

Use Applicative where applicable!

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<https://github.com/hermannhueck/use-applicative-where-applicable>

Abstract

Most Scala developers are familiar with monadic processing. Monads provide *flatMap* and hence for-comprehensions (syntactic sugar for *map* and *flatMap*).

Often we don't need Monads. Applicatives are sufficient in many cases.

In this talk I examine the differences between monadic and applicative processing and give some guide lines when to use which.

After a closer look to the Applicative trait I will contrast the gist of *Either* and *cats.data.Validated* (the latter being an Applicative but not a Monad).

I will also look at traversing and sequencing which harness Applicatives as well.

(The code examples are implemented with *Cats*.)

Agenda

1. Monadic Processing
2. Aside: Effects
3. Aside: Curried functions
4. Where Functor is too weak
5. Applicative Processing
6. Comparing Monad with Applicative
7. The Applicative trait
8. Either vs. Validated
9. Traversals need Applicative
10. Resources

1. Monadic Processing

See: *examples.MonadicProcessing*

The Problem:

How to compute values wrapped in a context?

Example context/effect: *Option*

```
def processInts(compute: (Int, Int, Int) => Int)
  (oi1: Option[Int], oi2: Option[Int], oi3: Option[Int])
  : Option[Int] = ???
```

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  : Option[Int] = ???
```

```
val sum3Ints: (Int, Int, Int) => Int = _ + _ + _

val result1 = processInts(sum3Ints, Some(1), Some(2), Some(3))
// result1: Option[Int] = Some(6)

val result2 = processInts(sum3Ints, Some(1), Some(2), None)
// result2: Option[Int] = None
```

The Standard Solution:

Monadic Processing with a for-comprehension (monad comprehension)

Example context/effect: *Option*

```
def processInts(compute: (Int, Int, Int) => Int)
  (oi1: Option[Int], oi2: Option[Int], oi3: Option[Int])
  : Option[Int] =
  for {
    i1 <- oi1
    i2 <- oi2
    i3 <- oi3
  } yield compute(i1, i2, i3)
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def processInts(compute: (Int, Int, Int) => Int)
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// result2: Option[Int] = None
```


Abstracting *Option* to $F[_]: \text{Monad}$

```
def processInts[F[_]: Monad](compute: (Int, Int, Int) => Int)
                             (fi1: F[Int], fi2: F[Int], fi3: F[Int]): F[Int] =
  for {
    i1 <- fi1
    i2 <- fi2
    i3 <- fi3
  } yield compute(i1, i2, i3)
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Abstracting *Option* to $F[_]: \text{Monad}$

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def processInts[F[_]: Monad](compute: (Int, Int, Int) => Int)
                             (fi1: F[Int], fi2: F[Int], fi3: F[Int]): F[Int] =
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// result1: Option[Int] = Some(6)

val result2 = processInts(sum3Ints, Some(1), Some(2), None)
// result2: Option[Int] = None

val result3 = processInts(sum3Ints)(List(1, 2), List(10, 20), List(100, 200))
// result3: List[Int] = List(111, 211, 121, 221, 112, 212, 122, 222)

val result4 = processInts(sum3Ints)(Future(1), Future(2), Future(3))
Await.ready(result4, 1 second)
// result4 = scala.concurrent.Future[Int] = Future(Success(6))
```

Abstracting away the *Ints*

```
def processABC[F[_]: Monad, A, B, C, D](compute: (A, B, C) => D)
  (fa: F[A], fb: F[B], fc: F[C]): F[D] =
  for {
    a <- fa
    b <- fb
    c <- fc
  } yield compute(a, b, c)
```

Abstracting away the *Ints*

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Await.ready(result4, 1 second)
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```

Desugaring for-comprehension to *map/flatMap*

```
def processABC[F[_]: Monad, A, B, C, D](compute: (A, B, C) => D)
                                         (fa: F[A], fb: F[B], fc: F[C]): F[D] =
  fa flatMap { a =>
    fb flatMap { b =>
      fc map { c =>
        compute(a, b, c)
      }
    }
  }
```

2. *Aside: Effects*

What is $F[_]$?

$F[_]$ is a type constructor.

It represents the **computational context** of the operation, also called the **effect** of the operation.

effect != side effect

With the context bound $F[_]: \text{Monad}$ we constrain the effect to be a Monad.

This makes F a place holder for any Monad which provides us *map* and *flatMap*.

Some Effects

<u>E[]</u>	<u>Effect</u>
Option	a possibly missing value
List	an arbitrary number of values of the same type (non-determinism)
Future	an asynchronously computed value
Either	either a value of a type or a value of another type
Id	the effect of having no effect
IO	the effect of having a side effect
Tuple2	two adjacent values of possibly different type
Function1 output	a pure computation on a (yet unknown) input producing an
Reader	a wrapped Function1
Writer	a values that has another value attached which acts as a sort of log value

3. Aside: Curried functions

See: *examples.CurriedFunctions*

Every function is a *Function1* ...

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```
val sum3Ints : (Int, Int, Int) => Int      = _ + _ + _  
val sum3Ints2: Function3[Int, Int, Int] = _ + _ + _
```

Every function is a *Function1* ...

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... if we curry it.

```
val sumCurried: Int => Int => Int => Int = sum3Ints.curried  
// sumCurried: Int => (Int => (Int => Int)) = scala.Function3$$Lambda$4346/9914305
```

Every function is a *Function1* ...

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The type arrow (`=>`) is syntactic sugar for `Function1`.

$A \Rightarrow B$ is equivalent to *Function1*[*A*, *B*].

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```
val sumCurried2: Function1[Int, Function1[Int, Function1[Int, Int]]] = sumCurried  
// sumCurried2: Int => (Int => (Int => Int)) = scala.Function3$$Lambda$4346/991430
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Every function is a *Function1* ...

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val sum3Ints : (Int, Int, Int) => Int      = _ + _ + _  
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```
val sumCurried2: Function1[Int, Function1[Int, Function1[Int, Int]]] = sumCurried  
// sumCurried2: Int => (Int => (Int => Int)) = scala.Function3$$Lambda$4346/991430
```

If uncurried again, we get the original function back.

