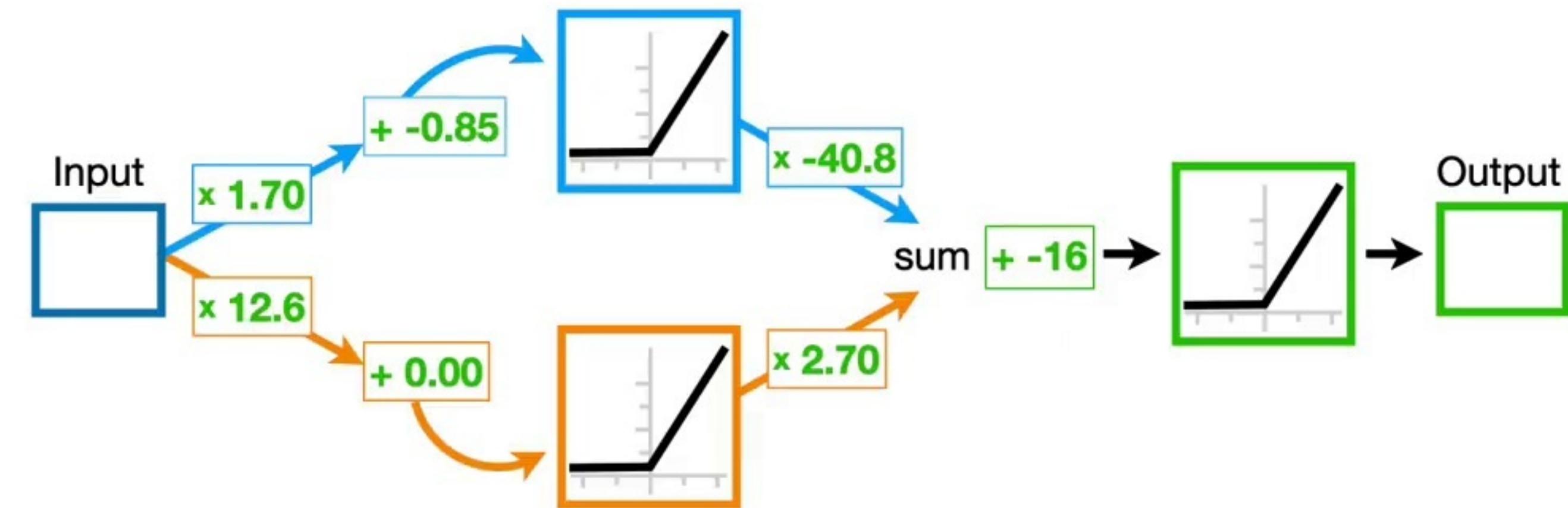
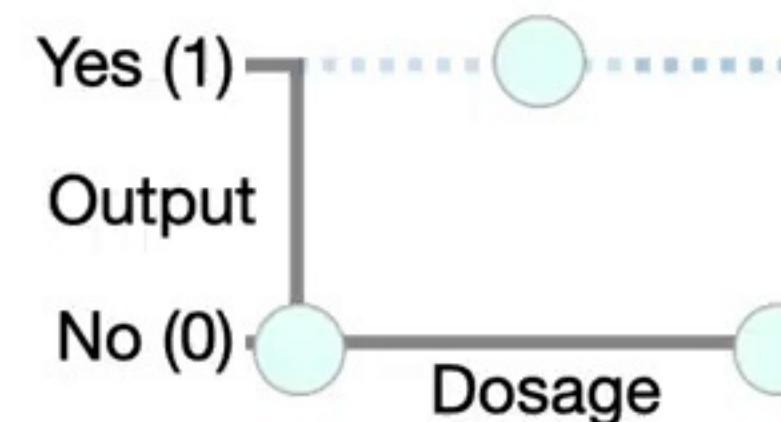


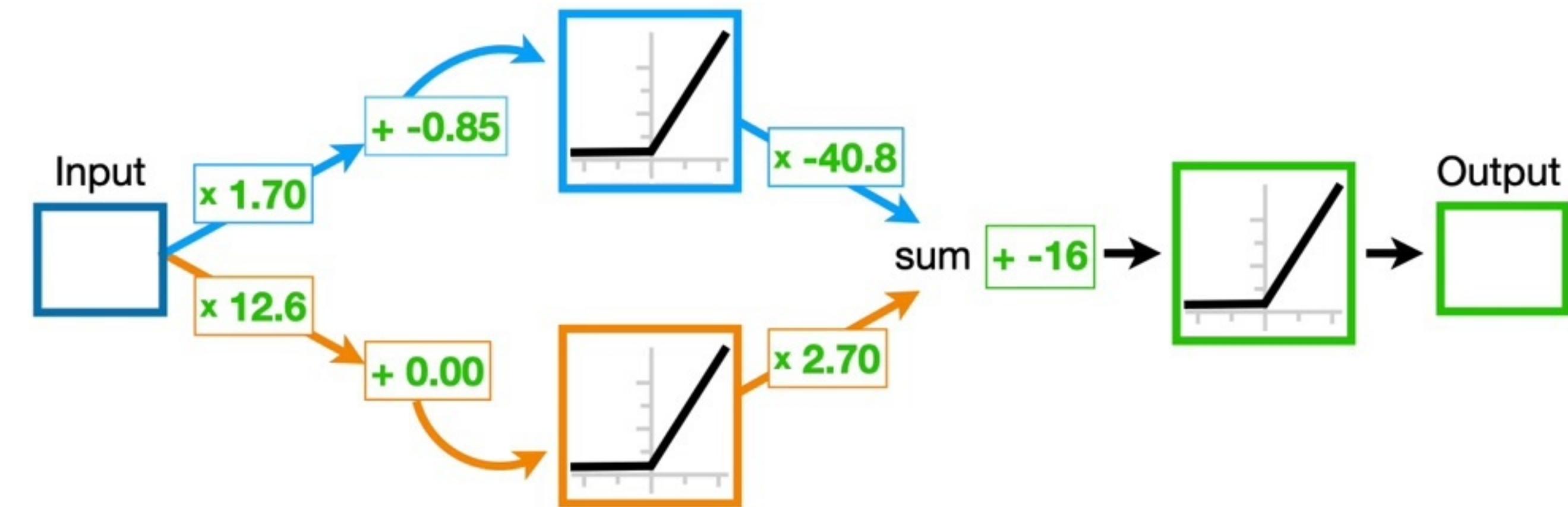
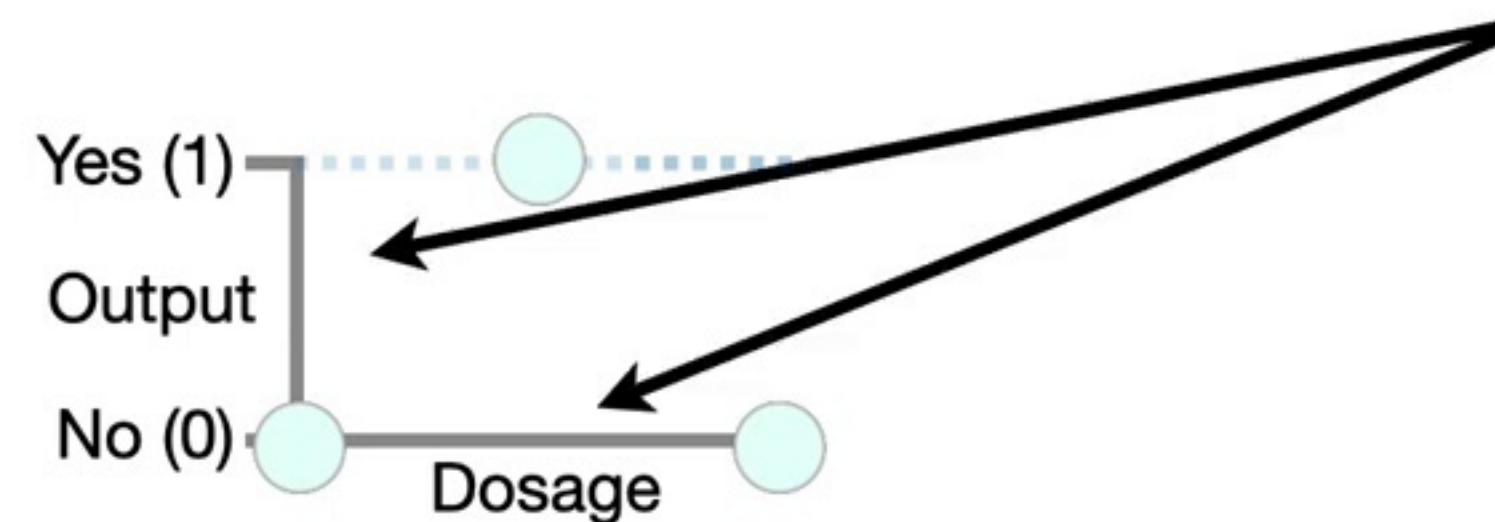


So far the **Neural Networks** that we've looked at have been super simple...



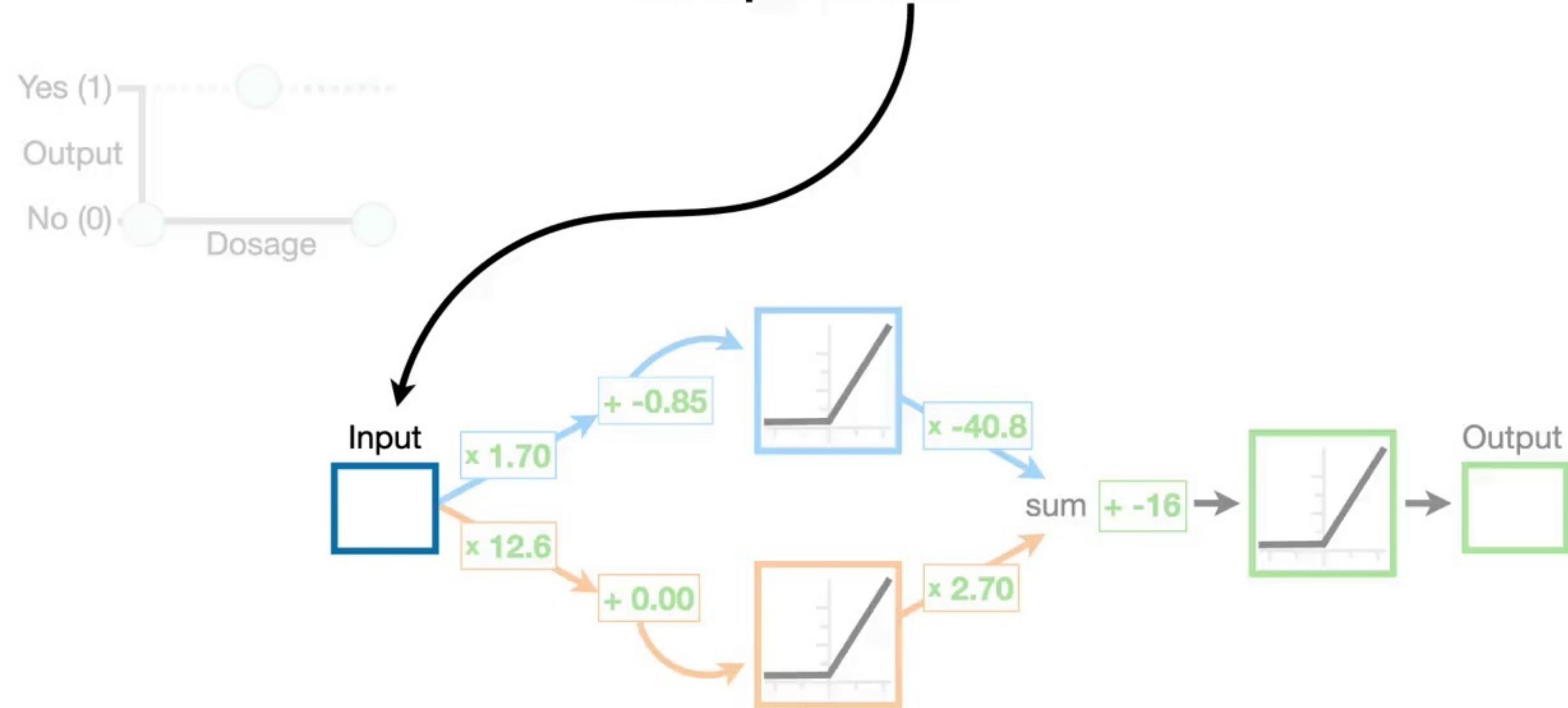


...and only predict whether or not the  
**Dosage** of a drug will be **Effective**.



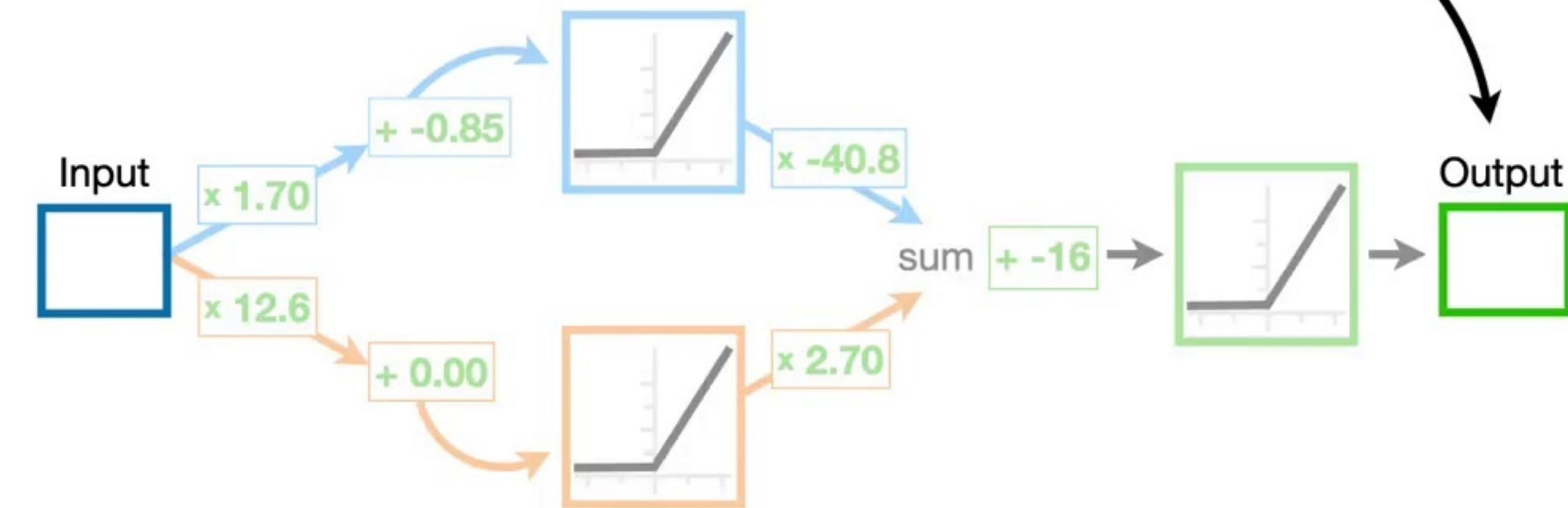
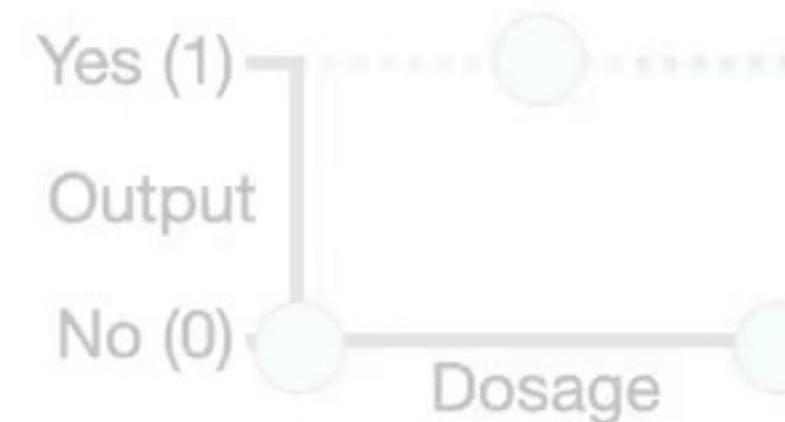


## The Neural Networks just have one Input Node...



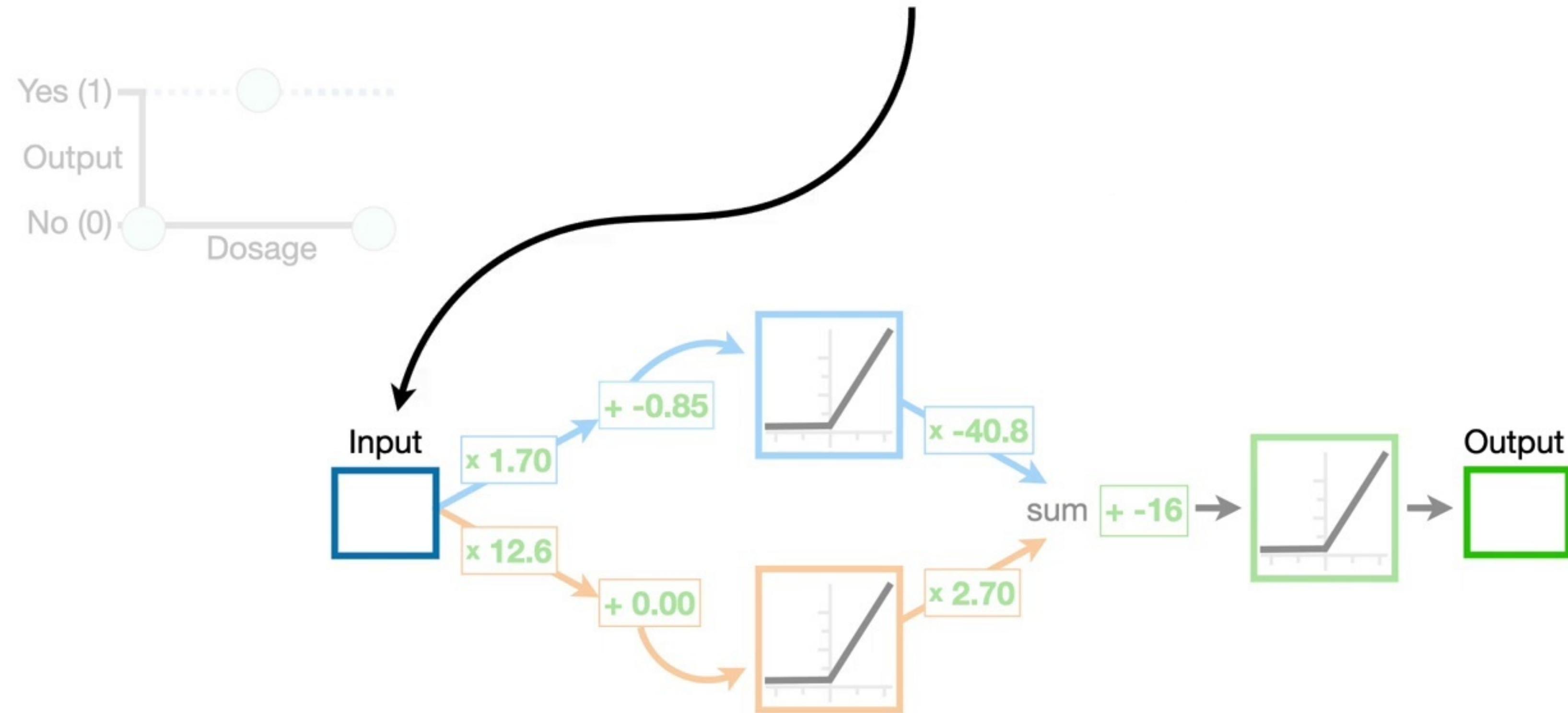


...and one **Output Node**.



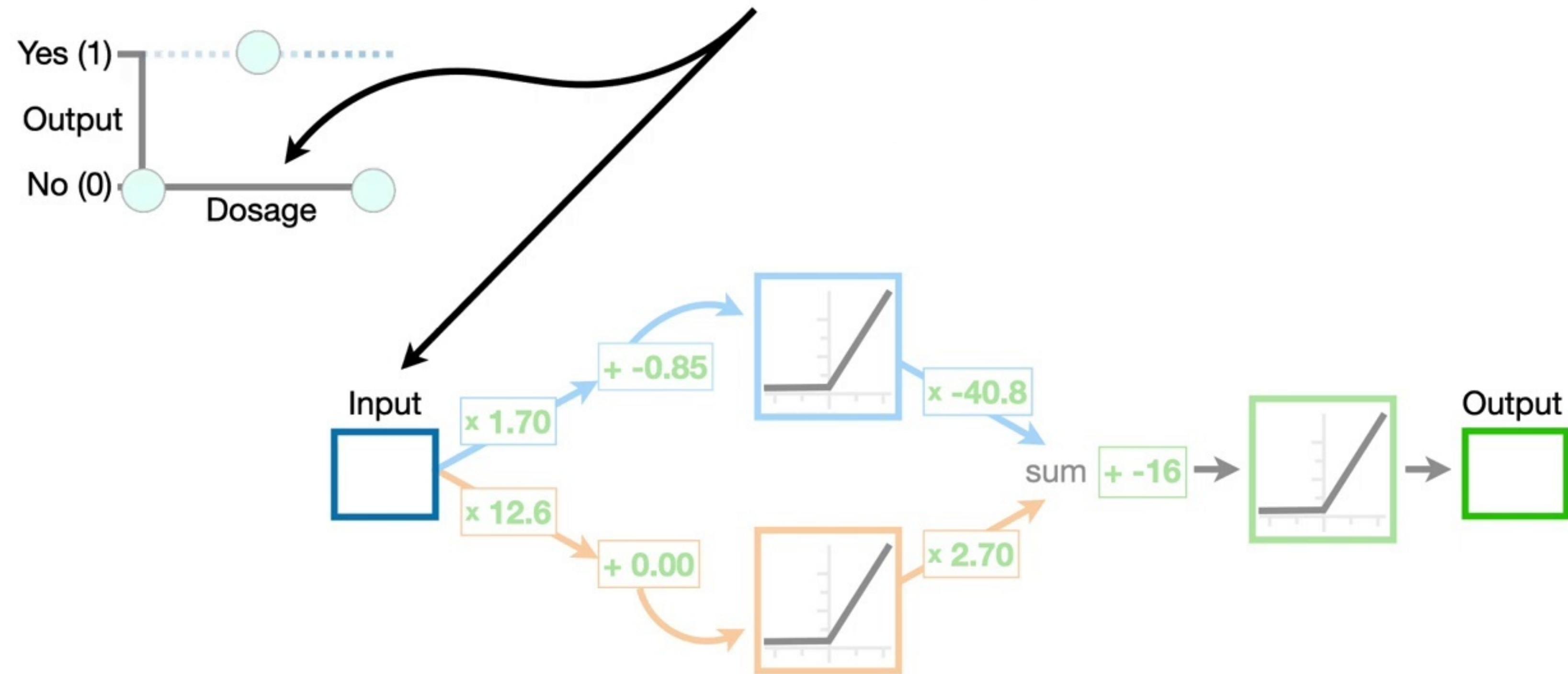


When there is only one input node...



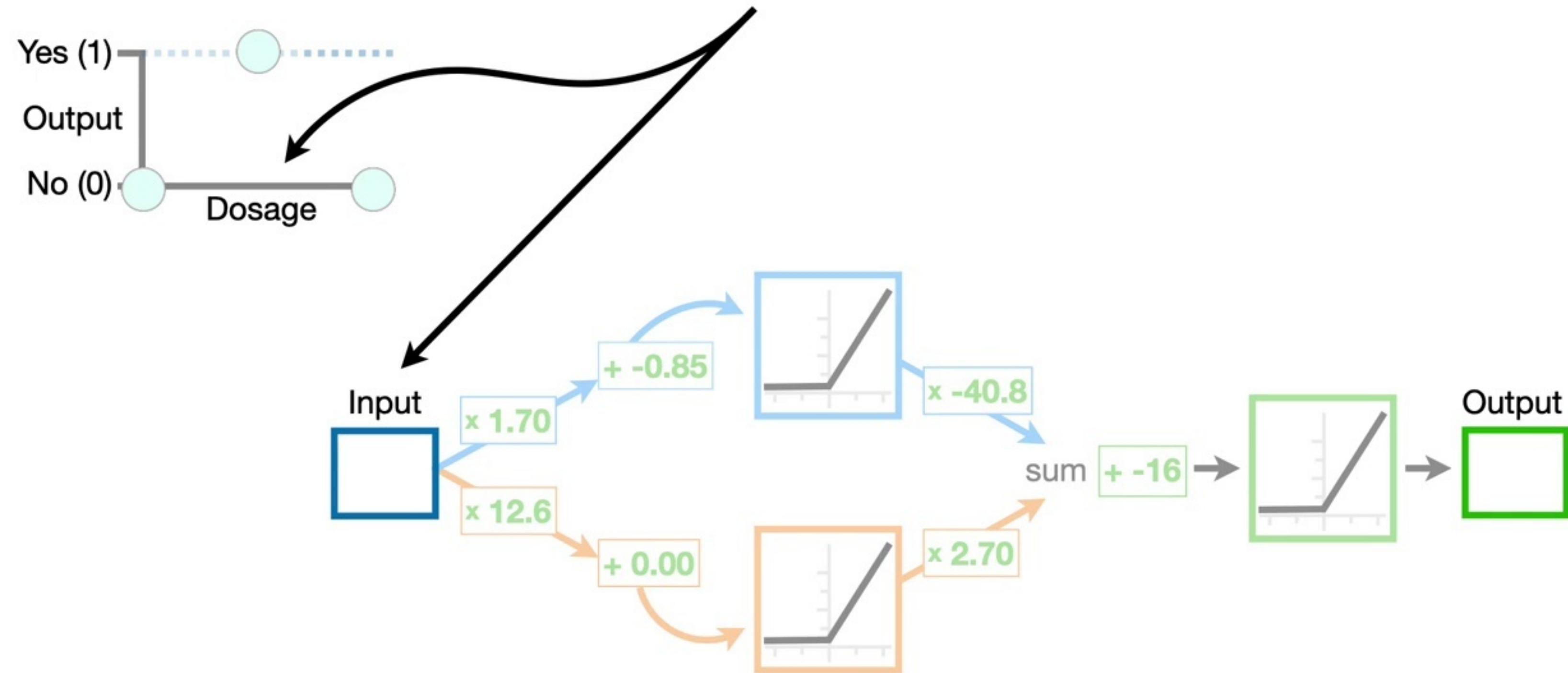


...then the data we are using to make predictions, in this case, **Dosages**, can all fit on the x-axis of this graph.



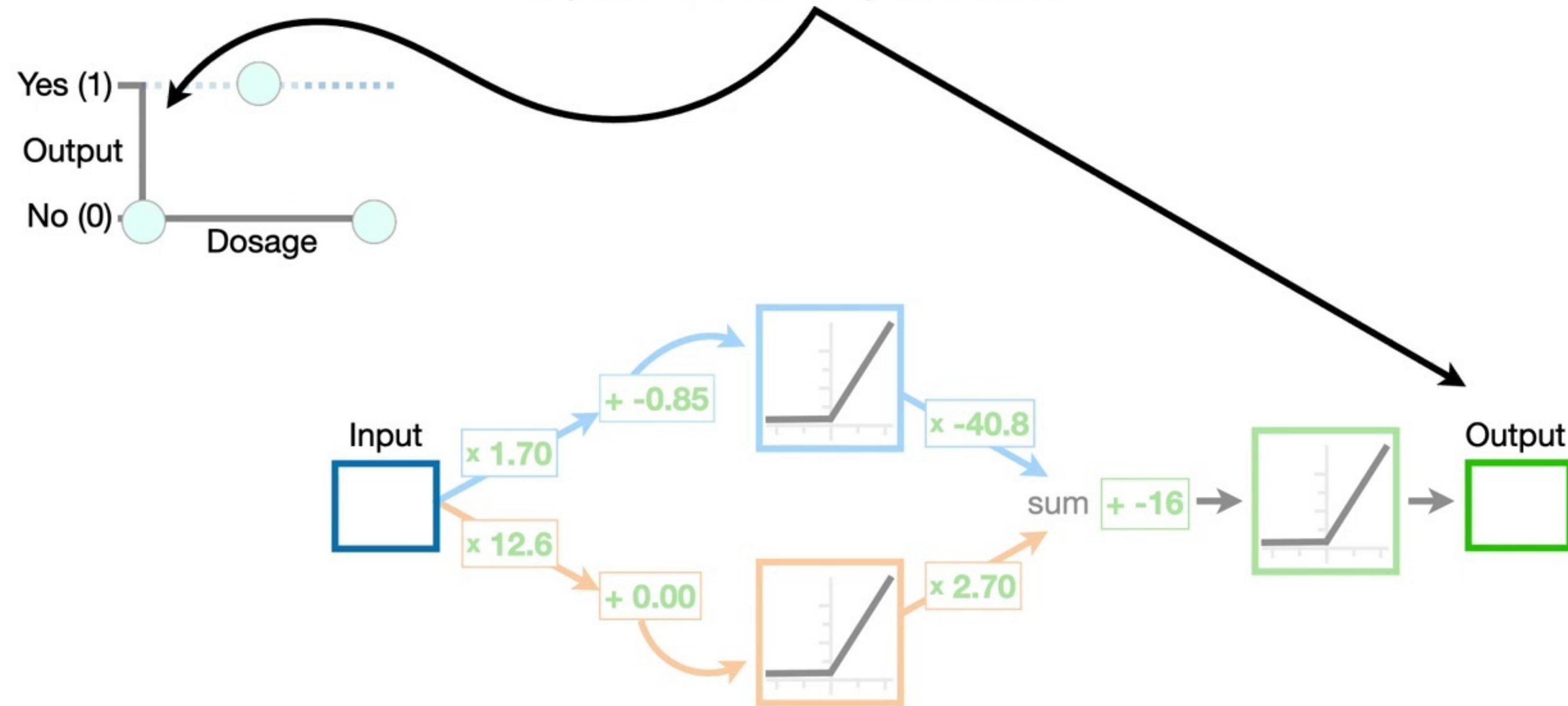


In other words, the input is **1-Dimensional**, since it only needs one axis in the graph.



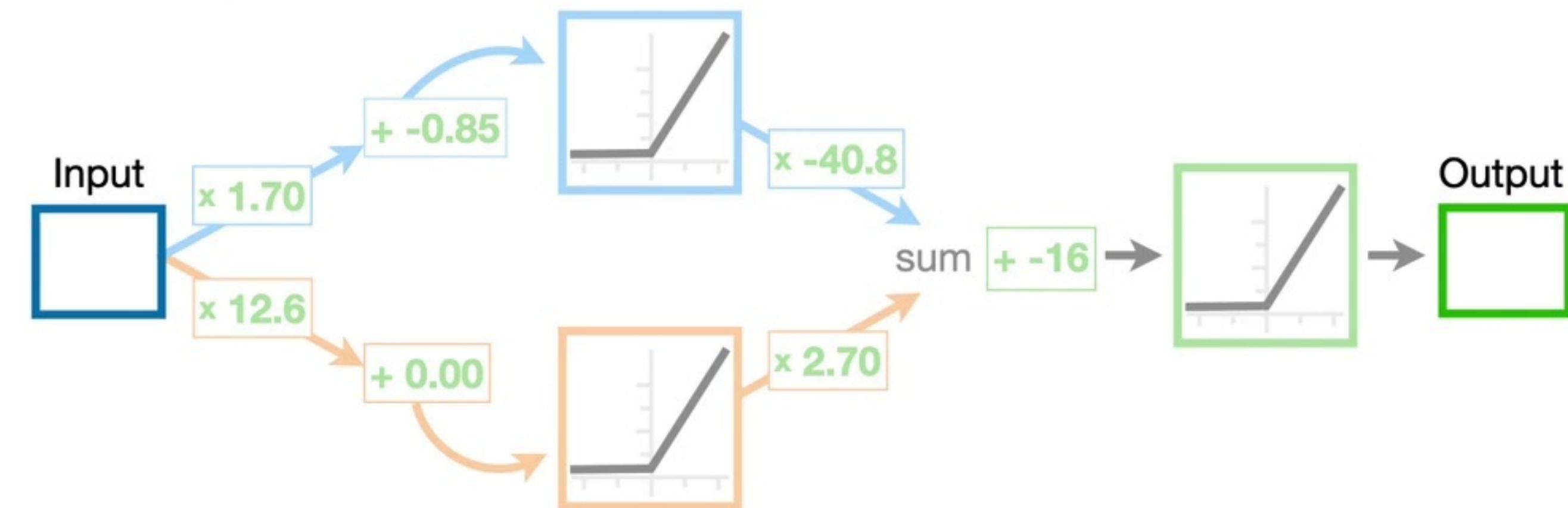
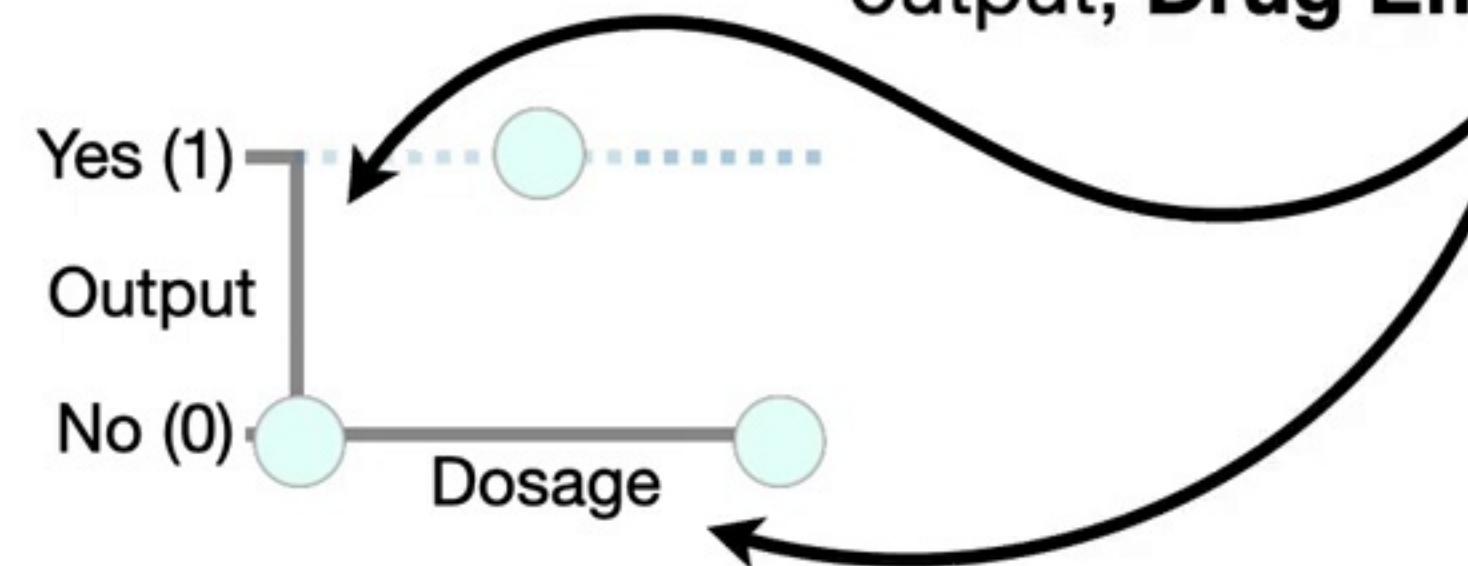


Likewise, a single dimension, the y-axis, represents the output values.



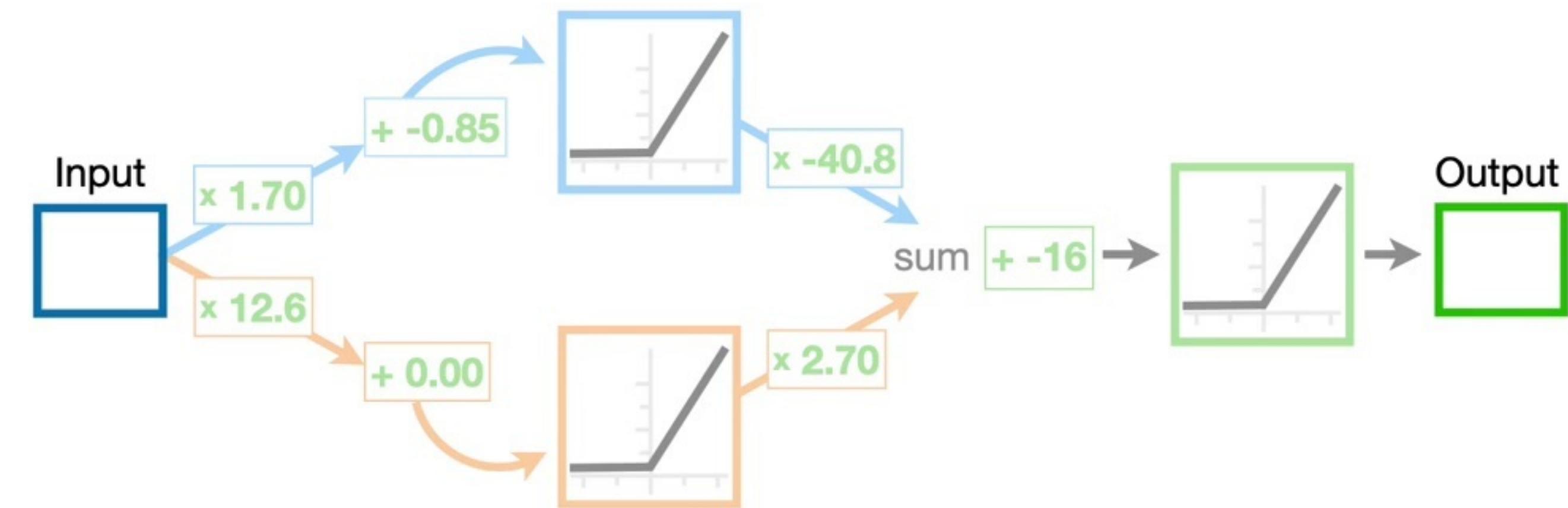
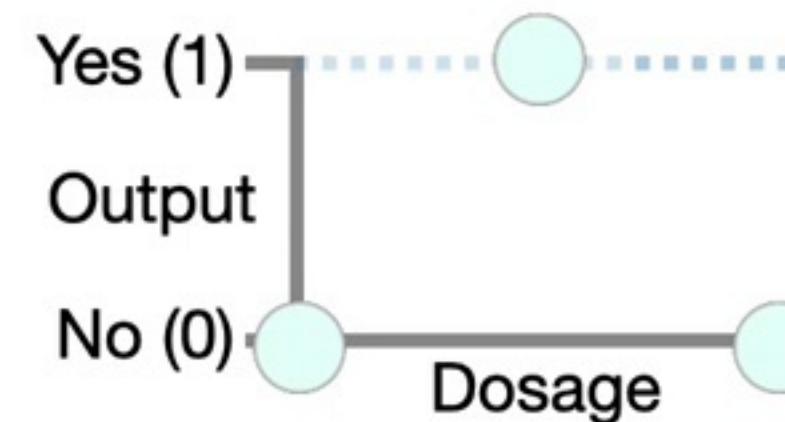


Combined, we get a **2-Dimensional** graph, with the input, **Dosage**, on the x-axis and the output, **Drug Effectiveness**, on the y-axis.



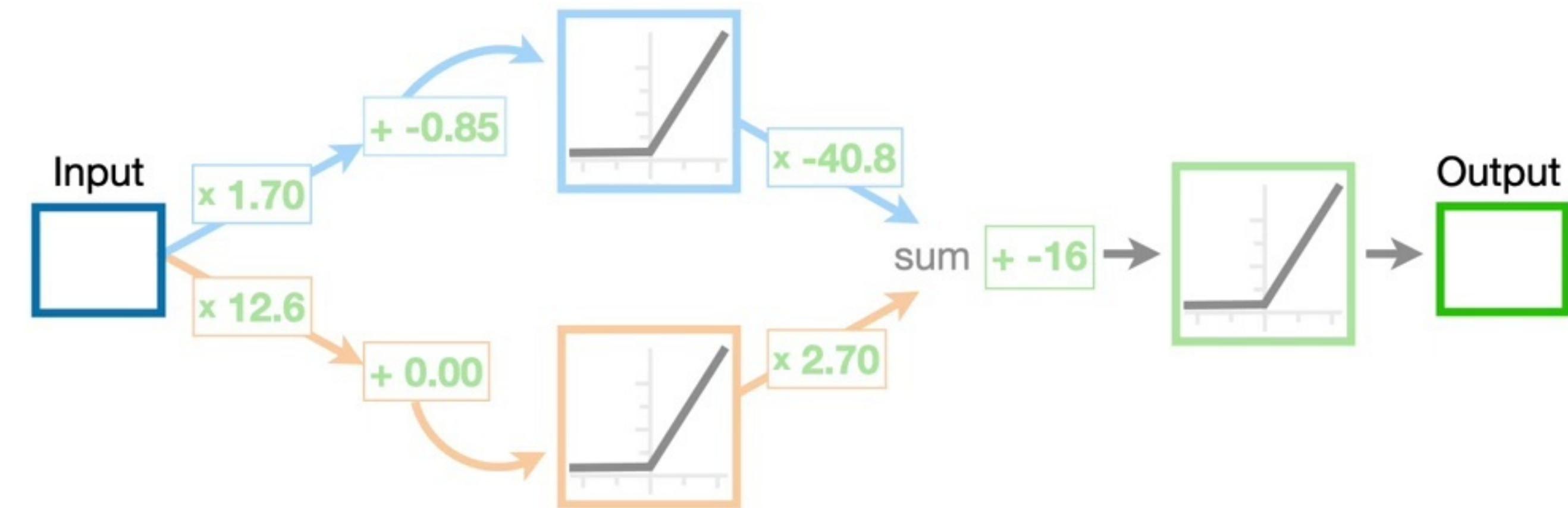
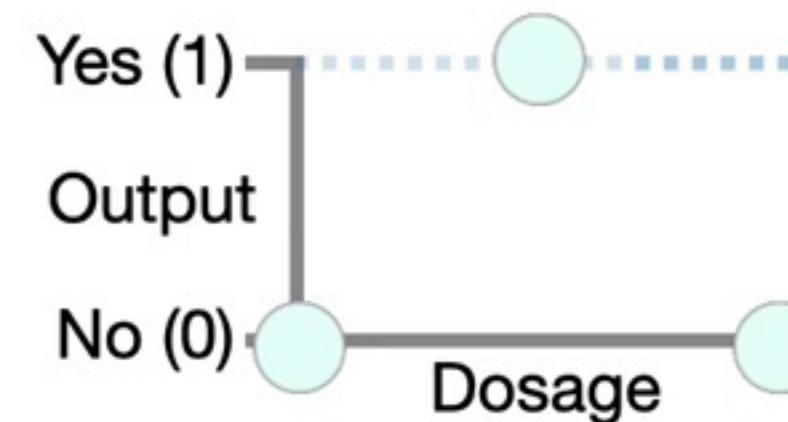


Because the input and the output combine  
to form a **2-Dimensional** graph...



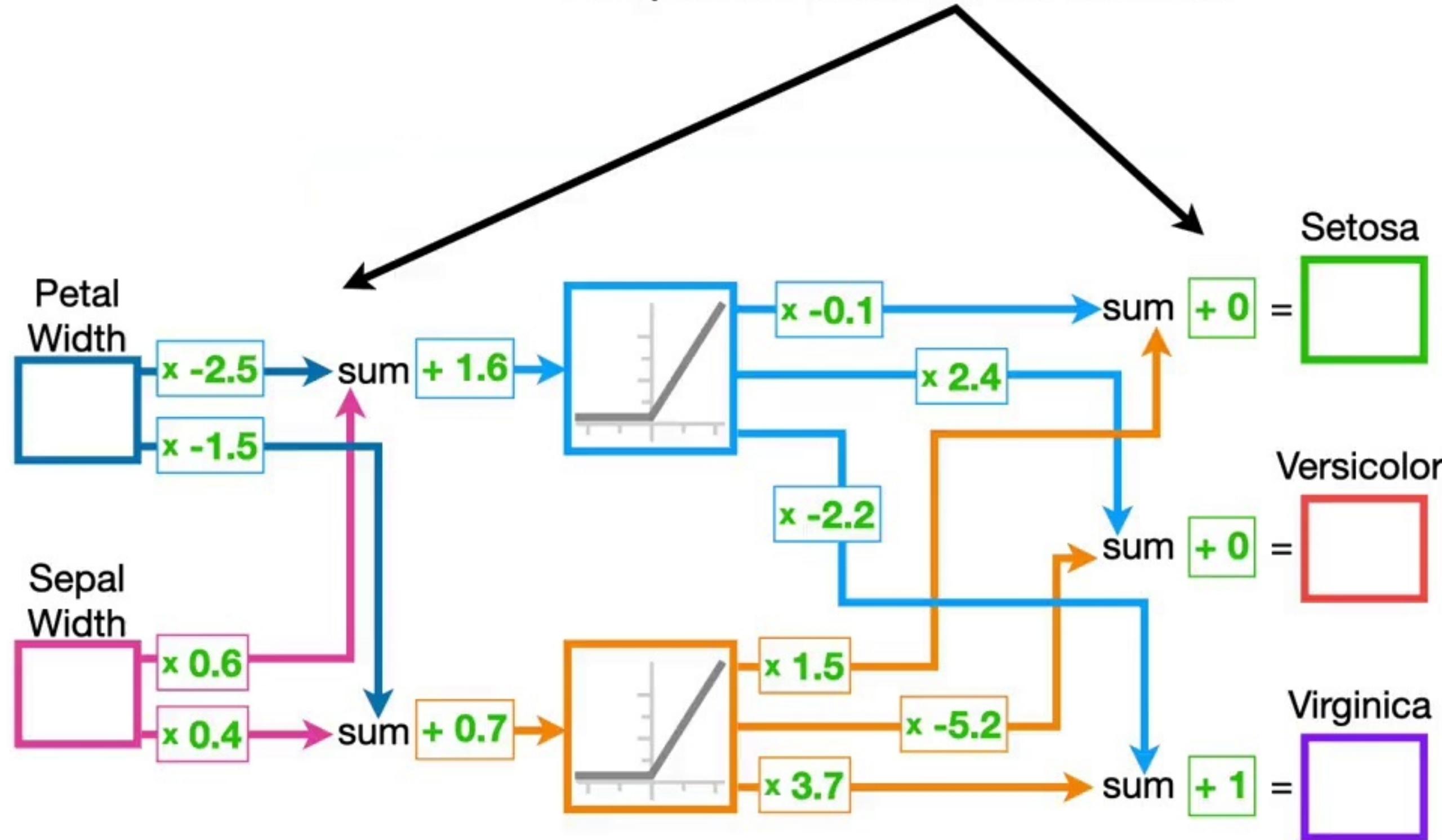


...we can see how the **Weights** and **Biases** in this **Neural Network** slice, flip and stretch the curved or bent **Activation Functions** into new shapes...



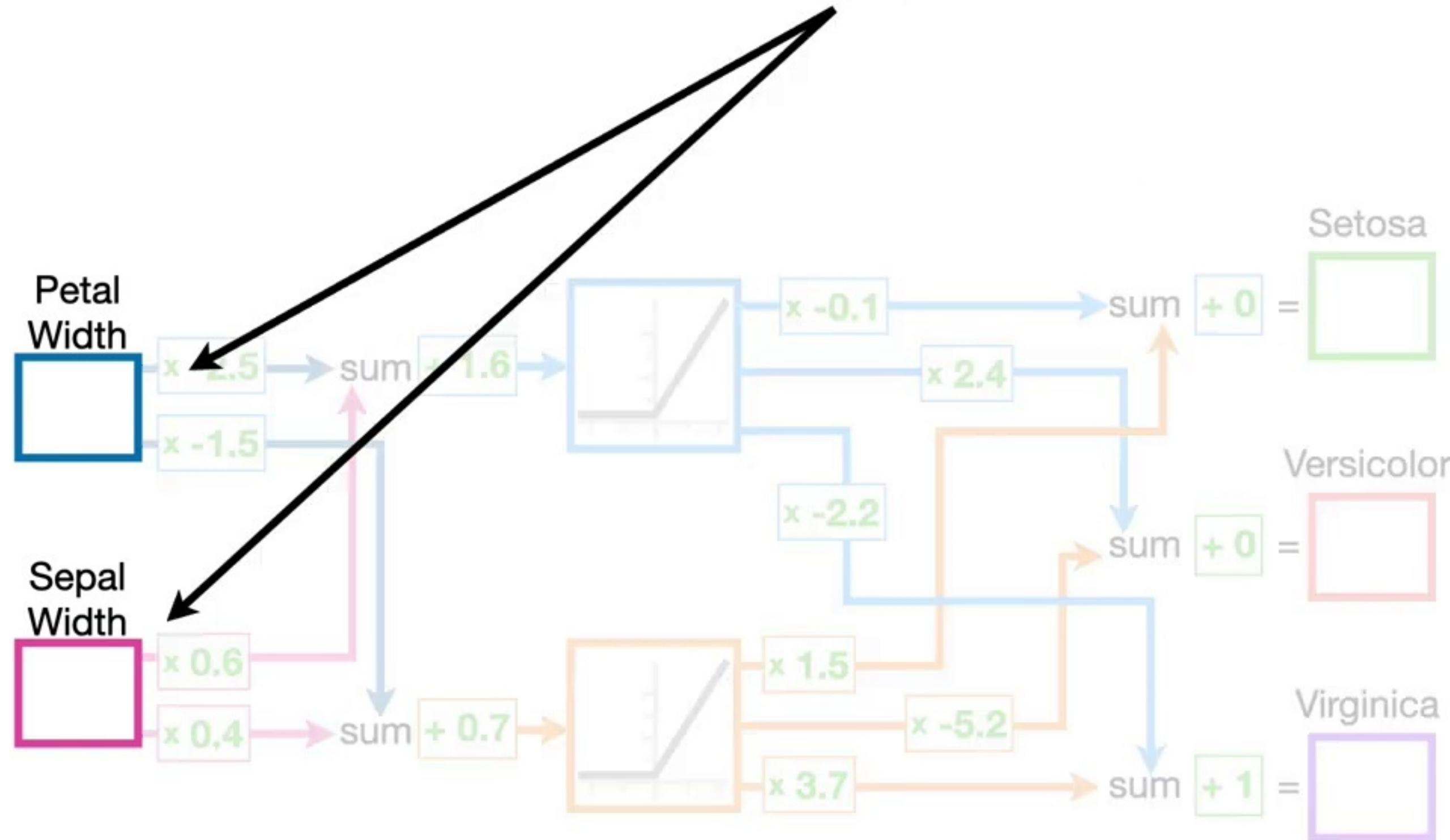


Now let's look at a more complicated **Neural Network**...



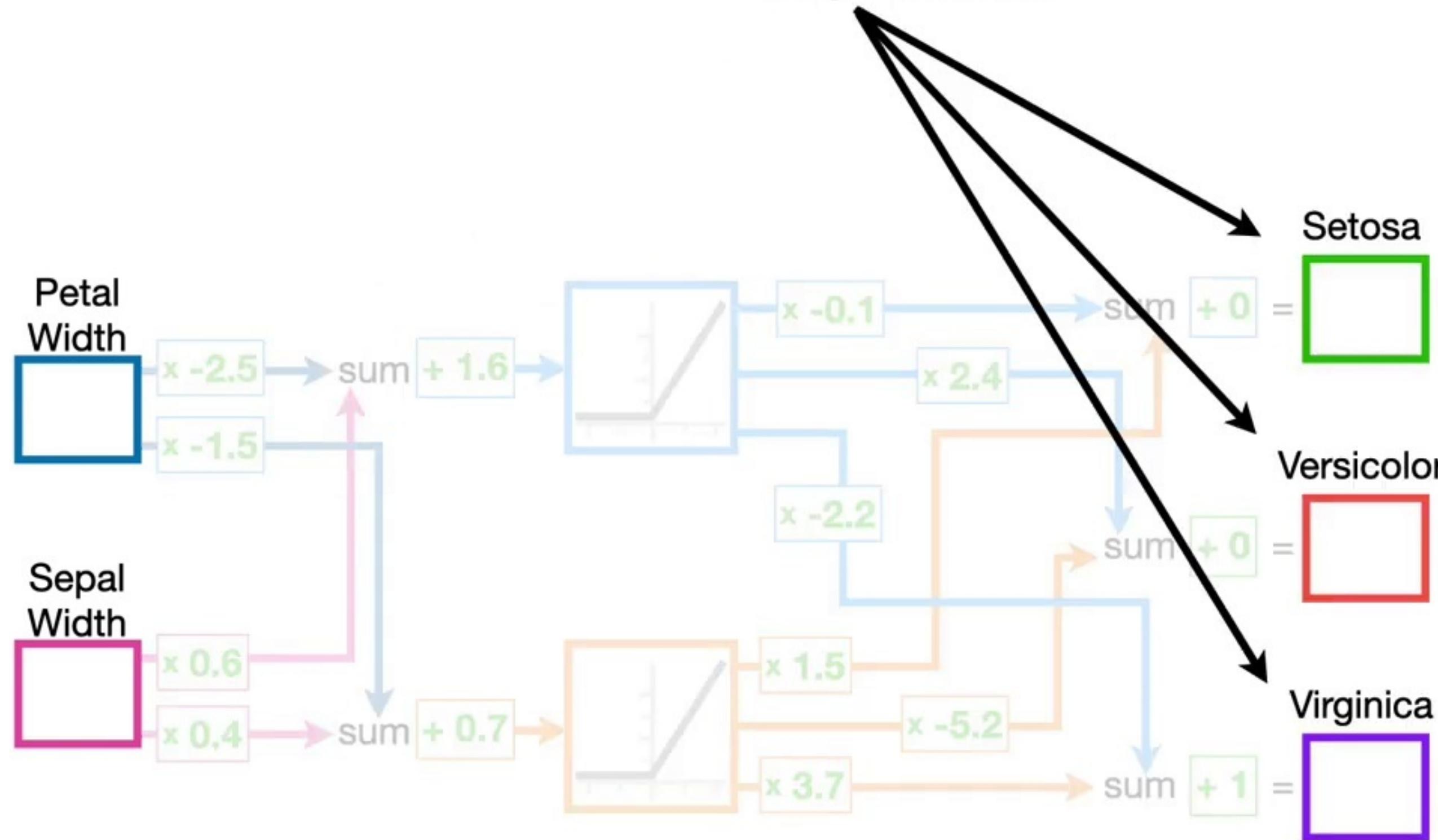


...that has more than  
one **Input Node**...



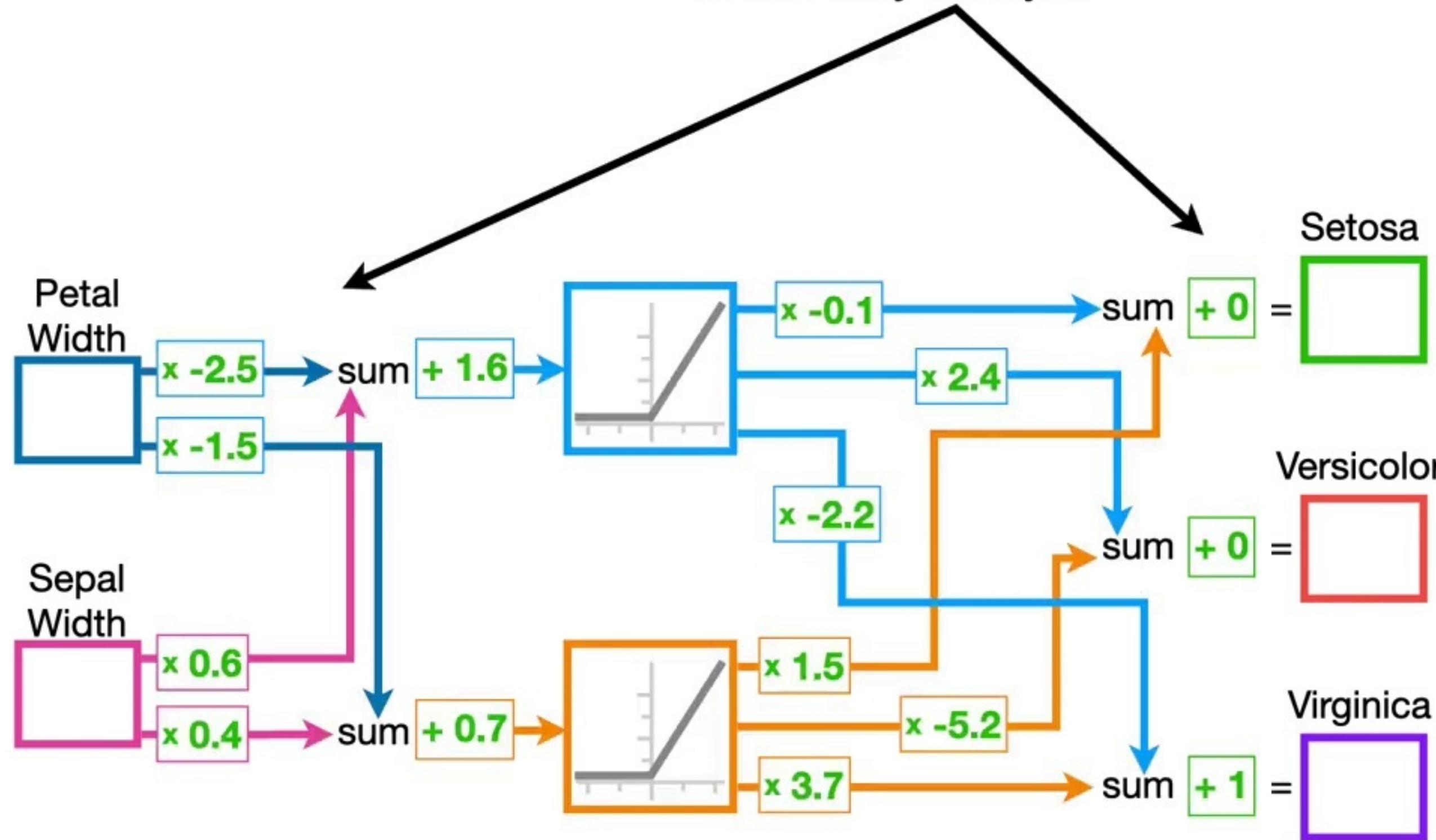


...and more than one  
**Output Node.**



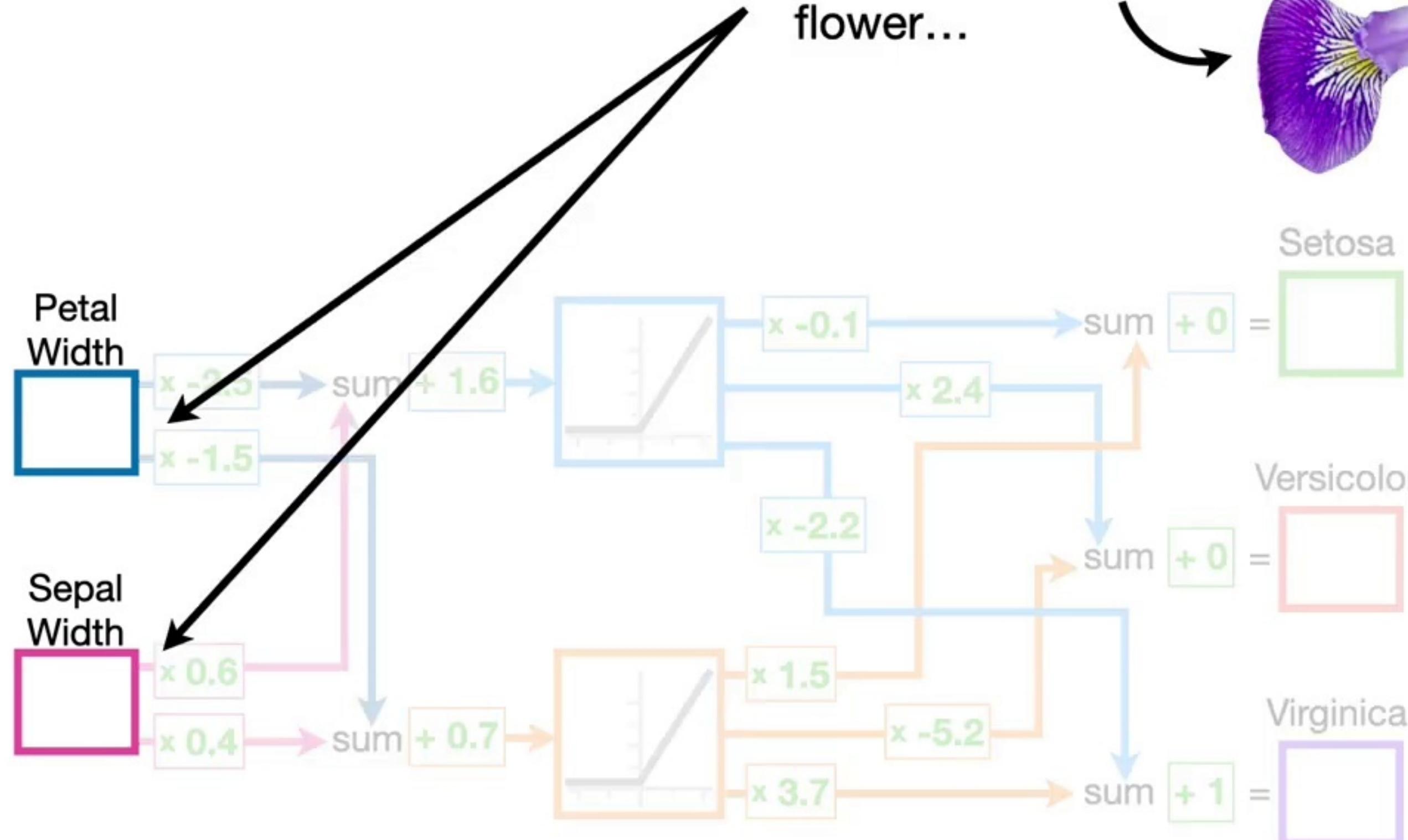
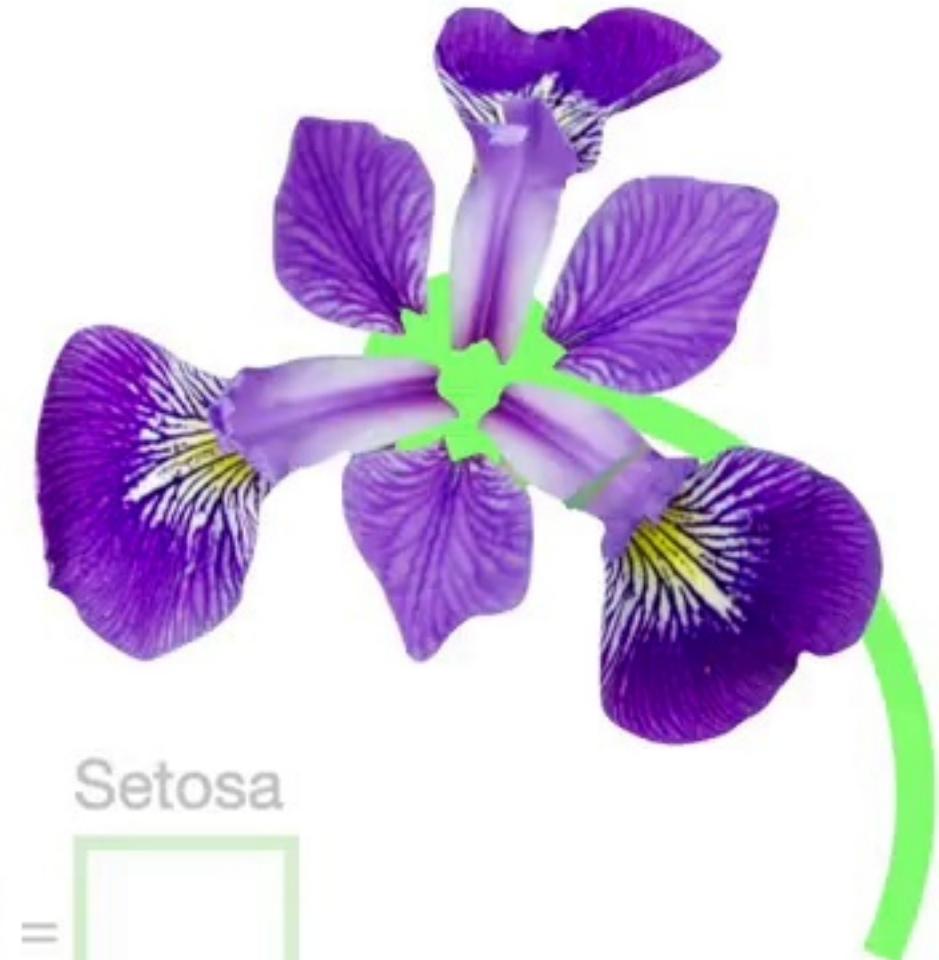


Now, this **Neural Network** may  
look really fancy...



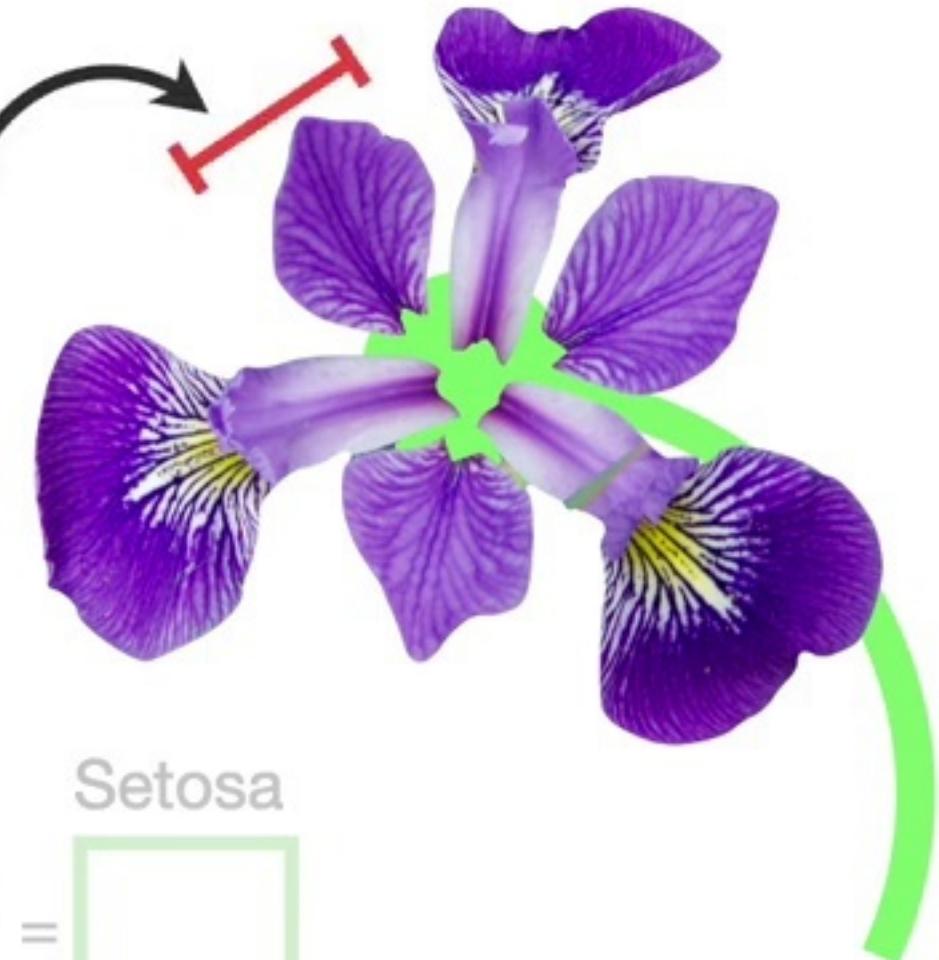


...but all it does it take two measurements from an Iris flower...





...the width of a **Petal**, which  
is this part of the flower...



Petal  
Width

$$\times -2.5$$

sum

$$+ 1.6$$



$$\times -0.1$$

$$\times 2.4$$

$$\times 0$$

$$+ 0$$

Setosa

Sepal  
Width

$$\times 0.6$$

sum

$$+ 0.7$$



$$\times -2.2$$

$$\times 1.5$$

$$\times 0$$

$$+ 0$$

Versicolor

$$\times 3.7$$

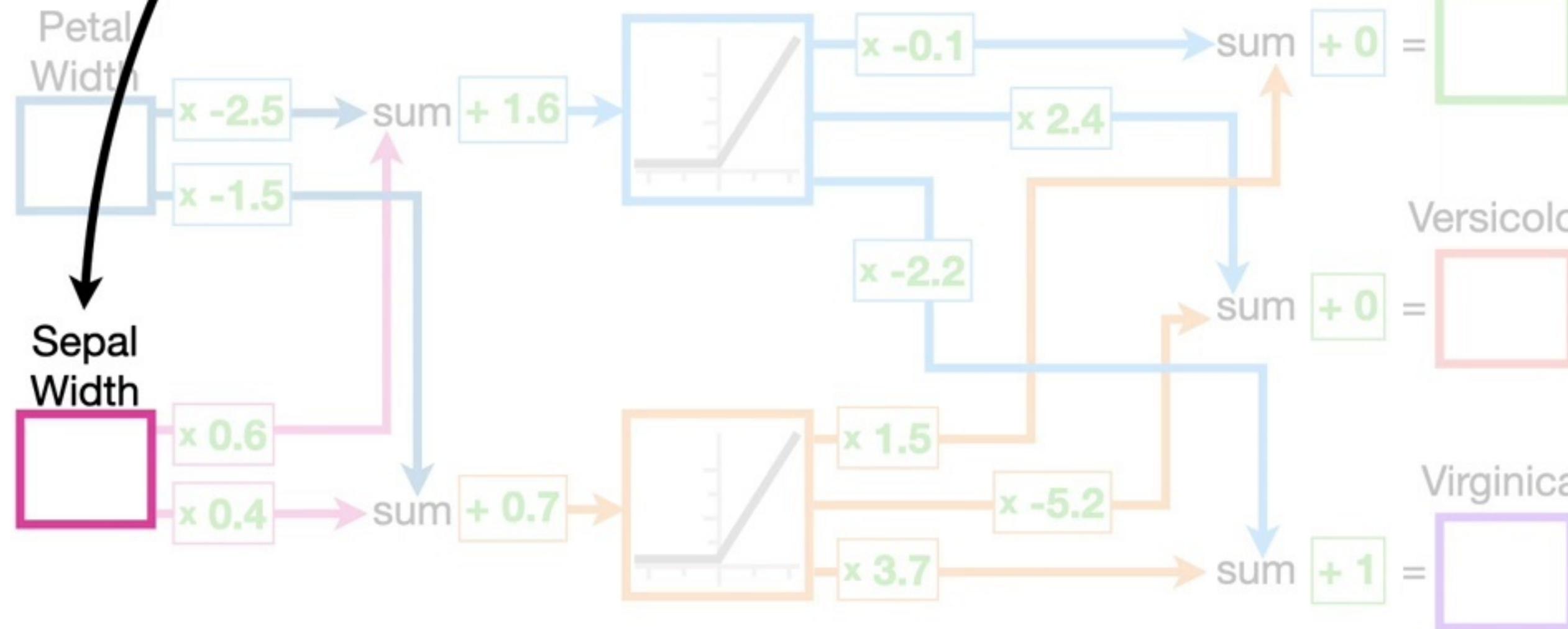
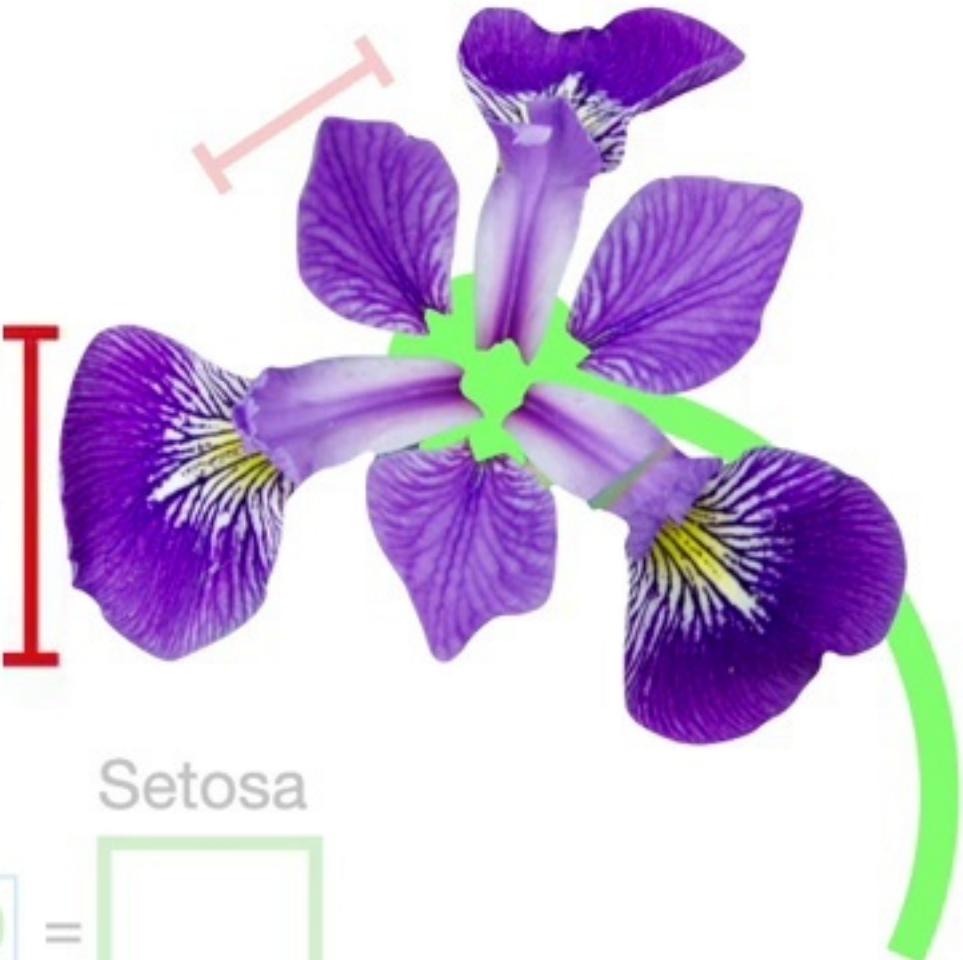
$$\times -5.2$$

$$\times 1$$

Virginica

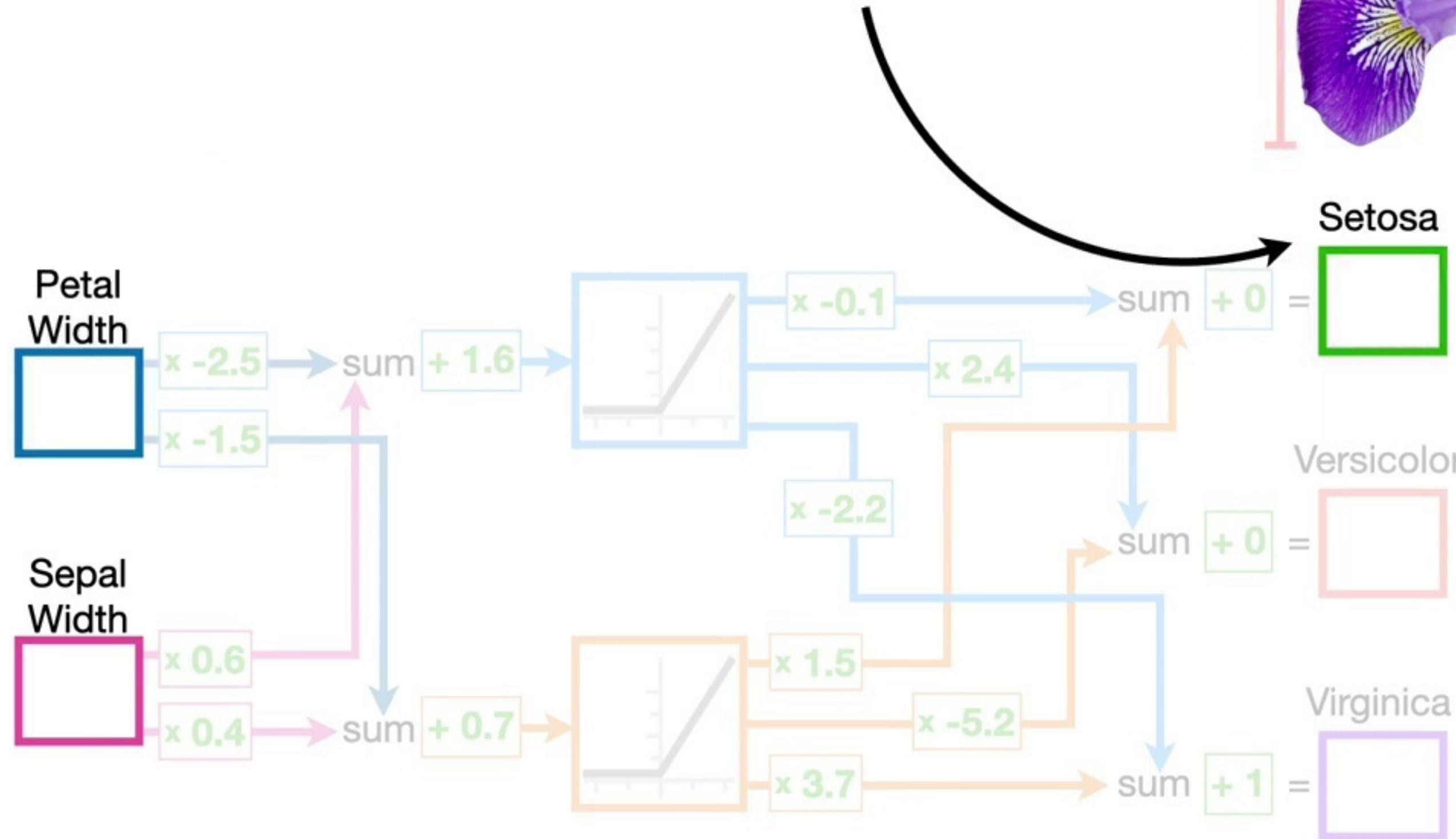
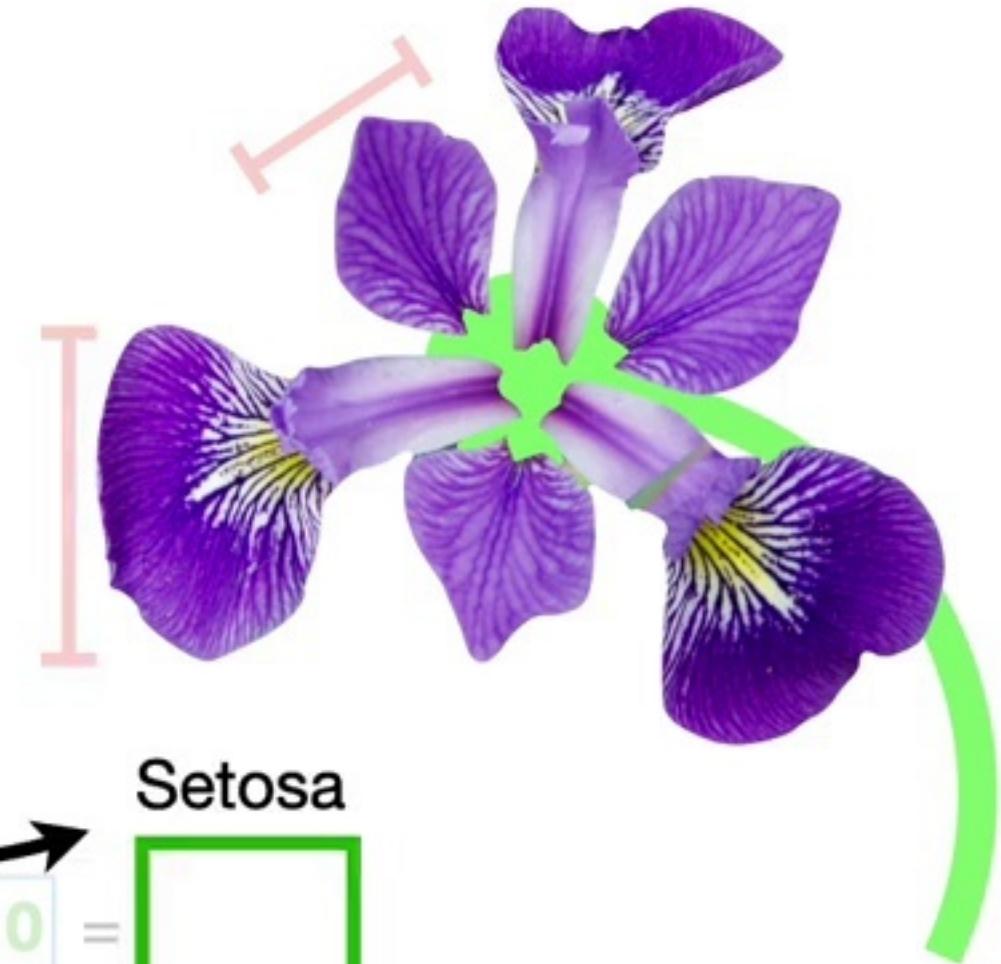


...and the width of a **Sepal**,  
which is this part of the flower...



