

Multi-way Feature Extraction and Selection for Alzheimers Disease Early Detection

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Abstract—Recently machine learning methods had gain lots of publicity among researchers in order to analyze the brain images such as functional Magnetic Resonance Imaging(fMRI) to obtain better understanding of the brain and brain related disease such as Alzheimer’s disease. Classification methods has been deployed in order to discriminate Alzheimer’s disease from normal controls. The majority of deployed techniques rely on constructing the functional connectivity (FC) and use the vectorized FC as the input for the classifiers which has two main drawbacks 1) The need for constructing the FC 2) The loss of possible valuable structural information in the vectorization step. Considering these problems and based on the 4D nature of the data, we have came up with a novel framework which omits the FC construction part and preserve the structural integrity of data for the classification. The proposed framework uses the High Order Singular Value Decomposition (HOSVD) in order to prune the classes and select the proper basis for each of them. This framework also allows us to obtain an FC matrix based on a class but not a single sample which helps us to shed more lights on the brain abnormalities in the Alzheimers disease at its early stages. Extensive experiments using the ADNI dataset demonstrate that our proposed framework effectively boosts the fMRI classification performance in Alzheimer’s disease.

Index Terms—IEEE, IEEEtran, journal, LATEX, paper, template.

I. INTRODUCTION

ALZHEIMERS disease (AD) is a progressive neurodegenerative disorder with a long pre-morbid asymptomatic period [1] which affects millions of elderly individuals worldwide. It is predicted that the number of affected people will double in the next 20 years, and 1 in 85 people will be affected by 2050 [2]. The predominant clinical symptoms of AD include a decline in some important brain cognitive and intellectual abilities, such as memory, thinking, and reasoning. Precise diagnosis of AD, especially at its early warning stage: early Mild Cognitive Impairment (eMCI), enables treatments to delay or even avoid such disorders [3].

In recent years, brain imaging techniques like Positron Emission Tomography(PET) [21], Electroencephalography (EEG)[22] and functional Magnetic Resonance Imaging (fMRI)[23] have been used in analysis of AD. Due to the high spatial resolution and relatively lower costs, fMRI is vastly used among researchers in order to monitor brain activities especially in AD and all it’s stages in which detecting abnormalities within small brain regions is essential. An fMRI sample is naturally a 4D tensor consisting of 3D voxels moving

in time, and each voxel contains an intensity value that is proportional to the strength of the Blood Oxygenation Level Dependent(BOLD) signal, which is a measure of the changes in blood flow, to estimate the active regions in the brain[7]. Resting State fMRI(rs-fMRI) is an fMRI technique in which the patient is asked to rest during the whole scan, focuses on the low-frequency ($< 0.1Hz$) oscillations of BOLD signal, which presents the underlying neuronal activation patterns of brain regions[8][10]. rs-fMRI is usually used in order to analyze the brain diseases like AD or autism[33], [34]

Since each fMRI volume consist of hundreds of thousands of voxels which are often highly correlated with the surrounding voxels in the brain volume, parcellation of the brain for further analysis has moved toward the use of anatomical atlases. These atlases are strictly defined using anatomical features of the brain, like locations of common gyri and do not rely on any functional information. To generate data using an atlas based approach, the BOLD signal from all voxels is averaged within each brain region called Region of Interest(ROI)[9]. By putting together the average time-series for all the ROIs, the i th volume would become $X_i \in \mathbb{R}^{T \times R}$, $i = \{1, 2, \dots, S\}$ in which R , T and S are the number of ROIs, time points and samples respectively. The process of obtaining such matrix is shown in Figure (1).

There are two major studies associated with rs-fMRI data: finding common brain disorders caused by diseases like Alzheimer’s or autism, and more recently detecting patients with brain disorders using classification techniques. Due to the high dimensionality of data and the nature of diseases like eMCI which does not show any reliable clinical symptoms, researchers moved towards advanced machine learning techniques in order to achieve more reliable analysis.

A powerful tool that is commonly used in order to achieve aforementioned goals is Functional Connectivity(FC) network. FC is a *region \times region* matrix \tilde{X} in which \tilde{x}_{ij} represents the functional connectivity between the i th and j th ROI. Functional connectivity is an observable phenomenon quantifiable with measures of statistical dependencies, such as correlations, coherence, or transfer entropy([11]). Recent studies have shown that some brain disorders like AD could alter the way that some brain regions interact with each other. For example, compared with the healthy, AD patients have been found decreased functional connectivity between hippocampus and other brain regions, and MCI patients have been observed increased functional connectivity between the frontal lobe and other brain regions[4]. Although FCs show promising results, they bring their own challenges. Variety of methods such as Pairwise Pearsons correlation coefficient [10], [11], sparse representation [10], [12], [13] and Sparse Inverse

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Covariance Estimation (SICE) exists to obtain an FC, While the first two are easy to understand and can capture pairwise functional relationship based on a pair of ROIs, the latter can account for more complex interactions among multiple ROIs, but the estimation of partial correlation involves an inversion of a covariance matrix, which may be ill-posed due to the singularity of the covariance matrix. These methods results in vastly different networks. On the other hand, computing the correlation based on the entire time series of fMRI data simply measures the FC between ROIs with a scalar value, which is fixed across time. This actually implicitly hypothesizes the **Stationary** interaction patterns among ROIs. As a result, this method may overlook the complex and dynamic interaction patterns among ROIs, which are essentially time-varying [16]–[19]. In order to overcome this issue, **Non-stationary** methods have been proposed which results in more complex networks.

Finding an FC that highlights the patterns caused by a disease has been a common goal in rs-fMRI study for a long time. Several approaches exists to find common patterns among different brain scans. Data driven methods such as kernel-PCA or clustering techniques have been proposed for this task. But ultimately most of them rely on calculating a network for each volume. This may overlook the role of noises or outliers within the data. As we will show later, our proposed method does not rely on any individual FC calculations and treats the each class as a whole in order to calculate the FC.

FCs are also used as features for classification. So instead of using X_i s, their corresponding FCs i.e. \bar{X}_i s are classified in order to detect the patients with eMCI. A straightforward way is to vectorize the FCs into high-dimensional vectors as features as in [33], which are then used to train a SVM or k-NN classifier. this method produces poor performance due to the phenomena known as Curse of Dimensionality. Variety of techniques have been proposed in order to reduce the dimensionality of these FCs but since they all use conventional classifiers like SVM or k-NN, one way or an other they have to vectorize the data in order to feed it to these classifiers. Alongside the curse of dimensionality, vectorization also destroys potential information that are embedded in the structure of data. This problem have been studied specially in image processing in which vectorization destroys the spatial relations within an image.