```
val sumUncurried: (Int, Int, Int) => Int = Function.uncurried(sumCurried)  
// sumUncurried: (Int, Int, Int) => Int = scala.Function$$$Lambda$6605/301079867@1
```

Partial application of curried functions

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```
val sum3Ints: (Int, Int, Int) => Int = _ + _ + _  
val sumCurried: Int => Int => Int => Int = sum3Ints.curried
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val sum3Ints: (Int, Int, Int) => Int = _ + _ + _  
val sumCurried: Int => Int => Int => Int = sum3Ints.curried
```

```
val applied1st: Int => Int => Int = sumCurried(1)
```

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```
val sum3Ints: (Int, Int, Int) => Int = _ + _ + _  
val sumCurried: Int => Int => Int => Int = sum3Ints.curried
```

```
val applied1st: Int => Int => Int = sumCurried(1)
```

```
val applied2nd: Int => Int = applied1st(2)
```

Partial application of curried functions

```
val sum3Ints: (Int, Int, Int) => Int = _ + _ + _  
val sumCurried: Int => Int => Int => Int = sum3Ints.curried
```

```
val applied1st: Int => Int => Int = sumCurried(1)
```

```
val applied2nd: Int => Int = applied1st(2)
```

```
val applied3rd: Int = applied2nd(3)
```

Partial application of curried functions

```
val sum3Ints: (Int, Int, Int) => Int = _ + _ + _  
val sumCurried: Int => Int => Int => Int = sum3Ints.curried
```

```
val applied1st: Int => Int => Int = sumCurried(1)
```

```
val applied2nd: Int => Int = applied1st(2)
```

```
val applied3rd: Int = applied2nd(3)
```

```
val appliedAllAtOnce: Int = sumCurried(1)(2)(3)
```

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```
def filter1[A](la: List[A], p: A => Boolean) = ??? // uncurried
```

```
scala> filter1(List(0,1,2), _ < 2)
<console>:50: error: missing parameter type for expanded function ((x$1: <error>)
    filter1(List(0,1,2), _ < 2)
                      ^
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scala> filter1(List(0,1,2), _ < 2)
<console>:50: error: missing parameter type for expanded function ((x$1: <error>)
    filter1(List(0,1,2), _ < 2)
                      ^
```

```
def filter2[A](la: List[A])(p: A => Boolean) = ??? // curried
```

```
scala> filter2(List(0,1,2))(_ < 2)
res5: List[Int] = List(0,1)
```

Curring in Java? -- (Sorry, I couldn't resist ;-)

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```
// Curring with lambdas
Function<Integer, Function<Integer, Function<Integer, Integer>>> sum3IntsCurried =
    a -> b -> c -> a + b + c;

Integer result = sum3IntsCurried.apply(1).apply(2).apply(3);
```

Curring in Java? -- (Sorry, I couldn't resist ;-)

```
// Curring with lambdas
Function<Integer, Function<Integer, Function<Integer, Integer>>> sum3IntsCurried =
    a -> b -> c -> a + b + c;

Integer result = sum3IntsCurried.apply(1).apply(2).apply(3);
```

```
// Curring without lambdas
Function<Integer, Function<Integer, Function<Integer, Integer>>> sum3IntsCurried =
    new Function<Integer, Function<Integer, Function<Integer, Integer>>>() {
        @Override
        public Function<Integer, Function<Integer, Integer>> apply(Integer a) {
            return new Function<Integer, Function<Integer, Integer>>() {
                @Override
                public Function<Integer, Integer> apply(Integer b) {
                    return new Function<Integer, Integer>() {
                        @Override
                        public Integer apply(Integer c) {
                            return a + b + c;
                        }
                    };
                }
            };
        }
    };

Integer result = sum3IntsCurried.apply(1).apply(2).apply(3);
```

Currying in Haskell?

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Every function is already curried.

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Every function is already curried.

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... and returns only one value which might be another function.

Invoking functions with more than one parameter is possible.
That is just syntactic sugar for curried functions.

Partial application in Haskell

```
sum3Ints :: Int -> Int -> Int -> Int  -- function already curried  
sum3Ints x y z = x + y + z
```

```
applied1st = sum3Ints 1           :: Int -> Int -> Int  
applied2nd = applied1st 2        :: Int -> Int  
applied3rd = applied2nd 3        :: Int  
appliedAll = sum3Ints 1 2 3      :: Int
```

4. Where Functor is too weak

See: *examples.WhereFunctorIsTooWeak*

Where Functor is too weak ...

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What to do if we want to fuse two Options to one by summing up the contained values?

`Option(1) + Option(2) == Option(3) // ???`

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val add1: Int => Int = 1 + _  
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```


Where Functor is too weak ...

What to do if we want to fuse two Options to one by summing up the contained values?

`Option(1) + Option(2) == Option(3) // ???`

```
val add1: Int => Int = 1 + _  
val sum2Ints: (Int, Int) => Int = _ + _
```

```
Option(1) map add1  
// res1: Option[Int] = Some(2)
```

Where Functor is too weak ...

What to do if we want to fuse two Options to one by summing up the contained values?

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```
val add1: Int => Int = 1 + _  
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```

```
Option(1) map add1  
// res1: Option[Int] = Some(2)
```

```
// Option(1) map sum2Ints  
// [error] found   : (Int, Int) => Int  
// [error] required: Int => ?  
// [error] Option(1) map sum2Ints  
// [error]           ^
```

Where Functor is too weak ...

What to do if we want to fuse two Options to one by summing up the contained values?

Option(1) + Option(2) == Option(3) // ???

```
val add1: Int => Int = 1 + _  
val sum2Ints: (Int, Int) => Int = _ + _
```

```
Option(1) map add1  
// res1: Option[Int] = Some(2)
```

```
// Option(1) map sum2Ints  
// [error] found   : (Int, Int) => Int  
// [error] required: Int => ?  
// [error] Option(1) map sum2Ints  
// [error]           ^
```

```
Option(1) map sum2Ints.curried  
// res2: Option[Int => Int] = Some(scala.Function2$$Lambda$4648/454529628@7c9e8cef)
```

Where Functor is too weak ...

What to do if we want to fuse two Options to one by summing up the contained values?

Option(1) + Option(2) == Option(3) // ???

