A Tensor Framework for Alzheimer's Disease early Detection and Functional Connectivity Analysis in Resting State fMRI

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Abstract

Recently machine learning methods had gain lots of publicity among researchers in order to analyze the brain images such as Resting-State Functional Magnetic Resonance Imaging(rs-fMRI) to obtain a better understanding of the brain and its related disease such as Alzheimers disease. Finding the common patterns caused by a brain disorder through analyzing the functional connectivity(FC) network along with discriminating brain diseases from normal controls have traditionally been two main goals in studying rs-fMRI data. The majority of techniques for finding an FC, calculate the FC matrix for each subject and then use simple techniques in order to combine them to obtain general functional connectivity. Also, the states of the art classification techniques for finding subjects with brain disorders, also rely on calculating an FC for each subject, vectorize them and then feed them to the classifier. Considering these problems and based on multidimensional nature data, we have come up with a novel tensor framework in which the FC calculation for each class is done without the need to construct the FC for each sample, also this framework allows us to reduce the dimensionality, and create a novel discriminant function that avoids vectorization in any step and uses the test data in the training process without forcing any prior knowledge about its label to the classifier Extensive experiments using the ADNI dataset demonstrate that our proposed framework effectively boosts the fMRI classification performance and reveals novel connectivity patterns in Alzheimer's disease at its early stages.

1. Introduction

Alzheimers disease (AD) is a progressive neurodegenerative disorder with a long pre-morbid asymptomatic period which affects millions of elderly individuals worldwide[1]. It is predicted that the number of affected people will double in the next 20 years, and 1 in 85 people will be affected by 2050 [2]. The predominant clinical symptoms of AD include a decline in some important brain cognitive and intellectual abilities, such as memory, thinking, and reasoning. Precise diagnosis of AD, especially at its early warning stage: early Mild Cognitive Impairment (eMCI), enables treatments to delay or even avoid such disorders [3].

In recent years, brain imaging techniques like Positron Emission Tomography (PET)[16], Electroencephalography (EEG)[17] and functional Magnetic Resonance Imaging (fMRI)[18] have been used in the analysis of AD. Due to the high spatial resolution and relatively lower costs, fMRI is vastly used among researchers in order to monitor brain activities especially in AD and all its stages in which detecting abnormalities within small brain regions is essential [5]. An fMRI sample is naturally a 4D tensor consisting of 3D voxels moving in time, and each voxel contains an intensity value that is proportional to the strength of the Blood Oxygenation Level Dependent(BOLD) signal, which is a measure of the changes in blood flow, to estimate the activity of different brain regions[6]. Resting-state fMRI(rs-fMRI) is an fMRI technique in which the patient is asked to rest during the whole scan, focuses on the low-frequency $(< 0.1Hz)$ oscillations of BOLD signal, which presents the underlying neuronal activation patterns of brain regions[8][10]. rs-fMRI is usually used in order to analyze brain diseases like AD or Autism[27, 28].

Since each fMRI volume consist of hundreds of thousands of voxels which are often highly correlated with the surrounding voxels in the brain volume, parcellation of the brain for further analysis has moved toward the use of anatomical atlases. These atlases are strictly defined using anatomical features of the brain, like locations of common gyri and do not rely on any functional information. To generate data using an Atlas-based approach, the BOLD signal from all voxels is averaged within each brain region called Region of Interest(ROI)[7]. By putting together the average time-series for all the ROIs, the ith volume would become $X_i \in \mathbb{R}^{T \times R}, i = \{1, 2, \cdots, S\}$
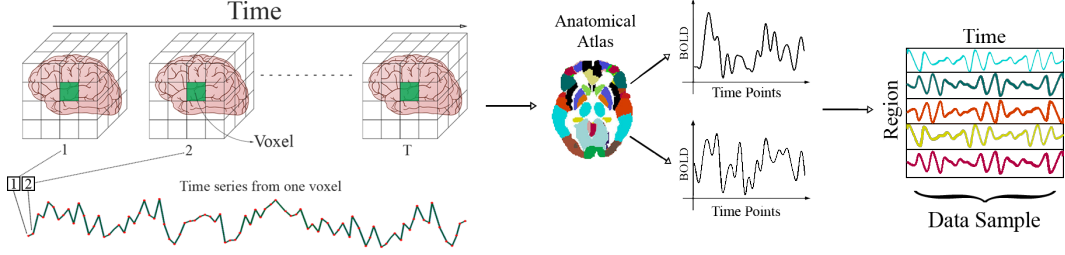
Figure 1: The process of extracting ROI time-series from the original 4D volume.

in which R, T and S are the number of ROIs, time points and samples respectively. The process of obtaining such a matrix is shown in Figure 1.

There are two major studies associated with rs-fMRI data: finding common brain disorders caused by diseases like Alzheimer's, Autism, schizophrenia and etc. and more recently detecting patients with brain disorders using classification techniques [29, 30]. Due to the high dimensionality of data and the nature of diseases like eMCI which does not show any reliable clinical symptoms, researchers moved towards advanced machine learning techniques in order to achieve more reliable analysis [31].

A powerful tool that is commonly used in order to achieve aforementioned goals is Functional Connectivity(FC) network. FC is a $region \times region$ matrix $\bar{X}$ in which $\bar{x}_{ij}$ represents the functional connectivity between the ith and jth ROI. Functional connectivity is an observable phenomenon quantifiable with measures of statistical dependencies, such as correlations, coherence, or transfer entropy [32]. Recent studies have shown that some brain disorders like AD could alter the way that some brain regions interact with each other. For example, compared with the healthy, AD patients have been found decreased functional connectivity between the hippocampus and other brain regions, and MCI patients have been observed increased functional connectivity between the frontal lobe and other brain regions[5]. So, Finding an FC that highlights the patterns caused by a disease, i.e. a **General** functional connectivity, has been a common goal in the rs-fMRI study for a long time. Several approaches exist to find common patterns among different brain scans. Data-driven methods such as PCA have been proposed for this task [49]. But ultimately most of them rely on calculating a network for each volume which may overlook the role of noises or outliers within the data[47, 48].

