

# A Tensor Based Framework for fMRI Classification and Functional Connectivity Construction

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**Abstract**—Recently machine learning methods had gain lots of publicity among researchers in order to analyze the brain images such as functional Magnetic Resonance Imaging(fMRI) to obtain better understanding of the brain and brain related disease such as Alzheimer’s disease. Classification methods has been deployed in order to discriminate Alzheimer’s disease from normal controls. The majority of deployed techniques rely on constructing the functional connectivity (FC) and use the vectorized FC as the input for the classifiers which has two main drawbacks 1) The need for constructing the FC 2) The loss of possible valuable structural information in the vectorization step. Considering these problems and based on the 4D nature of the data, we have came up with a novel framework which omits the FC construction part and preserve the structural integrity of data for the classification. The proposed framework uses the High Order Singular Value Decomposition (HOSVD) in order to prune the classes and select the proper basis for each of them. This framework also allows us to obtain an FC matrix based on a class but not a single sample which helps us to shed more lights on the brain abnormalities in the Alzheimers disease at its early stages. Extensive experiments using the ADNI dataset demonstrate that our proposed framework effectively boosts the fMRI classification performance and reveals novel connectivity patterns in Alzheimer’s disease at its early stages.

**Index Terms**—Alzheimer’s disease (AD) classification, Functional Connectivity, Tensor, High Order Singular Value Decomposition, Dimension Reduction.

## I. Introduction

ALZHEIMER’S disease (AD) is a progressive neurodegenerative disorder with a long pre-morbid asymptomatic period which affects millions of elderly individuals worldwide[1]. It is predicted that the number of affected people will double in the next 20 years, and 1 in 85 people will be affected by 2050 [2]. The predominant clinical symptoms of AD include a decline in some important brain cognitive and intellectual abilities, such as memory, thinking, and reasoning. Precise diagnosis of AD, especially at its early warning stage: early Mild Cognitive Impairment (eMCI), enables treatments to delay or even avoid such disorders [3].

In recent years, brain imaging techniques like Positron Emission Tomography(PET)[21], Electroencephalography (EEG)[22] and functional Magnetic Resonance Imaging (fMRI)[23] have been used in analysis of AD. Due to the high spatial resolution and relatively lower costs, fMRI is vastly used among researchers in order to monitor brain activities especially in AD and all its stages in which

detecting abnormalities within small brain regions is essential [4]. An fMRI sample is naturally a 4D tensor consisting of 3D voxels moving in time, and each voxel contains an intensity value that is proportional to the strength of the Blood Oxygenation Level Dependent(BOLD) signal, which is a measure of the changes in blood flow, to estimate the activity of different brain regions[7]. Resting-state fMRI(rs-fMRI) is an fMRI technique in which the patient is asked to rest during the whole scan, focuses on the low-frequency ( $< 0.1Hz$ ) oscillations of BOLD signal, which presents the underlying neuronal activation patterns of brain regions[8]–[10]. rs-fMRI is usually used in order to analyze brain diseases like AD or autism[33], [34].

Since each fMRI volume consist of hundreds of thousands of voxels which are often highly correlated with the surrounding voxels in the brain volume, parcellation of the brain for further analysis has moved toward the use of anatomical atlases. These atlases are strictly defined using anatomical features of the brain, like locations of common gyri and do not rely on any functional information. To generate data using an Atlas based approach, the BOLD signal from all voxels is averaged within each brain region called Region of Interest(ROI)[9]. By putting together the average time-series for all the ROIs, the  $i$ th volume would become  $X_i \in \mathbb{R}^{T \times R}$ ,  $i = \{1, 2, \dots, S\}$  in which  $R$ ,  $T$  and  $S$  are the number of ROIs, time points and samples respectively.

There are two major studies associated with rs-fMRI data: finding common brain disorders caused by diseases like Alzheimer’s or autism, and more recently detecting patients with brain disorders using classification techniques [35], [?]. Due to the high dimensionality of data and the nature of diseases like eMCI which does not show any reliable clinical symptoms, researchers moved towards advanced machine learning techniques in order to achieve more reliable analysis [?].

A powerful tool that is commonly used in order to achieve aforementioned goals is Functional Connectivity(FC) network. FC is a *region  $\times$  region* matrix  $\bar{X}$  in which  $\bar{x}_{ij}$  represents the functional connectivity between the  $i$ th and  $j$ th ROI. Functional connectivity is an observable phenomenon quantifiable with measures of statistical dependencies, such as correlations, coherence, or transfer entropy [?]. Recent studies have shown that some brain disorders like AD could alter the way that some brain regions interact with each other. For example, compared with the healthy, AD patients have been found decreased functional connectivity between the hippocampus and

other brain regions, and MCI patients have been observed increased functional connectivity between the frontal lobe and other brain regions[4]. Although FCs show promising results, they bring their own challenges. Variety of methods exists in order to calculate the FC which cause in vastly different results.

In recent years FCs are also used as features in classification. So, instead of using  $X_i$  as the  $i^{th}$  sample its corresponding FC i.e.  $\bar{X}_i$  is used as a feature. Since the conventional classifiers like SVM work on data in vector format, these matrix features should be vectorized in order to feed them to classifiers. This vectorization leads to high-dimensional vectors which produce poor performance due to the phenomena known as the Curse of Dimensionality. Alongside the curse of dimensionality, vectorization also destroys potential information that are embedded in the structure of data. This problem has been studied especially in image data in which vectorization destroys the spatial relations within an image.REF

In this paper, based on high order tensor decomposition, we have created a framework in which the mentioned goals i.e. finding an FC for a whole class and detecting a disorder via classification could be achieved with a single High Order Singular Value Decomposition (HOSVD) of each class. Here based on latent variables obtained by HOSVD a general representative pattern of FC for eMCI and Normal subjects is obtained.