```
val add1: Int => Int = 1 + _  
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```

```
Option(1) map add1  
// res1: Option[Int] = Some(2)
```

```
// Option(1) map sum2Ints  
// [error] found   : (Int, Int) => Int  
// [error] required: Int => ?  
// [error] Option(1) map sum2Ints  
// [error]           ^
```

```
Option(1) map sum2Ints.curried  
// res2: Option[Int => Int] = Some(scala.Function2$$Lambda$4648/454529628@7c9e8cef)
```

map doesn't help us to fuse another Option(2) to that.

... Applicative can help us out

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```
Option(1) map sum2Ints.curried ap Option(2)  
// res3: Option[Int] = Some(3)
```

... Applicative can help us out

```
Option(1) map sum2Ints.curried ap Option(2)  
// res3: Option[Int] = Some(3)
```

```
sum2Ints.curried.pure[Option] ap Option(1) ap Option(2)  
// res4: Option[Int] = Some(3)
```

... Applicative can help us out

```
Option(1) map sum2Ints.curried ap Option(2)  
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```

```
sum2Ints.curried.pure[Option] ap Option(1) ap Option(2)  
// res4: Option[Int] = Some(3)
```

```
sum2Ints.curried.pure[Option] ap 1.pure[Option] ap 2.pure[Option]  
// res5: Option[Int] = Some(3)           // pure is the same as Option.apply
```


... Applicative can help us out

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Option(1) map sum2Ints.curried ap Option(2)  
// res3: Option[Int] = Some(3)
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sum2Ints.curried.pure[Option] ap Option(1) ap Option(2)  
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```

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sum2Ints.curried.pure[Option] ap 1.pure[Option] ap 2.pure[Option]  
// res5: Option[Int] = Some(3)           // pure is the same as Option.apply
```

```
Applicative[Option].ap2(sum2Ints.pure[Option])(Option(1), Option(2))  
// res6: Option[Int] = Some(3)           // no currying with ap2
```

... Applicative can help us out

```
Option(1) map sum2Ints.curried ap Option(2)  
// res3: Option[Int] = Some(3)
```

```
sum2Ints.curried.pure[Option] ap Option(1) ap Option(2)  
// res4: Option[Int] = Some(3)
```

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Applicative[Option].ap2(sum2Ints.pure[Option])(Option(1), Option(2))  
// res6: Option[Int] = Some(3)           // no currying with ap2
```

```
Applicative[Option].map2(Option(1), Option(2))(sum2Ints)  
// res7: Option[Int] = Some(3)           // no pure with map2
```

... Applicative can help us out

```
Option(1) map sum2Ints.curried ap Option(2)  
// res3: Option[Int] = Some(3)
```

```
sum2Ints.curried.pure[Option] ap Option(1) ap Option(2)  
// res4: Option[Int] = Some(3)
```

```
sum2Ints.curried.pure[Option] ap 1.pure[Option] ap 2.pure[Option]  
// res5: Option[Int] = Some(3)           // pure is the same as Option.apply
```

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Applicative[Option].ap2(sum2Ints.pure[Option])(Option(1), Option(2))  
// res6: Option[Int] = Some(3)           // no currying with ap2
```

```
Applicative[Option].map2(Option(1), Option(2))(sum2Ints)  
// res7: Option[Int] = Some(3)           // no pure with map2
```

```
(Option(1), Option(2)) mapN sum2Ints  
// res8: Option[Int] = Some(3)           // Tuple2#mapN
```

Cartesian Product

When working with `Applicative` we always get the Cartesian product of two or more contexts. That isn't obvious when working with the *Option* context but becomes evident when we work with *List*.

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val add2: Int => Int => Int = ((_:Int) + (_:Int)).curried
val mult2: Int => Int => Int = ((_:Int) * (_:Int)).curried
val concat: (String, String) => String = _ ++ _
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val mult2: Int => Int => Int = ((_:Int) * (_:Int)).curried
val concat: (String, String) => String = _ ++ _
```

```
List((_:Int) * 0, (_:Int) + 100, (x:Int) => x * x) ap List(1, 2, 3)
// res10: List[Int] = List(0, 0, 0, 101, 102, 103, 1, 4, 9)
```

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```
List((_:Int) * 0, (_:Int) + 100, (x:Int) => x * x) ap List(1, 2, 3)
// res10: List[Int] = List(0, 0, 0, 101, 102, 103, 1, 4, 9)
```

```
List(add2, mult2) <*> List[Int](1, 2) <*> List[Int](100, 200)
// res11: List[Int] = List(101, 201, 102, 202, 100, 200, 200, 400)
```

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val mult2: Int => Int => Int = ((_:Int) * (_:Int)).curried
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```

```
List((_:Int) * 0, (_:Int) + 100, (x:Int) => x * x) ap List(1, 2, 3)
// res10: List[Int] = List(0, 0, 0, 101, 102, 103, 1, 4, 9)
```

```
List(add2, mult2) <*> List[Int](1, 2) <*> List[Int](100, 200)
// res11: List[Int] = List(101, 201, 102, 202, 100, 200, 200, 400)
```

```
concat.curried.pure[List] <*> List("ha", "heh", "hmm") <*> List("?", "!", ".")
// res12: List[String] = List(ha?, ha!, ha., heh?, heh!, heh., hmm?, hmm!, hmm.)
```


Cartesian Product

When working with Applicative we always get the Cartesian product of two or more contexts. That isn't obvious when working with the *Option* context but becomes evident when we work with *List*.

