<<CA2>>)}}$	
	$\xleftarrow{\texttt{CA1<<CA2>>}}$	

X509 Certificate Chains



X509 Certificate Chains

- A can acquire the following certificates from the directory to establish a certification path to B:
  - X<<W>>, W<<V>>, V<<Y>>, Y<<Z>>, Z<<B>>
- B does the same thing:
  - Z<<Y>>, Y<<V>>, V<<W>>, W<<X>>, X<<A>>

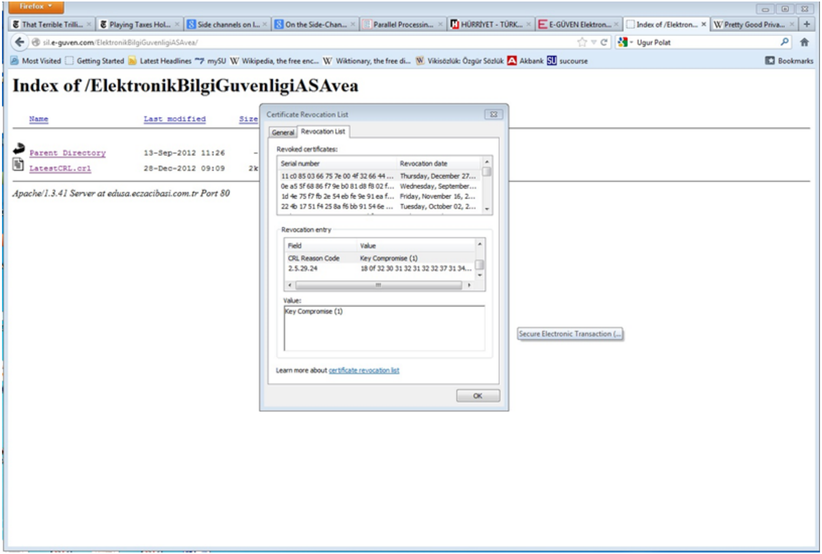
Revocation of Certificates

- Like credit cards, certificates expire.
- On occasion, it may be desirable to revoke (invalidate) a certificate before it expires.
- The reasons are
  1. The user's private key is (suspected to be) compromised.
  2. The user is no longer certified by this CA.
  3. The CA's certificate is (suspected to be) compromised.

Revocation of Certificates

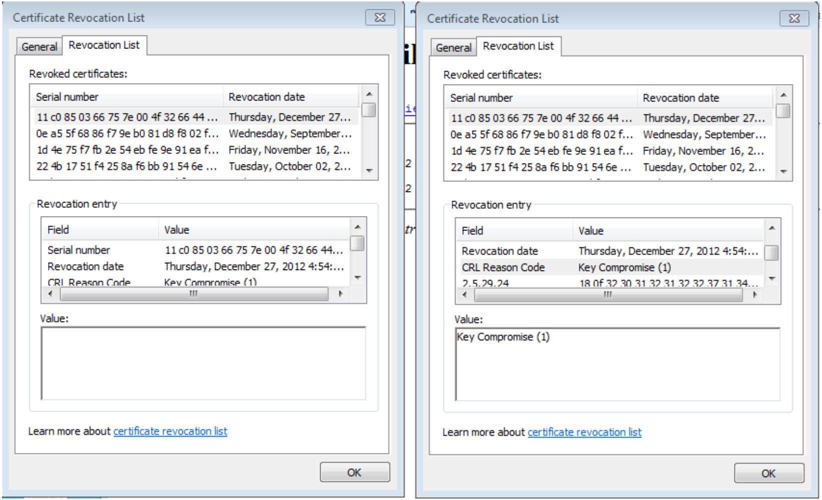
- Along with the certificates, certificate revocation list (CRL) is posted to the directory.
- CRL is signed by the issuer
- When a user receives a certificate, it also checks the CRL to see if the certificate is still valid.
- Example:
  - http://www.e-guven.com/
    - SIL (Sertifika Iptal Listeleri)
    - https://www.e-guven.com/bilgi-bankasi/sertifika-iptal-listeleri/
  - http://crl.verisign.com/Class3SoftwarePublishers.crl