Viewing each class as a tensor allows us to work with time and region features separately but simultaneously. This multilinear view ables us to design a proper dimension reduction relative to the nature of each feature along with a discriminant function based on linear regression on latent space of samples that uses the test data to enhance the quality of the training set without forcing any a prior knowledge to the classifier, a task which is not possible through well known classifiers like SVM, logistic regression or k-NN. It is also notable that the proposed discriminant function directly works with the  $X_i$ s as features. Having the FC calculation step omitted not only heavily affects the computational performance of the method, it also saves us from the troubles of FCs mentioned before.

To verify our approach, we conduct an extensive experimental study on rs-fMRI data from the benchmark dataset ADNI As will be seen, the results well demonstrate the effectiveness and advantages of our method. Specifically, the proposed framework, not only grants us superior classification accuracy to that from other methods, it is also much faster and more stable against different data selection schemes. We have also confirmed our achieved whole-class FC matrix using empirical data on the eMCI and Normal functional connectivity patterns.

## II. eMCI classification techniques

As it was mentioned before, obtaining and classifying FC matrices have become the dominant approach towards eMCI classification. Variety of methods such as Pairwise Pearson's correlation coefficient [10], [11], sparse representation [10], [12], [13] and Sparse Inverse

Covariance Estimation (SICE)[15] exists to obtain an FC, While the first two are easy to understand and can capture pairwise functional relationship based on a pair of ROIs, the latter can account for more complex interactions among multiple ROIs, but the estimation of partial correlation involves an inversion of a covariance matrix, which may be ill-posed due to the singularity of the covariance matrix. These methods result in vastly different networks[35]. On the other hand, computing the correlations, based on the entire time series of fMRI data simply measures the FC between ROIs with a scalar value, which is fixed across time. This actually implicitly hypothesizes the Stationary interaction patterns among ROIs. As a result, this method may overlook the complex and dynamic interaction patterns among ROIs, which are essentially time-varying. In order to overcome this issue, Non-stationary methods have been proposed which results in more complex networks[16]–[19].

In the following we briefly discuss two state of the art eMCI classification techniques belonging to these two paradigms:

- **KernelCompactSICE(K – SIEC) :**

This method which belongs to the stationary paradigm was proposed in [14]. In this method, the SICE matrix is chosen as the FC for each sample, then using the SPD property of this matrix, kernel-PCA is deployed in order to reduce its dimensions.

The SICE matrix is extracted from the data sample  $S$  using the following optimization:

$$S^* = \arg \max_{S \succ 0} \log(\det(S)) - \text{tr}(CS) - \lambda \|S\|_1 \quad (1)$$

where  $C$  is the sample-based covariance matrix;  $\det()$ ,  $\text{tr}()$ , and  $\|\cdot\|_1$  denote the determinant, trace, and the sum of the absolute values of the entries of a matrix. In order to reduce the dimensionality of the obtained SICE matrix, Kernel-PCA with a Gaussian kernel is used to extract the key features. Since SICE is an SPD matrix, specific distance functions such as Log-Euclidean distance[?] or Root Stein divergence[?] can be used as the distance function in the Gaussian kernel. Analogous to linear PCA, and by defining  $\Phi(\cdot) = \text{Sym}_d^+ \mapsto \mathcal{F}$  as the kernel map, for a given SICE matrix  $S$ ,  $\Phi(S)$  can then be projected onto the top  $m$  eigenvectors to obtain an  $m$ -dimensional principal component vector. These vectors are used to train an SVM classifier. The performance of this method heavily relies on the choice of sparsity parameter  $\lambda$  and the number of top eigenvectors  $m$ .

- **HighOrderNetworks(HON) :**

This method which belongs to non-stationary paradigm uses so called High Order Networks as features for classification purposes. It uses the sliding window technique in order to split the time-series into smaller pieces and then find the relation between them[?]-[?]. Let  $x_i^{(l)}(k) \in \mathbb{R}^N$  denote the  $k$ -th segment of subseries extracted from  $x_i^{(l)}$ , which comprises  $N$  image volumes. by taking each  $x_i^{(l)}(k)$

as a node, A network can be constructed with edges defined using:

$$C_{ij}^{(l)}(k) = \text{corr} \left( x_i^{(l)}(k), x_j^{(l)}(k) \right)$$

which represents the pairwise Pearson's correlation coefficients between the  $i$ -th and the  $j$ -th ROIs of the  $l$ -th subject using the  $k$ -th segment of subseries. by taking

$$y_{ij}^{(l)} = \left[ C_{ij}^{(l)}(1), C_{ij}^{(l)}(2), \dots, C_{ij}^{(l)}(K) \right] \in \mathbb{R}^K$$

as new nodes, an other network can be calculated as follow:

$$H_{ij,pq}^{(l)} = \text{corr} \left( y_{ij}^{(l)}, y_{pq}^{(l)} \right)$$

for each pair of correlation time series  $y_{ij}$  and  $y_{pq}$  thus,  $H_{ij,pq}^{(l)}$  indicates how the correlation between the  $i$ -th and the  $j$ -th ROIs influence the correlation between the  $p$ -th and the  $q$ -th ROIs. The total number of the high-order correlation coefficients  $\{H_{ij,pq}^{(l)}\}$  is proportional to  $R^4$  which will lead to a large-scale high-order FC network, containing at least thousands of vertices and millions of edges. In order to overcome this issue, the correlation time series within each subject is grouped into different clusters. Then, the correlation calculation between the original correlation time series can be converted into that between the respective mean correlation time series in clusters. After reducing the network size, the weighted-graph local clustering coefficients was used to select the key features for each network and then an SVM classifier is trained in order to classify the obtained features.

It is noteworthy that non of these techniques consider the multi-linearity nature of the data, and since both methods use traditional classifiers like SVM or KNN, they follow a rather complex path to find vector features as the representative of each FC matrix.