```
val add2: Int => Int => Int = ((_:Int) + (_:Int)).curried
val mult2: Int => Int => Int = ((_:Int) * (_:Int)).curried
val concat: (String, String) => String = _ ++ _
```

```
List((_:Int) * 0, (_:Int) + 100, (x:Int) => x * x) ap List(1, 2, 3)
// res10: List[Int] = List(0, 0, 0, 101, 102, 103, 1, 4, 9)
```

```
List(add2, mult2) <*> List[Int](1, 2) <*> List[Int](100, 200)
// res11: List[Int] = List(101, 201, 102, 202, 100, 200, 200, 400)
```

```
concat.curried.pure[List] <*> List("ha", "heh", "hmm") <*> List("?", "!", ".")
// res12: List[String] = List(ha?, ha!, ha., heh?, heh!, heh., hmm?, hmm!, hmm.)
```

```
List("ha", "heh", "hmm") map concat.curried ap List("?", "!", ".")
// res13: List[String] = List(ha?, ha!, ha., heh?, heh!, heh., hmm?, hmm!, hmm.)
```

5. Applicative Processing

See: *examples.ApplicativeProcessing*

Trait Applicative

Trait Applicative

Applicative is stronger than Functor, but weaker than Monad.

Trait Applicative

Applicative is stronger than Functor, but weaker than Monad.

```
trait Functor[F[_]] { // simplified
  def map[A, B](fa: F[A])(f: A => B): F[B]
}
```

Trait Applicative

Applicative is stronger than Functor, but weaker than Monad.

```
trait Functor[F[_]] { // simplified
  def map[A, B](fa: F[A])(f: A => B): F[B]
}
```

```
trait Applicative[F[_]] extends Functor[F] { // simplified
  def pure[A](a: A): F[A]
  def ap[A, B](ff: F[A => B])(fa: F[A]): F[B]
}
```

Trait Applicative

Applicative is stronger than Functor, but weaker than Monad.

```
trait Functor[F[_]] { // simplified
  def map[A, B](fa: F[A])(f: A => B): F[B]
}
```

```
trait Applicative[F[_]] extends Functor[F] { // simplified
  def pure[A](a: A): F[A]
  def ap[A, B](ff: F[A => B])(fa: F[A]): F[B]
}
```

```
trait Monad[F[_]] extends Applicative[F] { // simplified
  def flatMap[A, B](fa: F[A])(f: A => F[B]): F[B]
}
```

Replacing monadic with applicative context

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Applicative is strong enough for the problem
we solved before with a monad-comprehension.

Replacing monadic with applicative context

Applicative is strong enough for the problem we solved before with a monad-comprehension.

Monadic context: $F[_]$ constrained to be a *Monad*

```
def processABC[F[_]: Monad, A, B, C, D](compute: (A, B, C) => D)
  (fa: F[A], fb: F[B], fc: F[C]): F[D] =
  ??? // monadic solution
```

Replacing monadic with applicative context

Applicative is strong enough for the problem we solved before with a monad-comprehension.

Monadic context: $F[_]$ constrained to be a *Monad*

```
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                                     (fa: F[A], fb: F[B], fc: F[C]): F[D] =
  ??? // monadic solution
```

Applicative context: $F[_]$ constrained to be an *Applicative*

```
def processABC[F[_]: Applicative, A, B, C, D](compute: (A, B, C) => D)
                                     (fa: F[A], fb: F[B], fc: F[C]): F[D] =
  ??? // applicative solution
```

Replacing monadic with applicative context

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                                     (fa: F[A], fb: F[B], fc: F[C]): F[D] =
  ??? // monadic solution
```

Applicative context: $F[_]$ constrained to be an *Applicative*

```
def processABC[F[_]: Applicative, A, B, C, D](compute: (A, B, C) => D)
                                     (fa: F[A], fb: F[B], fc: F[C]): F[D] =
  ??? // applicative solution
```

Let's start with *Option[Int]* again and then abstract the solution.

Solution with *Applicative#ap*:

Example context/effect: *Option*

```
def processInts(compute: (Int, Int, Int) => Int)
  (oi1: Option[Int], oi2: Option[Int], oi3: Option[Int])
  : Option[Int] = {
  val f3Curried: Int => Int => Int => Int = compute.curried
  val of3: Option[Int => Int => Int => Int] = Some(f3Curried) // lifting
  val of2: Option[Int => Int => Int] = of3 ap oi1 // same as: oi1 map of3
  val of1: Option[Int => Int] = of2 ap oi2
  val result: Option[Int] = of1 ap oi3
  result
}
```

Some(f3Curried) lifts the curried function into the *Option* context.

Abstracting *Option* to $F[_]:\text{Applicative}$

```
def processInts[F[_]: Applicative](compute: (Int, Int, Int) => Int)
                                   (fi1: F[Int], fi2: F[Int], fi3: F[Int])
                                   : F[Int] = {
  val fCurried: Int => Int => Int => Int = compute.curried
  val ff: F[Int => Int => Int => Int] = Applicative[F].pure(fCurried) // lifting
  ff ap fi1 ap fi2 ap fi3
}
```

Applicative[F].pure(fCurried) lifts the curried function into the generic F context.

Abstracting away the *Ints*

```
def processABC[F[_]: Applicative, A, B, C, D](compute: (A, B, C) => D)
  (fa: F[A], fb: F[B], fc: F[C])
  : F[D] = {
  val fCurried: A => B => C => D = compute.curried
  val ff: F[A => B => C => D] = Applicative[F].pure(fCurried)
  ff ap fa ap fb ap fc
}
```

Using *pure* syntax and `<*>` (alias for *ap*)

```
def processABC[F[_]: Applicative, A, B, C, D](compute: (A, B, C) => D)
  (fa: F[A], fb: F[B], fc: F[C])
  : F[D] = {
  compute.curried.pure[F] <*> fa <*> fb <*> fc
}
```


Applicative#ap3 saves us from currying

```
def processABC[F[_]: Applicative, A, B, C, D](compute: (A, B, C) => D)
  (fa: F[A], fb: F[B], fc: F[C])
  : F[D] = {
  Applicative[F].ap3(compute.pure[F])(fa, fb, fc)
}
```

Applicative#map3 avoids lifting with *pure*

```
def processABC[F[_]: Applicative, A, B, C, D](compute: (A, B, C) => D)
  (fa: F[A], fb: F[B], fc: F[C])
  : F[D] = {
  Applicative[F].map3(fa, fb, fc)(compute)
}
```

map2, map3 .. map22 are available for *Applicative*.