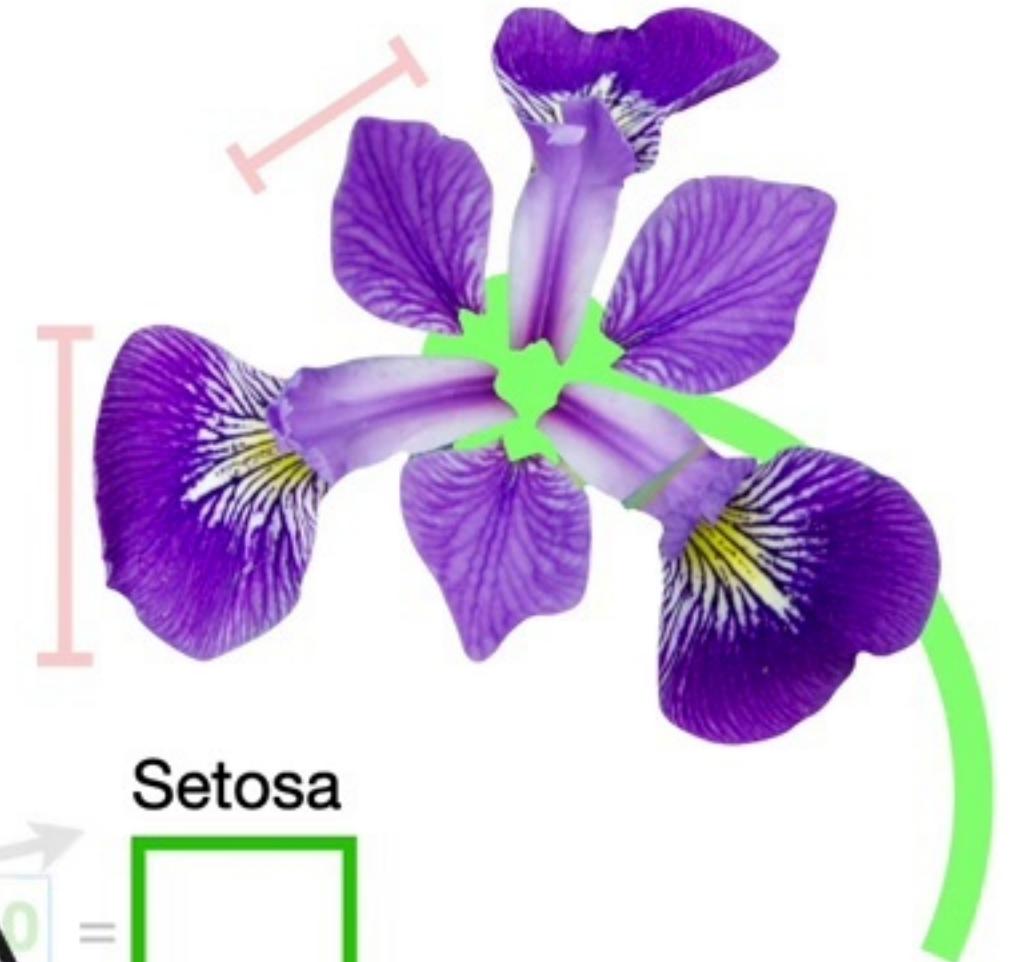
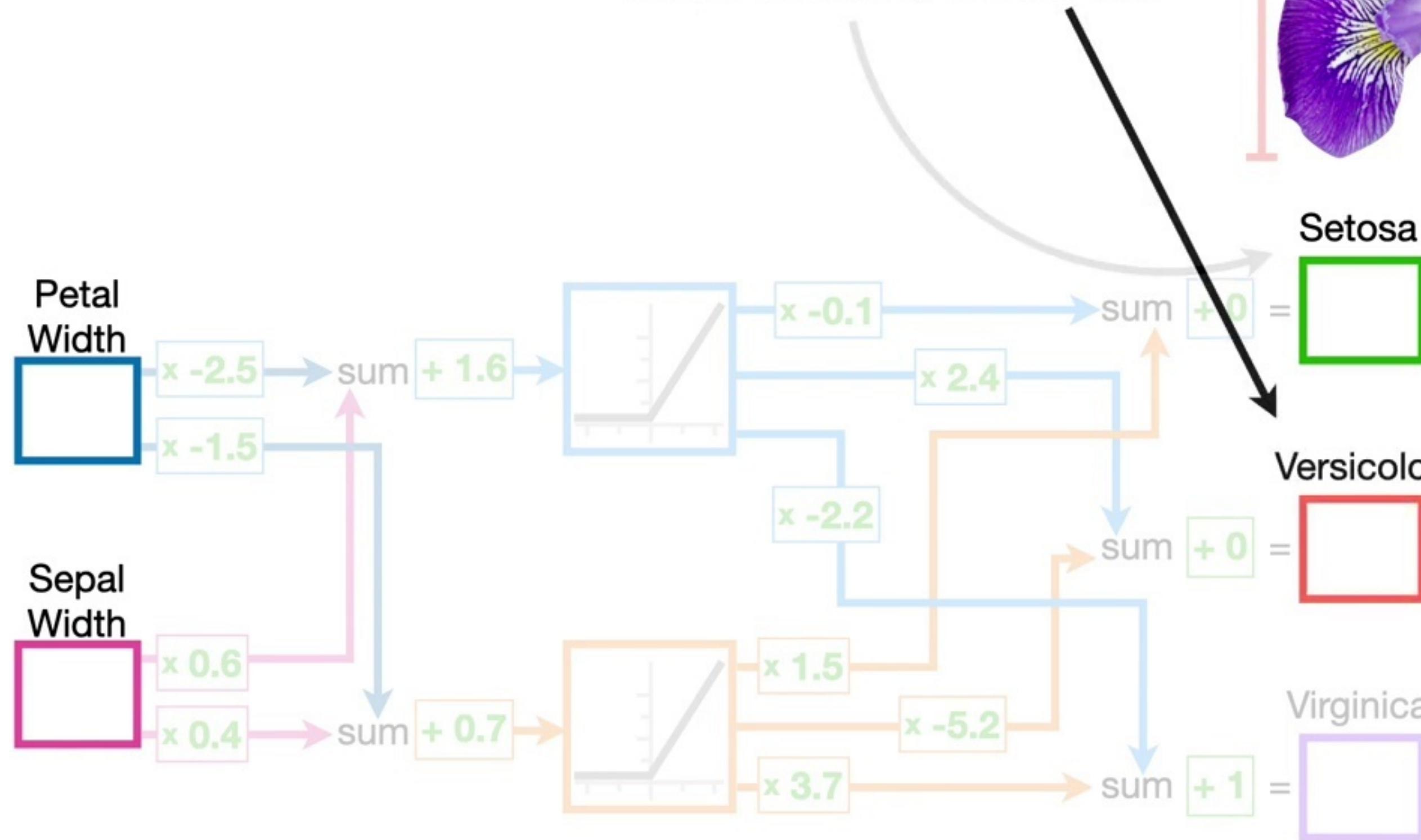


...and with that information,  
it predicts the species,  
either **Setosa**,



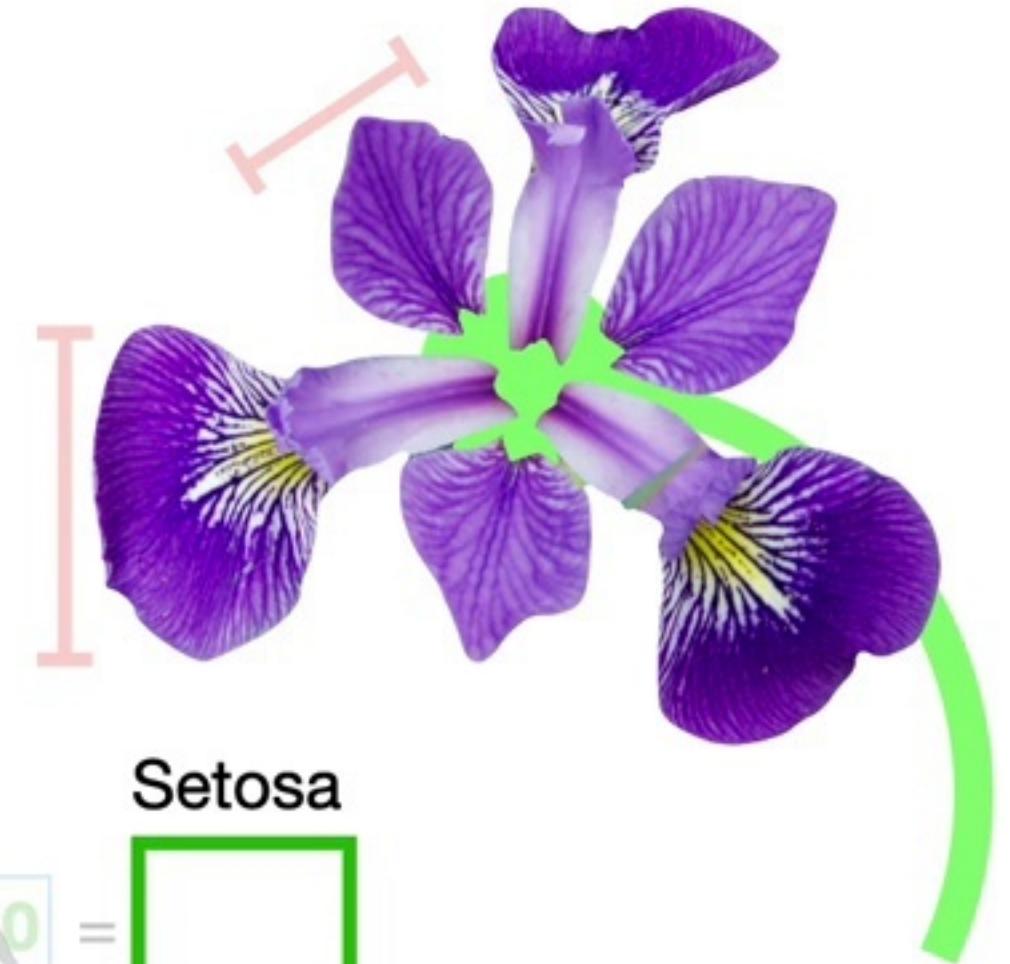
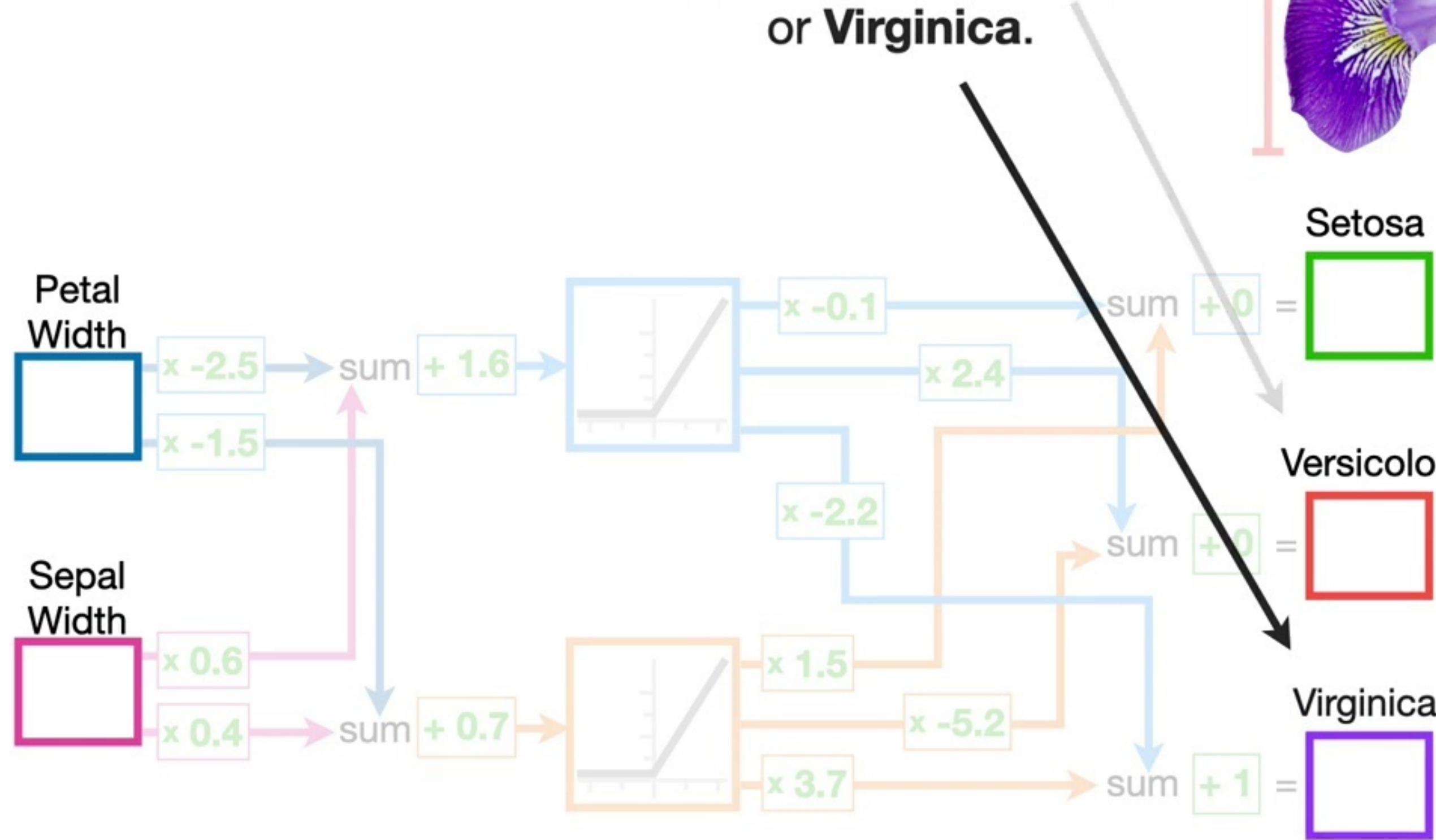


...and with that information,  
it predicts the species,  
either **Setosa**, **Versicolor**



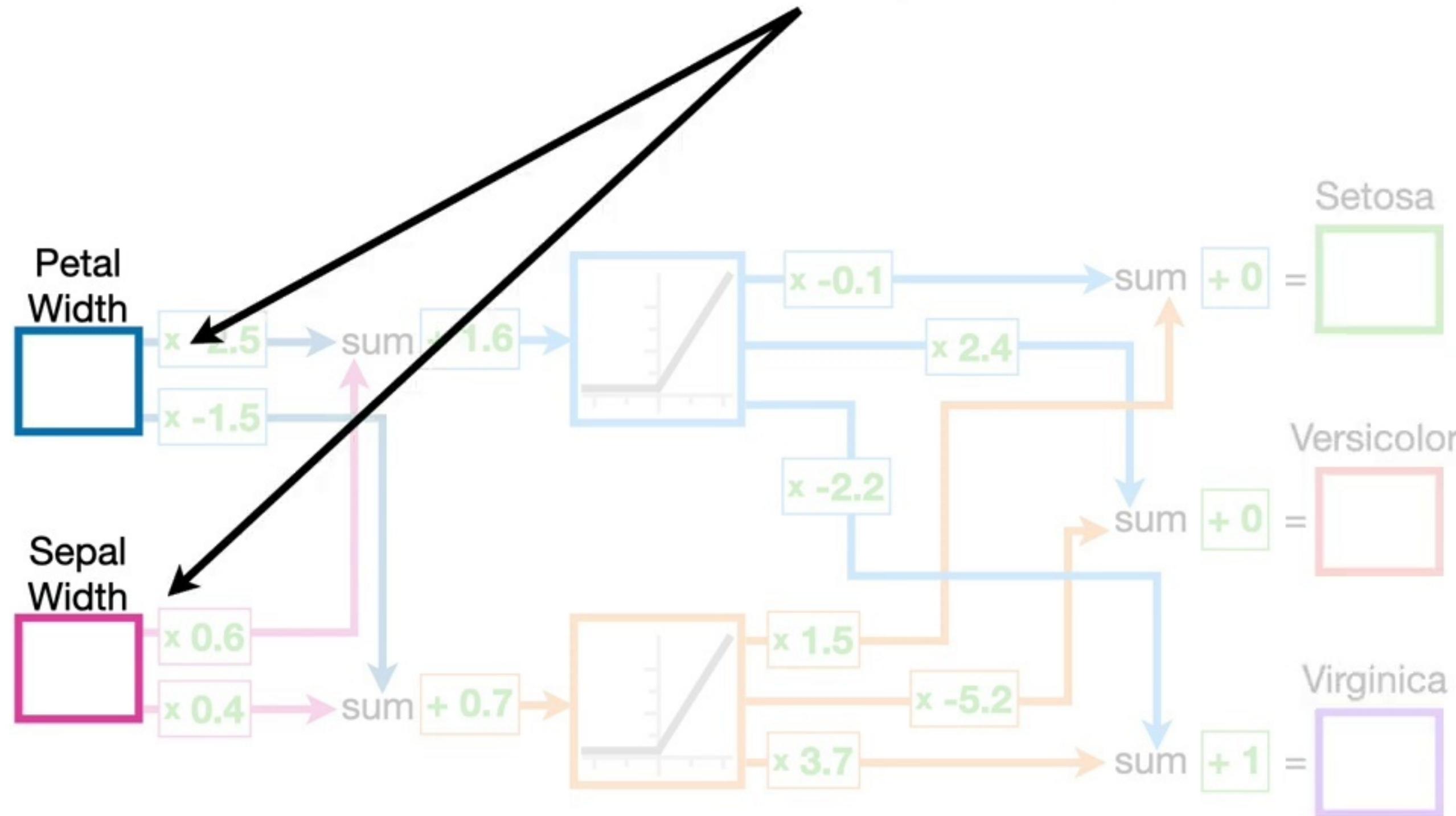


...and with that information,  
it predicts the species,  
either **Setosa**, **Versicolor**  
or **Virginica**.



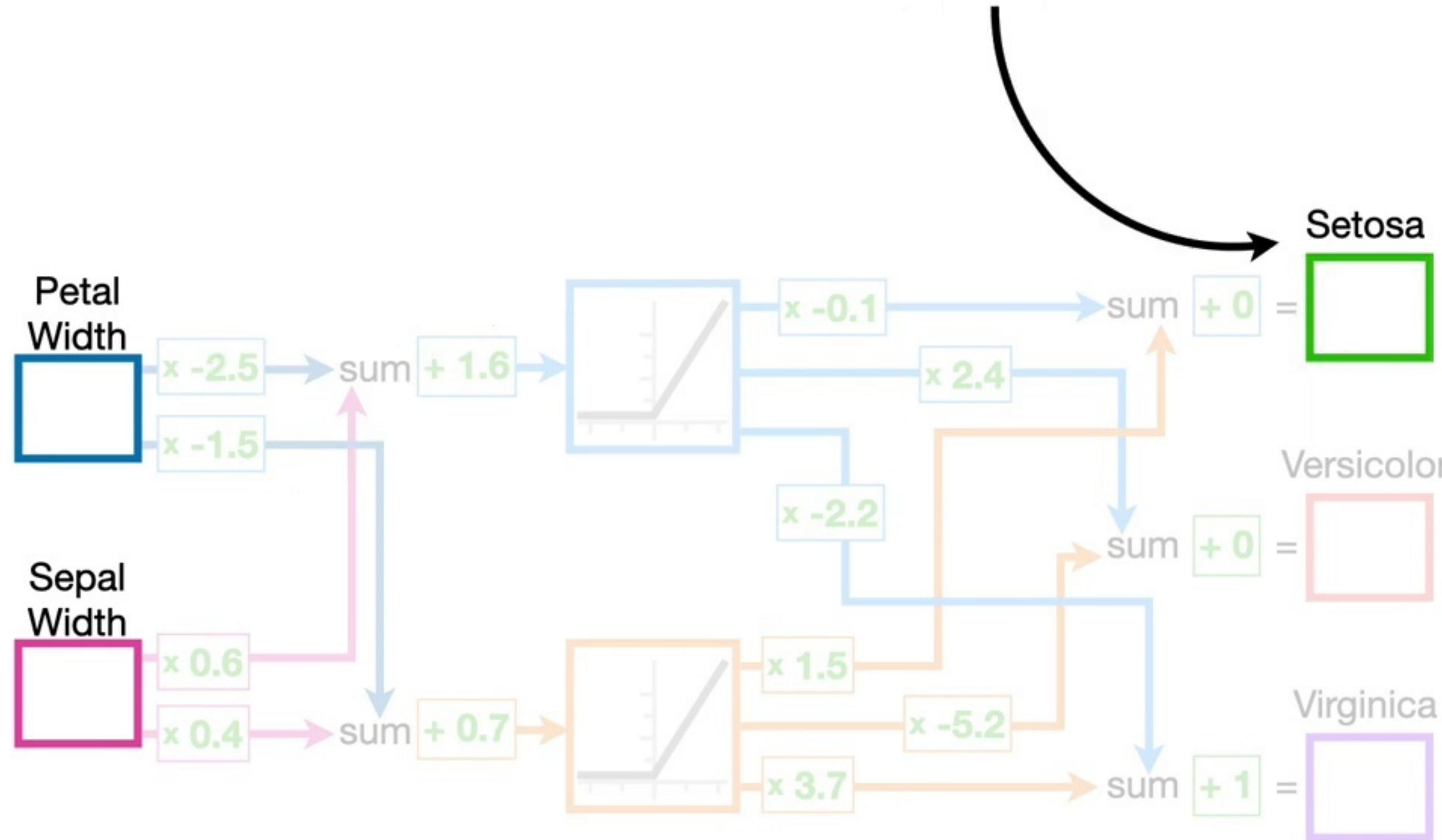


Anyway, to keep things simple at the start, let's begin with both input nodes...



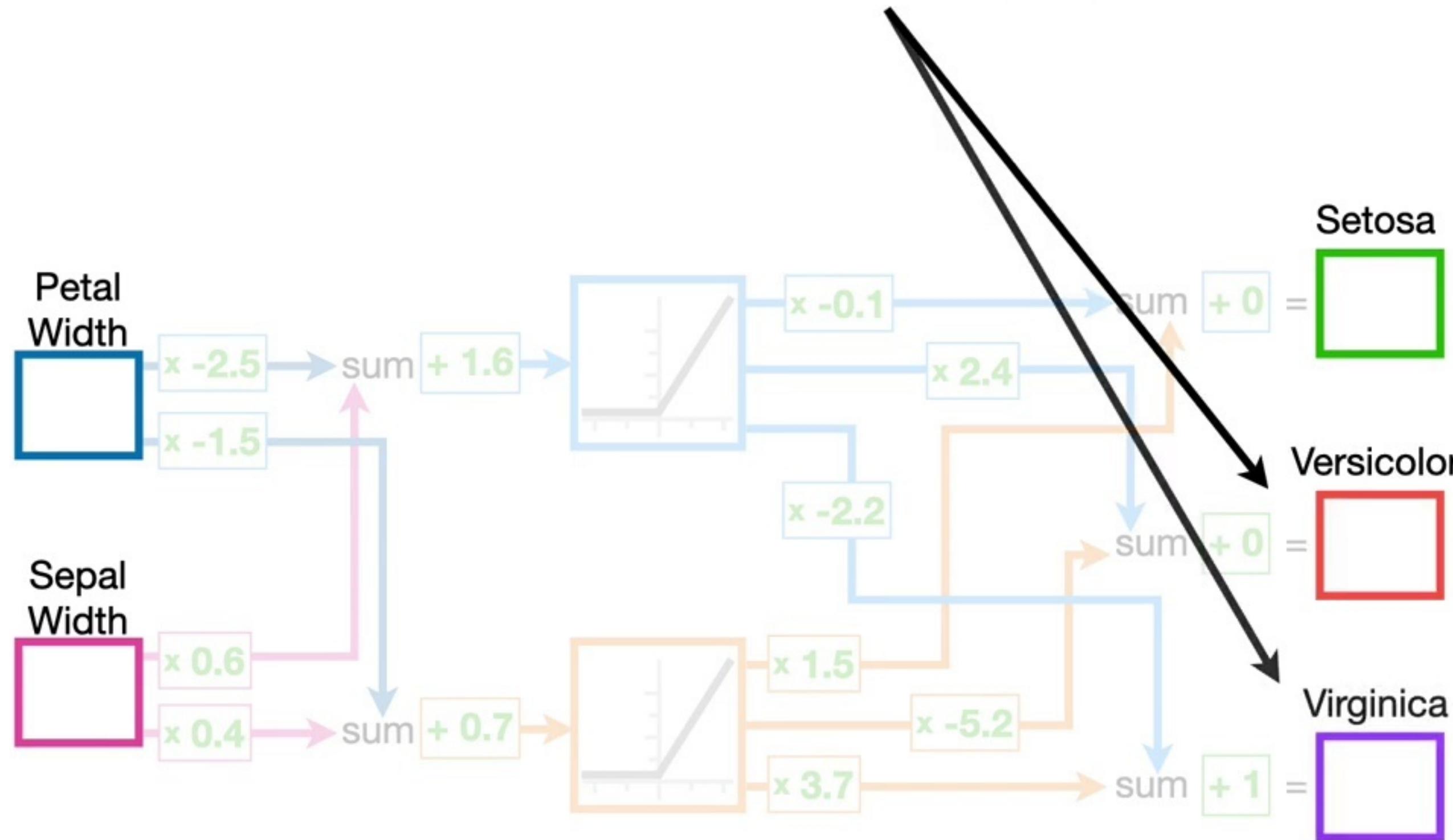


...but just one output node for **Setosa**.



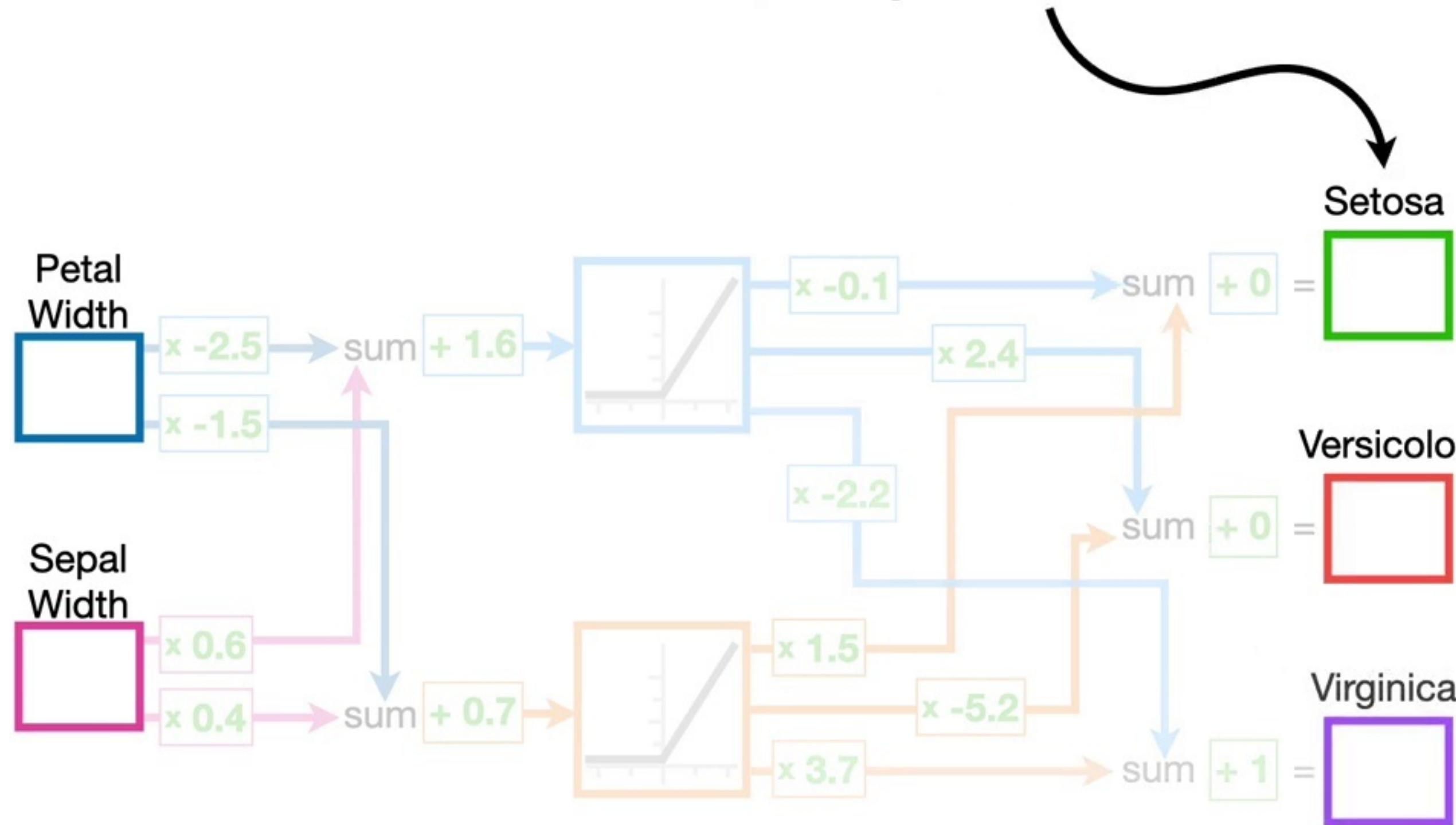


Later on we'll add the other  
two output nodes...



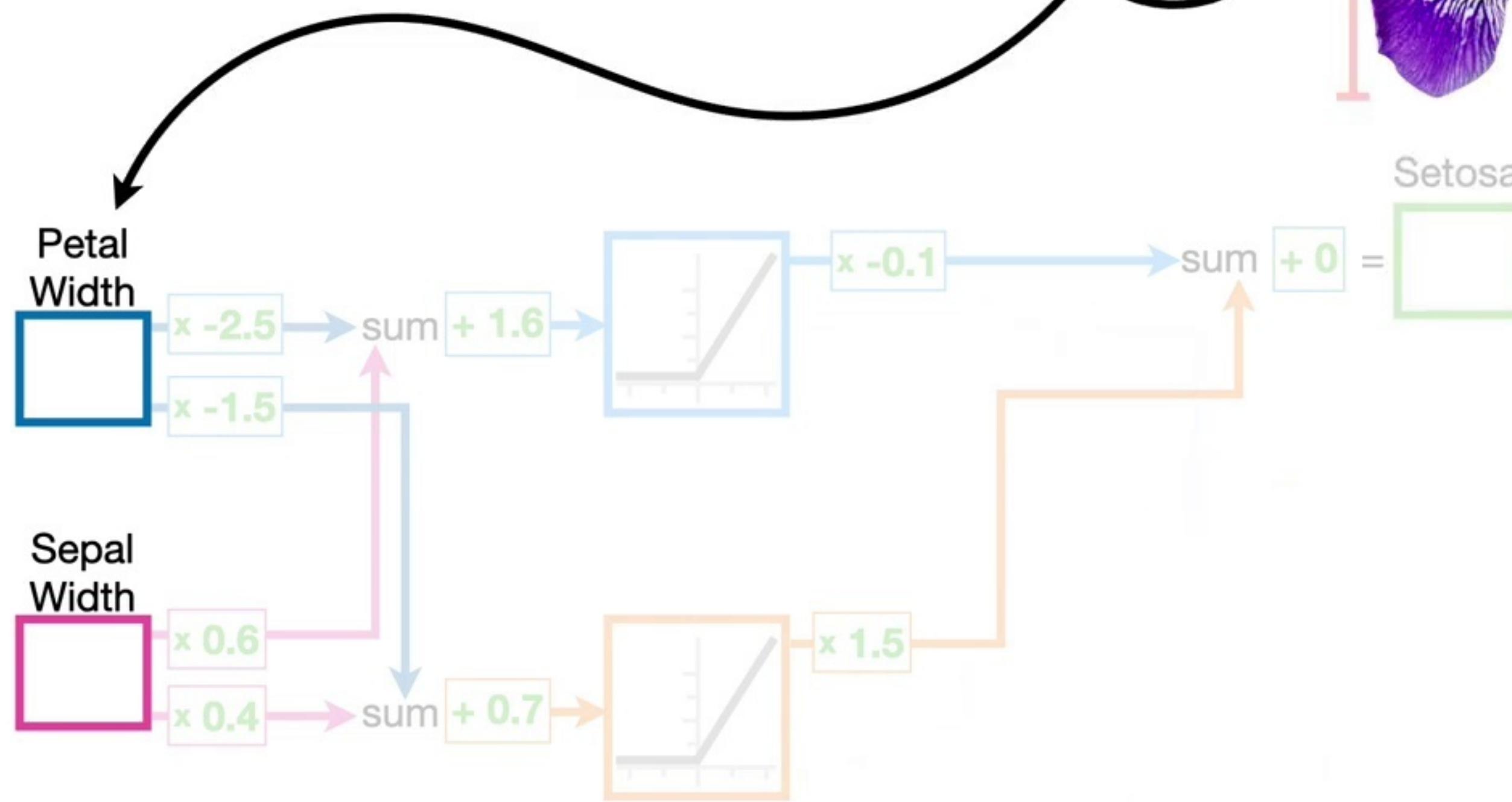


...but for now, let's keep things simple and just use one **Output Node**.



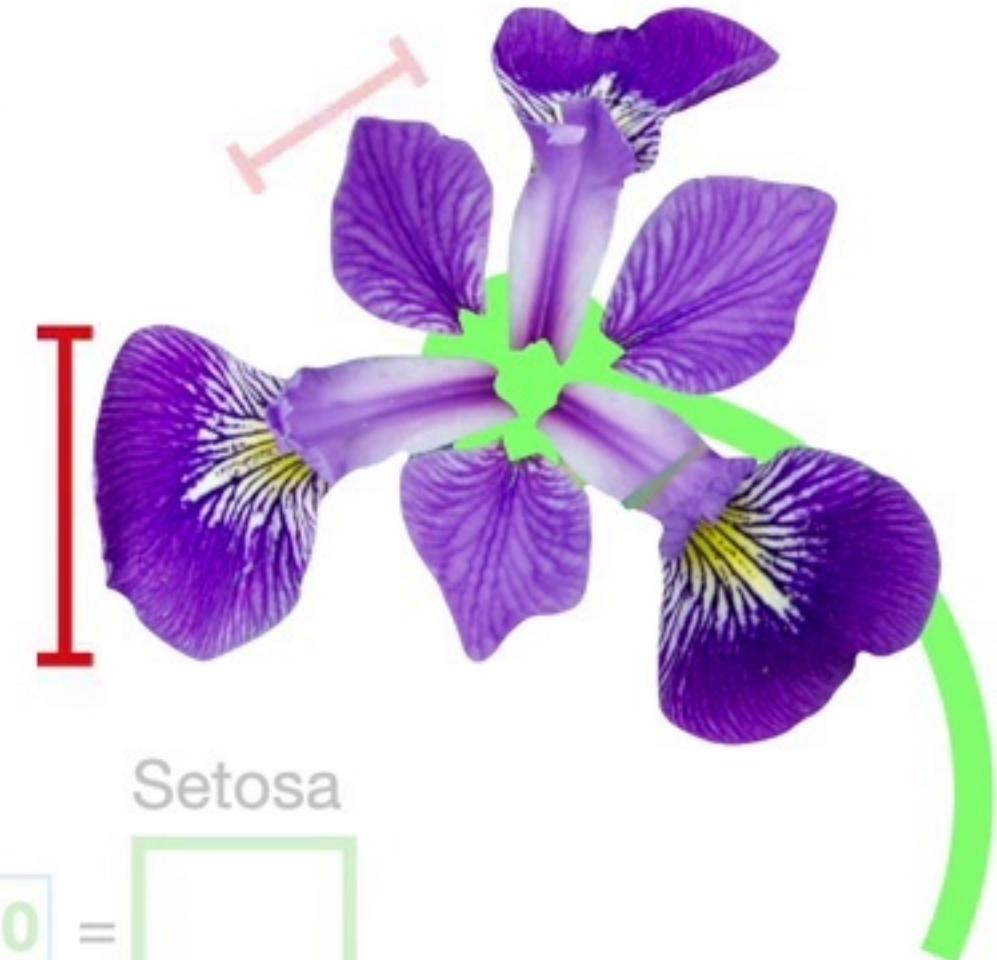
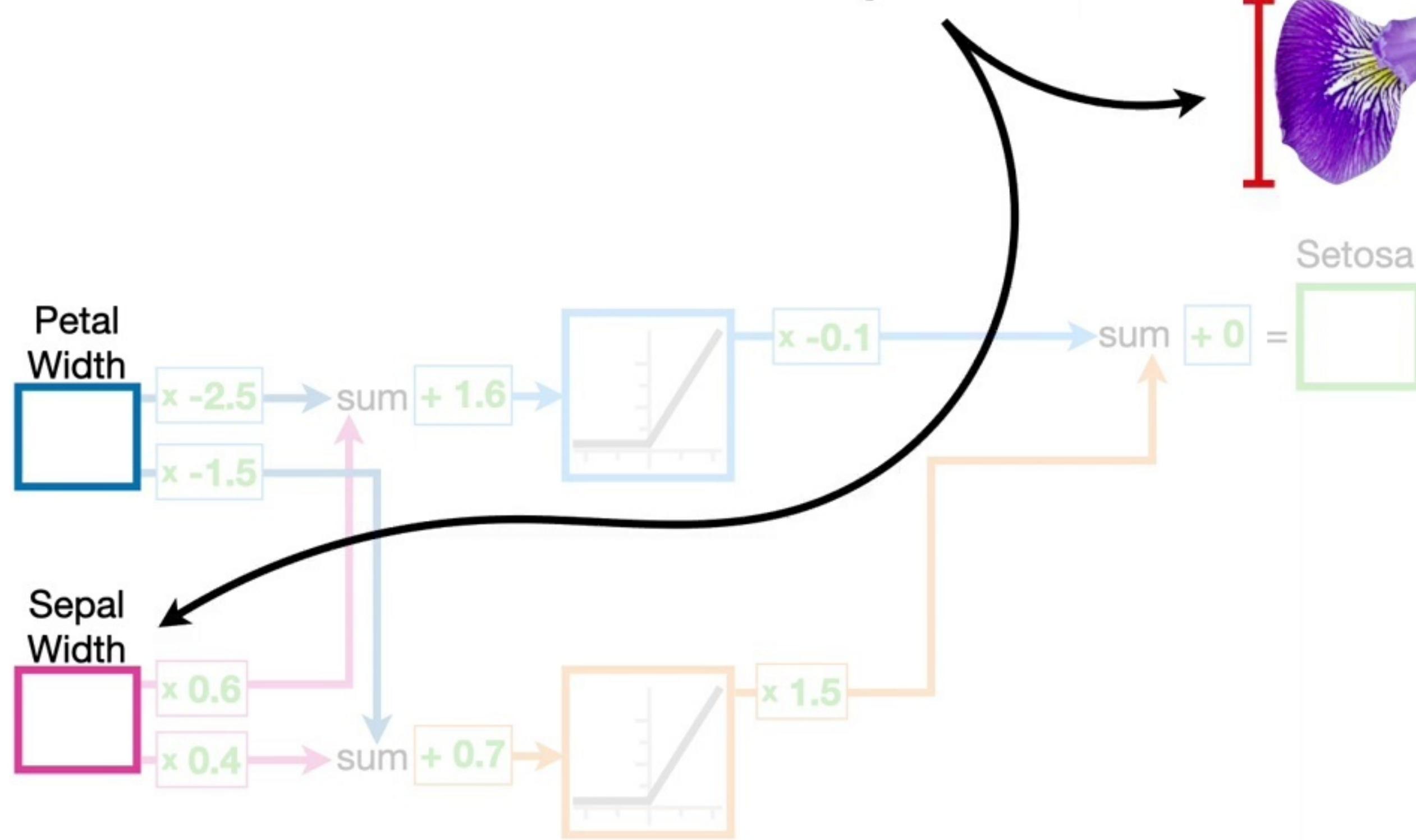


Now let's see what happens when we plug values for **Petal Width**...



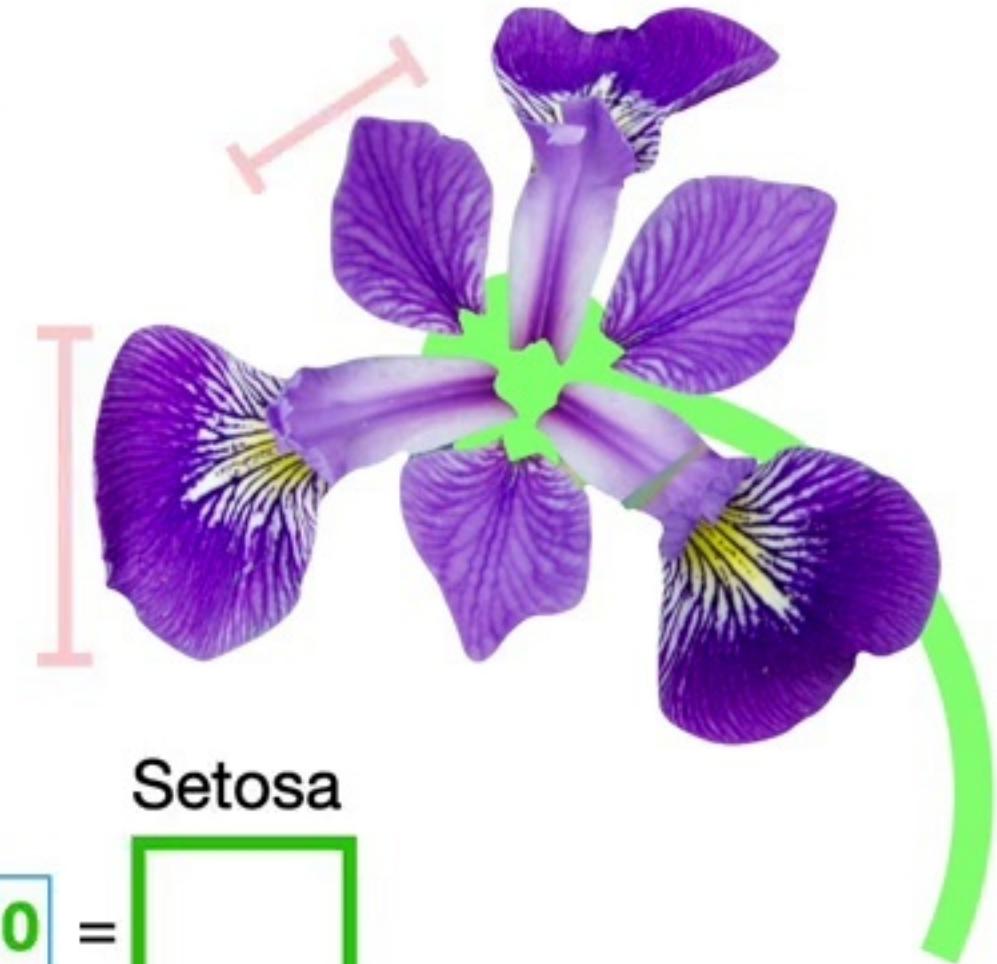
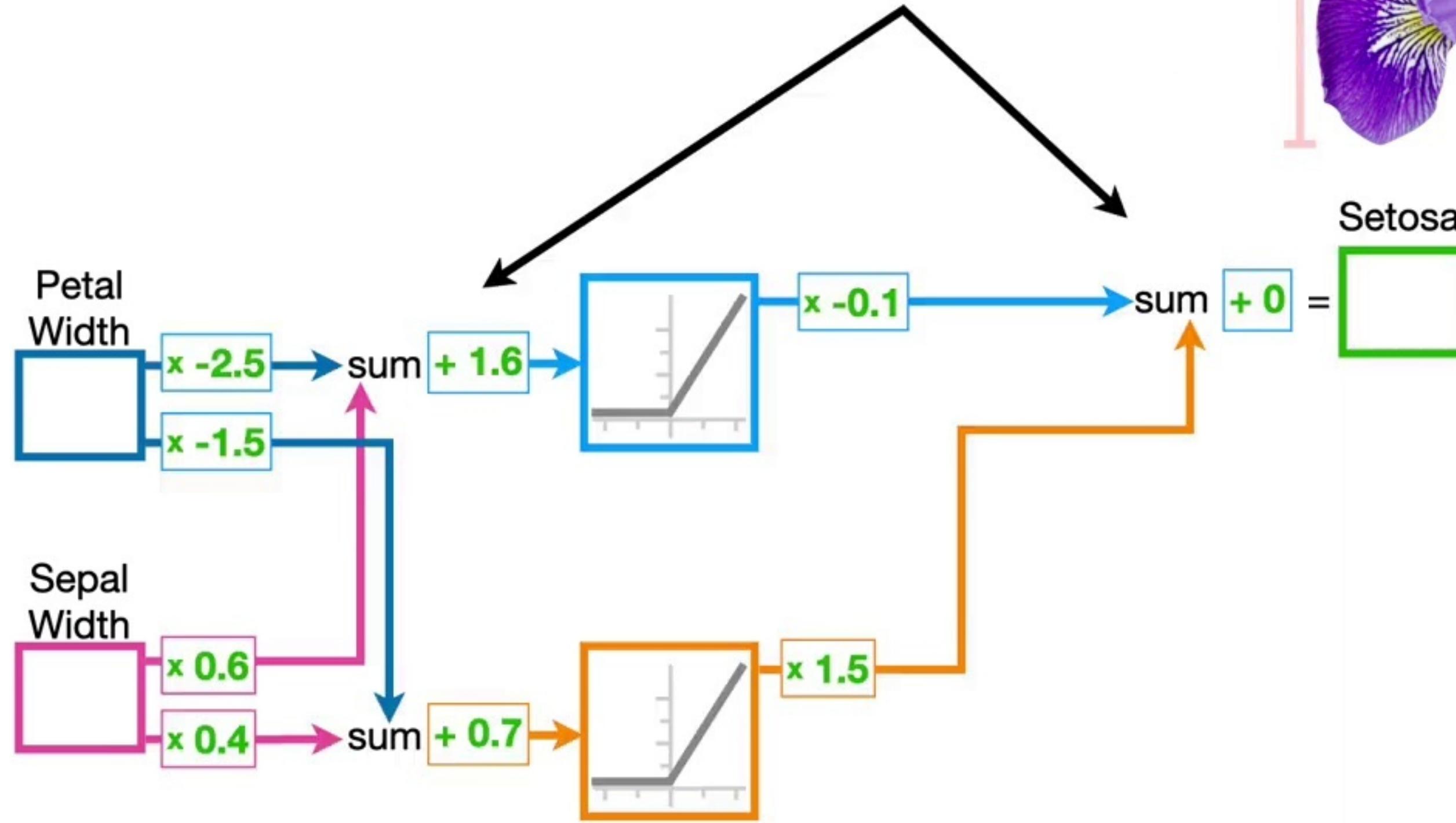


...and Sepal Width...



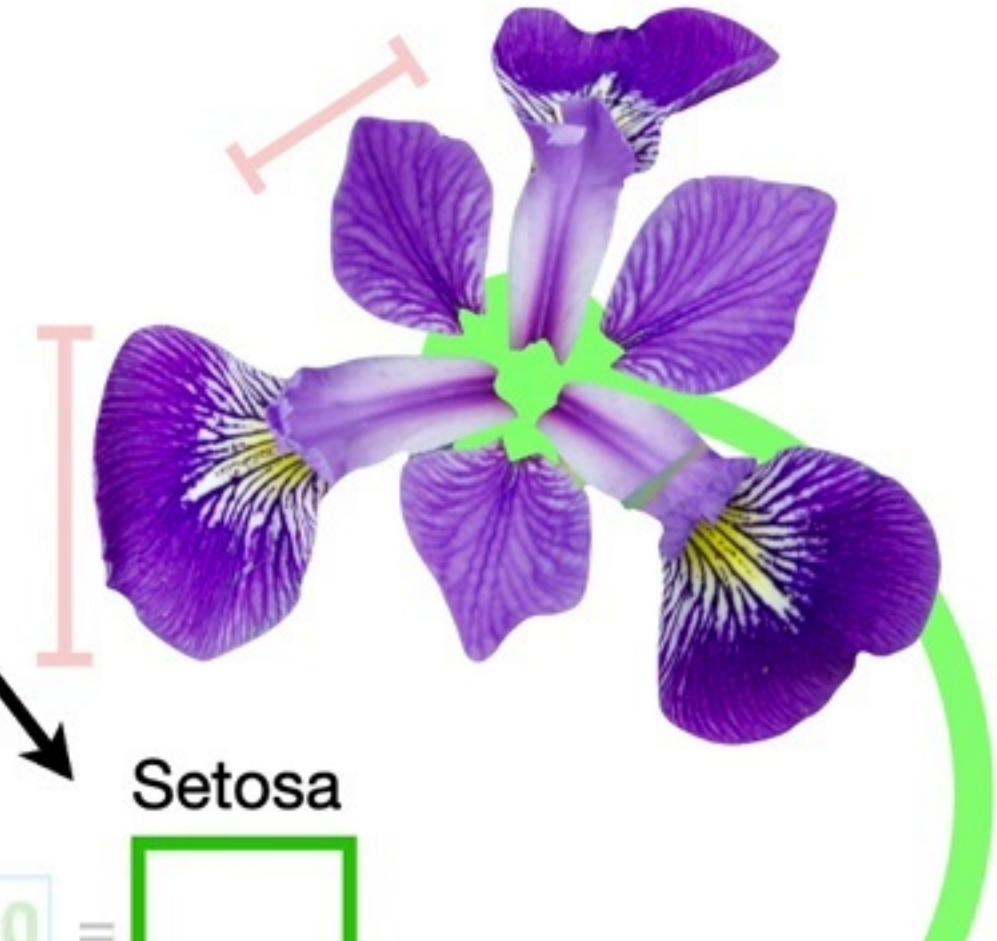
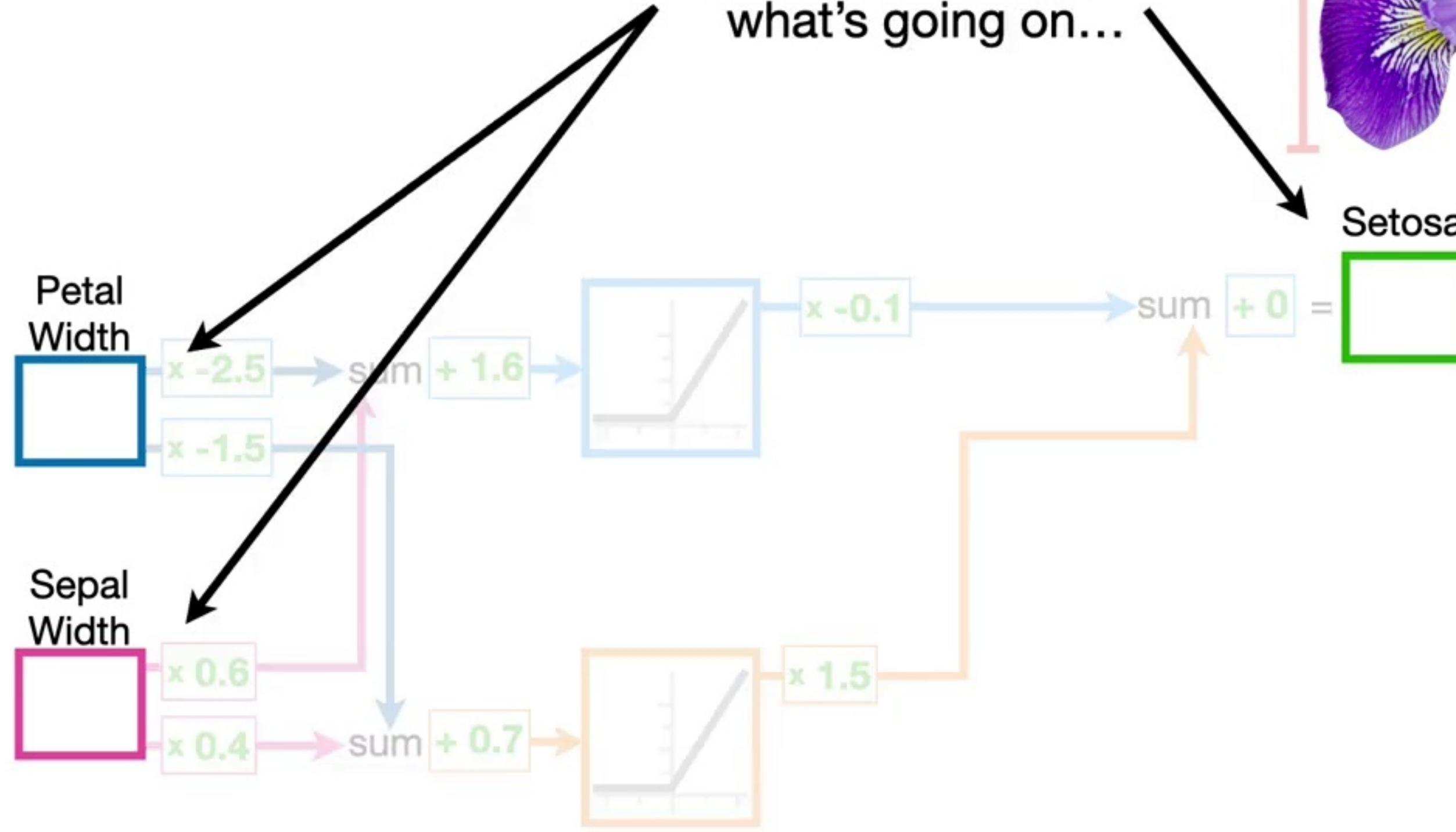


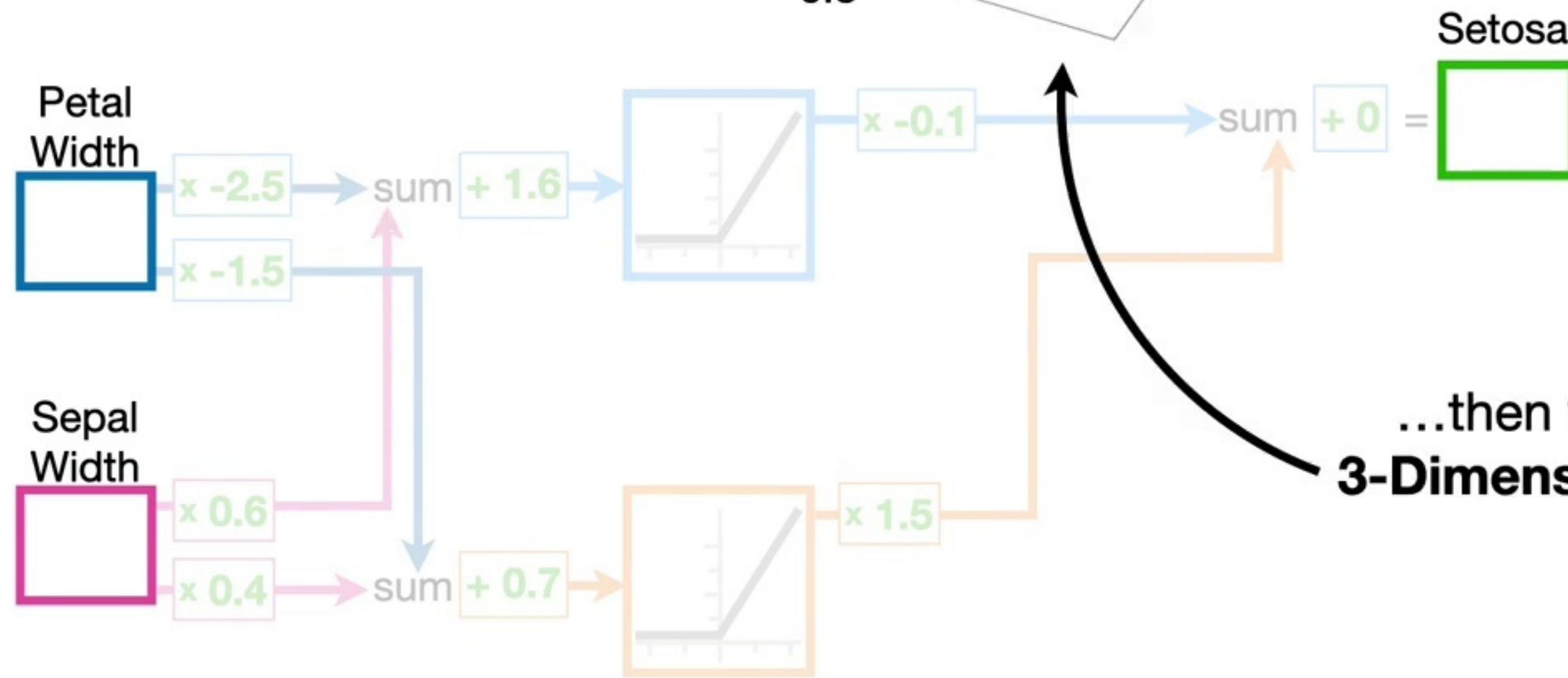
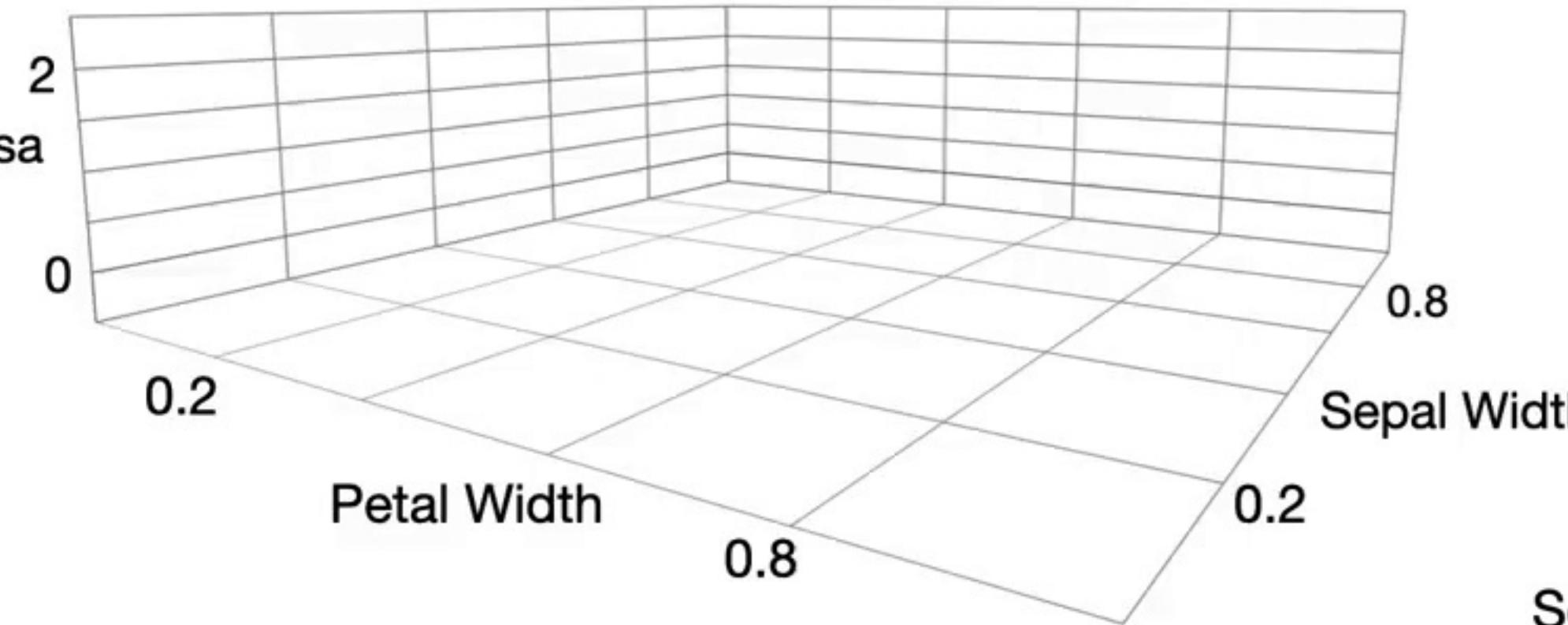
...into this simplified  
**Neural Network.**

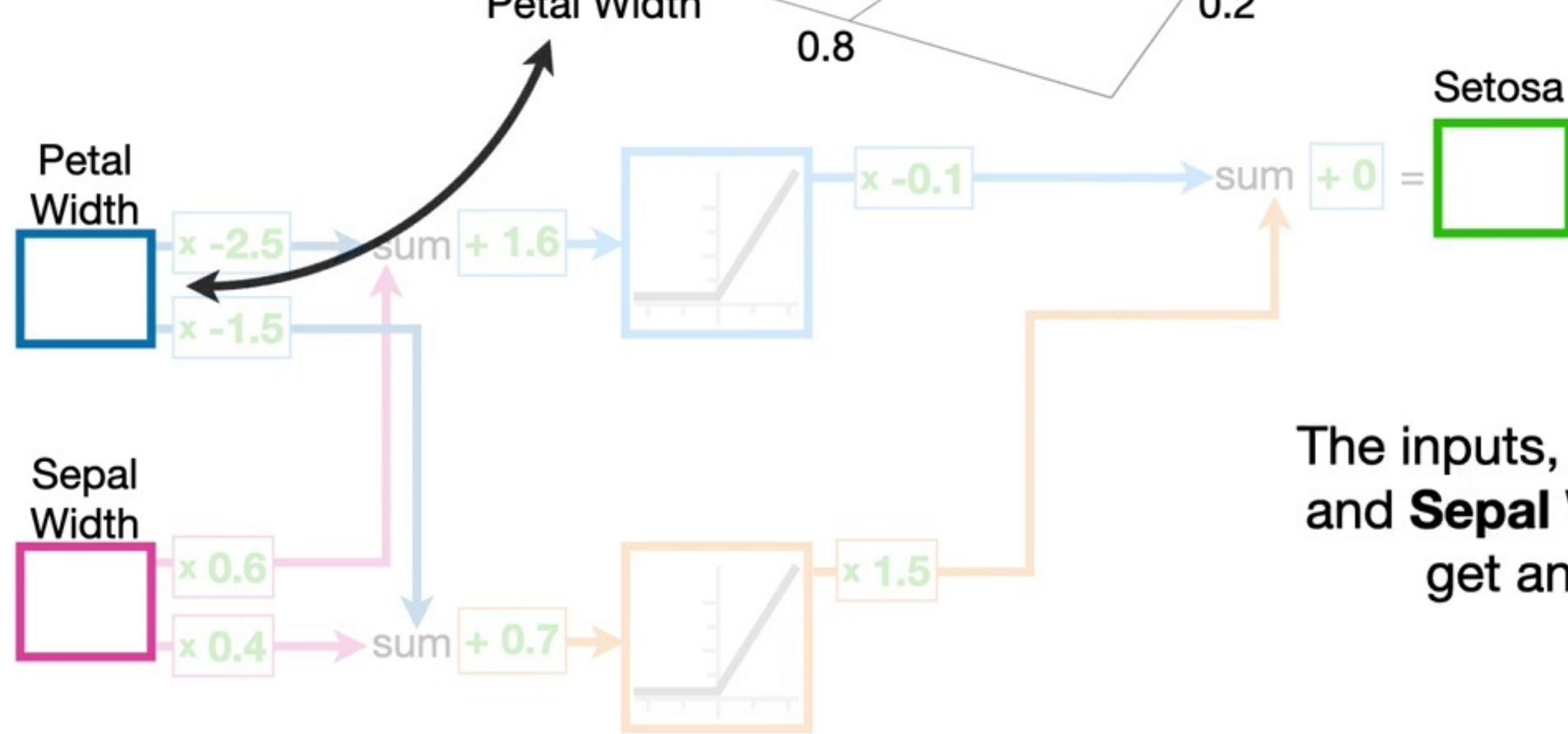
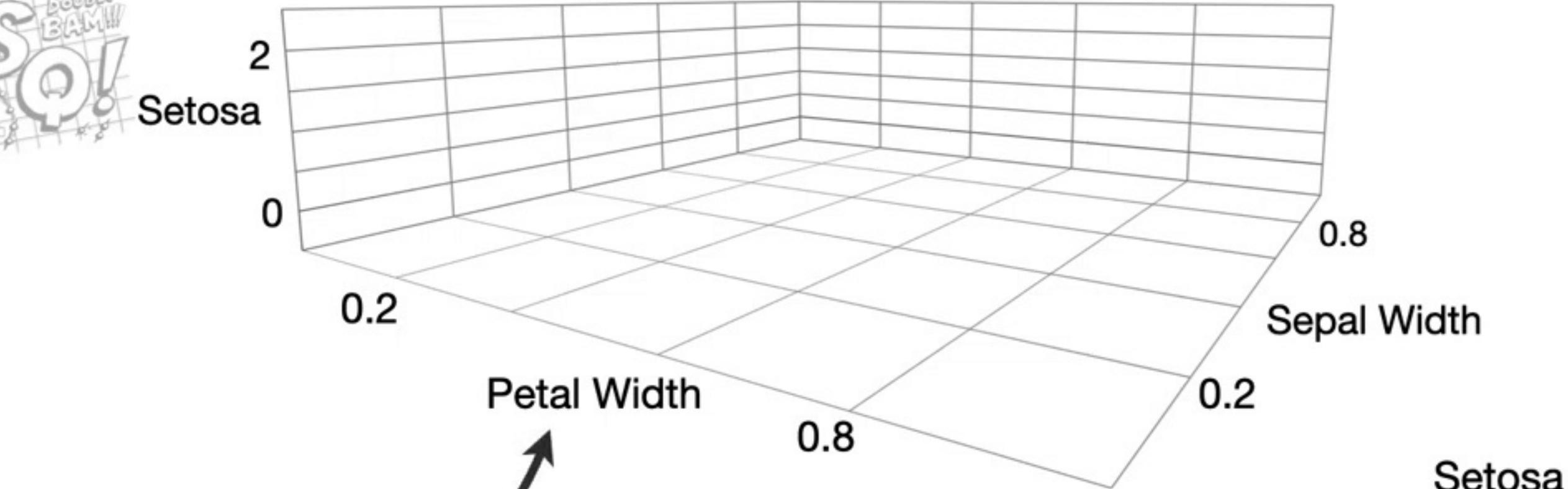


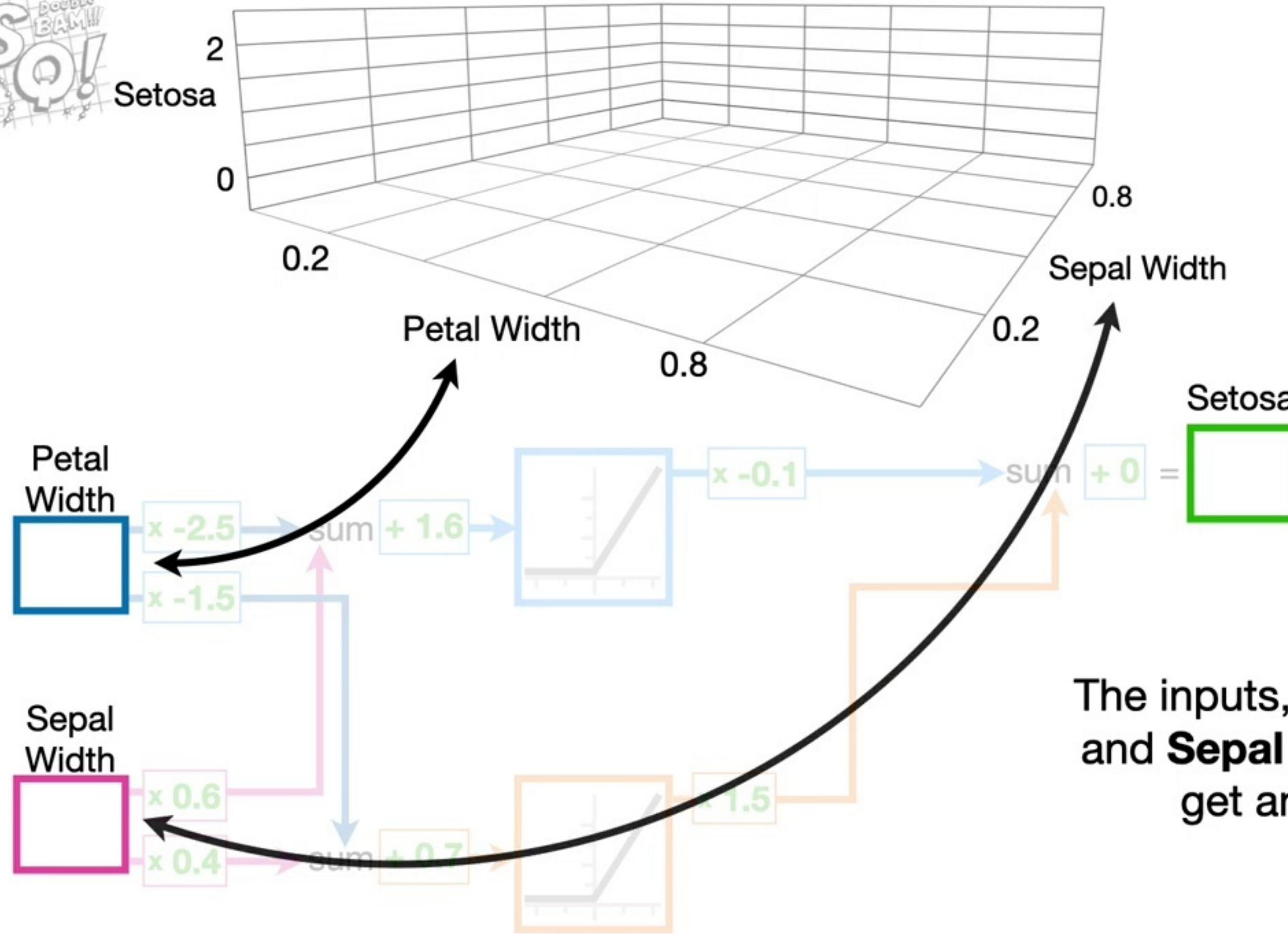


Since we have two inputs  
and one output, if we are  
going to draw a graph of  
what's going on...

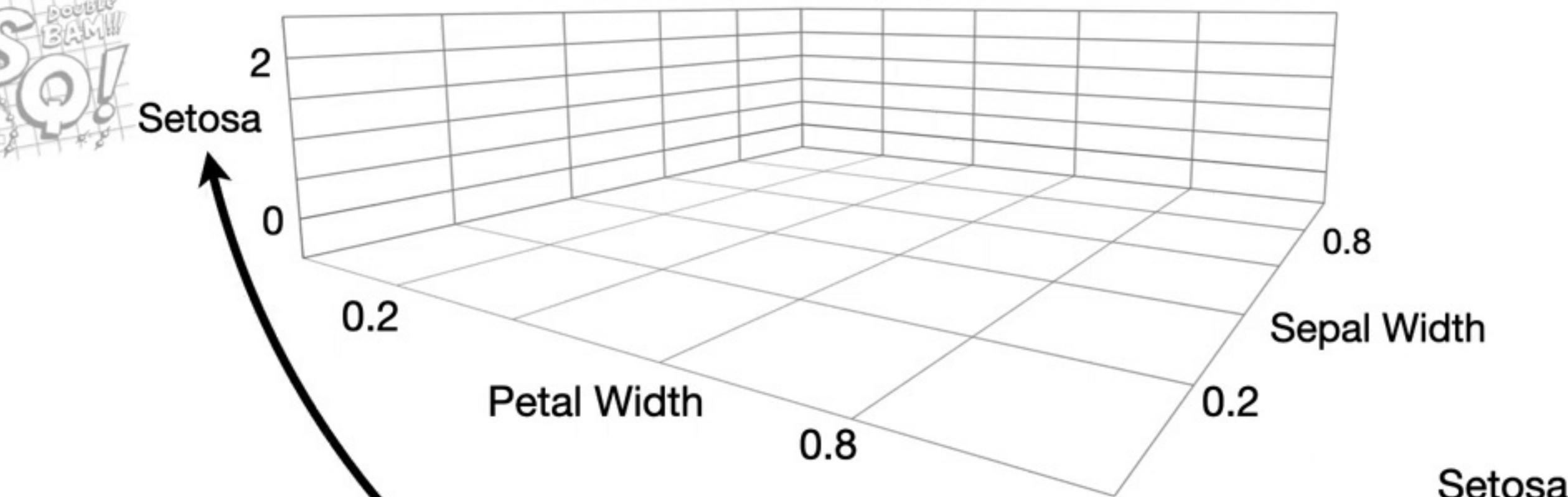








The inputs, **Petal Width** and **Sepal Width**, each get an axis...



Petal  
Width  
[ ]

$$\times -2.5 \rightarrow \text{sum}$$

$$+ 1.6 \rightarrow$$

$$\times -1.5 \rightarrow$$

sum

[ ]

[ ]

[ ]

$$\times -0.1 \rightarrow$$

[ ]

[ ]

[ ]

$$+ 0 \rightarrow$$

[ ]

Sepal  
Width  
[ ]

$$\times 0.6 \rightarrow$$

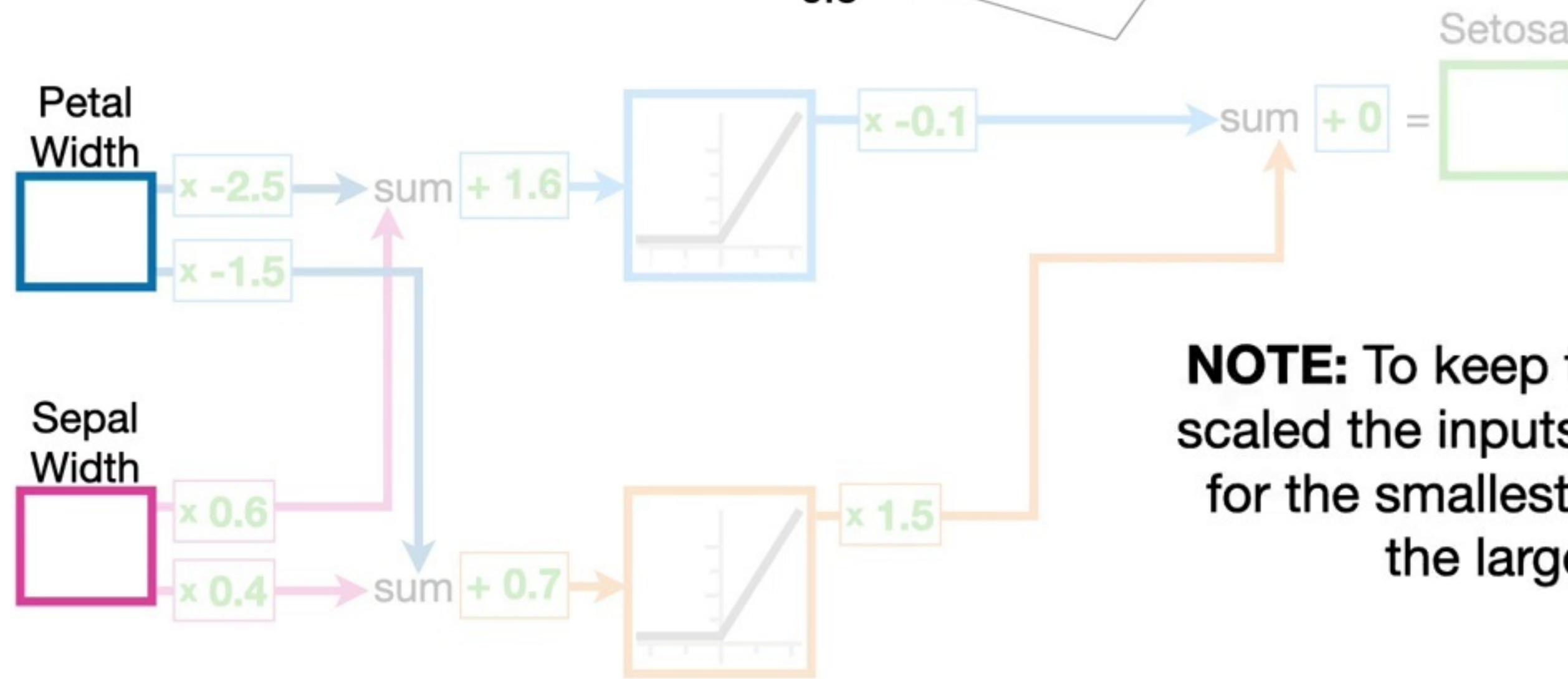
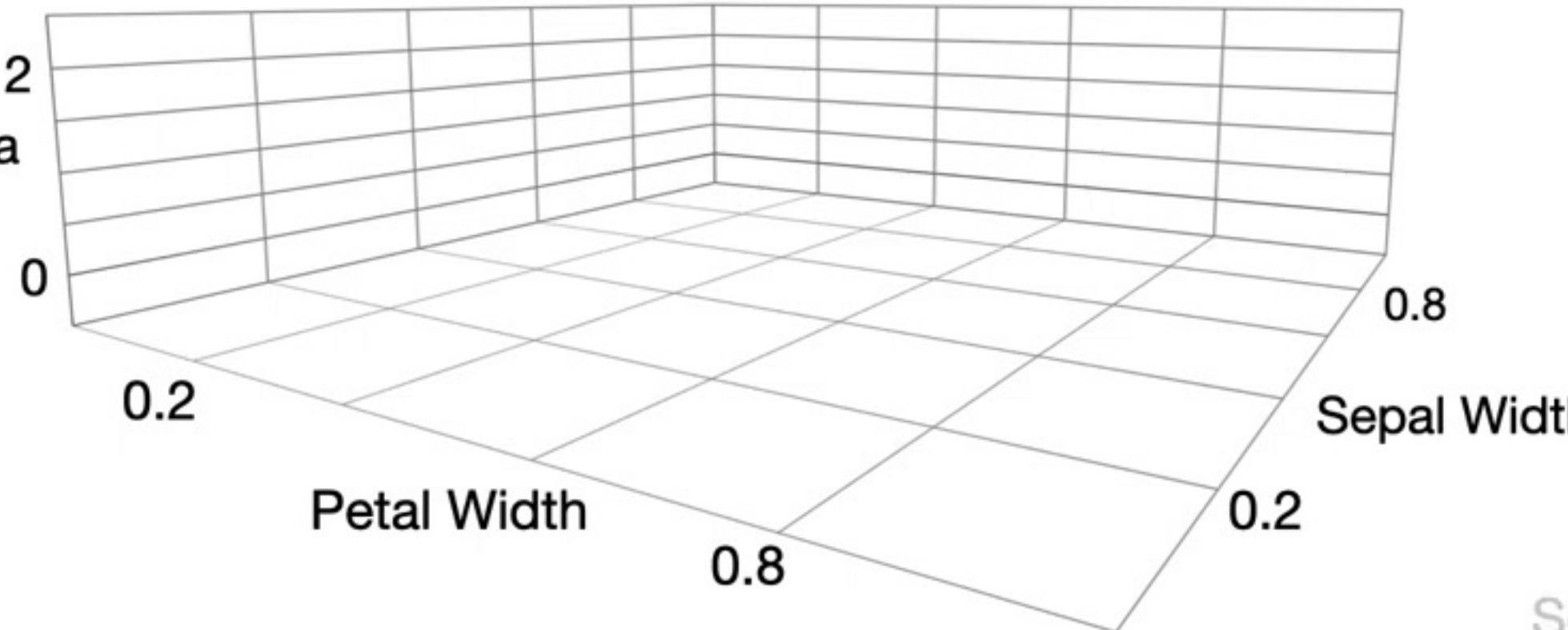
$$+ 0.7 \rightarrow$$

sum

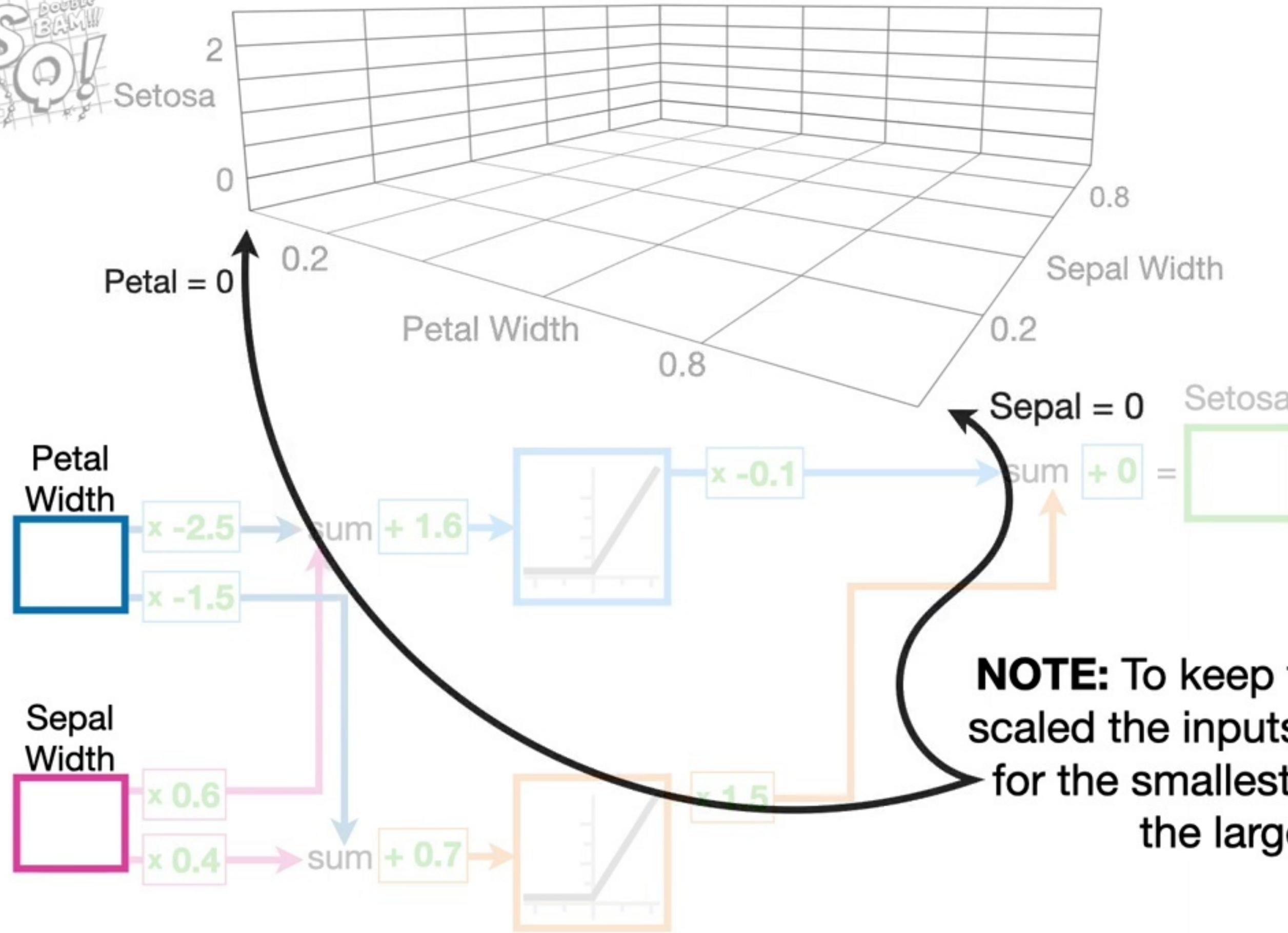
$$\times 1.5 \rightarrow$$

[ ]

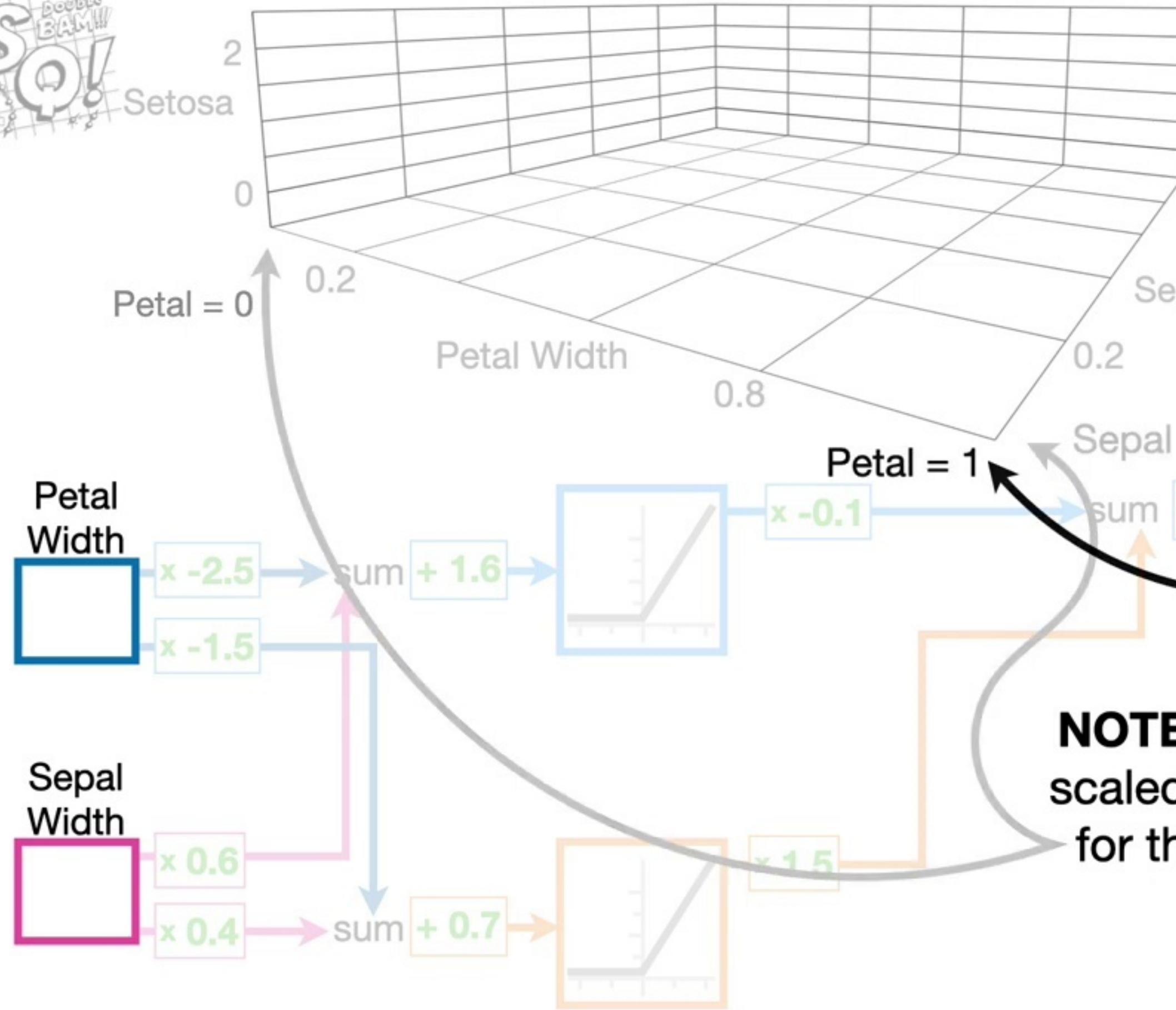
Setosa  
[ ]  
...and the output, the prediction for **Setosa**, gets the y-axis.