In recent years FCs are also used as features in classification. So, instead

of using X_i as the ith sample, corresponding FC i.e. $\bar{X}_i$ is used as a feature. Although FCs show promising results, they bring their own challenges. The computational cost of FC is usually high and also its quality massively affects the performance of the learning process. Also, Since the conventional classifiers like **S**upport **V**ector **M**achine(SVM) and or k-NN works on data in vector format, these matrix features should be vectorized in order be fed to these classifiers. This vectorization leads to high-dimensional vectors which produce poor performance due to the phenomena known as the Curse of Dimensionality. Alongside the curse of dimensionality, vectorization also destroys potential information that is embedded in the structure of data. This problem has been studied especially in image data in which vectorization destroys the spatial relations within an image[54].

In this paper, based on high order tensor decomposition, we have created a framework in which the aforementioned goals i.e. finding a general FC and detecting a disorder via classification could be achieved via a single **H**igh **O**rder **S**ingular **V**alue **D**ecomposition (HOSVD) of each class. Here based on latent variables obtained by HOSVD a general representative pattern of FC for eMCI and Normal controls are obtained. The majority of connectivity patterns detected by this method have been observed and studied in several separated types of research which shows the reliability and power of the proposed method. Along with these connections, we have also detected novel connectivities especially regarding the Cerebellum which is usually discarded in the analysis of AD. The proposed classifier also outperforms state of the art eMCI classification methods.

Viewing each class as a tensor allows us to work with *time* and *region* features separately but simultaneously. This multilinear view ables us to design a proper dimension reduction relative to the nature of each feature along with a discriminant function based on linear regression on latent space of samples that uses the test data to enhance the quality of the training set without forcing any a prior knowledge to the classifier, a task which is not possible through well known classifiers like SVM, logistic regression or k-NN. It is also notable that the proposed discriminant function directly works with the X_is as features. Having the FC calculation step omitted in classification not only heavily affects the computational performance of the method, but it also saves us from the troubles of FCs which will be discussed in the next section.

To verify our approach, we conduct an extensive experimental study on

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rs-fMRI data from the benchmark dataset ADNI [1]. As will be seen, the results demonstrate the effectiveness and advantages of our method. Specifically, the proposed framework, not only grants us superior classification accuracy to that from other methods, but it is also much faster and more stable against different data selection schemes. We have also confirmed our achieved general FC matrix using empirical data on the eMCI and Normal functional connectivity patterns.

2. eMCI classification and FC construction techniques

As it was mentioned before, obtaining and classifying FC matrices have become the dominant approach towards eMCI analysis. Variety of methods such as Pairwise Pearsons correlation coefficient [8, 9], sparse representation [8, 10, 11] and **S**parse **I**nverse **C**ovariance **E**stimation (SICE)[13] exists to obtain an FC. While the first two are easy to understand and can capture pairwise functional relationship based on a pair of ROIs, the latter can account for more complex interactions among multiple ROIs, but the estimation of partial correlation involves an inversion of a covariance matrix, which may be ill-posed due to the singularity of the covariance matrix. These methods result in vastly different networks[29]. On the other hand, computing the correlations, based on the entire time series of fMRI data simply measures the FC between ROIs with a scalar value, which is fixed across time. This actually implicitly hypothesizes the **Stationary** interaction patterns among ROIs which will result in a *static functional connectivity* (sFC). As a result, this method may overlook the complex and dynamic interaction patterns among ROIs, which are essentially time-varying. In order to overcome this issue, **Non-stationary** methods have been proposed which results in more complex networks also known as dynamic functional connectivity (dFC)[14, 15, 50]. The most common and straightforward way to investigate dFC is using windowed FC, which consists of calculating a given FC measure, for example, the Pearson correlation coefficient, over consecutive windowed segments of the data[52, 53]. Although such an analysis seems straightforward, there are also pitfalls associated with it which may cause in a non-accurate FC[51].

In the following, we briefly discuss two states of the art eMCI classification techniques belonging to these two paradigms:

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[1] http://adni.loni.usc.edu/

Kernel Compact SICE($\mathbf{K - SIEC}$) : SICE matrix have proven itself to be one of the best static functional connectivity models [13, 54, 55, 56, 57], which is extracted via the following optimization:

$$S^* = \arg\max_{S \succ 0} \quad \log\left(\det(S)\right) - \text{tr}(CS) - \lambda \left\| S \right\|_1 \tag{1}$$

where C is the sample-based covariance matrix; $\det()$, $\text{tr}()$, and $\left\|.\right\|_1$ denote the determinant, trace, and the sum of the absolute values of the entries of a matrix respectively. In classification with FC features, the vectorized SICE of each sample is used [15]. The occurrence of the curse of dimensionality and losing useful information contained in the SICE matrices(like SPD property) are two main drawbacks of this vectorization approach. To overcome these drawbacks, since each SICE matrix belongs to symmetric semidefinite positive definite (SPD) matrices Riemannian manifold, in the proposed method in [12], some SPD manifold-based distances like Log-Euclidean distance[42] and Root Stein divergence[43] are employed in kernel-based PCA to extract a compact representation of brain network. The power of this method resides in a massive dimension reduction of SICE, using its SPD property. The performance of this method heavily relies on the choice of sparsity parameter λ for SICE calculations and the number of top eigenvectors m.