### III. Proposed fMRI analysis Framework Based On Tensor framework

All main mentioned eMCI classification methods use FC of each sample as an input feature. So, the computational complexity of these methods are high due to the construction of FC matrices. In addition, the quality of the obtained FC heeavily affects the classification performance. Moreover, none of these methods attend the multi-linear propriety of such data. In this section by tensor viewpoint we show that only by one tensor decomposition we could do the following analysis on fMRI data:

- **Classification :** Viewing each class as a 3D tensor ables us to separately project each mode into a smaller one, without the necessity of unfolding it into matrices or vectors, and thus preserving the structural integrity of data along with reducing its dimensions. Transferring each sample matrix  $X_i \in \mathbb{R}^{T \times R}$  into the new feature space granted by tensor viewpoint, obsoletes the necessity of constructing the FC for each sample by producing a high quality and low-dimensional feature  $\bar{X}_i \in \mathbb{R}^{\bar{T} \times \bar{R}}$  in which  $\bar{T}$  and  $\bar{R}$  are drastically smaller that  $T$  and  $R$ . This

viewpoint also ables us to design a novel discriminant function in which the test data is used in the training process without forcing any apriory knowledge about its label to the classifier, a task which is impossible via the conventional classifiers such as SVM, K-NN or logistic regression.

- **General FC :** Using the components of HOSVD extracted in the previous step, a general FC could be constructed for each class that reveals patterns common shared among all samples within each class. This technique allows us to discard the role of outliers or noisy samples.

#### A. A Classification of Region-Time data of eMCI and normal data based on Tensor framework

For reducing the computational complexity and reducing the occurrence of over fitting, specially for data with large features (Like fMRI data), using dimensionality reduction is inevitable. Although each sample  $X \in \mathbb{R}^{T \times R}$  has two different time and region features, the classical methods like PCA, SVD ,... only could work on vectorized version  $x = \text{vec}(X)$  of such data. Although this approach is easy to deploy, it has several drawbacks like occurrence of Curse of dimensionality and mixing different features(time and region). Recently multilinear dimension reduction methods like MPCA, GLRAM have been proposed that could works with multidimensional data, without folding them into vectors. In these methods there is a freedom to select specific reduction for each kind of feature. In this section we will used well known tensor decomposition named HOSVD for dimension reduction and also classification of fMRI data.

Let tensors  $\mathcal{X}^{(i)} \in \mathbb{R}^{T \times R \times S_i}$ , consists normal and eMCI data, for  $i=1,2$ , respectively. Here  $S_1, S_2$  are the number of normal and eMCI data. For tensor  $\mathcal{X}^{(i)}$ , the decomposition

$$\mathcal{X}^{(i)} = \left( U^{(i)}, V^{(i)}, W^{(i)} \right) \cdot \mathcal{S}^{(i)}, \quad (2)$$

is known as higher order singular decomposition(HOSVD), where orthogonal matrices  $U^{(i)} \in \mathbb{R}^{T \times T}$ ,  $V^{(i)} \in \mathbb{R}^{R \times R}$  and  $W^{(i)} \in \mathbb{R}^{S_i \times S_i}$  are known as modes-1,2,3 singular matrices of and  $\mathcal{S}^{(i)}$  is the corresponding core tensor Ref?. Here  $U^{(i)}$  is a base of all mode-1 fibers  $\mathcal{X}(:, l, k)$ . Here  $\mathcal{X}^{(i)}(:, l, k)$  indicates the behavior of  $l$ th region of the  $k$ th sample of the  $i$ th class in all times. Also  $V^{(i)}$  is a base of all mode-2 fibers  $\mathcal{X}(l, :, k)$  which indicates the behavior of all regions of  $l$ th sample of the  $i$ th class in the  $k$ th time. Also, due to the properties of HOSVD inherited from svd, the first columns of mode- $k$  ( $k=1,2,3$ ) has more ability in construction of main parts of  $k$ th fibers and on the other hand, the last columns of this singular matrix, are corresponding to noise parts of the fibers of the mode ref??. Therefore, with appropriate values of  $k_1^i$  and  $k_2^i$  projection of mode-1 and mode-2 fibers into space spanned by the first  $k_1$  and  $k_2$  singular vectors of modes-1,2, which are denoted by  $U_{k_1^i}^{(i)}$  and  $V_{k_2^i}^{(i)}$ , respectively, is a suitable

dimension reduction. This dimensionality reduction could be done as

$$\mathbb{R}^{k_1 \times k_2 \times S_i} \ni \bar{\mathcal{X}}^{(i)} = \left( U_{k_1^i}^{(i)\top}, V_{k_2^i}^{(i)\top} \right)_{1,2} \cdot \mathcal{X}^{(i)} \quad (3)$$

Here it's clear that the reduced version of the  $k^{th}$  sample, i.e.,  $\bar{\mathcal{X}}(:, :, k) \in \mathbb{R}^{k_1 \times k_2}$  could be reduced separately in each mode without folding. This means that the structure of data is preserved in the reducing process. Base on the properties of the HOSVD, it could be shown that by small number of  $k_1^i, k_2^i$ , the reduced data have good reconstruction error.

In the following inspired by the structure of this reduction, we present a tensor based discrimination function. By HOSVD decomposition of  $\mathcal{X}^{(i)}$  the projected data  $\bar{\mathcal{X}}^{(i)}$  in equation (??) becomes

$$\begin{aligned} \bar{\mathcal{X}}^{(i)} &= ([I_{k_1^i} \ 0], [I_{k_2^i} \ 0], W) \cdot \mathcal{S}^{(i)} \\ &= (W)_3 \cdot \mathcal{S}^{(i)}(1 : k_1^i, 1 : k_2^i, :) \end{aligned}$$

So, each sample of the  $i^{th}$  class in the reduced space has the following form

$$\begin{aligned} \bar{\mathcal{X}}^{(i)}(:, :, k) &= \left( W^{(i)}(k, :) \right)_3 \cdot \mathcal{S}^{(i)}(1 : k_1^i, 1 : k_2^i, :) \\ &= \sum_{k'=1}^{S_i} W^{(i)}(k, k') \cdot \mathcal{S}^{(i)}(1 : k_1^i, 1 : k_2^i, k'). \end{aligned}$$