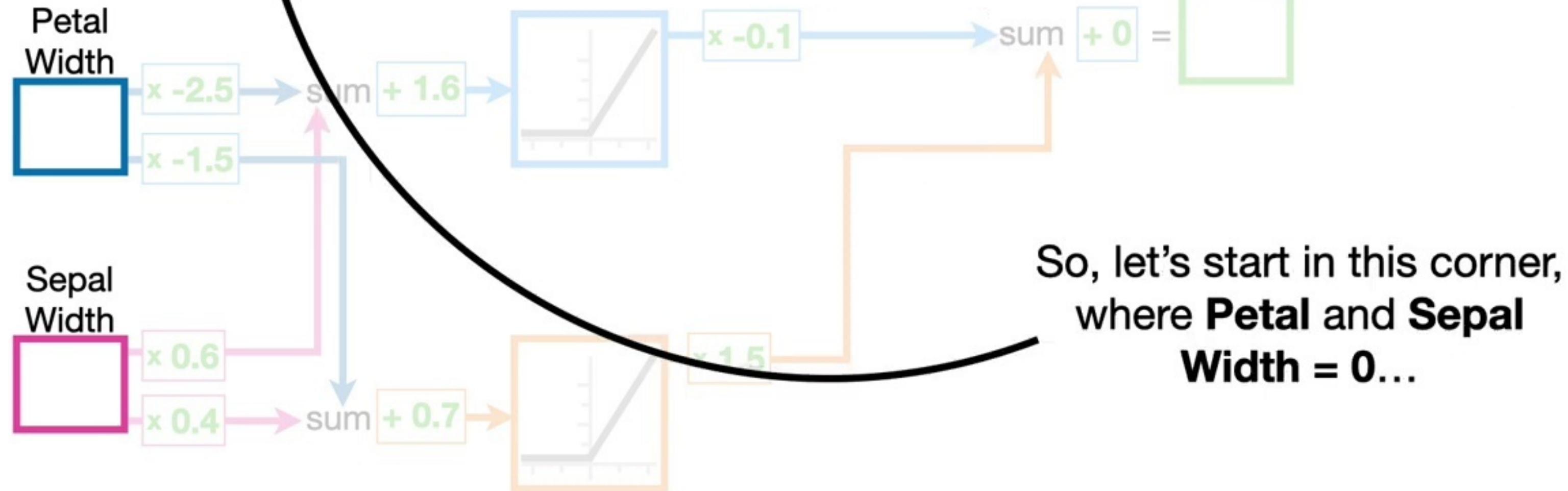
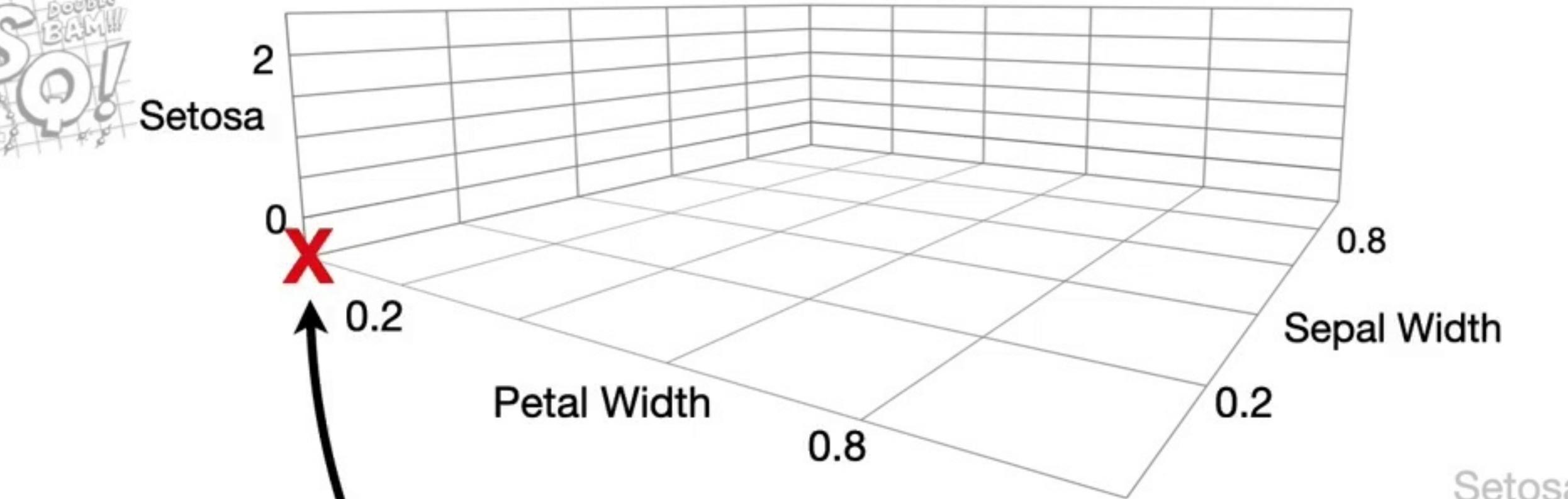
A large, bold, stylized text "SO!" is drawn on a grid background. The letters are white with black outlines. To the left of the "S", a small figure of a person is holding a rectangular sign with the word "SO!" written on it.

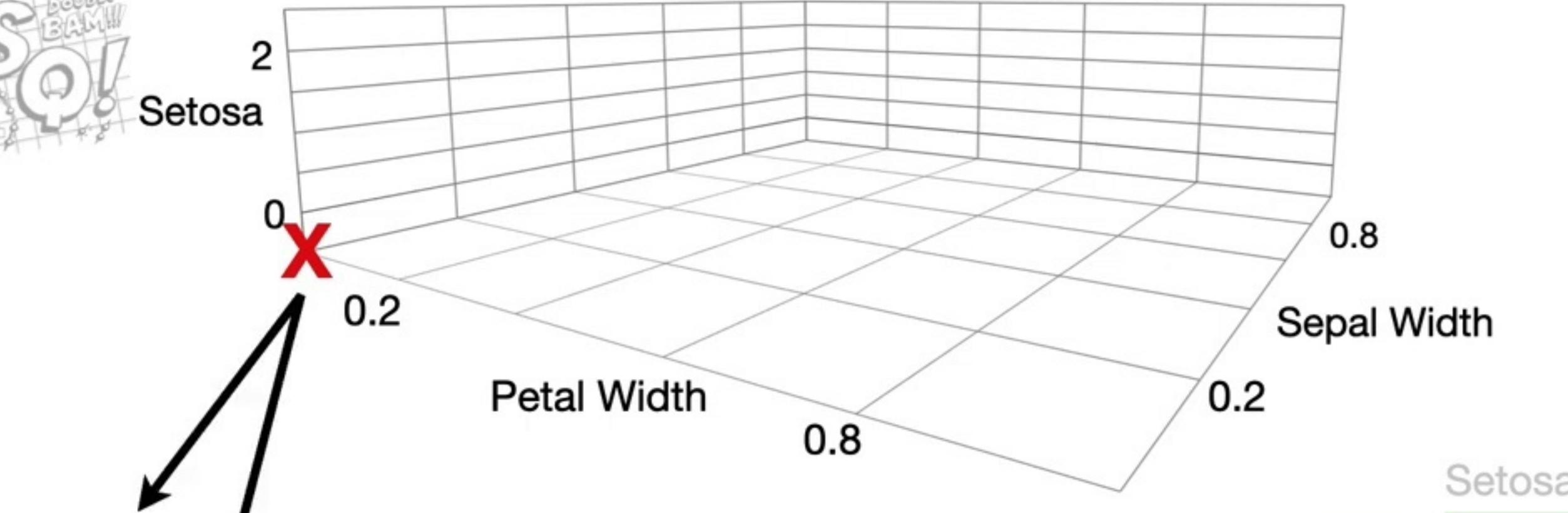


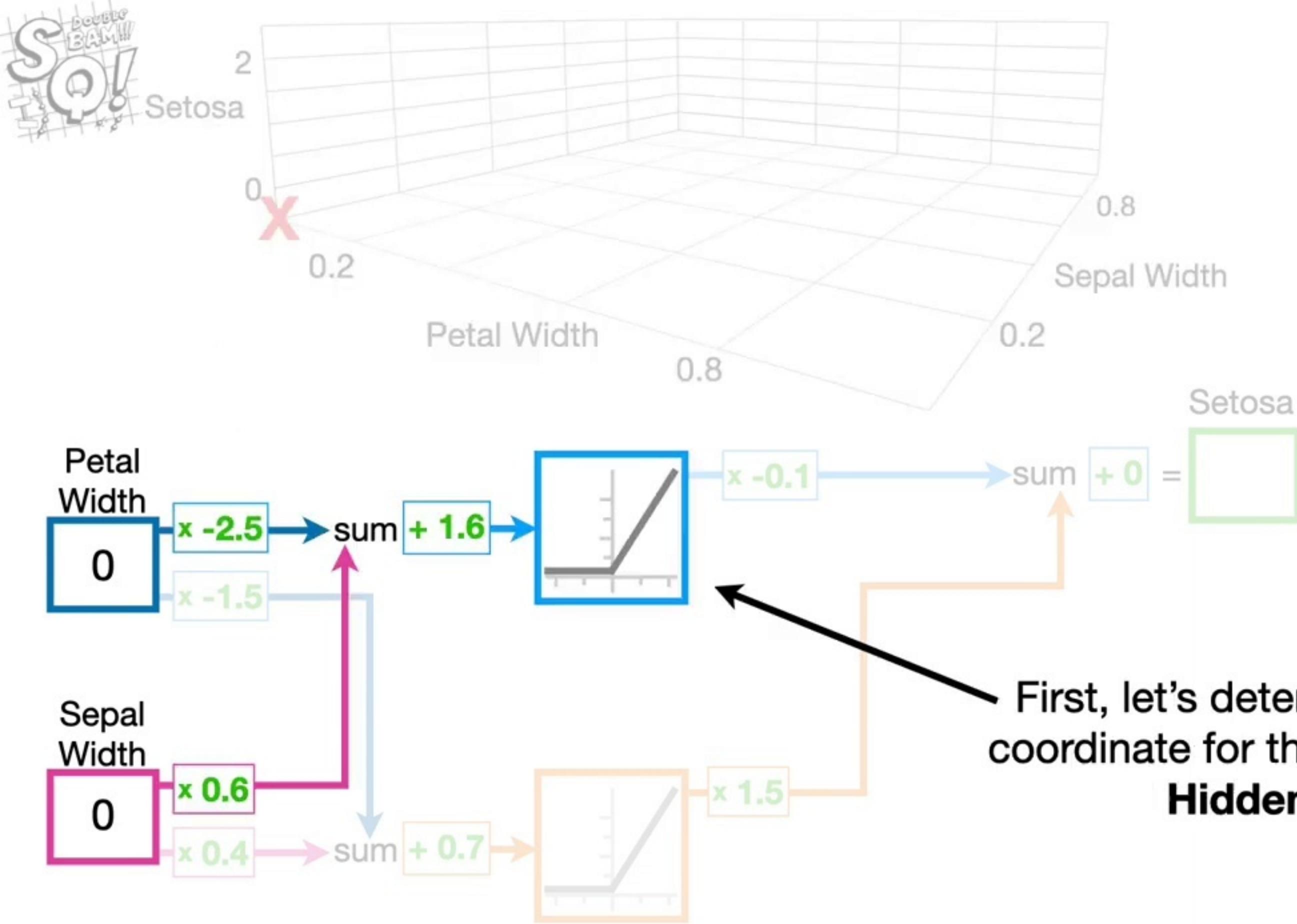
**SQ!**  
double  
BAM!!



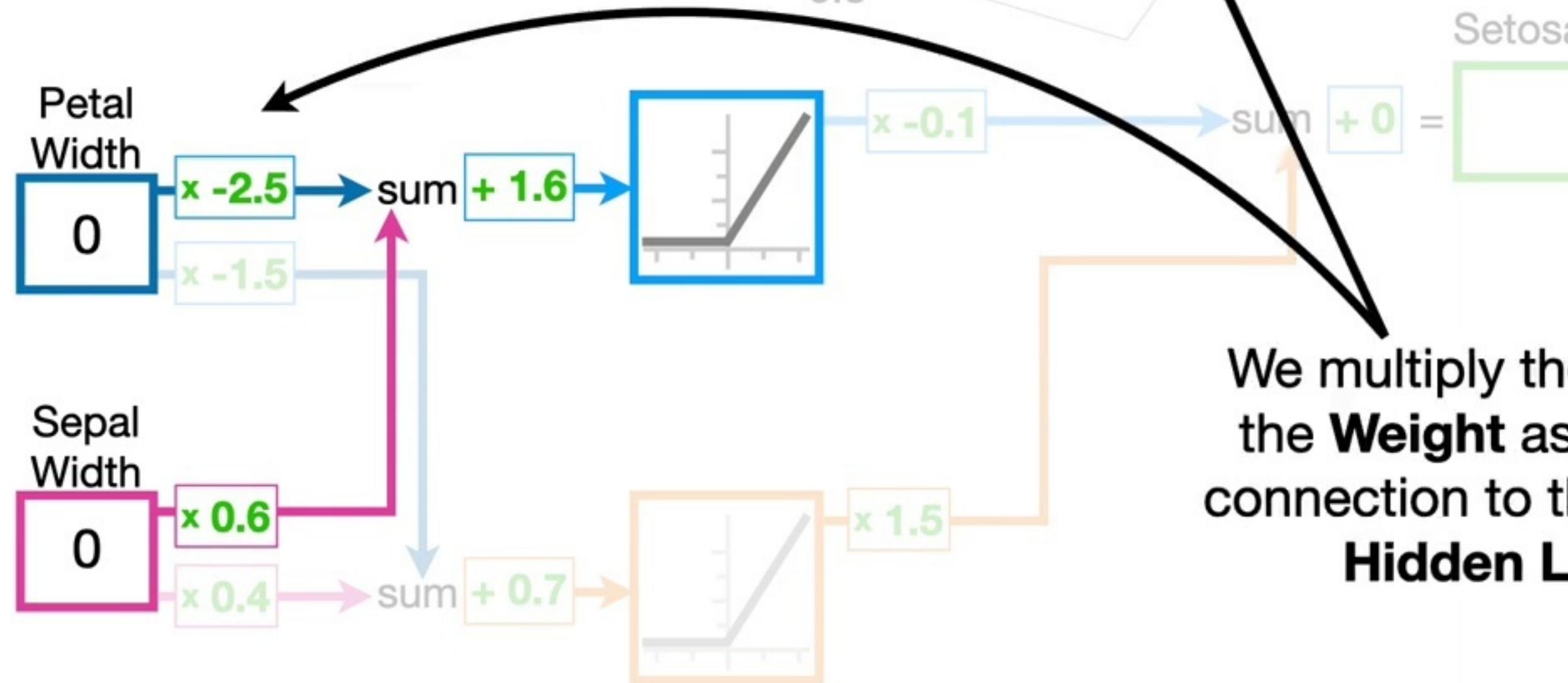
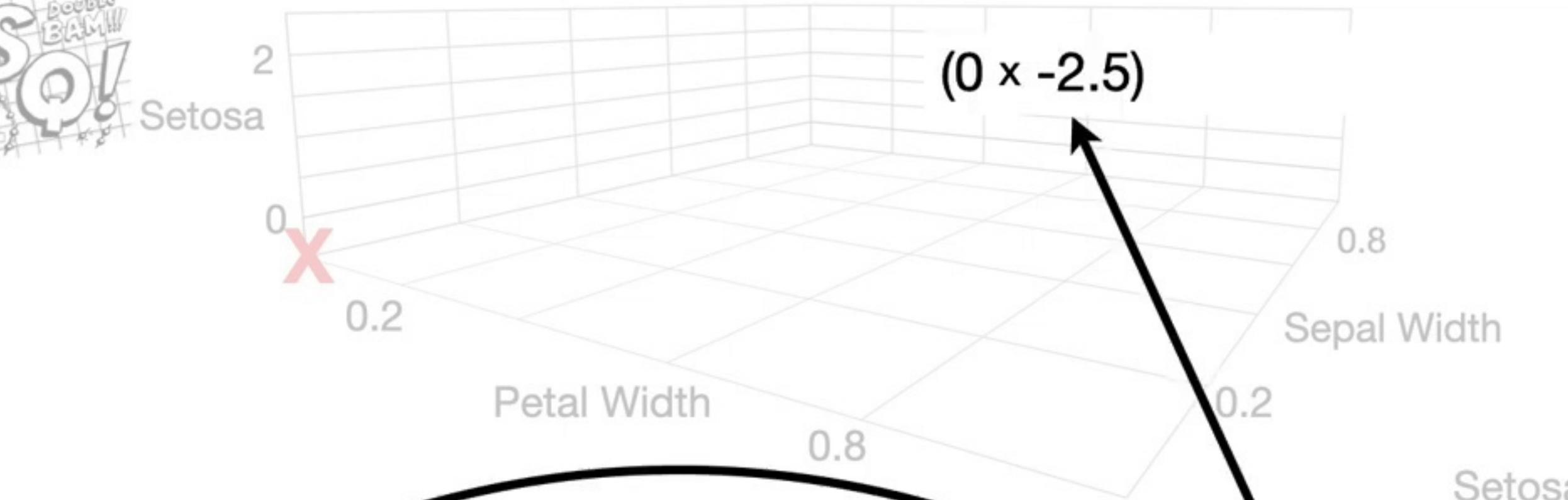
**NOTE:** To keep the math simple, I scaled the inputs to be between **0**, for the smallest value, and **1**, for the largest value.

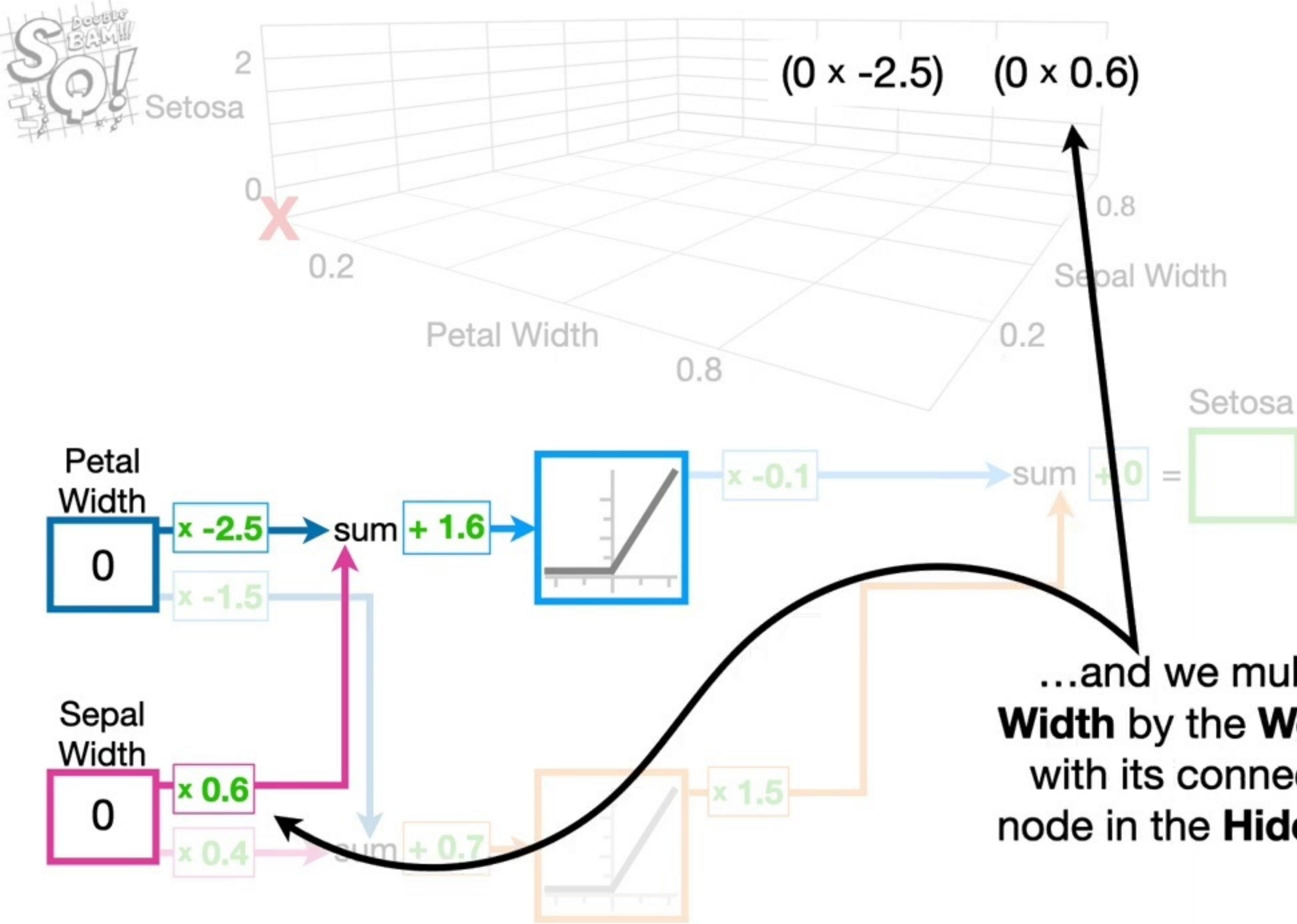






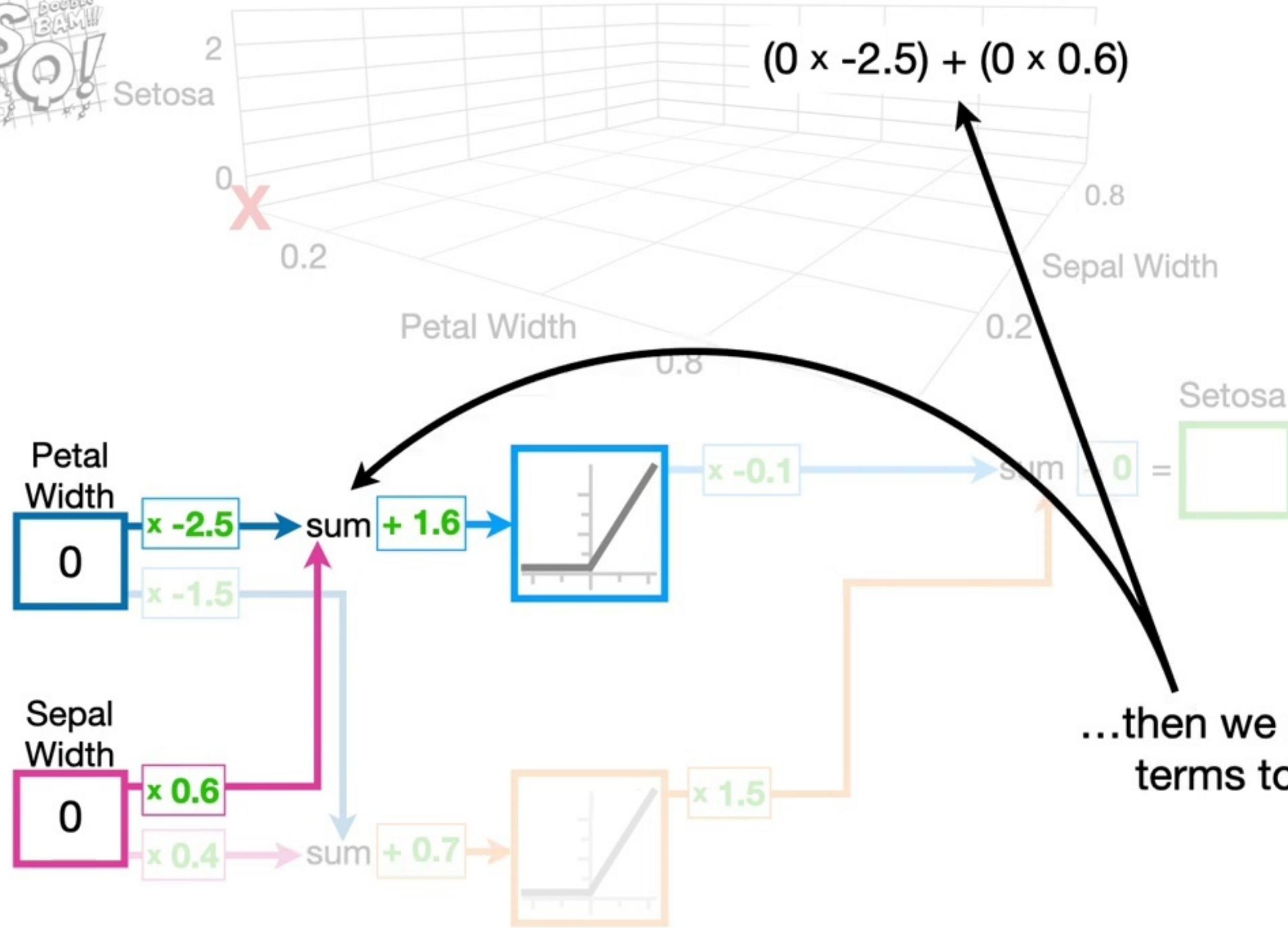
First, let's determine the x-axis coordinate for the top node in the **Hidden Layer**.



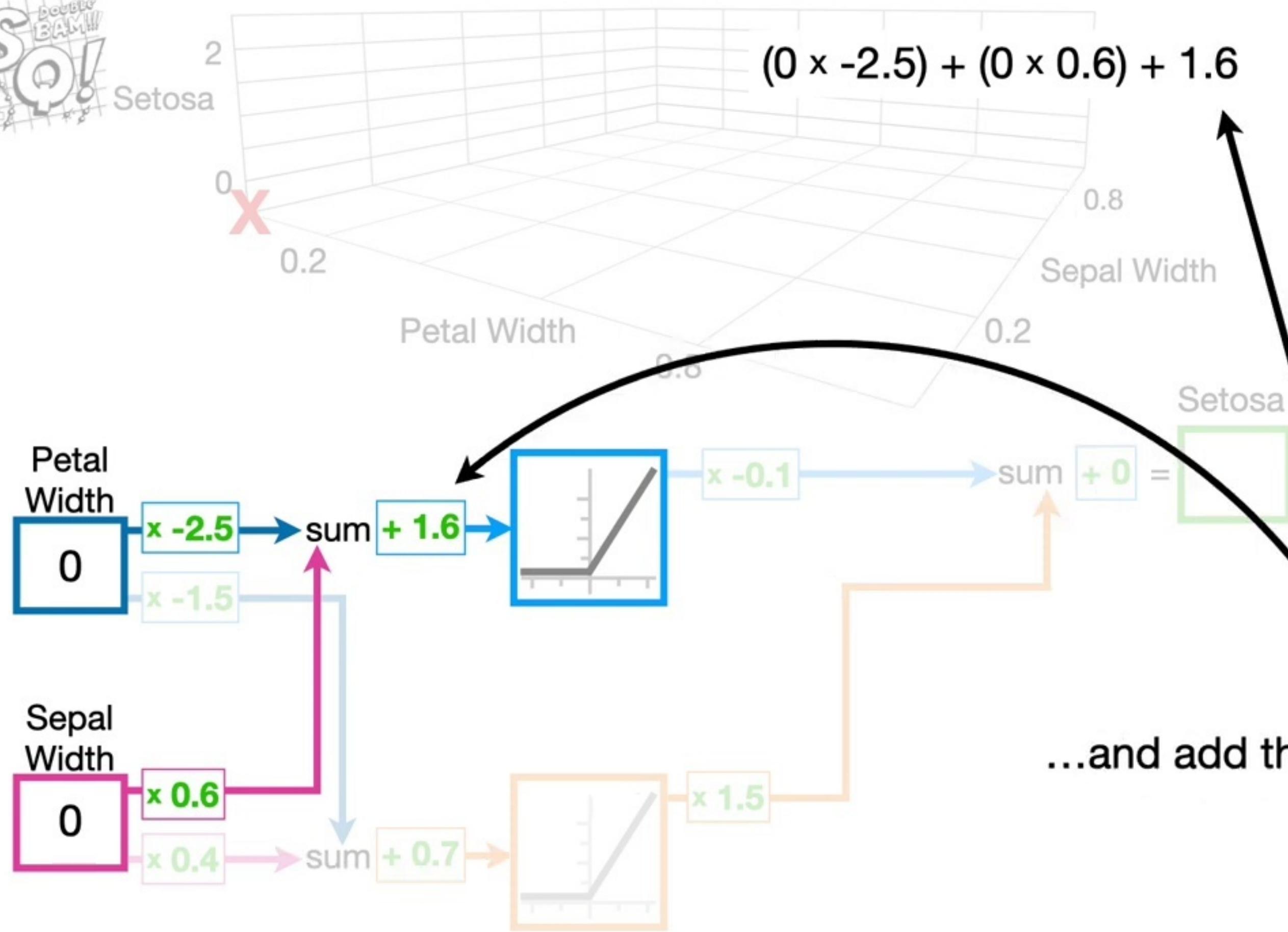


...and we multiply the **Sepal Width** by the **Weight** associated with its connection to the top node in the **Hidden Layer**, 0.6...

**SQ!**  
double  
BAM!!

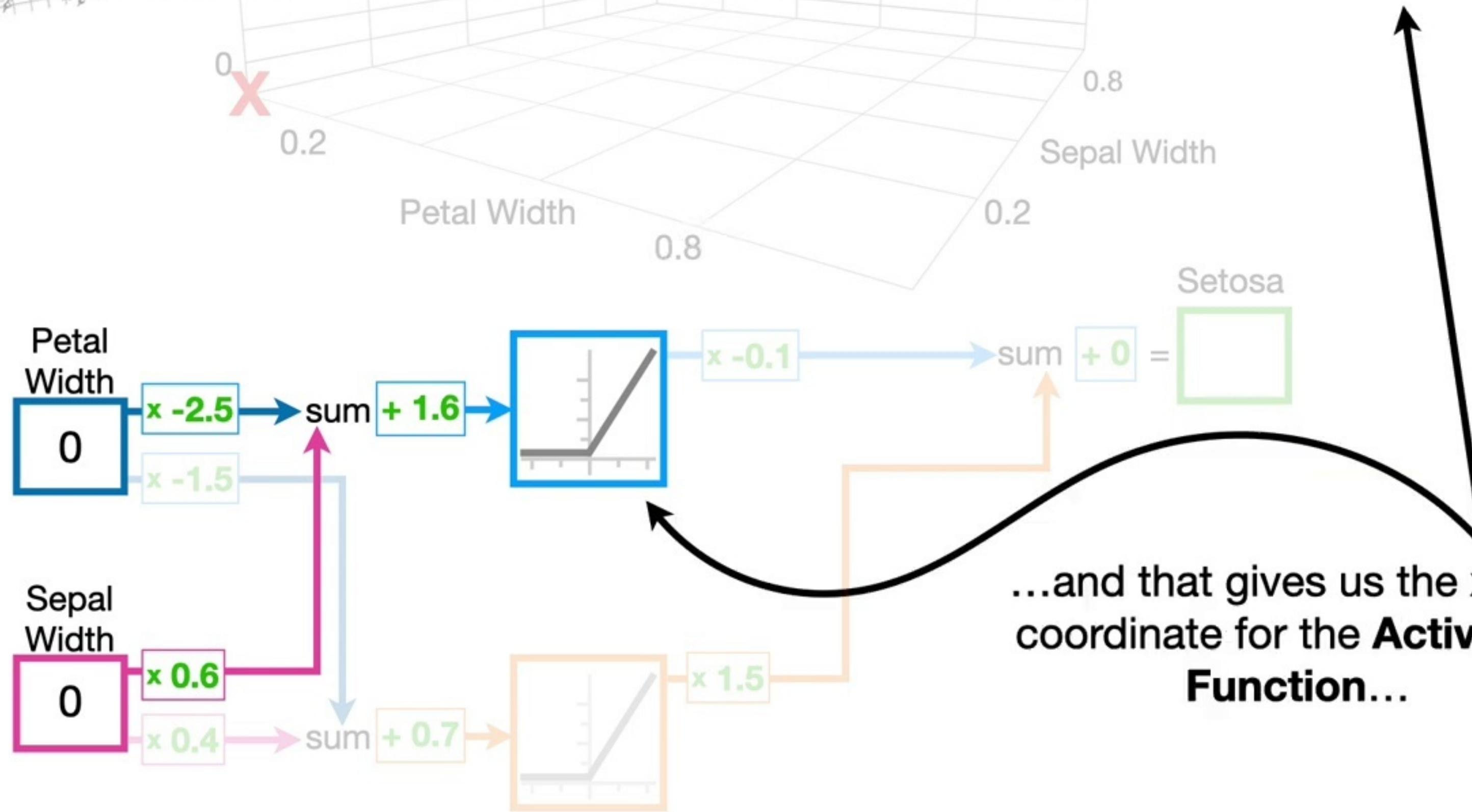


**SQ!**  
double  
BAM!!

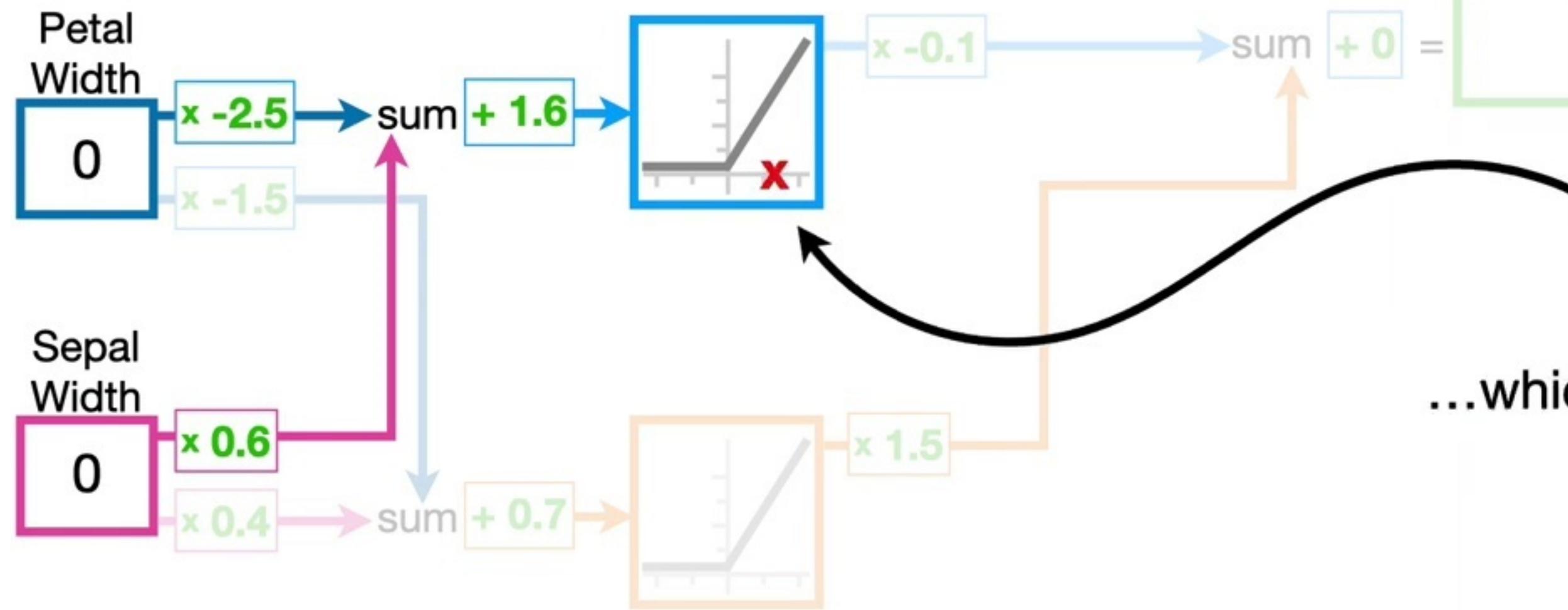
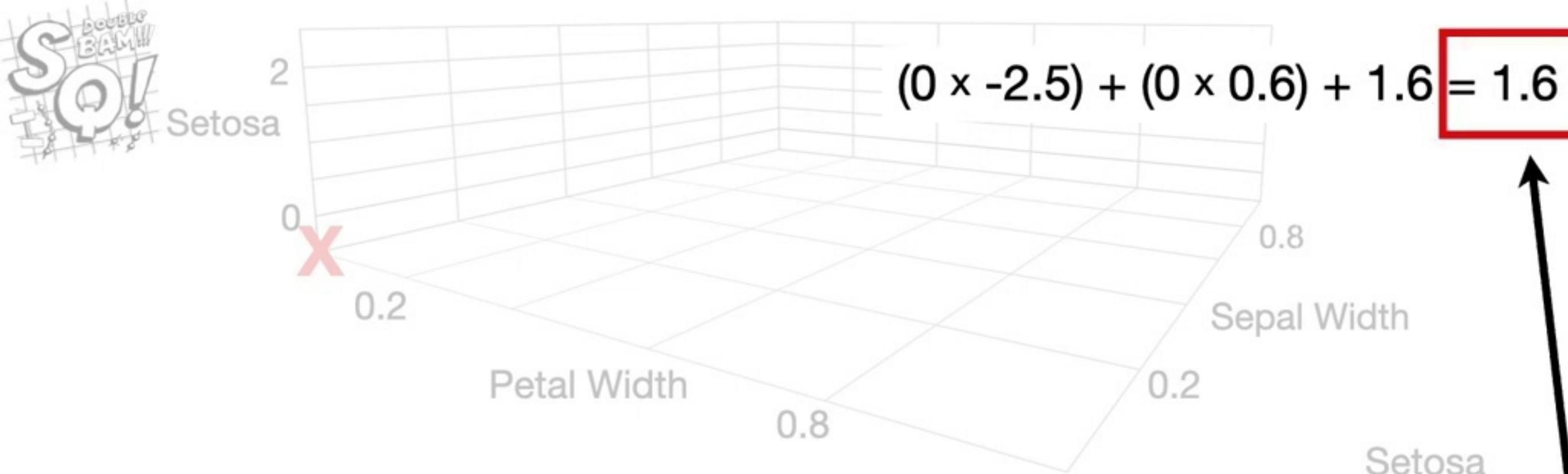


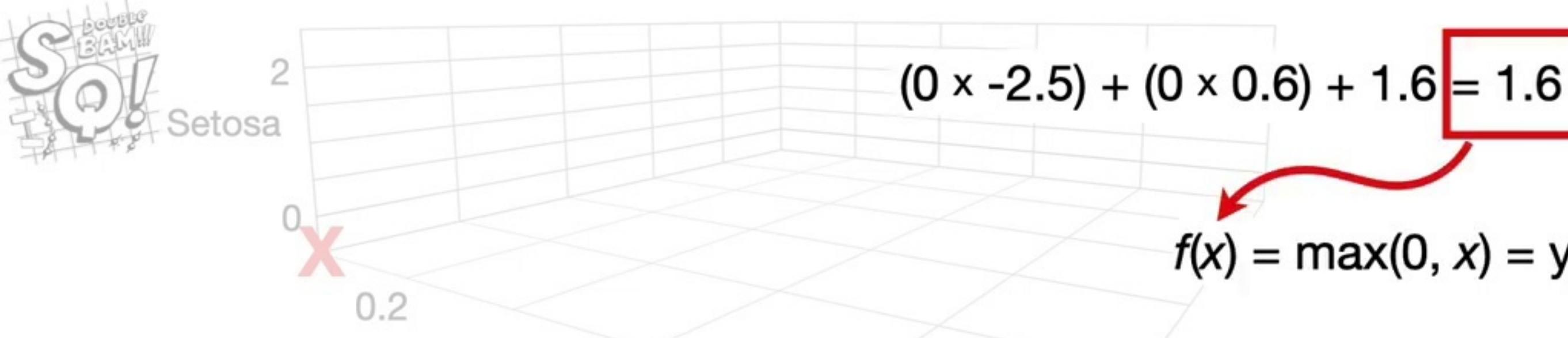
double  
BAM!!  
**SQ!**

$$(0 \times -2.5) + (0 \times 0.6) + 1.6 = \text{x-axis coordinate.}$$

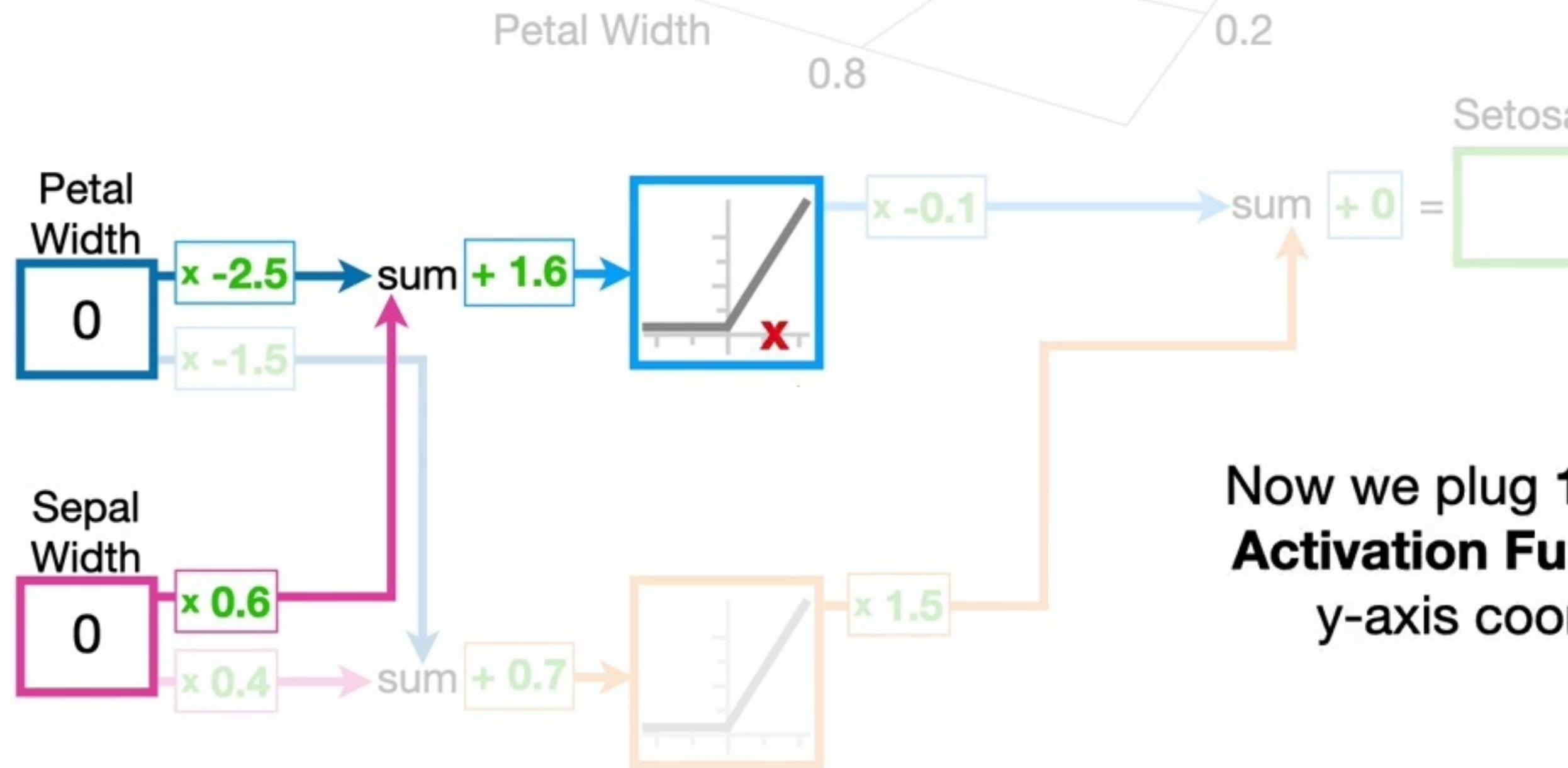


...and that gives us the x-axis coordinate for the **Activation Function**...

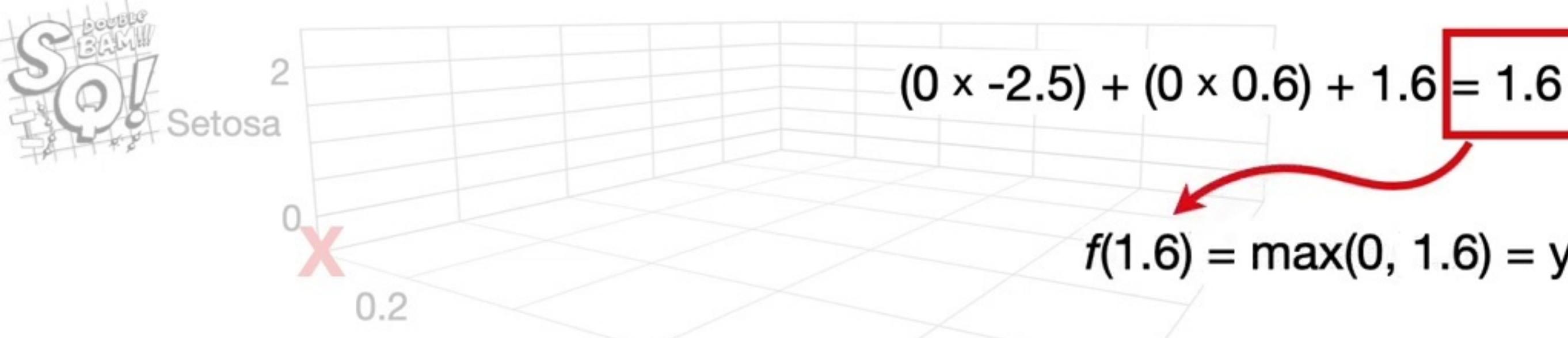




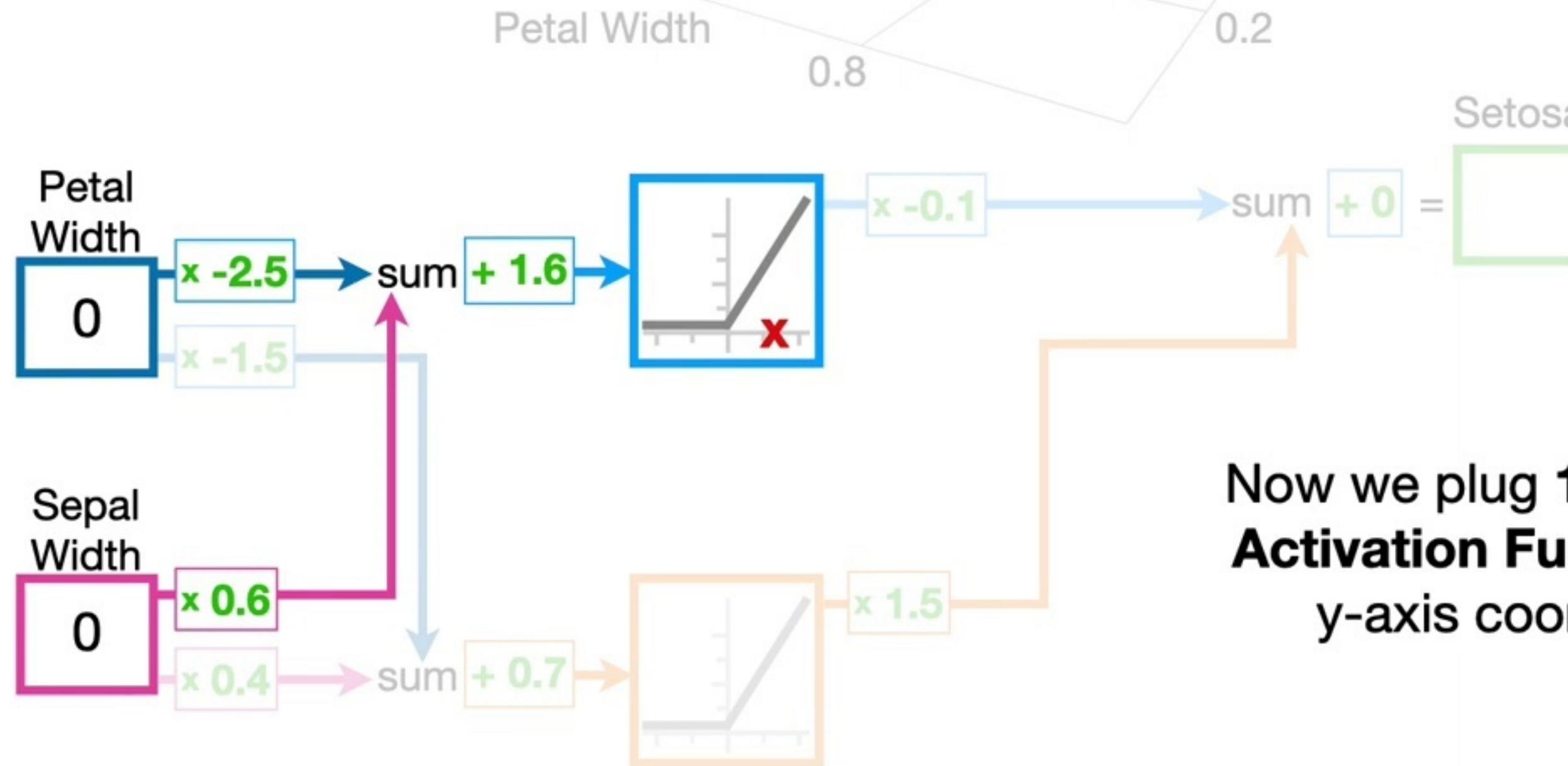
$f(x) = \max(0, x) = y\text{-axis coordinate}$



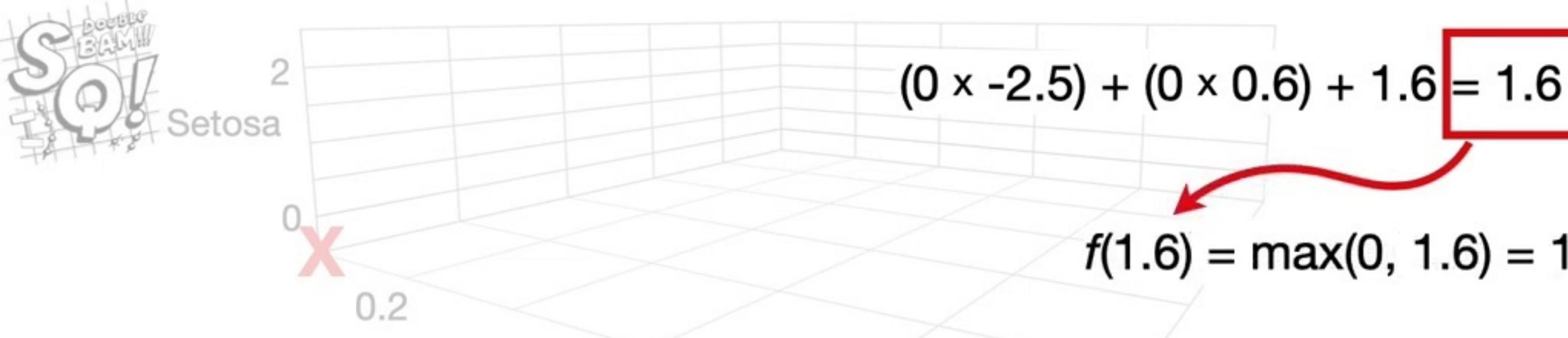
Now we plug **1.6** into the **ReLU Activation Function** to get the y-axis coordinate, **1.6...**



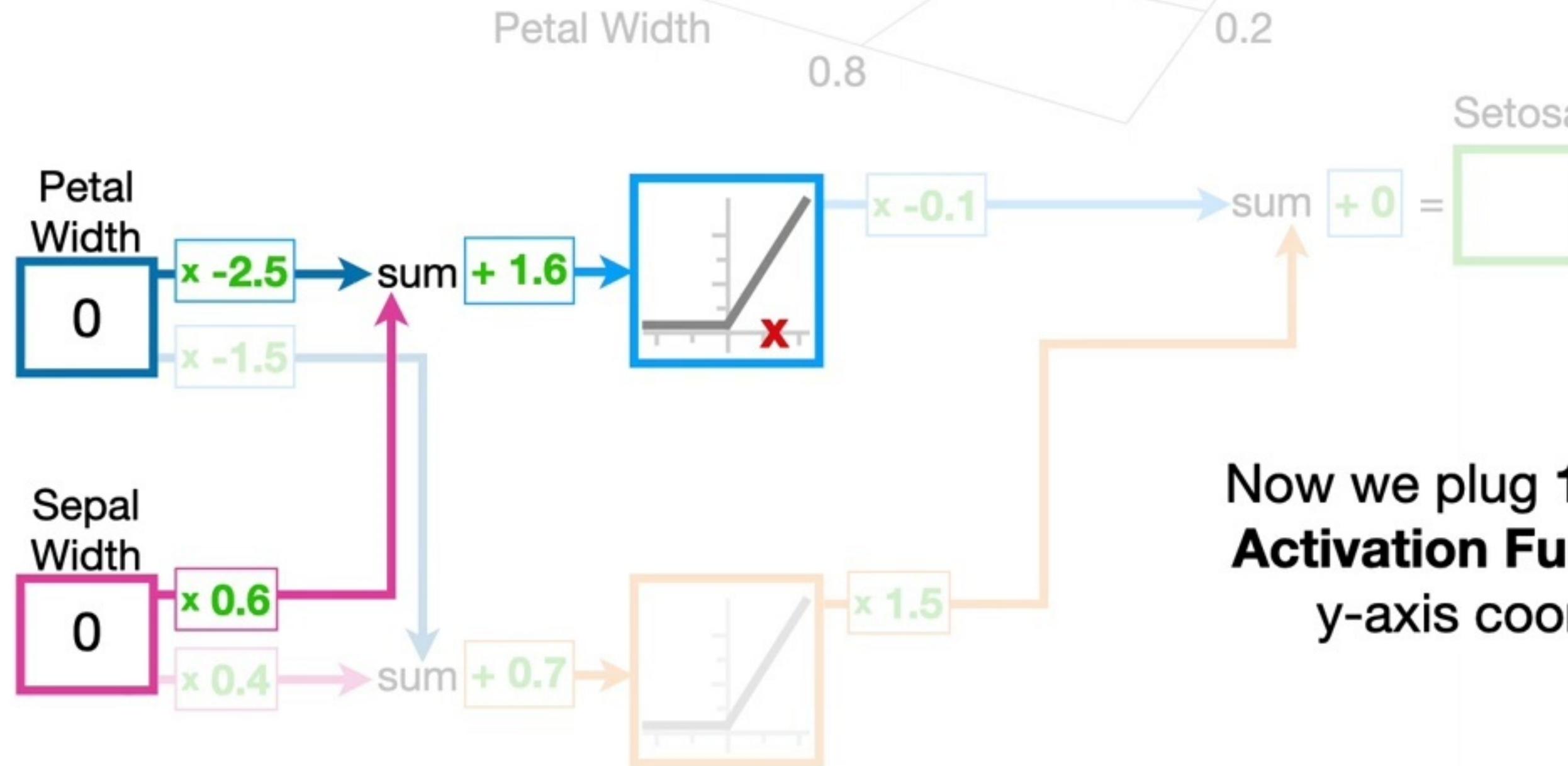
$f(1.6) = \max(0, 1.6) = \text{y-axis coordinate}$



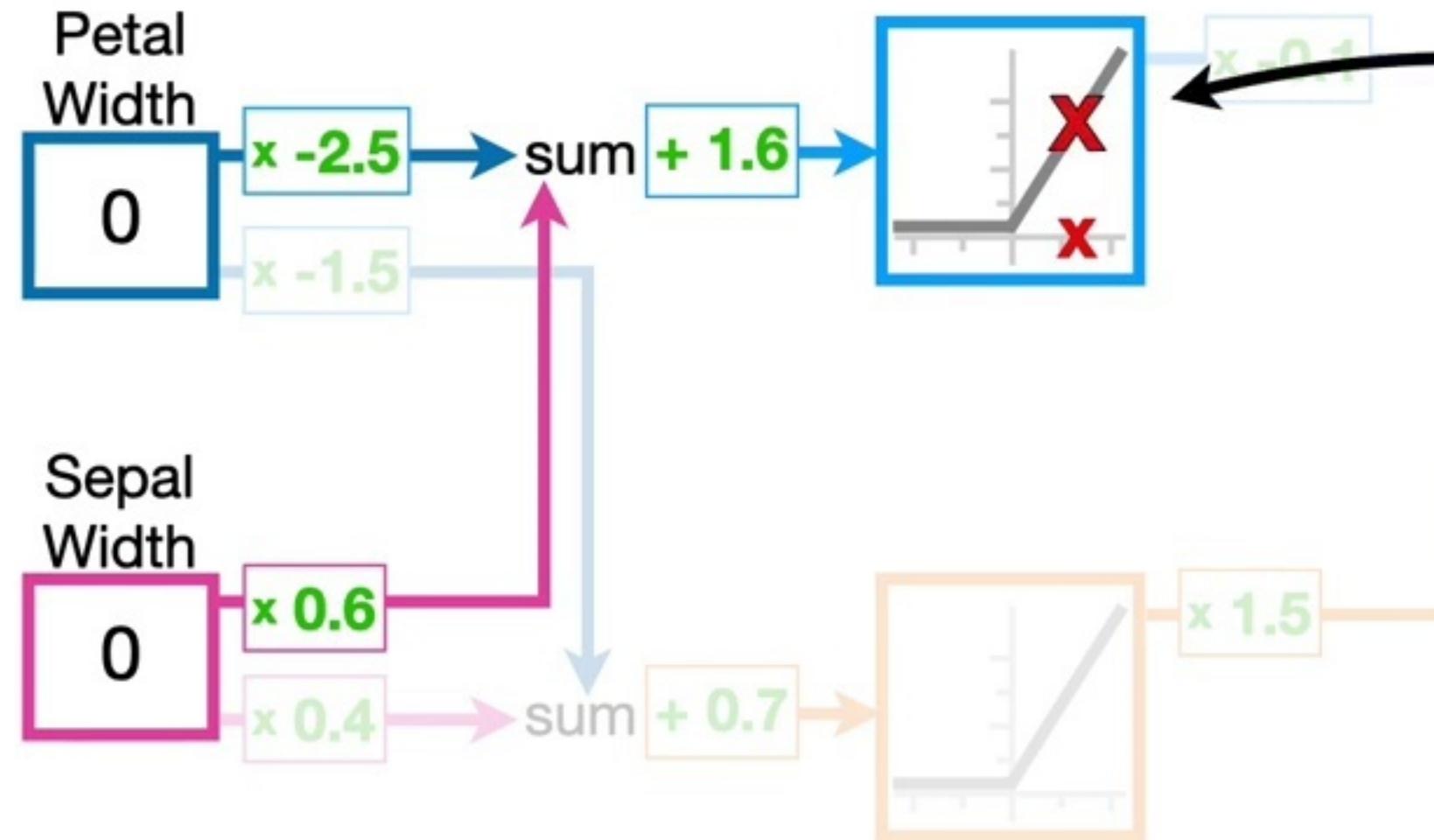
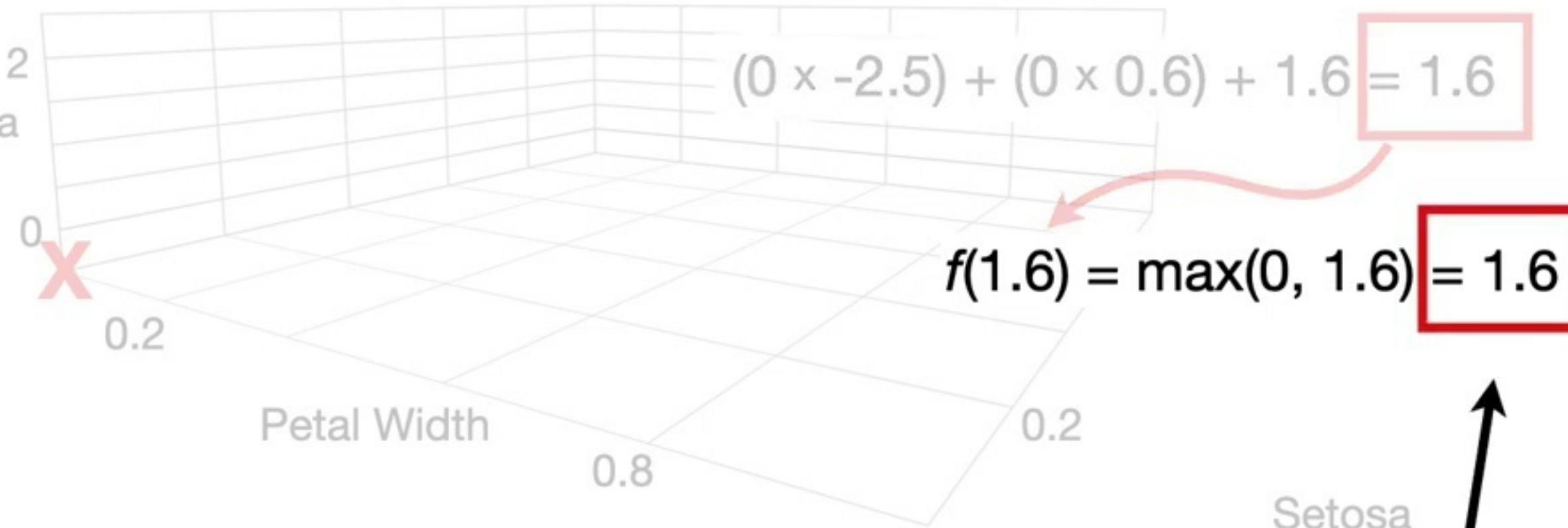
Now we plug **1.6** into the **ReLU Activation Function** to get the y-axis coordinate, **1.6...**



$$f(1.6) = \max(0, 1.6) = 1.6$$

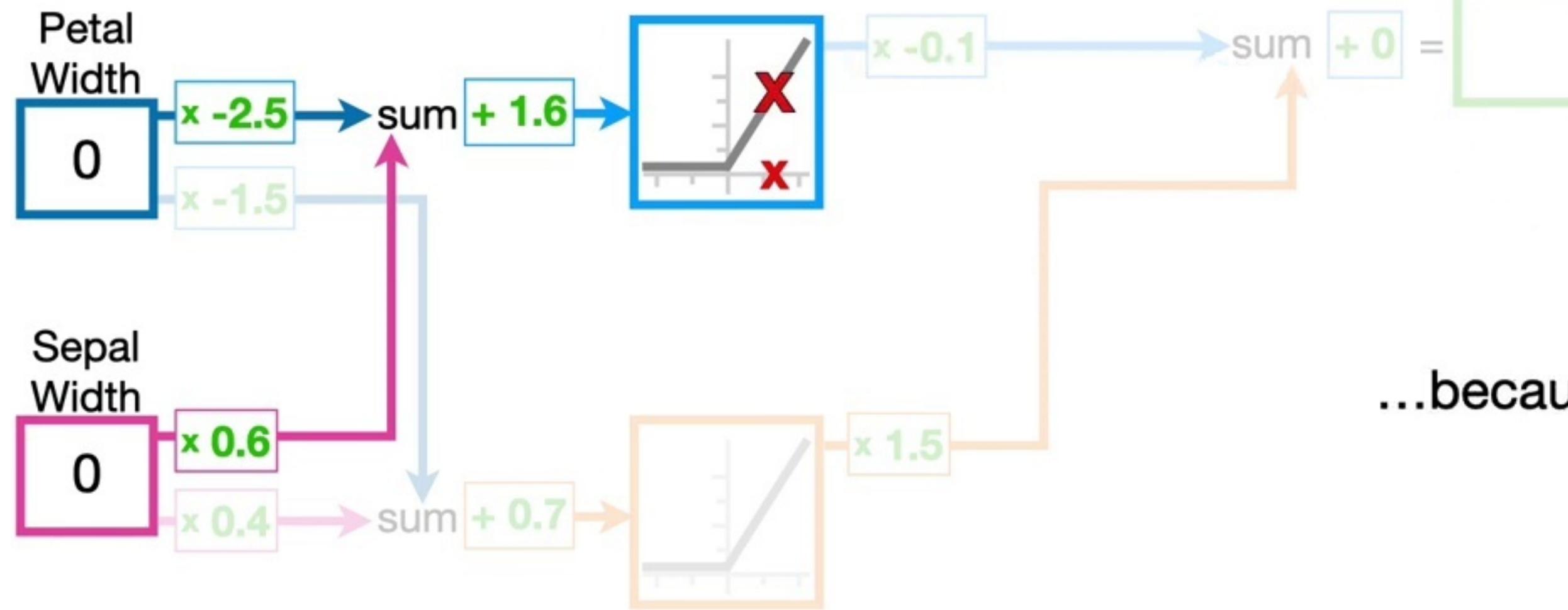
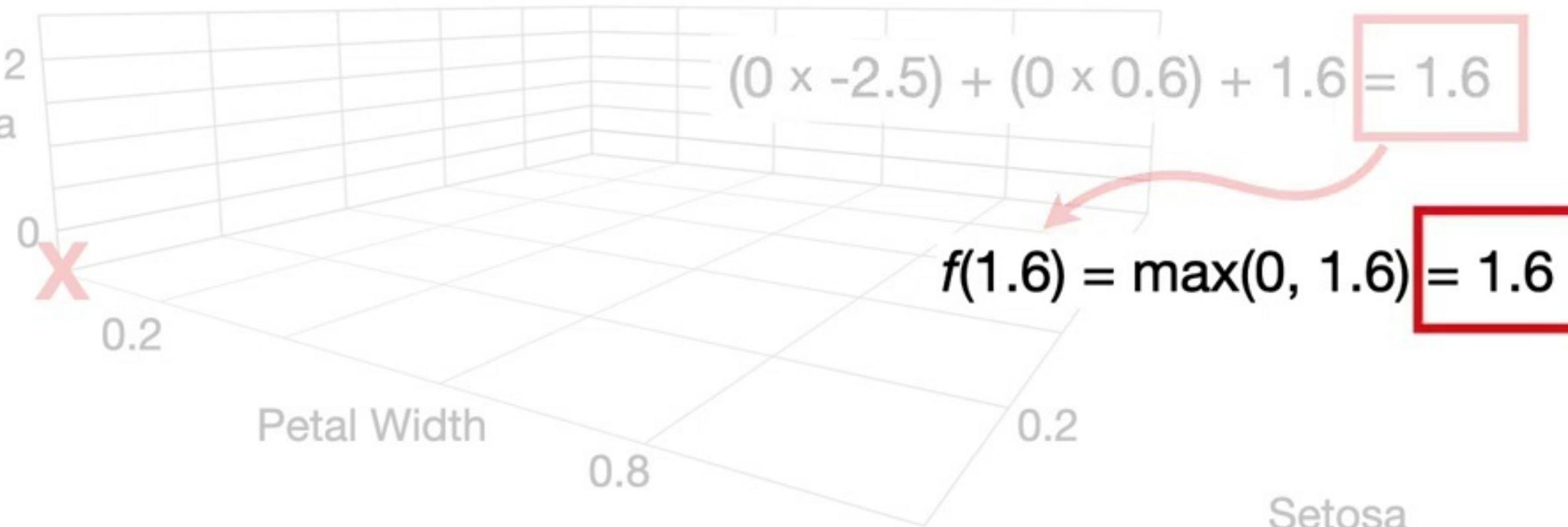


**SO! DOUBLE BAM!!!**

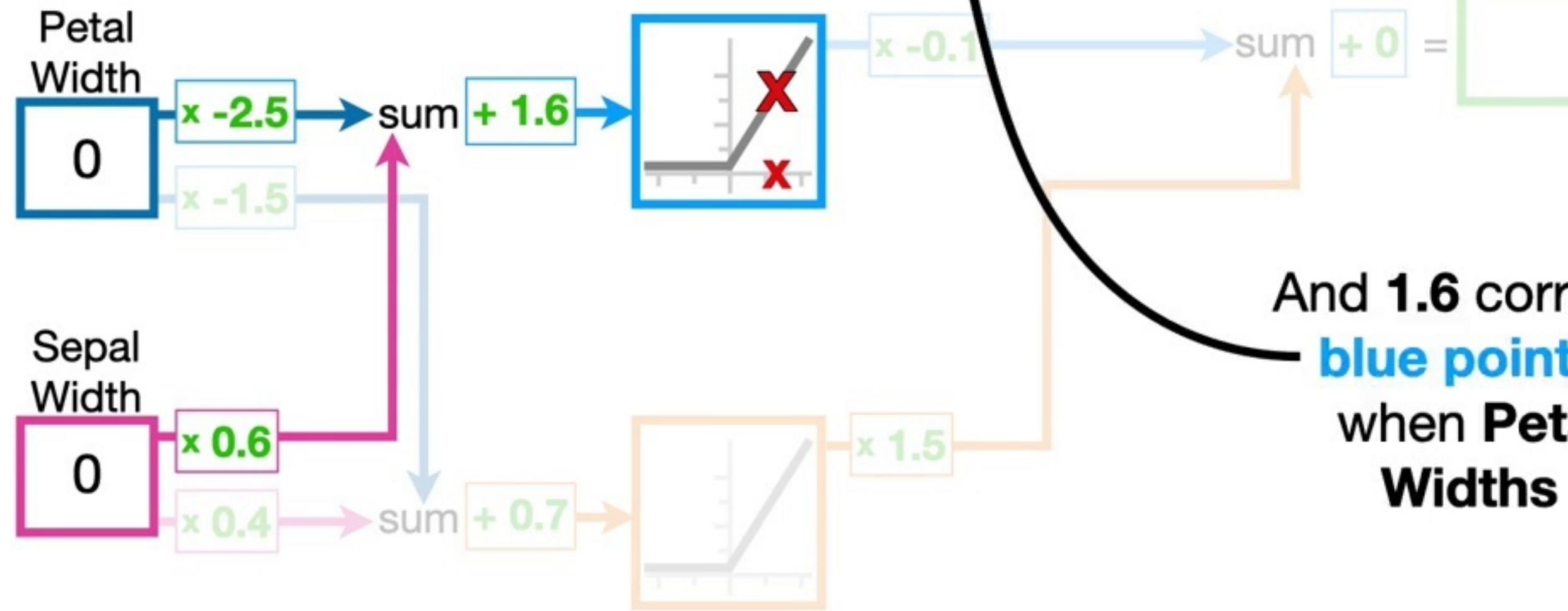
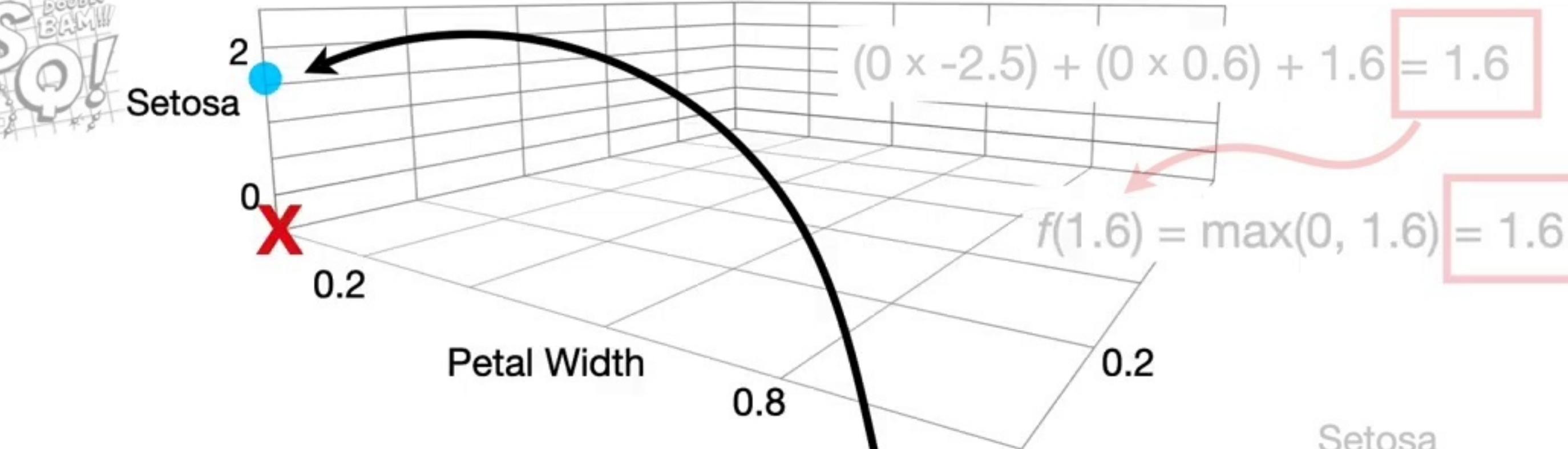


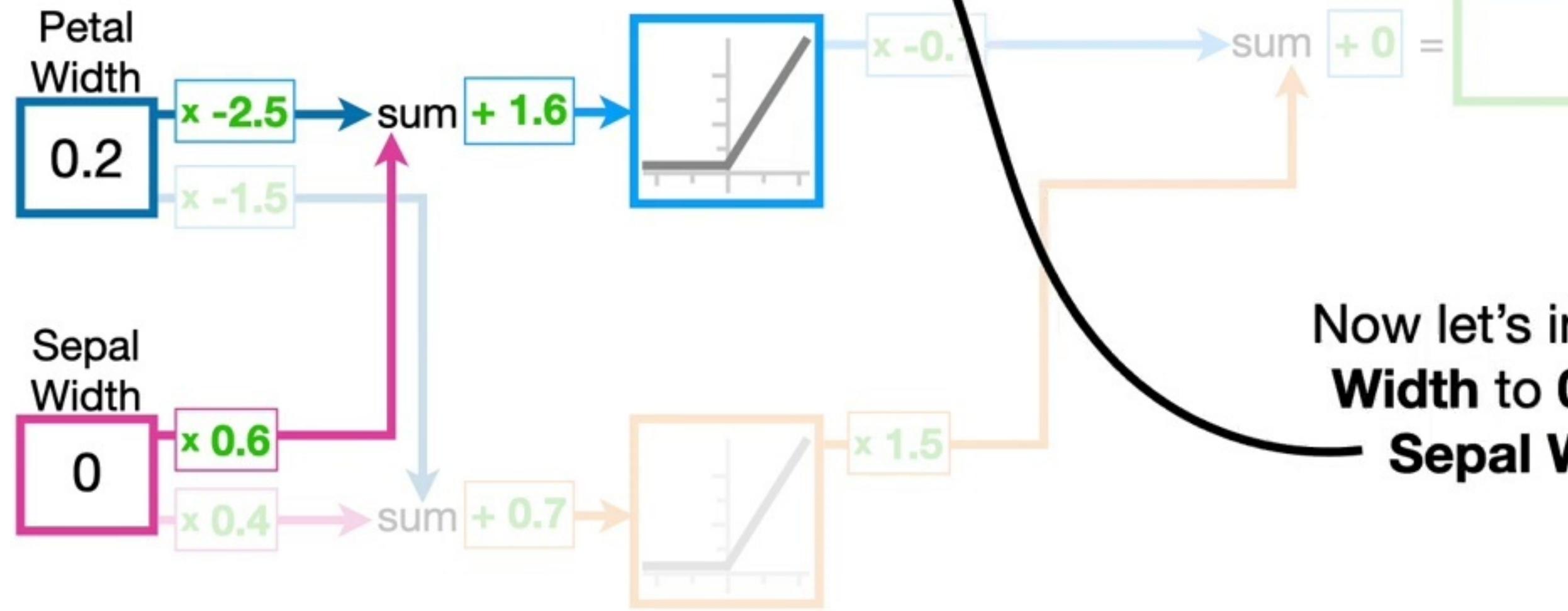
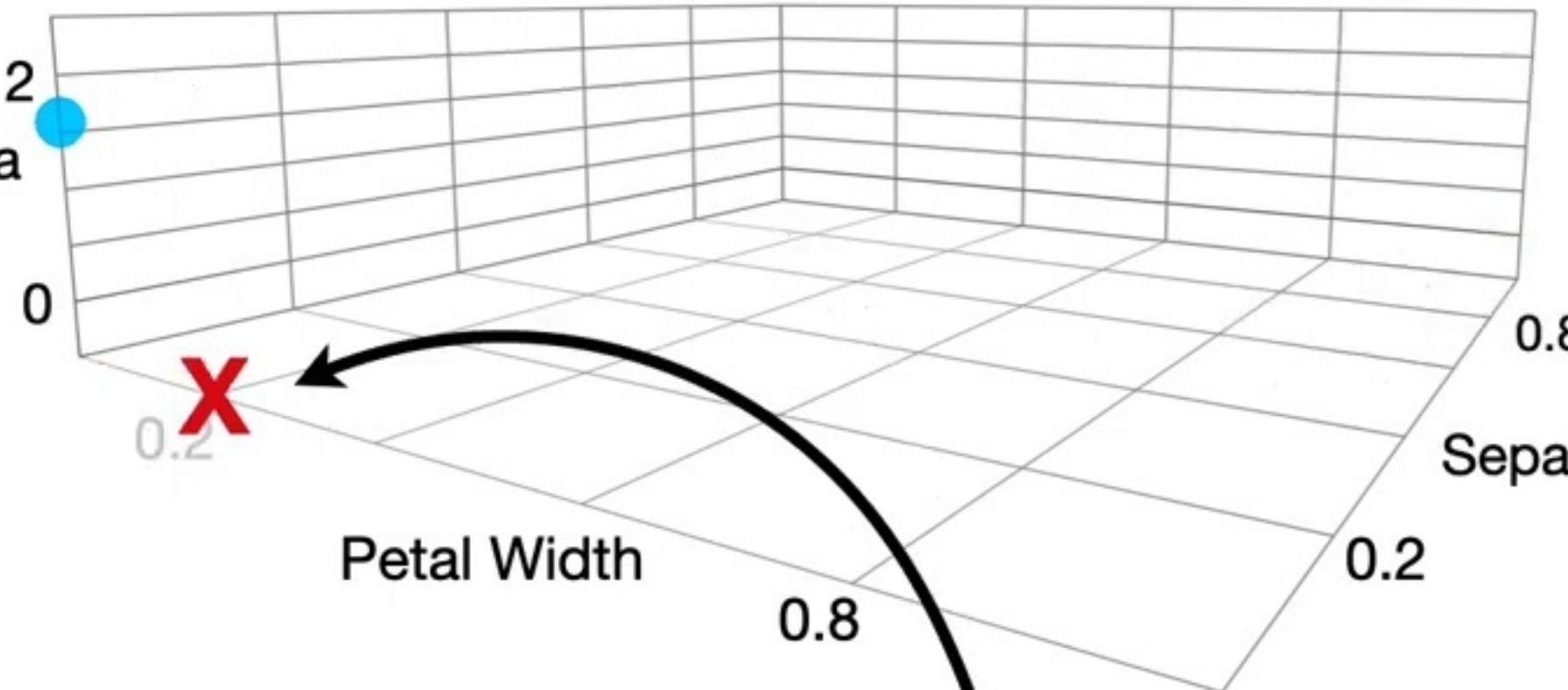
Now we plug 1.6 into the **ReLU Activation Function** to get the y-axis coordinate, 1.6...