High Order Networks($\mathbf{HON}$) : **This method which is proposed in ?? belongs to non-stationary paradigm uses so called High Order Networks as features for classification purposes. It uses the sliding window technique in order to split the time-series into smaller pieces and then find the relation between them[45, 46]. Let $x_i^{(l)}(k) \in \mathbb{R}^N$ denotes the k-th segment of the i-th region in the l-th sample. For each sample a network with nodes $x_i^{(l)}(k)$ could be constructed which its edge weights are obtained as

$$C_{ij}^{(l)}(k) = \text{corr}\left(x_i^{(l)}(k), x_j^{(l)}(k).\right)$$

Here the weight $C_{ij}^{(l)}(k)$ represents the pairwise Pearsons correlation coefficients between the i-th and the j-th ROIs of the l-th subject using the k-th segment of subseries. Now

$$y_{ij}^{(l)} = \left[C_{ij}^{(l)}(1), C_{ij}^{(l)}(2), \cdots, C_{ij}^{(K)}(1)\right] \in \mathbb{R}^K$$

represents the similarity of the ith and j-th, regions of the l-th sample in all segments. In ??, for each l by considering $y_{ij}^{(l)}$ as nodes of a networks with

weights

$$H_{ij,pq}^{(l)} = \text{corr}\left(y_{ij}^{(l)}, y_{pq}^{(l)}\right)$$

an higher-order network is obtained for each sample. Here for each pair of correlation time series y_{ij} and y_{pq}, $H_{ij,pq}^{(l)}$ indicates how the correlation between the i-th and the j-th ROIs influence the correlation between the p-th and the q-th ROIs. So for each sample its higher-order networks $\{H_{ij,pq}^{(l)}\}$ will be a matrix with size $R^4 \times R^4$(R is the number of regions) which will lead to a large-scale high-order FC network, containing at least thousands of vertices and millions of edges. In order to overcome this issue, the correlation time series within each subject are grouped into different clusters. Then, the correlation computations are carried out between the means of clusters. After reducing the network size, the weighted-graph local clustering coefficients was used to select the key features for each network and then an SVM classifier is trained in order to classify the obtained features. As a result of constructing a high-order network, the notion of a physical ROI become vague and thus such networks are not preferable choices in order to analyze functional connectivities.

It is noteworthy that none of these techniques consider the multi-linearity nature of the data, and since both methods use traditional classifiers like SVM or KNN, they follow a rather complex path to find vector features as the representative of each FC matrix.

3. Proposed fMRI analysis Framework Based On HOSVD

All dominant eMCI classification techniques use the FCs as the input feature of the classifier. As a result, the burden of calculating the FC along with its computational complexity is also added to the classification process. In addition, the quality of the obtained FC heavily affects the classification performance. Moreover, none of these methods attend the multi-linear propriety of such data. In this section by tensor viewpoint we show that only by one tensor decomposition we could do the following analysis on fMRI data:
• **Classification** : Viewing each class as a 3D tensor ables us to separately project each mode into a smaller one, without the necessity of unfolding it into matrices or vectors, and thus preserving the structural integrity of data along with reducing its dimensions. Transferring each sample matrix $X_i \in \mathbb{R}^{T \times R}$ into the new feature space granted by tensor viewpoint, obsoletes the necessity of constructing the FC for each sample by producing a

high quality and low-dimensional feature $\bar{X}_i \in \mathbb{R}^{\bar{T} \times \bar{R}}$ in which $\bar{T}$ and $\bar{R}$ are much smaller than T and R. This viewpoint also ables us to design a novel discriminant function in which the test data is used in the training process without forcing any prior knowledge about its label to the classifier, a task which is impossible via the conventional classifiers such as SVM, K-NN or logistic regression.

• **General FC Construction** : Using the components of HOSVD extracted in the previous step, a general FC could be constructed for each class that reveals common patterns shared among all samples within each class. This technique allows us to discard the role of outliers or noisy samples.

3.1. A Classification of Region-Time data based on HOSVD

For reducing the computational complexity and reducing the occurrence of overfitting, especially for data with large features relative to samples (Like fMRI data), using dimensionality reduction techniques is inevitable. Although each sample $X \in \mathbb{R}^{T \times R}$ has two different time and region features, the classical methods like PCA, SVD and etc. only works on vectorized version $(x = vec(X))$ of such data. Although this approach is easy to deploy, it has several drawbacks like the occurrence of Curse of dimensionality and mixing up different features(time and region). Recently multilinear dimension reduction methods like MPCA, GLRAM have been proposed that could work with multidimensional data, without folding them into vectors. In these methods, there is a freedom to select specific reduction for each kind of feature. In this section, we will use a well-known tensor decomposition named HOSVD for both dimension reduction and classification of fMRI data.

Let tensors $\mathcal{X}^{(i)} \in \mathbb{R}^{T \times R \times S_i}$, consists normal and eMCI data, for i=1,2, respectively. Here S_1, S_2 are the number of Normal and eMCI data. For tensor $\mathcal{X}^{(i)}$, the decomposition

$$\mathcal{X}^{(i)} = \left(U^{(i)}, V^{(i)}, W^{(i)} \right) \cdot \mathcal{S}^{(i)}, \tag{2}$$

is known as **H**igher **O**rder **S**ingular **V**alue **D**ecomposition(HOSVD), where orthogonal matrices $U^{(i)} \in \mathbb{R}^{T \times T}, V^{(i)} \in \mathbb{R}^{R \times R}$ and $W^{(i)} \in \mathbb{R}^{S_i \times S_i}$ are known as modes-1,2,3 singular matrices of and $\mathcal{S}^{(i)}$ is the corresponding core tensor [58]. Here $U^{(i)}$ is a base of all mode-1 fibers $\mathcal{X}^{(i)}(:, l, k)$ which indicates the behavior of lth region of the kth sample of the ith class in all times. Also $V^{(i)}$ is a base of all mode-2 fibers $\mathcal{X}(l, :, k)$ which indicates the behavior of all regions of lth sample of the ith class in the kth time. Due to the

properties of HOSVD inherited from svd, the first columns of the kth singular matrix ($k = 1, 2, 3$) have more ability in construction of main parts of kth fibers. On the other hand, the last columns of these singular matrices, have more fluctuations and are usually associated with the noisy parts of their corresponding fibers[58]. Therefore a suitable dimension reduction would be to project the mode-1 and mode-2 fibers into space spanned by the first k_1^i and k_2^i singular vectors of modes-1,2, which will be denoted by $U_{k_1^i}^{(i)}$ and $V_{k_2^i}^{(i)}$, respectively. This dimension reduction could be done as:

$$\mathbb{R}^{k_1 \times k_2 \times S_i} \ni \bar{\mathcal{X}}^{(i)} = \left(U_{k_1^i}^{(i)\mathsf{T}}, V_{k_2^i}^{\mathsf{T}} \right)_{1,2} \bullet \mathcal{X}^{(i)} \tag{3}$$

It is clear that this reduction could be done separately on each mode without the need to fold any of them. This means that the structural integrity of data is preserved during the dimension reduction process which is a key aspect in our work. It has been shown that even choosing relatively small values for k_1^1 and k_2^i would result in a very good reconstruction error[54].