Apply is just *Applicative* without *pure*

```
def processABC[F[_]: Apply, A, B, C, D](compute: (A, B, C) => D)
                                         (fa: F[A], fb: F[B], fc: F[C])
                                         : F[D] = {
  Apply[F].map3(fa, fb, fc)(compute)
}
```

map2, *map3* .. *map22* come from *Apply*.

Apply is a base trait of *Applicative* and provides us *map3*.

Using *Tuple3#mapN* for convenience

```
def processABC[F[_]: Apply, A, B, C, D](compute: (A, B, C) => D)
  (fa: F[A], fb: F[B], fc: F[C])
  : F[D] = {
  (fa, fb, fc) mapN compute
}
```

We just tuple up the three *F*'s and invoke *mapN* with a function that takes three parameters. *mapN* fuses the *F*'s into an *F*-result.

Cats provides *mapN* as an enrichment for *Tuple2*, *Tuple3* .. *Tuple22*.

Comparing the solutions

Comparing the solutions

Monadic solution:

```
def processABC[F[_]: Monad, A, B, C, D](compute: (A, B, C) => D)
  (fa: F[A], fb: F[B], fc: F[C]): F[D] =
  for {
    a <- fa
    b <- fb
    c <- fc
  } yield compute(a, b, c)
```

Comparing the solutions

Monadic solution:

```
def processABC[F[_]: Monad, A, B, C, D](compute: (A, B, C) => D)
  (fa: F[A], fb: F[B], fc: F[C]): F[D] =
  for {
    a <- fa
    b <- fb
    c <- fc
  } yield compute(a, b, c)
```

Applicative solution:

```
def processABC[F[_]: Apply, A, B, C, D](compute: (A, B, C) => D)
  (fa: F[A], fb: F[B], fc: F[C]) : F[D] =
  (fa, fb, fc) mapN compute
```

Currying again

Currying again

We provided *processABC* with two parameter lists.

```
def processABC[F[_]: Apply, A, B, C, D](compute: (A, B, C) => D)  
  (fa: F[A], fb: F[B], fc: F[C]) : F[D] =  
  (fa, fb, fc) mapN compute
```

Currying again

We provided *processABC* with two parameter lists.

```
def processABC[F[_]: Apply, A, B, C, D](compute: (A, B, C) => D)  
    (fa: F[A], fb: F[B], fc: F[C]) : F[D] =  
    (fa, fb, fc) mapN compute
```

This improves composability and allows us provide the *compute* function and the effectful *F*'s in separate steps.

Currying again

We provided *processABC* with two parameter lists.

```
def processABC[F[_]: Apply, A, B, C, D](compute: (A, B, C) => D)
                                     (fa: F[A], fb: F[B], fc: F[C]) : F[D] =
  (fa, fb, fc) mapN compute
```

This improves composability and allows us provide the *compute* function and the effectful *F*'s in separate steps.

```
// providing the computation
def processEffectfulInts[F[_]: Apply](fi1: F[Int], fi2: F[Int], fi3: F[Int])
                                     : F[Int] =
  processABC(sum3Ints)(fi1, fi2, fi3)
```

Currying again

We provided *processABC* with two parameter lists.

```
def processABC[F[_]: Apply, A, B, C, D](compute: (A, B, C) => D)
                                     (fa: F[A], fb: F[B], fc: F[C]) : F[D] =
  (fa, fb, fc) mapN compute
```

This improves composability and allows us provide the *compute* function and the effectful *F*'s in separate steps.

```
// providing the computation
def processEffectfulInts[F[_]: Apply](fi1: F[Int], fi2: F[Int], fi3: F[Int])
                                   : F[Int] =
  processABC(sum3Ints)(fi1, fi2, fi3)
```

```
// providing the 'effectful' parameters
val result1 = processEffectfulInts(Option(1), Option(2), Option(3))
// result1: Option[Int] = Some(6)
val result2 = processEffectfulInts(List(1, 2), List(10, 20), List(100, 200))
// result2: List[Int] = List(111, 211, 121, 221, 112, 212, 122, 222)
```

6. Comparing Monad with Applicative

Sequential vs. parallel

Sequential vs. parallel

Monads enforce sequential operation!

Imagine a for-comprehension.

The generators are executed in sequence, one after the other.

The yield clause is executed after all generators have finished.

Sequential vs. parallel

Monads enforce sequential operation!

Imagine a for-comprehension.

The generators are executed in sequence, one after the other.

The yield clause is executed after all generators have finished.

Applicatives allow for parallel/independent operations!

The operations are by nature independent of each other.

(That does not mean, they are asynchronous.)

Fail-fast semantics

Fail-fast semantics

Monads enforce short-circuiting!

If an 'erraneous' value (e.g. *None*, *Nil* or *Left*) is found in a monadic computation, the computation stops immediately, because the result will not change if processing were continued.

That is why we are not able to collect errors.

Fail-fast semantics

Monads enforce short-circuiting!

If an 'erraneous' value (e.g. *None*, *Nil* or *Left*) is found in a monadic computation, the computation stops immediately, because the result will not change if processing were continued.

That is why we are not able to collect errors.

Applicatives do not short-circuit!

As applicative operations are independent of each other, processing does not stop if an error occurs.

It is possible to collect errors (see: *cats.data.Validated*)

cats.data.Validated has an *Applicative* instance, but no *Monad* instance.

We will come to that later.

Composition

Composition

Monads do not compose!

In order to kind of 'compose' Monads we need an extra construct such as a Monad Transformer which itself is a Monad. I.e.: If we want to compose two Monads we need a third Monad to stack them up.

Composition

Monads do not compose!

In order to kind of 'compose' Monads we need an extra construct such as a Monad Transformer which itself is a Monad. I.e.: If we want to compose two Monads we need a third Monad to stack them up.

Applicatives compose!

Composition of (Functor and) Applicative is a breeze.
It is genuinely supported by these type classes.