This means that each sample in the  $i^{th}$  class could be represented as linear combination of the slices of the tensor  $\bar{\mathcal{S}}^{(i)} = \mathcal{S}^{(i)}(1 : k_1^i, 1 : k_2^i, :)$ . So if a test data like  $X \in \mathbb{R}^{T \times R}$ , be in the  $i^{th}$  class it's natural to expect that its projected version into principle region and times spaces, spanned by  $U_{k_1^i}, V_{k_2^i}$ , i.e.,

$$Z^{(i)} = \left( U_{k_1^i}^{(i)\top}, V_{k_2^i}^{(i)\top} \right)_{1,2} \cdot X$$

could be approximated well as a linear combination of the slices of the tensor  $\bar{\mathcal{S}}^{(i)}$  as follows

$$Z^{(i)} \approx \sum_{k=1}^{S_i} \lambda_k^i \bar{\mathcal{S}}^{(i)}(:, :, k). \quad (4)$$

Based on this viewpoint, each test data  $X$  could be assigned to a class that its projected version have the best approximation in the form (4). Due to importance of core tensor elements with small indices in reconstruction of the signal part of data in comparison with the last parts, the small number  $k_3^i < S_i$  of slices  $\bar{\mathcal{S}}^{(i)}(:, :, k)$  could be used in (4).

In this viewpoint each test data  $X$  assignment to the  $l^{th}$  class, if

$$r_l = \min_{i=1,2} r_i,$$

where

$$r_i = \min_{\lambda^i} \|Z^{(i)} - \sum_{k=1}^{k_3^i} \lambda_k^i \bar{\mathcal{S}}^{(i)}(:, :, k)\|, \quad \lambda^i = \begin{pmatrix} \lambda_1^i \\ \vdots \\ \lambda_{k_3^i}^i \end{pmatrix} \quad (5)$$

shows the reconstruction error of the projected version of  $X$  in the  $i^{th}$  class. The minimization (5) is a simple least

square problem that could be solved easily. The proposed method have an interesting property that bring us to propose a novel method to improve its quality. By the properties of HOSVD, the principle properties of the  $i^{th}$  class could be reflected in the slices of  $\bar{\mathcal{S}}^{(i)}$ . Also, for small indices these Slices have a better role in construction of main properties of this class. So the first slices of  $\bar{\mathcal{S}}$  could represent signal parts, while last ones do not this role and sometimes represents the waste parts. Now consider the test data  $X$  added to data set  $\mathcal{X}^{(i)}$  of the  $i^{th}$  class. So new data set will be  $\tilde{\mathcal{X}} \in \mathbb{R}^{T \times R \times (S_i+1)}$ . For example

$$\begin{aligned} \tilde{\mathcal{X}}^{(i)}(:, :, 1 : S_i) &= \mathcal{X}^{(i)}, \\ \tilde{\mathcal{X}}^{(i)}(:, :, S_i+1) &= X. \end{aligned}$$

If  $X$  belongs to this class then in HOSVD of this tensor  $X$  reinforce the slices of core tensor with small indices. But when it dose not belong to this class it will changes the behavior of last slices of core tensor of new tensor. This means that before classification of a test data  $X$ , We could added it to both classes. This addition, will changed the first slices of core tensor when it belongs to this class or will changed the last Slices when dose not belong. But in our classification method only the first Slices of core tensor are exits. Also the elements of  $S$  in the first and second modes are filtered and we work with  $S(1 : k_1^i, 1 : k_2^i, 1 : k_3^i)$ . This means that by addition of  $X$  in both classes for class that it belongs to it, the first slices in (5), will be adapted to have good reconstruction for this data. But for a class that dose not belong to, this addition have small changes in the slices in (5). It should be mentioned that since  $X$  added to both data sets, so we did not use its label and the method in true. After computing the HOSVD of this new data sets  $\tilde{\mathcal{X}}^{(i)}$ , we apply the method in (5) for classification. Algorithm 1 summarized the proposed classification method.

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Algorithm 1 TNBeMCI: Tensor based Classification method

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- 1) Input: Normal train data  $\mathcal{X}^{(1)}$ , eMCI train data  $\mathcal{X}^{(2)}$   
 $k_i^j, i = 1, 2, 3, \quad j = 1, 2.$   
 Test data  $X$
  - 2) Construct  $\tilde{\mathcal{X}}^{(i)}$  for  $i = 1, 2$  by adding  $X$ .
  - 3) Compute  $U_{k_1^i}, V_{k_2^i}$  and  $\mathcal{S}(1 : k_1^i, 1 : k_2^i, k_3^i)$  of  $\tilde{\mathcal{X}}^{(i)}$ .
  - 4) Compute  $Z^{(i)} = \left( U_{k_1^i}^{(i)\top}, V_{k_2^i}^{(i)\top} \right)_{1,2} \cdot X, i = 1, 2.$
  - 5) Compute  $r_1, r_2$  from (5)
  - 6) Assign  $X$  to class  $l$ , if  $l = \arg \min_i \{r_i\}$
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In this section by HOSVD decomposition on both normal and eMCI data, we proposed a novel tensor based classification. The benefits of the proposed tensor based classification method could be summarized as follow

- This method uses multi linear property of region-Time matrix data and could works with time and region features separately based on their specific bases(corresponding singular matrices). This means that the classification works on data without folding them into vectors.

- In this classification, the test data has a role in construction of bases for both classes, without using its label. This increase the quality of the discrimination. This could not applied on important classification methods like SVM, logistic regression classifier and neuronal networks.
- This method works with time-region features, and dose not need to have FC matrices for each sample. So its computational complexity is more less than other state of the art methods based on FC features. Also in this method we do not wary about the quality of FC methods. It should be mentioned that our method also could be applied on FC matrices as input features. But in experiments the proposed method gives better results on original time-region features.