Inspired by the structure of this reduction, In the following, we present a tensor-based discriminant function. By HOSVD decomposition of $\mathcal{X}^{(i)}$ the projected data $\bar{\mathcal{X}}^{(i)}$ in equation (3) becomes

$$\bar{\mathcal{X}}^{(i)} = \left(\begin{bmatrix} I_{k_1^i} & 0 \end{bmatrix}, \begin{bmatrix} I_{k_2^i} & 0 \end{bmatrix}, W \right) \bullet \mathcal{S}^{(i)}$$
$$= (W)_3 \bullet \mathcal{S}^{(i)}(1 : k_1, 1 : k_2, :)$$

So, each sample of the ith class in the reduced space has the following form

$$\bar{\mathcal{X}}^{(i)}(:, :, k) = \left(W^{(i)}(k, :) \right)_3 \bullet \mathcal{S}^{(i)}(1 : k_1^i, 1 : k_2^i, :)$$
$$= \sum_{k'=1}^{S_i} W^{(i)}(k, k') \bullet \mathcal{S}^{(i)}(1 : k_1^i, 1 : k_2^i, k').$$

This means that each sample in the ith class could be represented as linear combination of the slices of the tensor $\overline{\mathcal{S}}^{(i)} = \mathcal{S}^{(i)}(1 : k_1^i, 1 : k_2^i, :)$. So if a test data like $X \in \mathbb{R}^{T \times R}$ belongs to the ith class it's natural to expect that its projected version into principle region and times spaces, spanned by $U_{k_1^i}, V_{k_2^i}$, i.e,

$$Z^{(i)} = \left(U_{k_1^i}^{(i)\mathsf{T}}, V_{k_2^i}^{(i)\mathsf{T}} \right)_{1,2} \bullet X$$

could be approximated well as a linear combination of the slices of the tensor $\overline{\mathcal{S}}^{(i)}$ as follows

$$Z^{(i)} \approx \sum_{k=1}^{S_i} \lambda_k^i \overline{\mathcal{S}}^{(i)}(:,:,k). \tag{4}$$

Based on this viewpoint, each test data X could be assigned to a class that its projected version has the best approximation in the form (4). Due to the importance of core tensor elements with small indices in the reconstruction of the signal part of data in comparison with its last parts, the small number $k_3^i < S_i$ of slices $\overline{\mathcal{S}}^{(i)}(:,:,k)$ could be used in (4). In this viewpoint each test data X would be assigned to the l^{th}class, if

$$r_l = \min_{i=1,2} r_i,$$

where

$$r_i = \min_{\lambda^i} \|Z^{(i)} - \sum_{k=1}^{k_3^i} \lambda_k^i \overline{\mathcal{S}}^{(i)}(:,:,k)\|, \quad \lambda^i = \begin{pmatrix} \lambda_1^i \\ \vdots \\ \lambda_{s_i}^i \end{pmatrix} \tag{5}$$

shows the reconstruction error of the projected version of X in the ith class. The minimization (5) is a simple least square problem that could be solved easily.

The proposed method has an interesting property which allows us to enhance the classification performance by using the test data in the training process without forcing any prior knowledge to the classifier. We have shown that the principal properties of the ith class is reflected in $\overline{\mathcal{S}}^{(i)}$, we also know that the first slices of this tensor, i.e. slices with lower indices, have the most role in reconstructing the main parts of this class i.e. the signal parts. The same reasoning also leads to the conclusion that slices with higher indices are responsible for the possible noise in this class. Now consider that the test data X is added to data set $\mathcal{X}^{(i)}$ of the ith class. So the new data set will be $\widetilde{\mathcal{X}} \in \mathbb{R}^{T \times R \times (S_i+1)}$,

$$\begin{aligned}
\widetilde{\mathcal{X}}^{(i)}(:,:,1:S_i) &= \mathcal{X}^{(i)}, \\
\widetilde{\mathcal{X}}^{(i)}(:,:,S_i+1) &= X.
\end{aligned}$$

If X belongs to the ith class, then in the decomposition of $\widetilde{\mathcal{X}}^{(i)}$, X would reinforce the first slices of the core tensor. On the other hand, if X does

not belong to the ith class, HOSVD would naturally consider it as noise, since X is not similar to other samples and thus does not play a key role in reconstructing them. So its effect would be on the last slices of the core tensor, i.e. slices with higher indices.

Remember that the last slices of the core tensor are discarded in the dimension reduction process. As a result, if X does not belong to the ith class, it would not be involved in the classification process, on the other hand, if X belongs to this class it would affect the first slices of the core tensor and thus would lead into smaller reconstruction error. So if we add X to all classes before the decomposition process, the reconstruction error for the right class would be less than other classes. Note that since X is added to all classes, without sneaking any information about its label to the training process this technique is legit. After computing the HOSDVD of this new data sets $\widetilde{\mathcal{X}}^{(i)}$, we apply the method in (5) for classification. Algorithm 1 summarizes the proposed classification method.