double  
BAM!!  
**SQ!**

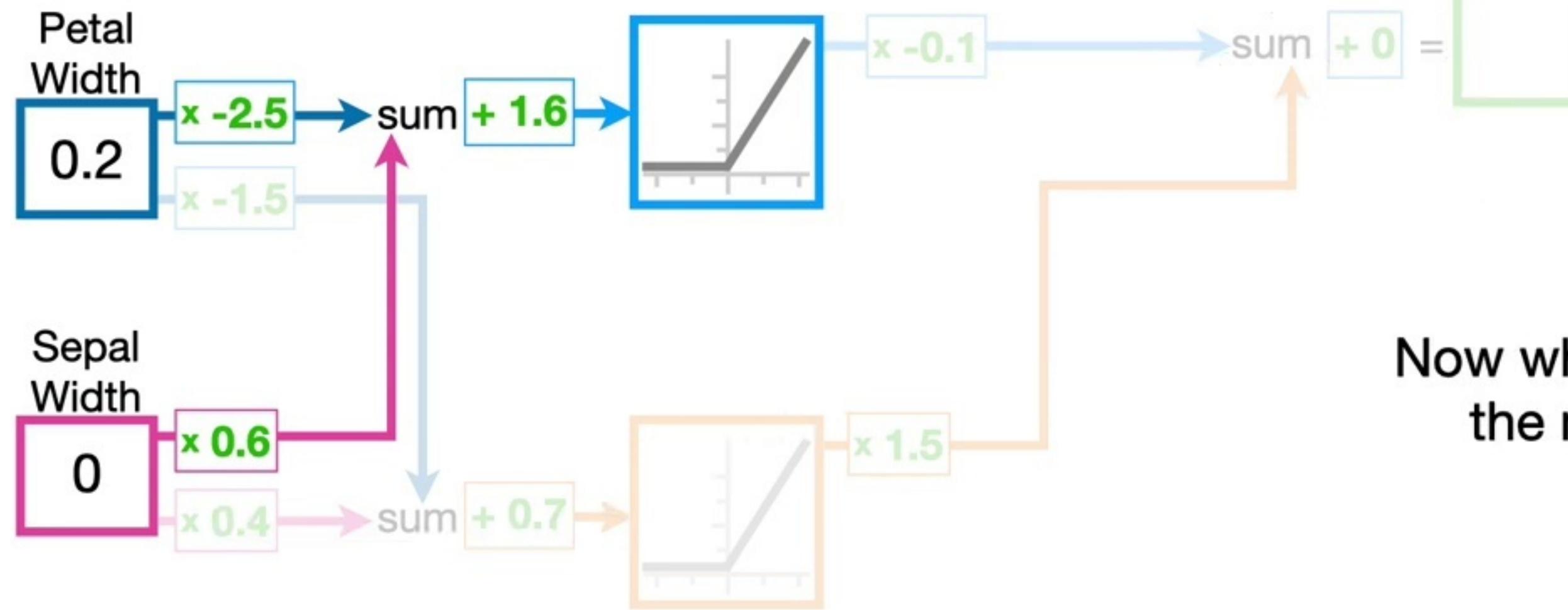
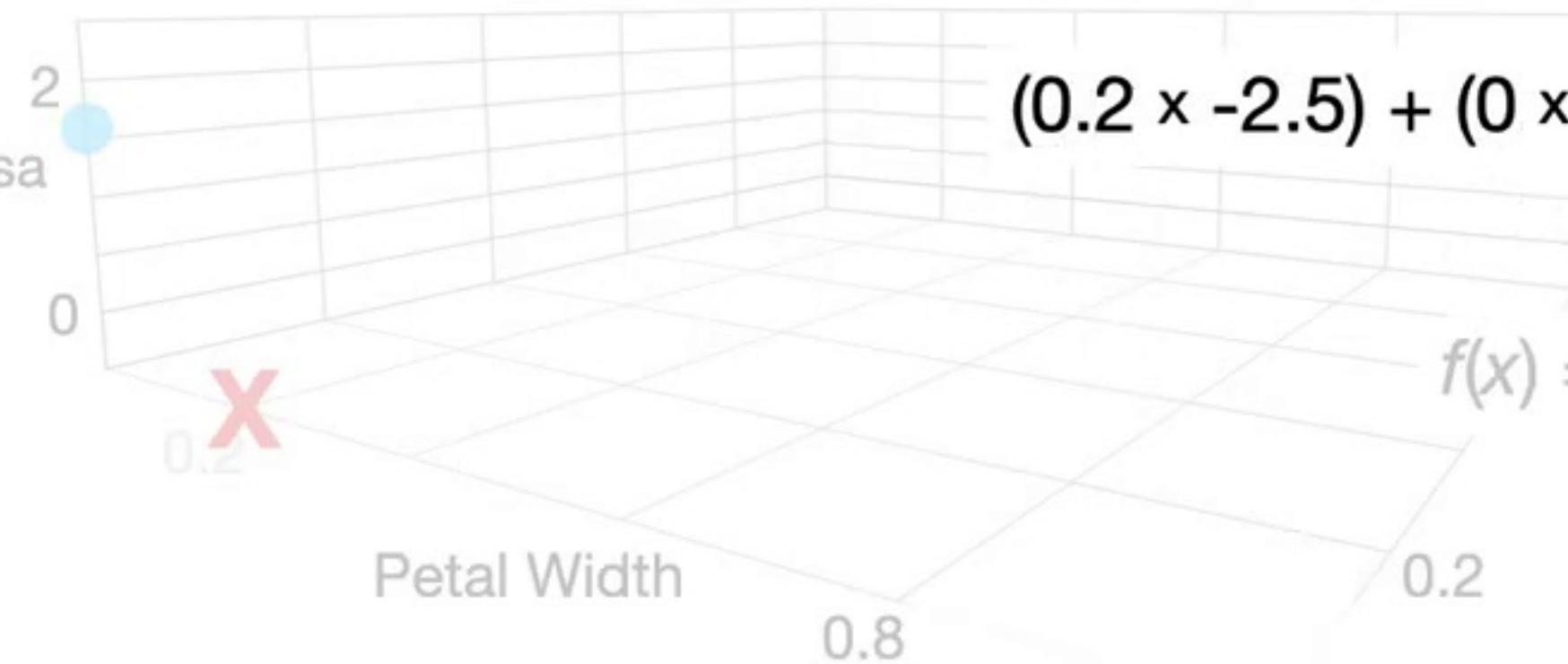


**SQ!**  
double  
BAM!!





double  
BAM!!  
**SQ!**



double  
BAM!!  
**SQ!**

2

0

X

Setosa

$$(0.2 \times -2.5) + (0 \times 0.6) + 1.6 = 1.1$$

$f(x) = \max(0, x) = y\text{-axis coordinate}$

Petal Width

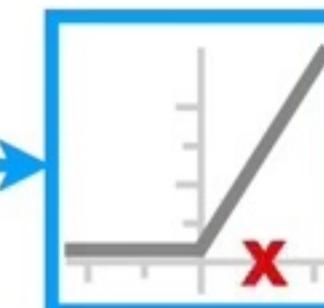
0.2

Petal Width  
0.2

x -2.5

x -1.5

+ 1.6



x -0.1

sum

+ 0

=

Setosa

Sepal Width

0

x 0.6

x 0.4

sum

+ 0.7

x 1.5

x 0.4

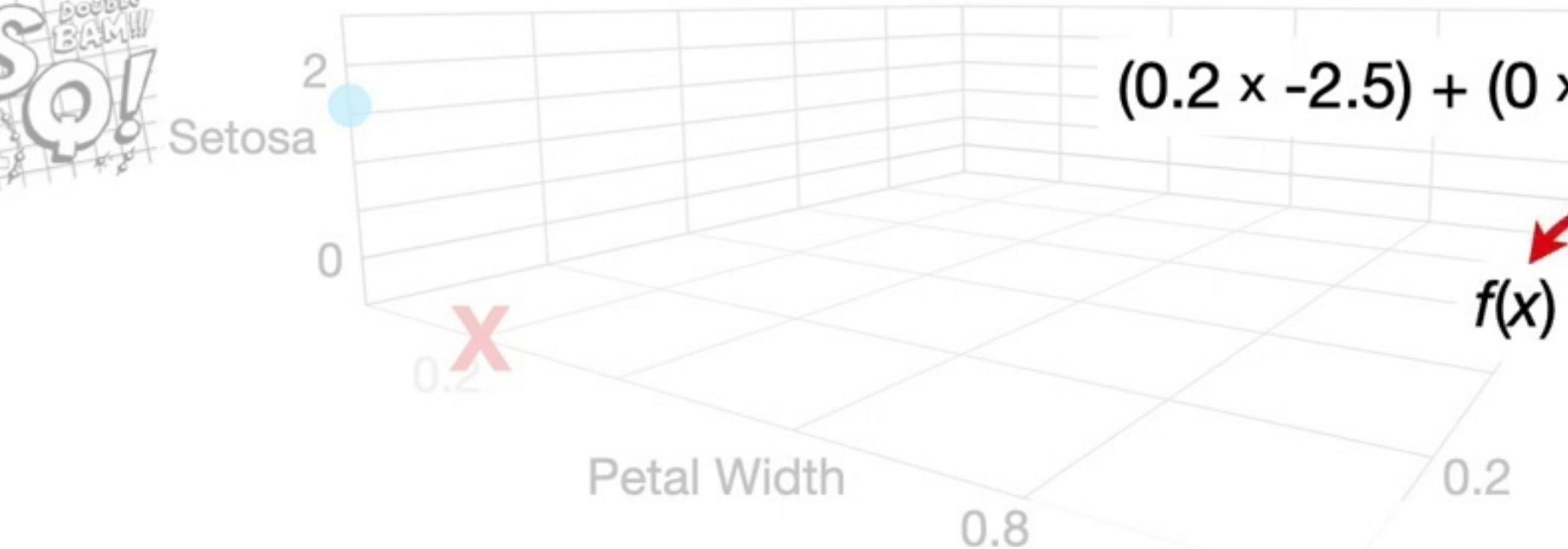
sum

+ 0.7



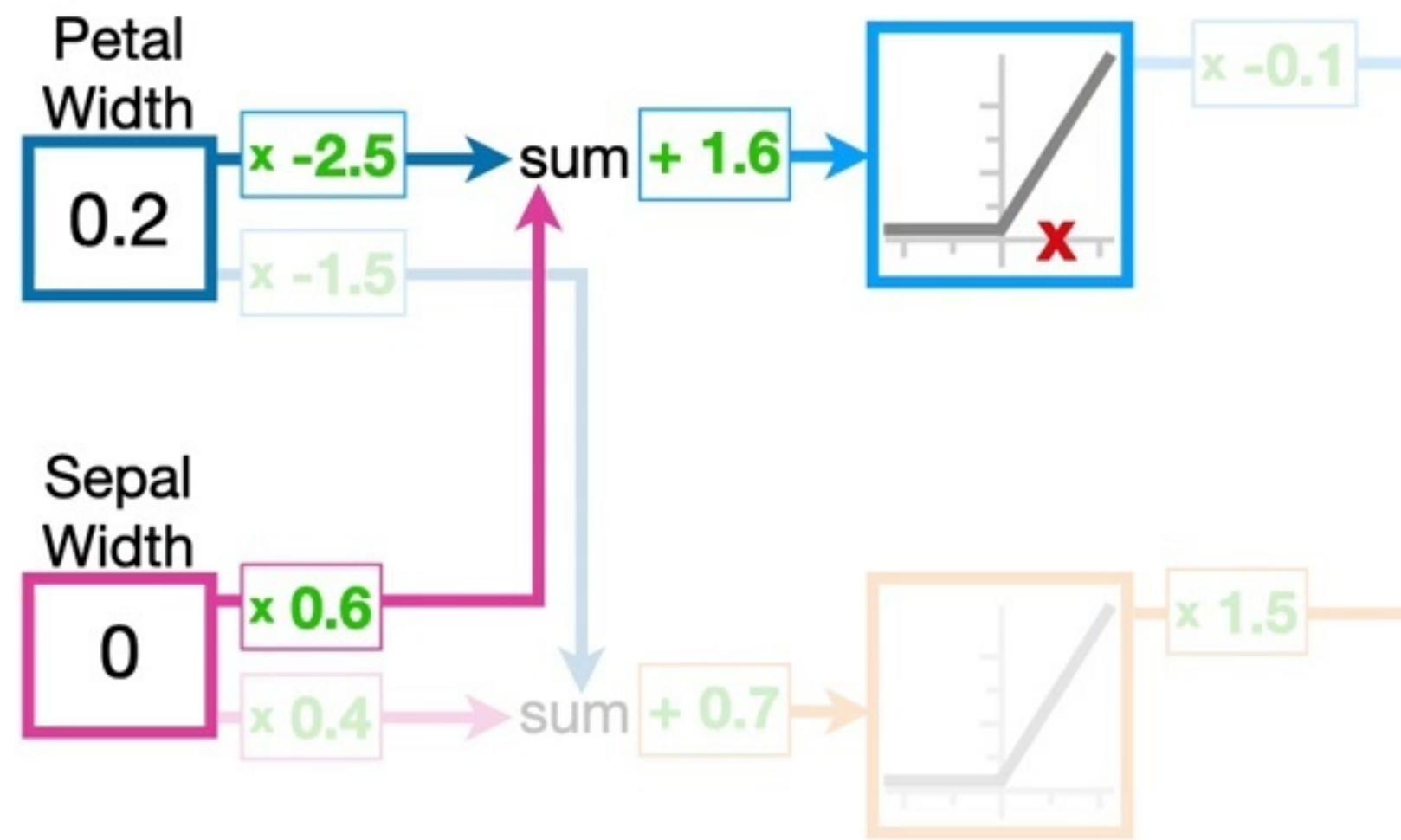
...we get 1.1 for the x-axis coordinate...

double  
BAM!!  
**SQ!**



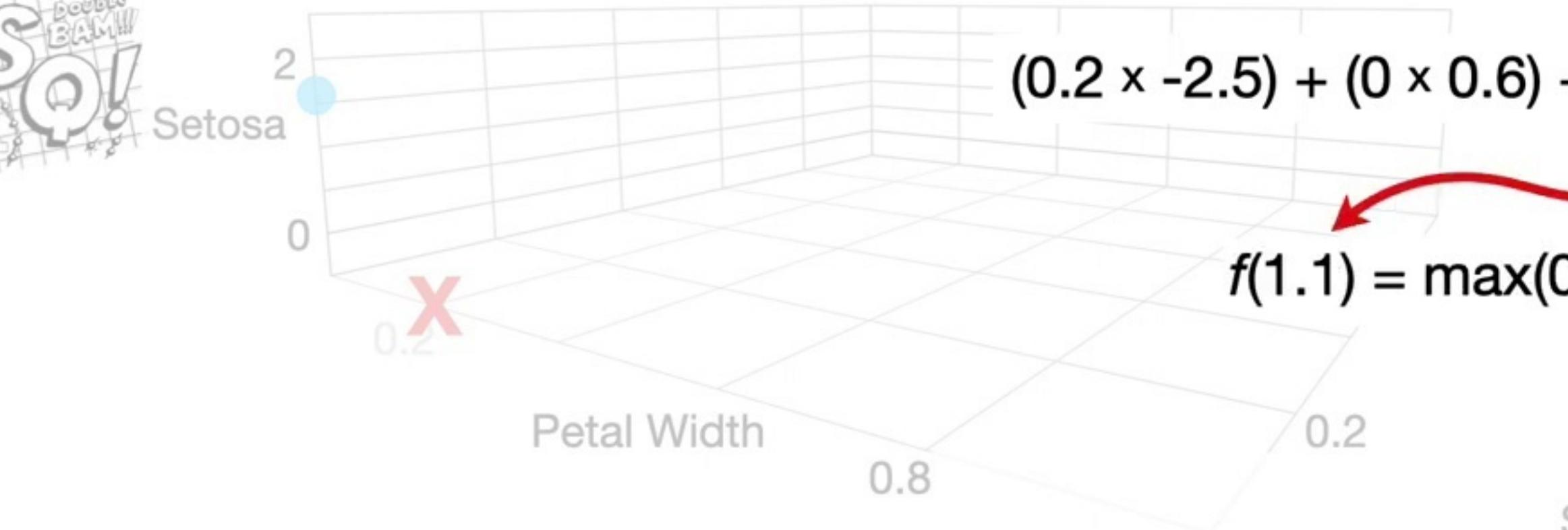
$$(0.2 \times -2.5) + (0 \times 0.6) + 1.6 = 1.1$$

$$f(x) = \max(0, x) = \text{y-axis coordinate}$$

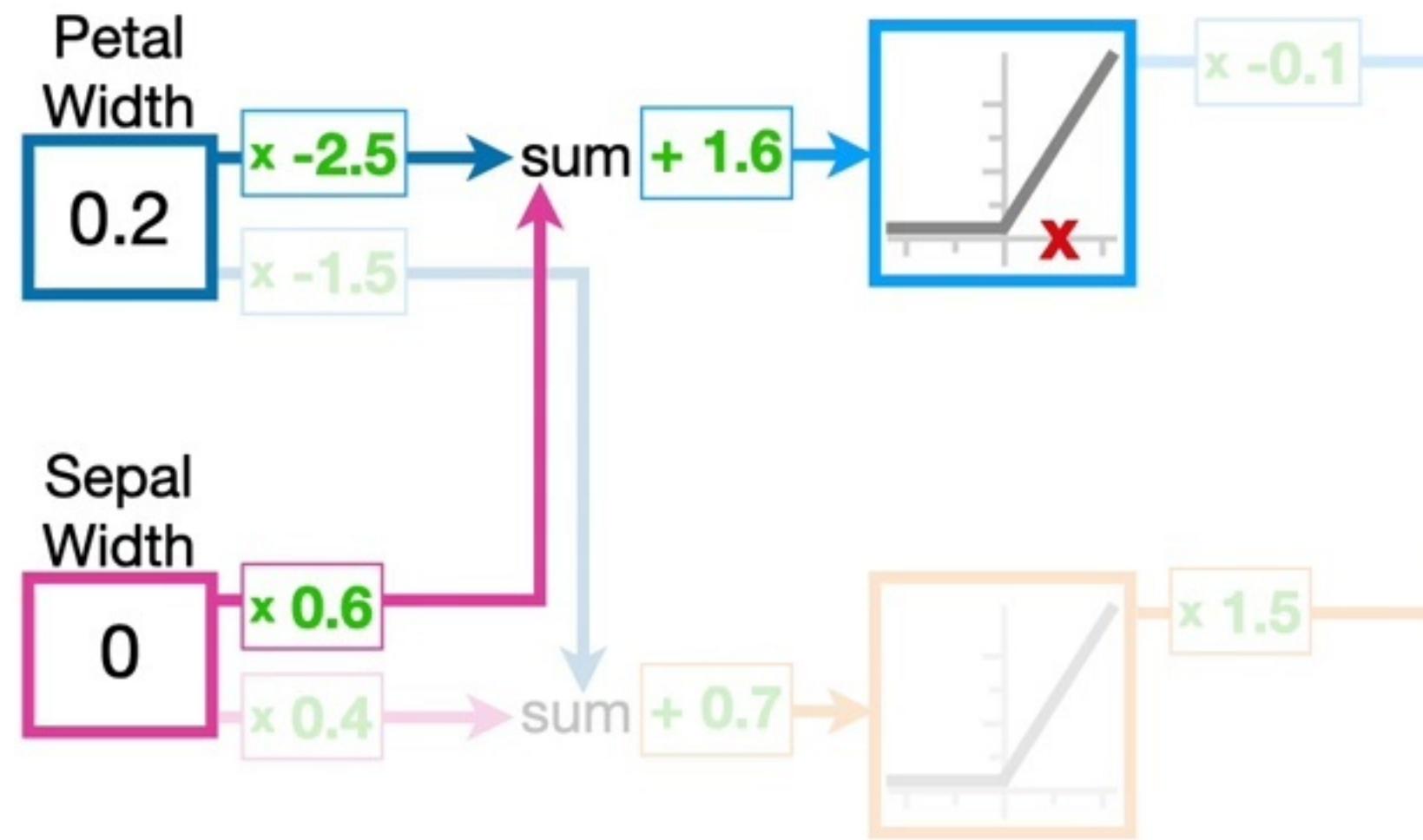


...and 1.1 for the y-axis coordinate.

double  
BAM!!  
**SQ!**



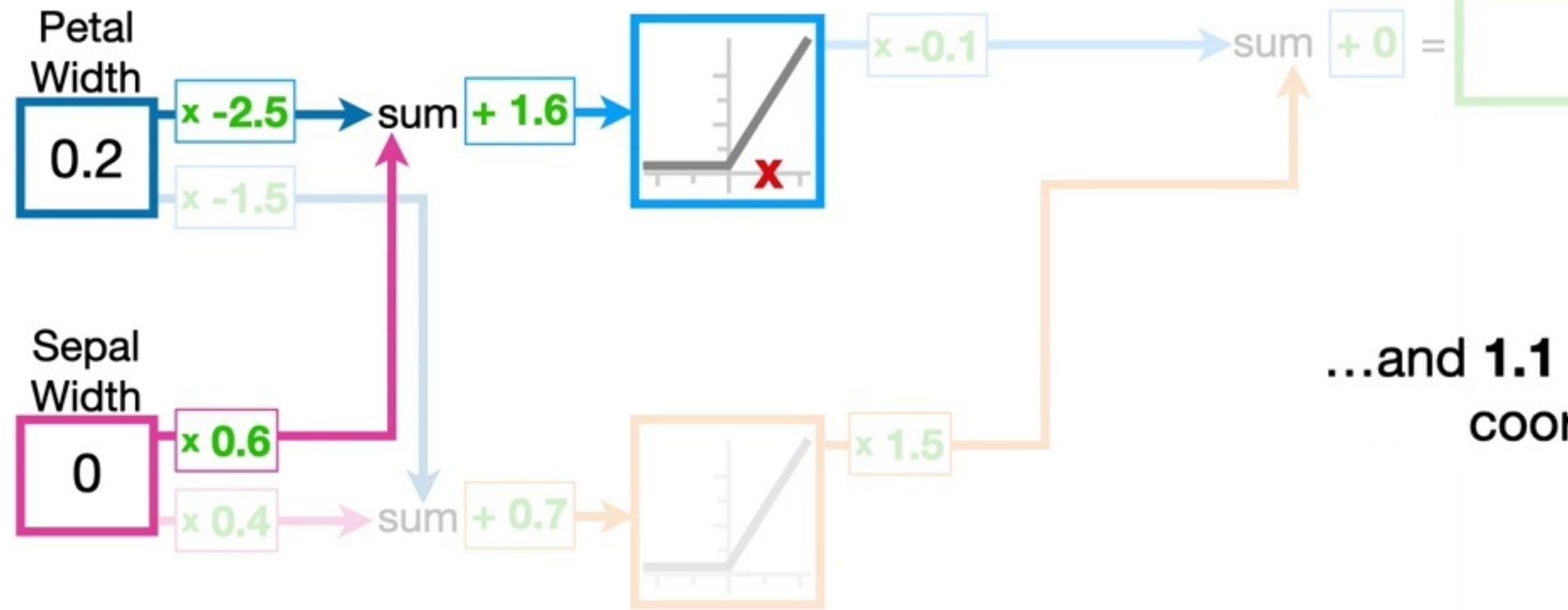
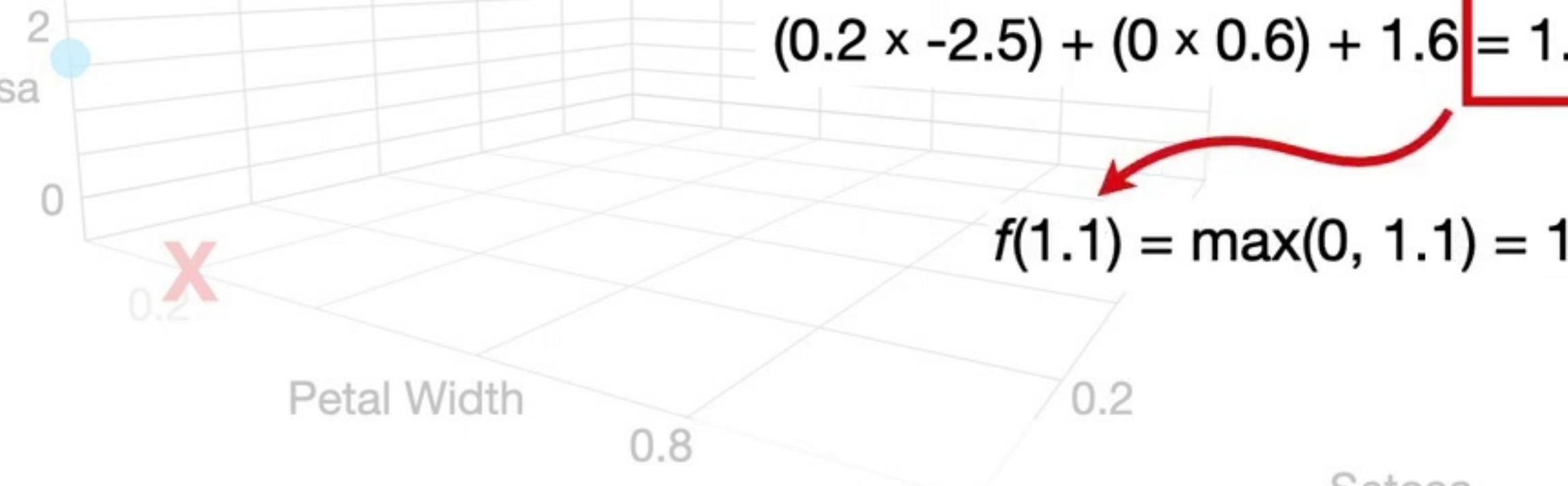
$$f(1.1) = \max(0, 1.1) = \text{y-axis coordinate}$$



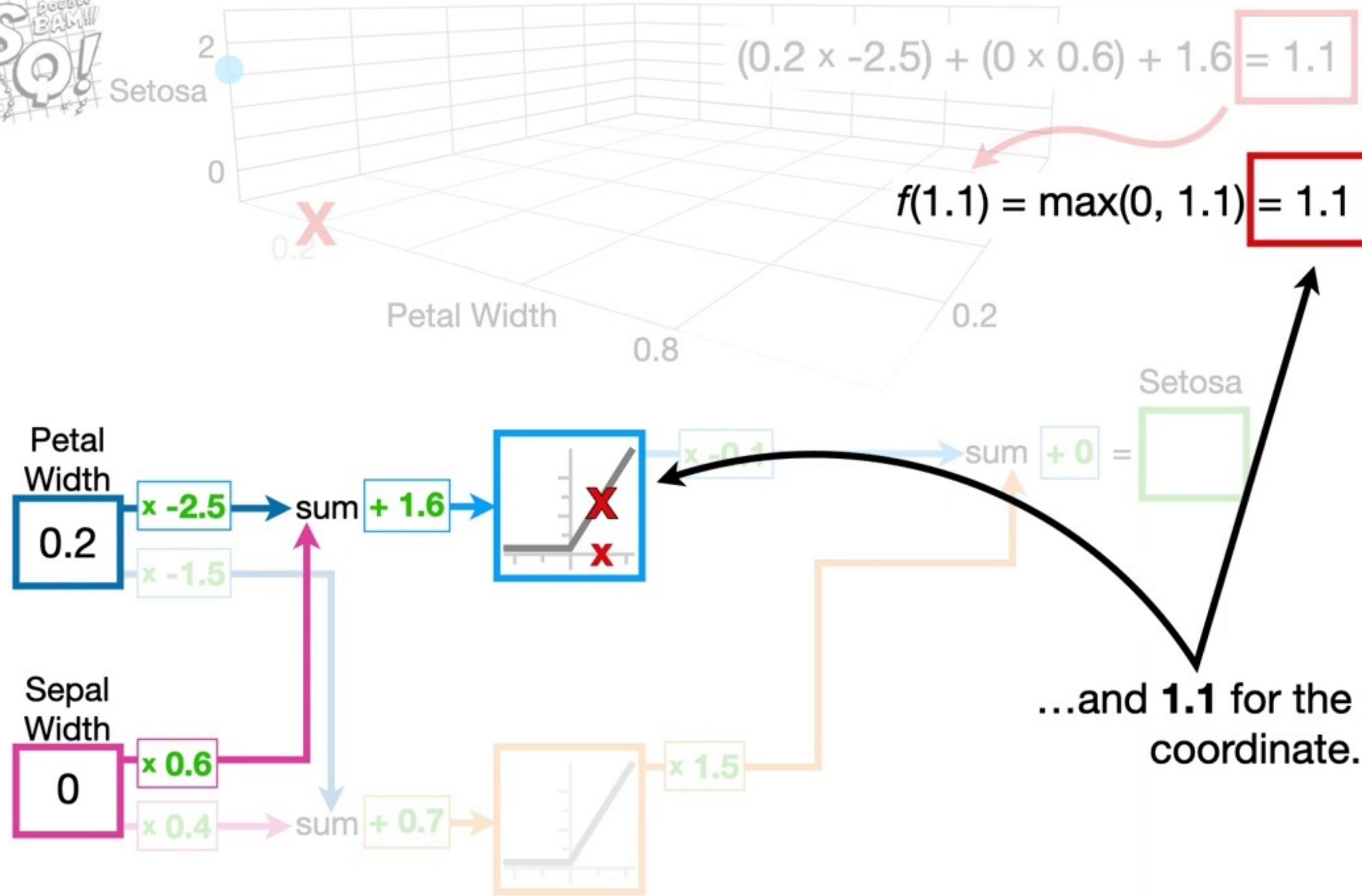
Setosa  
 + 0 =

...and 1.1 for the y-axis coordinate.

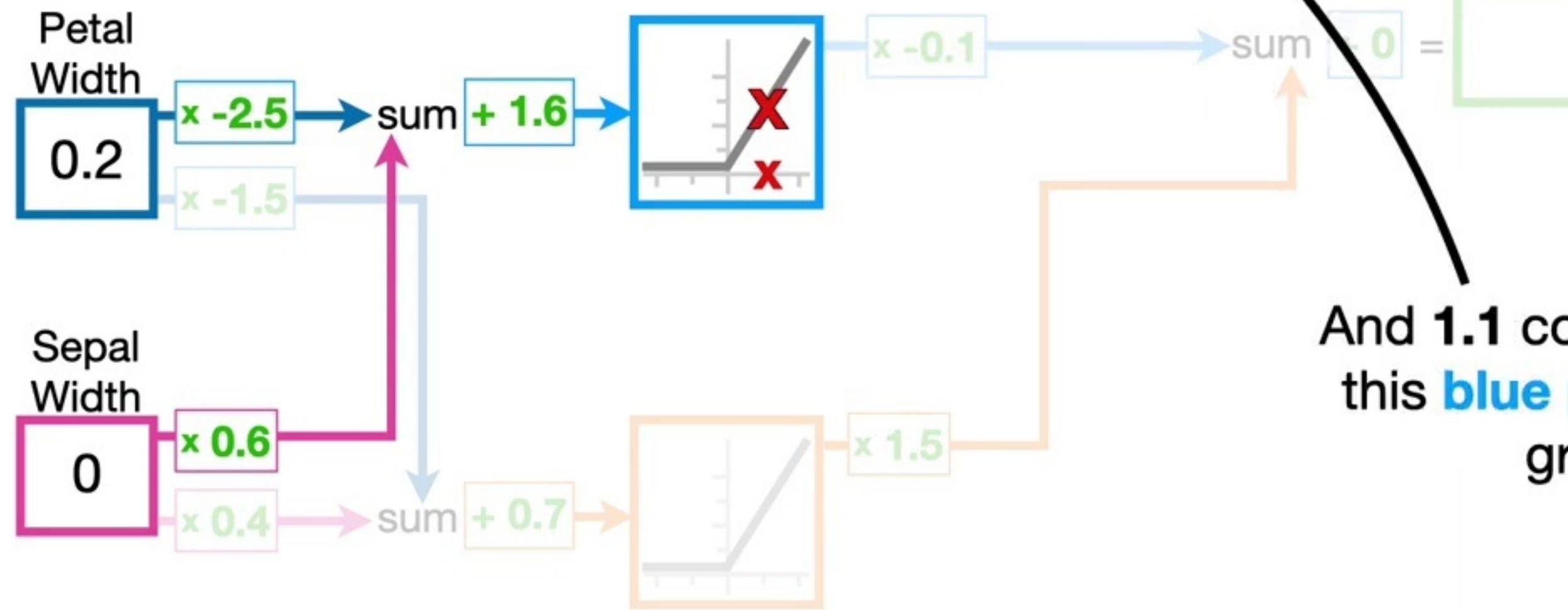
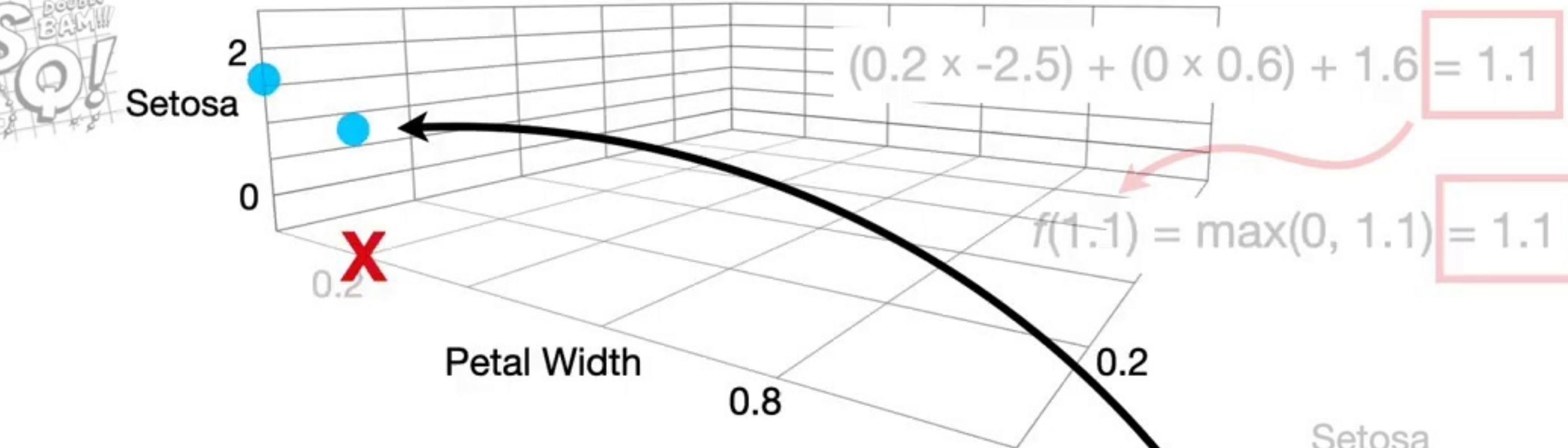
double  
BAM!!  
**SQ!**



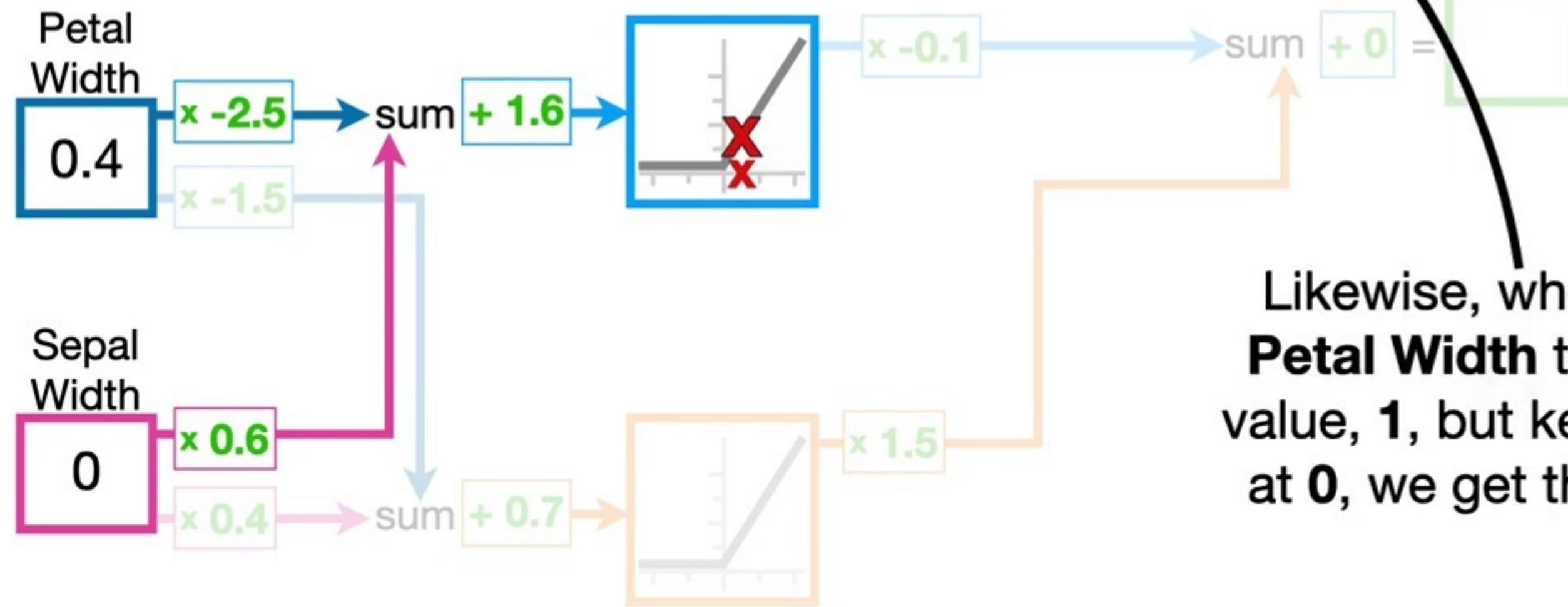
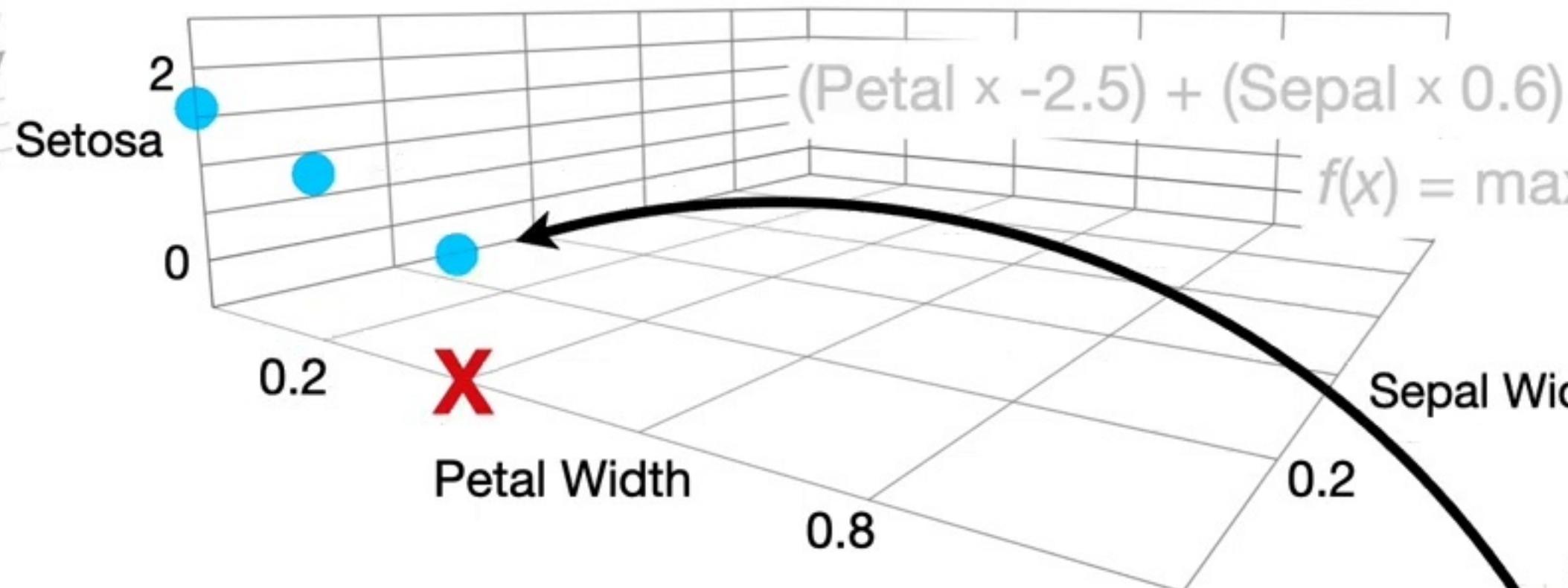
double  
BAM!!  
**SQ!**



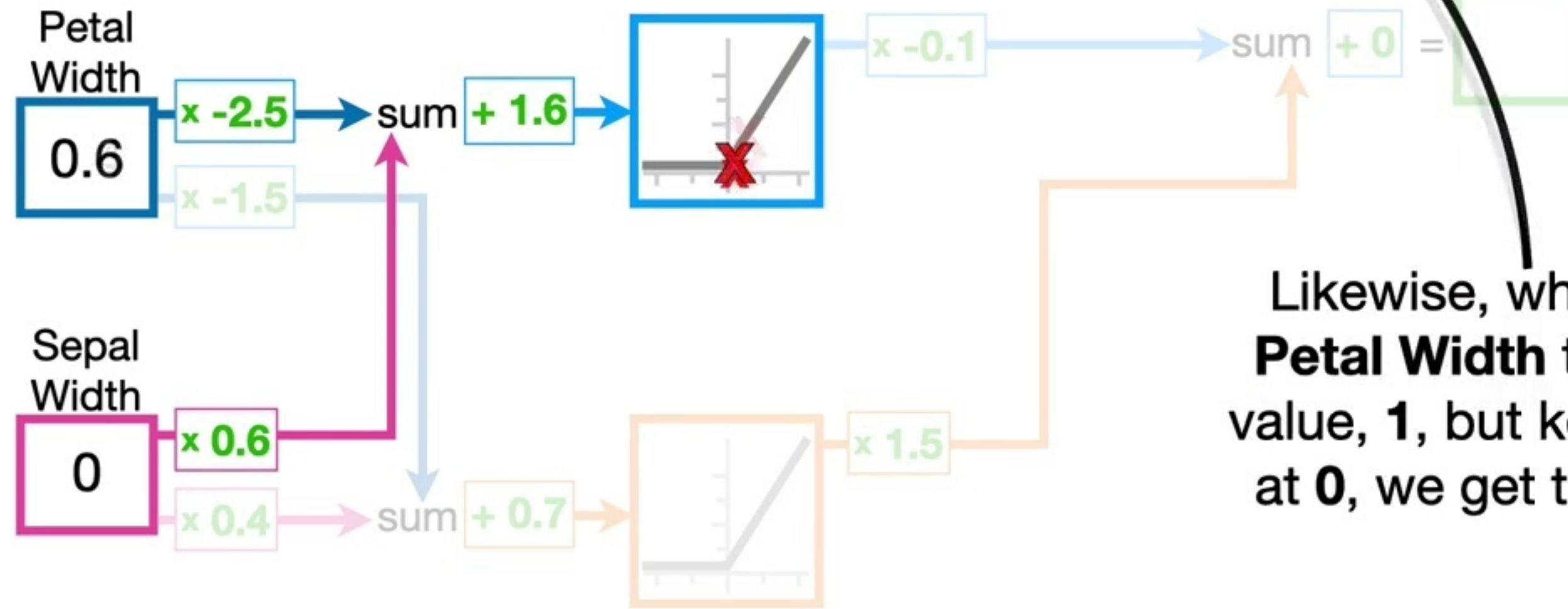
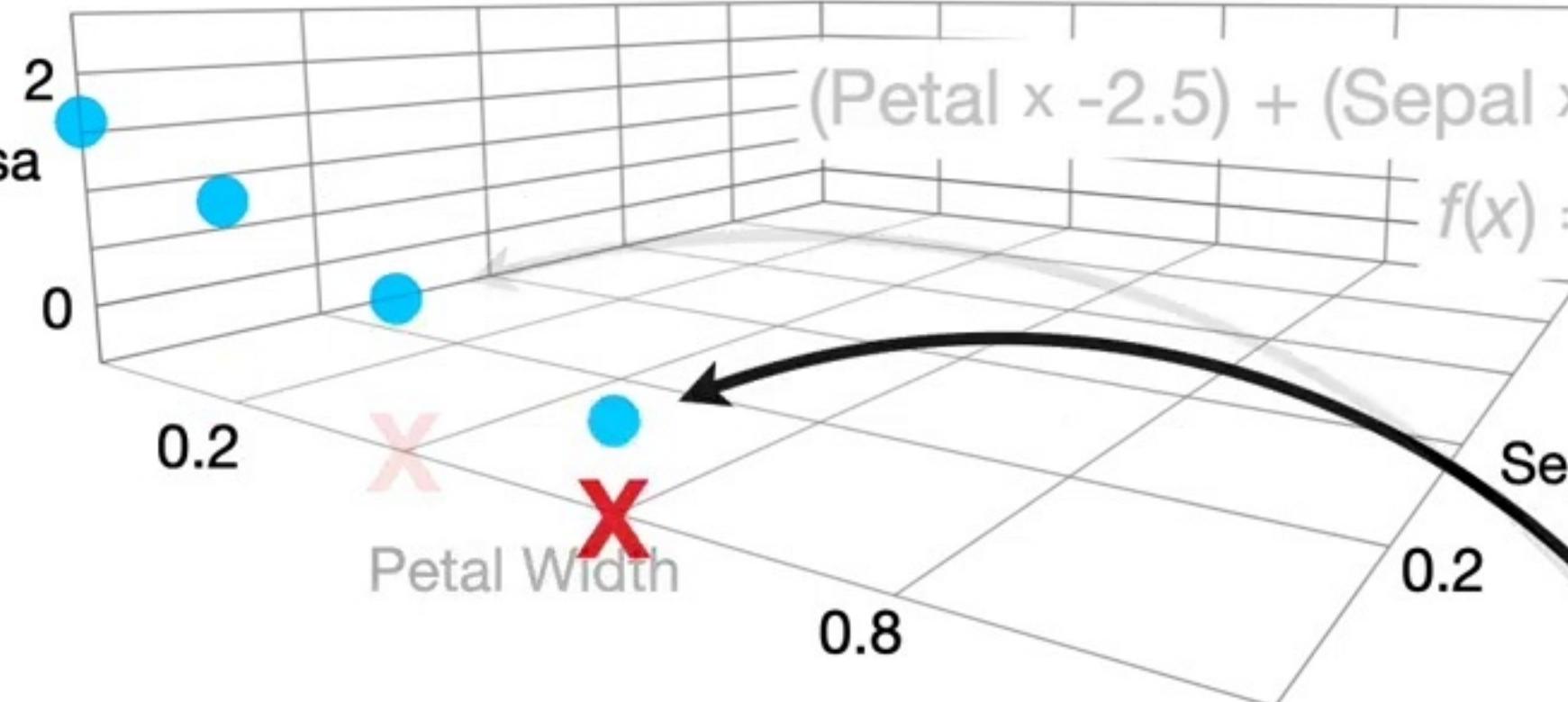
**SQ!**  
double  
BAM!!



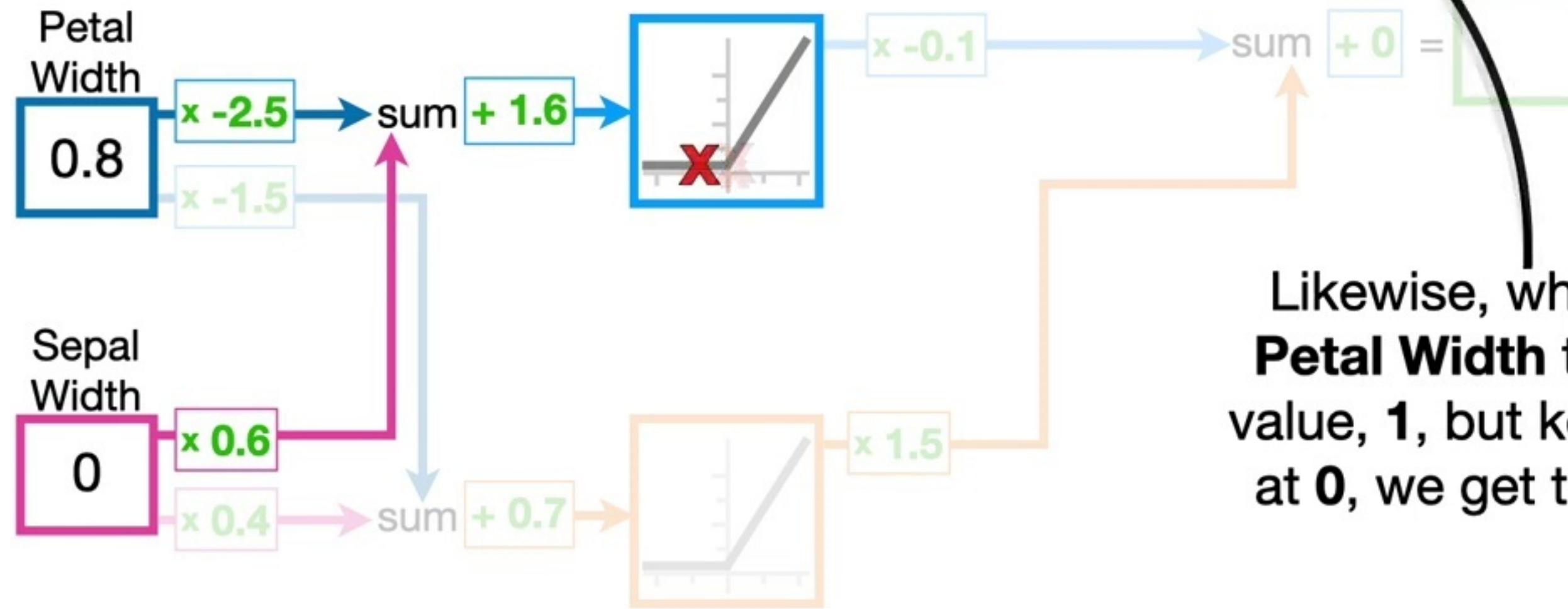
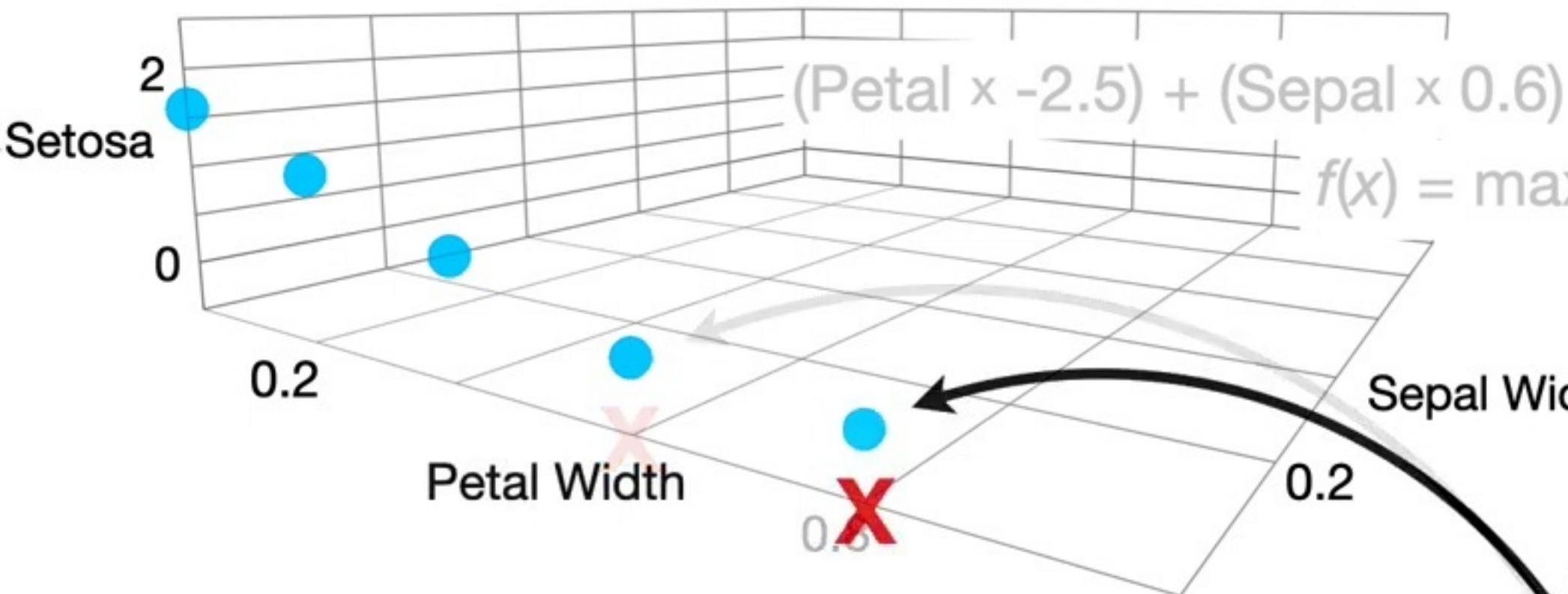
**SQ!**  
double  
BAM!!



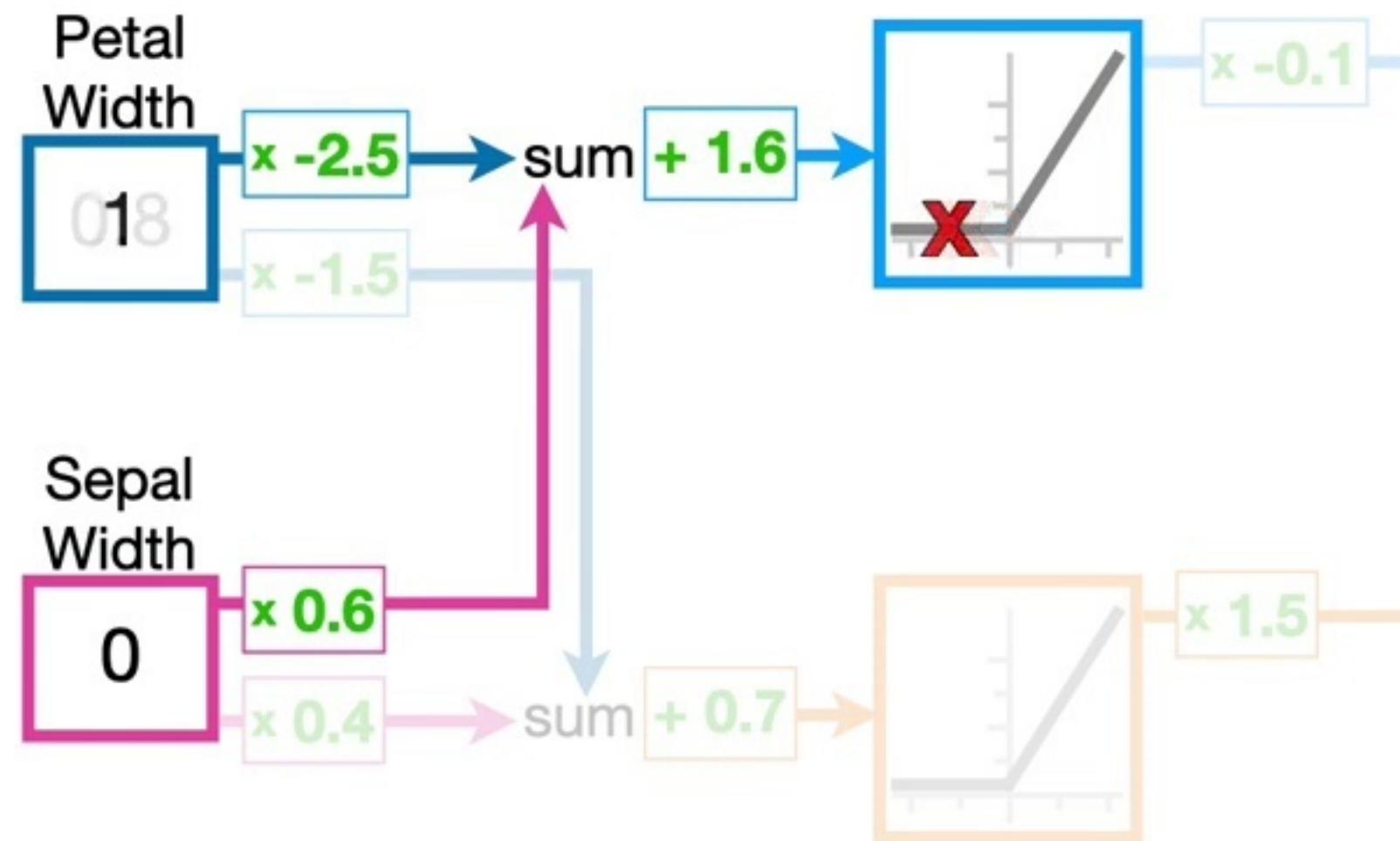
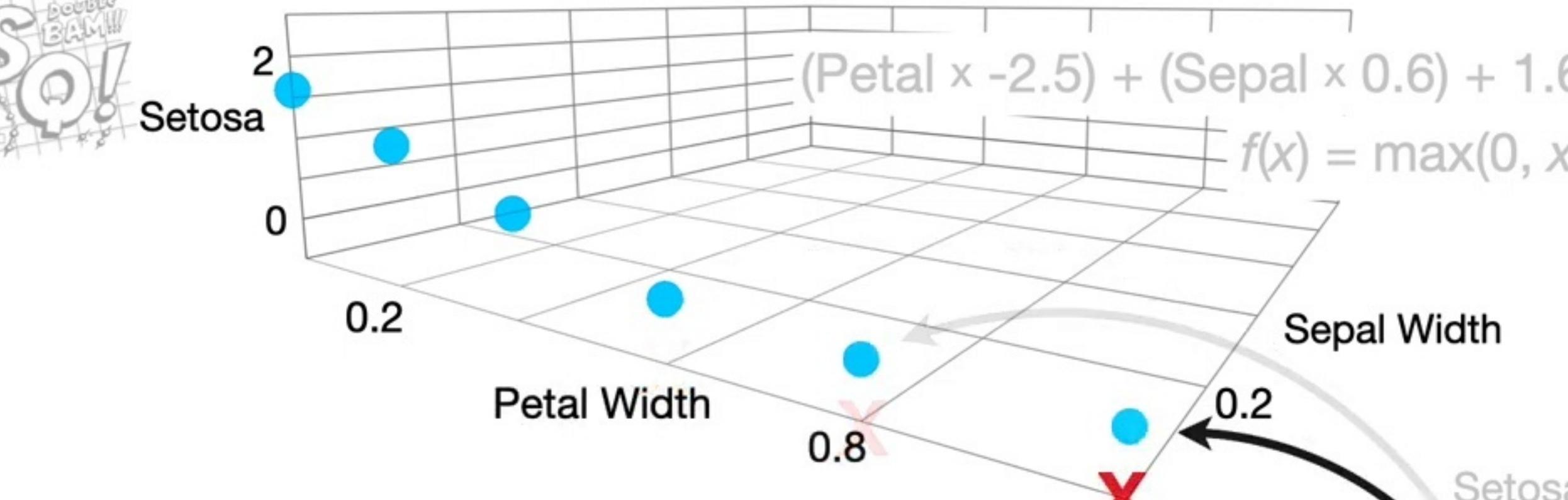
**SQ!**  
double  
BAM!!



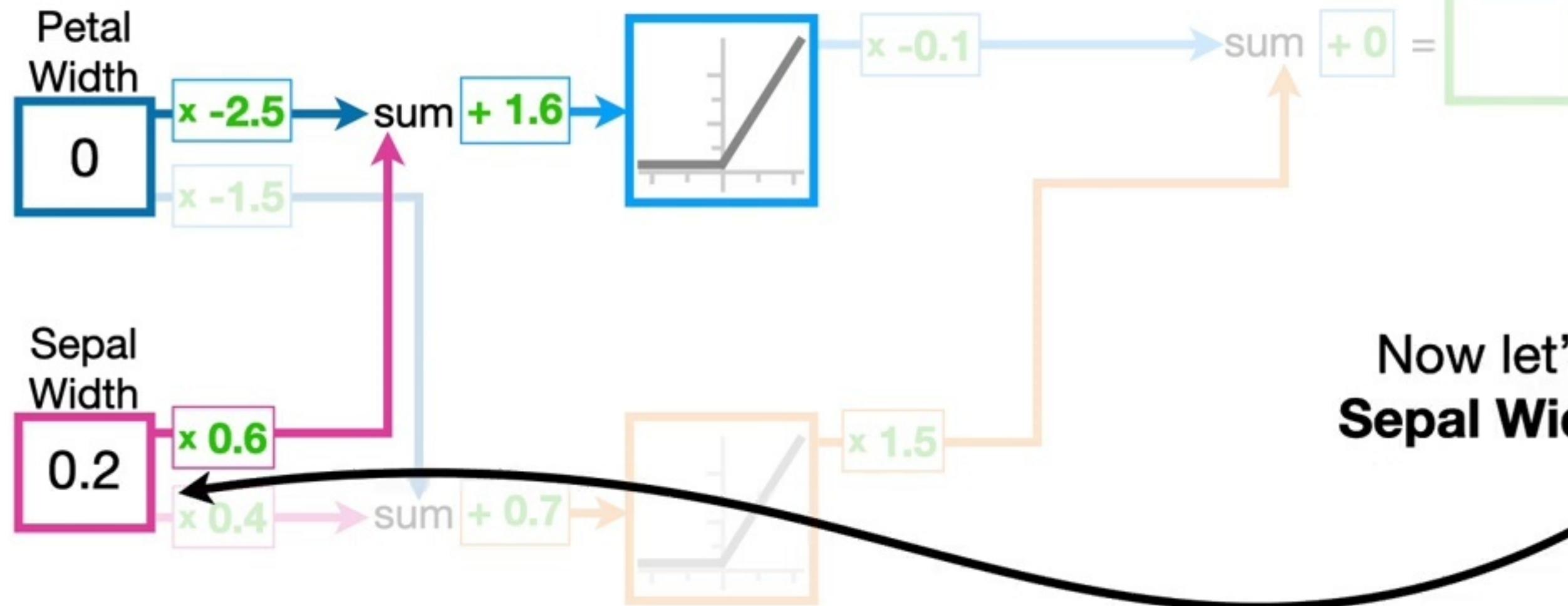
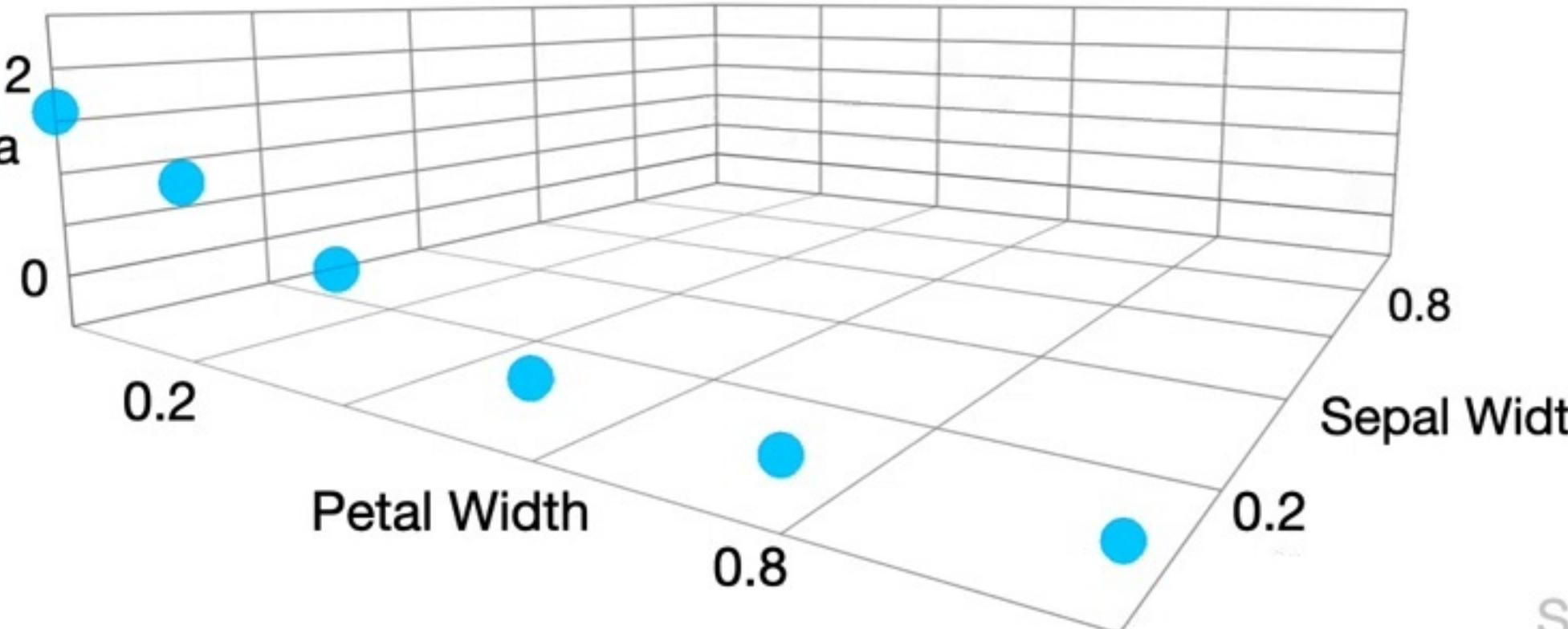
**SQ!**  
double  
BAM!!



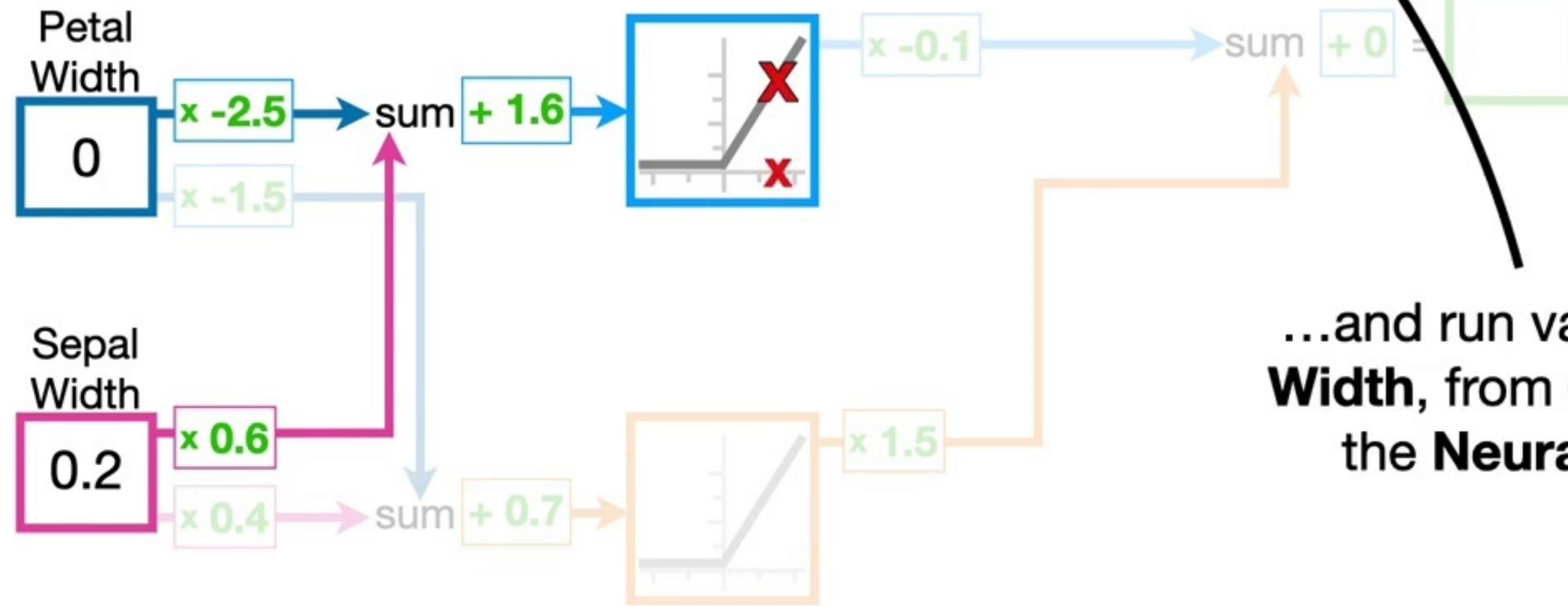
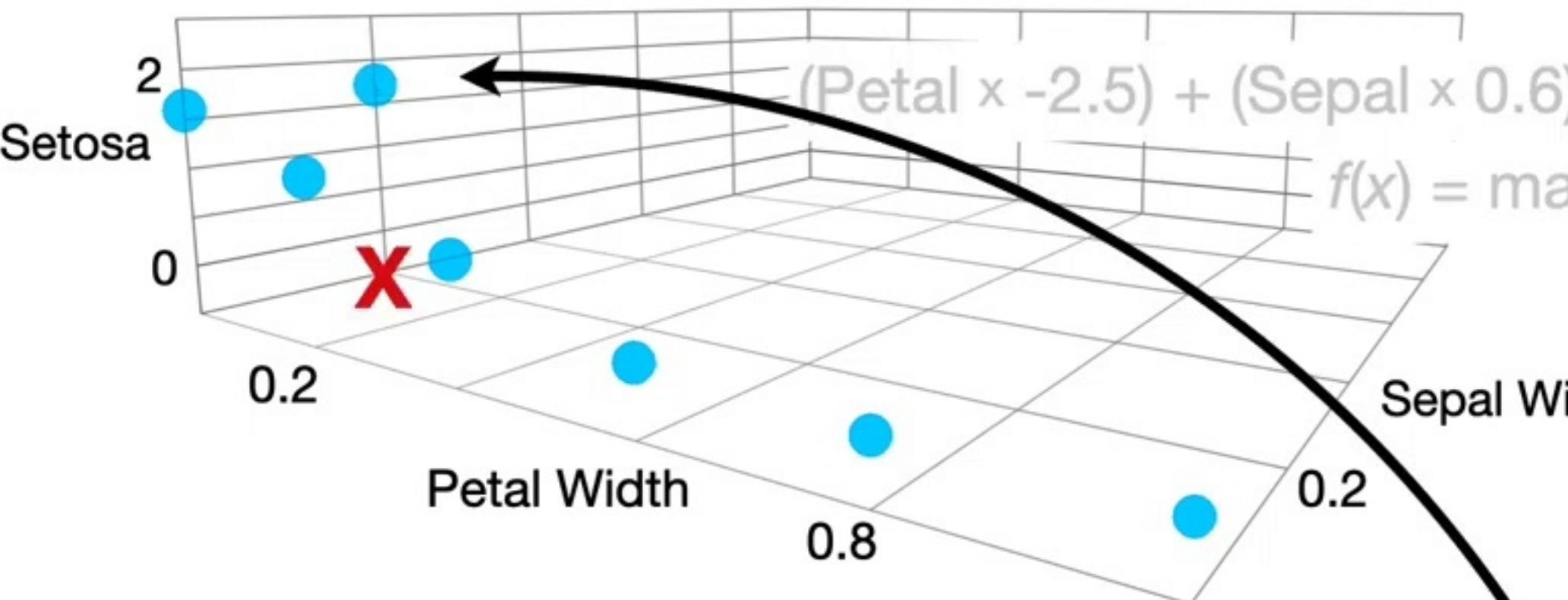
**SQ!**  
double  
BAM!!



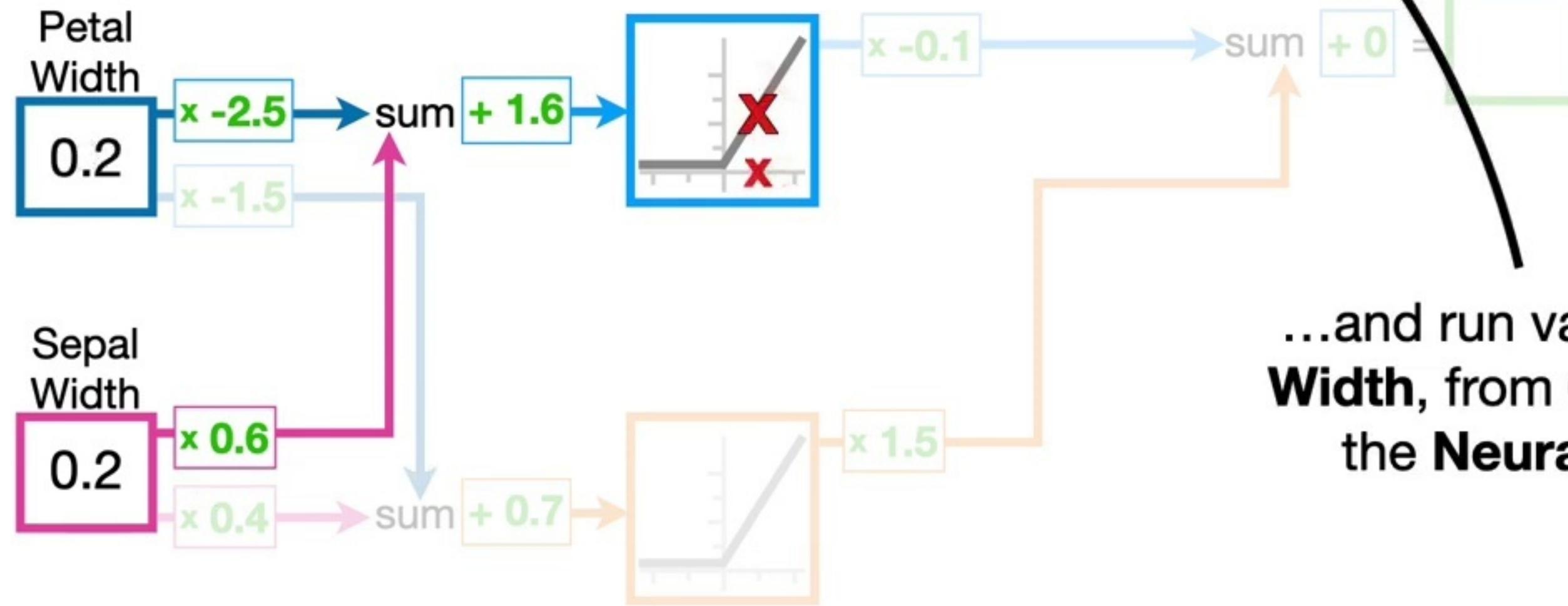
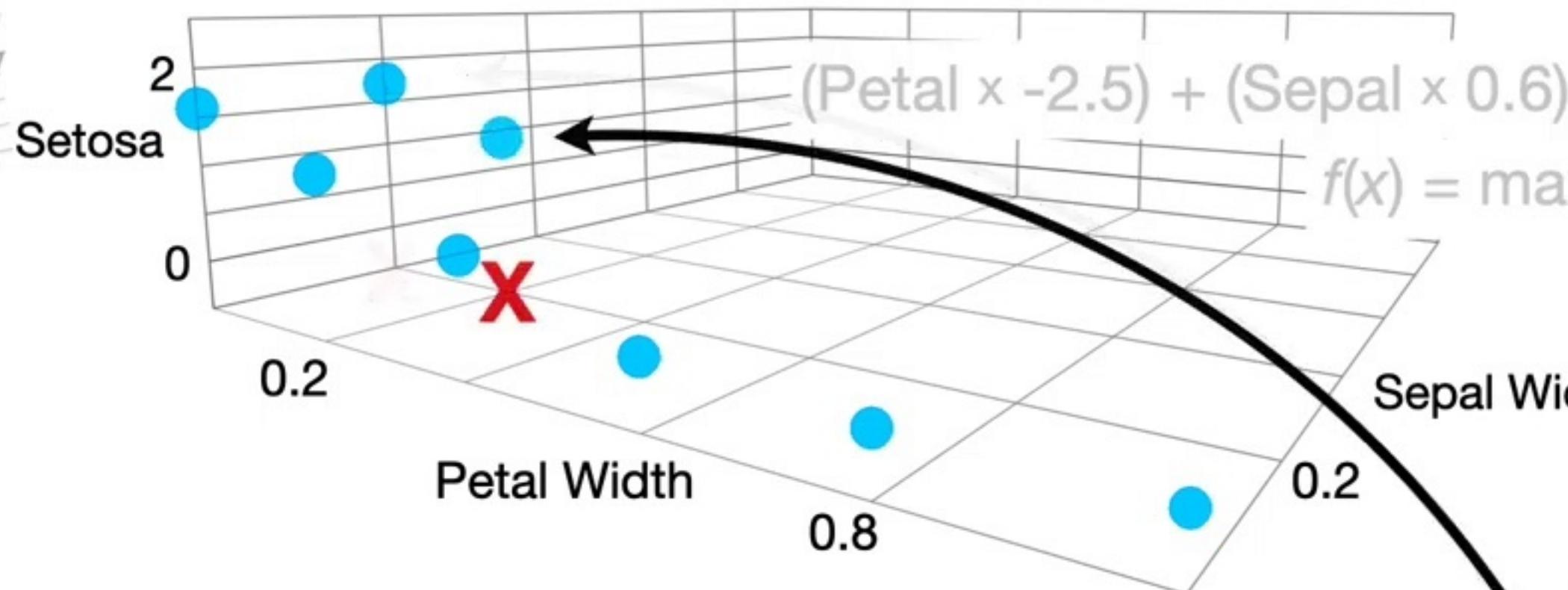
Likewise, when we increase **Petal Width** to the maximum value, 1, but keep **Sepal Width** at 0, we get these **blue dots**.