So far we have listed two goals: finding an FC for a whole class and detecting a disorder via classification, along with common methods to reach them. In this paper we propose a framework based on high dimensional data structures known as tensors, in order to achieve both goals with a single operation.

in this paper we show that tensor representation is the natural form to present fMRI images. by this representation, we would be able to work with time and region features seperately in the same time. also with this representation we an easy and affordable multilinear dimension reduction that works with time and region features seperately this will be done by high order singular value decomposition of the normal and eMCI subjects.

also we show that by this representation and using the

obtained HOSVD, dimension reduction step we can obtain tensor based discriminat features for classification. this discriminant method furthermore simplicity is very effective. here we show that by this framework the test data also could have effect in construction of discriminant function which is impossible in well known classification methods like SVM, logistic regression and etc.

by this approach the construction of FC feature that was time consuming is ignored and we represent an other method that at the same time with simple structure and low computation cost gives very high quality results with the other state of the art methods.

in fMRI data, one other feature is the fnctional connectivity of normal and abnormal subjects. as the third innovation of this paper we showed that based on hosvd of normal and eMCI patients and effective and high quality functional connectivity network can be extracted for both classes. we will show that some connectivities that are discovered via these FCs are well studied in recent clinical documents and thus . . .

Distinguishing two rs-fMRI volumes in the machine learning viewpoint can be considered as a two class classification problem. Some methods use the vectorized version of samples ie, $x_i = \text{vec}(X_i) \in \mathbb{R}^T$ as inputs of the learning process. However as we will discuss later, this vectorization may cause the loss of some important properties within the structure of data, and because of that the dominant approaches tend to find different set of features for each sample. These methods construct a *region* \times *region* matrix $\bar{X}_i \in \mathbb{R}^{R \times R}$ which is often called functional connectivity (FC) matrix and indicates the between correlation of ROIs. Since in most fMRI samples the number of timepoints is larger that the number of ROIs i.e. $T > R$, substituting X_i with \bar{X}_i reduce the number of features and the effects of the *curse of dimensionality*, also it has been shown that using FC can enhance small between region connections hence turns FC into a powerful tool for rs-fMRI data analysis. For correlation computation, different methods have been explored, among which the pairwise Pearsons correlation coefficient [10], [11], sparse representation [10], [12], [13] and Sparse Inverse Covariance Estimation (SICE) are of the popular ones [14], [15]. While the first two are easy to understand and can capture pairwise functional relationship based on a pair of ROIs, the latter can account for more complex interactions among multiple ROIs, but the estimation of partial correlation involves an inversion of a covariance matrix, which may be ill-posed due to the singularity of the covariance matrix. On the other hand, computing the correlation based on the entire time series of RS-fMRI data simply measures the FC between ROIs with a scalar value, which is fixed across time. This actually implicitly hypothesizes the stationary interaction patterns among ROIs. As a result, this method may overlook the complex and dynamic interaction patterns among ROIs, which are essentially time-varying [16]–[19]. In order to overcome this issue, some methods have been proposed that consider the time as a non-stationery property. As for an example [] uses sliding-window technique in order to divide the time series into several smaller parts and then calculate the between correlation of these parts.[][] although these methods show promissing classification results, they are

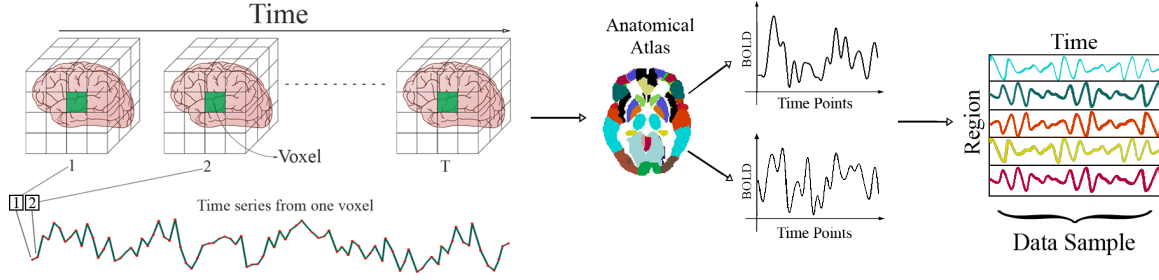


Fig. 1. Simulation results for the network.

not computational favorable and since the aspect of region is not preserved in the final model, the relation between the high-order FC and the real world FC is somewhat ambiguous. After calculating the FC, conventional classifiers like SVM or KNN is deployed in order to classify the vectorized FC for each sample [20].

Although FC grants us certain useful structural properties such as being SPD and having relatively low dimensionality, using it in the classification process has its own drawbacks such as calculating the proper FC and extracting key features from it. Considering these issues we have come up with a framework that eliminate the need for finding the FC in the classification process. Also the proposed framework works directly with the sample matrix and preserve its structural integrity by avoiding the vectorization using novel multilinear techniques. (more about vectorization?)

In this paper we claim that by considering $X_i \in \mathbb{R}^{T \times R}$ as the sample, the dataset could be considered as an order three tensor. Using this representation we have shown that by extremely lower computational cost compared with other methods, and without the need to construct FC, a framework can be designed that only by one High Order Singular Value Decomposition (HOSVD) for each class could give us the desired results. This framework which we call it **TBNA** (High Order Feature Selection and Extraction) does three main tasks:

- **Dimension Reduction:** The proposed frameworks allows us to select key features of each mode (i.e. *Time*, *Region* and *sample*) of the constructed tensor separately and differently. This feature extraction would cause a massive reduction of the dimensions.
- **Classification:** Based on the properties of the HOSVD, we have eliminated the vectorization at any step and hence assure that no information is lost in the vectorization process. Moreover we have formed a novel classification enhancement technique that allows the test samples to cooperate in the training phase. This technique increases the tendency of the test sample to it's true class without forcing any apriory knowledge about it's label to the trainer.
- **Functional Connectivity Network Construction:** Being able to see the class as a whole ables us to derive a Functional Connectivity network for each class. Such FCs allows us to investigate on shared properties within each class such as functional abnormalities of some ROIs or the connection between them.

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To verify our approach, we conduct an extensive experimental study on rs-fMRI data from the benchmark dataset ADNI¹. As will be seen, the results well demonstrate the effectiveness and advantages of our method. Specifically, the proposed TBNA system, not only grants us superior classification accuracy to that from other methods, it is also much faster. We have also confirmed our achieved FC matrix using empirical data on the eMCI functional connectivity patterns.

II. EMCI CLASSIFICATION TECHNIQUES

As it was discussed before, classification techniques have become a favorable method for Alzheimer disease early detection. early classification methods used X_i s as the representative for each subject and used them directly in the classification process. As the functional connectivity matrix gain popularity among researchers, the majority of these classification methods shifted towards classifying the functional connectivity matrices. There are two main paradigms towards obtaining the FCs. Stationary and non-stationary methods, Stationary methods use a single scaler value in order to determine the functional connectivity between two ROIs. Non-stationary methods consider a more complex relation between ROIs that can not be best captured with a single scaler value.