See: *examples.Composition*

Composition - Code

```
val loi1 = List(Some(1), Some(2))  
val loi2 = List(Some(10), Some(20))
```

Monads do not compose!

```
def processMonadic(xs: List[Option[Int]], ys: List[Option[Int]]): List[Option[Int]]  
  val otli: OptionT[List, Int] = for {  
    x <- OptionT[List, Int](xs)  
    y <- OptionT[List, Int](ys)  
  } yield x + y  
  otli.value  
}  
val result1 = processMonadic(loi1, loi2)  
// result1: List[Option[Int]] = List(Some(11), Some(21), Some(12), Some(22))
```

Applicatives compose!

```
def processApplicative(xs: List[Option[Int]], ys: List[Option[Int]]): List[Option[Int]]  
  Applicative[List].compose[Option].map2(xs, ys)((_:Int) + (_:Int))  
  
val result2 = processApplicative(loi1, loi2)  
// result2: List[Option[Int]] = List(Some(11), Some(21), Some(12), Some(22))
```

When to use which

Use Applicative if all computations are independent of each other.

Howto:

- Write a monadic solution with a for-comprehension.
- If the generated values (to the left of the generator arrow `<-`) are only used in the *yield* clause at the end (not in an other generator) the computations are independent and allow for an applicative solution.
- Tuple up the computations and *mapN* them with a function which fuses the computation results to a final result.

(This howto is applicable only if the effect in question also has a Monad instance.)

When to use which - counter example

```
val result =  
  for {  
    x <- Future { computeX }  
    y <- Future { computeY(x) }  
    z <- Future { computeZ(x, y) }  
  } yield resultFrom(z)
```

In this for-comprehension the subsequent computations depend on the previous ones.

Hence this for-comprehension cannot be substituted by applicative processing.

Principle of Least Power

**Given a choice of solutions,
pick the least powerful solution
capable of solving your problem.**

-- Li Haoyi

7. The Applicative trait

Typeclass Functor

Functor is the base trait of *Applicative*.

```
trait Functor[F[_]] {  
  // ----- primitive map  
  def map[A, B](fa: F[A])(f: A => B): F[B]  
  // ----- implementations in terms of the primitive map  
  def fmap[A, B](fa: F[A])(f: A => B): F[B] = map(fa)(f) // alias for map  
  def lift[A, B](f: A => B): F[A] => F[B] = fa => map(fa)(f)  
  def as[A, B](fa: F[A], b: B): F[B] = map(fa)(_ => b)  
  def void[A](fa: F[A]): F[Unit] = as(fa, ())  
  def compose[G[_]: Functor]: Functor[Lambda[X => F[G[X]]]] = ???  
}
```

Typeclass Applicative

with primitives *pure* and *ap*

```
trait Applicative[F[_]] extends Functor[F] {  
  // ----- primitives  
  
  def pure[A](a: A): F[A]  
  def ap[A, B](ff: F[A => B])(fa: F[A]): F[B]  
  
  // ----- implementations in terms of the primitives  
  
  def map2[A, B, Z](fa: F[A], fb: F[B])(f: (A, B) => Z): F[Z] =  
    ap(map(fa)(a => f(a, _: B)))(fb)  
  
  override def map[A, B](fa: F[A])(f: A => B): F[B] =  
    ap(pure(f))(fa)  
  
  def product[A, B](fa: F[A], fb: F[B]): F[(A, B)] =  
    map2(fa, fb)((_, _))  
}
```

Typeclass Applicative

with primitives *pure* and *map2*

```
trait Applicative[F[_]] extends Functor[F] {  
  // ----- primitives  
  
  def pure[A](a: A): F[A]  
  def map2[A, B, Z](fa: F[A], fb: F[B])(f: (A, B) => Z): F[Z]  
  
  // ----- implementations in terms of the primitives  
  
  def ap[A, B](ff: F[A => B])(fa: F[A]): F[B] =  
    map2(ff, fa)((f, a) => f(a)) // or: map2(ff, fa)(_(_))  
  
  override def map[A, B](fa: F[A])(f: A => B): F[B] =  
    map2(fa, pure(()))((a, _) => f(a))  
  
  def product[A, B](fa: F[A], fb: F[B]): F[(A, B)] =  
    map2(fa, fb)((_, _))  
}
```

Typeclass Applicative

with primitives *pure* and *map* and *product*

```
trait Applicative[F[_]] extends Functor[F] {  
  // ----- primitives  
  
  def pure[A](a: A): F[A]  
  override def map[A, B](fa: F[A])(f: A => B): F[B]  
  def product[A, B](fa: F[A], fb: F[B]): F[(A, B)]  
  
  // ----- implementations in terms of the primitives  
  
  def map2[A, B, Z](fa: F[A], fb: F[B])(f: (A, B) => Z): F[Z] =  
    map(product(fa, fb)) { case (a, b) => f(a, b) }  
  
  def ap[A, B](ff: F[A => B])(fa: F[A]): F[B] =  
    map2(ff, fa)((f, a) => f(a)) // or: map2(ff, fa)(_(_))  
}
```

Typeclass Applicative

```
trait Applicative[F[_]] extends Functor[F] {  
  // ----- primitives  
  def pure[A](a: A): F[A]  
  def ap[A, B](ff: F[A => B])(fa: F[A]): F[B]  
  
  // ----- implementations in terms of the primitives  
  override def map[A, B](fa: F[A])(f: A => B): F[B] = ap(pure(f))(fa)  
  
  def <*>[A, B](ff: F[A => B])(fa: F[A]): F[B] = ap(ff)(fa) // alias for ap  
  
  def ap2[A, B, Z](ff: F[(A, B) => Z])(fa: F[A], fb: F[B]): F[Z] = {  
    val ffBZ: F[B => Z] = ap(map(ff)(f => (a:A) => (b:B) => f(a, b)))(fa)  
    ap(ffBZ)(fb)  
  } // also: ap3, ap4 .. ap22  
  
  def map2[A, B, Z](fa: F[A], fb: F[B])(f: (A, B) => Z): F[Z] =  
    ap(map(fa)(a => f(a, _: B)))(fb)  
  // also: map3, map4 .. map22  
  
  def product[A, B](fa: F[A], fb: F[B]): F[(A, B)] = map2(fa, fb)((_, _))  
  
  def tuple2[A, B](fa: F[A], fb: F[B]): F[(A, B)] = product(fa, fb)  
  // also: tuple3, tuple4 .. tuple22  
  
  def compose[G[_]: Applicative]: Applicative[Lambda[X => F[G[X]]]] = ???  
}
```


Cats typeclass hierarchy (a small section of it)

Complete hierarchy [here](#)

7. Either vs. Validated

See: *examples.EitherVsValidated*

Monadic processing with *Either*

Monadic processing enforces fail-fast semantics.
After an erroneous operation subsequent operations are not executed.
Hence we get only the first of possibly multiple errors.