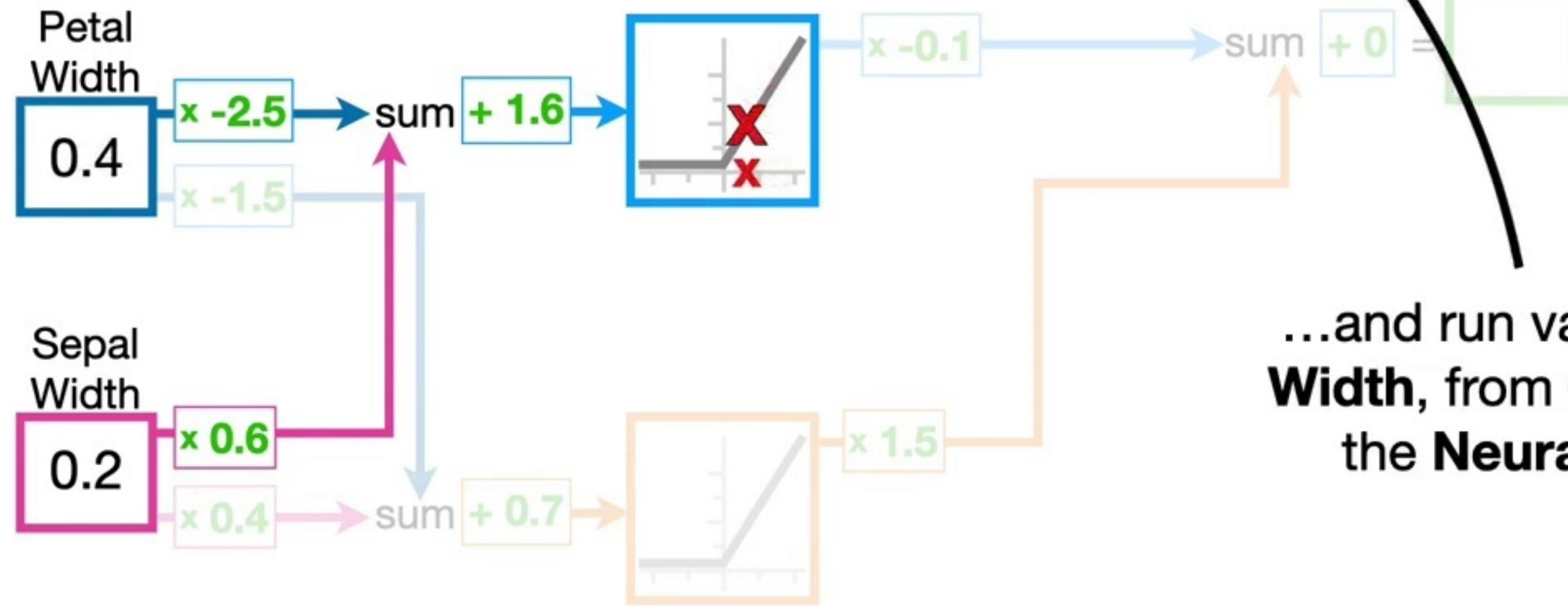
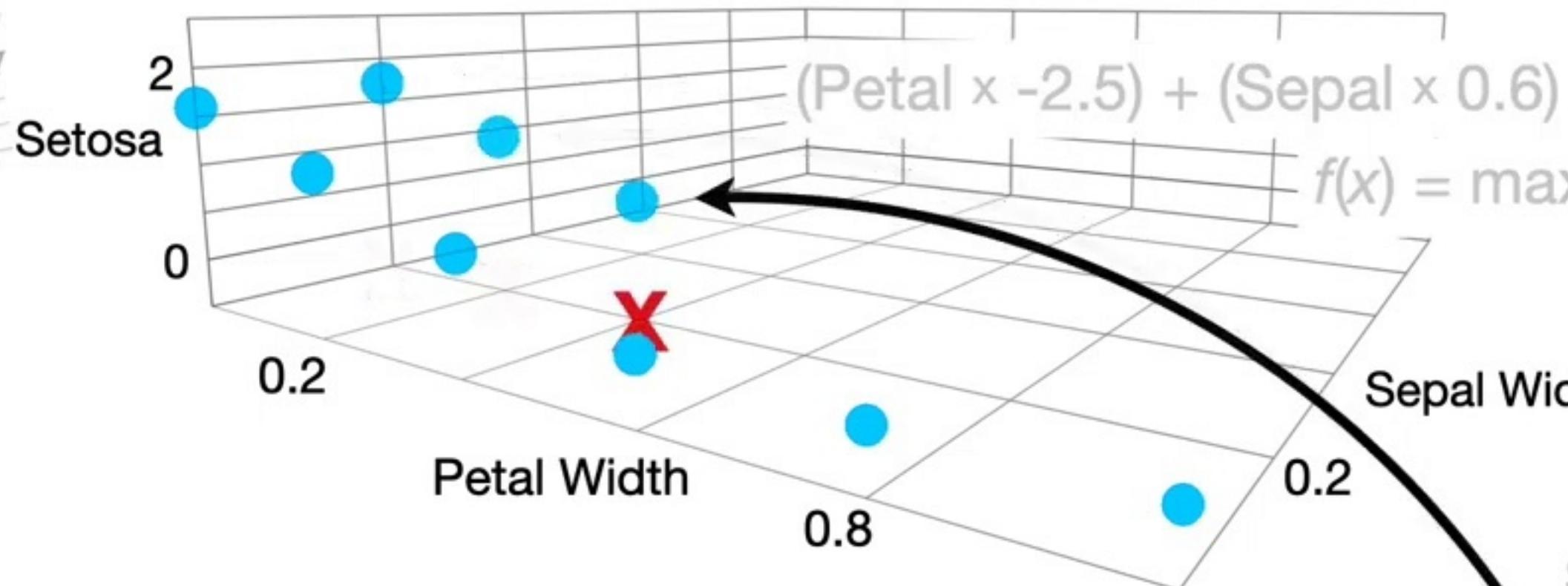
double  
BAM!!  
**SQ!**



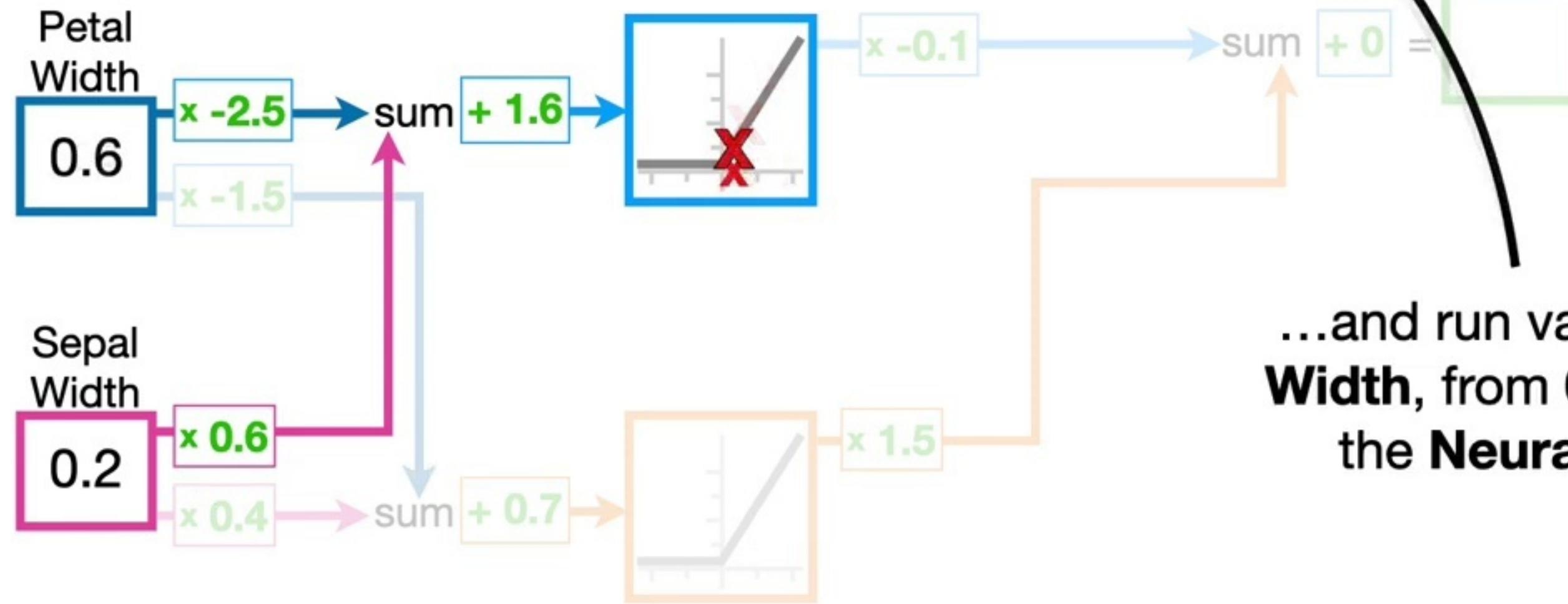
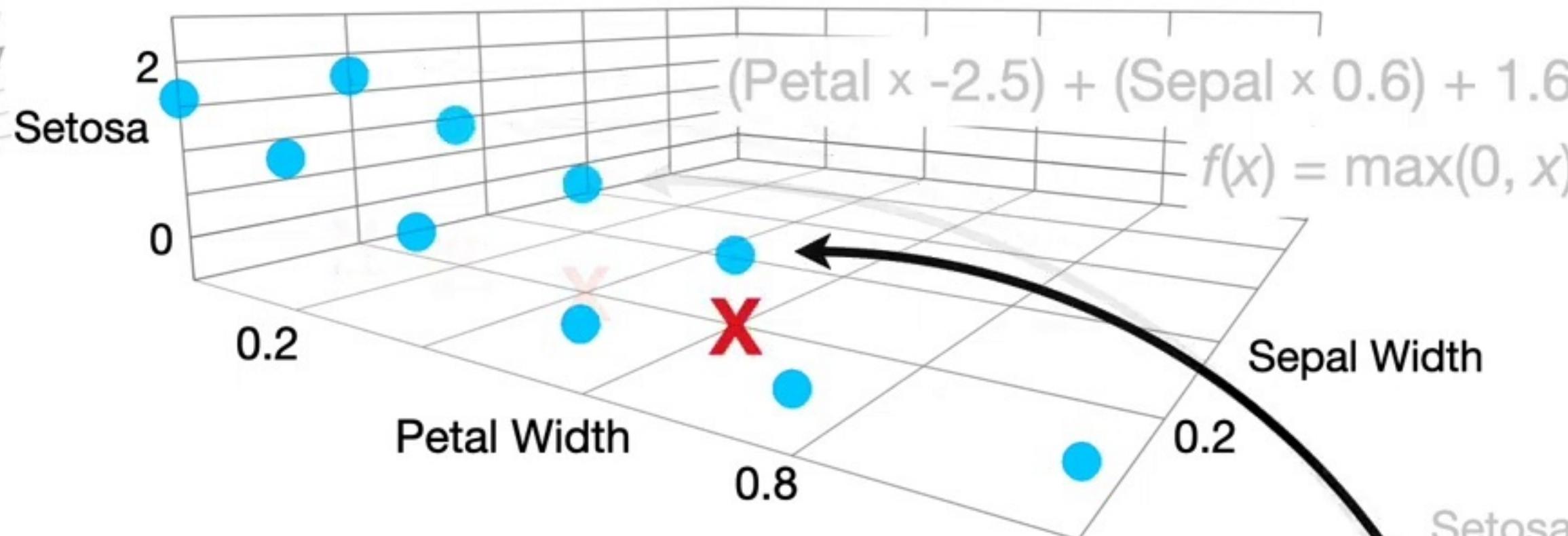
double  
BAM!!  
**SQ!**



**SQ!**  
double  
BAM!!

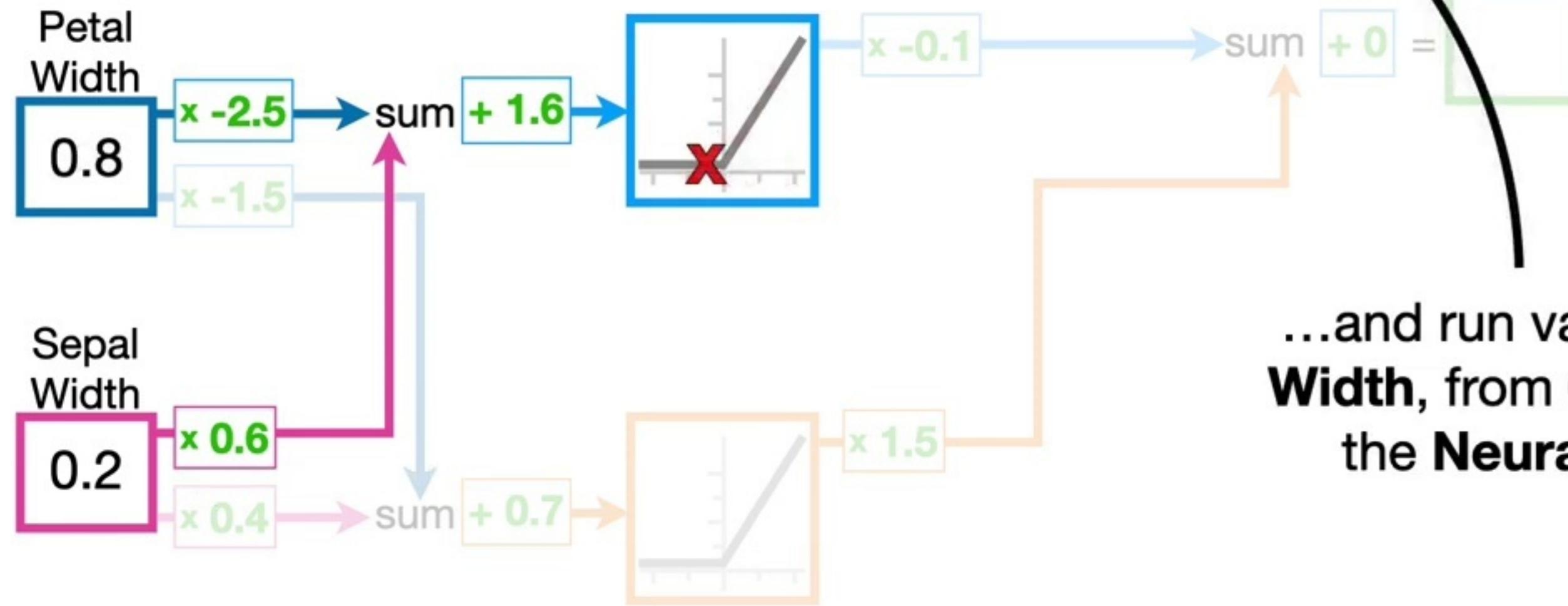
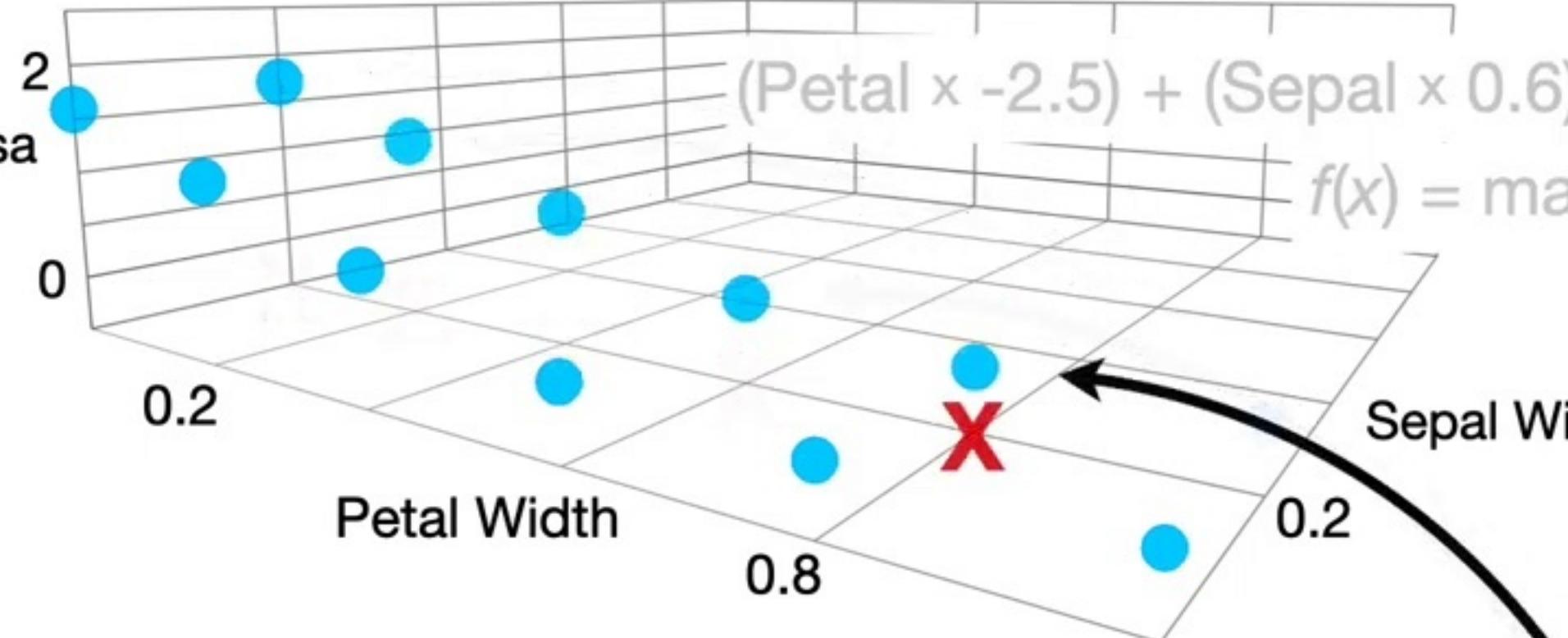


**SQ!**  
double  
BAM!!

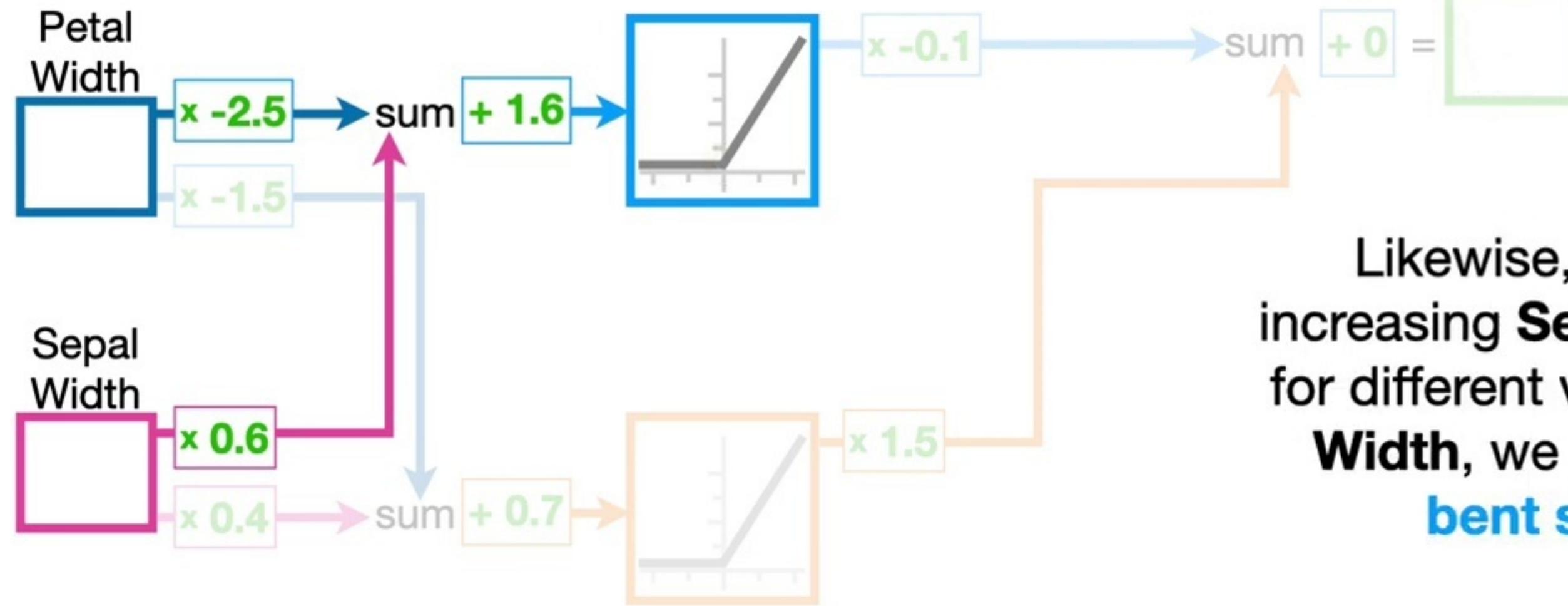
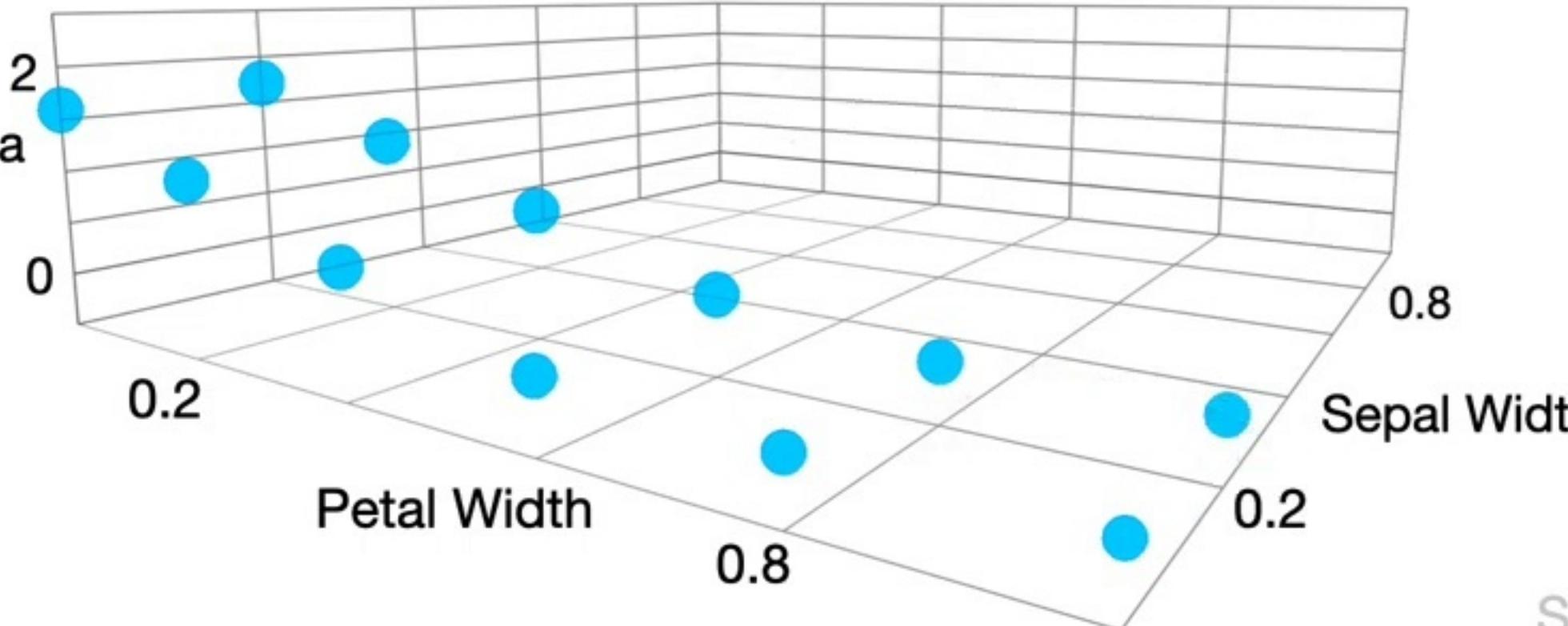


...and run values for **Petal Width**, from **0** to **1**, through the **Neural Network**.

**SQ!**  
double  
BAM!!

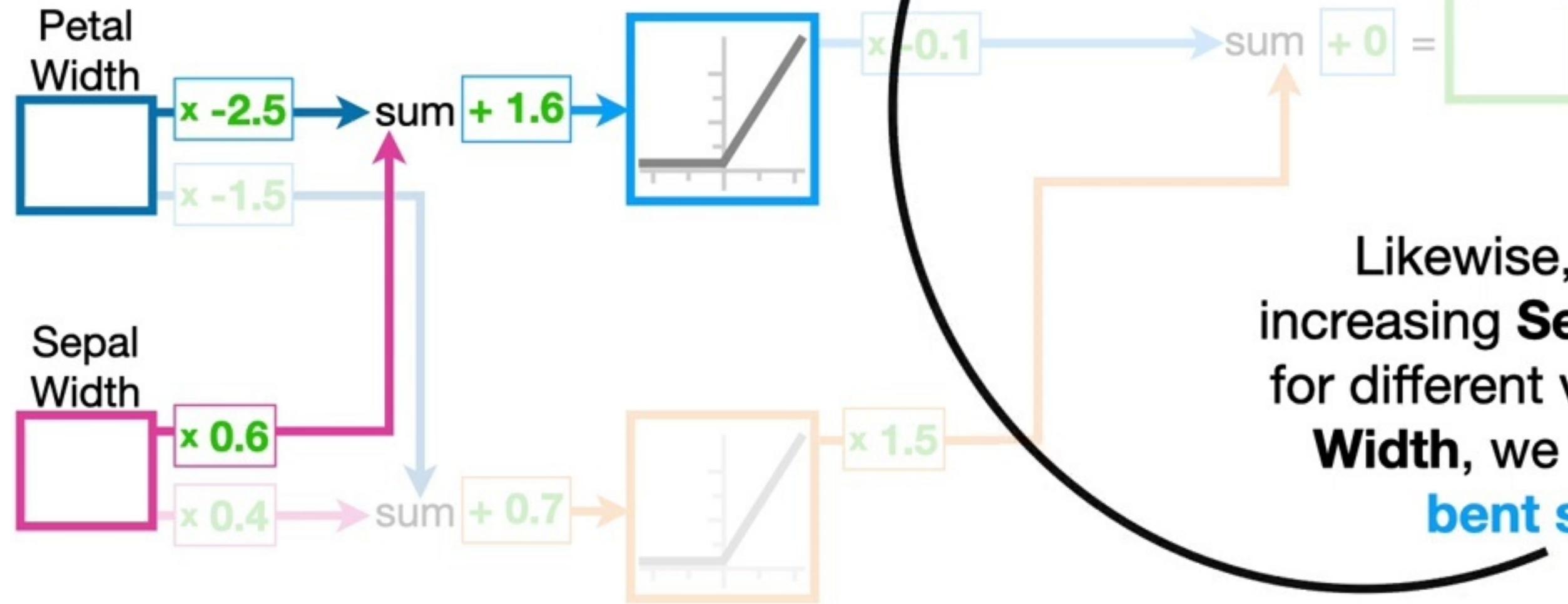
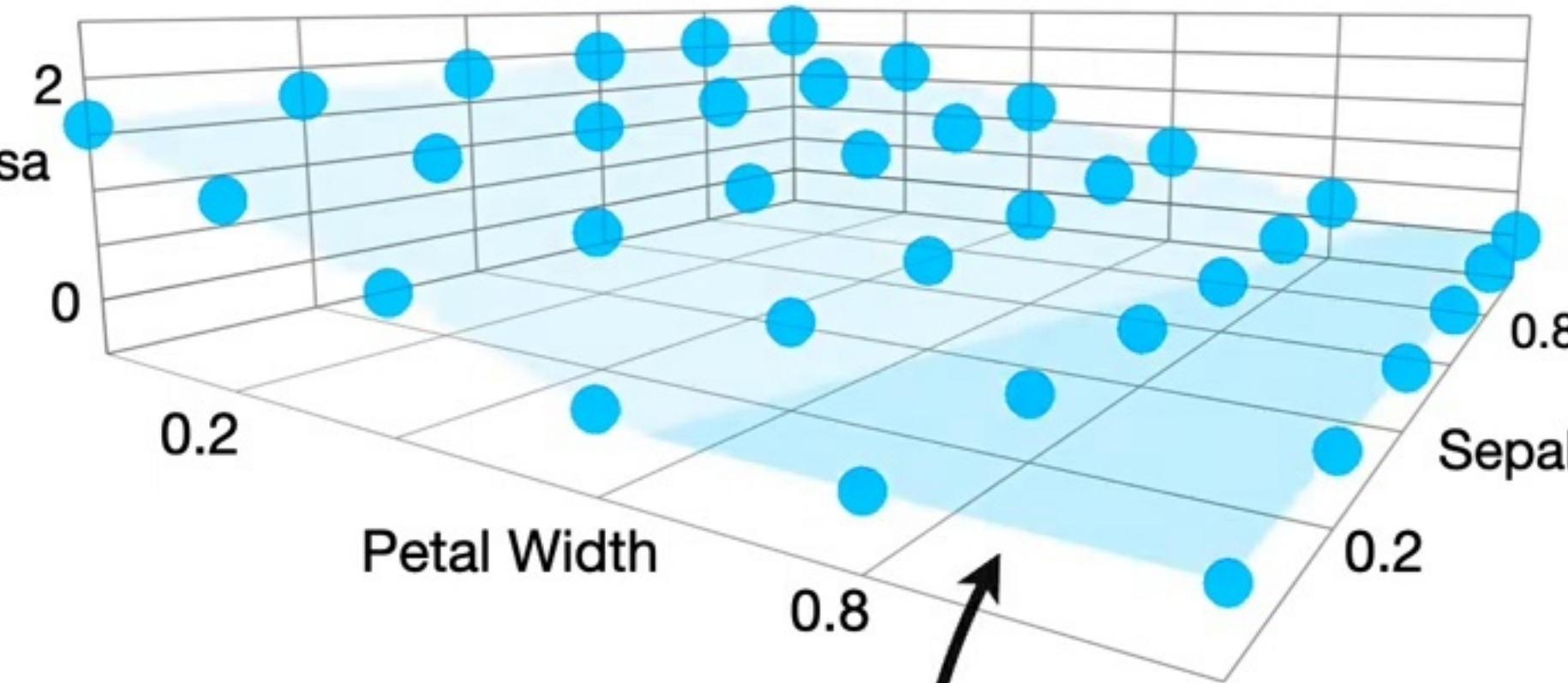


**SQ!**  
double  
BAM!!



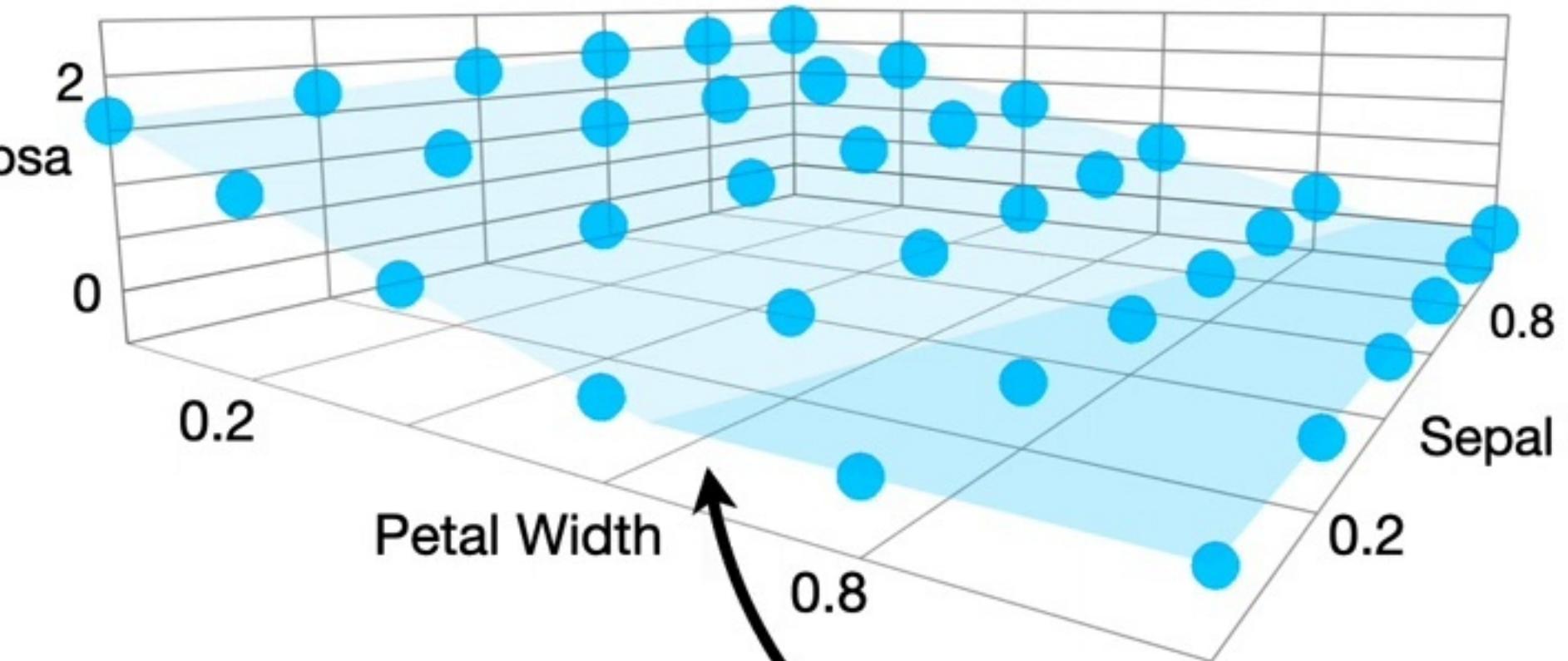
Likewise, if we keep increasing **Sepal Width** to 1 for different values of **Petal Width**, we get this **blue bent surface**.

**SQ!**  
double  
BAM!!

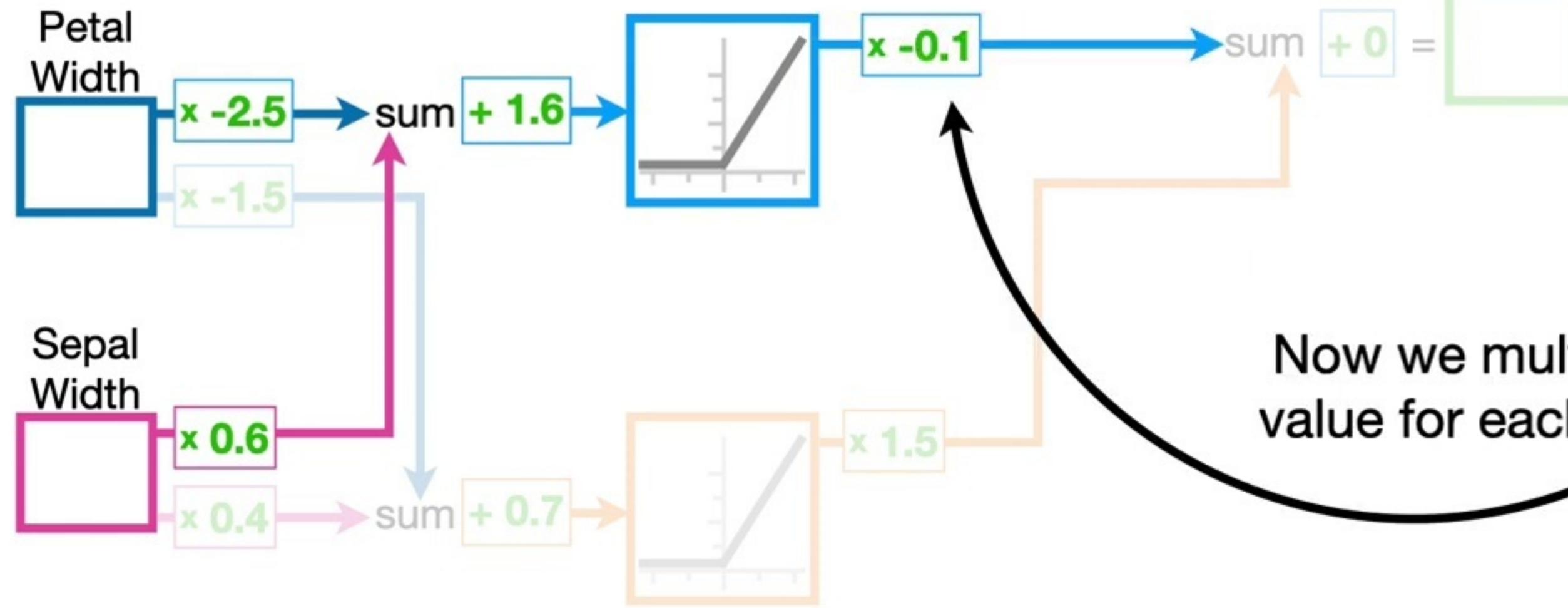
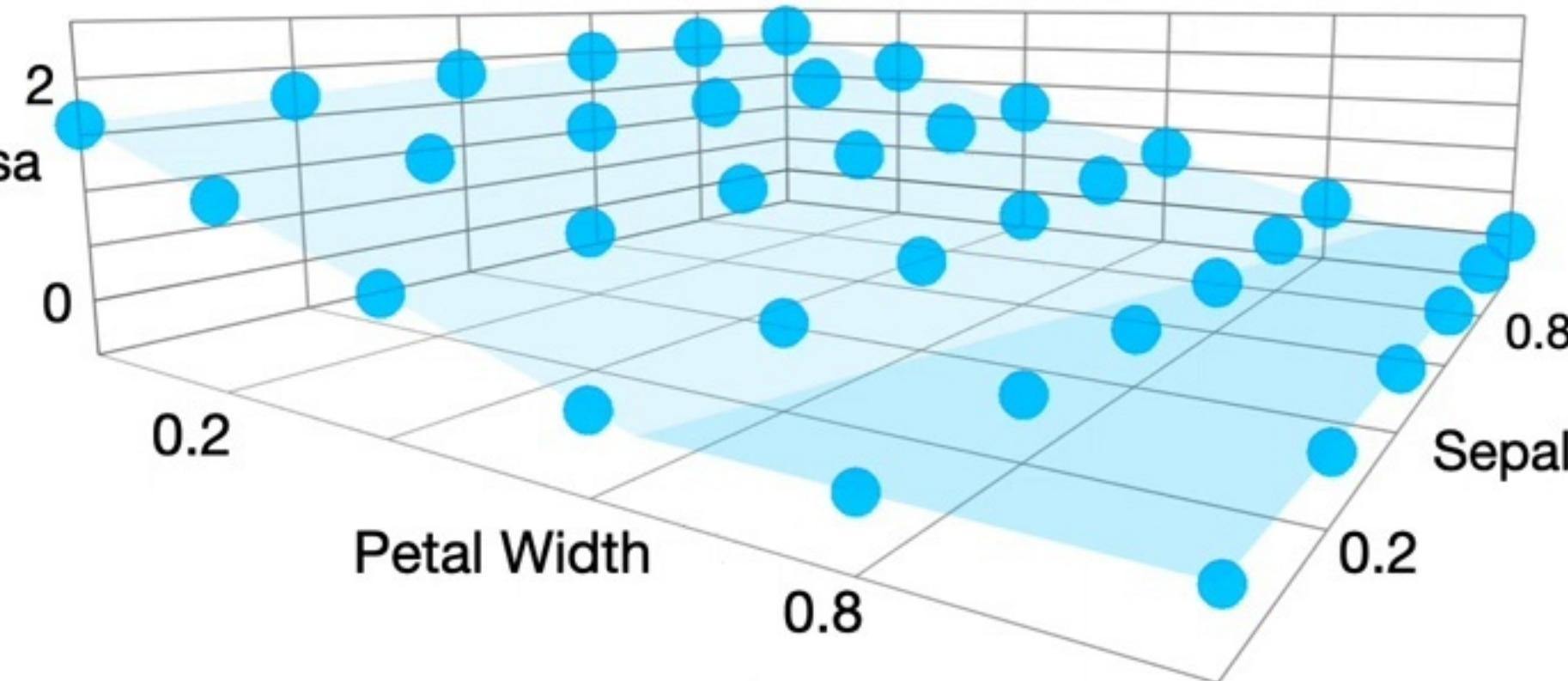


Likewise, if we keep increasing **Sepal Width** to 1 for different values of **Petal Width**, we get this **blue bent surface**.

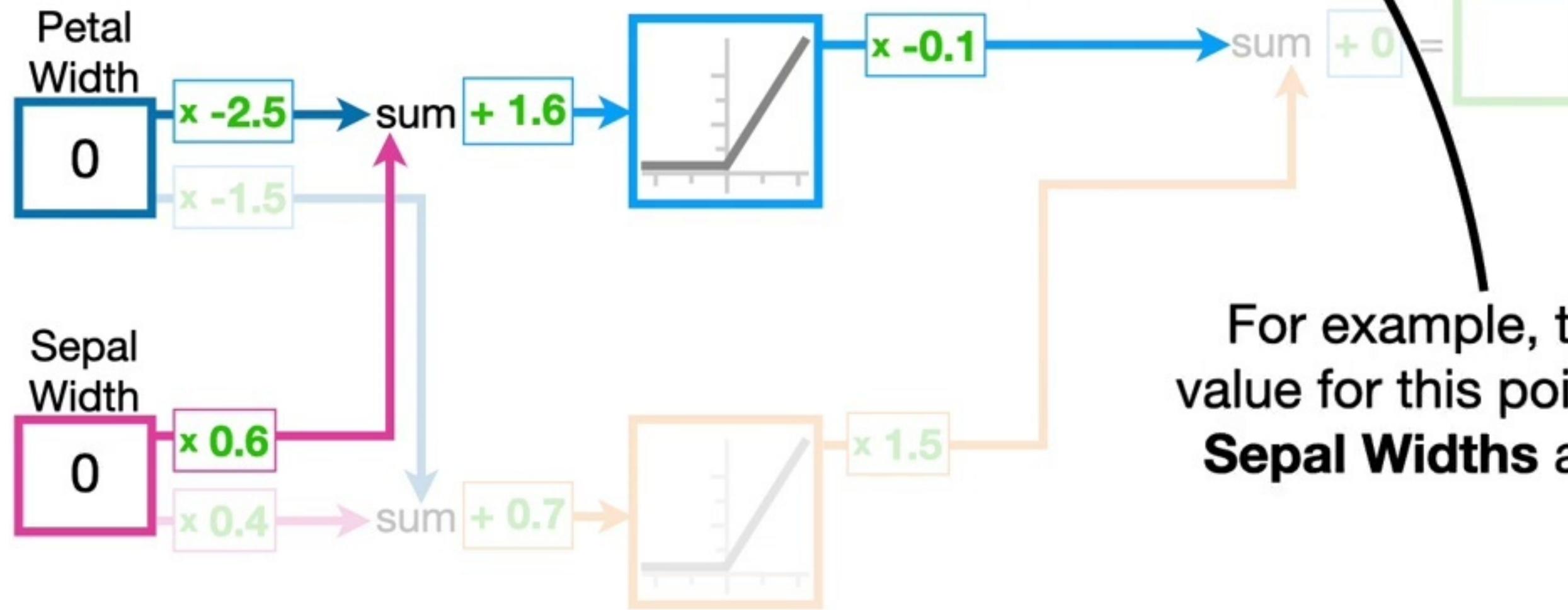
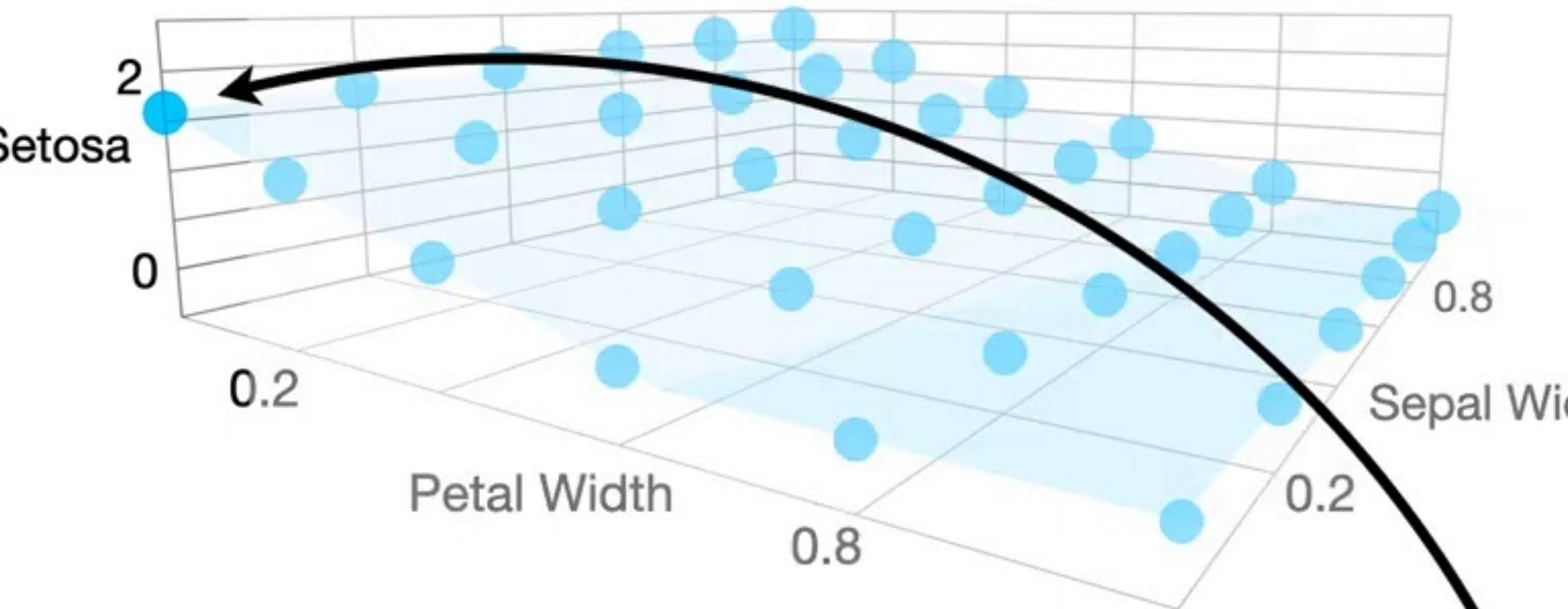
double  
BAM!!  
**SQ!**



double  
BAM!!  
**SQ!**

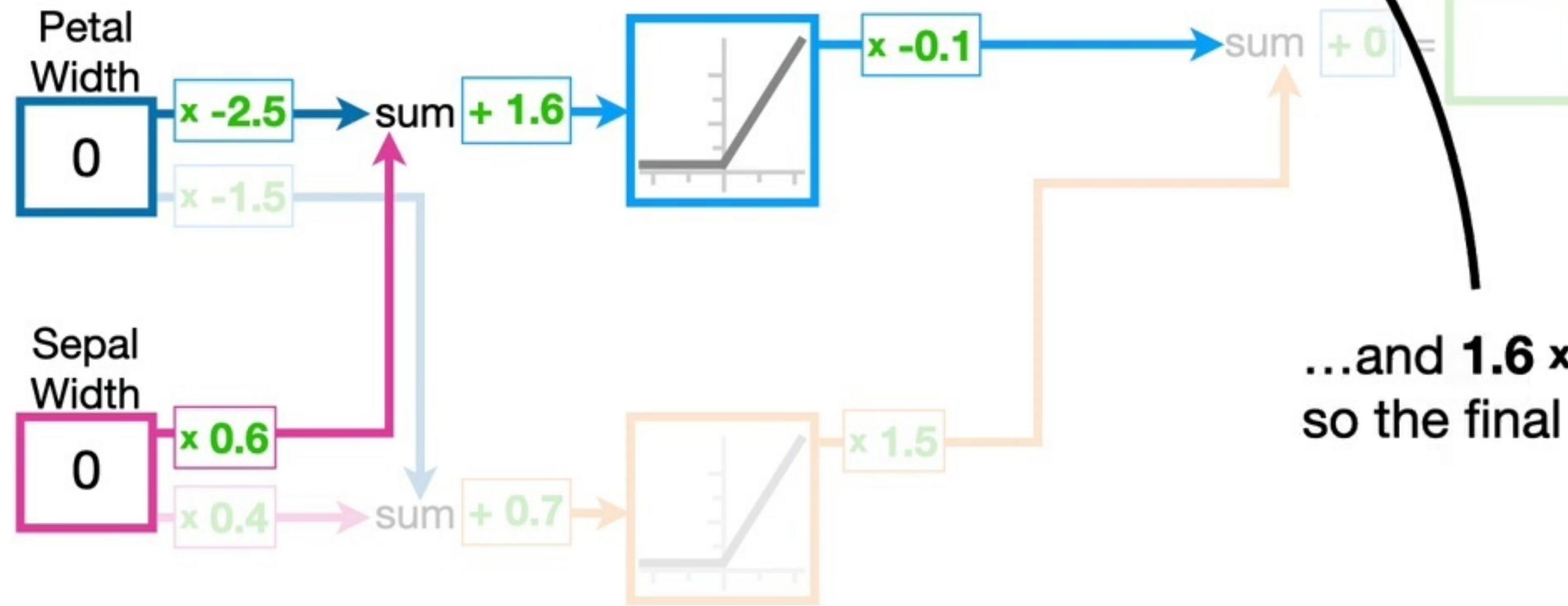
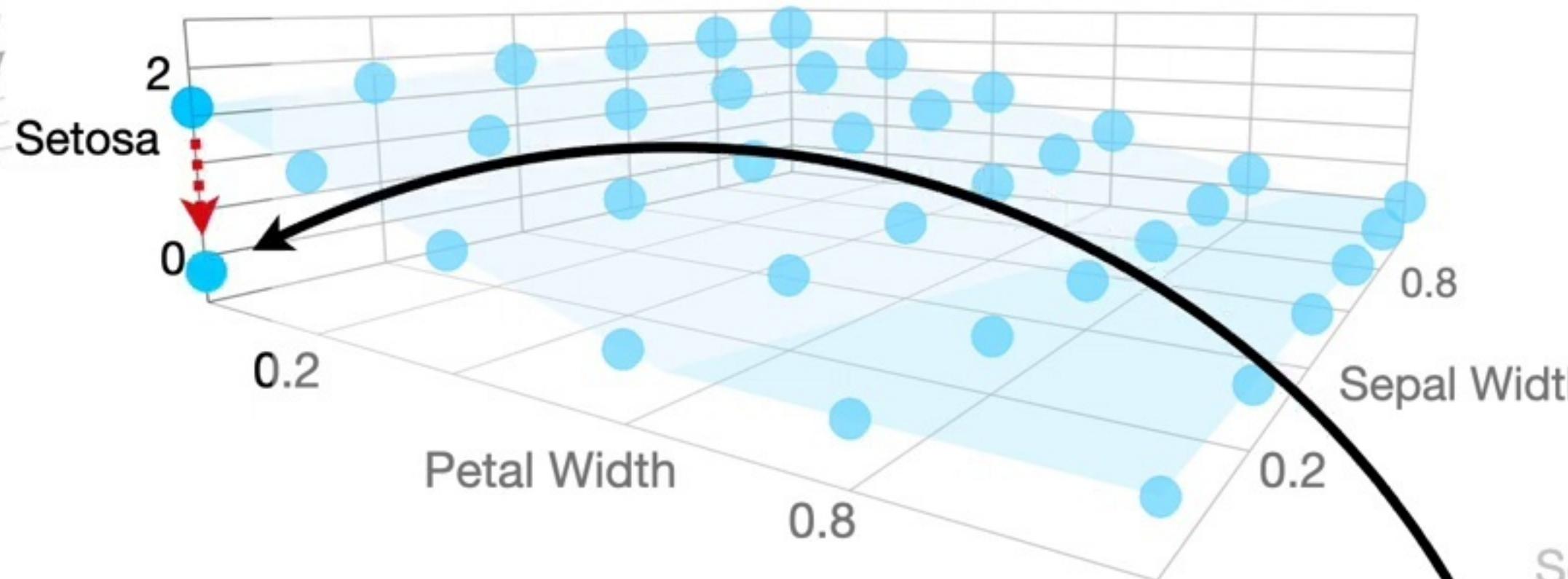


**SQ!**  
double  
BAM!!

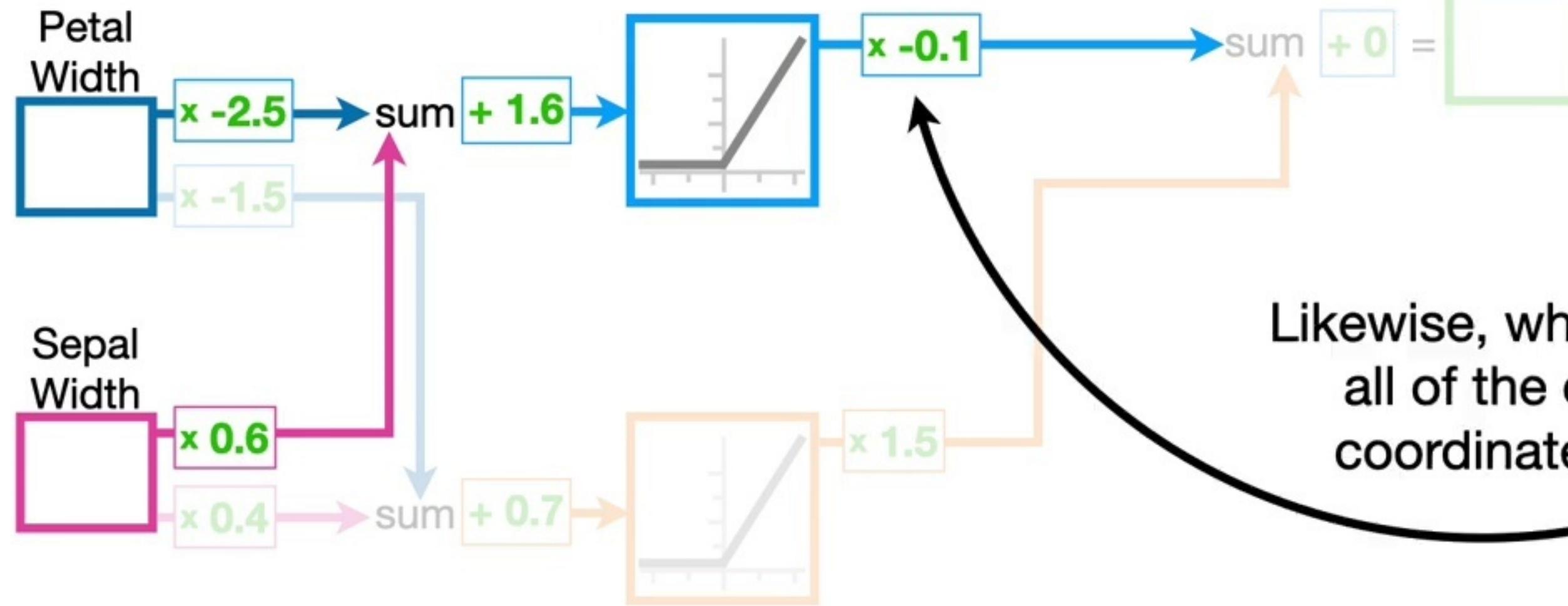
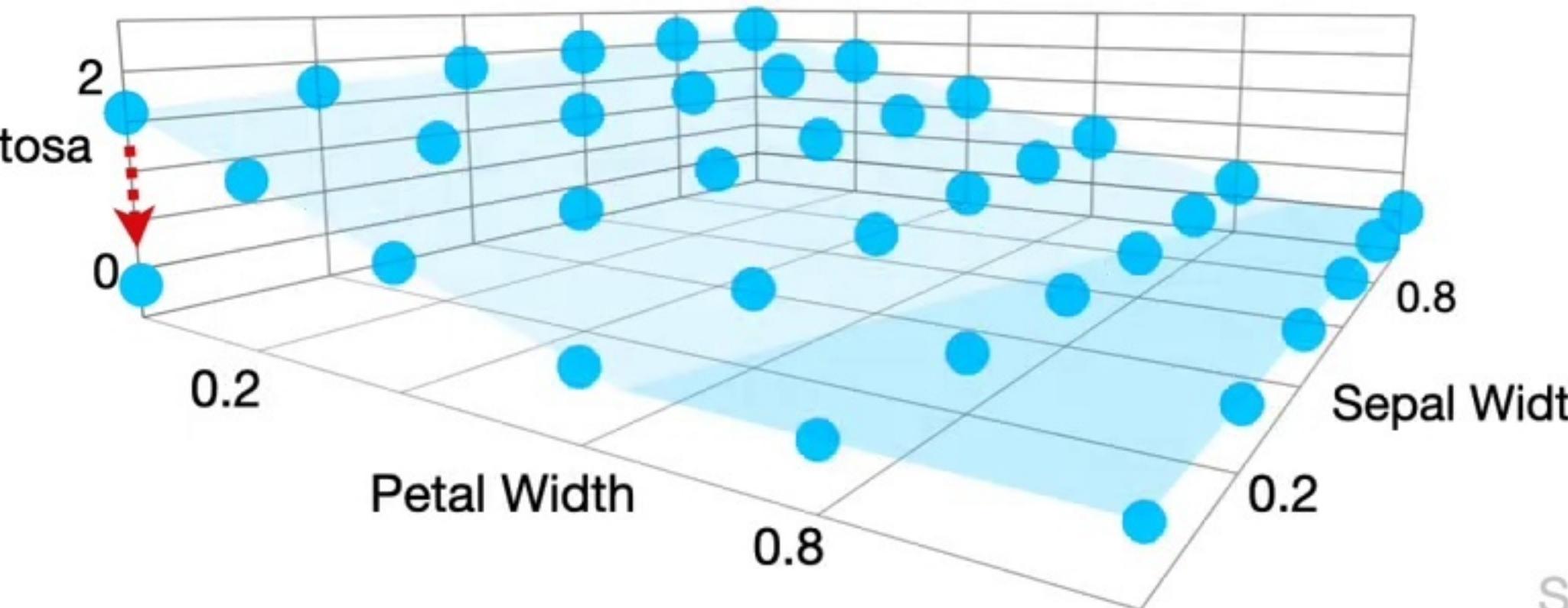


For example, the original y-axis value for this point, when **Petal and Sepal Widths** are both 0, is 1.6...

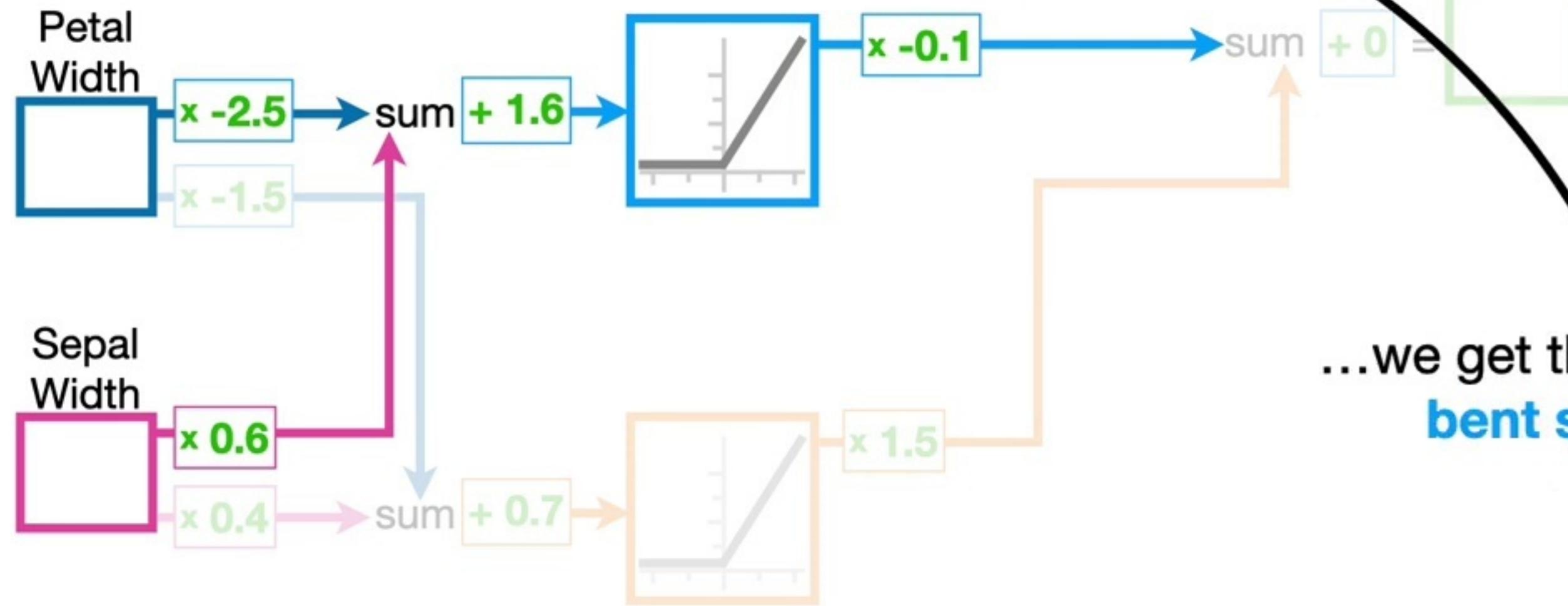
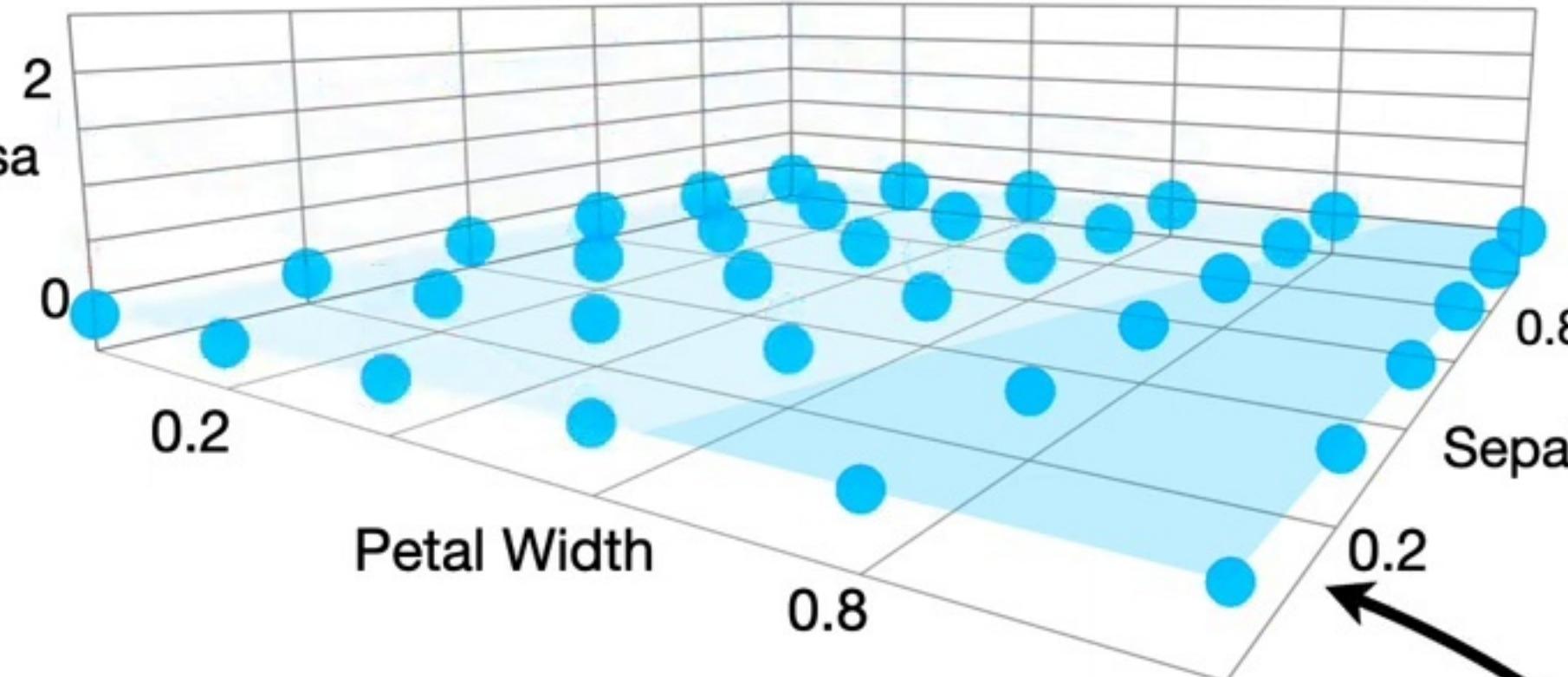
**SQ!**  
double  
BAM!!

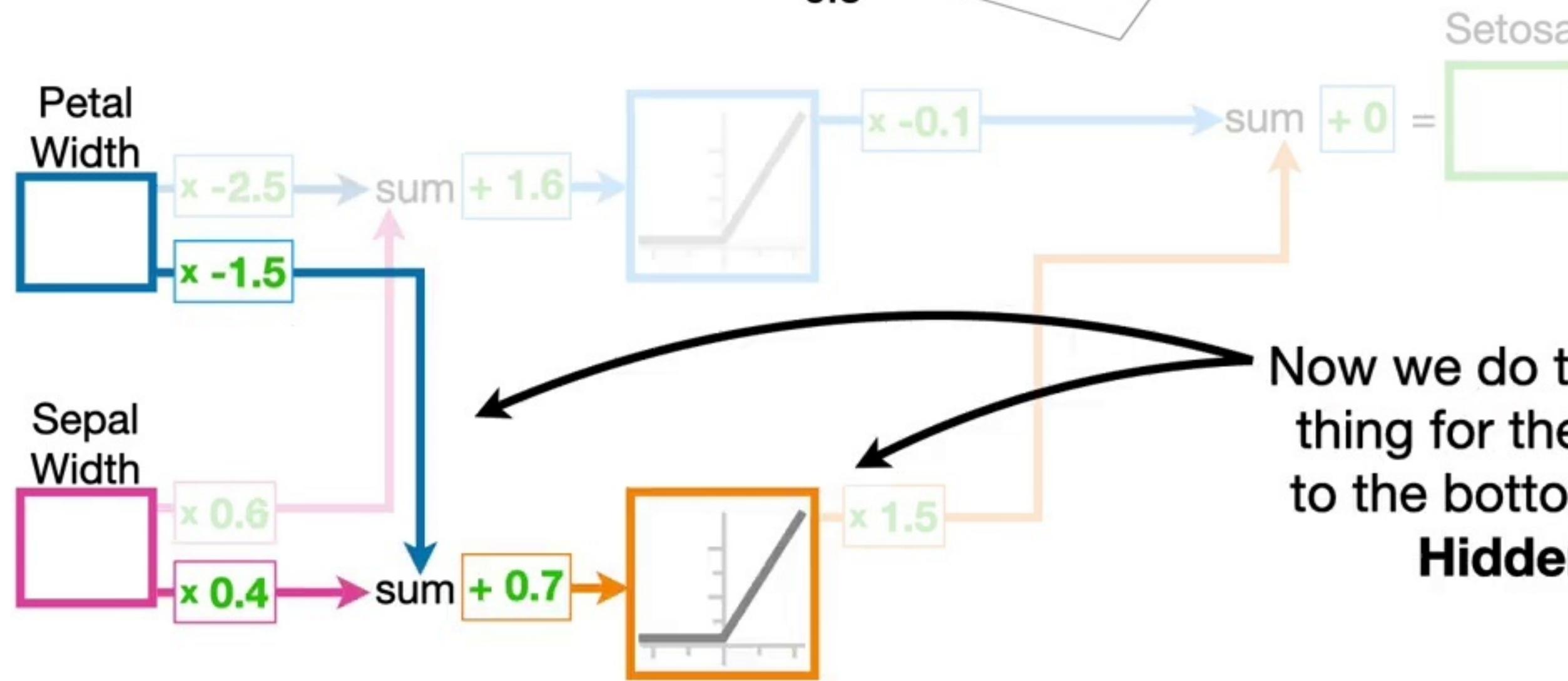
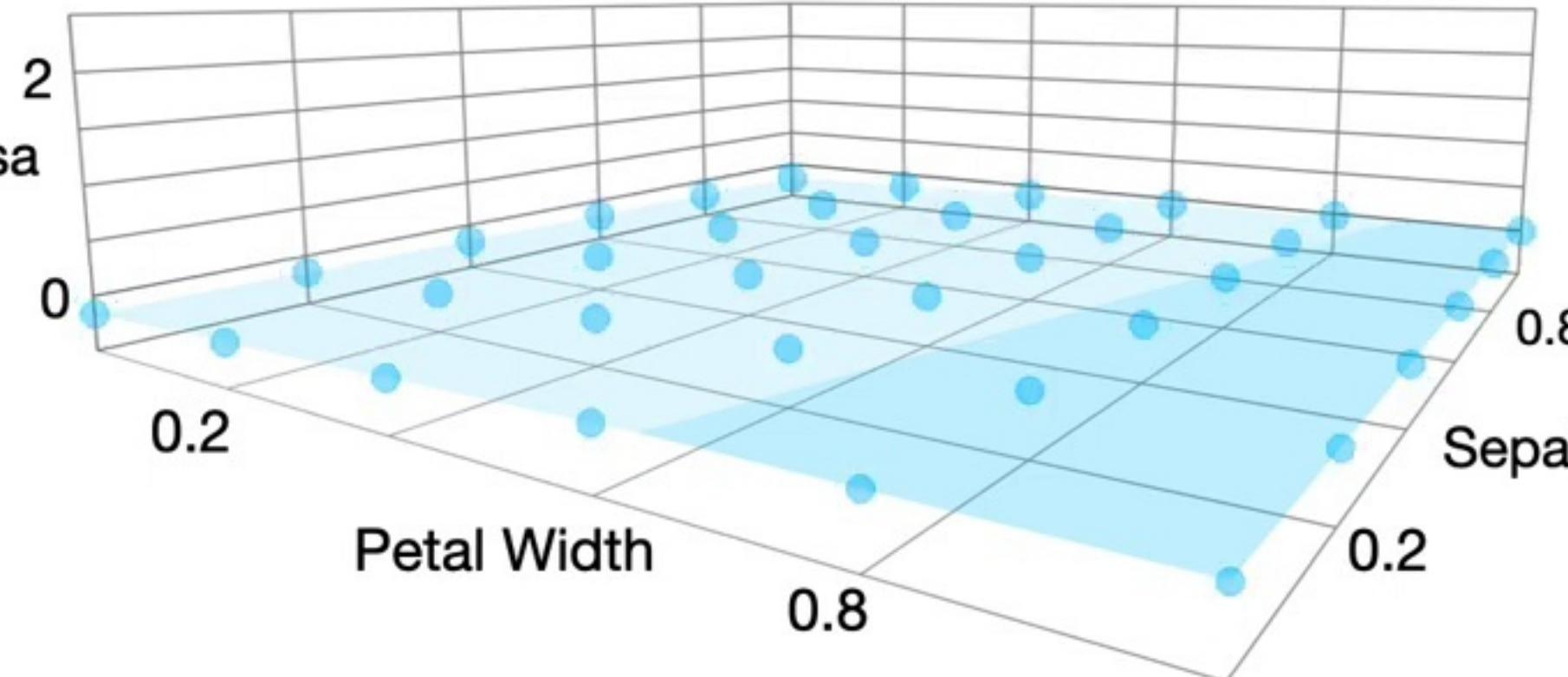


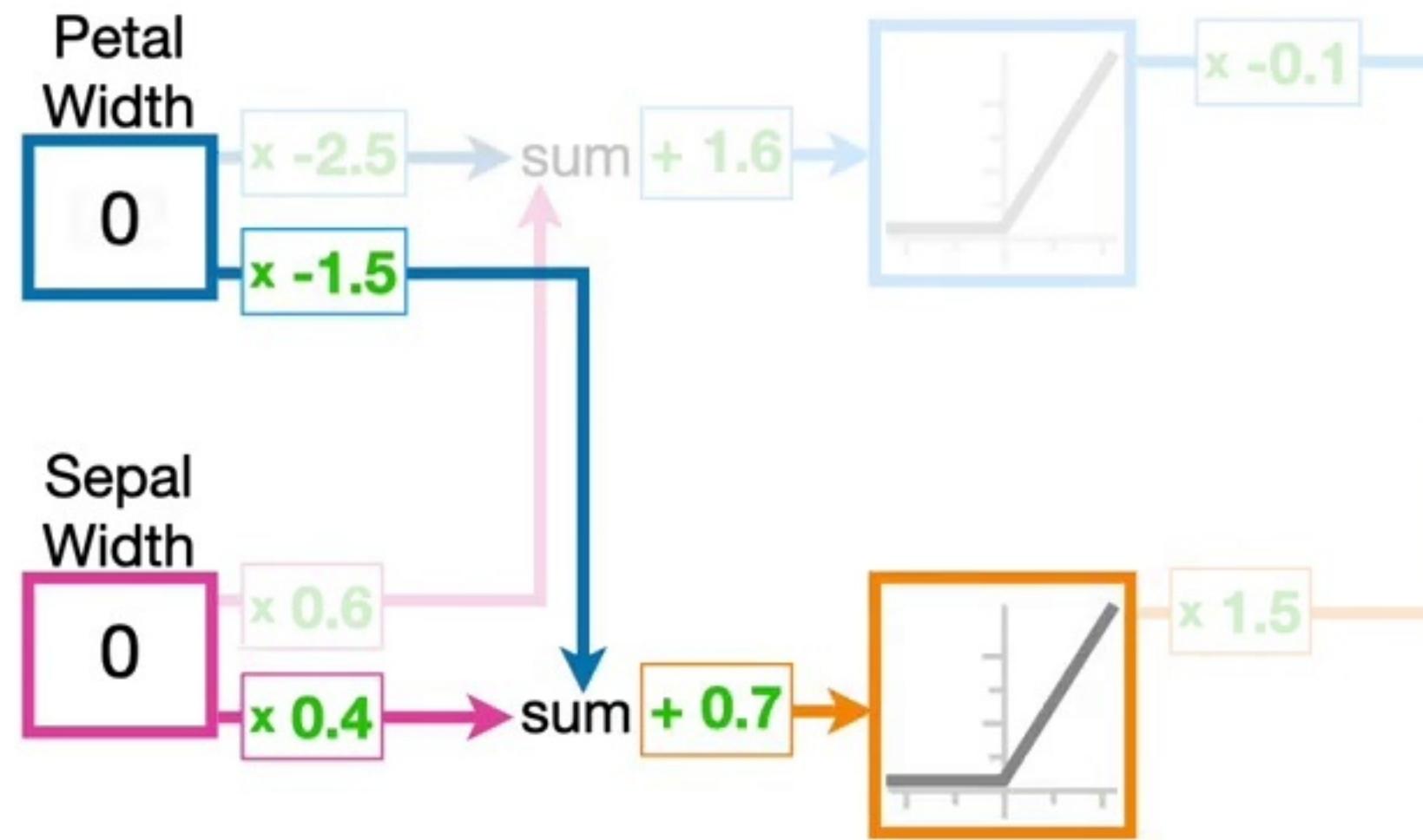
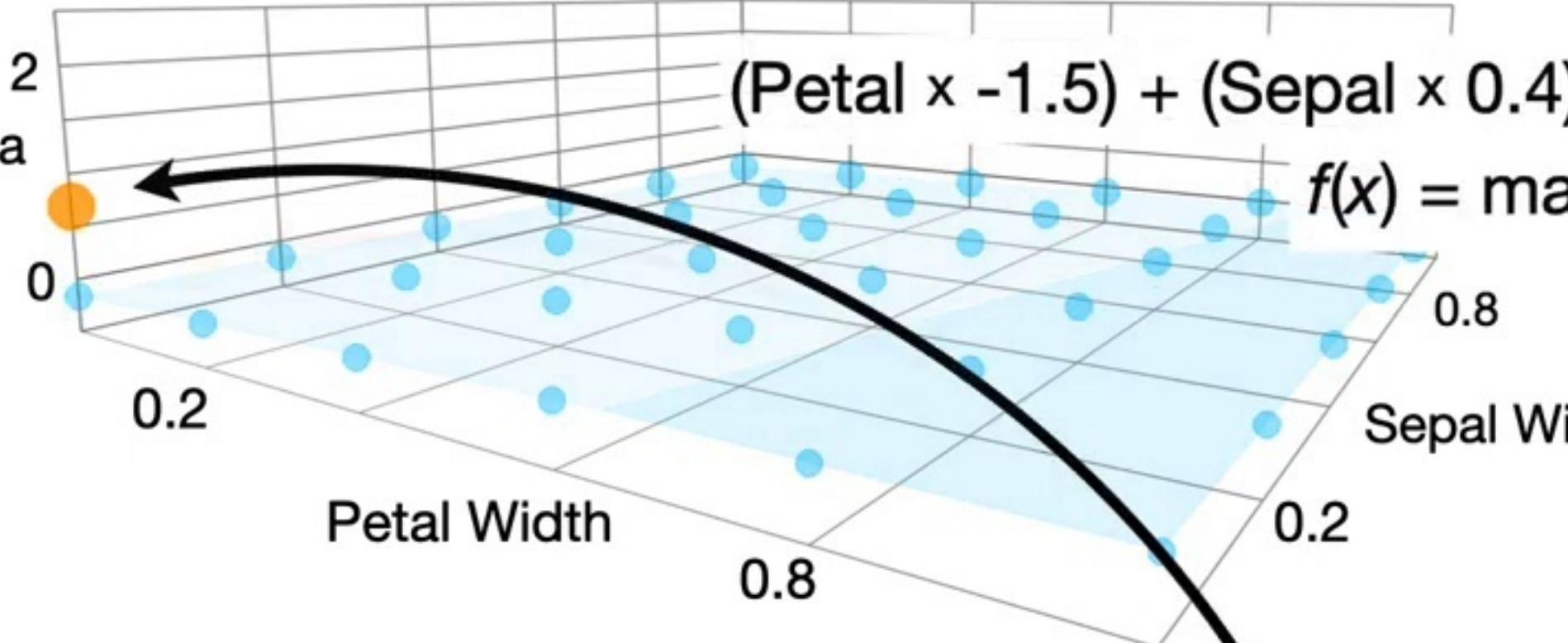
**SQ!**  
double  
BAM!!