In order to demonstrate the power of our proposed framework, we have implemented an state of the art method from each of these paradigms. The first method which is an stationary one uses the Sparse Inverse Covariance matrix in order to establish a functional connectivity matrix and then using the SPD property of SICE, propose a dimension reduction technique in order to find a set of low dimensional features for classification. The second method which is non-stationary, uses sliding windows to construct a more complex connectivity matrix and uses clustering in order to obtain low dimensial features for classification.

- **Compact SICE:** In this method, first the SICE matrix is extracted from the data sample S using the following optimization:

$$S^* = \arg \max_{S \succ 0} \log(\det(S)) - \text{tr}(CS) - \lambda \|S\|_1 \quad (1)$$

where C is the sample-based covariance matrix; $\det()$, $\text{tr}()$, and $\|\cdot\|_1$ denote the determinant, trace, and the sum of the absolute values of the entries of a matrix.

¹<http://adni.loni.usc.edu/>

Since the dimensions of SICE matrix is R^2 , with R representing the number of ROIs, the obtained matrix is still relatively large. Principal Component Analysis(PCA) has proved itself to be one of the most powerful methods of dimension reduction and this method uses Kernel-PCA with a Gaussian kernel in order to extract the key features of SICE. Since SICE is an SPD matrix, specific distance functions such as Log-Euclidean distance or Root Stein divergence can be used as the distance function in the Gaussian kernel. After extracting key features, conventional methods like SVM or Knn could be deployed for classification.

- **High Order Networks(HON)** This method uses so called High Order Networks as features for classification purposes. it uses the sliding window technique in order to split the time-series into smaller pieces and then find the relation between them. Let $x_i^{(l)}(k) \in \mathbb{R}^N$ denote the k -th segment of subseries extracted from $x_i^{(l)}$, which comprises N image volumes. by taking each $x_i^{(l)}(k)$ as a node A network can be constructed with edges defined using:

$$C_{ij}^{(l)}(k) = \text{corr} \left(x_i^{(l)}(k), x_j^{(l)}(k) \right)$$

which represents the pairwise Pearsons correlation coefficients between the i -th and the j -th ROIs of the l -th subject using the k -th segment of subseries. by taking

$$y_{ij}^{(l)} = \left[C_{ij}^{(l)}(1), C_{ij}^{(l)}(2), \dots, C_{ij}^{(l)}(K) \right] \in \mathbb{R}^K$$

as new nodes, an other network can be calculated as follow:

$$H_{ij,pq}^{(l)} = \text{corr} \left(y_{ij}^{(l)}, y_{pq}^{(l)} \right)$$

for each pair of correlation time series y_{ij} and y_{pq} thus, $H_{ij,pq}^{(l)}$ indicates how the correlation between the i -th and the j -th ROIs influence the correlation between the p -th and the q -th ROIs. The total number of the high-order correlation coefficients $\{H_{ij,pq}^{(l)}\}$ is proportional to R^4 which will lead to a large-scale high-order FC network, containing at least thousands of vertices and millions of edges. In order to overcome this issue, the correlation time series within each subject is grouped into different clusters. Then, the correlation calculation between the original correlation time series can be converted into that between the respective mean correlation time series in clusters. After reducing the network size, the weighted-graph local clustering coefficients was used to select the key features for each network and then SVM is used in order to classify the obtained features.

It is noteworthy that non of these techniques consider the multi-linearity nature of the data, and since both methods use traditional classifiers like SVM or KNN, they follow a rather complex path to find vector features as the representative of each FC matrix.

III. PROPOSED FMRI ANALYSIS FRAMEWORK BASED ON TENSOR FRAMEWORK

All main mentioned eMCI classification methods use FC of each sample as input feature. So, the computational complexity of these method due to construction of FC matrices are high and also the quality of these FC matrices have a direct effect in the quality of classification.

Also know of them did not used the multi-linear propriety of such data. In this section by tensor viewpoint we show that only by one tensor decomposition we could doe the following analysis on fMRI data

- **Classification:** Based on HOSvd decomposition we define a discriminant function to classify matrix data X_i without folding and without construction of FC matrix per- sample.
 - By the obtained base vector from HOVD By using High order singular value eecomposition (HOSVD), all region-time matrices are projected to smaller matrices (without folding the data to vectors)
 - As the first time we propose a novel method that alow test data have a contribution in constructions of discriminant function of each class. This idea hav a big effect in the quality of the propped method

Since this method directly works on region-time matrices as input features, its computational complexity is more smaller than state of the aret methods that use FC matrices as input feature. Also the experimental results confirm the quality of this method in recognition of normal and obnormal data.

- By the previous HOSVD decomposition we proposed a novel method that could find a general representative FC for eMCI and Normal data. In this method computing the FC of all smaple is not necessary to find FC of all samples. In the experiments the obtained FC contains a relations that recently founded experimentaly(cilinally).

A. Dimension reduction and classification based on Tensor framework

In region based fMRI data each data is a region-Time matrix $X \in \mathbb{R}^{T \times R}$, where T, R denote the length of time and regions of the data. For reducing the computational complexity and reducing the occurrence of over fitting, specially for data with large features (Like fMRI data), using dimesionality reduction is inevitable. Although each sampe X have two different king features (time and region), the classical methods like PCA, SVD ,... only could works on vectorizaed version $x = \text{vec}(X)$ of such data. In these methods by having projection matrix U (Due to method), the projected dat will be $y = U^T x$. Although this approach is easy to deploy, it has several drawbacks, one main drawback would be the Curse of dimensionality that appears when the proportion of the number of features to the number of samples is relatively high (which results in over-fitting). Also in this view different kind of features(like *Time* and *region* in our case) would be mixed together which may discard some important information within these features. The second approach is to deploy multilinear methods.

This vectorization furthermore increasing the computational complexity, mixed the mentioned two type of vectors. Recently some works like MPCA, GLRAM methods have been proposed that are able to reduce sample with matrix data types without folding them to vectors. In these methods there is a freedom to select specific reduction for each sample. In this multilinear methods for each feature its corresponding projection matrix is obtained. In this section we will use well-known tensor decomposition named HOSVD for dimension reduction and also classification of fMRI data.

Let X_1, \dots, X_{s_1} and X_1, \dots, X_{s_2} be the train data of eMCI and Normal classes, respectively. Now we substitute these data at tensors $\mathcal{X} \in \mathbb{R}^{T \times R \times S_i}$, where each mode-2 slice shows sample data. Since the same process will be done on these tensors, so for simplicity we explain our proposed process on tensor \mathcal{X} without up-script.