CRL



Firefox
sil.e-guven.com/ElektronikBilgiGuvenligiASAvea/
Index of /ElektronikBilgiGuvenligiASAvea
Name
Last modified
Size
Parent Directory
13-Sep-2012 11:26
LatestCRL.crl
28-Dec-2012 09:09
Apache/1.3.41 Server at edusa.eczacibasi.com.tr Port 80
Certificate Revocation List
General
Revocation List
Revoked certificates:
Serial number
Revocation date
11 c0 85 03 66 75 7e 00 4f 32 66 44 ...
Thursday, December 27...
0e a5 5f 68 86 f7 9e b0 81 d8 f8 02 f...
Wednesday, September...
1d 4e 75 f7 fb 2e 54 eb fe 9e 91 ea f...
Friday, November 16, 2...
22 4b 17 51 f4 25 8a f6 bb 91 54 6e ...
Tuesday, October 02, 2...
Revocation entry
Field
Value
CRL Reason Code
Key Compromise (1)
2.5.29.24
18 0f 32 30 31 32 31 32 32 37 31 34...
Value:
Key Compromise (1)
Learn more about certificate revocation list
OK
Secure Electronic Transaction (...

CRL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Revocation date
Thursday, December 27, 2012 4:54:...
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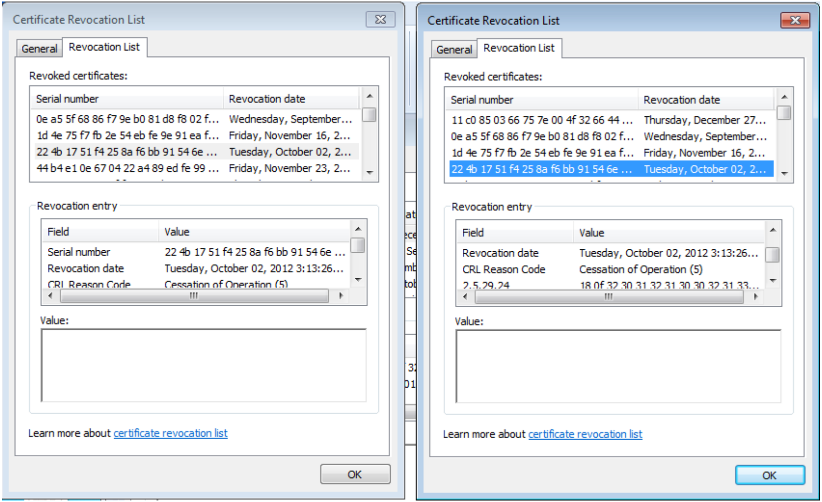
Learn more about certificate revocation list
OK

CRL



Certificate Revocation List
General
Revocation List
Revoked certificates:
Serial number
Revocation date
0e a5 5f 68 86 f7 9e b0 81 d8 f8 02 f...
Wednesday, September...
1d 4e 75 f7 fb 2e 54 eb fe 9e 91 ea f...
Friday, November 16, 2...
22 4b 17 51 f4 25 8a f6 bb 91 54 6e ...
Tuesday, October 02, 2...
44 b4 e1 0e 67 04 22 a4 89 ed fe 99 ...
Friday, November 23, 2...
Revocation entry
Field
Value
Serial number
22 4b 17 51 f4 25 8a f6 bb 91 54 6e ...
Revocation date
Tuesday, October 02, 2012 3:13:26...
CRL Reason Code
Cessation of Operation (5)
Value:
Learn more about certificate revocation list
OK
Certificate Revocation List
General
Revocation List
Revoked certificates:
Serial number
Revocation date
11 c0 85 03 66 75 7e 00 4f 32 66 44 ...
Thursday, December 27...
0e a5 5f 68 86 f7 9e b0 81 d8 f8 02 f...
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Value:
Learn more about certificate revocation list
OK

OCSP

- The Online Certificate Status Protocol (OCSP)
  - an Internet protocol used for obtaining the revocation status of an X.509 digital certificate.
  - created as an alternative to certificate revocation lists (CRL), specifically addressing certain problems associated with using CRLs in a public key infrastructure (PKI)
- How It Works
  - Alice and Bob have public key certificates issued by Ivan, the (CA).
  - Alice wishes to perform a transaction with Bob and sends him her public key certificate.