**SQ!**  
double  
BAM!!



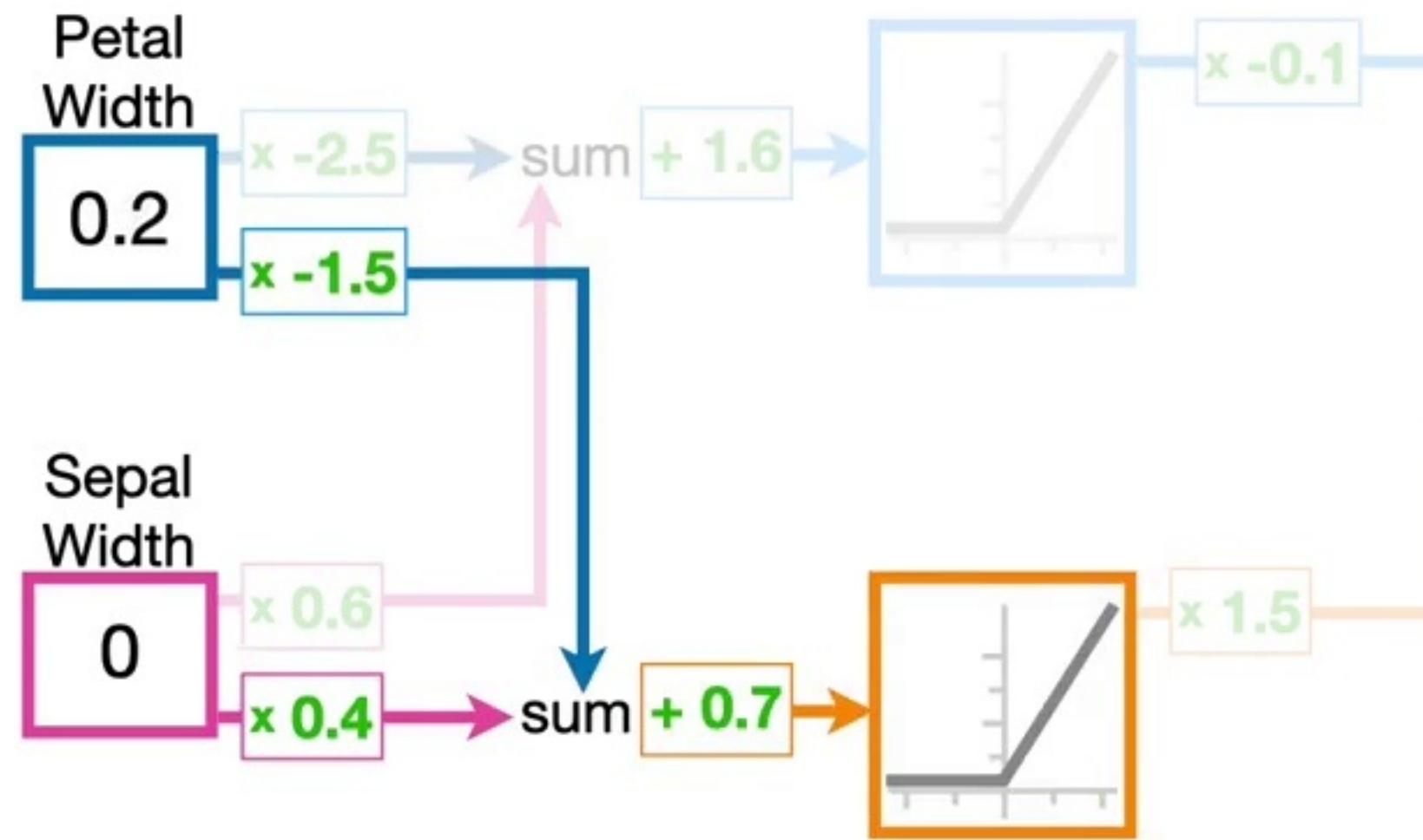
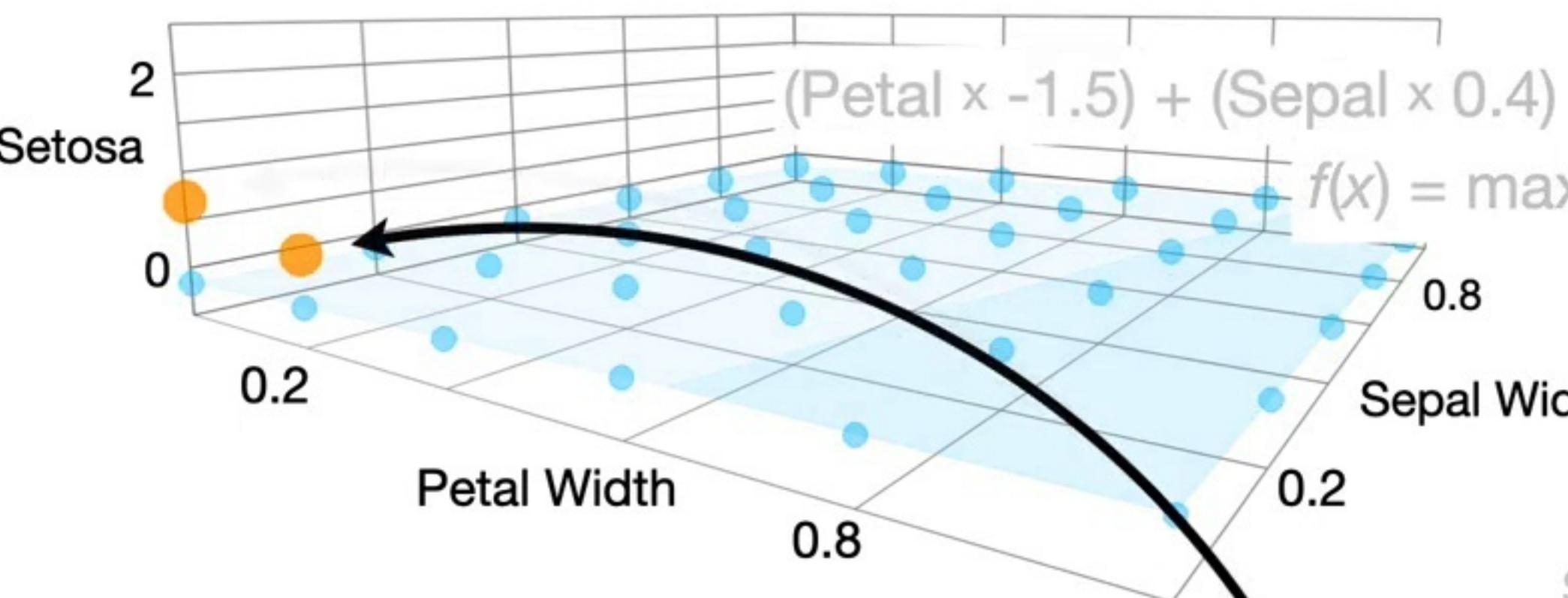




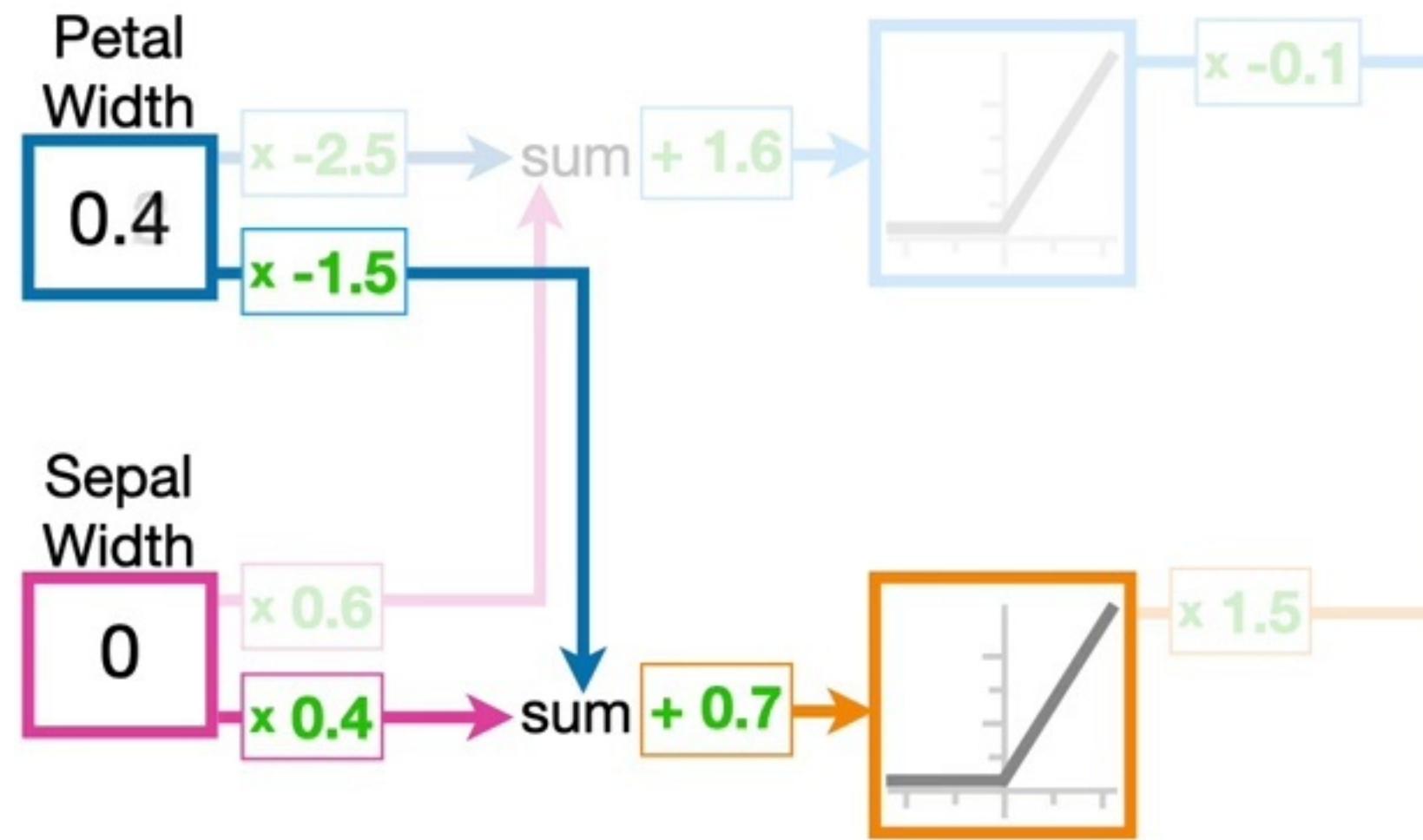
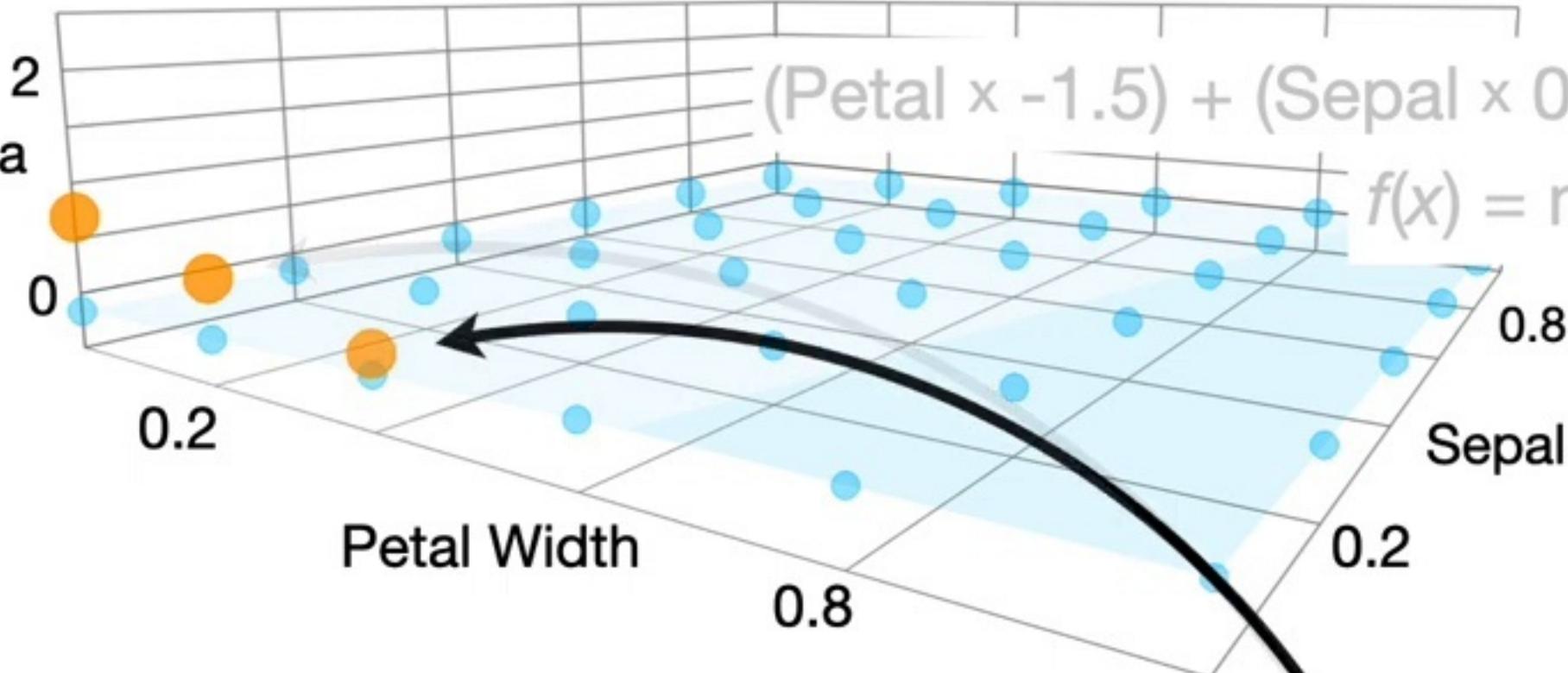
Now we do the exact same thing for the connections to the bottom node in the **Hidden Layer**.



double  
BAM!!  
**SQ!**



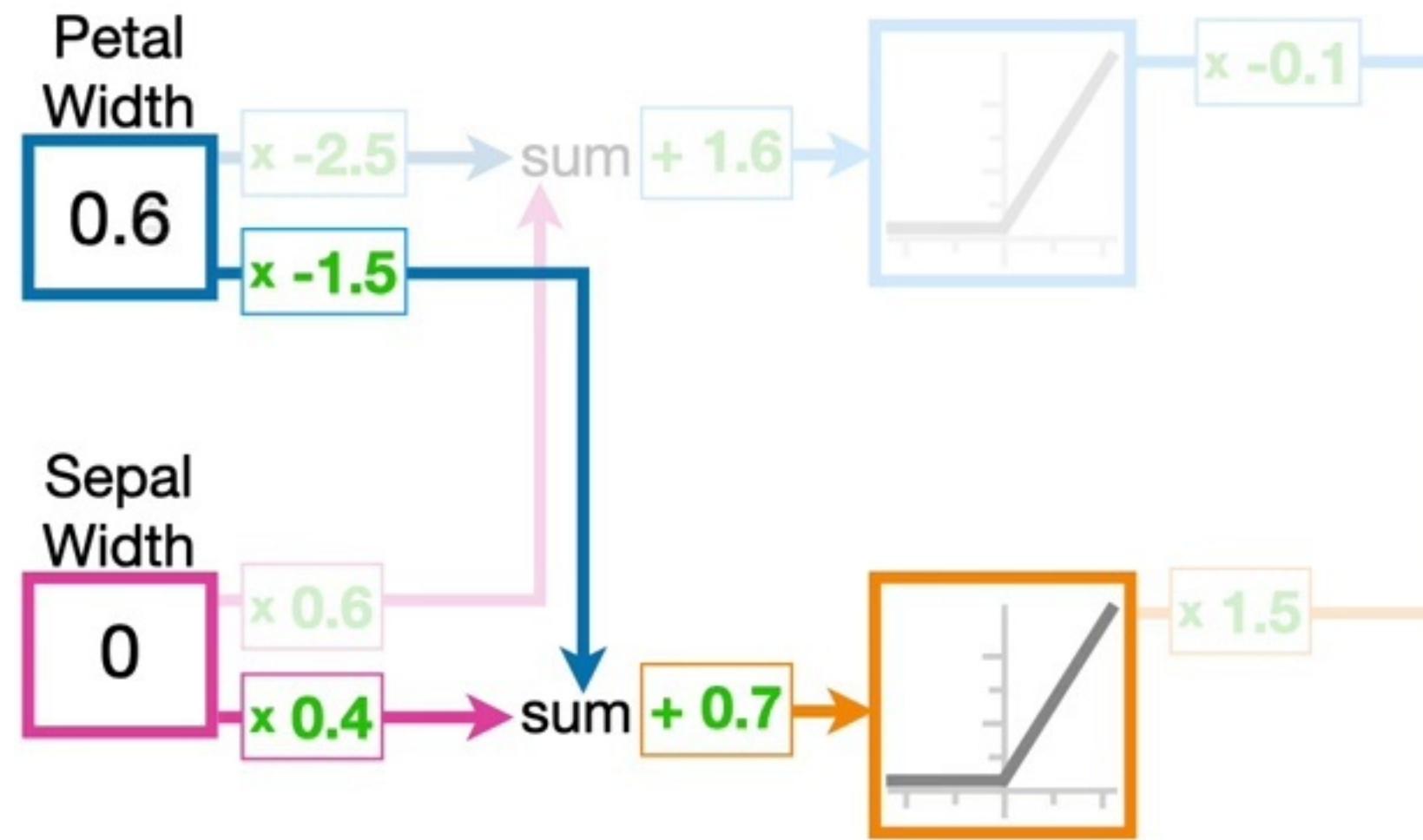
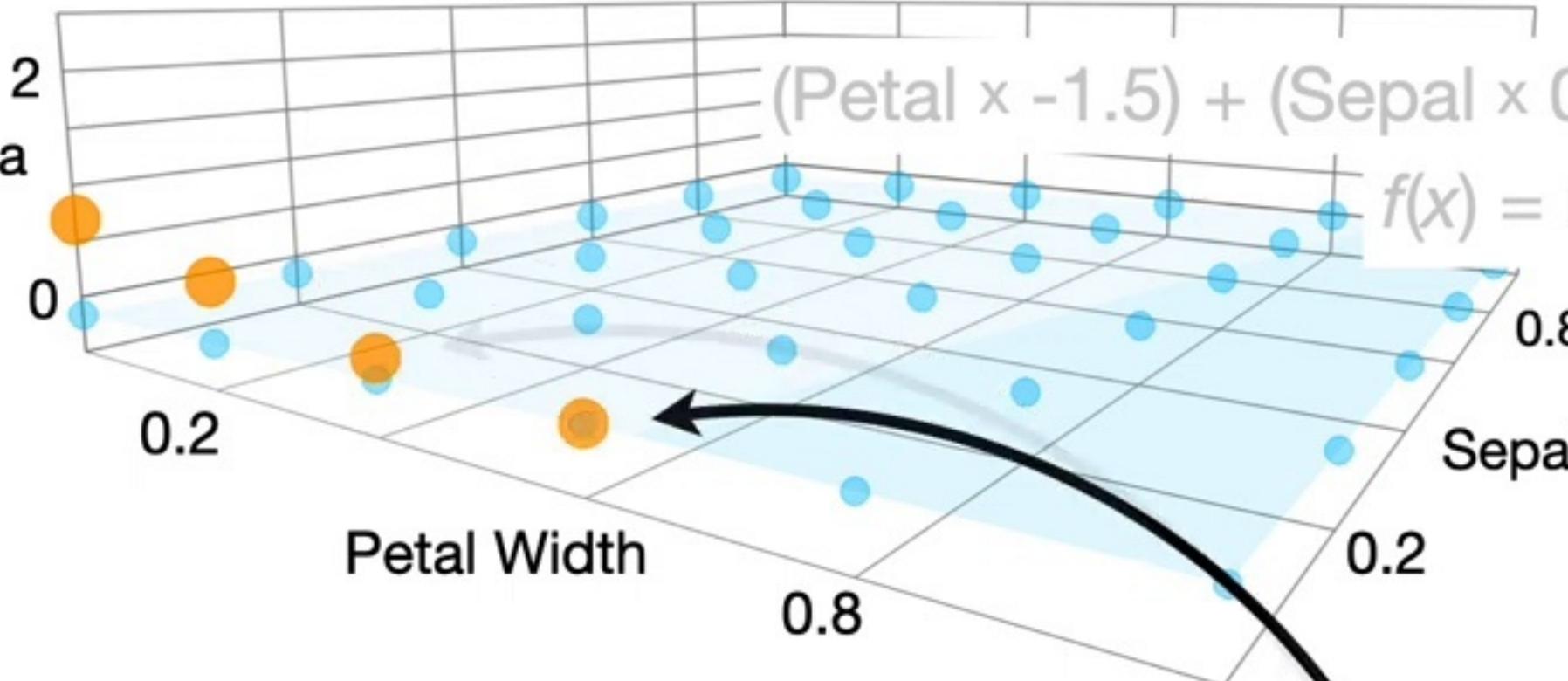
Now we do the exact same thing for the connections to the bottom node in the **Hidden Layer**.



Now we do the exact same thing for the connections to the bottom node in the **Hidden Layer**.

Setosa  
+ 0 =

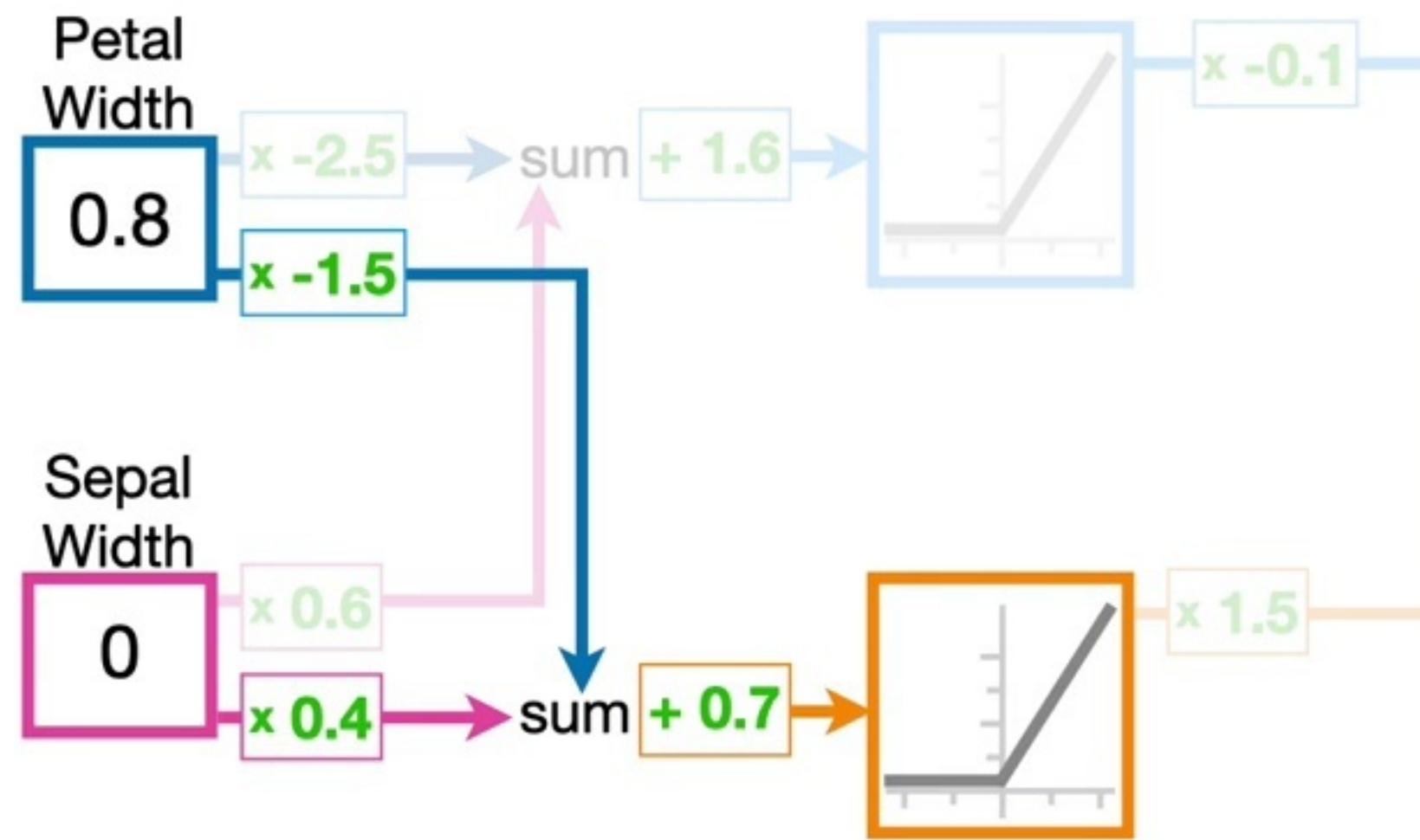
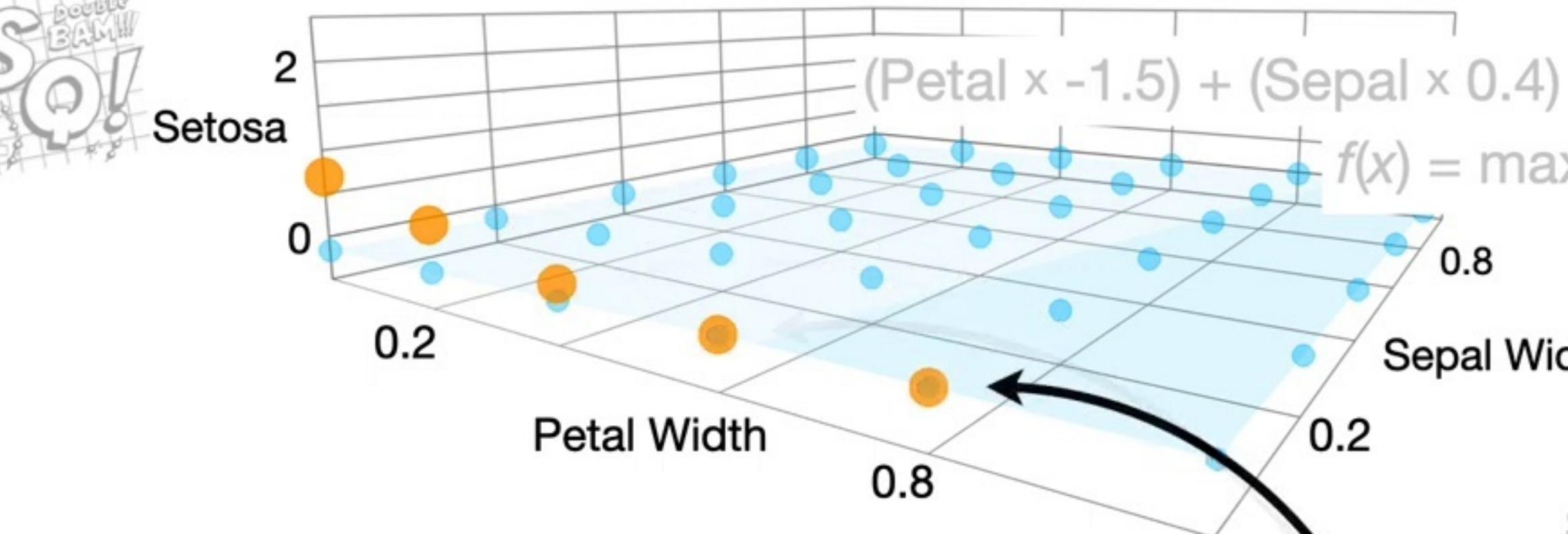
double  
BAM!!  
**SQ!**



Setosa

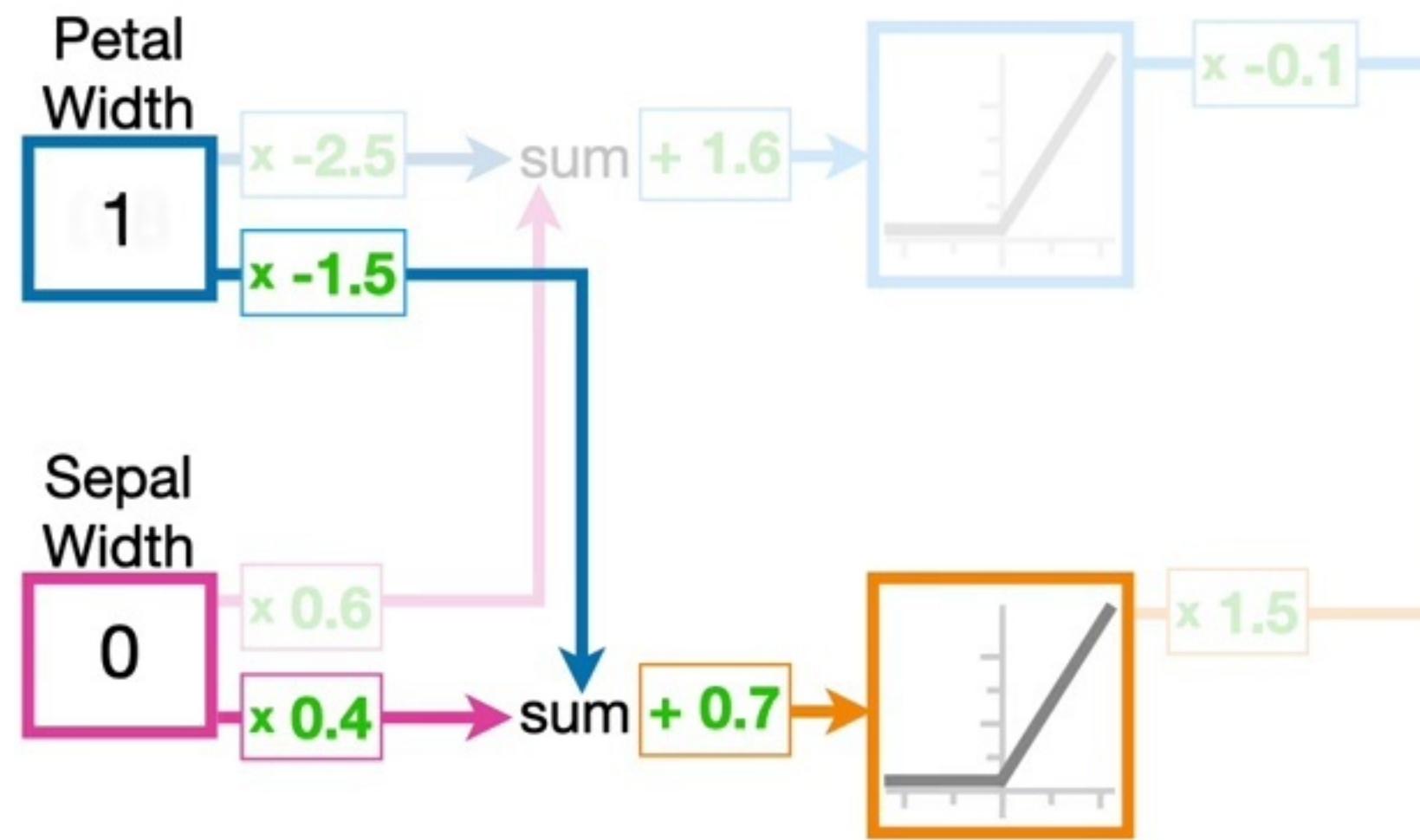
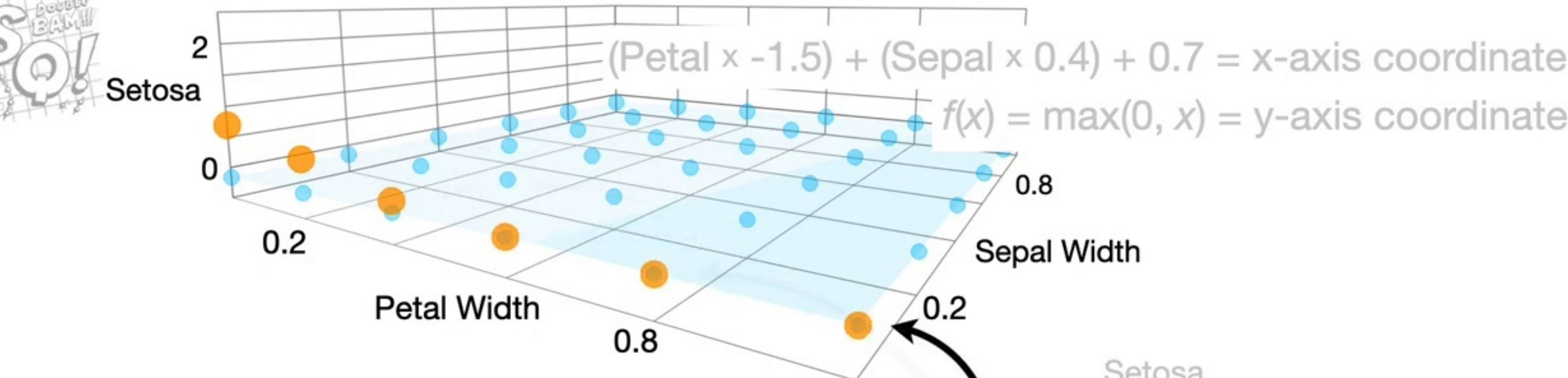
$+ 0$  =

Now we do the exact same thing for the connections to the bottom node in the **Hidden Layer**.



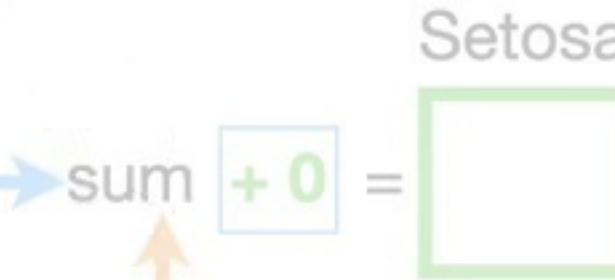
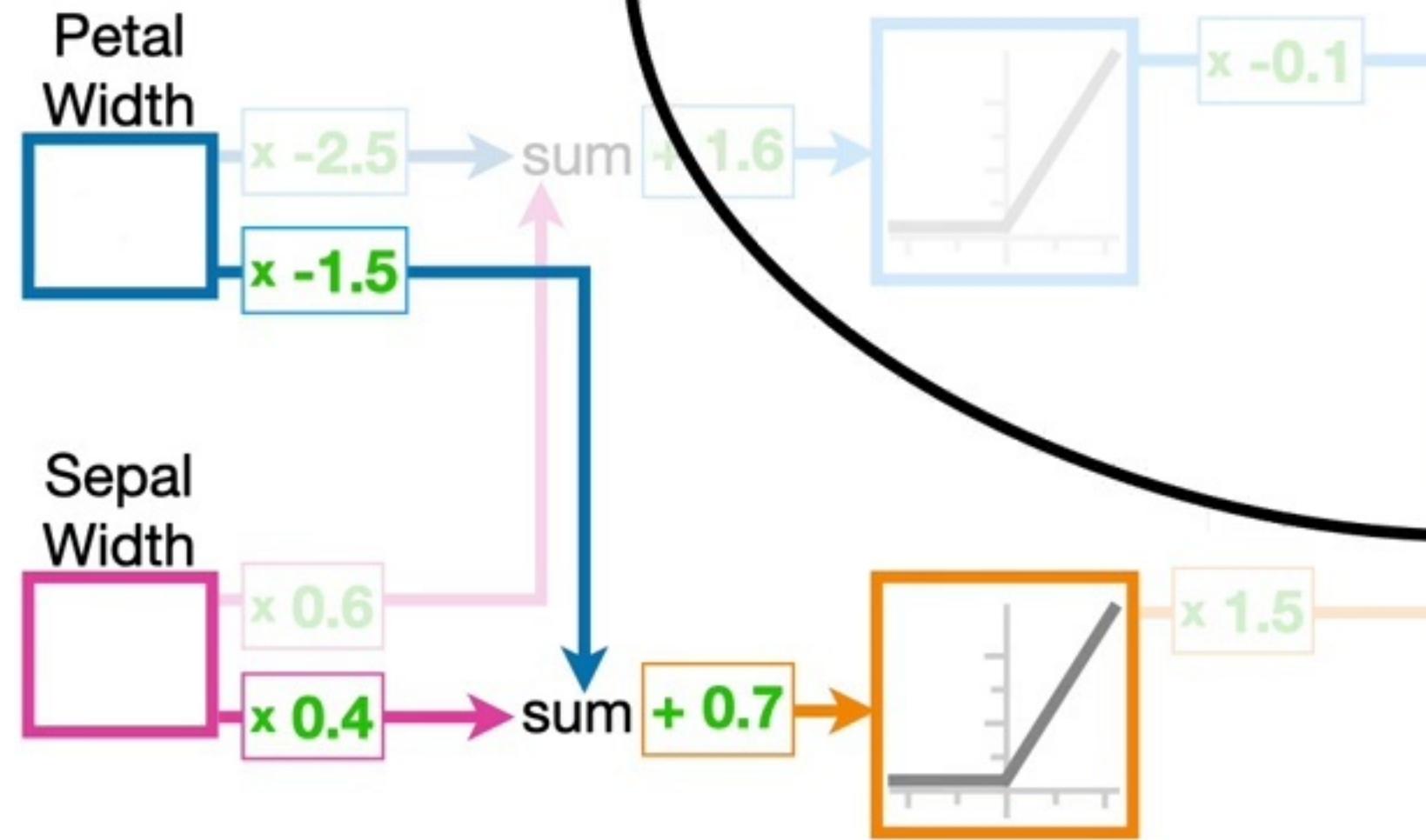
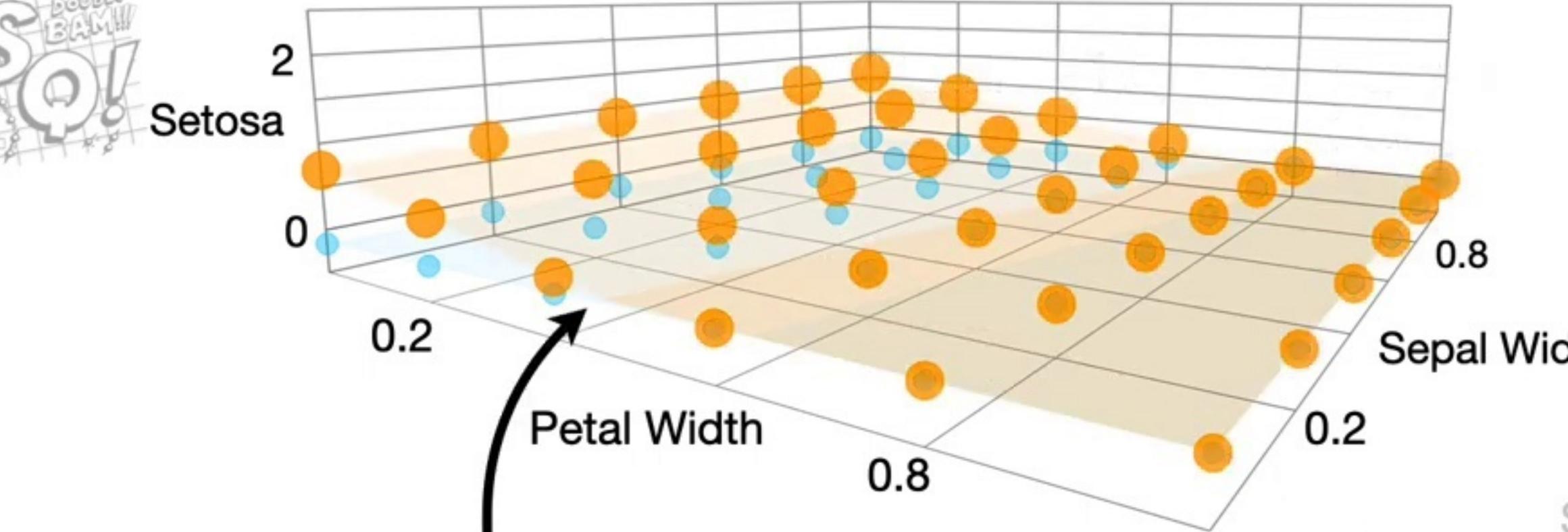
Now we do the exact same thing for the connections to the bottom node in the **Hidden Layer**.

Setosa  
[ ]

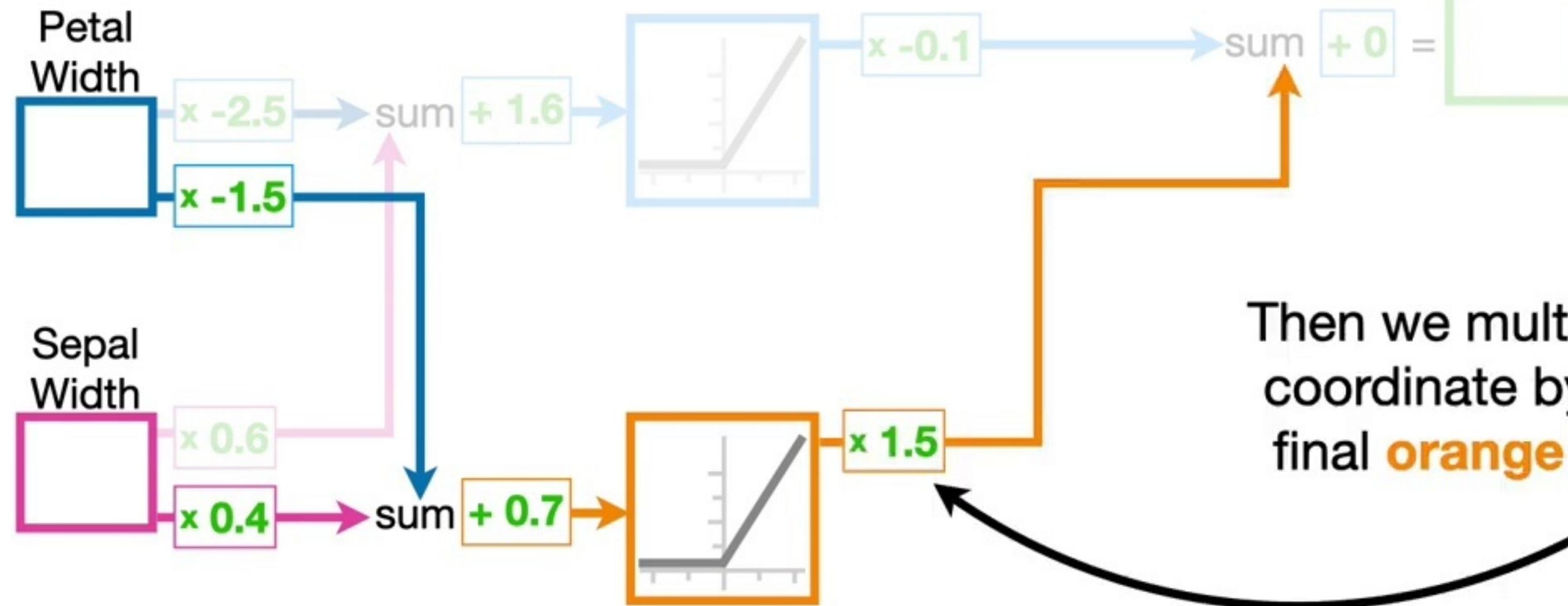
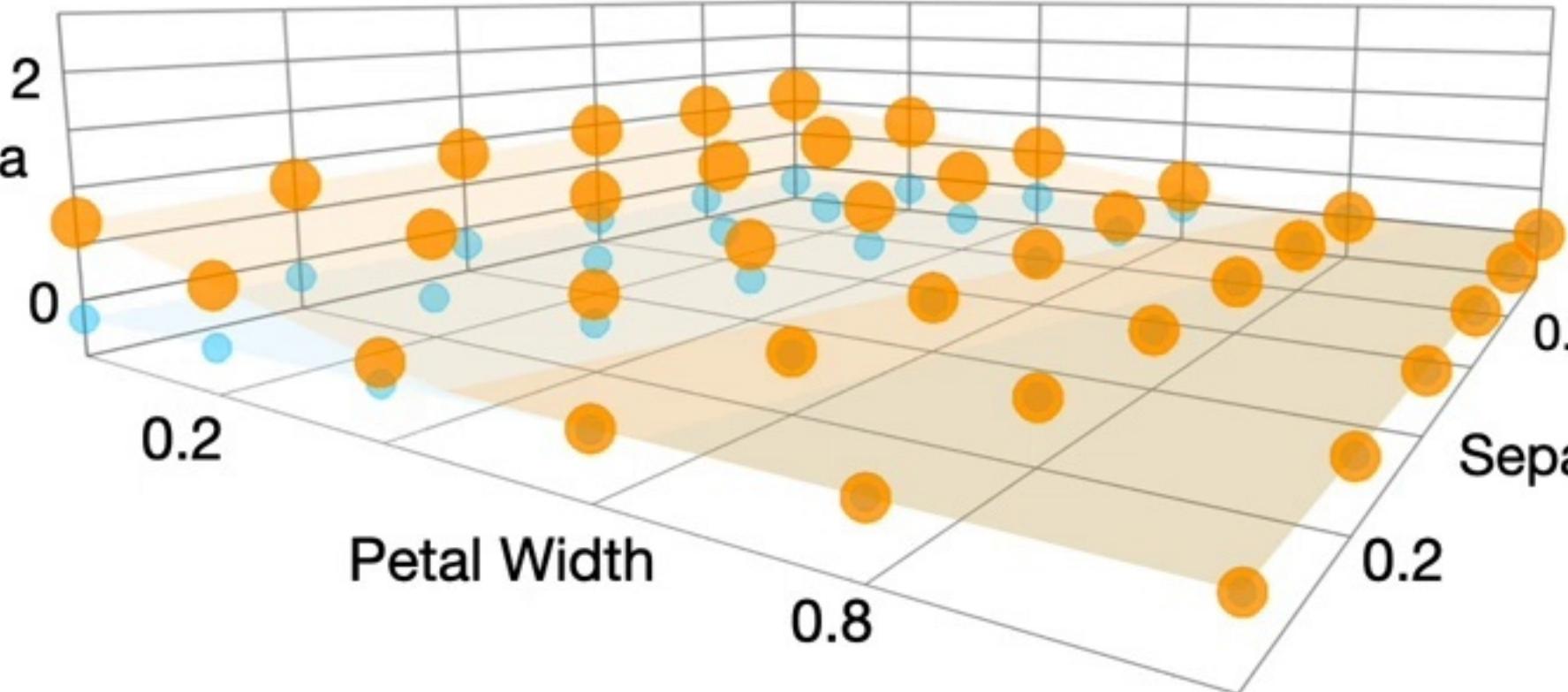


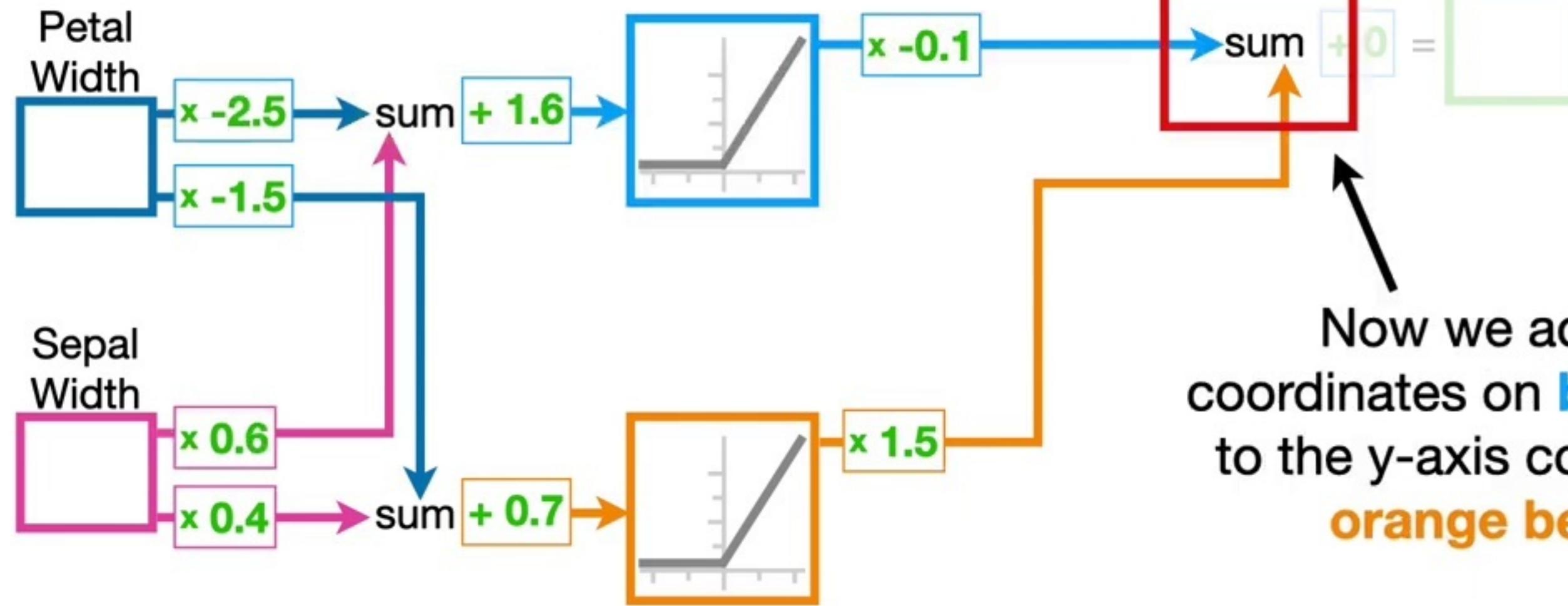
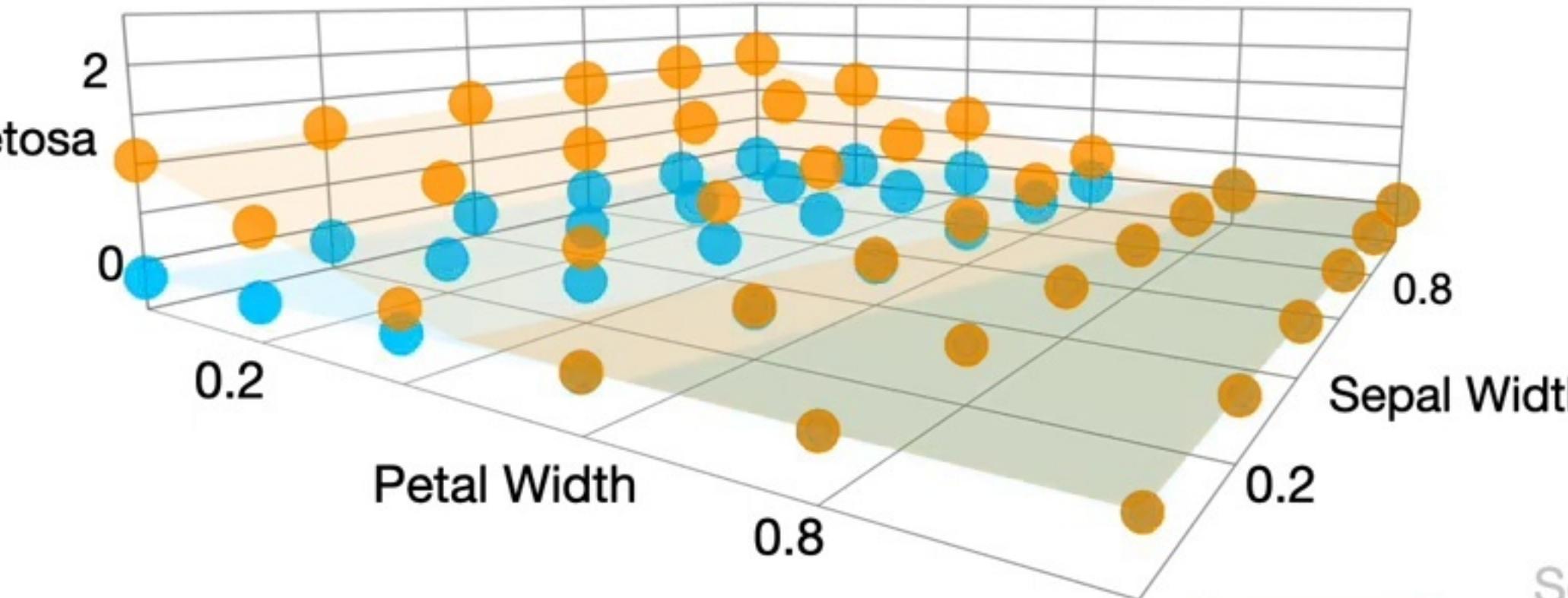
Now we do the exact same thing for the connections to the bottom node in the **Hidden Layer**.

Setosa  
 $+ 0$  = 

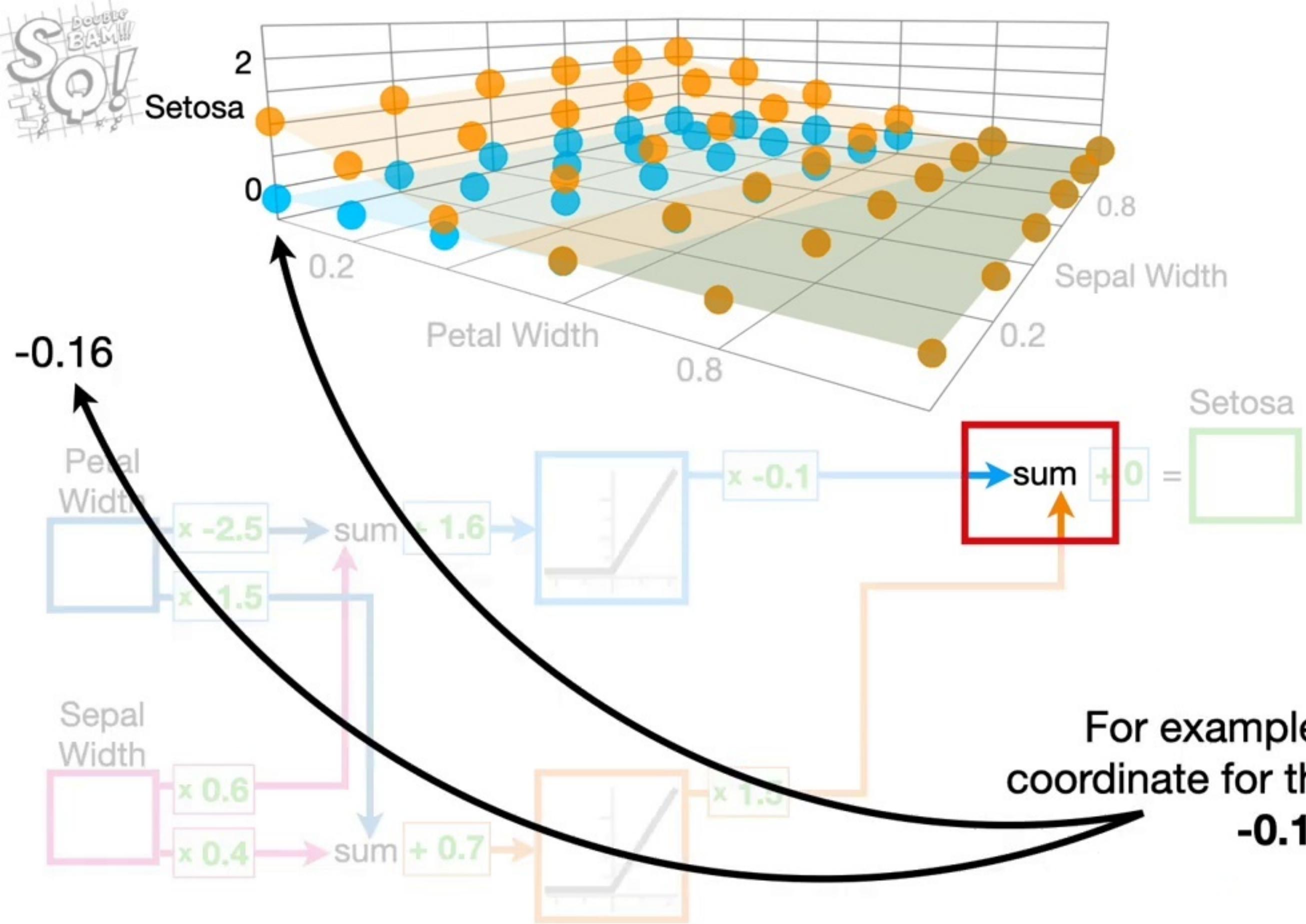


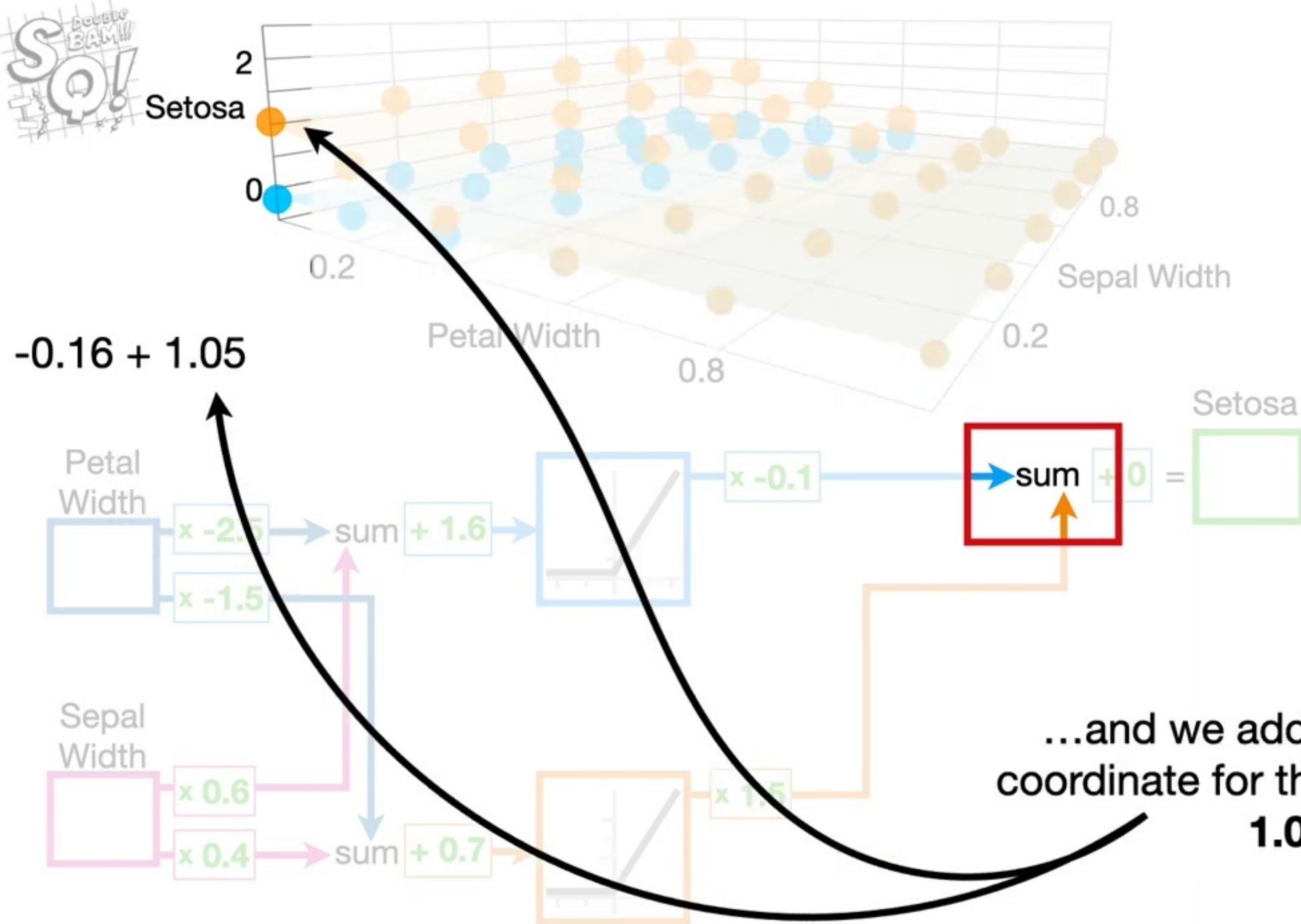
And we end up with this **orange bent surface**, where the bend occurs where the **ReLU Activation Function** set the y-axis values to 0.



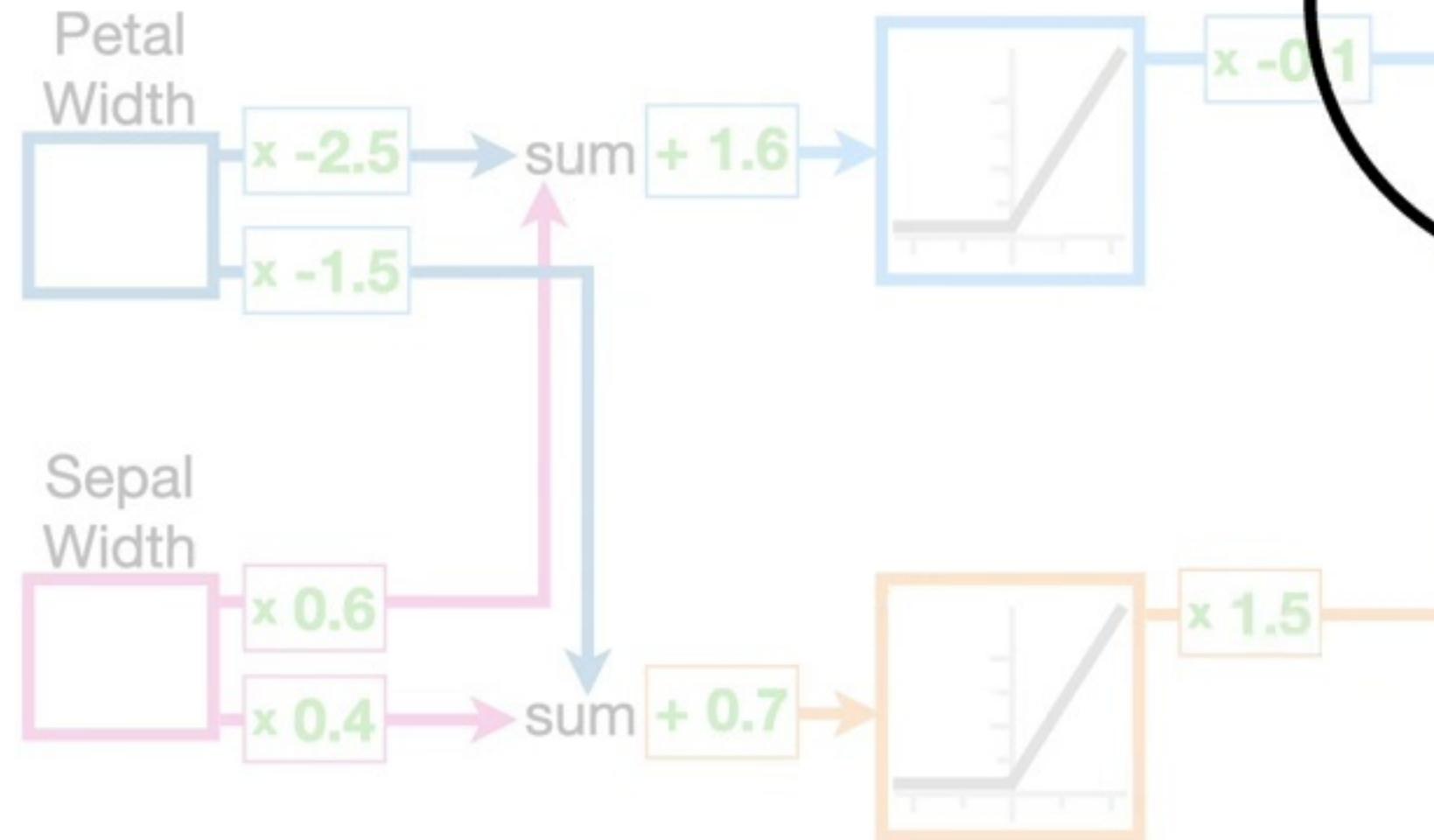
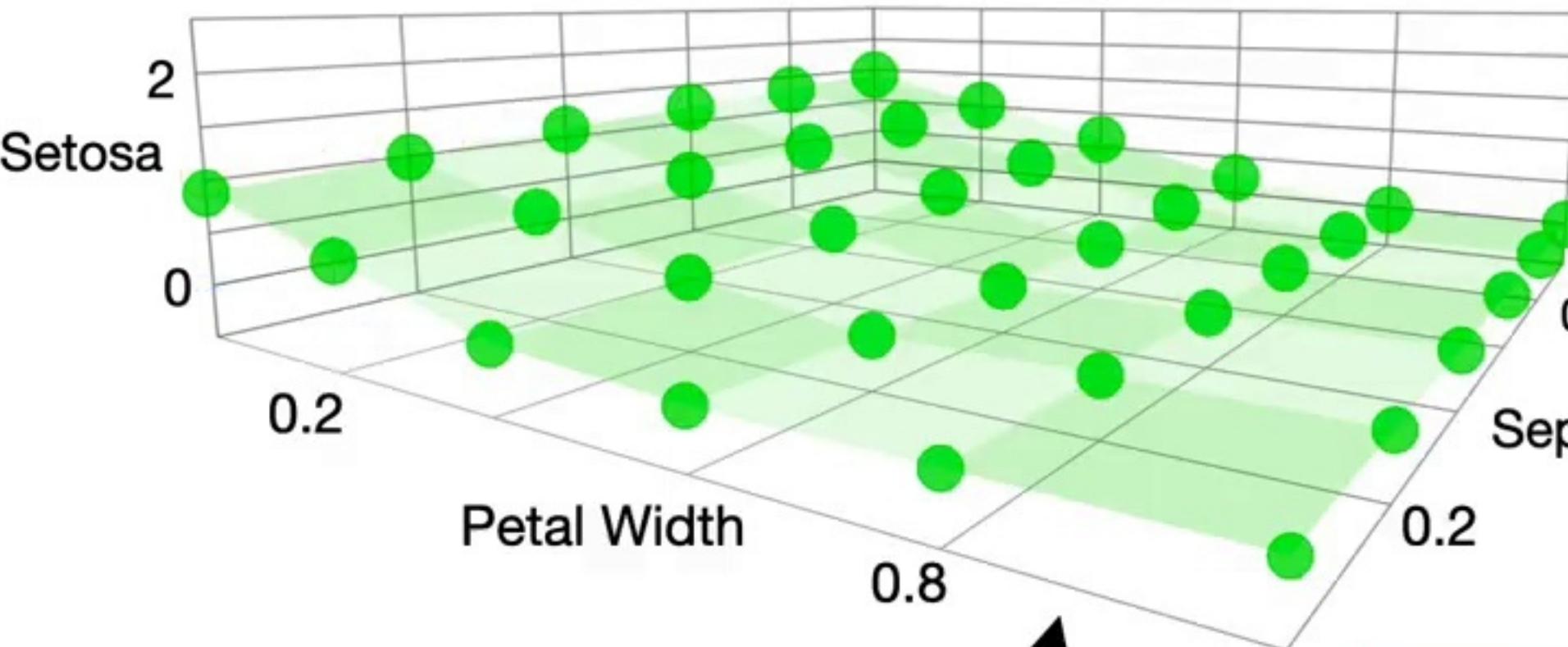


The logo features the letters 'S' and 'Q!' in a large, bold, outlined font. The 'S' is on top and the 'Q!' is below it. To the right of the 'Q!' is the word 'BAM!!' in a smaller, stylized font. The entire logo is set against a background of horizontal grid lines.

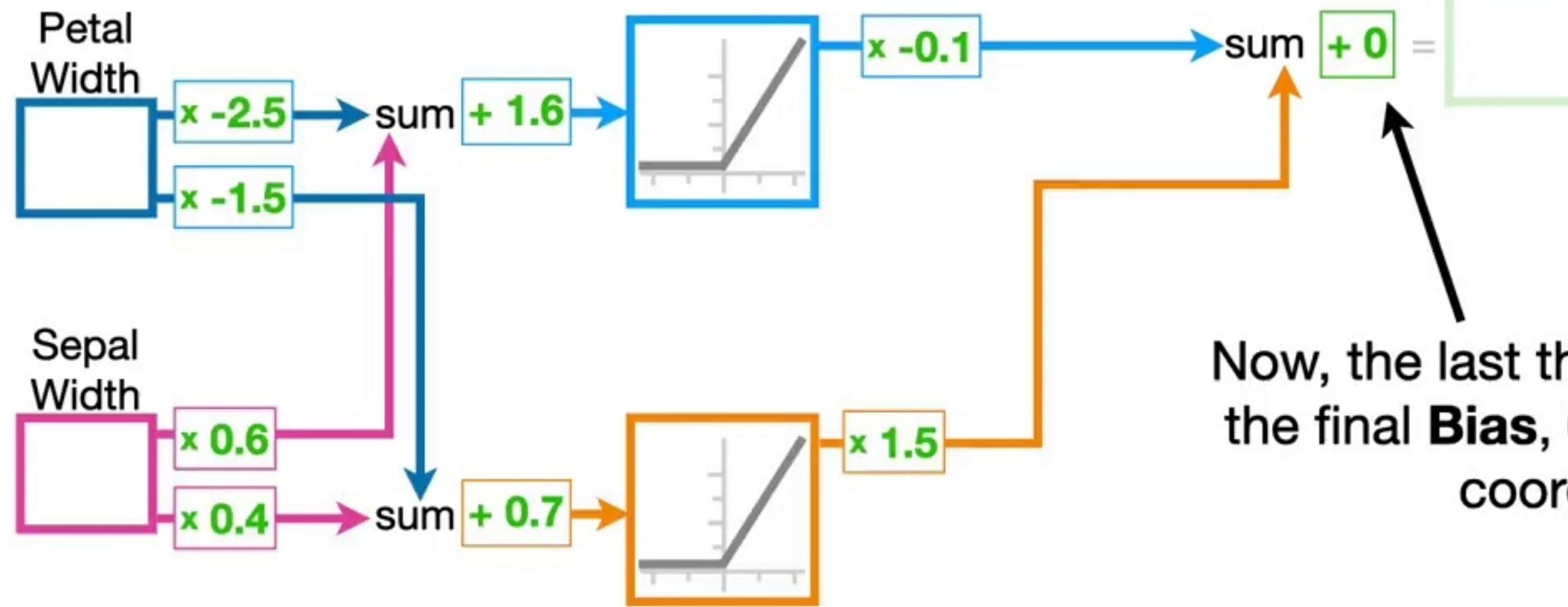
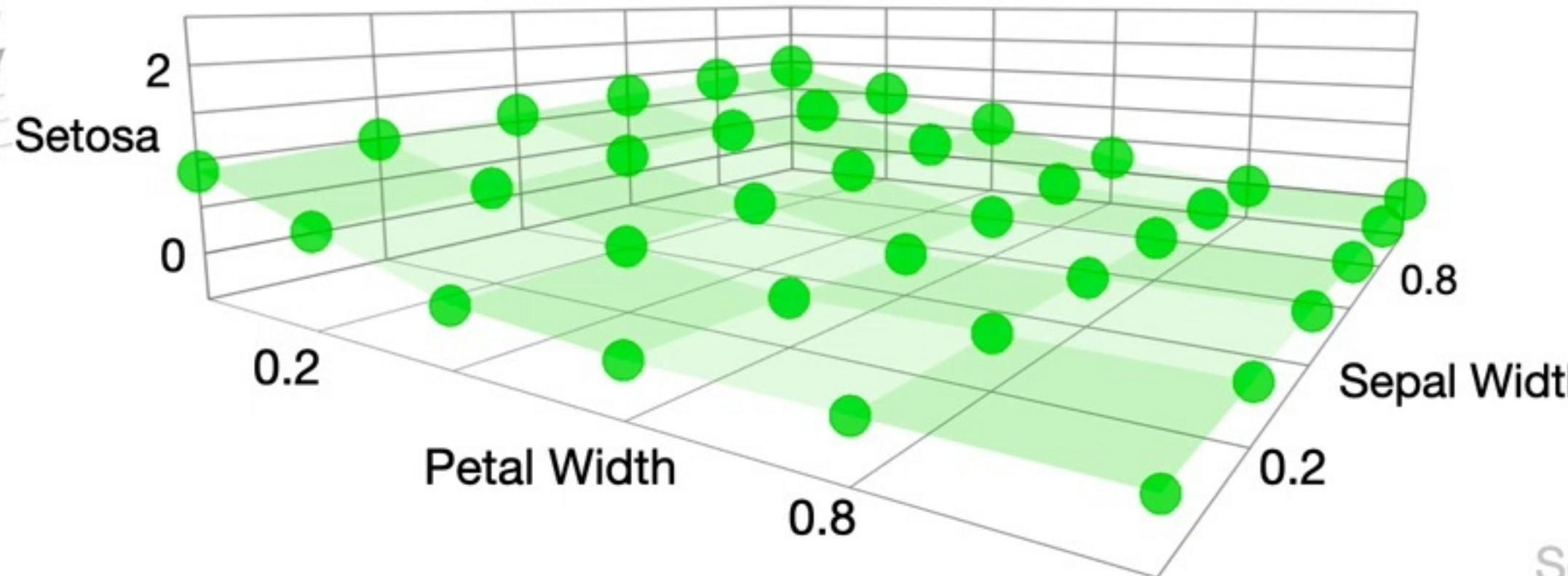




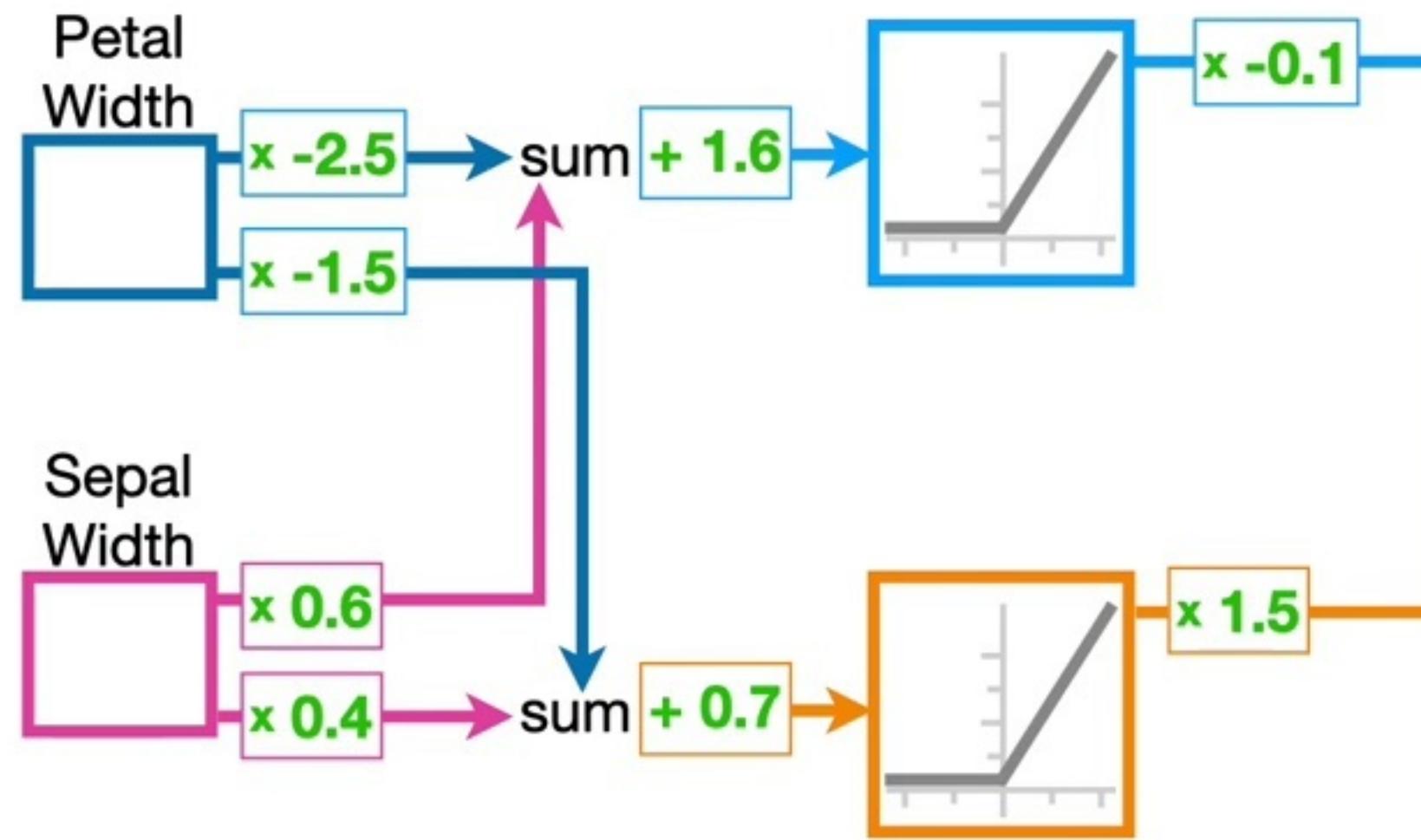
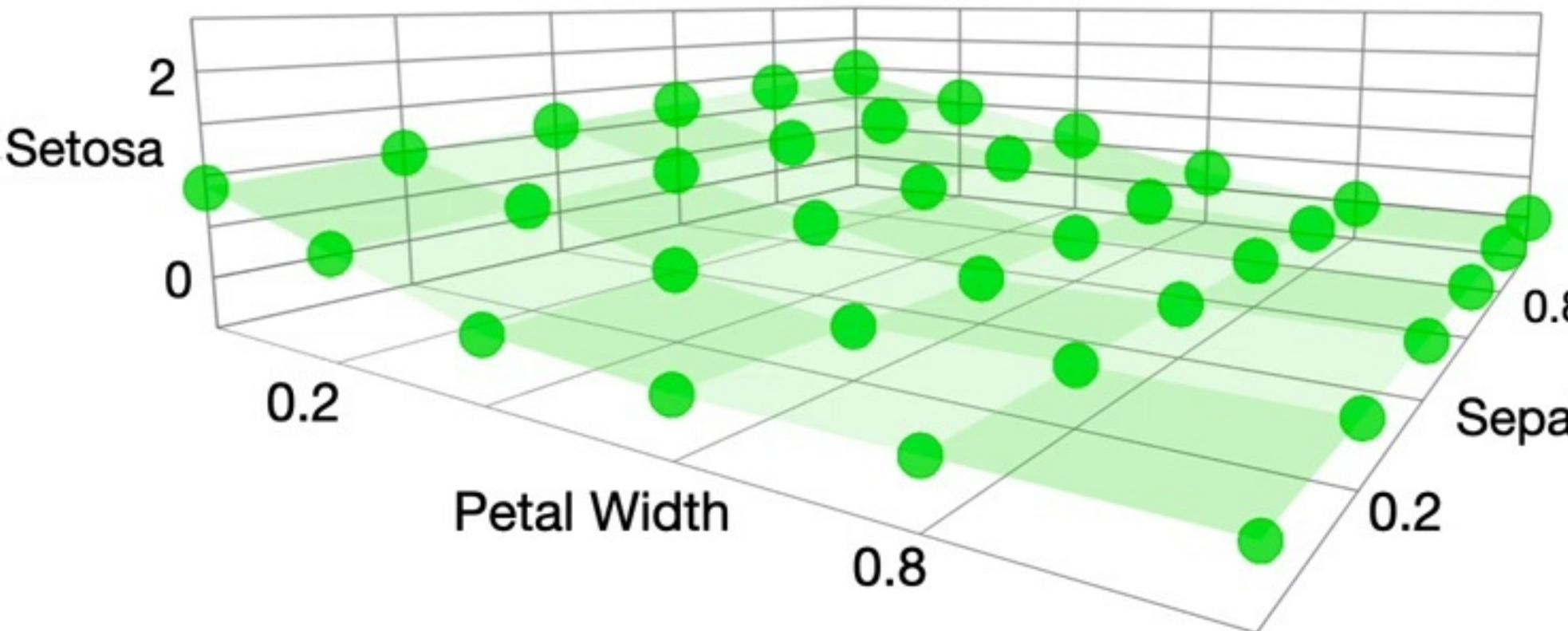
**SQ!**  
double  
BAM!!



Anyways, we do that for every single point and, ultimately, we end up with this **green crinkled surface**.

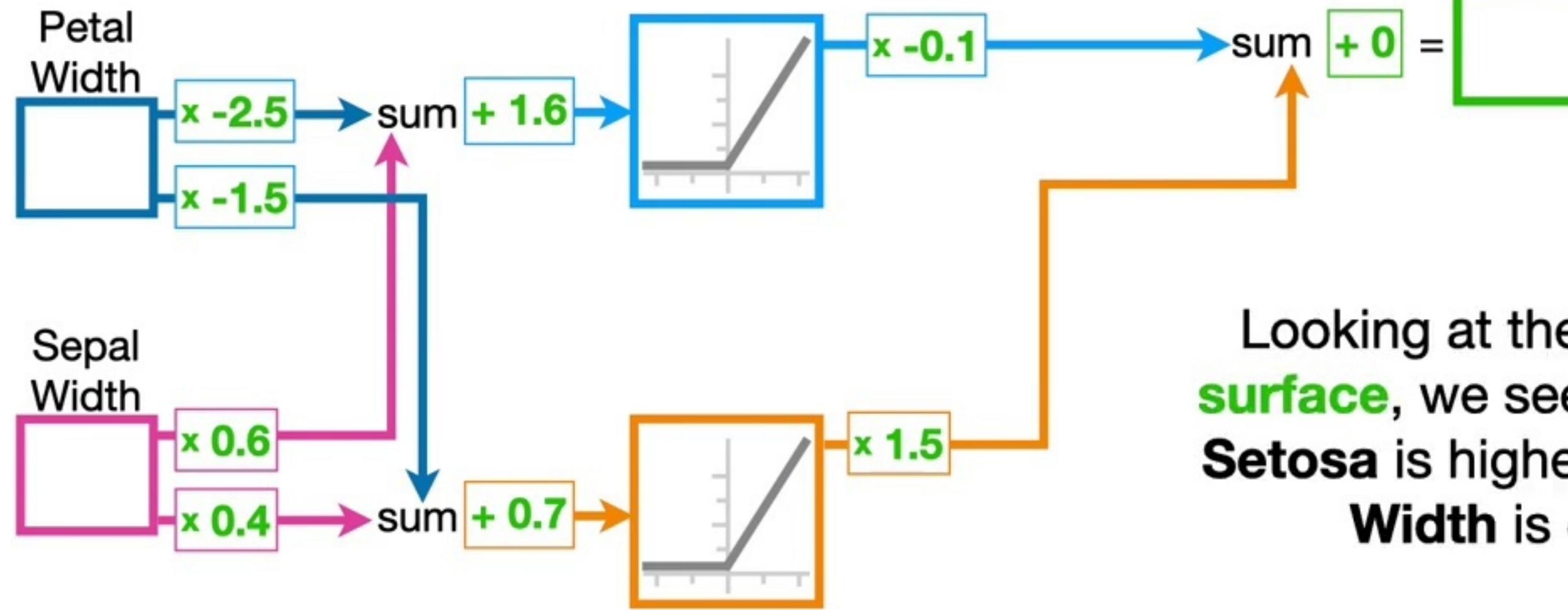
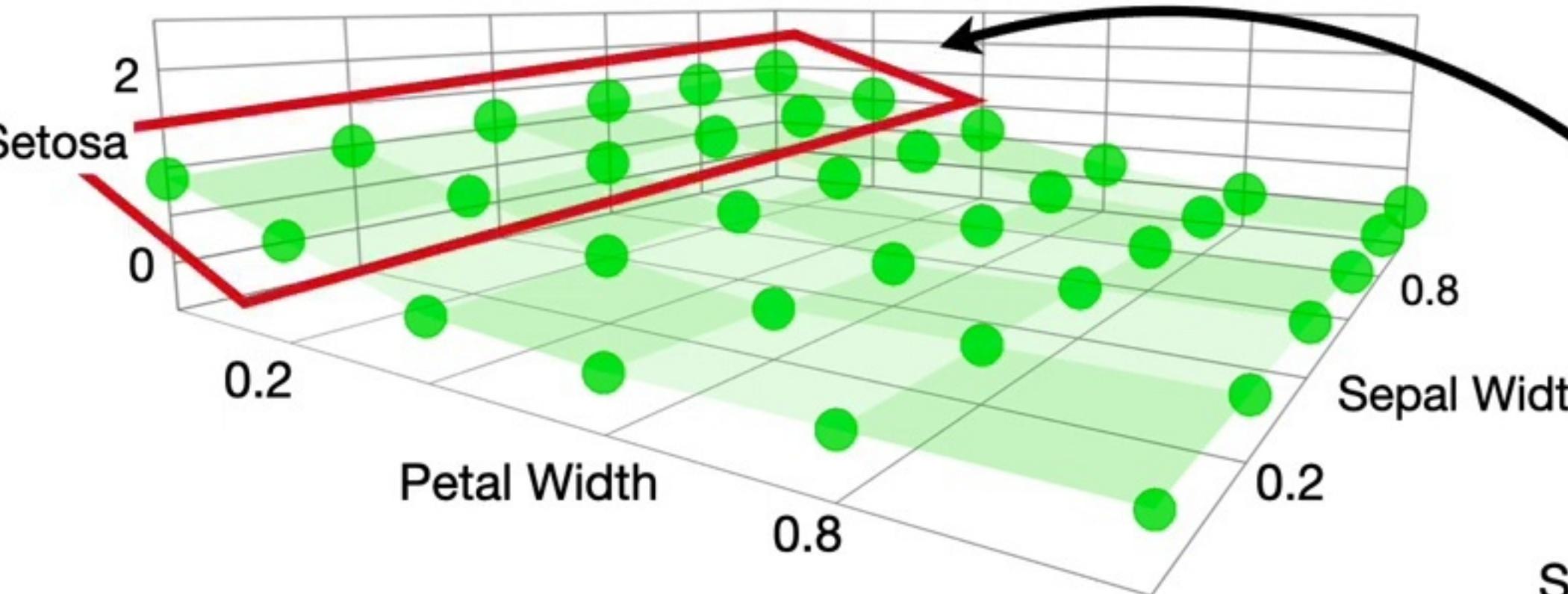


**SQ!**  
double  
BAM!!

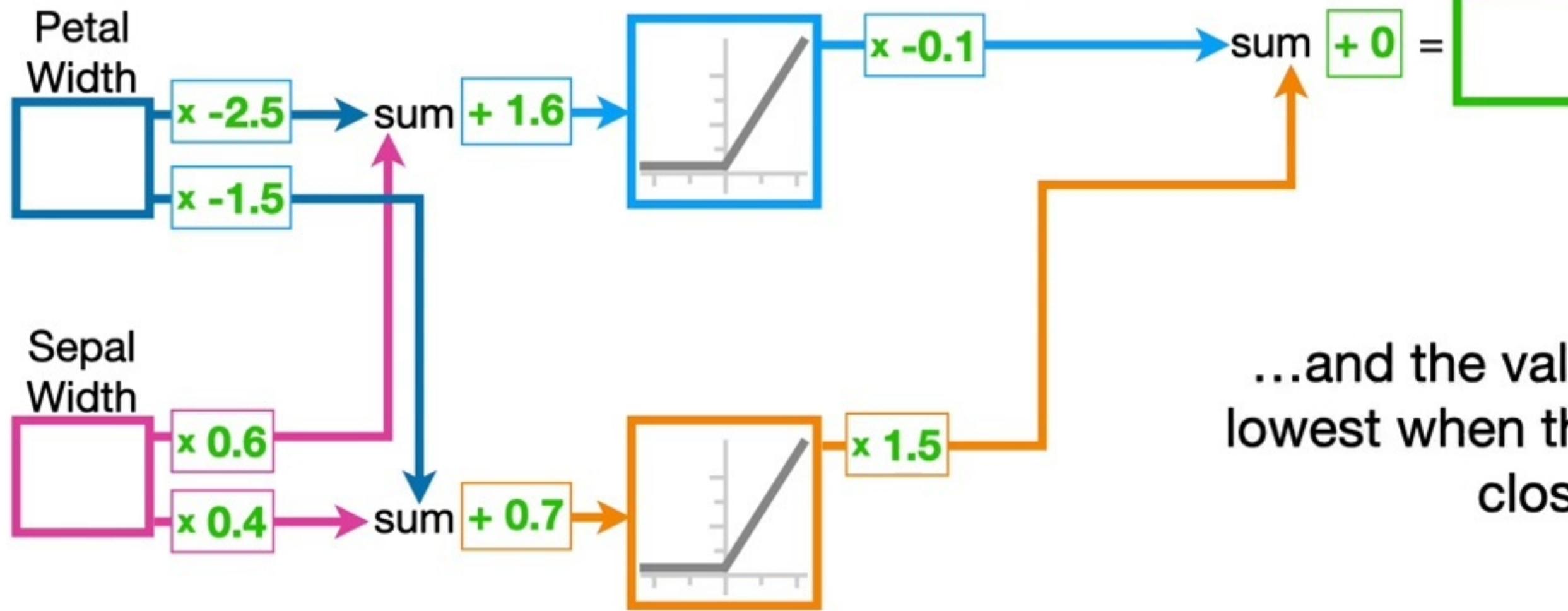
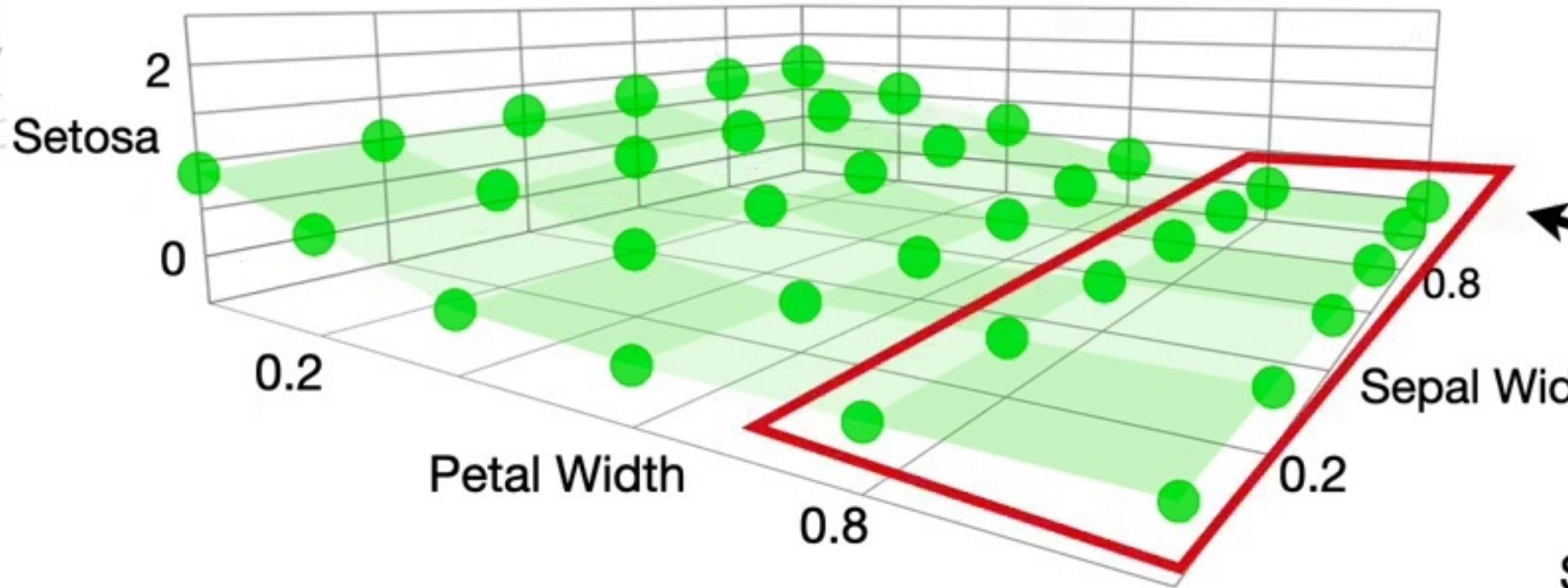


And since adding **0** doesn't change the **green crinkled surface**, this is the output for **Setosa**.