Let $\mathcal{X} \in \mathbb{R}^{T \times R \times S}$, where each slice $X(:, :, i)$ denotes the time-region feature of the i^{th} sample. If

$$\mathcal{X} = (U^{(i)}, V^{(i)}, W^{(i)}) \cdot \mathcal{S}, \quad (2)$$

where orthogonal matrices $U \in \mathbb{R}^{T \times T}$, $V \in \mathbb{R}^{R \times R}$ and $W \in \mathbb{R}^{S \times S}$ are modes-1,2,3 singular matrices of \mathcal{X} , and \mathcal{S} is the corresponding core tensor. As it was mentioned in (??) U is a base of all mode-1 fibers $\mathcal{X}(:, i, j)$ which indicates the behavior of i^{th} region of the j^{th} sample in all times. Also V is a base of all mode-2 fibers $\mathcal{X}(i, :, j)$ which indicates the behavior of all regions of i^{th} j^{th} sample in the i^{th} time. Also due to the properties of HOSVD inherited from svd, the first columns of mode- k ($k=1,2,3$) has more ability in construction of main parts of k^{th} fibers and on the other hand, the last columns of this singular matrix, are corresponding to noise parts of the fibers of the corresponding mode. Therefore for appropriate values of k_1 and k_2 projection mode-1 and mode-2 fibers into space spanned by the first k_1 and k_2 singular vectors of modes-1,2, i.e., matrices $U_{k_1} = [u_1, \dots, u_{k_1}]$ and $V_{k_2} = [v_1, \dots, v_{k_2}]$ is a suitable dimension reduction. This dimensionality reduction could be done as

$$\mathbb{R}^{k_1 \times k_2 \times S} \ni \bar{\mathcal{X}} = (U_{k_1}^T, V_{k_2}^T)_{1,2} \cdot \mathcal{X} \quad (3)$$

So, by having mode-1 and mode-2 singular matrices of tensor \mathcal{X} , its reduced version $\bar{\mathcal{X}}$ without folding the data into vectors could be obtained. Here it's clear that the reduced version of the i^{th} sample, i.e., $\bar{\mathcal{X}}(:, :, i) \in \mathbb{R}^{k_1 \times k_2}$ could be reduced separately in each mode. This means that in this case the structure of data is preserved in the reducing process. ?? So, if

$$\mathcal{X}^{(i)} = (U^{(i)}, V^{(i)}, W^{(i)}) \cdot \mathcal{S}^{(i)}, \quad (4)$$

be the HOSVD decomposition of the data of i^{th} class, for appropriate k_1^i, k_2^i indices, its reduced data will be

$$\mathbb{R}^{k_1^i \times k_2^i \times S_i} \ni \bar{\mathcal{X}}^{(i)} = \left(U_{k_1^i}^{(i)T}, V_{k_2^i}^{(i)T} \right)_{1,2} \cdot \mathcal{X}^{(i)}. \quad (5)$$

The error analysis and the property of HOSVD, it could be shown that by small number of k_1^i, k_2^i , the reduced data have good reconstruction error.

In the following inspired by the structure of this reduction, we present a tensor-based discrimination function. By

substituting $\mathcal{X}^{(i)}$ in ?? by its HOSVD decomposition (4), the projected data $\bar{\mathcal{X}}^{(i)}$ becomes

$$\begin{aligned} \bar{\mathcal{X}}^{(i)} &= ([I_{k_1^i} \ 0], [I_{k_2^i} \ 0], W) \cdot \mathcal{S}^{(i)} \\ &= (W)_3 \cdot \mathcal{S}^{(i)}(1 : k_1, 1 : k_2, :) \end{aligned}$$

By this equation, we can see that each sample of the i^{th} class in the reduced space have the following form

$$\begin{aligned} \bar{\mathcal{X}}^{(i)}(:, :, k) &= \left(W^{(i)}(k, :) \right)_3 \cdot \mathcal{S}^{(i)}(1 : k_1^i, 1 : k_2^i, :) \\ &= \sum_{k'=1}^{S_i} W^{(i)}(k, k') \cdot \mathcal{S}^{(i)}(1 : k_1^i, 1 : k_2^i, k'). \end{aligned}$$

For simplicity, if we define $\bar{\mathcal{S}}^{(i)} = \mathcal{S}^{(i)}(1 : k_1^i, 1 : k_2^i, :)$, it is clear that each sample in the i^{th} class could be represented as linear combination of slices $\bar{\mathcal{S}}^{(i)}$. So if a test data like $X \in \mathbb{R}^{T \times R}$, be in the i^{th} class its natural to expect that its projected version into principle region and times spaces spanned by $U_{k_1^i}, V_{k_2^i}$, i.e.,

$$Z^{(i)} = ??$$

could be approximated well as a linear combination of slices of $\bar{\mathcal{S}}^{(i)}$ as follows

$$Z^{(i)} \approx \sum_{k=1}^{S_i} \lambda_k^i \bar{\mathcal{S}}^{(i)}(:, :, k).$$

So, for each test data X , the best approximation its projection versions for spaces of two normal and abnormal is computed and then X assigned to one class with best approximation. mathematically this could be written as follows: For given test data X , its projection data $Z^{(i)}$ for two classes is obtained. Then the best approximation of these projected data in corresponding spaces are obtained as follows

$$r_i = \min_{\lambda^i} \|Z^{(i)} - \sum_{k=1}^{S_i} \lambda_k^i \bar{\mathcal{S}}^{(i)}(:, :, k)\|, \quad \lambda^i = \begin{pmatrix} \lambda_1^i \\ \vdots \\ \lambda_{S_i}^i \end{pmatrix} \quad (6)$$

Here $r^{(i)}$ shows the reconstruction error of the projected version of X in the i^{th} class. So we assign X to l^{th} class if

$$r_l = \min_{i=1,2} r_i.$$

The minimization problem (6) is a simple least square problem that could be solved easily. The proposed method has an interesting property that brings us to propose a novel method to improve its quality. By the properties of HOSVD, the principle properties of the i^{th} class could be reflected in the slices of $\bar{\mathcal{S}}^{(i)}(:, :, i)$. Also for small indices these slices have a better role in construction of main properties of this class. So the first slices of $\bar{\mathcal{S}}$ could represent signal parts, while last slices don't play this role and sometimes represent the waste parts. Now consider a data X added to data set $\mathcal{X}^{(i)}$ of the i^{th} class. So new data set will be $\tilde{\mathcal{X}} \in \mathbb{R}^{T \times R \times (S_i+1)}$. For example

$$\begin{aligned} \tilde{\mathcal{X}}^{(i)}(:, :, 1 : S_i) &= \tilde{\mathcal{X}}^{(i)}, \\ \tilde{\mathcal{X}}^{(i)}(:, :, S_i+1) &= X. \end{aligned}$$

If X belongs to this class then in HOSVD of this tensor X reinforce the slices of core tensor with small indices. But when it dose not belong to this class then it will changes the behavior of last slices of core tensor of new tensor. This means that befor classification of a test data X , We could added it to both classes. This addition, will changed the first slices of core tensor when it beloges to this class or will cahged the last Slices when dose not belog to this class. But in our classification method only the first Slices of core tensor are exits. Also the elements of S in the first and second modes are filtered and we work with $S(1 : k_1^i, 1 : k_2^i, 1 : k_3^i)$. This means that by addition of X in both classes for class that it beloge to it, the first slices in $??$, will be adapted to have good reconstruction for this data. But for a class that dose not beloge to, this addition have small chages in the slices in $??$.

