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## Derivative Products: 2° Term Exam

LAT4012

### Academic Integrity Statement

“I certify that I am completing this exam individually and without the use of unauthorized resources. I commit to upholding academic integrity standards and confirm that I have neither received nor provided inappropriate assistance during this exam.”

Signature: \_\_\_\_\_

### Q1. Basics

- a) Define a **derivative** and list **three** common types of underlyings
- b) Compare **OTC vs. exchange-listed** in two points.
- c) Distinguish **hedger**, **speculator**, and **arbitrageur** in one sentence each.

### Q2. Forwards: multi-case valuation

**Data:**  $S_0 = 95$ . Horizon  $T = 9 \text{ months}$ . (Assume 1 year means  $T = 1$ )  
Compute  $F_{0,T}$  for:

- i) **No dividends**,  $r = 6\%$ (continuous compounding)
- ii) **Continuous dividends**,  $r = 6\%$ (cont. comp.),  $d = 2\%$
- iii) **FX forward** USD/MXN:  $x_0 = 18.20$ ,  $r_{MXN} = 10\%$  (cont.),  $r_{USD} = 4\%$ (cont.),  $T = 0.5$ .
- iv) If in (i) the market forward is  $F^{mkt} = 100.6$ , is there an **arbitrage**? Describe the trade.

### Q3. Forwards: payoff and profit

**Long forward** with  $K = 100$ ; maturity in 6 months. Compute **payoff and profit** for **long** and **short** when  $S_T \in \{90, 100, 115\}$ . Present in a table.

## Q4. Put–call parity

**Non-dividend-paying stock:**  $S_0 = 40$ . **European call:**  $K = 45$ ,  $T = 0.75$  years, premium  $C_0 = 2.84$ . **Rate**  $r = 5\%$ (cont.).

- Use **put–call parity** to **compute**  $P_0$ .
- If the put trades at 6.80, is parity **violated**? What **arbitrage** would you implement?

## Q5. Option strategies

a) **Bull call spread:** Buy  $C(K_1 = 50)$  at 6.20, sell  $C(K_2 = 60)$  at 2.30.

- Draw the **payoff at maturity** and report **max gain, max loss, and breakeven**.

b) **Bear put spread (debit spread):** Let  $S_0 = 55$ . Buy **put**  $K_H = 60$  at **4.50** and sell **put**  $K_L = 50$  at **1.80** (same maturity).

- i) **Net cost** today.
- ii) **Max gain, max loss, and breakeven**.
- iii) Describe the **payoff shape** at maturity.

c) Explain the difference between a **cap** and a **floor** is preferable (one line each). (6 pts)

d) Explain when a **covered call (written call)** vs. a **protective put (written put)** is preferable.

## Q6. Synthetics & Parity

a) Show how to **replicate a stock or a bond** with options and cash using **put–call parity** (state the identity and explain each term).

b) **Parity check/no-arbitrage:**  $S_0 = 52$ ,  $K = 50$ ,  $T = 1$  year,  $r = 4\%$ (cont.),  $C_0 = 9$ ,  $P_0 = 7$ .

- Does parity hold? If **not**, design an **arbitrage** (what to buy/sell **today** and how it closes at  $T$ ).