Algorithm 1 TNBeMCI: Tensor based Classification method

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1) **Input**: Normal train data $\mathcal{X}^{(1)}$, eMCI train data $\mathcal{X}^{(2)}$
   $k_i^j, i = 1, 2, 3, \quad j = 1, 2.$
   Test data X
2) Construct $\widetilde{\mathcal{X}}^{(i)}$ for $i = 1, 2$ by adding X.
3) Compute $U_{k_1^i}, V_{k_2^i}$ and $\mathcal{S}(1 : k_1^i, 1 : k_2^i, k_3^i)$ of $\widetilde{\mathcal{X}}^{(i)}$.
4) Compute $Z^{(i)} = \left(U_{k_1^i}^{(i)\mathsf{T}}, V_{k_2^i}^{(i)\mathsf{T}} \right)_{1,2} \cdot X, i = 1, 2.$
5) Comput r_1, r_2 from (5)
6) Assign X to class l, if $l = \arg\min_i\{r_i\}$

In this section by HOSVD on both Normal and eMCI classes, we proposed a novel tensor-based classification and dimension reduction technique. The benefits of the proposed framework could be summarized as follow:

- With respect to the multilinear nature of data, the proposed method works with *time*, *region* and *sample* features separately and simultaneously using the extracted singular matrix for each mode without any folding sessions in order to preserve the structural integrity of each class.

- The proposed classification technique allows us to use the test data in the training process in order to enhance the classification performance.

A task which is not possible via conventional classifiers such as SVM, logistic regression and or neuronal networks.

- The fact that the proposed method does not require the calculation of FC for each sample, helps us to classify the data much faster than other states of the art methods.

In the next section, we show that based on the singular matrices obtained via HOSVD, general functional connectivity for each of the eMCI and Normal classes could be obtained.

3.2. General Functional Connectivity Calculations based on HOSVD

As it was mentioned before, one of the main studies associated with rs-fMRI analysis is finding common functional disorders caused by a disease like AD. This can be done by constructing proper FC matrices. The majority of techniques calculate the FC matrix for each individual subject(like SICE). This may overlook tiny but common connectivities shared within a class. It is also noteworthy that the majority of non-stationary methods are not capable of constructing a relatable FC since the concept of a physical ROI is not well defined in them.

In this section, we show that based on HOSVD decomposition one general functional connectivity matrix could be obtained for each class without obtaining the per-sample FC of all data separately. Here the classification is not our goal, instead of finding a general and representative relation of regions for eMCI and Normal subjects is our demand. This general pattern could be used clinically by cognitive scientists in order to obtain deeper knowledge about Alzheimer's disease and brain in general. As we saw in the previous section, the obtained U, V, W matrices are the basis for time, region and sample respectively. We used these matrices in order to reduce the dimensionality of data and create a discriminant function. In this section, we will show that these basis matrices could be reused in order to obtain a general functional connectivity matrix for each class.

In the ith class which is represented by $\mathcal{X}^{(i)}$, the slice $\mathcal{X}^{(i)}(:,l,:)$ denotes the behavior of lth region of all samples in all times. This slice could be considered as a feature for the lth region of the ith class so each region is represented as a Times-sample feature matrix. Viewing each region as a slice would allow us to consider it's behavior in all times and across all samples, which itself allows us to shed more light on common properties and ignore

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individual differences that are highly possible due to the presence of noise and outliers. Thus, by the properties of singular matrices in modes-1,3, and for appropriate values k_1^i, k_3^i, each region $\mathcal{X}(:, l, :)$ could be reduced in both time and sample features separately based on mode-1 and mode-3 truncated singular matrices $U_{k_1^i}^{(i)}$ and $W_{k_3}^{(i)}$ as follows:

$$\mathcal{Y}^{(i)}(:, l, :) = \left(U_{k_1^i}^{(i)^\mathsf{T}}, W_{k_3}^{(i)^\mathsf{T}} \right)_{1,3} \cdot \mathcal{X}^{(i)}(:, l, :). \tag{6}$$

Here $\mathcal{Y}^{(i)}(:, l, :)$ denotes a reduced version of $\mathcal{X}^{(i)}(:, l, :)$ into space spanned by $U_{k_1^i}^{(i)}$ and $W_{k_3}^{(i)}$ in modes-1,3. So,

$$\mathbb{R}^{k_1^i \times R \times k_3^i} \ni \mathcal{Y}^{(i)} = \left(U_{k_1^i}^{(i)^\mathsf{T}}, W_{k_3^i}^{(i)^\mathsf{T}} \right)_{1,3} \cdot \mathcal{X}^{(i)} \tag{7}$$

denote all reduced regions of the ith class. By this structure and substituting the HOSVD decomposition of $\mathcal{X}^{(i)}$ in (7), we obtain

$$\begin{aligned} \mathcal{Y}^{(i)} &= \left(\begin{bmatrix} I_{k_1^i} & 0 \end{bmatrix}, V, \begin{bmatrix} I_{k_3^i} & 0 \end{bmatrix} \right) \cdot \mathcal{S}^{(i)} \\ &= (V)_2 \cdot \mathcal{S}^{(i)}(1 : k_1^i, :, 1 : k_3^i) \end{aligned}$$

thus

$$\begin{aligned} \mathcal{Y}^{(i)}(:, k, :) &= \sum_{k'}^{R} V^{(i)}(k, k') \bar{\mathcal{C}}^{(i)}(:, k', :) \\ &= \left(V^{(i)}(k, :) \right)_2 \cdot \mathcal{C}^{(i)} \end{aligned} \tag{8}$$

in which

$$\mathbb{R}^{k_1^i \times R \times k_3^i} \ni \mathcal{C}^{(i)} = \mathcal{S}(1 : k_1^i, :, 1 : k_3^i).$$

The equation (8), shows that the reduced version of each region in the ith class could be written as the linear combinations of mode-2 slices of $\mathcal{C}^{(i)}$. So the coefficients of slices in this linear combination could be considered as a new feature for the lth region of the ith class. Also as we mentioned before, the first slices are better than the last ones to reflect the principle properties of the data. So for appropriate k_3^i we could select only the first coefficients in (8) as new features for the lth region. Mathematically this means each region in the ith class could be represented by a new feature vector $V(l, 1; k_3^i) \in \mathbb{R}^{k_3^i}$.