It should be mentioed that since X added to both data sets, so we did not its labe and the method in true. After computing the HOSVD of this new data sets $\mathcal{X}; (i)$, we apply the approach in $??$. In summery this algorithm could be summerized as follows: In this section by HOSVD decomposition on both normal and

In the expermental results we compaire the quality of the method with some of the sate of the art methods for recognition of eMCI based on accuray nad elapsed times.

B. General Functional Connectivity for normal and eMCI by tensor framework

Functional connectivity simply means the relation between different ROIs. As we mentioed the FC could be used for two different pourouses. Some classification methods for each samle by time-region matrix compute a region-region matrix wich shows the FC per sample. These method use this new feareure inseed of time-region feature. But, in other view point we want to obtaine only one representative functional connectivity for each normal or eMCI classes. Here the classification is not our goal, instaed finding a gereral and repretative realltion of regions for eMCI and normal preson is our demand. This general pattern could be used clinically by expert cognitive scinticts to found functional relation Disorders accrued by eMCI.

Although several approaches have been proposed in order to find the functional connectivity, the majority of them focus on the individual samples rather than the whole class. This may overlook tiny but common connectivities shared within a class like the class of people in their early Alzheimer's disease.

As we know in HOSVD the singular matrices U, V, W , are the base of time, region features and also the samples, receptively. By property of these matrices we design our classification method. In this section we show that, the same idea could helps us to define a general FC matrix based on HOSVD decomposition for normal and eMCI data. It show be mentioed that here we did not use the FC of per-samples to construct this gerenral FC matrix.

Due to structure of data for $\mathcal{X}^{(i)}$, the slice $\mathcal{X}^{(i)}(:, l, :)$, denotes the behavior of l^{th} region of all samples in all times. So this could be consider as features of the l^{th} region of the i^{th} class and each region is shown with an Times-sample feature matrix. Viewing each region as a slice would allow us to consider it's behavior in all time points and across all samples, which itself allows us to shed more light on common properties and ignore individual differences that is highly possible due to the presence of noise and outliers. So, by the properties of singula matrices in modes-1,3, for appropriate values k_1^i, k_3^i , each regin $\mathcal{X}(:, l, :)$ could be reduced in bith time and sample dfeatures based on mode-1 and mode-3 truncated singular matrices $U_{k_1^i}^{(i)}$ and $W_{k_3^i}^{(i)}$ as follows

$$\mathcal{Y}^{(i)}(:, l, :) = \left(U_{k_1^i}^{(i)\top}, W_{k_3^i}^{(i)\top} \right)_{1,3} \cdot \mathcal{X}^{(i)}(:, l, :). \quad (7)$$

Here $\mathcal{Y}^{(i)}(:, l, :)$ denotes a reduced version of $\mathcal{X}^{(i)}(:, l, :)$ into space spanned by $U_{k_1^i}^{(i)}$ and $W_{k_3^i}^{(i)}$ in modes-1,3. So,

$$\mathbb{R}^{k_1^i \times R \times k_3^i} \ni \mathcal{Y}^{(i)} = \left(U_{k_1^i}^{(i)\top}, U_{k_3^i}^{(i)\top} \right)_{1,3} \cdot \mathcal{X}^{(i)} \quad (8)$$

Algorithm 1 TNBeMCI: Tensor based Classification method

- 1) **Input:** Normal train data $\mathcal{X}^{(1)}$, eMCI train data $\mathcal{X}^{(2)}$
 $k_j^i, i = 1, 2, 3, \quad j = 1, 2.$
 Test data X
 - 2) Construct $\tilde{\mathcal{X}}^{(i)}$ for $i = 1, 2$ by adding X as $??$
 - 3) Compute $U_{k_1^i}, V_{k_2^i}$ and $S(1 : k_1^i, 1 : k_2^i, k_3^i)$ for $\tilde{\mathcal{X}}^{(i)}$.
 - 4) Compute $Z^{(i)} = \left(U_{k_1^i}^{(i)\top}, V_{k_2^i}^{(i)\top} \right)_{1,2} \cdot X, i = 1, 2.$
 - 5) Comput r_1, r_2 from $??$
 - 6) Assign X to class l , if $l = \arg \min_i \{r_i\}$
-

eMCI data, we proposed a novel tensor based classification. The benifits of the proposed tensor based classification method could be summerized as follows

- This method use multilinear propret of these data and works could works with time and region features separatly based on their specific onbatned bases(corresponding singular matrices).
- The classification works on data without folding them ti vectors.
- As we mentioed the test data has a role in construction of bases for both classes, without knowing the class of test data. This incearse the quality of the discrimination. This could not applied on important classification ,methods like SVM, logistic regression classifier and neroual networks. This is also could be applied on classifications based on matrix factorization.
- This method works with time-region features, and dose not need to have FC matrices for each sample. So its computational complexity is more less than other state of the art methods like methods mentied in this paper. It should be mentioed that our method also could be applied on FC matrices as input featur. But in experments the propoed method gives better results on original time-region faetres. So, in this feature we do not worry about the qauality of FC methods.

denote all reduced regions of the i^{th} class. By this structure and substituting the HOSVD decomposition of $\mathcal{X}^{(i)}$ in (10), we obtain

$$\begin{aligned}\mathcal{Y}^{(i)} &= ([I_{k_1^i} \ 0], V, [I_{k_3^i} \ 0]) \cdot \mathcal{S}^{(i)} \\ &= (V)_2 \cdot \mathcal{S}^{(i)}(1 : k_1^i, :, 1 : k_3^i)\end{aligned}$$

and so

$$\begin{aligned}\mathcal{Y}^{(i)}(:, k, :) &= \sum_{k'}^R V^{(i)}(k, k') \bar{\mathcal{C}}^{(i)}(:, k', :) \\ &= \left(U_2^{(i)}(k, :) \right)_2 \cdot \mathcal{C}^{(i)}\end{aligned}\quad (9)$$

in which

$$\mathbb{R}^{k_1^i, R, k_3^i} \ni \mathcal{C}^{(i)} = \mathcal{S}(1 : k_1^i, :, 1 : k_3^i).$$