How OSCP Works

- Bob, creates an 'OCSP request' that contains Alice's certificate serial number and sends it to Ivan.
- Ivan's OCSP responder reads the certificate serial number from Bob's request. The OCSP responder uses the serial number to look up the revocation status of the certificate in a CA database that Ivan maintains.
- Ivan's OCSP responder confirms that Alice's certificate is still OK, and returns a signed, successful 'OCSP response' to Bob.
- Bob cryptographically verifies Ivan's signed response. Bob has stored Ivan's public key sometime before this transaction. Bob uses Ivan's public key to verify Ivan's response.
- Bob completes the transaction with Alice.

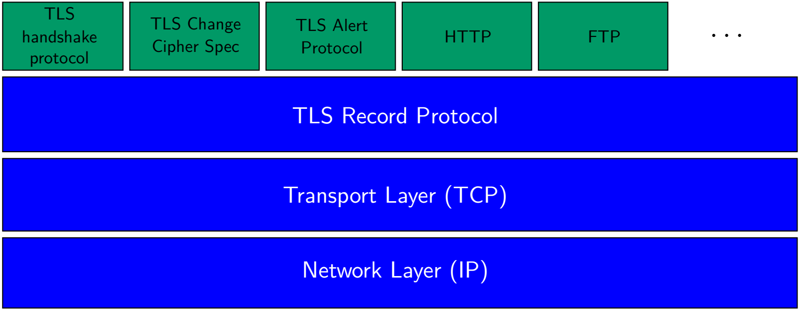
Secure Socket Layers 1/3

- Originally developed by Netscape in 1996
- SSL or TLS
- Negotiable encryption and authentication algorithms
- www.openssl.org
- Unencrypted communication for initial exchanges
- public-key cryptography to establish secret keys
- switch to secret-key cryptography
  - hybrid encryption scheme
- secure channel is established between a client and a server

A Threat report from Fortinet Networks suggests that 73% of internet traffic is now encrypted

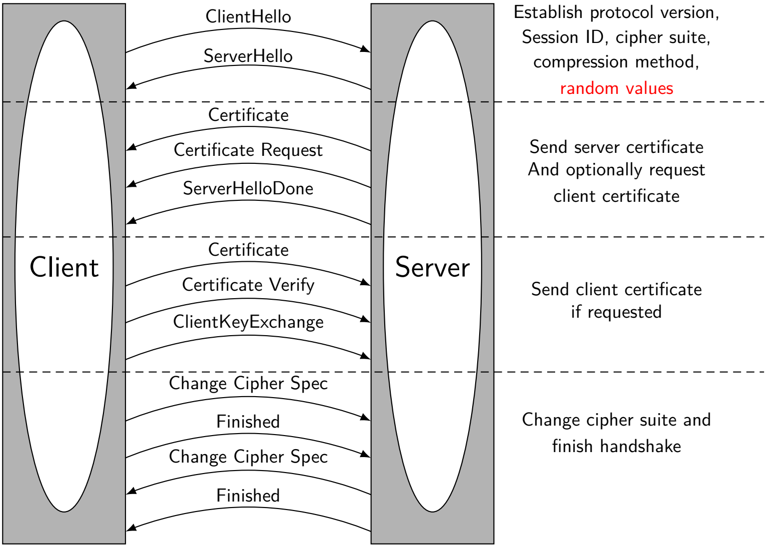
	Q1 2016	Q2 2016	Q3 2016	Q4 2016	Q1 2017	Q2 2017	Q3 2017	Q4 2017	Q1 2018	Q2 2018	Q3 2018
HTTPS ratio	52.5%	49.8%	52.4%	50.8%	54.9%	57.3%	55.4%	58.5%	61.7%	65.7%	72.2%
SaaS apps	33	35	35	36	33	28	32	37	32	34	38
IaaS apps	26	22	23	27	29	25	26	28	23	25	32

FIGURE 2: QUARTERLY MEDIAN VALUES FOR HTTPS RATIO, SAAS USAGE, AND IAAS USAGE.