Monadic processing with *Either*

Monadic processing enforces fail-fast semantics.
After an erroneous operation subsequent operations are not executed.
Hence we get only the first of possibly multiple errors.

```
val result: Either[List[String], Int] =  
  for {  
    x <- 5.asRight[List[String]]  
    y <- List("Error 1").asLeft[Int]  
    z <- List("Error 2").asLeft[Int] // List("Error 2") is lost!  
  } yield x + y + z  
  
// result: Either[List[String],Int] = Left(List(Error 1))
```

Applicative processing with *Either*

Applicative processing disables fail-fast semantics.
But with *Either* we get the same result as before.
Because *Either* has a Monad instance.

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But with *Either* we get the same result as before.
Because *Either* has a Monad instance.

```
val result: Either[List[String], Int] =  
  ( 5.asRight[List[String]],  
    List("Error 1").asLeft[Int],  
    List("Error 2").asLeft[Int] // List("Error 2") is lost!  
  ) mapN ((_: Int) + ( _: Int) + ( _: Int))  
  
// result: Either[List[String],Int] = Left(List(Error 1))
```

Applicative processing with *Validated*

cats.data.Validated is designed in analogy to *Either*.
Instead of *Right* and *Left* it has *Valid* and *Invalid*.
Validated has an *Applicative* instance but no *Monad* instance.

Applicative processing with *Validated*

cats.data.Validated is designed in analogy to *Either*.
Instead of *Right* and *Left* it has *Valid* and *Invalid*.
Validated has an Applicative instance but no Monad instance.

```
val result: Validated[List[String], Int] =  
  ( 5.valid[List[String]],  
    List("Error 1").invalid[Int],  
    List("Error 2").invalid[Int] // List("Error 2") is preserved!  
  ) mapN ((_: Int) + ( _: Int) + ( _: Int))  
  
// result: cats.data.Validated[List[String],Int] = Invalid(List(Error 1, Error 2))
```


Conversions between *Either* and *Validated*

Conversion is supported in both directions

Either#toValidated converts an *Either* to a *Validated*.

Validated#toEither converts a *Validated* to an *Either*.

Conversions between *Either* and *Validated*

Conversion is supported in both directions

Either#*toValidated* converts an *Either* to a *Validated*.

Validated#*toEither* converts a *Validated* to an *Either*.

```
val result: Validated[List[String], Int] =
  ( 5.asRight[List[String]].toValidated,
    List("Error 1").asLeft[Int].toValidated,
    List("Error 2").asLeft[Int].toValidated // List("Error 2") is preserved!
  ) mapN ((_: Int) + ( _: Int) + ( _: Int))

// result: cats.data.Validated[List[String],Int] = Invalid(List(Error 1, Error 2))

val resultAsEither = result.toEither
// resultAsEither: Either[List[String],Int] = Left(List(Error 1, Error 2))
```

Conversions between *Either* and *Validated*

Conversion is supported in both directions

Either#*toValidated* converts an *Either* to a *Validated*.

Validated#*toEither* converts a *Validated* to an *Either*.

```
val result: Validated[List[String], Int] =  
  ( 5.asRight[List[String]].toValidated,  
    List("Error 1").asLeft[Int].toValidated,  
    List("Error 2").asLeft[Int].toValidated // List("Error 2") is preserved!  
  ) mapN ((_: Int) + ( _: Int) + ( _: Int))  
  
// result: cats.data.Validated[List[String],Int] = Invalid(List(Error 1, Error 2))  
  
val resultAsEither = result.toEither  
// resultAsEither: Either[List[String],Int] = Left(List(Error 1, Error 2))
```

An elaborated example of form validation with *Validated* (contrasted to a solution with *Either*) can be found in the Cats documentation:

<https://typelevel.org/cats/datatypes/validated.html>

9. Traversals need Applicative

See: *examples.Traversals*

Recap: *Future.traverse* and *Future.sequence*

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Simply spoken: *sequence* turns a *List[Future[A]]* into a *Future[List[A]]*.

```
val lfd: List[Future[Double]] = List(Future(2.0), Future(4.0), Future(6.0))
val fld: Future[List[Double]] = Future.sequence(lfd)
```

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Typically in an application we don't have a *List[Future[B]]*, but we produce it by processing a *List[A]* asynchronously.

We can first map the *List[A]* with the function *A => Future[B]* and then invoke *sequence* on the resulting *List[Future[B]]* in order to get a *Future[List[B]]*.

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```
val li: List[Int] = List(1, 2, 3)
val doubleItAsync: Int => Future[Double] = x => Future { x * 2.0 }
val lfi: List[Future[Double]] = li.map(doubleItAsync)
val fld: Future[List[Double]] = Future.sequence(lfi)
```

Recap: *Future.traverse* and *Future.sequence*

Mapping and sequencing traverses the list twice.

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Future.traverse takes a *List[A]* and a mapping function from $A \Rightarrow Future[B]$ and returns a *Future[List[B]]*.

```
val li: List[Int] = List(1, 2, 3)
val doubleItAsync: Int => Future[Double] = x => Future { x * 2.0 }
val fld: Future[List[Double]] = Future.traverse(li)(doubleItAsync)
```

Recap: *Future.traverse* and *Future.sequence*

Mapping and sequencing traverses the list twice.
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Future.traverse takes a *List[A]* and a mapping function from $A \Rightarrow Future[B]$ and returns a *Future[List[B]]*.

```
val li: List[Int] = List(1, 2, 3)
val doubleItAsync: Int => Future[Double] = x => Future { x * 2.0 }
val fld: Future[List[Double]] = Future.traverse(li)(doubleItAsync)
```

Providing *identity* as mapping function to *traverse* has the same effect as *sequence*.