In order to calculate the FC, we first reduced the dimensions of our data similar to what we did in the previous part:

$$\mathbb{R}^{k_1^i \times R \times k_3^i} \ni \bar{\mathcal{X}} = \left(U_{k_1^i}^{(i)\top}, U_{k_3^i}^{(i)\top} \right)_{1,3} \cdot \mathcal{X} \quad (10)$$

it can be seen that each region slice can be written as:

$$\begin{aligned}\bar{\mathcal{X}}^{(i)}(:, k, :) &= \sum_{k'}^{N_i} U_2^{(i)}(k, k') \bar{\mathcal{C}}^{(i)}(:, k', :) \\ &= \left(U_2^{(i)}(k, :) \right)_2 \cdot \bar{\mathcal{C}}^{(i)}\end{aligned}\quad (11)$$

in which

$$\bar{\mathcal{C}}^{(i)} = \mathcal{C}(1 : k_1^i, :, 1 : k_3^i).$$

The equation (11), show that the reduced version of each region in the i^{th} class could written as the linear combinations of mode-2 slices of \mathcal{C} . So the coefficient of slices in this linear combination could be considered as a new feature for the l^{th} region of the i^{th} class. Also as we mentioned the first slices are better than to reflect the principle of the data. So for appropriate k_3^i we could select only the first coefficient in ?? as new features for the l^{th} region. Mathematically this means each region in the i^{th} class could be represented by new feature $V(l, 1; k_3) \in \mathbb{R}^3$. The benefits of this approach is that each region could be represented only by a vector with size k_3 , instead of large feature matrix time-sample. Now different methods could be used to find the correlation of regions based on this small and clean matrix $V(:, 1 : k_3)$ which its rows corresponding to different regions and columns are new features. In this due to quality of Sparse Inverse Covariance, this method is applied to the obtained feature-region matrix $V(:, 1 : k_3^i)^\top$ in order to find the functional connectivity of the i^{th} class.

IV. EXPERIMENTAL STUDY

A. Data Preprocessing and Experimental Settings

Rs-fMRI data of 196 subjects were downloaded from the ADNI website². Nine subjects were discarded due to the corruption of data, and the remaining 187 subjects were preprocessed for analysis. After removing subjects that had

²<http://adni.loni.usc.edu>

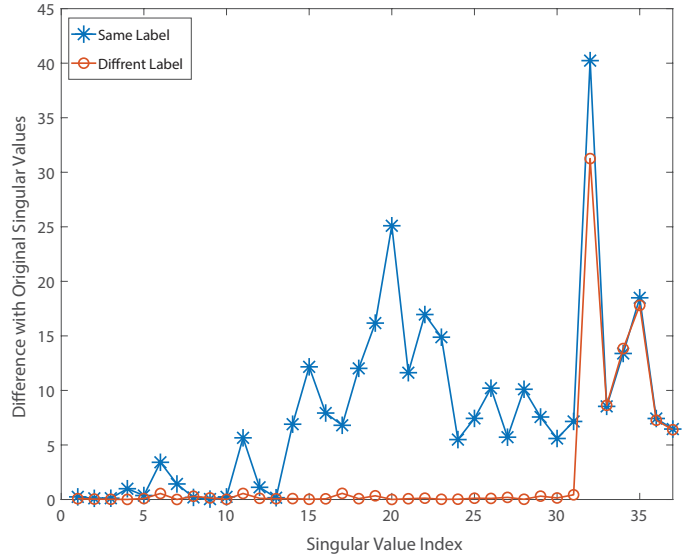


Fig. 2. The blue line with the star indicator, shows the difference between the mode-3 singular values of the original data and the data appended with a *same* label subject. The orange line indicated with circles, shows the difference between the mode-3 singular values of the original data and the data appended with a *different* label subject.

problems in the preprocessing steps, such as large head motion, 156 subjects were kept, including 26 AD, 44 early MCI, 38 late MCI, 38 NC, and ten significant memory concern labeled by ADNI. We used the 38 NC and the 44 early MCI because our focus in this paper is to identify MCI at very early stage, which is the most challenging and significant task in AD prediction. The IDs of the 82 (38 NC and 44 early MCI) subjects are provided in the supplementary material.

The data are acquired on a 3-T (Philips) scanner with TR/TE set as 3000/30 ms and flip angle of 80. Each series has 140 volumes, and each volume consists of 48 slices of image matrices with dimensions 64×64 with voxel size of $3.31 \times 3.31 \times 3.31 \text{ mm}^3$. The preprocessing is carried out using SPM12 and DPARSFA [40]. The first ten volumes of each series are discarded for signal equilibrium. Slice timing, head motion correction, and MNI space normalization are performed. Participants with too much head motion are excluded. The normalized brain images are warped into automatic anatomical labeling (AAL) [41] atlas to obtain 116 ROIs as nodes. By following common practice [15][17], the ROI mean time series are extracted by averaging the time series from all voxels within each ROI and then bandpass filtered to obtain multiple sub-bands as in [17].

B. Classification

Almost every subject in ADNI dataset has several scans. Usually a random scan data is selected and enters the processing step. This random selection may cause several problems. Since the number of train data is very low, a small perturbation in it could drastically change the set of input parameters in order to achieve the highest prediction accuracy and other classification evaluation methods. Also achieving high quality results with a classifier does not guarantee its effectiveness on

TABLE I
THE AVERAGE OF DIFFERENT CLASSIFICATION MEASUREMENTS IN ALL
PERTURBATIONS IN %

Method	ACC	F-Score	SEN	SPE	YI	BAC
k-SICE	75.57	77.36	78.50	72.19	50.69	75.34
FON	75.66	77.44	78.40	72.48	50.89	75.44
TBNA	80.43	82.20	84.60	75.59	60.20	80.09

other datasets even with fine tuning the parameters since the training set may contain outliers and unidentified corrupted data. In order to show that the proposed framework is less sensitive against the choice of different perturbations and is less vulnerable towards the aforementioned issues, we have selected 18 different perturbations and two test state of the art classification methods on them: **HON** and **k-SICE**. To make full use of the limited subjects, a leave-one-out procedure is used for training and test. That is, each sample is reserved for test in turn, while the remaining samples are used for training. We have use five evaluation measures: accuracy (ACC), sensitivity (SEN), Youdens index(YI), F-score, and balanced accuracy (BAC). In this article, we treat the eMCI samples as positive class and the NC samples as negative class.

1) *Classification performance*: The classification accuracy measure(ACC), After fine-tuning the input parameter set for each method, shows that for 16 out of 18 different perturbations, our approach works better than k-SICE, the same also holds for 15 datasets comparing to HON. i.e. in 88.8% of datasets, TBNA works better than k-SICE and in 83.3% of datasets, it works better than FON. The highest classification accuracy(86.59%) is achieved with the TBNA in the 15th perturbation. The highest accuracy for the HON (84.15%) is achieved in the 14th, and the highest accuracy for the SICE method (85.37%) is achieved in the 6th perturbation. As it was mentioned before, being stable when the input dataset changes is a very important aspect for a classifier, in order to measure the stability, standard deviation of accuracy along with other measures are calculated. The std. of accuracy for TBNA is 0.64 times less than HON and 1.73 times less than SICE method. Similar results also holds for other classification measures.

