

$$C = S_t N(d_1) - K e^{-rt} N(d_2)$$

where;

$$d_1 = \frac{\ln \frac{S}{K} + (r + \frac{\sigma^2}{2})t}{\sigma \sqrt{t}} \quad , \quad d_2 = d_1 - \sigma \sqrt{t}$$

SOLUTION

$$S = \$40$$

$$K = \$45$$

$$t = 4 \text{ months} = 0.33 \text{ yrs}$$

$$r = 3 \% = 0.03$$

$$\sigma = 40 \% = 0.4$$

$$d_1 = \frac{\ln(\frac{40}{45}) + (0.03 + \frac{0.4^2}{2})0.3333}{4\sqrt{0.3333}}$$

$$\frac{\ln(0.8889) + (0.03 + 0.08)0.3333}{0.23093}$$

$$\frac{-0.11778 + 0.03667}{0.23093}$$

$$\frac{-0.08111}{0.23093}$$

$$= -0.35123$$

$$d_2 = -0.35123 - (0.4)\sqrt{0.3333}$$

$$-0.35123 - 0.13333$$

$$-0.58217$$

Therefore approximating the D values to 2 decimal places

$$d_1 = -0.35, \quad d_2 = -0.58$$

Using the standard normal distribution table

$$N(d_1) = 0.3632, \quad N(d_2) = 0.2810$$

$$\text{Black-Scholes Call price, } C = 40(0.3632) - 45(e^{-0.03(\frac{1}{3})})(0.2810)$$

$$C = 14.528 - 12.519$$

$$C = \$2.009$$