```
val lfd: List[Future[Double]] = List(Future(2.0), Future(4.0), Future(6.0))
val fld: Future[List[Double]] = Future.traverse(lfd)(identity)
```

Typeclass *Traverse*

Cats generalizes this concept into the *Traverse* typeclass.

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```
trait Traverse[F[_]] extends Foldable[F] with Functor[F] { // simplified

  def traverse[G[_]: Applicative, A, B](fa: F[A])(f: A => G[B]) : G[F[B]]

  def sequence[G[_]: Applicative, A](fga: F[G[A]]): G[F[A]] =
    traverse(fga)(identity)

  // map in terms of traverse using the Id context
  override def map[A, B](fa: F[A])(f: A => B): F[B] = traverse(fa)(f: A => Id[B])
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Hence *Traverse* extends these two traits.

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traverse and *sequence* require the *G[_]* to be an *Applicative* (*Future* before).

The structure traversed over (*List* before) must be *Foldable with Functor*.
Hence *Traverse* extends these two traits.

The *traverse* function can indeed be implemented with *map* and *foldLeft* or *foldRight*. On the other hand *foldLeft*, *foldRight* and *map* can be implemented with *traverse*.

Traverse[List].sequence[Future, A]

Instead of *Future.sequence* we can use *Traverse[List].sequence*.

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```
val lfd: List[Future[Double]] = List(Future(2.0), Future(4.0), Future(6.0))  
  
val fld1: Future[List[Double]] = Traverse[List].sequence(lfd)  
// fld1: scala.concurrent.Future[List[Double]] = Future(Success(List(2.0, 4.0, 6.0))  
  
import cats.syntax.traverse._ // supports 'sequence' as an enrichment of List  
  
val fld2: Future[List[Double]] = lfd.sequence  
// fld2: scala.concurrent.Future[List[Double]] = Future(Success(List(2.0, 4.0, 6.0))
```

Traverse[List].traverse[Future, A, B]

Instead of *Future.traverse* we can use *Traverse[List].traverse*.

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Instead of *Future.traverse* we can use *Traverse[List].traverse*.

```
val li: List[Int] = List(1, 2, 3)

val doubleItAsync: Int => Future[Double] = x => Future { x * 2.0 }

val fld1: Future[List[Double]] = Traverse[List].traverse(li)(doubleItAsync)
// fld1: scala.concurrent.Future[List[Double]] = Future(Success(List(2.0, 4.0, 6.0))

import cats.syntax.traverse._ // supports 'traverse' as an enrichment of List

val fld2: Future[List[Double]] = li traverse doubleItAsync
// fld2: scala.concurrent.Future[List[Double]] = Future(Success(List(2.0, 4.0, 6.0))
```

Traverse[Vector].traverse[Option, A, B]

With *cats.Traverse* can traverse not only over *Lists* but over any other *Foldable with Functor* that has a *Traverse* instance, e.g. *Vector*. The mapping function may produce any applicative effect, e.g. *Option* instead of *Future*.

Traverse[Vector].traverse[Option, A, B]

With *cats.Traverse* can traverse not only over *Lists* but over any other *Foldable with Functor* that has a *Traverse* instance, e.g. *Vector*. The mapping function may produce any applicative effect, e.g. *Option* instead of *Future*.

```
val vi1: Vector[Int] = Vector(3, 2, 1)
val vi2: Vector[Int] = Vector(3, 2, 0)

val divideBy: Int => Option[Double] = x => if (x == 0) None else Some { 6.0 / x }

val ovd1_1 = Traverse[Vector].traverse(vi1)(divideBy)
// ovd1_1: Option[Vector[Double]] = Some(Vector(2.0, 3.0, 6.0))
val ovd1_2 = Traverse[Vector].traverse(vi2)(divideBy)
// ovd1_2: Option[Vector[Double]] = None

import cats.syntax.traverse._ // supports 'traverse' as an enrichment of Vector

val ovd2_1 = vi1 traverse divideBy
// ovd2_1: Option[Vector[Double]] = Some(Vector(2.0, 3.0, 6.0))
val ovd2_2 = vi2 traverse divideBy
// ovd2_2: Option[Vector[Double]] = None
```

10. Resources

Scala Resources (1/2)

- Code and Slides of this Talk:
<https://github.com/hermannhueck/use-applicative-where-applicable>
- Cats documentation:
<https://typelevel.org/cats/typeclasses/applicative.html>
<https://typelevel.org/cats/typeclasses/traverse.html>
<https://typelevel.org/cats/datatypes/validated.html>
- Herding Cats, Day 2 and 3:
<http://eed3si9n.com/herding-cats/Functor.html>
<http://eed3si9n.com/herding-cats/Semigroupal.html>
<http://eed3si9n.com/herding-cats/Apply.html>
<http://eed3si9n.com/herding-cats/Applicative.html>
- "Scala with Cats", Chapters 6 and 7
Book by Noel Welsh and Dave Gurnell
<https://underscore.io/books/scala-with-cats/>

Scala Resources (2/2)

- Live Coding Tutorial on Functor and Applicative by Michael Pilquist
FSiS Part 1 - Type Constructors, Functors, and Kind Projector
<https://www.youtube.com/watch?v=Dsd4pc99FSY>
FSiS Part 2 - Applicative type class
https://www.youtube.com/watch?v=tD_EyIKqqCk

Haskell Resources

- Learn You a Haskell for Great Good!, Chapter 11
Online book by Miran Lipovaca
<http://learnyouahaskell.com/functors-applicative-functors-and-monoids>
- Applicative Programming with Effects
Conor McBride and Ross Paterson in Journal of Functional Programming
18:1 (2008), pages 1-13
<http://www.staff.city.ac.uk/~ross/papers/Applicative.pdf>
- The Essence of the Iterator Pattern
Jeremy Gibbons and Bruno C. d. S. Oliveira, Oxford University Computing
Laboratory
<https://www.cs.ox.ac.uk/jeremy.gibbons/publications/iterator.pdf>

Thanks for Listening

Q & A

<https://github.com/hermannhueck/use-applicative-where-applicable>