Figure (3) shows the performance of these three methods in all five measurements. Some statistical information about these plots are also included in the embedded table. As it can be seen in this figure, similar to the accuracy, the proposed method in overall works much better than FON and k-SICE. For a better Demonstration, table (I) provides the average of several classification measurements scores for all permutations. As it can be seen in this table, the average accuracy of TBNA which is 80.43% is 4.77% higher than the next method HON, and 4.86% better than k-SICE. It is noteworthy that The other two methods i.e HON and SICE shows similar results in average.

2) *Runtime Comparison*: One other key features of TBNA is that it works significantly faster than the other two methods. Table (II) shows the average elapsed time (Training plus Testing) of each method for all selected permutations. These

TABLE II
ELAPSED TIME OF THE TEST AND TRAIN PHASE IN SECONDS

Method	HON	k-SICE	TBNA
Elapsed Time	6950	230	11

methods were executed in matlab R2017b and carried with an intel Core-i7 processor and 16GB of RAM. As it can be seen in this table, TBNA is more than 600 times faster than HON and 20 times faster than SICE. Having a huge execution time specially affects the parameter selection for HON, since it uses cross-validation procedure in order to find the optimal parameters which itself require several runs of the algorithm.

C. Functional connectivity Network

The functional connectivity networks of the Normal and eMCI classes was obtained via TBNA as it is described in (III-B). In order to better highlight the differences between Normal and eMCI subjects, a difference graph D is constructed by subtracting the Normal FC from the eMCI FC. This graph could be seen in Figure(4). The nodes of D shows the ROIs according to the AAL atlas. The size of each node is proportional to its graph clustering coefficient, i.e. the bigger node, demonstrates higher activity in eMCI subjects in the corresponding ROI. Similar to nodes, the size of each edge is also proportional to the correlation between two ROIs. In addition, the edges are also color coded in a way that the green edges shows the positive edges in D and the orange edges shows the negative edges in D . In this manner, the green edges demonstrates decreasing in activity between the corresponding nodes in eMCI subjects and vice versa, the orange edges shows increasing activity between corresponding ROIs in the eMCI subjects.

As it can be seen in the difference graph, the big nodes i.e. ROIs with higher activities does not necessarily establish strong connections with the other nodes. As an obvious example, higher activities in Lingual gyrus(ROI index: 47,48)[24], [25], Calcarine sulcus(ROI index: 43, 44)[26], [27], Supplementary motor area(ROI index: 19,20)[27], [28] and Temporal_mid_L(ROI index: 85)[29] are easily detectable. The majority of ROIs located in frontal lobe also shows rather high activities comparing to normal subjects[31], [30].

Similar to the nodes, strong edge between two ROIs does not necessarily requires the nodes to be highly active in eMCI. Although a strong edge does indicate high activities and functional connectivity between the two corresponding ROIs. The difference Graph shows significant increase in connectivity between Rectus(ROI index: 28, 27 in Frontal lobe) and Parietal_Sup_R(ROI index: 60 in Parietal lobe), Frontal_Inf_Orb_R(ROI index: 16 in Frontal lobe) and Cingulum_Ant(ROI index: 31,32 in Limbic lobe), Insula_L, Temporal_Pole_Sup_L(ROI index: 29,83 in Limbic lobe) and Pallidum_R, Caudate_R(ROI index: 29,83 in Sub Cortical Grey Nuclei). It can also be seen that within activities in frontal lobe also increased in patients with eMCI. There is a decrease in connectivity between Amygdala_L(ROI index: 41

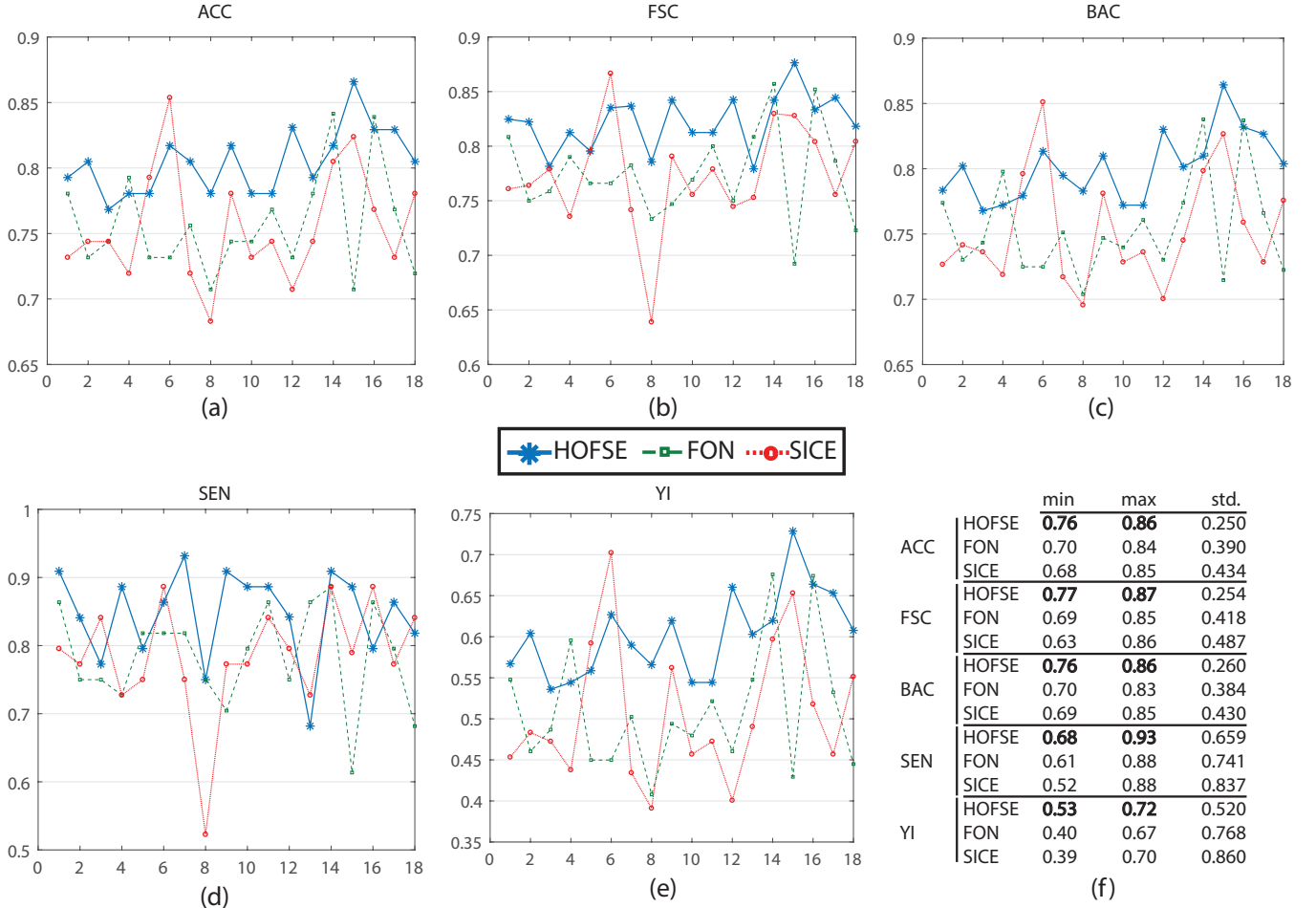


Fig. 3. sdsss

in Sub Cortical Grey Nuclei) with Frontal_Mid_Orb_R(ROI index: 10 in Sub Frontal lobe) and ParaHippocampal_L(ROI index: 39 in Sub Limbic lobe). The connectivity between Heschl_L(ROI index: 79 in Temporal lobe) and two ROIs Temporal_Mid_R(ROI index: 86 also in Temporal lobe) and Occipital_Inf_R(ROI index: 54 in Occipital lobe) also decreased in eMCI.