The main benefit of this approach is that each the region could be represented only be a vector with size k_3^i, instead of a large time-sample matrix.

Having each region be represented via a single low dimensional vector variety of methods such as SICE and other mentioned similarity measures could be deployed in order to construct a general FC for each class.

4. EXPERIMENTAL STUDY

4.1. Data Preprocessing and Experimental Settings

Rs-fMRI data of 196 subjects were downloaded from the ADNI website[2]. Nine subjects were discarded due to the corruption of data, and the remaining 187 subjects were preprocessed for analysis. After removing subjects that had problems in the preprocessing steps, such as large head motion, 156 subjects were kept, including 26 AD, 44 early MCI, 38 late MCI, 38 NC, and ten significant memory concern labeled by ADNI. We used the 38 NC and the 44 early MCI because our focus in this paper is to identify MCI at a very early stage, which is the most challenging and significant task in AD prediction. The IDs of the 82 (38 NC and 44 early MCI) subjects are provided in the supplementary material.

The data are acquired on a 3-T (Philips) scanner with TR/TE set as 3000/30 ms and flip angle of 80. Each series has 140 volumes, and each volume consists of 48 slices of image matrices with dimensions 64×64 with voxel size of $3.31 \times 3.31 \times 3.31$ mm^3 . The preprocessing is carried out using SPM12 and DPARSFA [40]. The first ten volumes of each series are discarded for signal equilibrium. Slice timing, head motion correction, and MNI space normalization are performed. Participants with too much head motion are excluded. The normalized brain images are warped into automatic anatomical labeling (AAL) [41] atlas to obtain 116 ROIs as nodes. By following common practice [15][17], the ROI mean time series are extracted by averaging the time series from all voxels within each ROI and then bandpass filtered to obtain multiple sub-bands as in [17].

4.2. Classification

Almost every subject in ADNI dataset has several scans. Usually, random scan data is selected and enters the processing step[**?**]. This random selection may cause several problems. Since the number of train data is very low, a small alteration in the samples could drastically change the set of input

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parameters in order to achieve the highest prediction accuracy and other classification evaluation methods. Also achieving high-quality results with a classifier does not guarantee its effectiveness on other datasets even with fine-tuning the parameters since the training set may contain outliers and unidentified corrupted data.

In order to show that the proposed framework is less sensitive against the choice of different permutations of data (i.e. Same patient with the different scan) is less vulnerable towards the aforementioned issues, we have selected 18 different permutations of data and test two state of the art classification methods on them: **HON** and **k-SICE**. To make full use of the limited subjects, a leave-one-out procedure is used for training and test. That is, each sample is reserved for the test in turn, while the remaining samples are used for training. We have use five evaluation measures: accuracy (ACC), sensitivity (SEN), Youdens index(YI), F-score, and balanced accuracy (BAC)[59].

In this article, we treat the eMCI samples as positive class and the NC samples as negative class.

4.2.1. Classification performance

The classification accuracy measure(ACC), After fine-tuning the input parameter set for each method, shows that for 16 out of 18 different random selected datasets, our approach performs better than k-SICE, the same also holds for 15 datasets comparing to HON. i.e. in 88.8% of datasets, proposed method works better than k-SICE and in 83.3% of datasets, it works better than FON. The highest classification accuracy(86.59%) is achieved with the proposed method in the 15th sample data. The highest accuracy for the HON (84.15%) is achieved in the 14th, and the highest accuracy for the SICE method (85.37%) is achieved in the 6th sample data. As it was mentioned before, being stable when the input dataset changes is a very important aspect for a classifier, in order to measure the stability, the standard deviation of accuracy along with other measures are calculated. The std. of accuracy for the proposed method is 0.64 times less than HON and 1.73 times less than k-SICE method. Similar results also hold for other classification measures.

Figure (2) shows the performance of these three methods in all five measurements. Some statistical information about these plots is also included in the embedded table. As it can bee seen in this figure, similar to the accuracy, the proposed method in overall works much better than FON and k-SICE. For a better Demonstration, table (1) provides the average of several classification measurements scores for all dataset permutations. As it can be seen
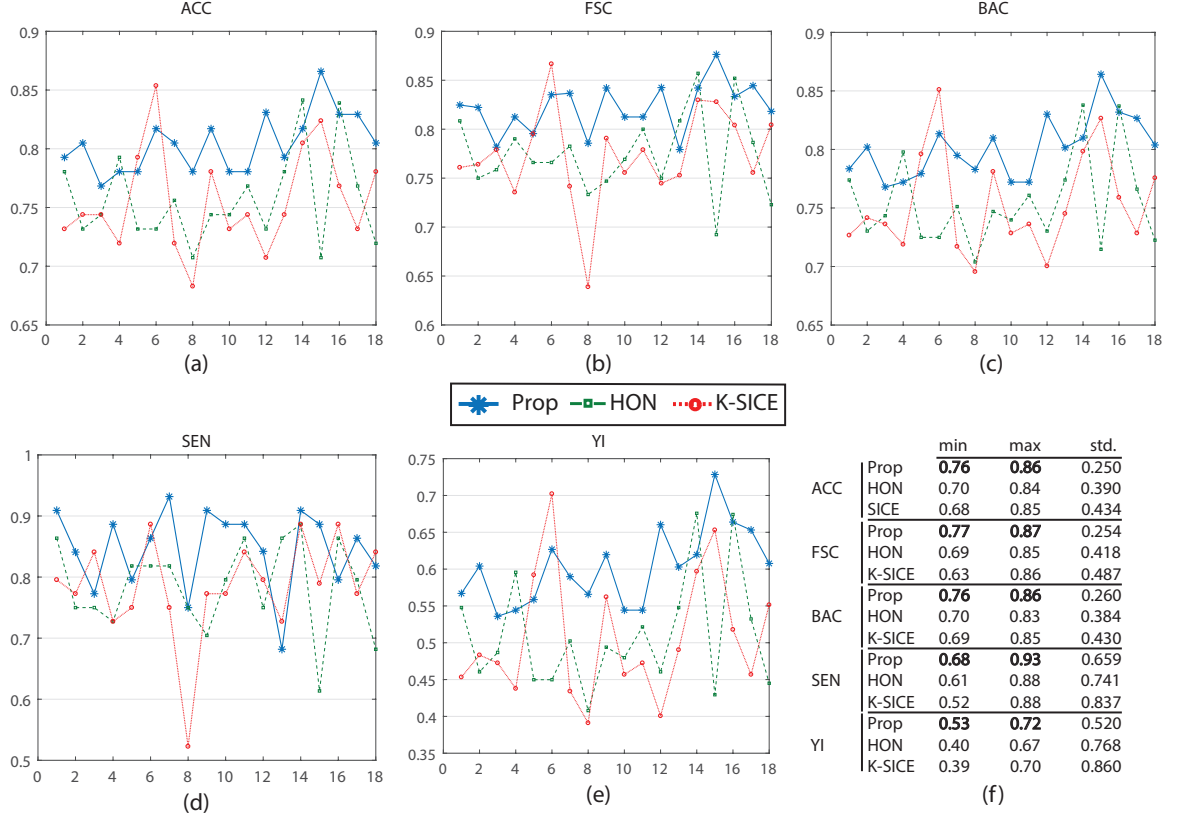
15