In the experiments we compare the quality of the method with some of the sate of the art methods for recognition of eMCI like mentioned k-SICE and HON . Experimental results confirm the quality of the proposed method. In the next section we show that based the obtained HOSVD decomposition for both classes one could obtain appropriate General patterns for normal and eMCI data.

#### B. General Functional Connectivity for Normal and eMCI by tensor framework

As it was mentioned before, one of the main studies associated with rs-fMRI analysis is finding common functional disorders cause by a disease like AD. This can be done via constructing proper FC matrices. The majority of techniques calculate the FC matrix for each individual subject(like SICE). This may overlook tiny but common connectivities shared within a class. It is also noteworthy that the majority of non-stationary methods are not capable of constructing a relatable FC since the concept of a physical ROI is not well defined in them.

In this section we show that based on HOSVD decomposition one could obtain one representative functional connectivity for each normal or eMCI classes without obtaining the per-sample FC of all data separately. Here the classification is not our goal, instead finding a general and representative relation of regions for eMCI and normal person is our demand. This general pattern could be used clinically by expert cognitive scientists to found functional relation disorders caused by Alzheimer's disease.

As we know in HOSVD the singular matrices  $U, V, W$ , are the base of time, region features and also the samples, receptively. In the laset section by property of these matrices we designed our classification method. know in this section we show that , the same idea could helps us to define a general FC matrix based on HOSVD decomposition for normal and eMCI data. It should be mentioned that here we did not use the FC of per-samples to construct this general FC matrix.

In tensor  $\mathcal{X}^{(i)}$  of the  $l^{th}$  class, the slice  $\mathcal{X}^{(i)}(:, l, :)$  denotes the behavior of  $l^{th}$  region of all samples in all times in the  $i^{th}$  class. So this could be consider as a feature of the  $l^{th}$  region of the  $i^{th}$  class and each region is shown

with an Times-sample feature matrix. Viewing each region as a slice would allow us to consider it's behavior in all time points and across all samples, which itself allows us to shed more light on common properties and ignore individual differences that is highly possible due to the presence of noise and outliers. So, by the properties of singular matrices in modes-1,3, for appropriate values  $k_1^i, k_3^i$ , each region  $\mathcal{X}(:, l, :)$  could be reduced in both time and sample features, separately based on mode-1 and mode-3 truncated singular matrices  $U_{k_1^i}^{(i)}$  and  $W_{k_3^i}^{(i)}$  as follows

$$\mathcal{Y}^{(i)}(:, l, :) = \left( U_{k_1^i}^{(i)\top}, W_{k_3^i}^{(i)\top} \right)_{1,3} \cdot \mathcal{X}^{(i)}(:, l, :). \quad (6)$$

Here  $\mathcal{Y}^{(i)}(:, l, :)$  denotes a reduced version of  $\mathcal{X}^{(i)}(:, l, :)$  into space spanned by  $U_{k_1^i}^{(i)}$  and  $W_{k_3^i}^{(i)}$  in modes-1,3. So,

$$\mathbb{R}^{k_1^i \times R \times k_3^i} \ni \mathcal{Y}^{(i)} = \left( U_{k_1^i}^{(i)\top}, W_{k_3^i}^{(i)\top} \right)_{1,3} \cdot \mathcal{X}^{(i)} \quad (7)$$

denote all reduced regions of the  $i^{th}$  class. By this structure and substituting the HOSVD decomposition of  $\mathcal{X}^{(i)}$  in (??), we obtain

$$\begin{aligned} \mathcal{Y}^{(i)} &= ([I_{k_1^i} \quad 0], V, [I_{k_3^i} \quad 0]) \cdot \mathcal{S}^{(i)} \\ &= (V)_2 \cdot \mathcal{S}^{(i)}(1 : k_1^i, :, 1 : k_3^i) \end{aligned}$$

and so

$$\begin{aligned} \mathcal{Y}^{(i)}(:, k, :) &= \sum_{k'}^R V^{(i)}(k, k') \bar{\mathcal{C}}^{(i)}(:, k', :) \\ &= \left( V^{(i)}(k, :) \right)_2 \cdot \mathcal{C}^{(i)} \end{aligned} \quad (8)$$

in which

$$\mathbb{R}^{k_1^i \times R \times k_3^i} \ni \mathcal{C}^{(i)} = \mathcal{S}(1 : k_1^i, :, 1 : k_3^i).$$

The equation (10), show that the reduced version of each region in the  $i^{th}$  class could be written as the linear combinations of mode-2 slices of  $\mathcal{C}^{(i)}$ . So the coefficients of slices in this linear combination could be considered as a new feature for the  $l^{th}$  region of the  $i^{th}$  class. Also as we mentioned the first slices are better than the last ones to reflect the principle properties of the data. So for appropriate  $k_3^i$  we could select only the fits coefficient in (10) as new features for the  $l^{th}$  region. Mathematically this means each region in the  $i^{th}$  class could be represented by new feature  $V(l, 1; k_3^i) \in \mathbb{R}^{k_3^i}$ .

The main benefit of this approach is that each region could be represented only be a vector with size  $k_3^i$ , instead large feature matrix time-sample. Now different methods could be used to find the correlation of reigns based on this new type of feature and clean matrix  $V(:, 1 : k_3^i)$  which its rows corresponding to different regions and columns are new features. Due to quality of Sparse Inverse Covariance , this method is applied the obtained feature-region matrix  $V(:, 1 : k_3^i)^\top$  in order to find the functional connectivity of the  $i^{th}$  class.



