Session 3.1

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Notes to keep in mind

Make sure you have these things in your notes, because I will refer to them with the expectation that you have learned, memorized, or written them down.

- 1. Two lines are **parallel** if they have the same slope
- 2. Points are <u>collinear</u> if they lie on the same line. *Note:* it is sufficient to check slopes between all the points are equal (think about it!).
- 3. Two lines are **perpendicular** if the slope of one is the negative inverse of the other.
 - (a) Slopes are m_1 and m_2 and $m_1 = -\frac{1}{m_2}$
 - (b) The y-intercepts don't matter draw it out and see why it makes sense!
- 4. Characteristics of a polynomial, such as $ax^2 + bx + c$, or, more generally $ax^n + bx^{n-1} + \ldots + z$
 - (a) The **degree** of a polynomial is the highest variable exponent, such as 2 or n
 - (b) The **leading coefficient** is the coefficient of the variable with the highest degree, such as a
 - (c) The **constant term** is the number without a variable next to it, such as c or z

Main problems

1. Find all points on the following graphs with the specified value of y

(a)
$$y = |x - 3|$$
 where $y = 7$

(b)
$$y = |x+5| - 11$$
 where $y = -5$

- 2. Find the y-intercept of a line that has slope -3 and passes through (-5, 18).
- 3. For each line, write two line equations of one that is parallel, and one that is perpendicular

(a)
$$y = \frac{3}{2}x - 2$$

(b)
$$y = -1.2x + 1$$

- 4. Find an equation of the line through the point (-3,2) that is parallel to the line $y = \frac{2}{3}x 1$. Also find one that is perpendicular.
- 5. For each set of three points say whether or not they're on the same line, and prove it.

(a)
$$(5,8)$$
, $(1,14)$, and $(11,-1)$

(b)
$$(-1,6), (-5,17), \text{ and } (3,-4)$$

6. For each of the systems of equations, find the (x, y) solution with the substitution method

(a)
$$\begin{cases} -5x + 2y = 9\\ y = 7x \end{cases}$$

(c)
$$\begin{cases} 8x + 5y = 24\\ y = -4x \end{cases}$$

(b)
$$\begin{cases} 15x + 31y = -3 \\ x = -y + 3 \end{cases}$$

(d)
$$\begin{cases} 10x - 9y = 24 \\ y = x - 2 \end{cases}$$

7. For each of the systems of equations, find the (x,y) solution with the elimination method

(a)
$$\begin{cases} 3x - 4y = 8 \\ 18x - 5y = 10 \end{cases}$$

(b)
$$\begin{cases} 6x - 5y = -32 \\ -7x + 8y = 46 \end{cases}$$
 (c)
$$\begin{cases} -2x - 7y = 30 \\ 7x + 4y = 18 \end{cases}$$

(c)
$$\begin{cases} -2x - 7y = 30\\ 7x + 4y = 18 \end{cases}$$

8. For each of the systems of equations, find the (x, y) solution. If there are \underline{no} or infinitely many solutions, say that too!

(a)
$$\begin{cases} 6x - 3y = 5\\ y - 2x = 8 \end{cases}$$

(c)
$$\begin{cases} 2x = 3y - 1 \\ 6x - 9y = -3 \end{cases}$$

(e)
$$\begin{cases} 5x - 6y = -25 \\ 4x - 3y + 20 = 0 \end{cases}$$

(a)
$$\begin{cases} 6x - 3y = 5 \\ y - 2x = 8 \end{cases}$$
 (c)
$$\begin{cases} 2x = 3y - 1 \\ 6x - 9y = -3 \end{cases}$$

(b)
$$\begin{cases} -4x + 7y + 5 = 0 \\ x - 3y = -5 \end{cases}$$
 (d)
$$\begin{cases} y = 3x + 8 \\ 12x - 4y = -32 \end{cases}$$

(d)
$$\begin{cases} y = 3x + 8 \\ 12x - 4y = -32 \end{cases}$$

9. Simplify each of the following polynomials

(a) Add
$$6x^2 - 2x - 1$$
 to $-4x^2 + 7x + 5$

(b) Subtract
$$-7x^2 + 3x - 9$$
) from $5x^2 - 6x - 4$

(c) Subtract
$$-7x^2 + 3x - 6$$
) from $3x^2 + 4x + 4$

(d) Add
$$-8x^2 + 11x - 6$$
 to $-7x^2 - 9x + 14$

(e) Multiply/expand
$$(x+4)(x-3)$$

(f) Multiply/expand
$$(x+5)(x+7)$$

10. Graph each of the following quadratic polynomials

(a)
$$y = x^2$$

(e)
$$y = -x^2$$

(h)
$$y = -(x+4)^2$$

(b)
$$y = x^2 + 3$$

(f)
$$y = \frac{1}{2}x^2$$

(i)
$$y = 2(x+4)^2$$

(c)
$$y = x^2 - 4$$

(f)
$$y = \frac{1}{2}x^2$$

(j)
$$y = (x+2)^2 - 5$$

(d)
$$y = 2x^2$$

(g)
$$y = (x-3)^2$$

(k)
$$y = -(x-5)^2 + 7$$

11. In general, what happens if we add 2 to the constant term? subtract 2? add c (a constant)?

12. In general, what happens if we multiply the polynomial by -1?

13. In general, what happens if we add 2 to x in an equation (inside the quadratic)? subtract 3? add c (a constant)?

More problems

1. Work on: 2013 AMC 10A

2. Use the "Noah sheets"