Figure 2: Comparison of proposed method(Prop) with K-SICE and HON applied on 18 different dataset permutations in five different classification evaluation measures. Figures *a* through *e* shows *accuracy*, *F-Score*, *balanced accuracy*, *sensitivity* and *Youden Index* respectively along with the max, min and standard deviation of each one presented at the embedded table (f).

Table 1: The Average of Different Classification Measurements in all dataset permutations in %

Method	ACC	F-Score	SEN	SPE	YI	BAC
k-SICE	75.57	77.36	78.50	72.19	50.69	75.34
FON	75.66	77.44	78.40	72.48	50.89	75.44
Proposed	**80.43**	**82.20**	**84.60**	**75.59**	**60.20**	**80.09**

Table 2: Elapsed time of the test and train phase in seconds

Method	HON	k-SICE	proposed method
Elapsed Time	6950	230	11

in this table, the average accuracy of Proposed method which is 80.43% is 4.77% higher than the next method HON, and 4.86% better than k-SICE. It is noteworthy that The other two methods i.e HON and SICE shows similar results in average.

4.2.2. Runtime Comparison

One other key features of the proposed method is that it works significantly faster than the other two methods. Table (2) shows the average elapsed time (Training plus Testing) of each method for all data permutations. These methods were executed in Matlab R2017b and carried with an Intel Core-i7 processor and 16GB of RAM. As it can be seen in this table, the proposed method is more than 600 times faster than HON and 20 times faster that SICE. Having a huge execution time especially affects the parameter selection for HON, since it uses cross-validation procedure in order to find the optimal parameters which itself require several runs of the algorithm.

4.3. Functional connectivity Network

The vector features for both Normal and eMCI classes was obtained via the proposed method as it is described in (3.2). Due to the aforementioned qualities of partial correlation, SICE is deployed in order to obtain the final FC. In order to better highlight the differences between Normal and eMCI subjects, a difference graph D is constructed by subtracting the Normal FC from the eMCI FC. This graph could be seen in Figure(3). The nodes of D shows the ROIs according to the AAL atlas. The size of each node is proportional to its graph clustering coefficient, i.e. the bigger node demonstrates higher activity in eMCI subjects in the corresponding ROI. Similar to nodes, the size of each edge is also proportional to the correlation between two ROI's. In addition, the edges are also color-coded in a way that the green edges show the positive edges in D and the orange edges shows the negative edges in D. In this manner, the green edges demonstrate decreasing in activity between the corresponding nodes in eMCI subjects and vice versa,
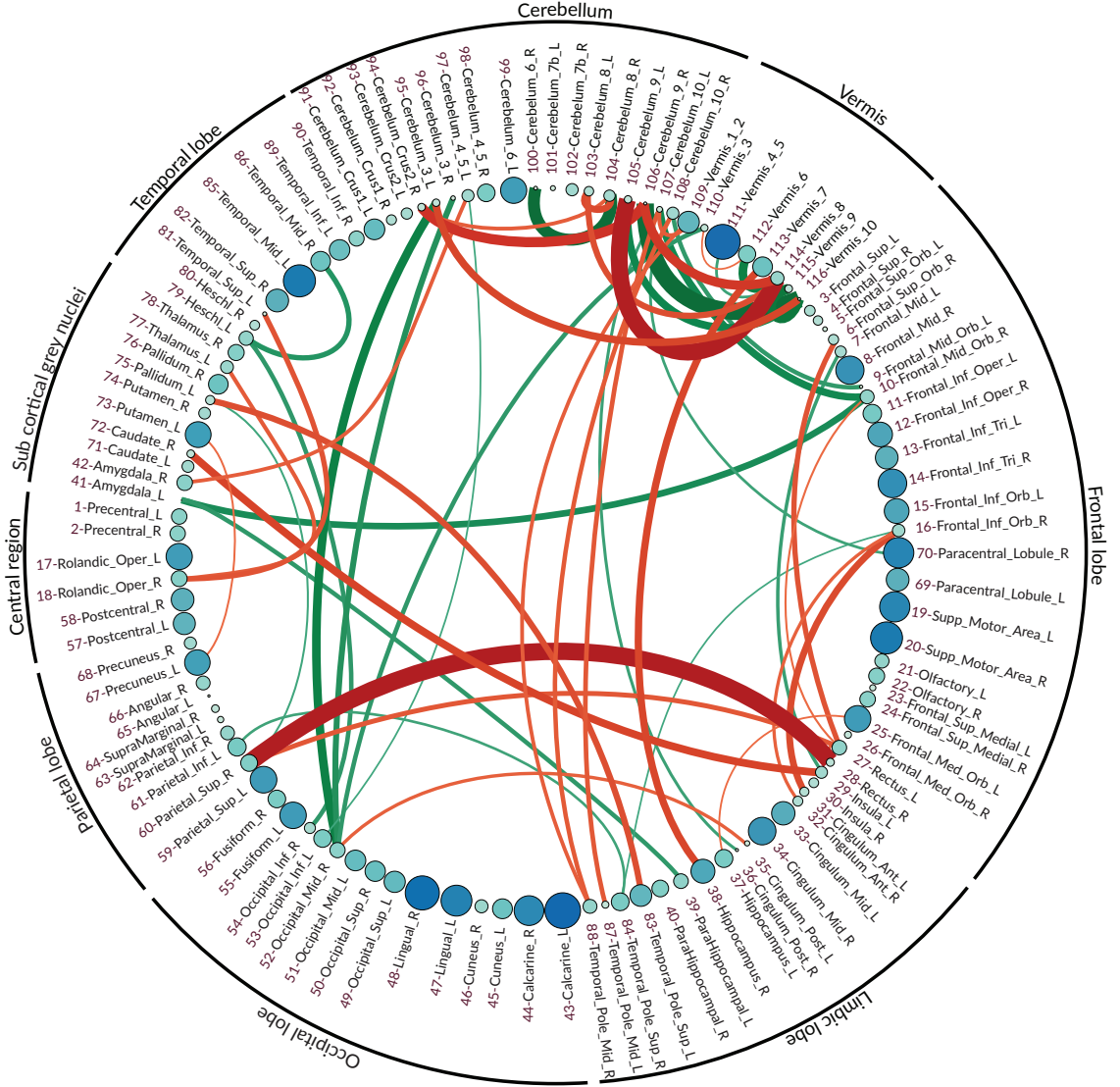
Figure 3: The difference graph. This graph is obtained via subtracting the functional connectivity of eMCI subjects from normal subjects. Each circle represents a ROI in AAL atlas and the color and size of each circle is proportional to the graph clustering coefficient of the difference graph. red = more activity in EMCI, green: less.