## IV. EXPERIMENTAL STUDY

### A. Data Preprocessing and Experimental Settings

Rs-fMRI data of 196 subjects were downloaded from the ADNI website<sup>1</sup>. Nine subjects were discarded due to the corruption of data, and the remaining 187 subjects were preprocessed for analysis. After removing subjects that had problems in the preprocessing steps, such as large head motion, 156 subjects were kept, including 26 AD, 44 early MCI, 38 late MCI, 38 NC, and ten significant memory concern labeled by ADNI. We used the 38 NC and the 44 early MCI because our focus in this paper is to identify MCI at very early stage, which is the most challenging and significant task in AD prediction. The IDs of the 82 (38 NC and 44 early MCI) subjects are provided in the supplementary material.

The data are acquired on a 3-T (Philips) scanner with TR/TE set as 3000/30 ms and flip angle of 80. Each series has 140 volumes, and each volume consists of 48 slices of image matrices with dimensions  $64 \times 64$  with voxel size of  $3.31 \times 3.31 \times 3.31 \text{ mm}^3$ . The preprocessing is carried out using SPM12 and DPARSFA [40]. The first ten volumes of each series are discarded for signal equilibrium. Slice timing, head motion correction, and MNI space normalization are performed. Participants with too much head motion are excluded. The normalized brain images are warped into automatic anatomical labeling (AAL) [41] atlas to obtain 116 ROIs as nodes. By following common practice [15]–[17], the ROI mean time series are extracted by averaging the time series from all voxels within each ROI and then bandpass filtered to obtain multiple subbands as in [17].

### B. Classification

Almost every subject in ADNI dataset has several scans. Usually a random scan data is selected and enters the processing step. This random selection may cause several problems [ref](#). Since the number of train data is very low, a small perturbation in it could drastically change the set of input parameters in order to achieve the highest prediction accuracy and other classification evaluation methods. Also achieving high quality results with a classifier does not guarantee its effectiveness on other datasets even with fine tuning the parameters since the training set may contain outliers and unidentified corrupted data. In order to show that the proposed framework is less sensitive against the choice of different perturbations and is less vulnerable towards the aforementioned issues, we have selected 18 different perturbations and two test state of the art classification methods on them: HON and k-SICE. To make full use of the limited subjects, a leave-one-out procedure is used for training and test. That is, each sample is reserved for test in turn, while the remaining samples are used for training. We have use five evaluation measures: accuracy (ACC), sensitivity (SEN), Youden's

TABLE I  
The Average of Different Classification Measurements in all perturbations in %

Method	ACC	F-Score	SEN	SPE	YI	BAC
k-SICE	75.57	77.36	78.50	72.19	50.69	75.34
FON	75.66	77.44	78.40	72.48	50.89	75.44
Proposed	80.43	82.20	84.60	75.59	60.20	80.09

index(YI), F-score, and balanced accuracy (BAC). [Tan Book](#)

In this article, we treat the eMCI samples as positive class and the NC samples as negative class.

1) Classification performance: The classification accuracy measure(ACC), After fine-tuning the input parameter set for each method, shows that for 16 out of 18 different perturbations, our approach works better than k-SICE, the same also holds for 15 datasets comparing to HON. i.e. in 88.8% of datasets, proposed method works better than k-SICE and in 83.3% of datasets, it works better than FON. The highest classification accuracy(86.59%) is achieved with the proposed method in the 15th perturbation. The highest accuracy for the HON (84.15%) is achieved in the 14th, and the highest accuracy for the SICE method (85.37%) is achieved in the 6th perturbation. As it was mentioned before, being stable when the input dataset changes is a very important aspect for a classifier, in order to measure the stability, standard deviation of accuracy along with other measures are calculated. The std. of accuracy for proposed method is 0.64 times less than HON and 1.73 times less than SICE method. Similar results also holds for other classification measures.

Figure (3) shows the performance of these three methods in all five measurements. Some statistical information about these plots are also included in the embedded table. As it can be seen in this figure, similar to the accuracy, the proposed method in overall works much better than FON and k-SICE. For a better Demonstration, table (I) provides the average of several classification measurements scores for all permutations. As it can be seen in this table, the average accuracy of Proposed method which is 80.43% is 4.77% higher than the next method HON, and 4.86% better than k-SICE. It is noteworthy that The other two methods i.e HON and SICE shows similar results in average.

2) Runtime Comparison: One other key features of proposed method is that it works significantly faster than the other two methods. Table (II) shows the average elapsed time (Training plus Testing) of each method for all selected permutations. These methods were executed in matlab R2017b and carried with an intel Core-i7 processor and 16GB of RAM. As it can be seen in this table, proposed method is more than 600 times faster than HON and 20 times faster than SICE. Having a huge execution time specially affects the parameter selection for HON, since it uses cross-validation procedure in order to find