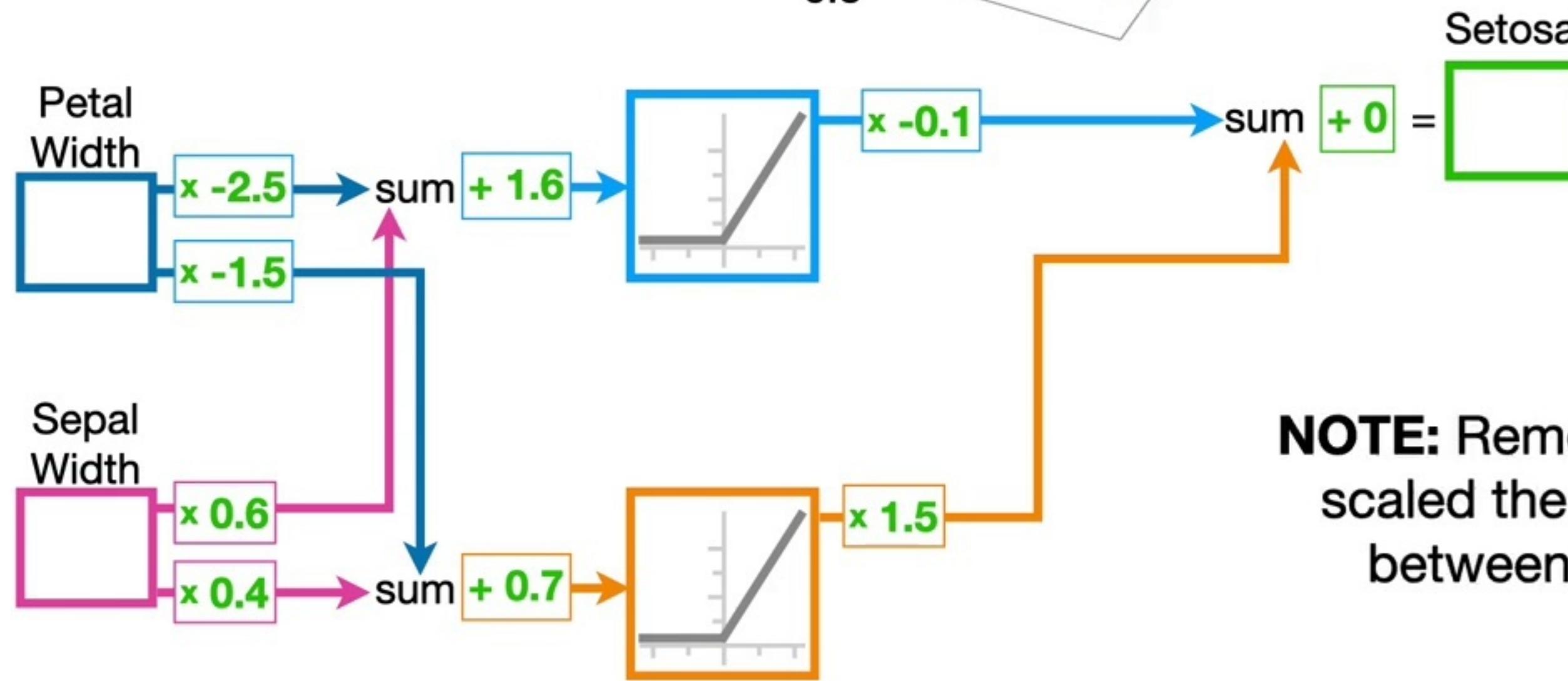
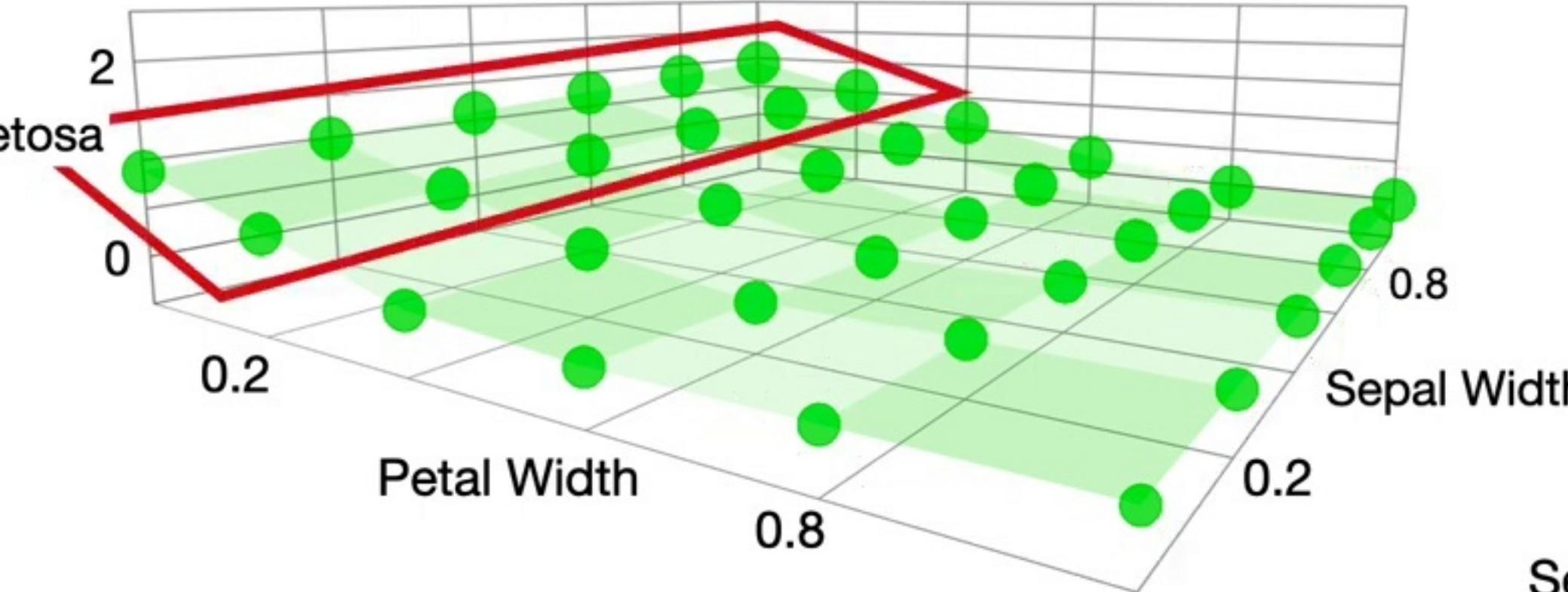
**SQ!**  
double  
BAM!!



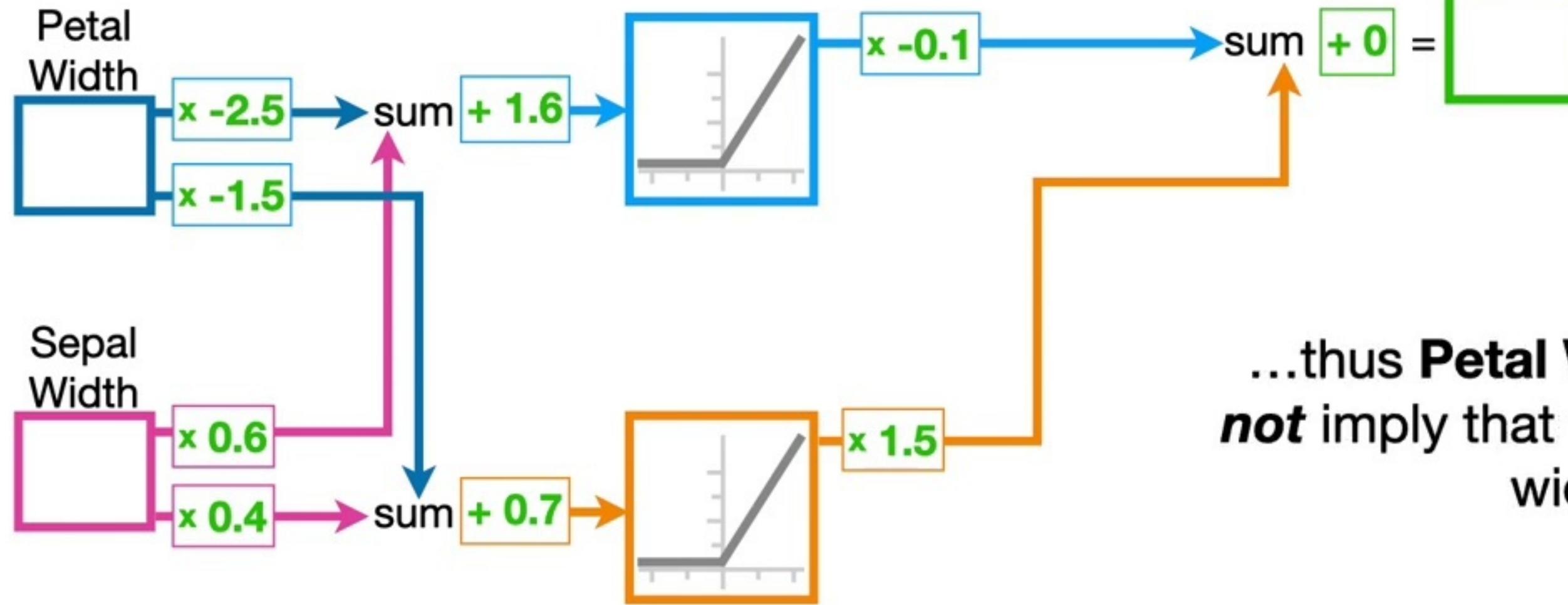
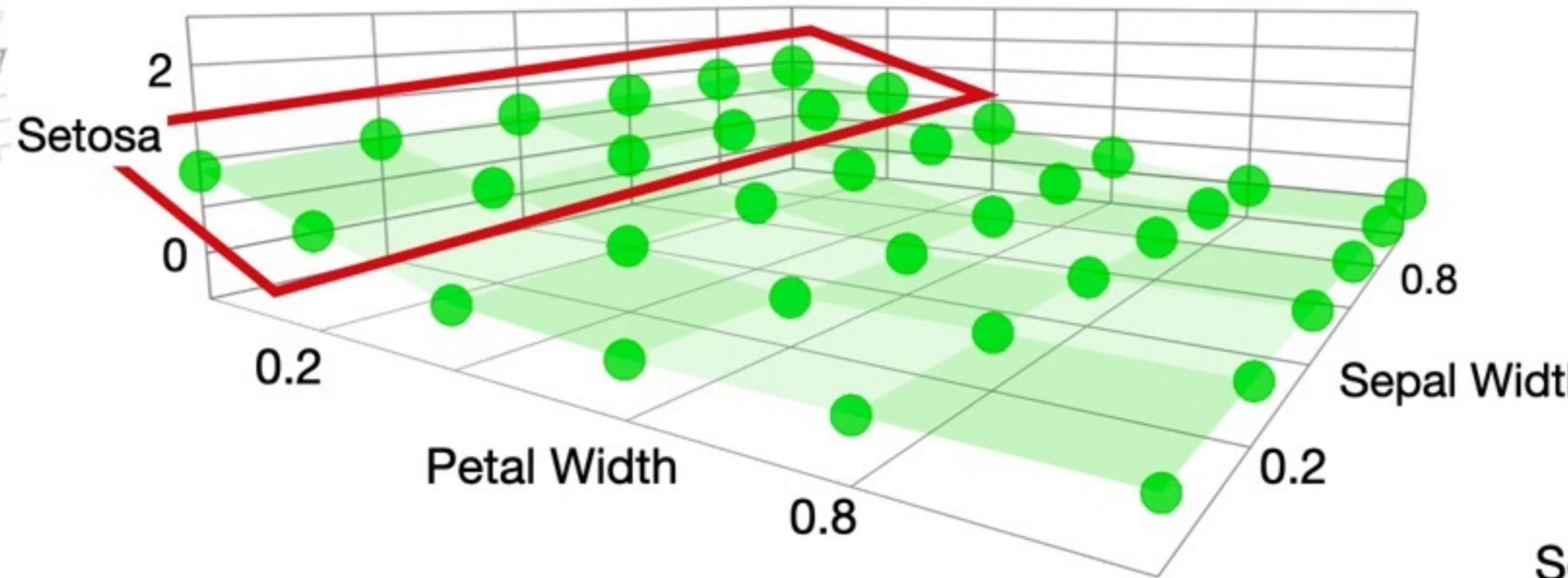
Looking at the **green crinkled surface**, we see that the value for **Setosa** is highest when the **Petal Width** is close to 0...



...and the value for **Setosa** is  
lowest when the **Petal Width** is  
close to 1.

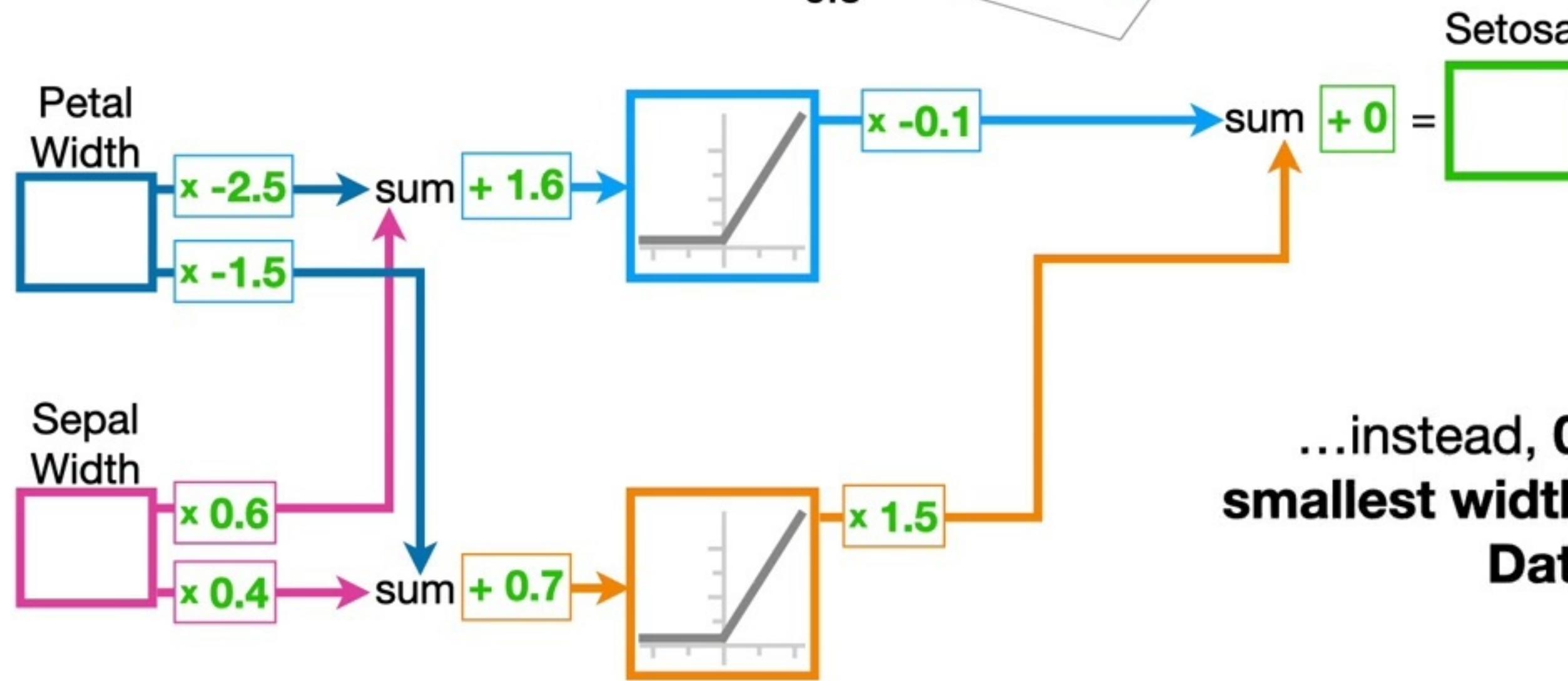
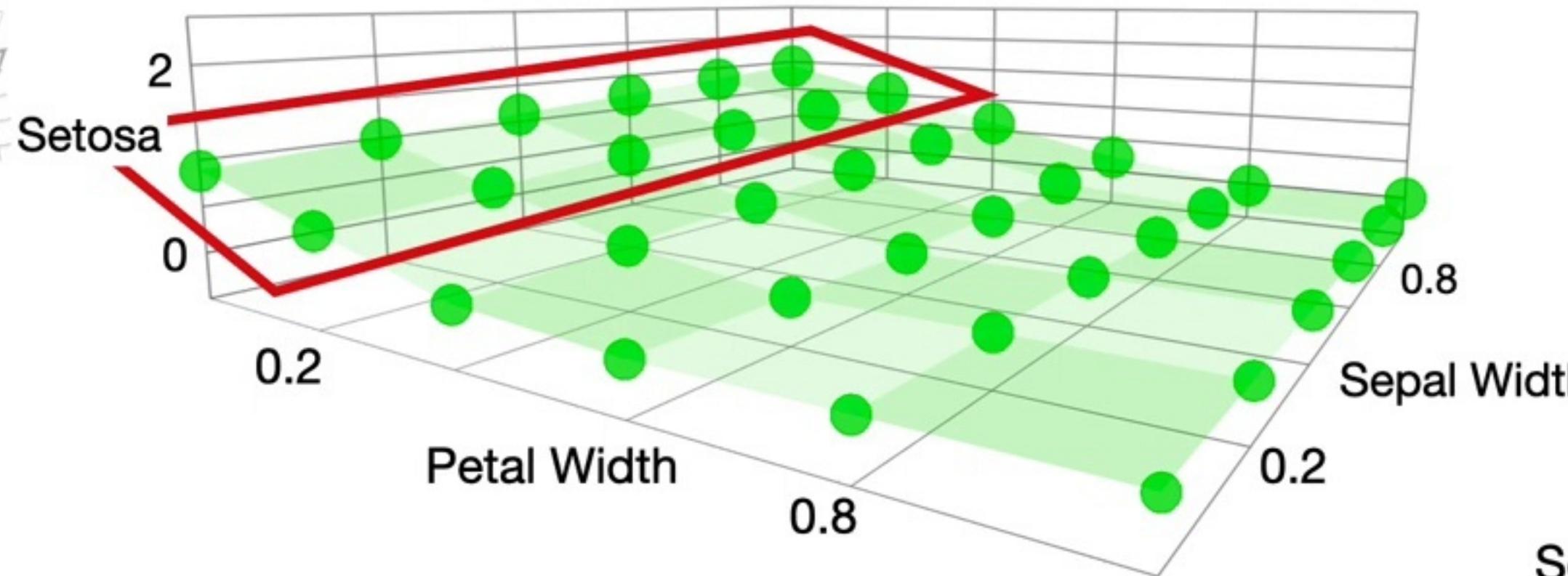


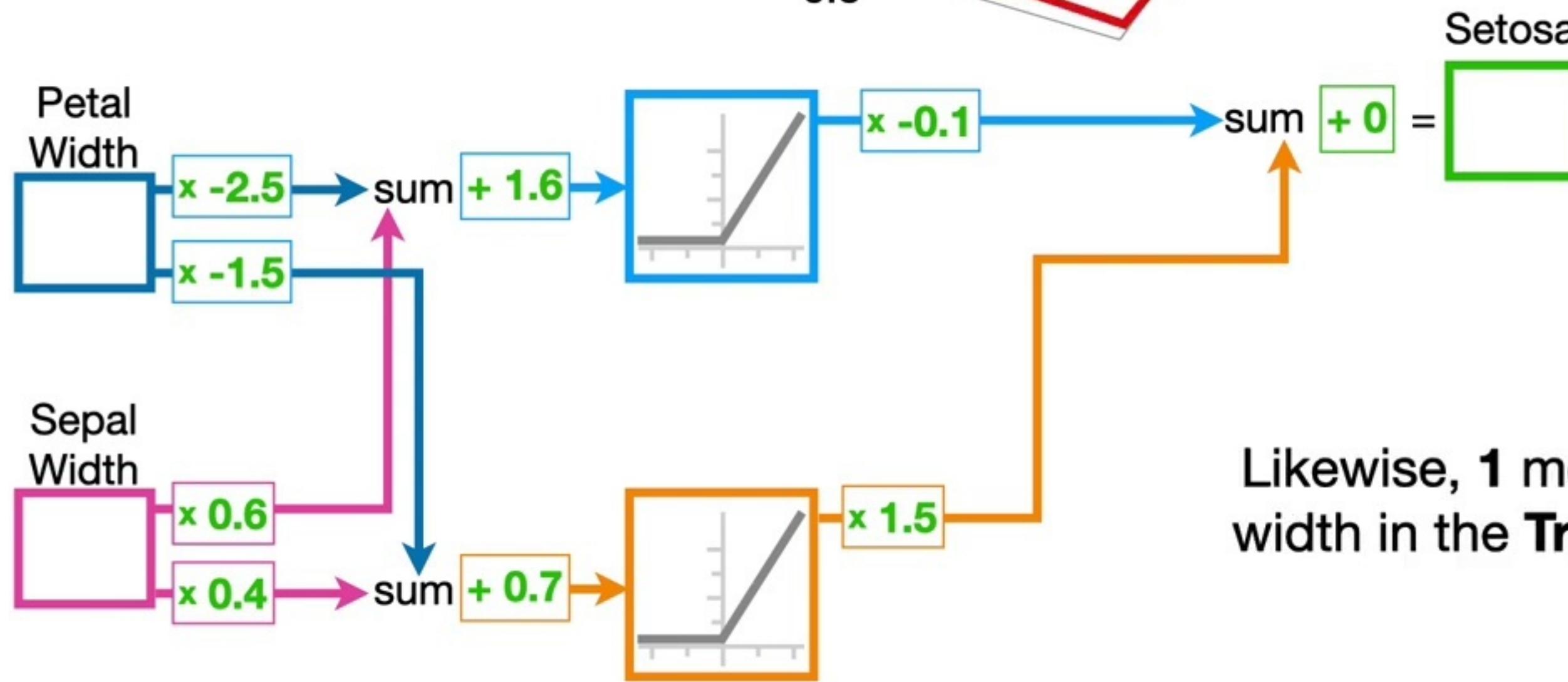
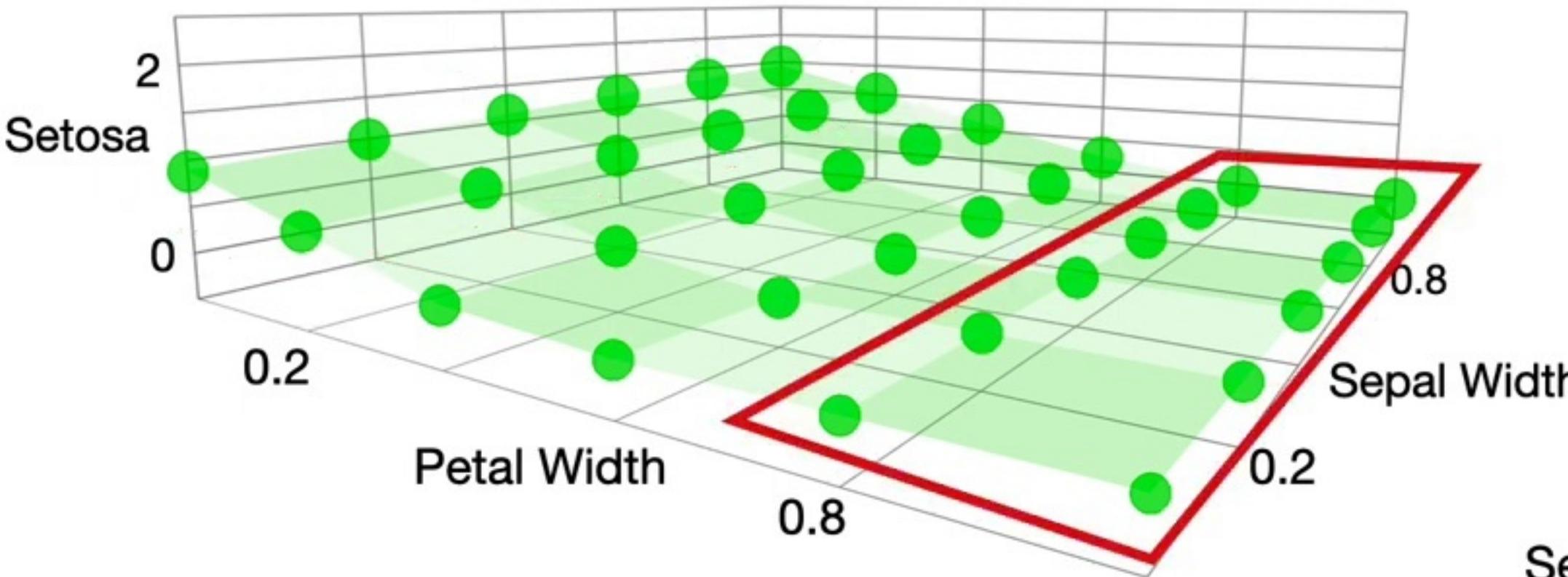
**SQ!**  
double  
BAM!!

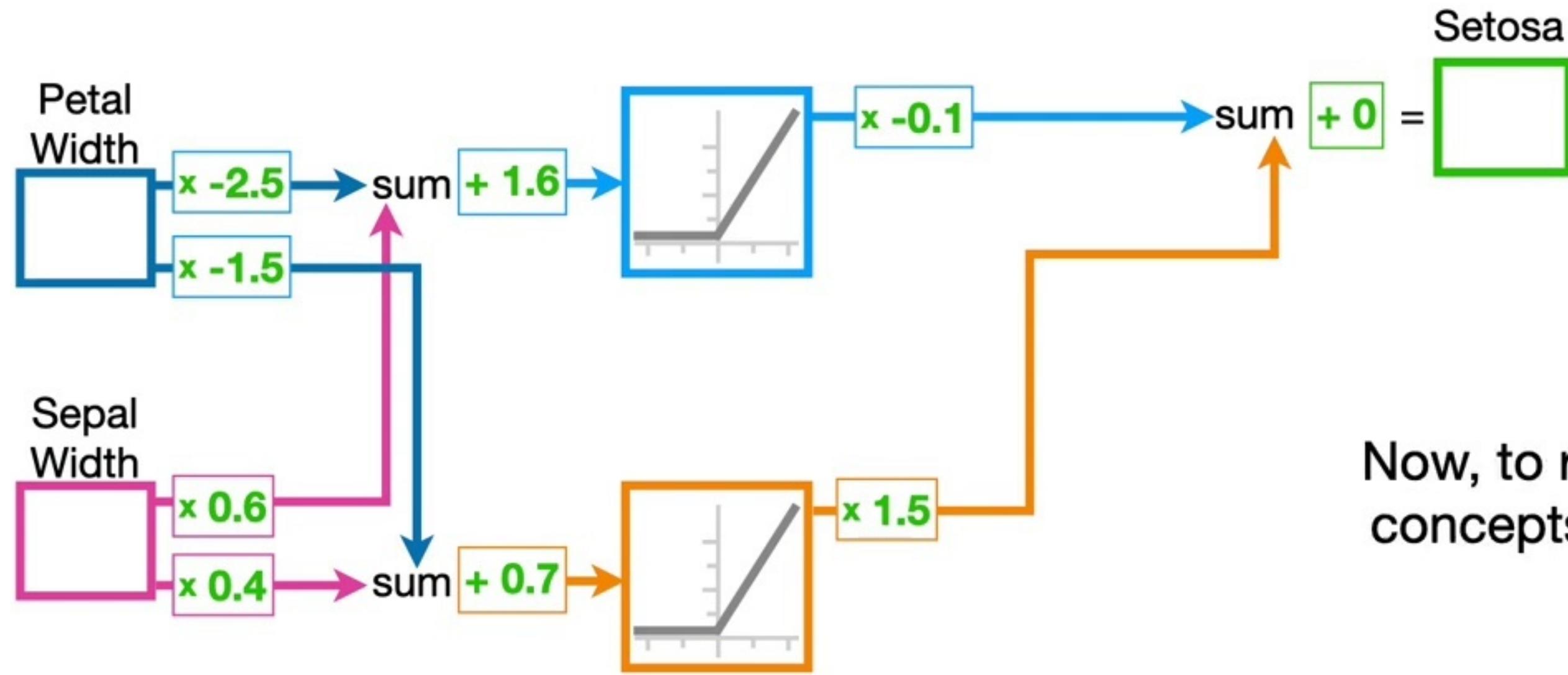




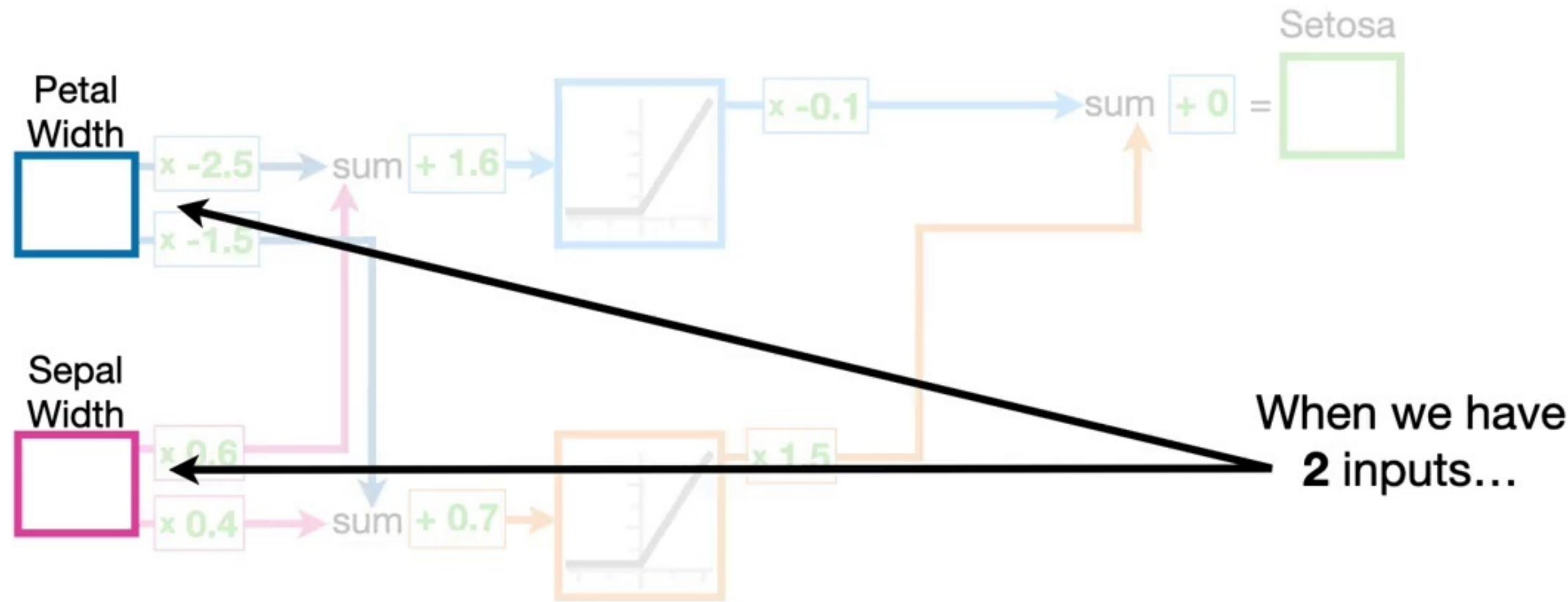
double  
BAM!!

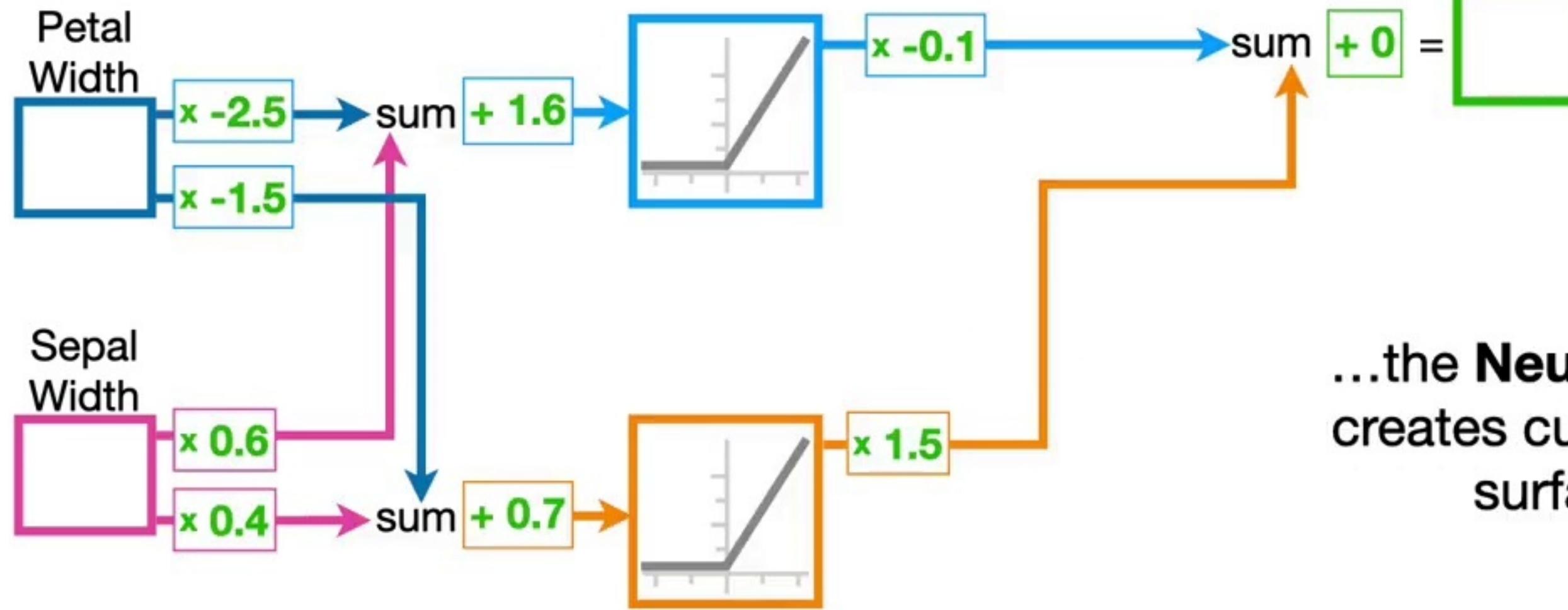
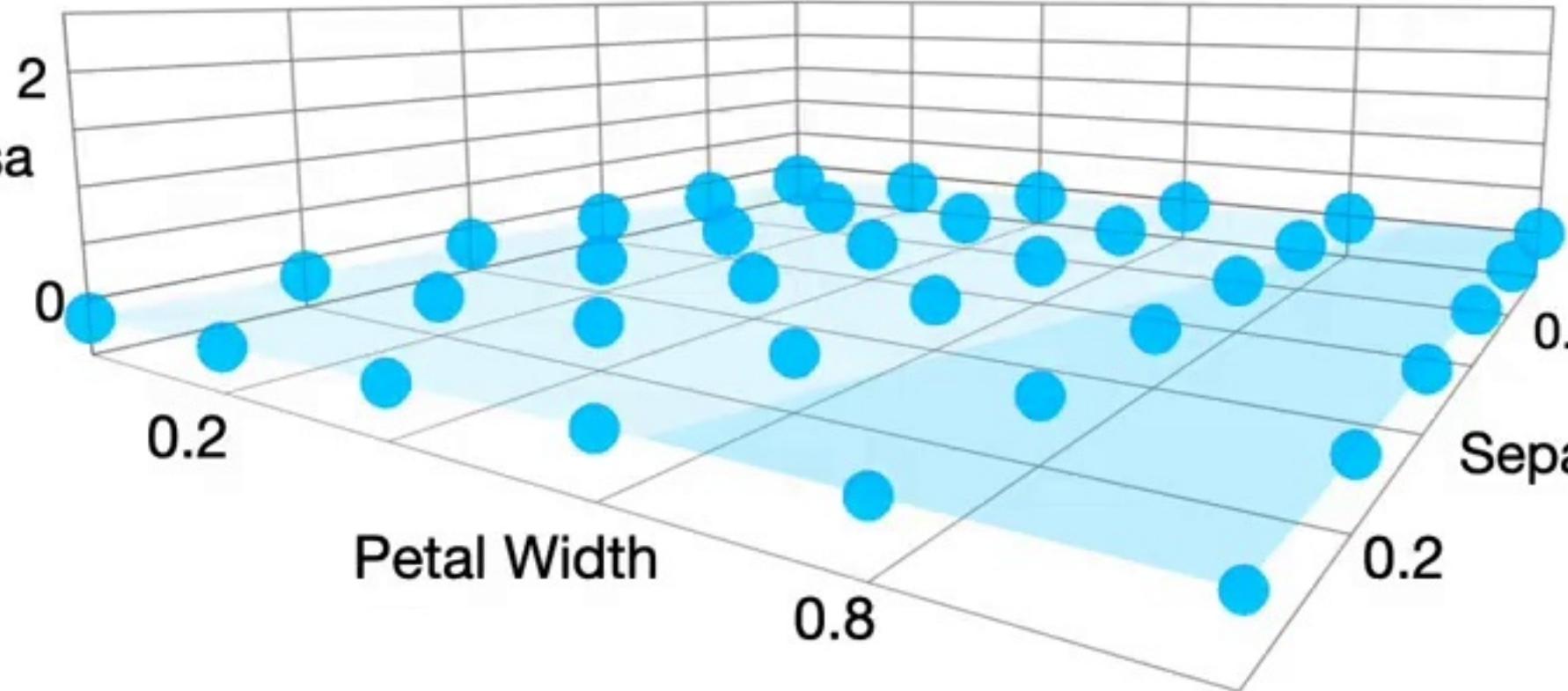




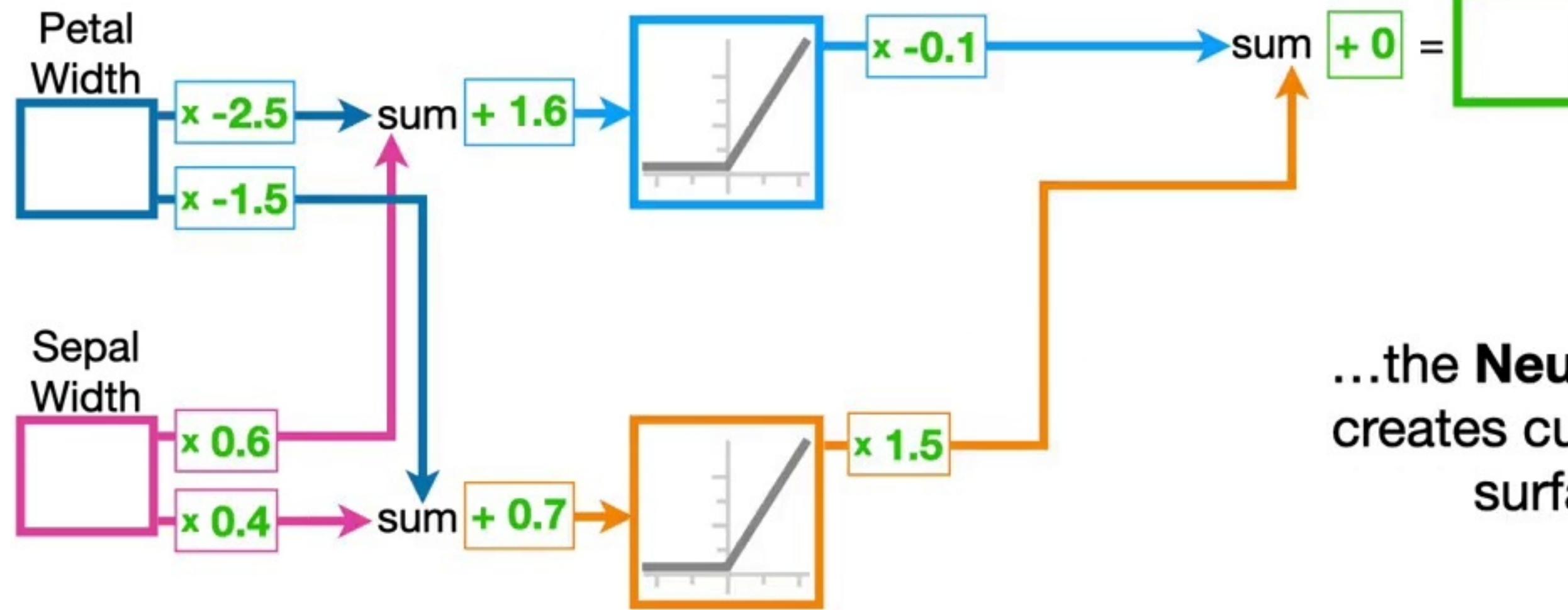
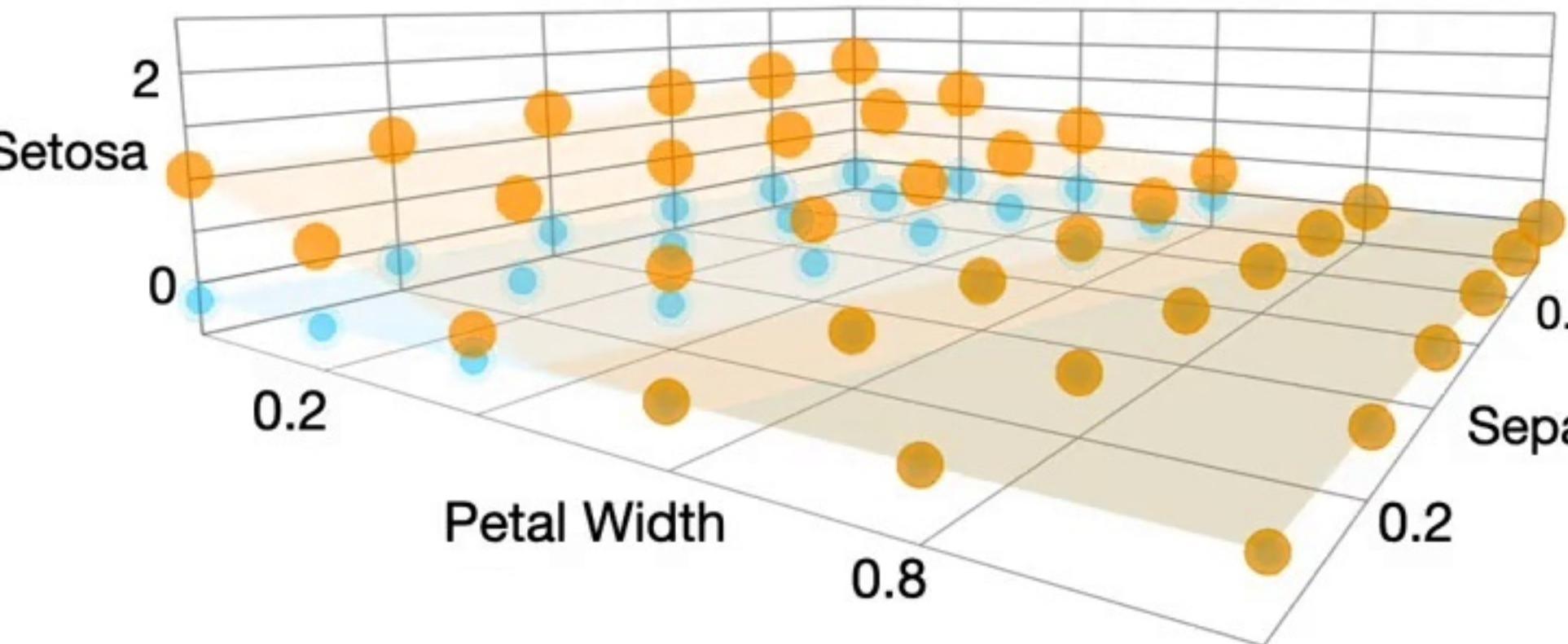


Now, to review the concepts so far...



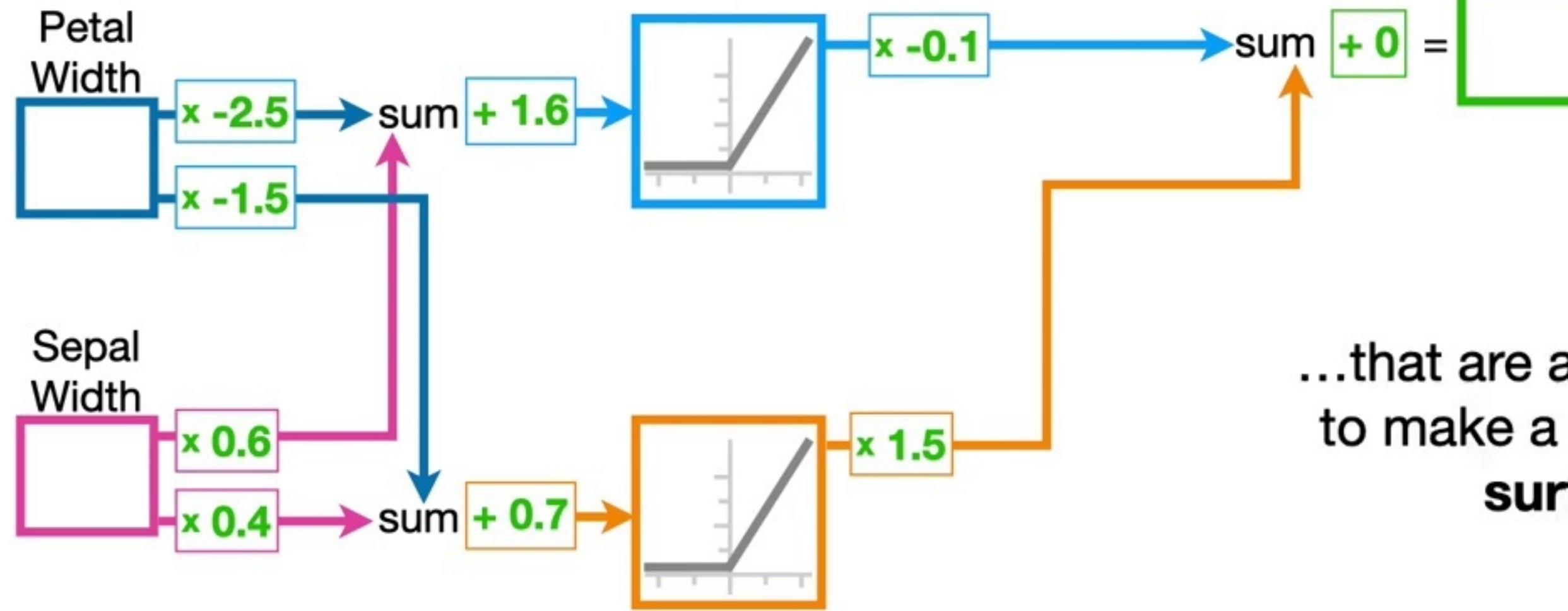
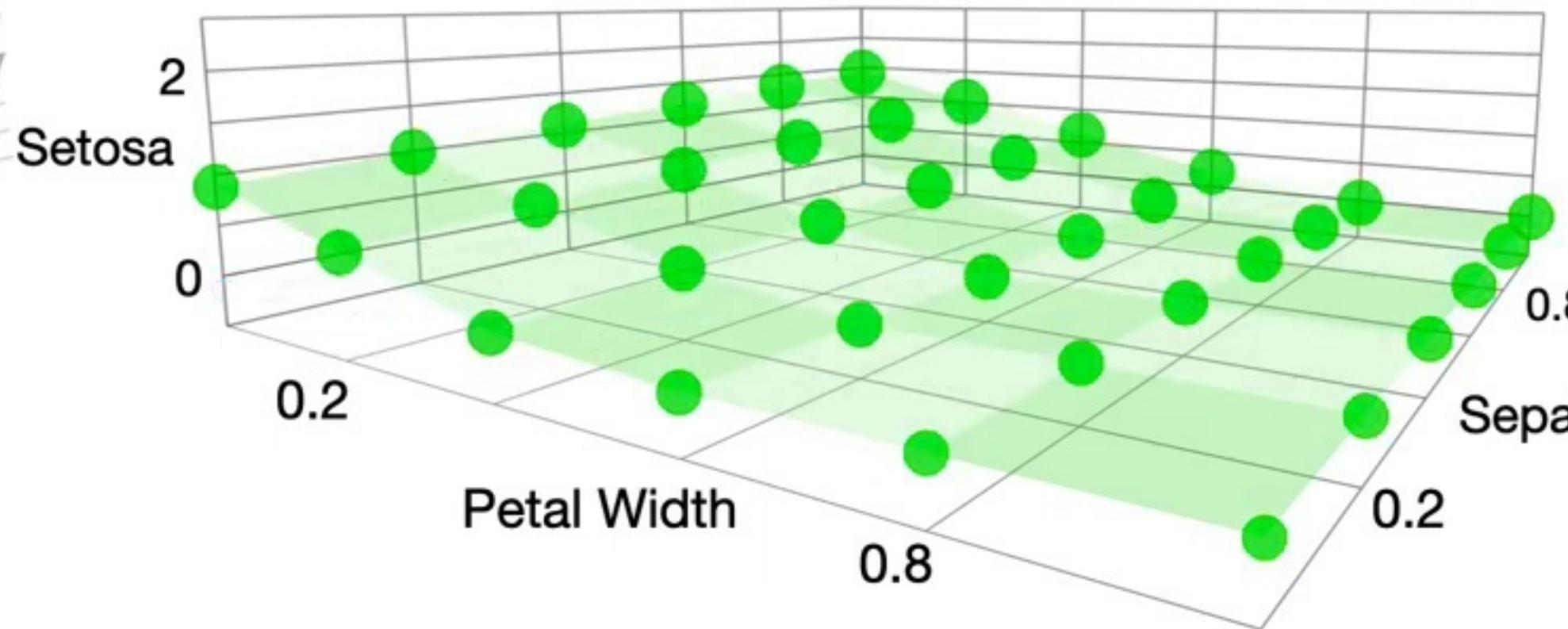


...the **Neural Network**  
creates curved or bent  
surfaces...

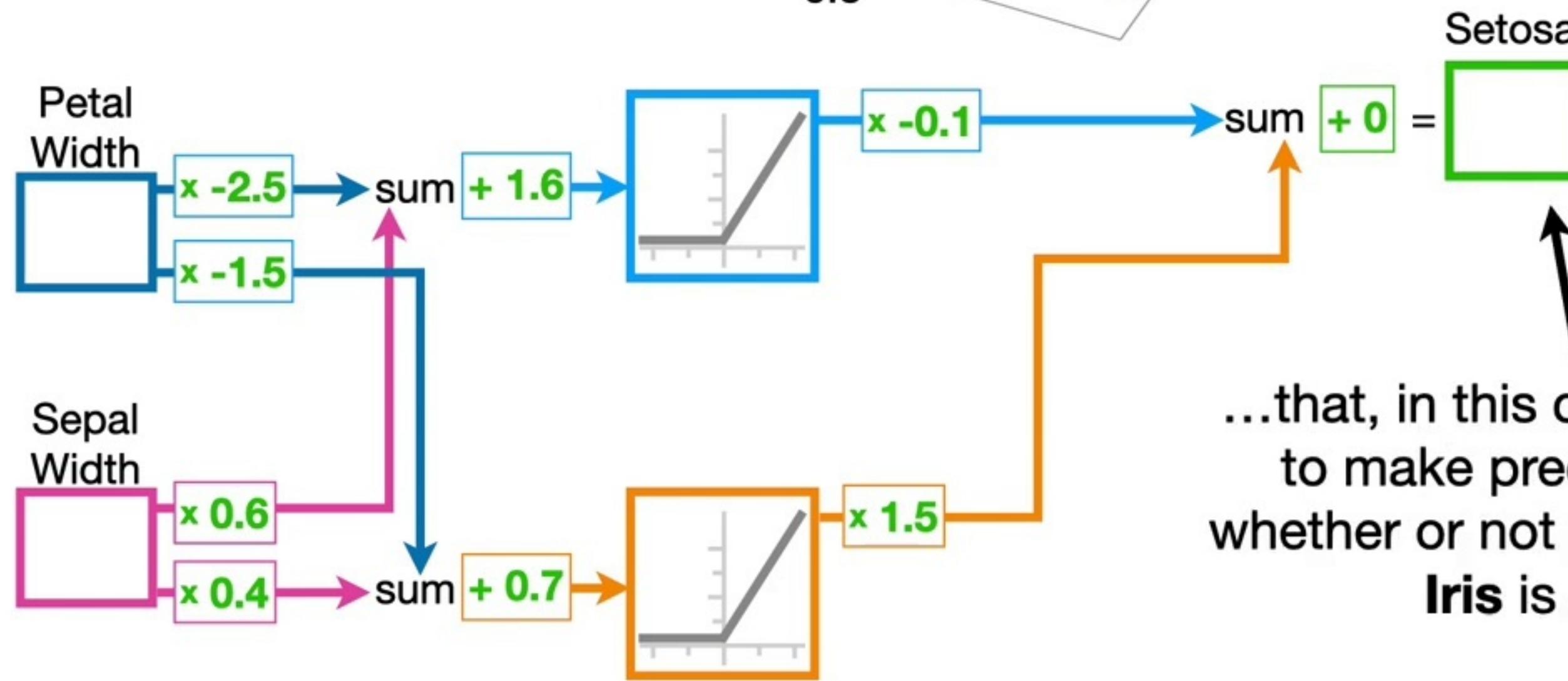
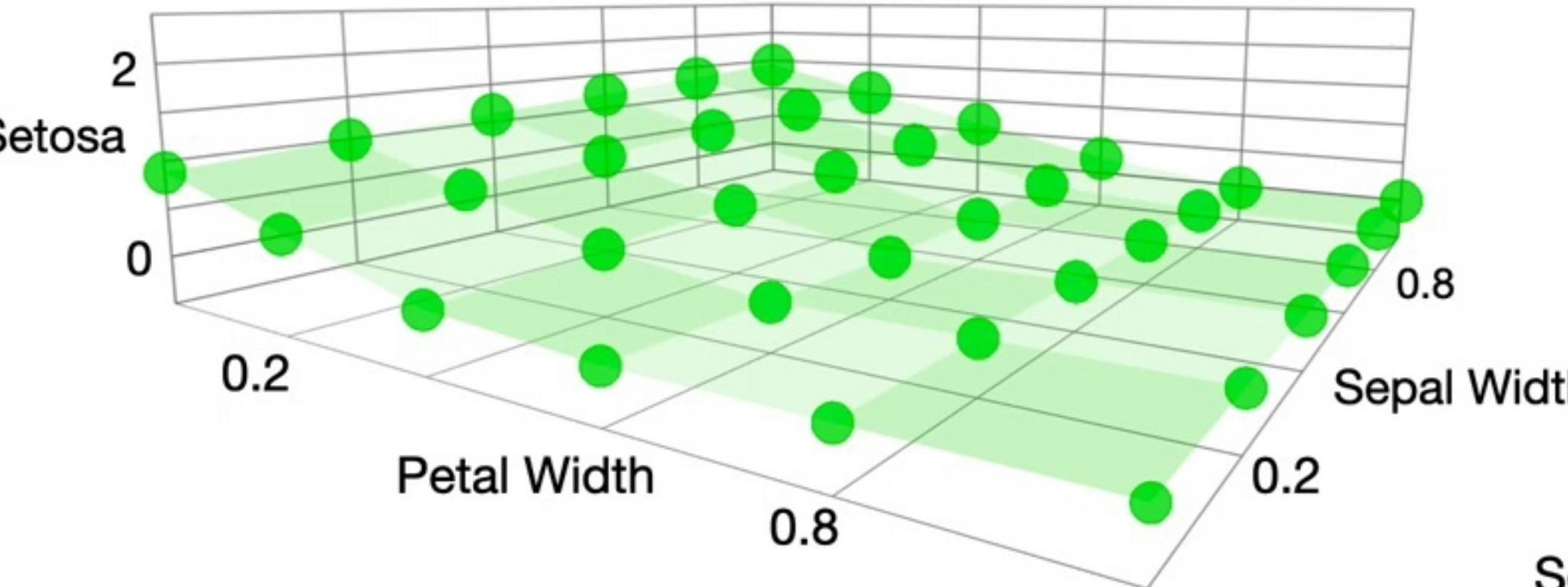


...the **Neural Network**  
creates curved or bent  
surfaces...

**SQ!**  
double  
BAM!!

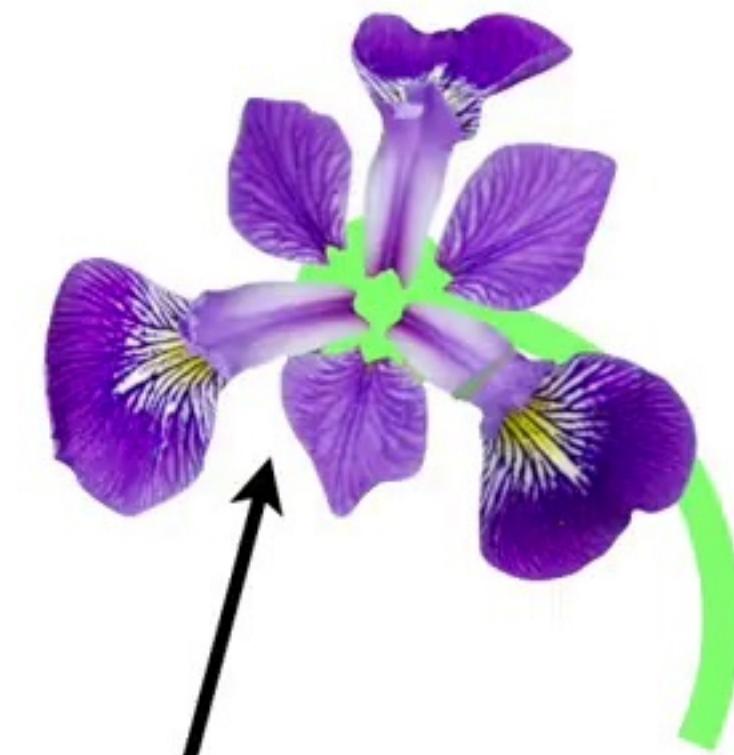
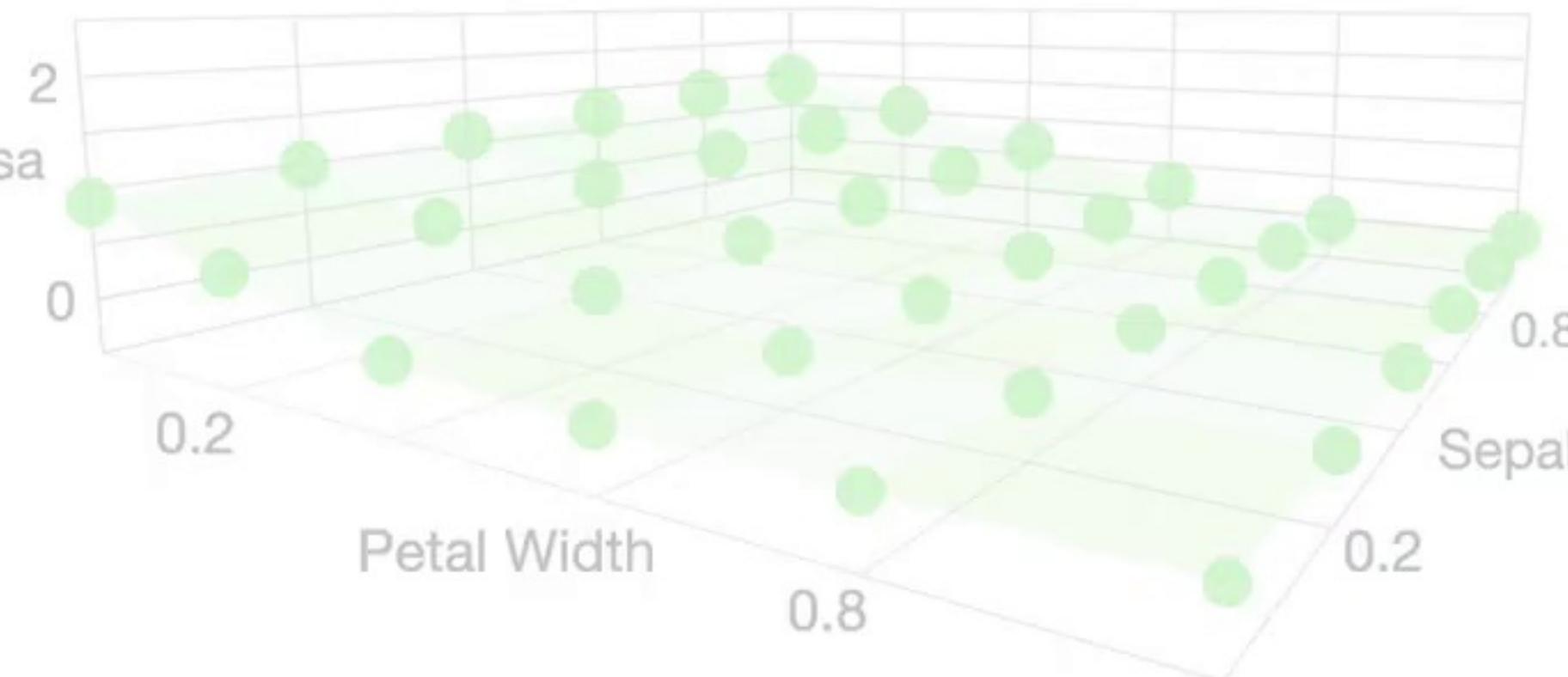


**SQ!**  
double  
BAM!!

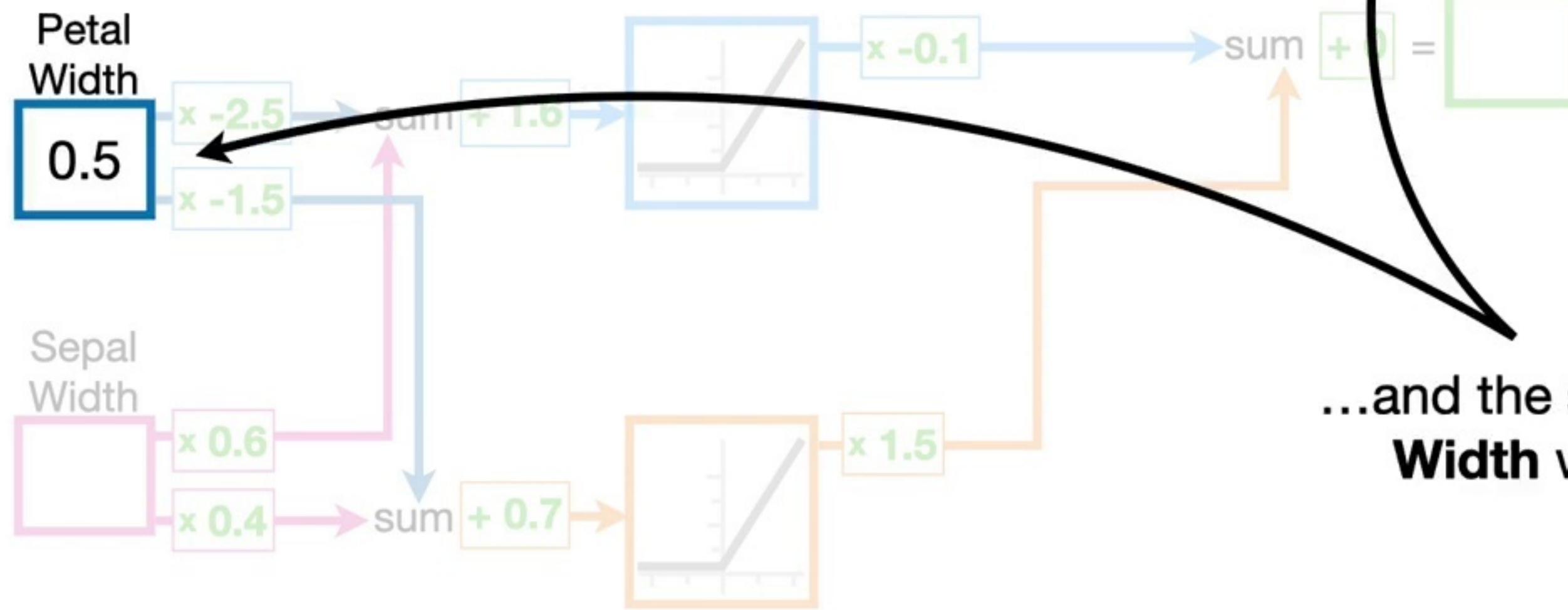
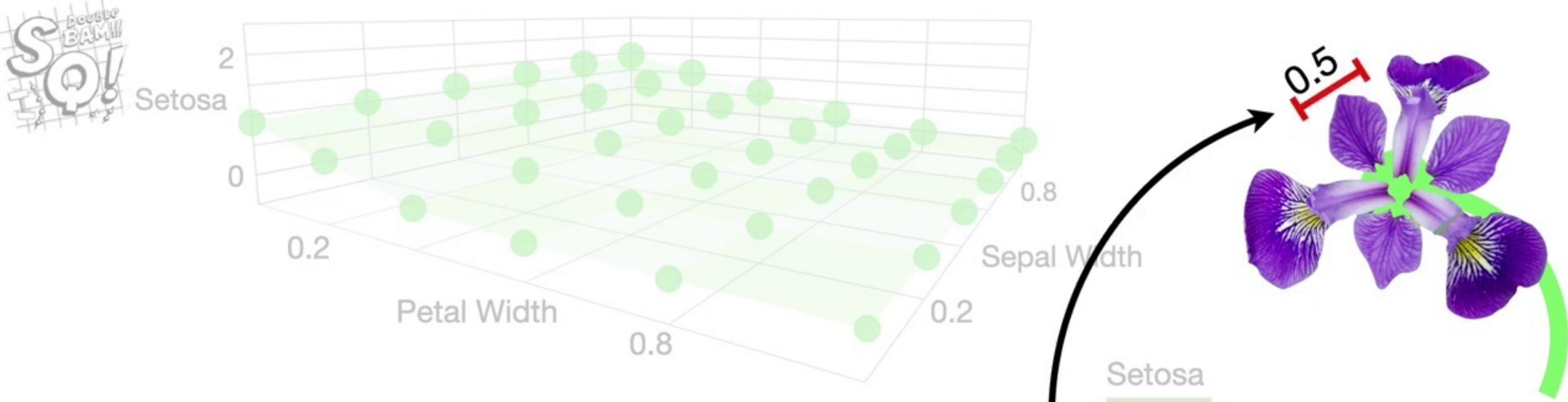


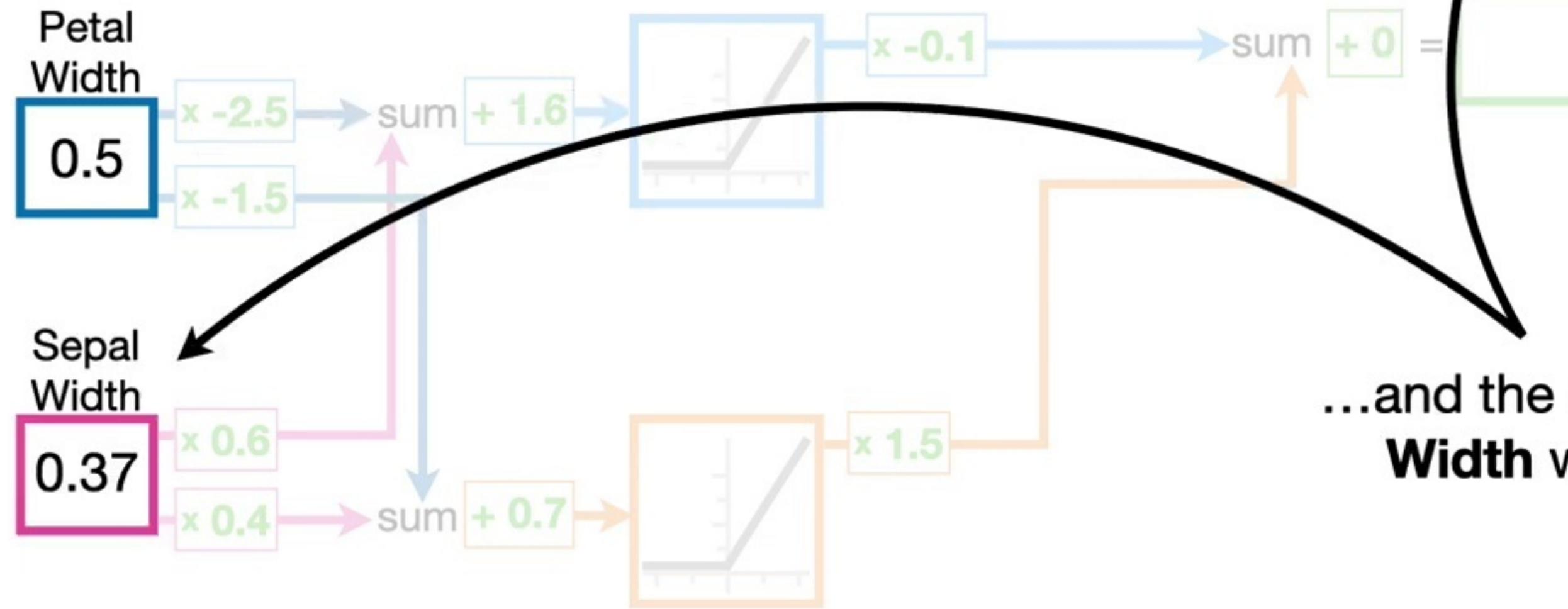
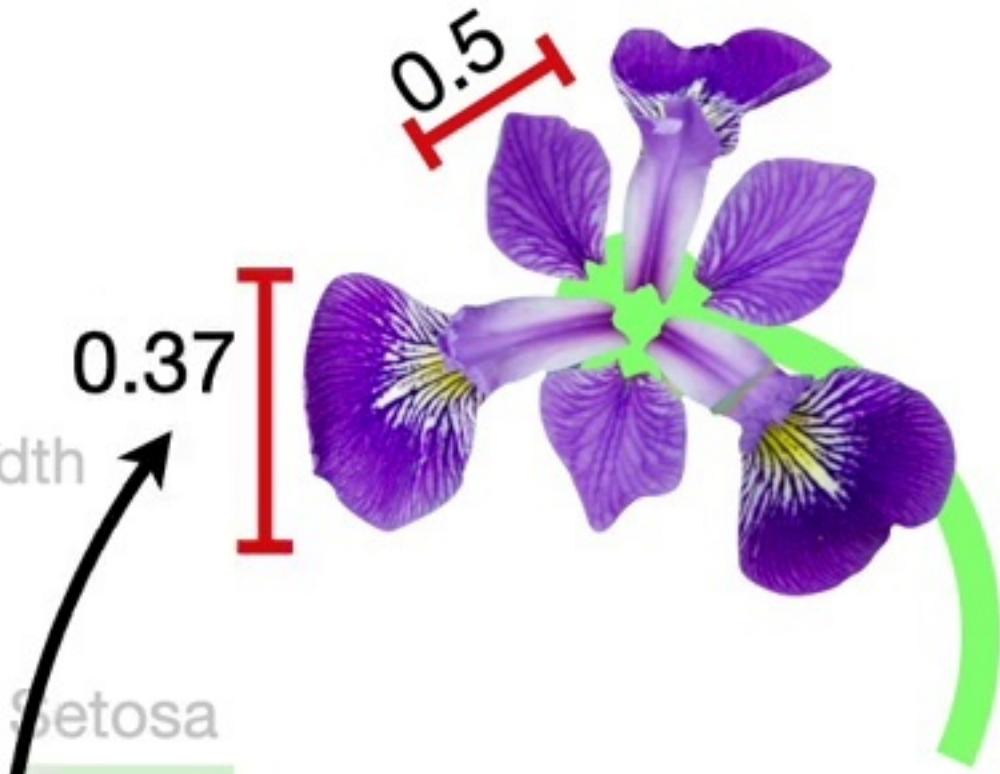
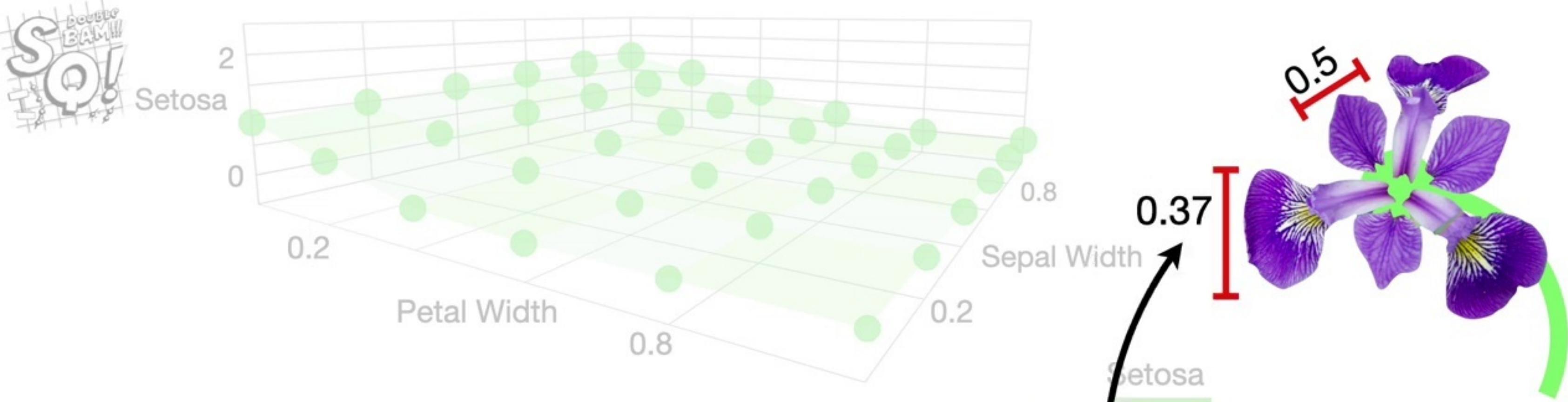
...that, in this case, we can use  
to make predictions about  
whether or not the species of an  
**Iris** is **Setosa**.

double  
BAM!!  
**SQ!**



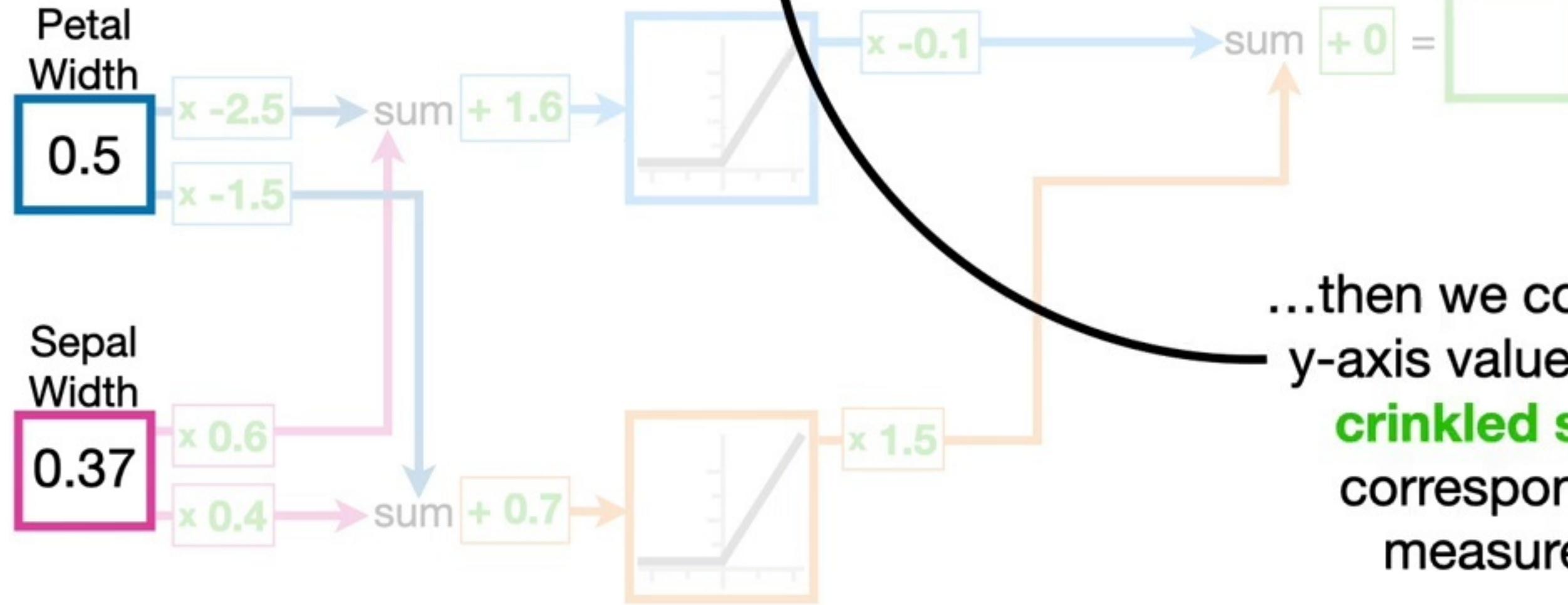
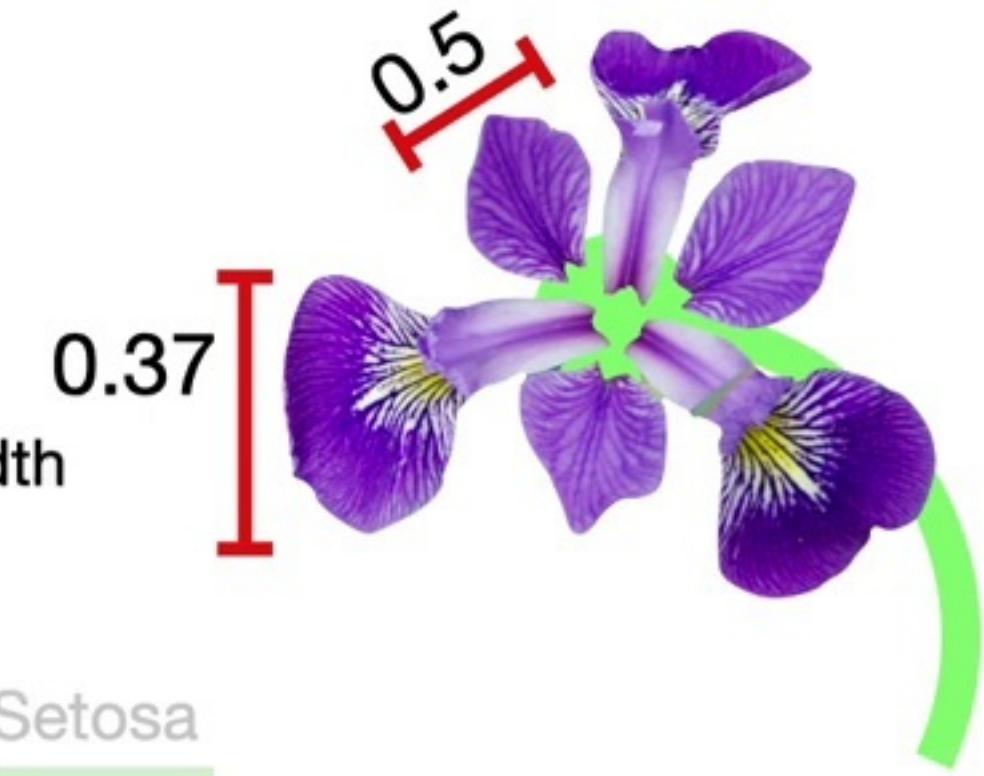
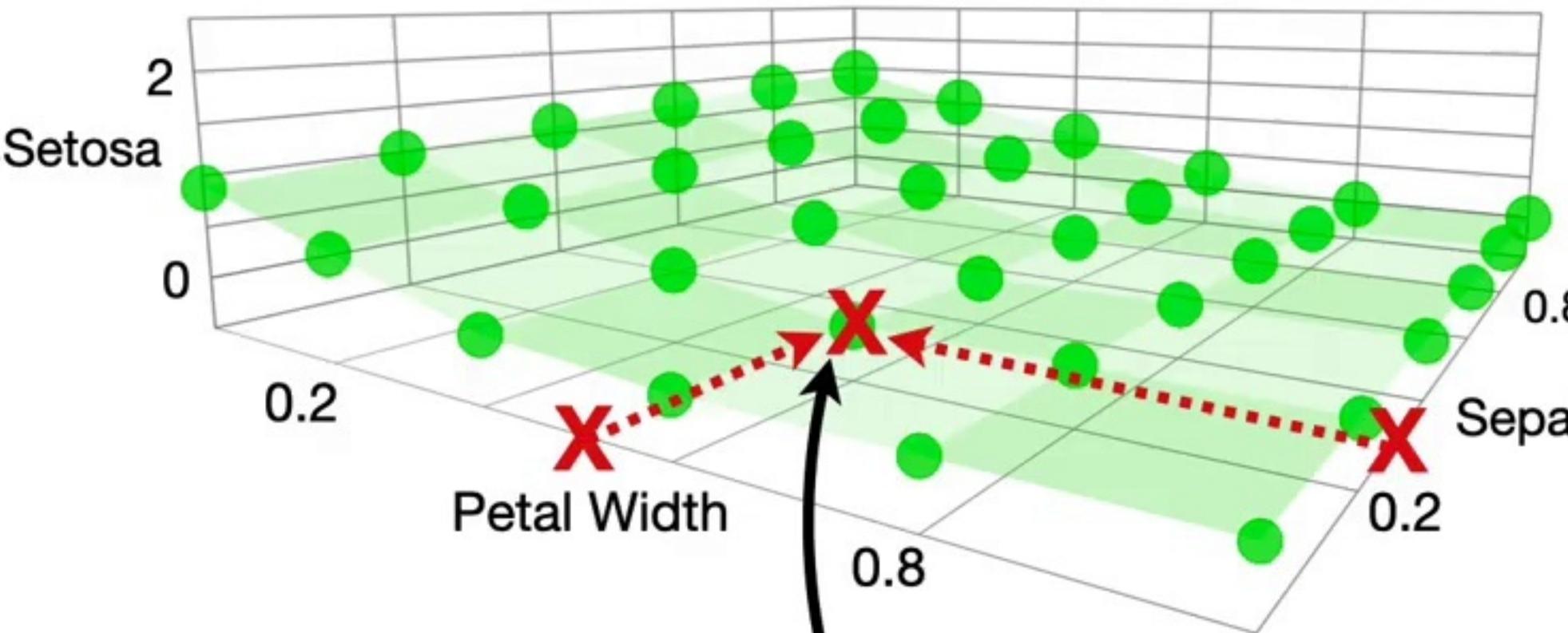
For example, if we found this **Iris** while walking in the woods...





