
Algorithm Knapsack (S, K) ;

Input: S (an array of size n storing the sizes of the items),
and K (the size of the knapsack).

Output: P (a two-dimensional array such that $P[i, k].exist = \text{true}$ if there exists a solution to the knapsack problem with the first i elements and a knapsack of size k , and $P[i, k].belong = \text{true}$ if the i th element belongs to that solution).

{ See Exercise 5.15 for suggestions about improving this program. }

begin

$P[0, 0].exist := \text{true}$;

for $k := 1$ **to** K **do**

$P[0, k].exist := \text{false}$;

{ there is no need to initialize $P[i, 0]$ for $i \geq 1$, because it will
be computed from $P[0, 0]$ }

for $i := 1$ **to** n **do**

for $k := 0$ **to** K **do**

$P[i, k].exist := \text{false}$; { the default value }

if $P[i-1, k].exist$ **then**

$P[i, k].exist := \text{true}$;

$P[i, k].belong := \text{false}$

else if $k - S[i] \geq 0$ **then**

if $P[i-1, k - S[i]].exist$ **then**

$P[i, k].exist := \text{true}$;

$P[i, k].belong := \text{true}$

end

Figure 5.10 Algorithm *Knapsack*.

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
$k_1=2$	O	-	I	-	-	-	-	-	-	-	-	-	-	-	-	-	-
$k_2=3$	O	-	O	I	-	I	-	-	-	-	-	-	-	-	-	-	-
$k_3=5$	O	-	O	O	-	O	-	I	I	-	I	-	-	-	-	-	-
$k_4=6$	O	-	O	O	-	O	I	O	O	I	O	I	-	I	I	-	I

Figure 5.11 An example of the table constructed for the knapsack problem. The input consists of four items of sizes 2, 3, 5, and 6. The symbols in the table are the following: "I": a solution containing this item has been found; "O": a solution without this item has been found; "-": no solution has not yet been found. (If the symbol "-" appears in the last line, then there is no solution for a knapsack of this size.)