<sup>1</sup><http://adni.loni.usc.edu>

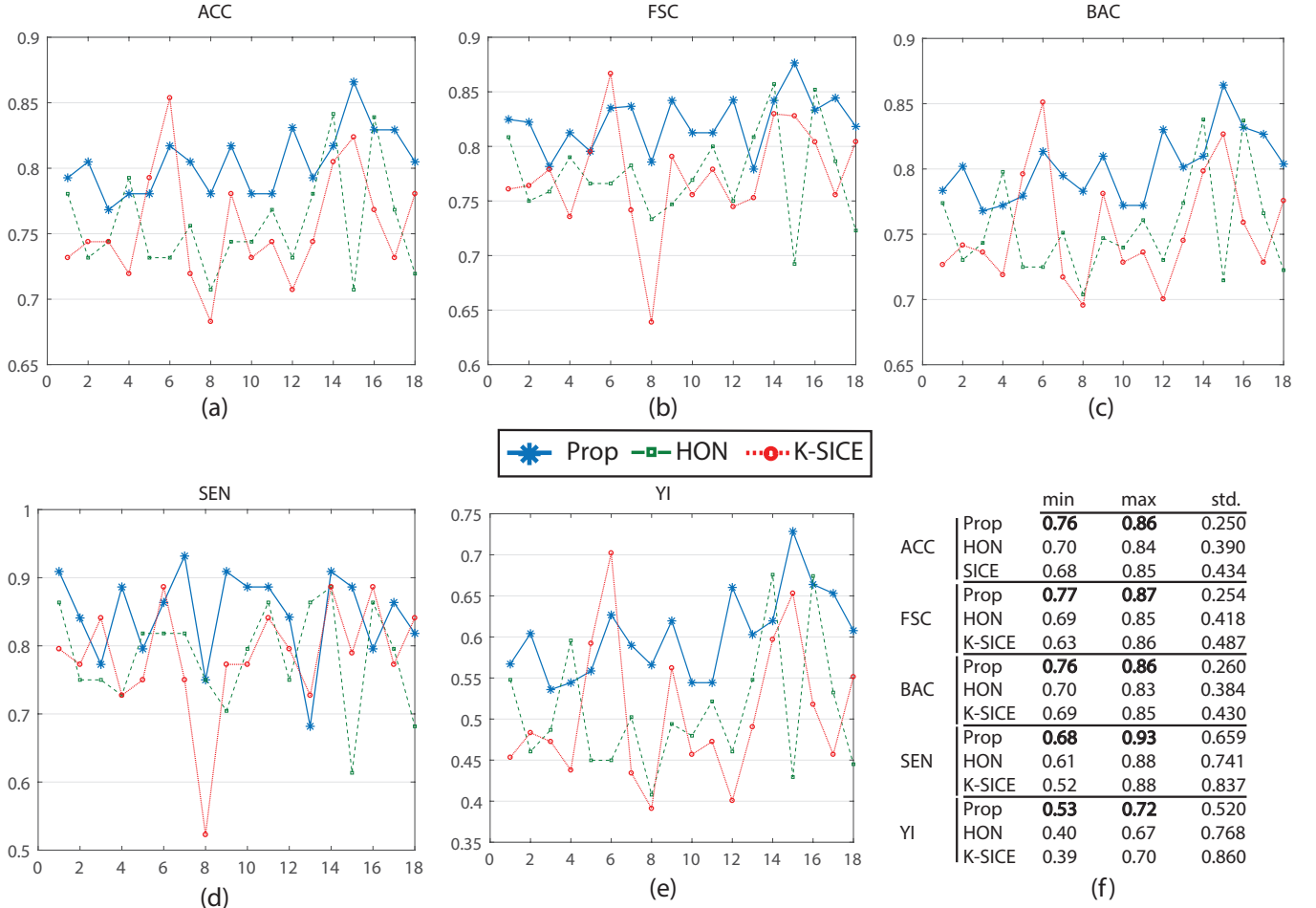


Fig. 1. Comparison of proposed method(Prop) with K-SICE and HON in five different classification evaluation measures along with the standard deviation of each one. As it can be seen, the both the minimum and maximum of the proposed methods in these measurements are higher than the other two. Also the lower std. of our method indicates its stability.

TABLE II  
Elapsed time of the test and train phase in seconds

Method	HON	k-SICE	proposed method
Elapsed Time	6950	230	11

the optimal parameters which itself require several runs of the algorithm.

### C. Functional connectivity Network

The functional connectivity networks of the Normal and eMCI classes was obtained via proposed method as it is described in (III-B). In order to better highlight the differences between Normal and eMCI subjects, a difference graph  $D$  is constructed by subtracting the Normal FC from the eMCI FC. This graph could be seen in Figure(4). The nodes of  $D$  shows the ROIs according to the AAL atlas. The size of each node is proportional to its graph clustering coefficient, i.e. the bigger node, demonstrates higher activity in eMCI subjects in the corresponding ROI. Similar to nodes, the size of each

edge is also proportional to the correlation between two ROIs. In addition, the edges are also color coded in a way that the green edges shows the positive edges in  $D$  and the orange edges shows the negative edges in  $D$ . In this manner, the green edges demonstrates decreasing in activity between the corresponding nodes in eMCI subjects and vice versa, the orange edges shows increasing activity between corresponding ROIs in the eMCI subjects.

As it can be seen in the difference graph, the big nodes i.e. ROIs with higher activities does not necessarily establish strong connections with the other nodes. As an obvious example, higher activities in Lingual gyrus(ROI index: 47,48)[24], [25], Calcarine sulcus(ROI index: 43, 44)[26], [27], Supplementary motor area(ROI index: 19,20)[27], [28] and Temporal\_mid\_L(ROI index: 85)[29] are easily detectable. The majority of ROIs located in frontal lobe also shows rather high activities comparing to normal subjects[30], [31].

Similar to the nodes, strong edge between two ROIs does not necessarily requires the nodes to be highly active in eMCI. Although a strong edge does indicate high activities and functional connectivity between the two corresponding ROIs. The difference Graph shows significant

