

省题1.

$$(1) \quad x_i = 0 \Rightarrow \sum_i w^T x_i - 1 + \xi_i = 0$$

$$y_i w^T x_i = 1 - \xi_i$$

$$\geq 1 \quad (\because \xi_i \geq 0)$$

(Q.E.D)

(2) $0 < \alpha_i < C \Rightarrow \beta_i \neq 0$

$$\therefore \xi_i = 0 \quad (\because \beta_i \xi_i = 0)$$

$$y_i w^T x_i - 1 + \xi_i, 0$$

$$y_i w^T x_i = 1 \quad (\text{Q.E.D.})$$

(3) $\alpha_i = C \Rightarrow \beta_i = 0$ ($\because \alpha_i + \beta_i = C$)

$$\therefore \zeta_i \neq 0 \quad \therefore \zeta_i > 0$$

$$y_i w^T x_i = 1 - \epsilon_i$$

$$> 1 \quad (\because \epsilon_i > 0)$$

(R.F.D)

$$(4) \quad y_i w^T x_i > 1 \Rightarrow y_i w^T x_i - 1 + \xi_i > 0 \quad (\because \xi_i \geq 0)$$

$$\therefore \alpha_i = 0$$

$$(5) \quad y_i w^T x_i < 1 \Rightarrow y_i w^T x_i - 1 + \xi_i \geq 0 \quad \forall i$$

$$\therefore \alpha_i = C$$