Regarding the Cerebellum and Vermis: In fMRI data analysis and especially in Alzheimer's disease studies, ROIs within the Cerebellum and Vermis are usually excluded[ref] since their role was regarded as insignificant. Recent studies have shown that the traditional assumption that Cerebral area is essential only for the coordination of voluntary motor activity and motor learning is not valid and indicates the significant role of cerebellum in nervous system function, cognition and emotion[32].

As it can be seen in the difference graph that we obtained, ROIs within Cerebellum and Vermis are highly active and both their intra and inter connections are noticeable. There is an increasing functional connectivity between the Limbic lobe especially Hippocampus_R, Temporal_Pole_Mid(ROI index: 38,87,88) and Cerebral areas in eMCI patients. Also, the connectivity between Occipital lobe, especially Occipital_mid_R(ROI index: 52), the Frontal lobe, especially in

Frontal_mid_orb(ROI index: 9,10) and Cerebral areas seems to decrease in patients with eMCI.

V. CONCLUSION

The majority of classification techniques uses the vectorized version of data as the input of the discriminant function. As the number of the dimensions grows, i.e. when data is naturally a high order tensor, this vectorization become problematic and it would highly affect the performance. Taking advantage of the techniques designed for the tensors, we have developed a framework for fMRI data analysis in which the following objectives:

- 1) Dimension Reduction
- 2) Classification
- 3) Obtaining Functional Connectivity network

are achieved via a single **High Order SVD** of the input tensors.

Extensive studies on the rs-fMRI provided by ADNI shows the superiority of the proposed framework in both classification and functional connectivity. The obtained FC network not only acknowledge the previous discovered connections but also reveals new connectivity patterns previously unknown. The framework proposed in this paper can be easily extended to other studies involved with high order data.

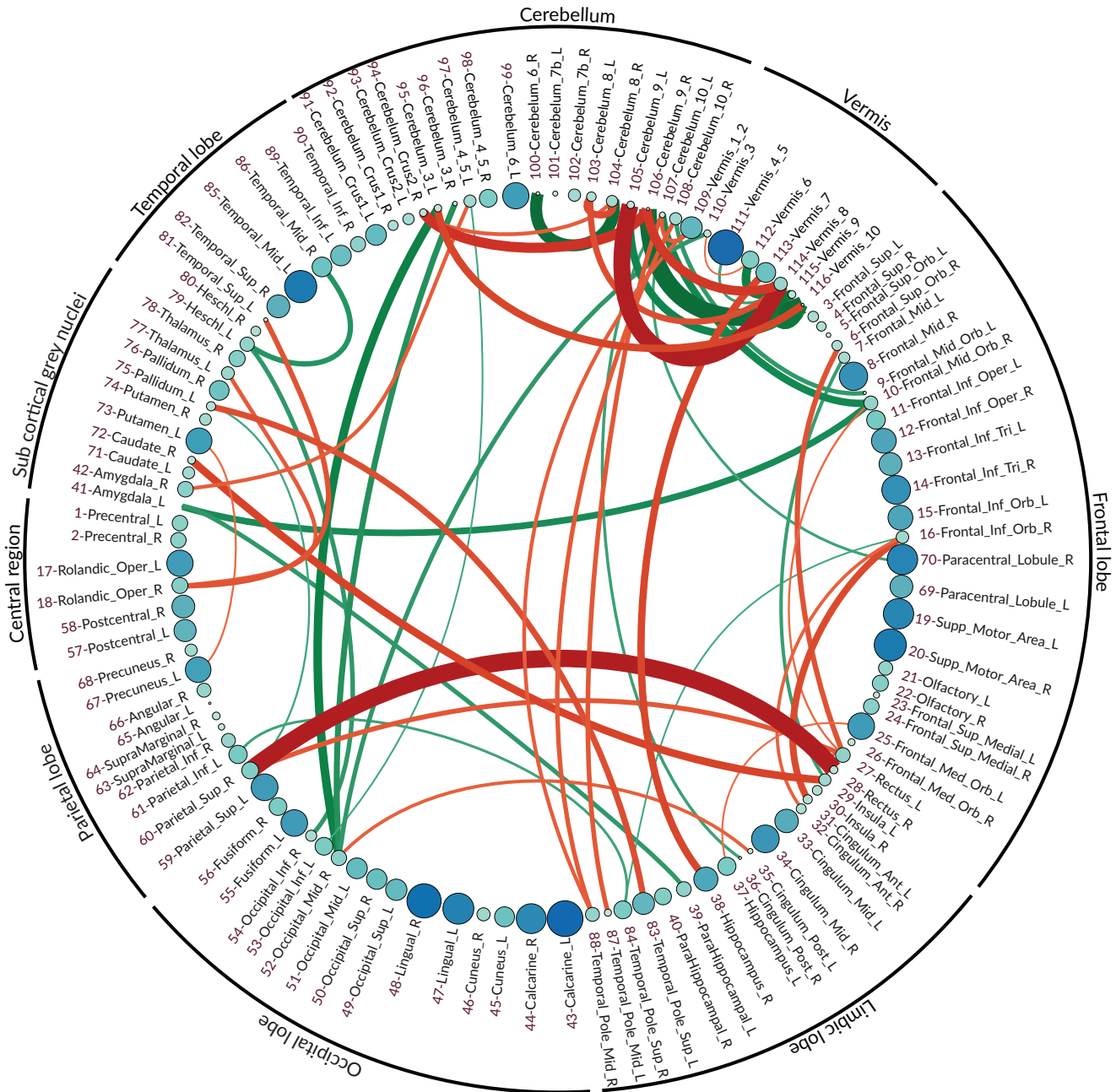


Fig. 4. The difference graph. This graph is obtained via subtracting the functional connectivity of eMCI subjects from normal subjects. Each circle represents a ROI in AAL atlas and the color and size of each circle is proportional to the graph clustering coefficient of the difference graph. red = more activity in EMCI, green: less.

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