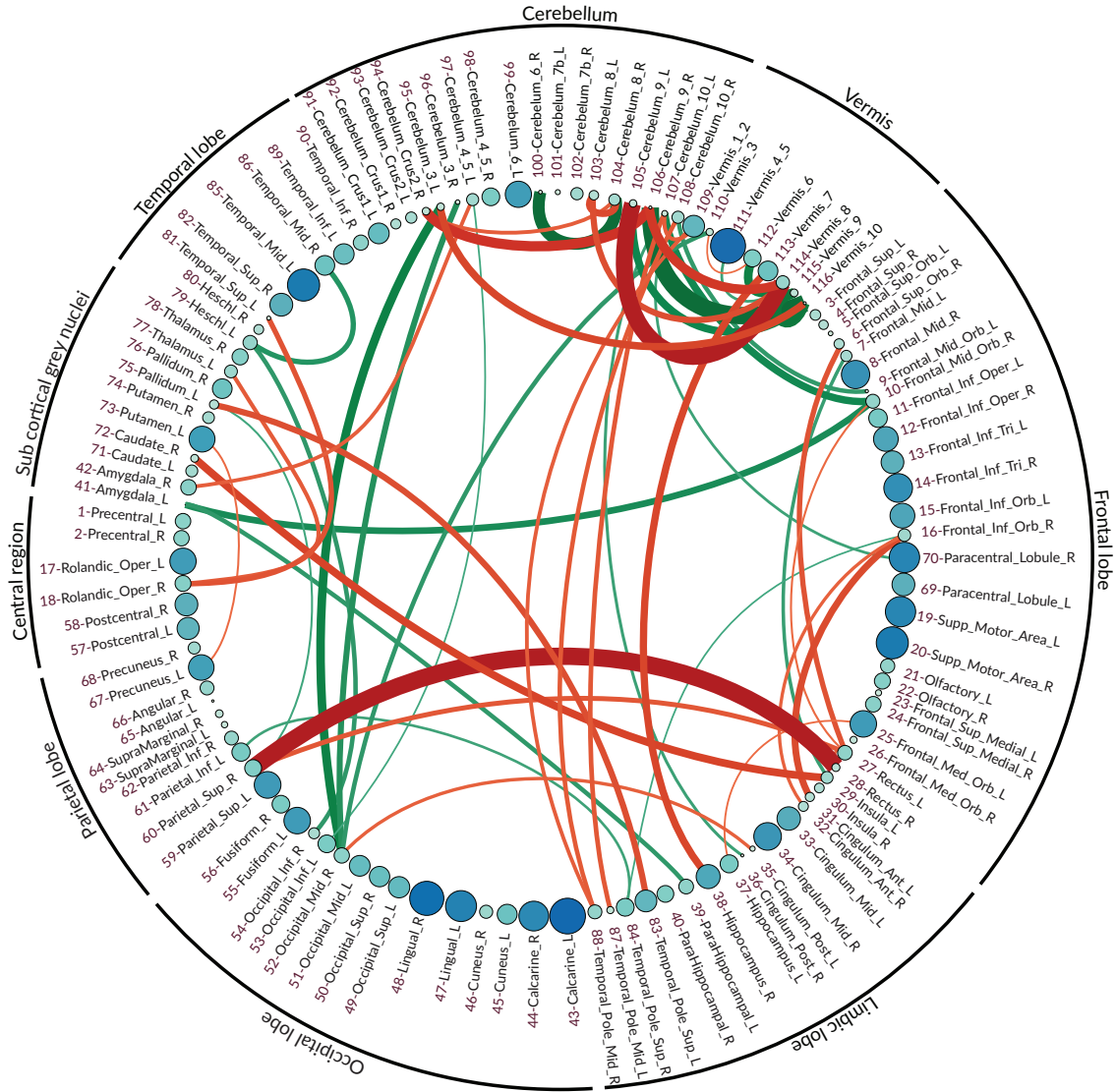


Fig. 2. The difference graph. This graph is obtained via subtracting the functional connectivity of eMCI subjects from normal subjects. Each circle represents a ROI in AAL atlas and the color and size of each circle is proportional to the graph clustering coefficient of the difference graph. red = more activity in eMCI, green: less.

increase in connectivity between Rectus (ROI index: 28, 27 in Frontal lobe) and Parietal\_Sup\_R (ROI index: 60 in Parietal lobe) [?], [?], Frontal\_Inf\_Orb\_R (ROI index: 16 in Frontal lobe) and Cingulum\_Ant (ROI index: 31, 32 in Limbic lobe) [?], Insula\_L, Temporal\_Pole\_Sup\_L (ROI index: 29, 83 in Limbic lobe) and Pallidum\_R, Caudate\_R (ROI index: 29, 83 in Sub Cortical Grey Nuclei) [?]. It can also be seen that within activities in frontal lobe also increased in patients with eMCI [?]. There is a decrease in connectivity between Amygdala\_L (ROI index: 41 in Sub Cortical Grey Nuclei) with Frontal\_Mid\_Orb\_R (ROI index: 10 in Sub Frontal lobe) and ParaHippocampal\_L (ROI index: 39 in Sub Limbic lobe) [?]. The connectivity between Heschl\_L (ROI index: 79 in Temporal lobe) and two ROIs Temporal\_Mid\_R (ROI index: 86 also in Temporal lobe) and Occipital\_Inf\_R (ROI index: 54 in Occipital lobe) also decreased in eMCI [?].

Regarding the Cerebellum and Vermis: In fMRI data analysis and especially in Alzheimer's disease studies, ROIs within the Cerebellum and Vermis are usually excluded since their role was regarded as insignificant [?], [?]. Recent studies have shown that the traditional assumption that Cerebral area is essential only for the coordination of voluntary motor activity and motor learning is not valid and indicates the significant role of cerebellum in nervous system function, cognition and emotion [32].

As it can be seen in the difference graph that we obtained, ROIs within Cerebellum and Vermis are highly active and both their intra and inter connections are noticeable. There is an increasing functional connectivity between the Limbic lobe especially Hippocampus\_R, Temporal\_Pole\_Mid (ROI index: 38, 87, 88) and Cerebral areas in eMCI patients. Also, the connectivity between Occipital lobe, especially Occipital\_mid\_R (ROI index:



52), the Frontal lobe, especially in Frontal\_mid\_orb(ROI index: 9,10) and Cerebral areas seems to decrease in patients with eMCI.

### V. Conclusion

The majority of classification techniques uses the vectorized version of data as the input of the discriminant function. As the number of the dimensions grows, i.e. when data is naturally a high order tensor, this vectorization become problematic and it would highly affect the performance. Taking advantage of the techniques designed for the tensors, we have developed a framework for fMRI data analysis in which the following objectives:

- 1) Classification
- 2) General Functional Connectivity network

are achieved via a single High Order SVD of the input tensors.

Extensive studies on the rs-fMRI provided by ADNI shows the superiority of the proposed framework in both classification and functional connectivity. The obtained FC network not only acknowledge the previous discovered connections but also reveals new connectivity patterns previously unknown. The framework proposed in this paper can be easily extended to other studies involved with high order data.

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