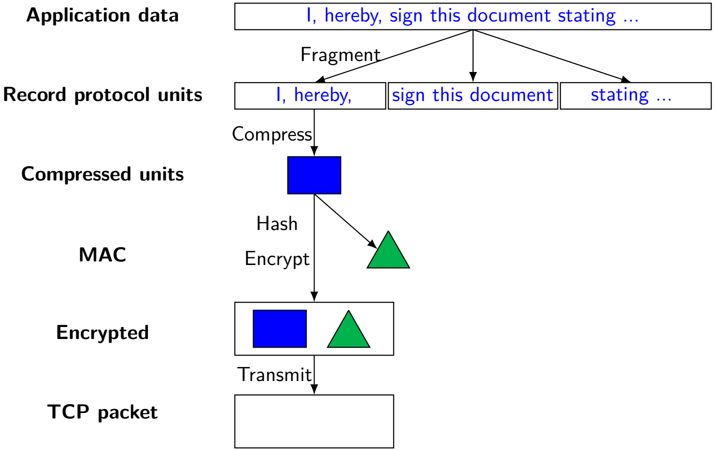


- TLS record protocol implements a secure channel
  - encrypting and authenticating messages in any connection-oriented protocol
- Other related protocols
  - establish and maintains a TLS session

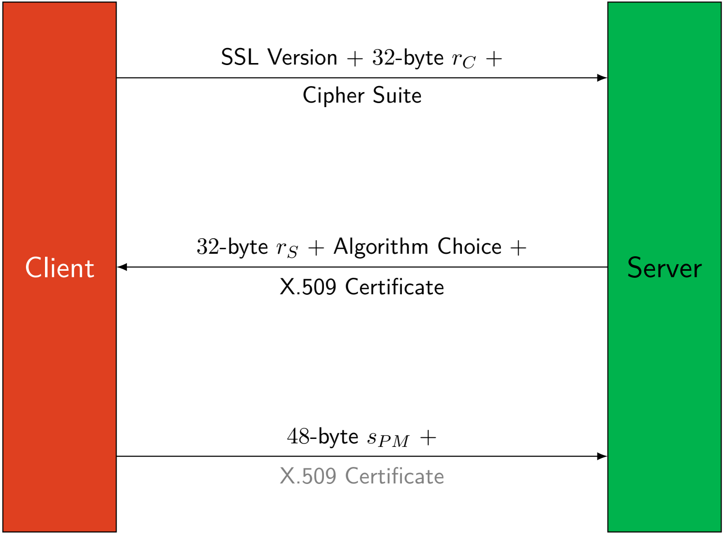
TLS Handshake Protocol



TLS Record Protocol



SSL 3.0 (TLS 1.0)



Client
Server
SSL Version + 32-byte r_C +
Cipher Suite
32-byte r_S + Algorithm Choice +
X.509 Certificate
48-byte s_{PM} +
X.509 Certificate

SSL 3.0 (TLS 1.0)

- Master secret key
  - $\texttt{MD5}(s_{PM} || \texttt{SHA1}(C || s_{PM} || r_C || r_S)) ||$
    $\texttt{MD5}(s_{PM} || \texttt{SHA1}(pad_0 || s_{PM} || r_C || r_S)) ||$
    $\texttt{MD5}(s_{PM} || \texttt{SHA1}(pad_1 || s_{PM} || r_C || r_S))$
  - 48 bytes
- Master secret key $\rightarrow$ key block
  - Six secrets from the key block
  - 2 keys for confidentiality (for each direction)
  - 2 keys for authentication (for each direction)
  - 2 initial values for CBC mode of the block cipher

TLS 1.2

- $s = \mathrm{PRF}(s_{PM}, \text{“}\texttt{master secret}\text{''}, r_C + r_S)$ returns 48 B
- PRF stands for pseudo-random function and uses SHA256
  - It takes as input a secret, a seed, and an identifying label and produces an output of arbitrary length.
- $\mathrm{P\_SHA256}(s_{PM}, \text{“}\texttt{master secret}\text{''} + r_C + r_S)$
  - $\mathrm{P\_SHA256}$ is a keyed message authentication code (MAC).

$$
\begin{aligned}
\mathrm{P\_SHA256}(\texttt{secret}, \texttt{seed}) &= \mathrm{HMAC\_SHA256}(\texttt{secret}, \texttt{A(1)+seed}) + \\
&= \mathrm{HMAC\_SHA256}(\texttt{secret}, \texttt{A(2)+seed}) + \\
&= \mathrm{HMAC\_SHA256}(\texttt{secret}, \texttt{A(3)+seed}) + \ldots
\end{aligned}
$$

where `A(0) = seed` and $\texttt{A}(i) = \mathrm{HMAC\_SHA256}(\texttt{secret, A(i-1)})$.

TLS with Forward Secrecy