the orange edges shows increasing activity between corresponding ROIs in the eMCI subjects.

As it can be seen in the difference graph, the big nodes i.e. ROIs with higher activities does not necessarily establish strong connections with the other nodes. As an obvious example, higher activities in Lingual gyrus(ROI index: 47,48)[19, 20], Calcarine sulcus(ROI index: 43, 44)[21, 22], Supplementary motor area(ROI index: 19,20)[22, 23] and Temporal_mid_L(ROI index: 85)[24] are easily detectable. The majority of ROIs located in frontal lobe also shows rather high activities comparing to normal subjects[25, 5].

Similar to the nodes, the strong edge between two ROIs does not necessarily require the nodes to be highly active in eMCI. Although a strong edge does indicate high activities and functional connectivity between the two corresponding ROIs. The difference Graph shows a significant increase in connectivity between Rectus(ROI index: 28, 27 in Frontal lobe) and Parietal_Sup_R(ROI index: 60 in Parietal lobe) [33, 34], Frontal_Inf_Orb_R(ROI index: 16 in Frontal lobe) and Cingulum_Ant(ROI index: 31,32 in Limbic lobe)[35], Insula_L, Temporal_Pole_Sup_L(ROI index: 29,83 in Limbic lobe) and Pallidum_R, Caudate_R(ROI index: 29,83 in Sub Cortical Grey Nuclei)[36]. It can also be seen that within activities in frontal lobe also increased in patients with eMCI[37]. There is a decrease in connectivity between Amygdala_L(ROI index: 41 in Sub Cortical Grey Nuclei) with Frontal_Mid_Orb_R(ROI index: 10 in Sub Frontal lobe) and ParaHippocampal_L(ROI index: 39 in Sub Limbic lobe)[38]. The connectivity between Heschl_L(ROI index: 79 in Temporal lobe) and two ROIs Temporal_Mid_R(ROI index: 86 also in Temporal lobe) and Occipital_Inf_R(ROI index: 54 in Occipital lobe) also decreased in eMCI[39].

Regarding the Cerebellum and Vermis

In fMRI data analysis and especially in Alzheimer's disease studies, ROIs within the Cerebellum and Vermis are usually excluded since their role was regarded as insignificant[40, 41]. Recent studies have shown that the traditional assumption that Cerebral area is essential only for the coordination of voluntary motor activity and motor learning is not valid and indicates the significant role of the cerebellum in nervous system function, cognition, and emotion[26].

As it can be seen in the difference graph that we obtained, ROIs within Cerebellum and Vermis are highly active and both their Intra and interconnections are noticeable. There is increased functional connectivity be-

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tween the Limbic lobe especially Hippocampus_R, Temporal_Pole_Mid(ROI index: 38,87,88) and Cerebral areas in eMCI patients. Also, the connectivity between Occipital lobe, especially Occipital_mid_R(ROI index: 52), the Frontal lobe, especially in Frontal_mid_orb(ROI index: 9,10) and Cerebral areas seems to decrease in patients with eMCI.

5. Conclusion

The majority of functional connectivity analysis methods rely on calculating the FC matrix for each individual, then using simple methods to combine them in order to obtain a general FC network for a class. Also, the state of the art classification techniques use FC as the representative for each sample. In this paper, based on multilinear nature of data, we have proposed a novel framework in which the general FC is extracted directly from the Time-Region features and does not rely on individual FC calculations. Also the obtained FC by the proposed method contains some relations that recently approved experimentally. This framework also ables us to design a discriminant function that works directly with $Time \times Region$ samples rather that their FC. The new discriminant function also uses the test data in order to enhance the training set. The benefits of the proposed method could be summarize as follow: Extensive studies on the rs-fMRI provided by ADNI shows the superiority of the proposed framework in both classification and functional connectivity. The obtained FC network not only acknowledge the previous discovered connections but also reveals new connectivity patterns previously unknown. The framework proposed in this paper can be easily extended to other studies involved with high order data.

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