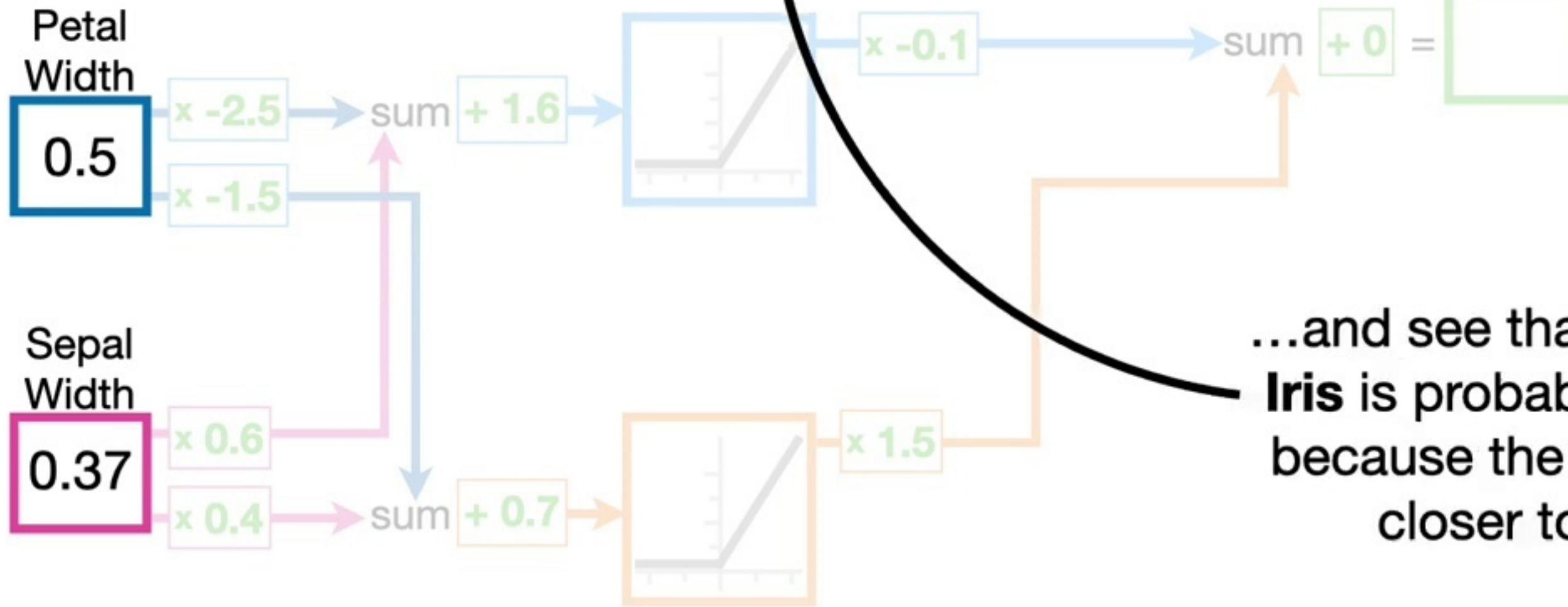
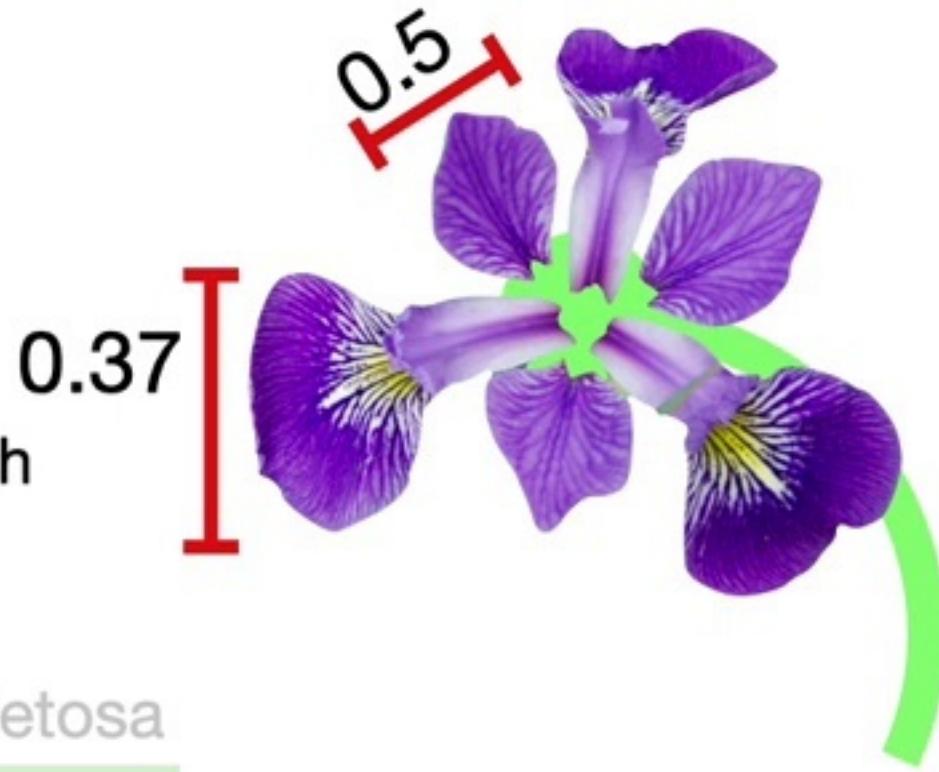
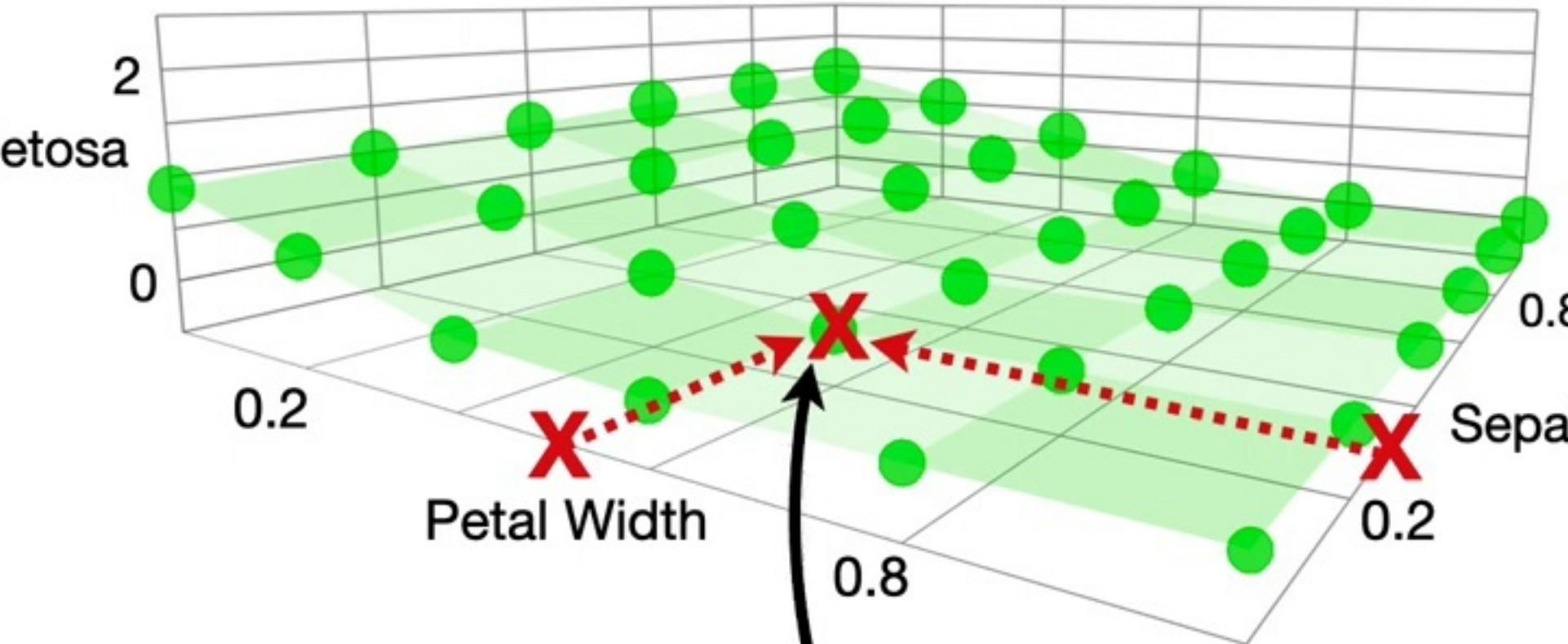
...and the scaled **Sepal Width** was **0.37**...

**SQ!**  
double  
BAM!!



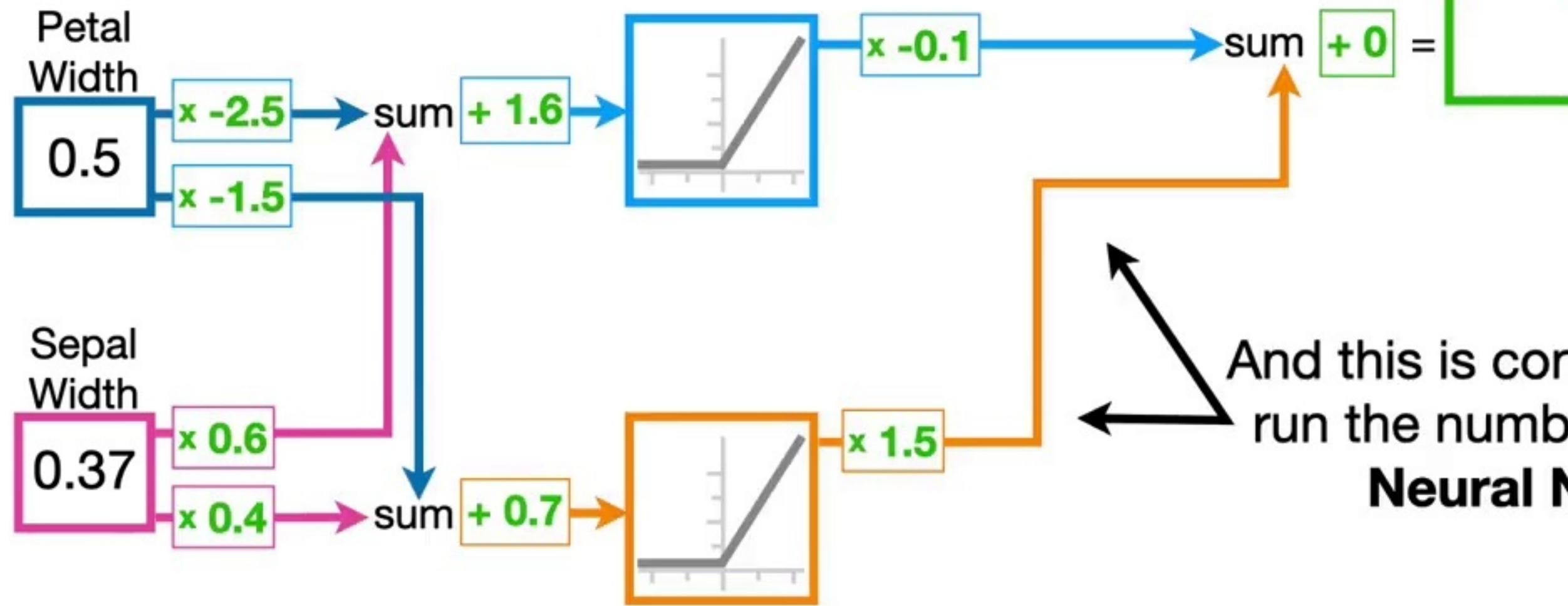
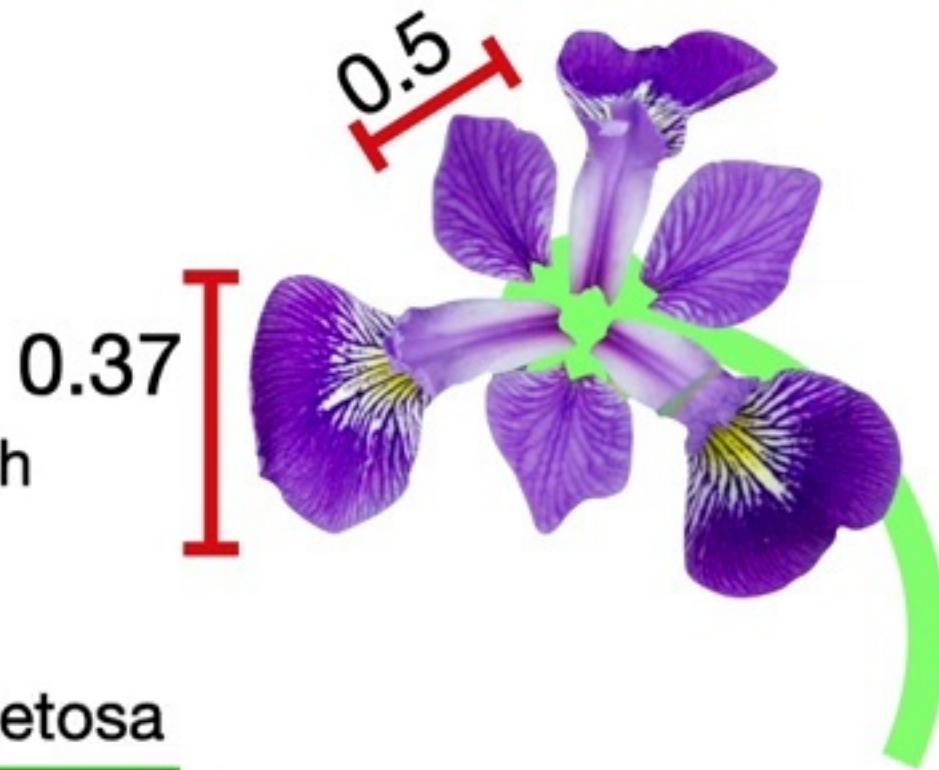
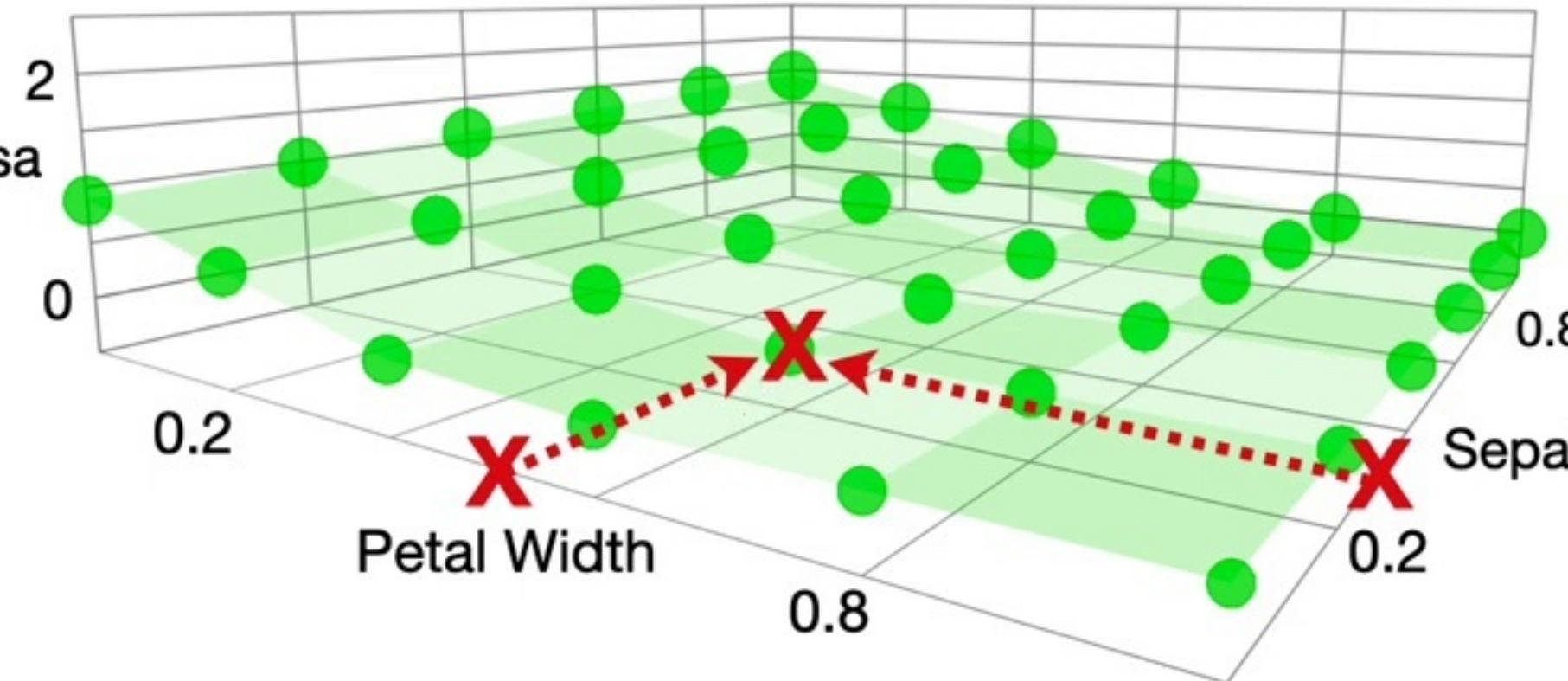
...then we could look at the y-axis value on the **green crinkled surface** that corresponds to these measurements....

**SQ!**  
double  
BAM!!



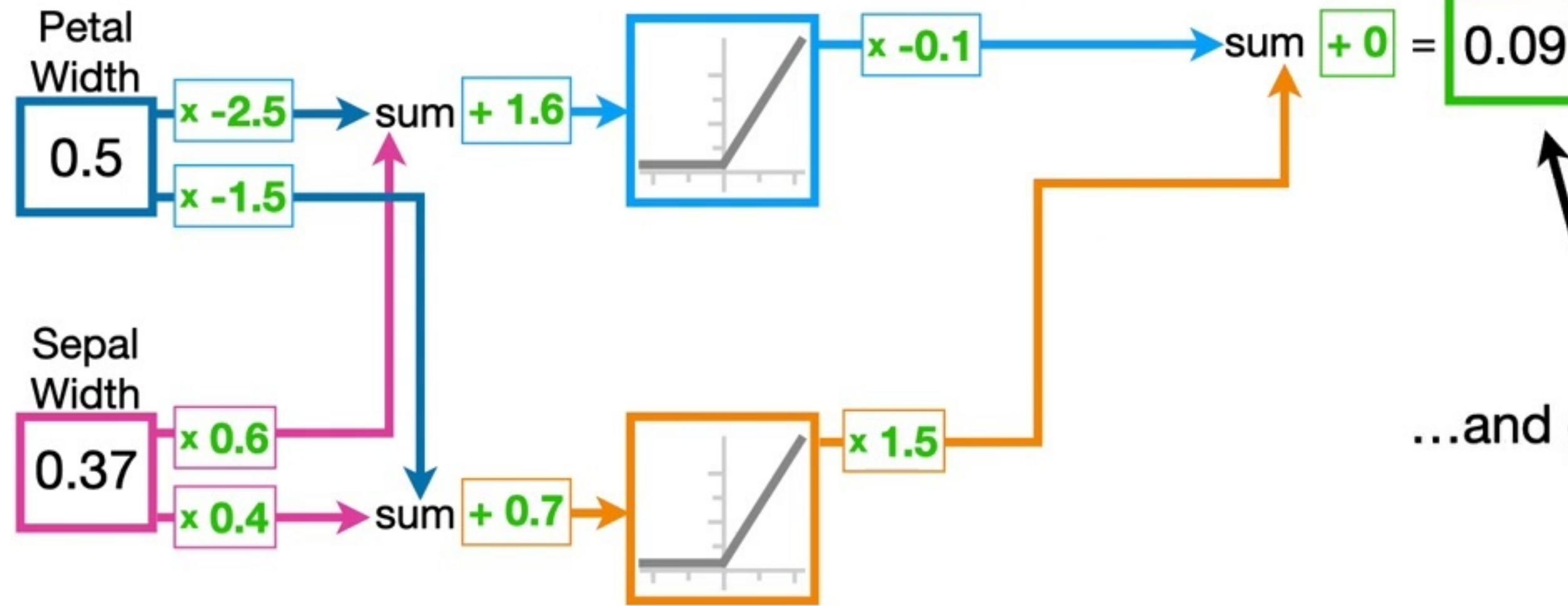
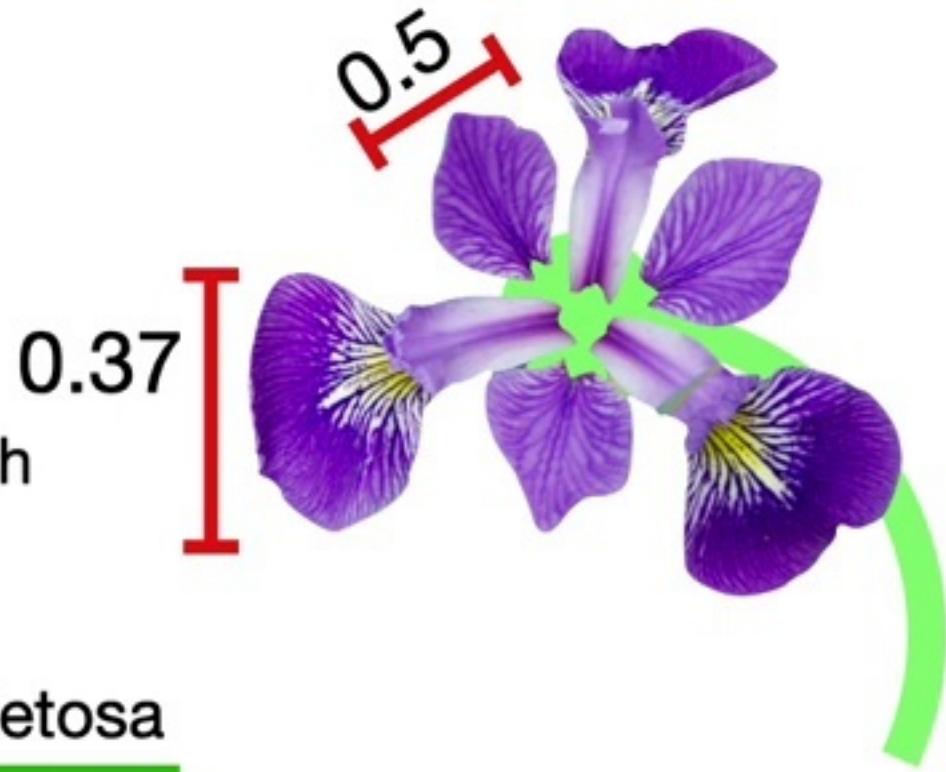
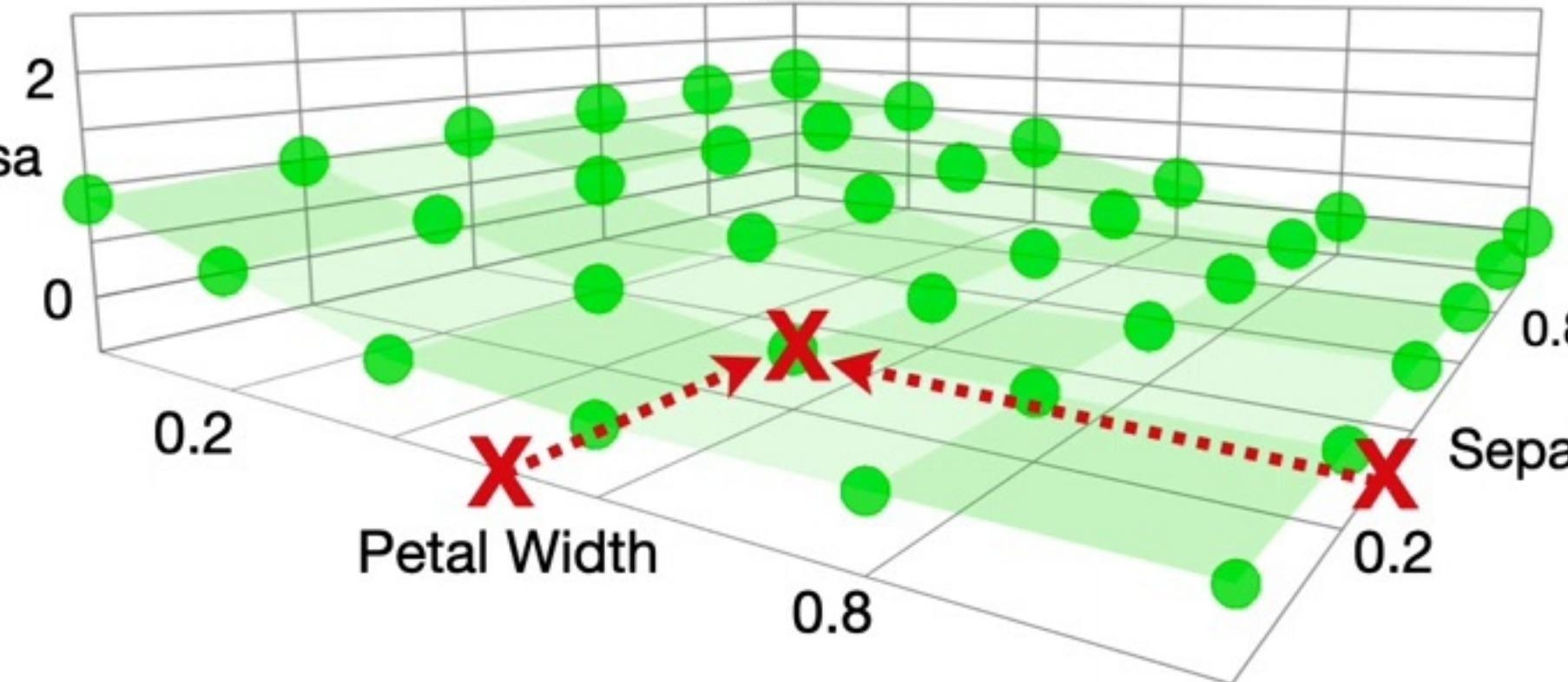
...and see that this particular Iris is probably not **Setosa**, because the y-axis value is closer to **0** than **1**.

**SQ!**  
double  
BAM!!

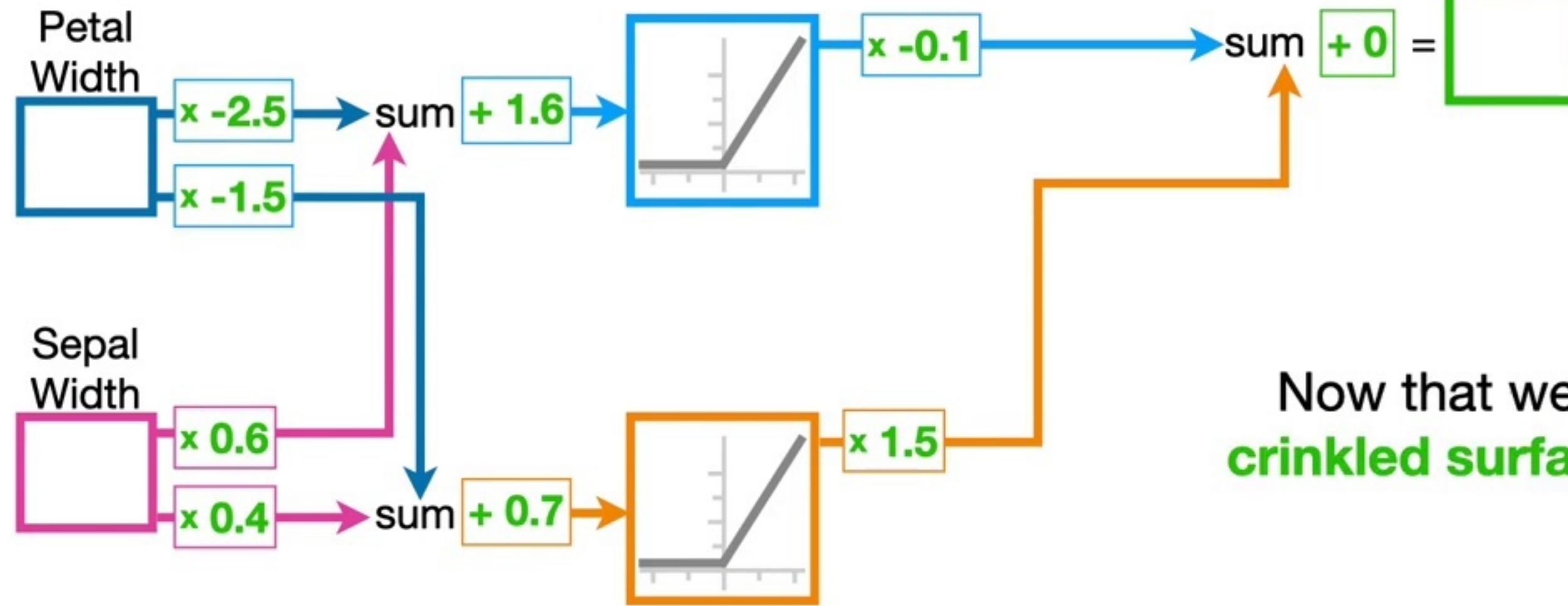
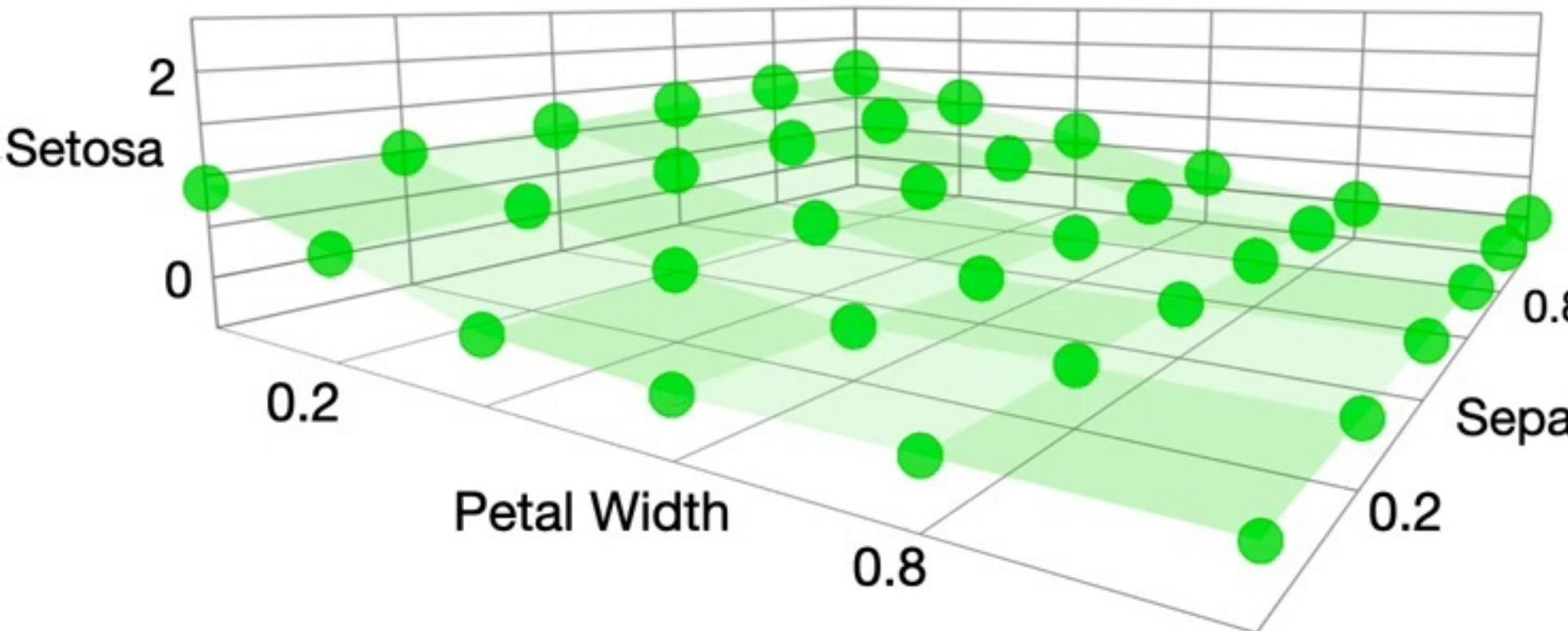


And this is confirmed when we run the numbers through the **Neural Network...**

**SQ!**  
double  
BAM!!



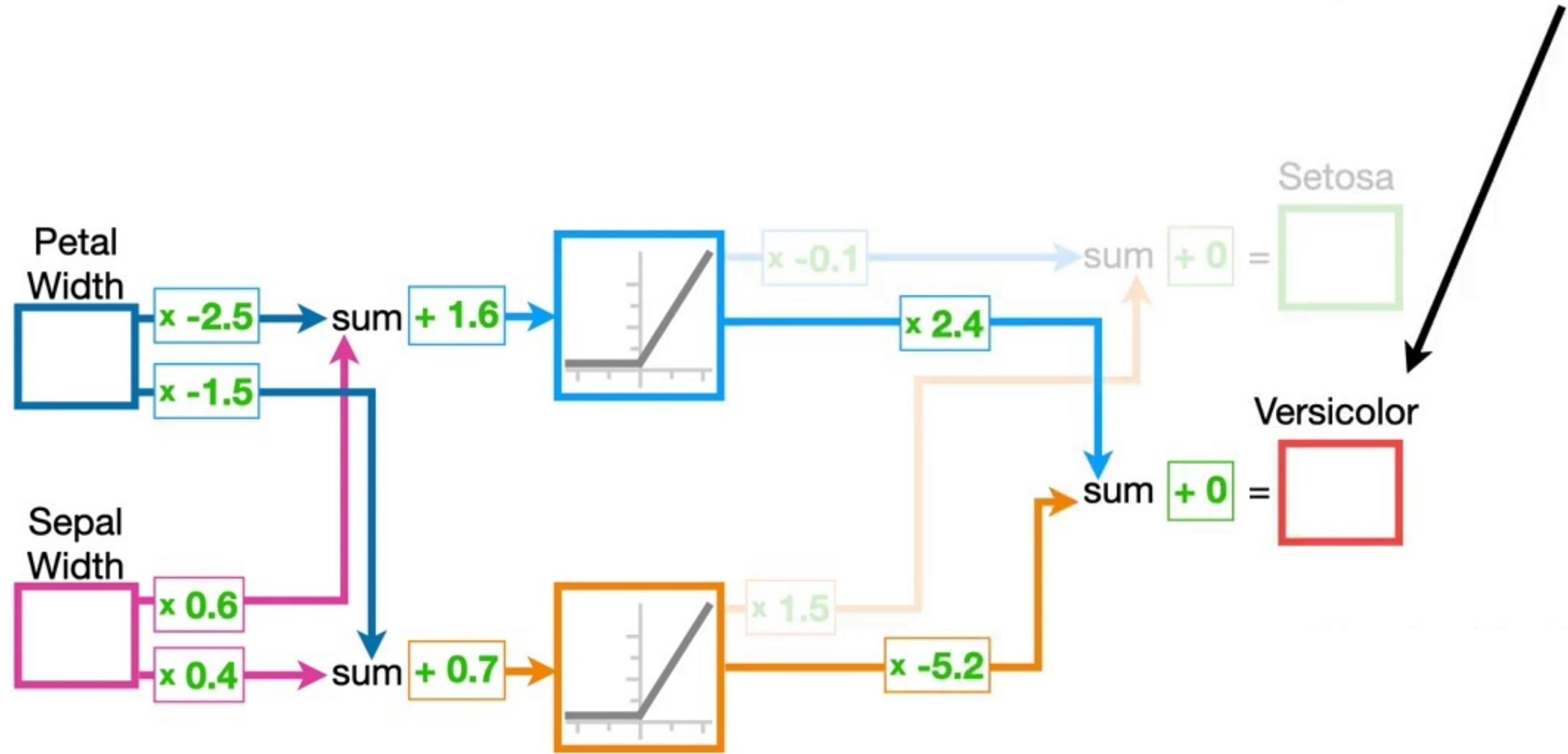
**SQ!**  
double  
BAM!!



Now that we have a **green crinkled surface** for **Setosa**...

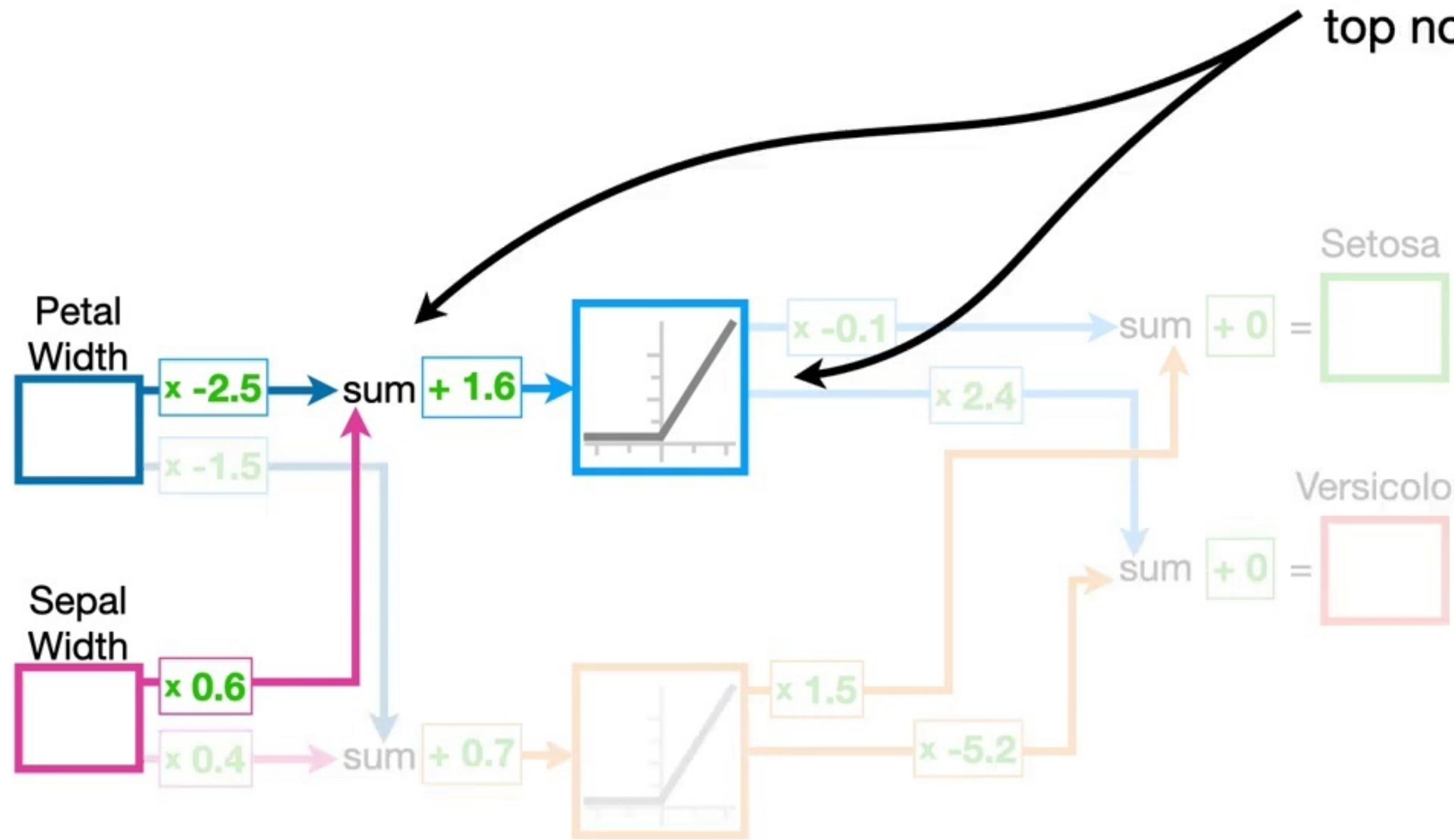


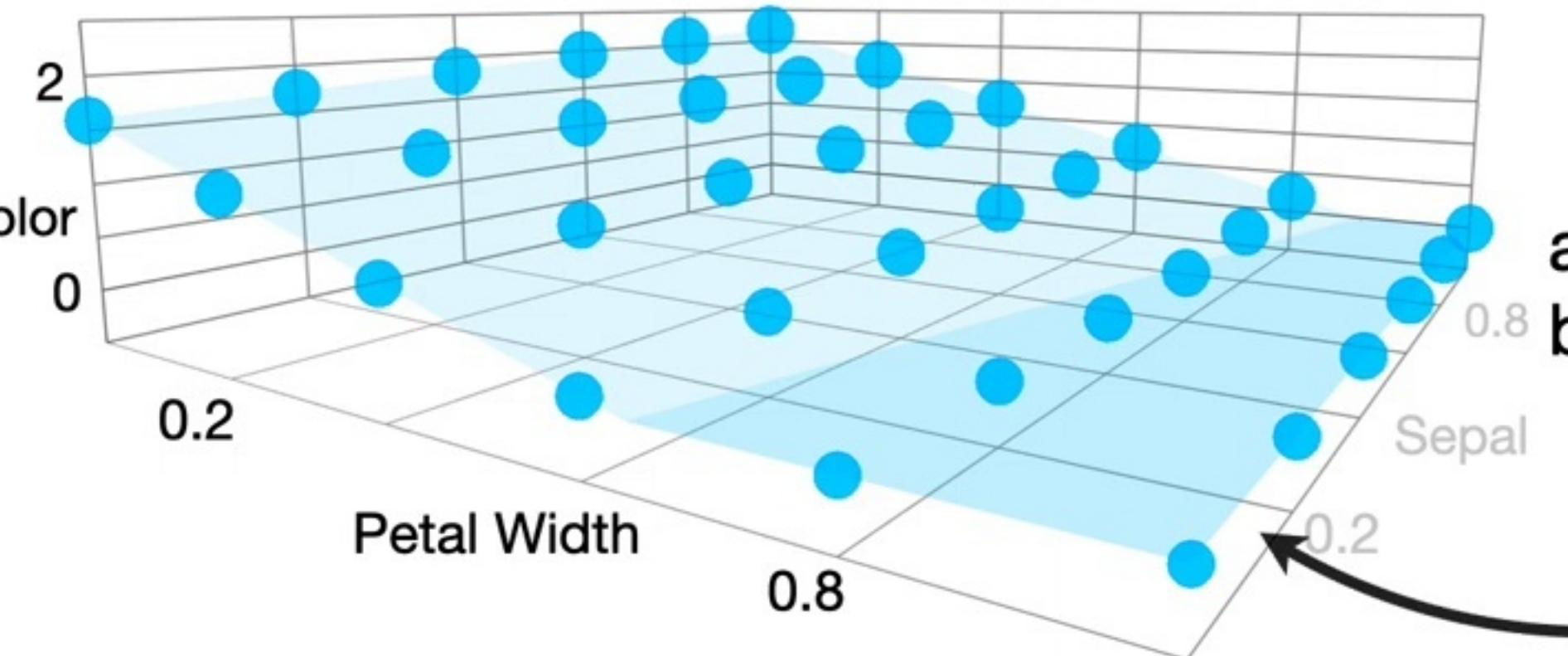
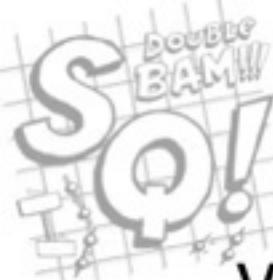
...let's determine the output for the second species, **Versicolor**.



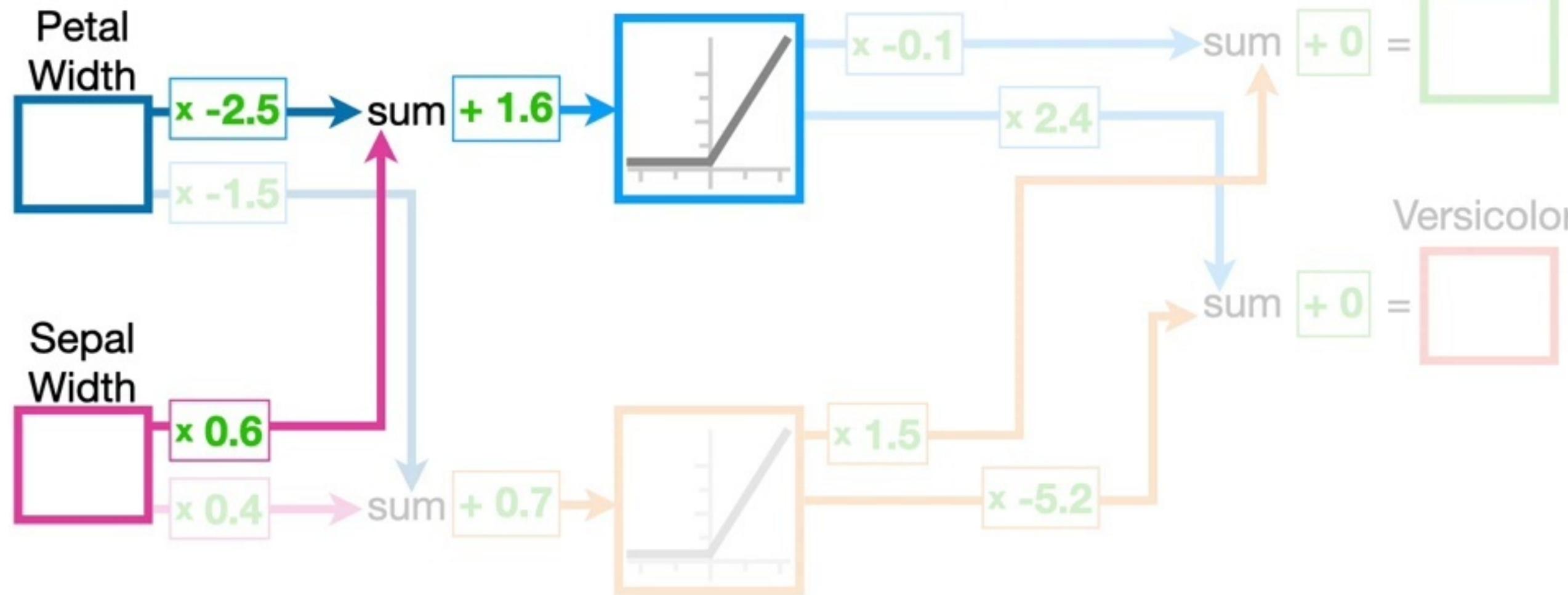


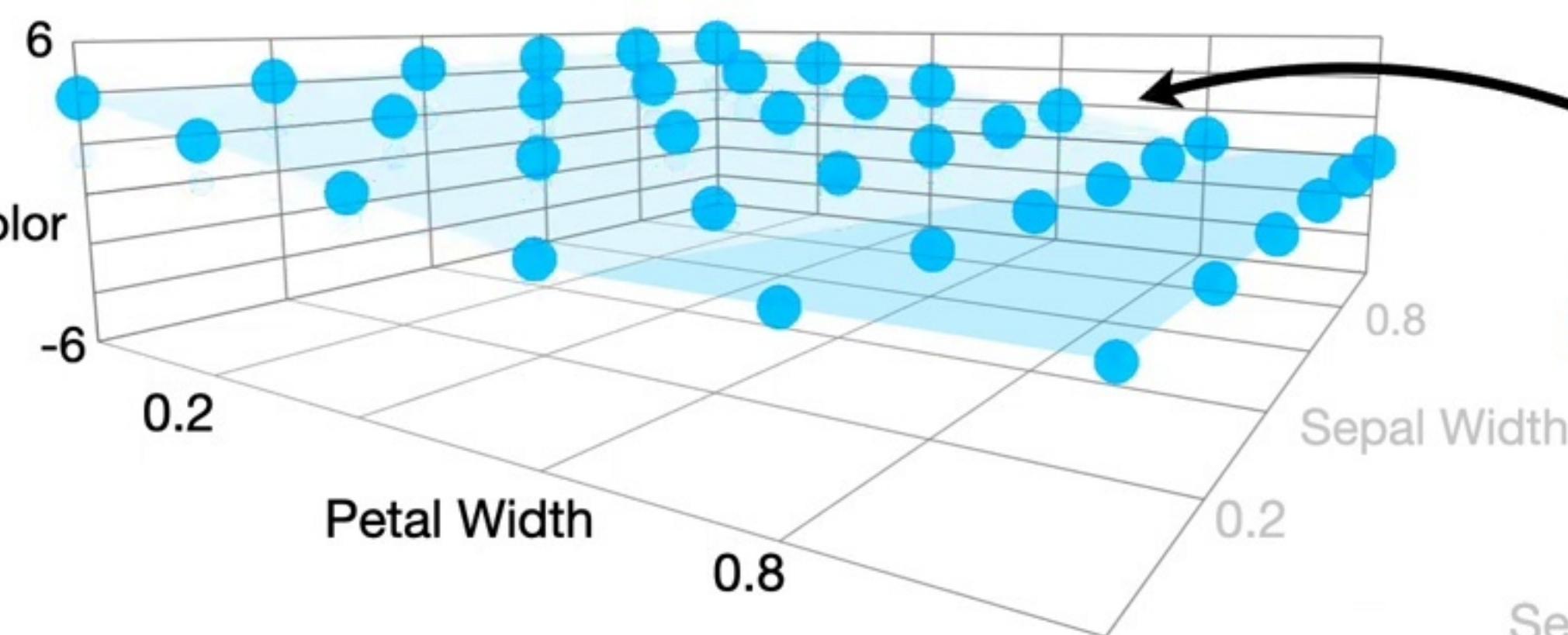
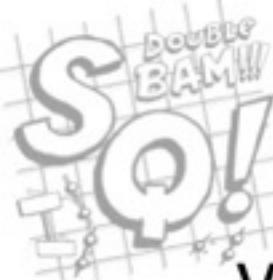
Just like before, we'll start with the connections to the top node in the **Hidden Layer**.



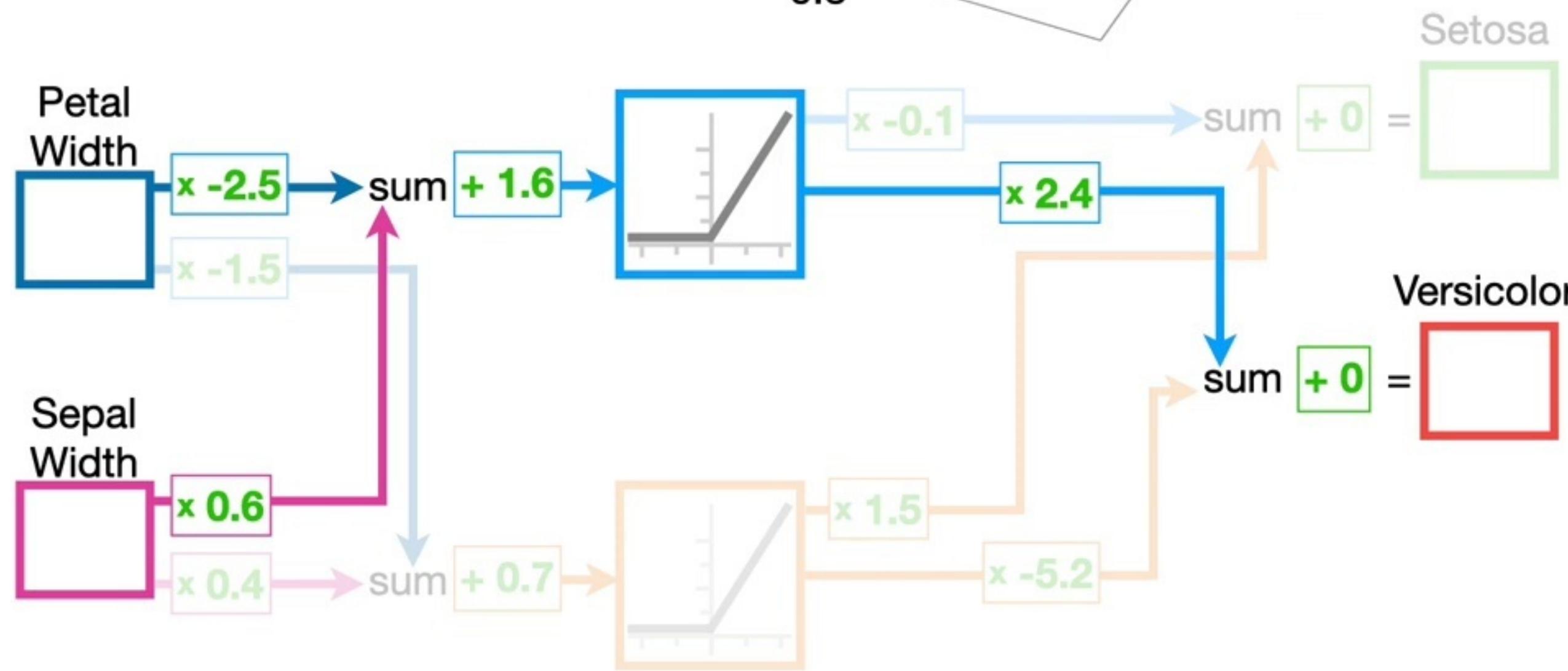


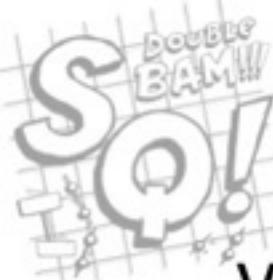
And because the **Weights** and **Biases** are the same as before, we start out with the same **blue bent surface**.



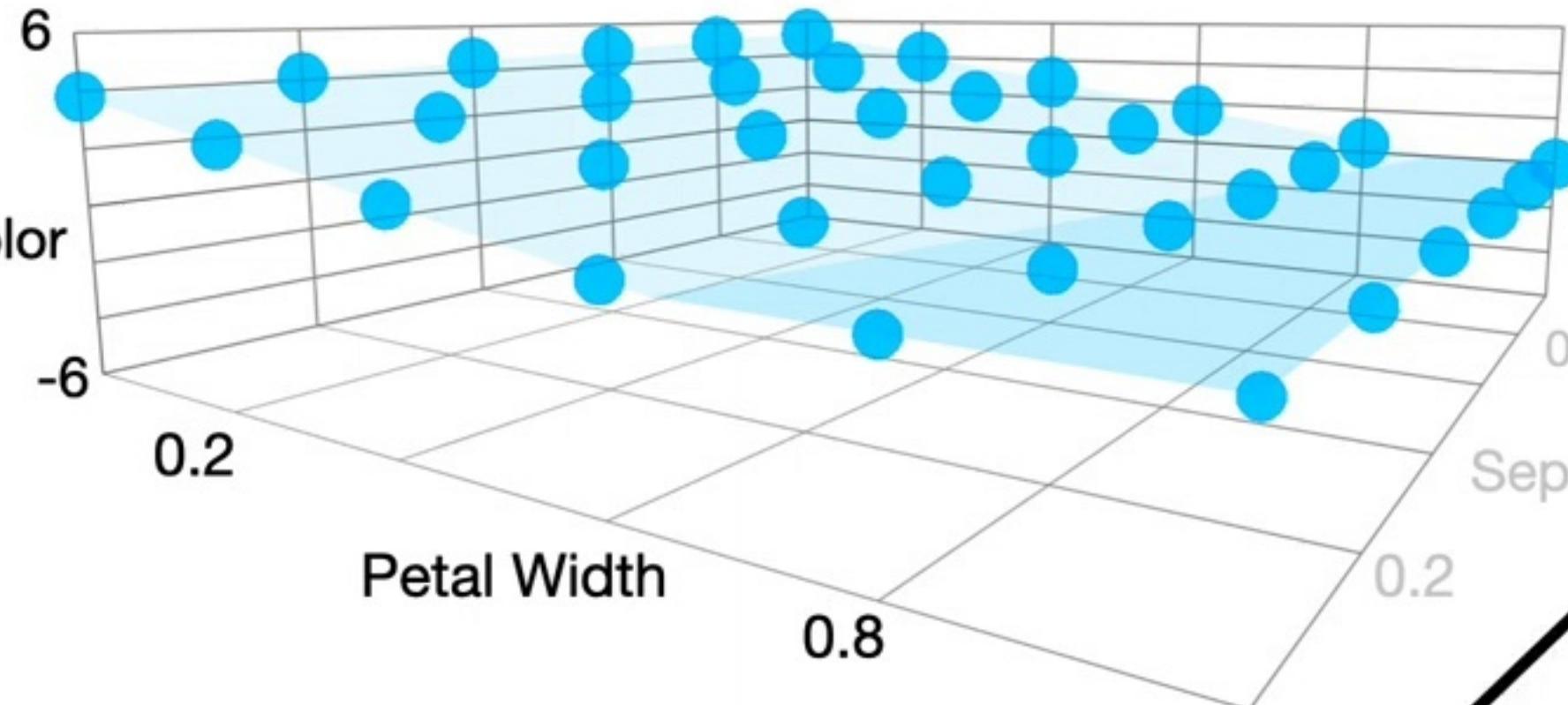


...gives us this final  
**blue bent surface.**



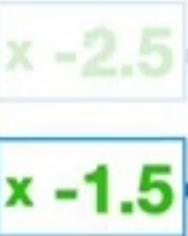


Versicolor



Petal Width

Petal Width



sum



sum



$\times -0.1$

sum

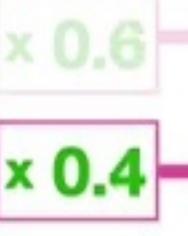
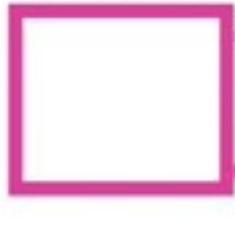


$+ 0$



=

Sepal Width



sum



sum



$\times 1.5$

sum

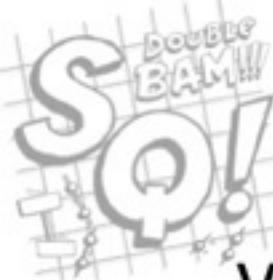


$+ 0$

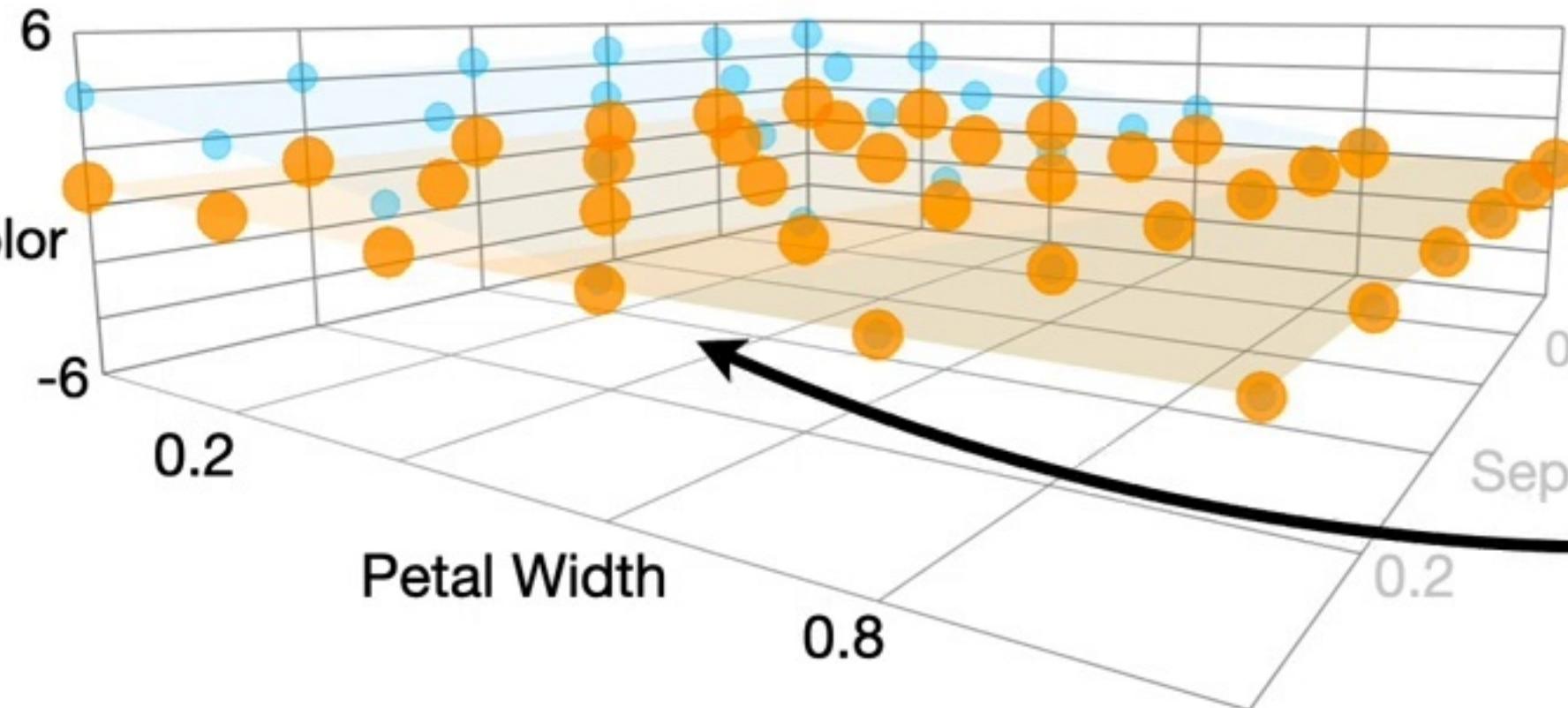


=

Now we create the **orange bent surface** from the bottom node in the **Hidden Layer**...

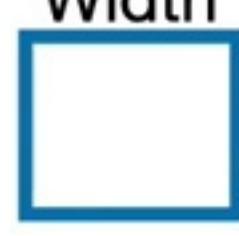


Versicolor

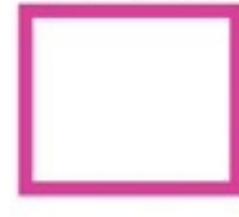


...and multiply the y-axis coordinates on the **orange bent surface** by **-5.2**.

Petal  
Width



Sepal  
Width

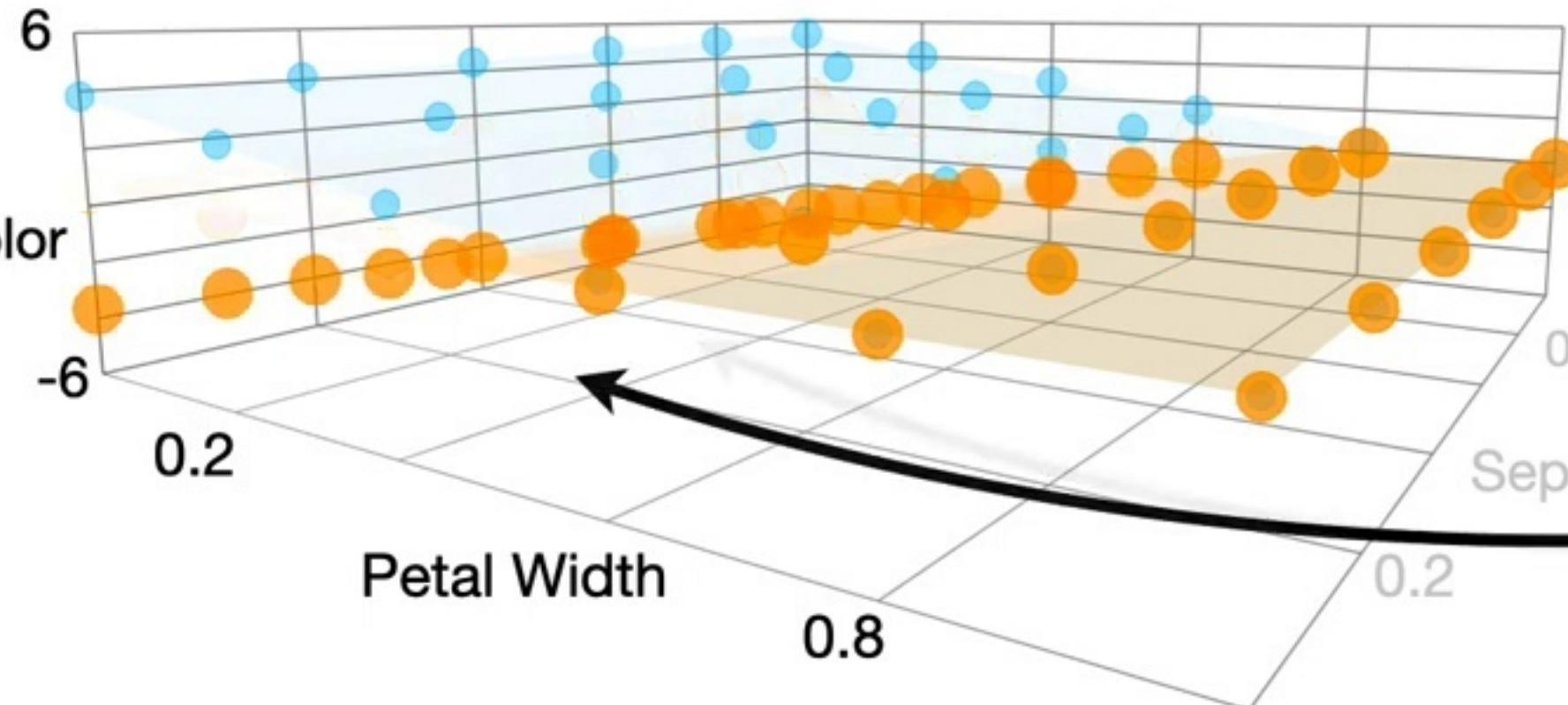


Setosa

Versicolor



Versicolor

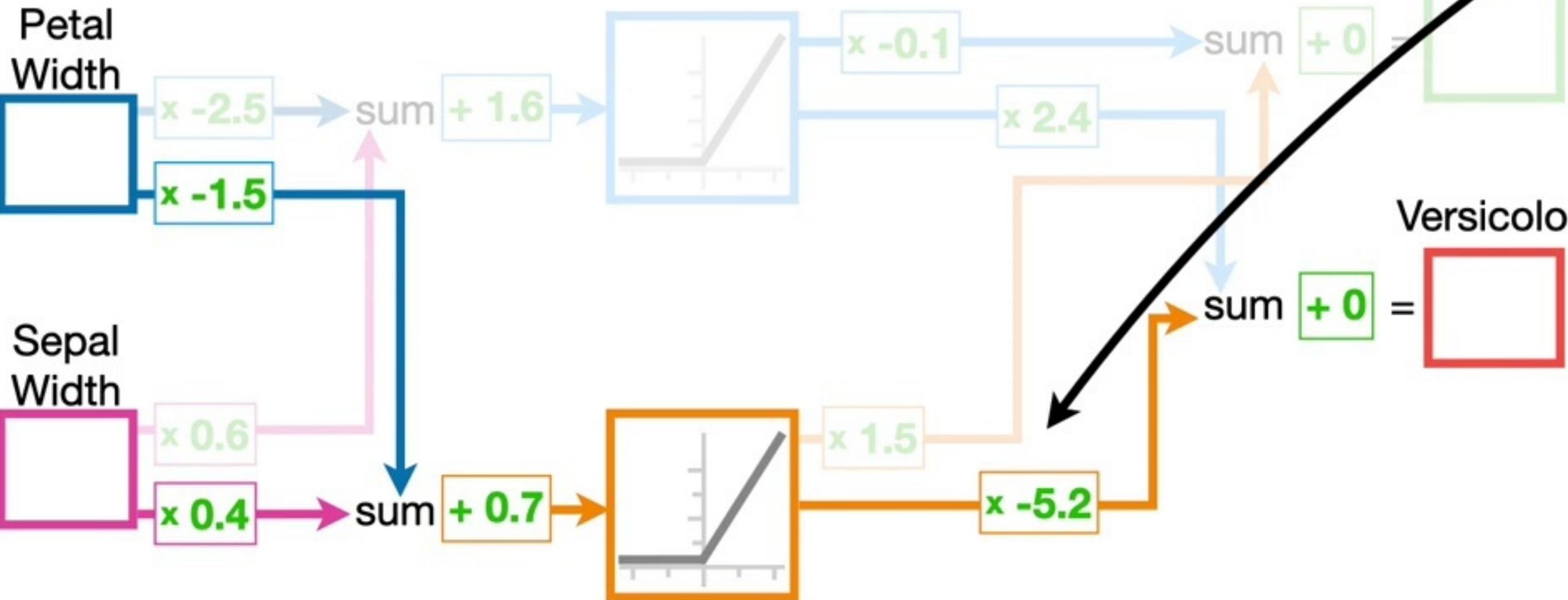


...and multiply the y-axis  
coordinates on the **orange**  
**bent surface** by **-5.2**.

Petal  
Width



Sepal  
Width

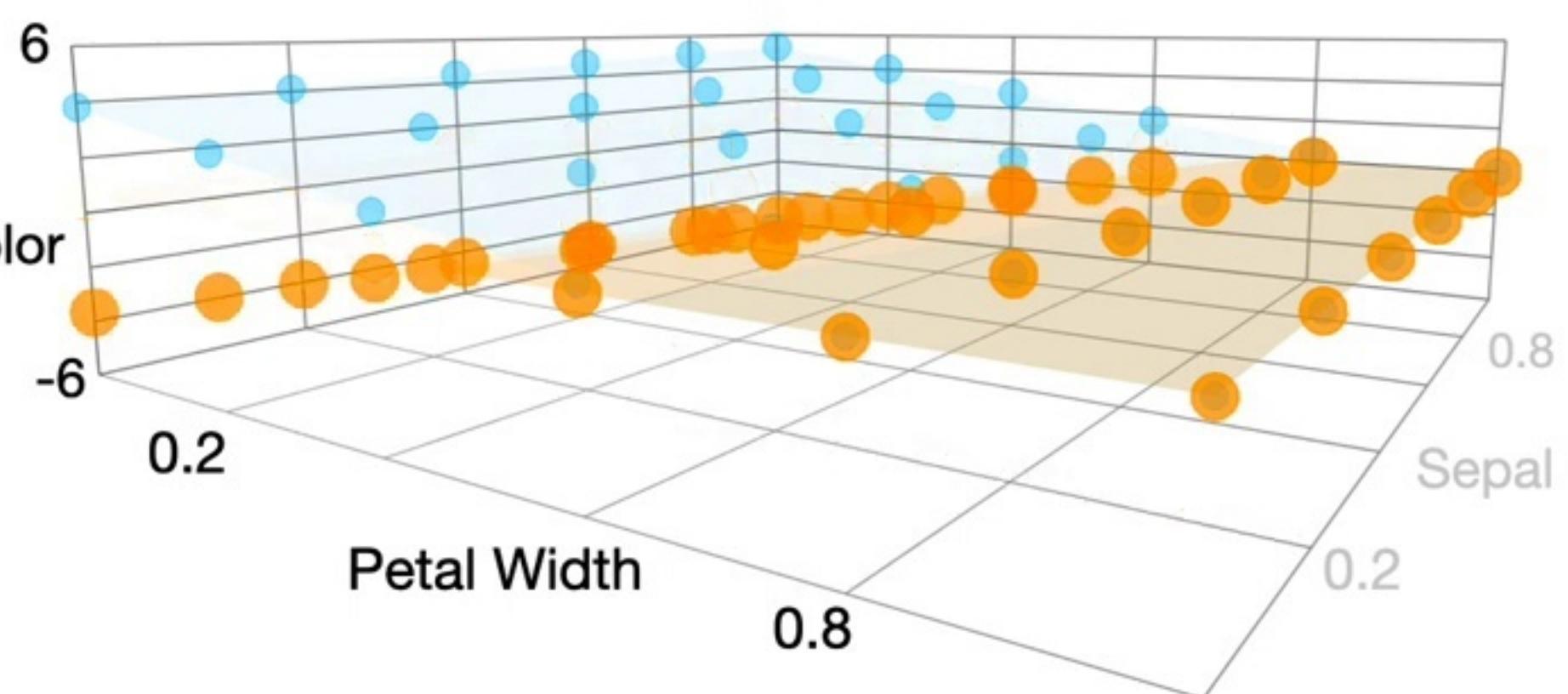


Setosa

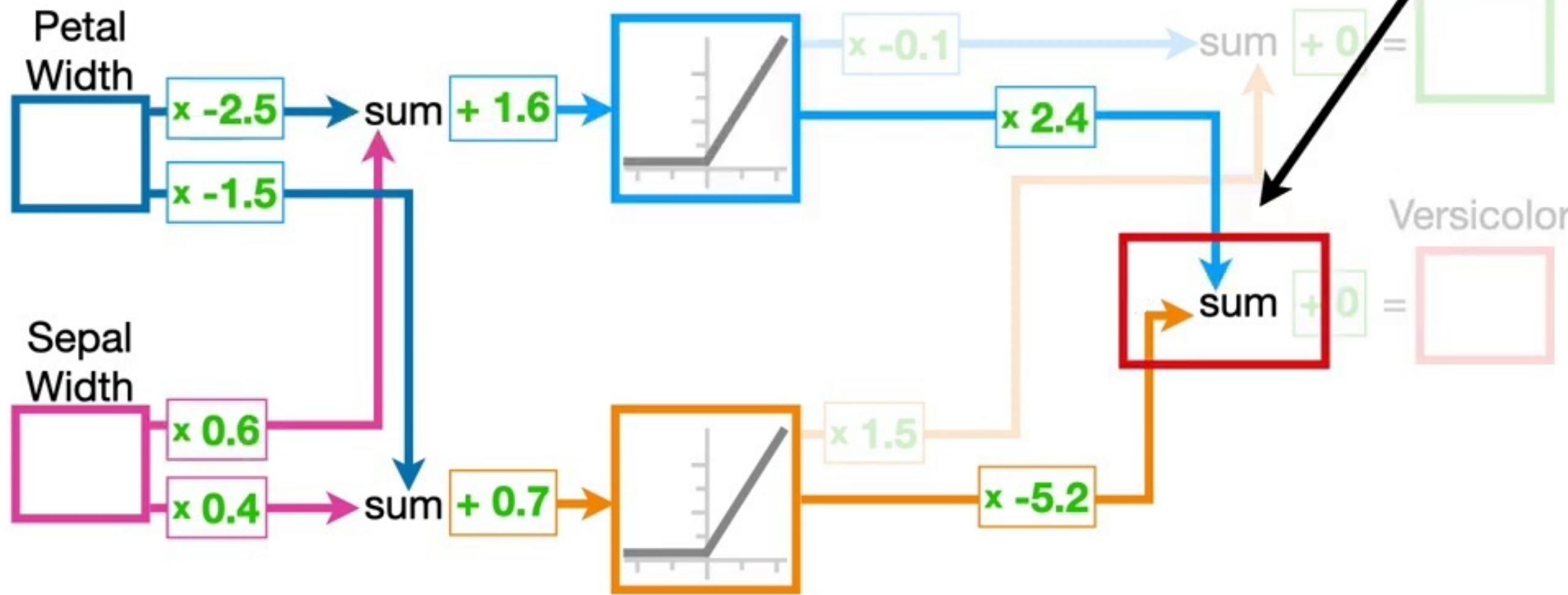
Versicolor



Versicolor

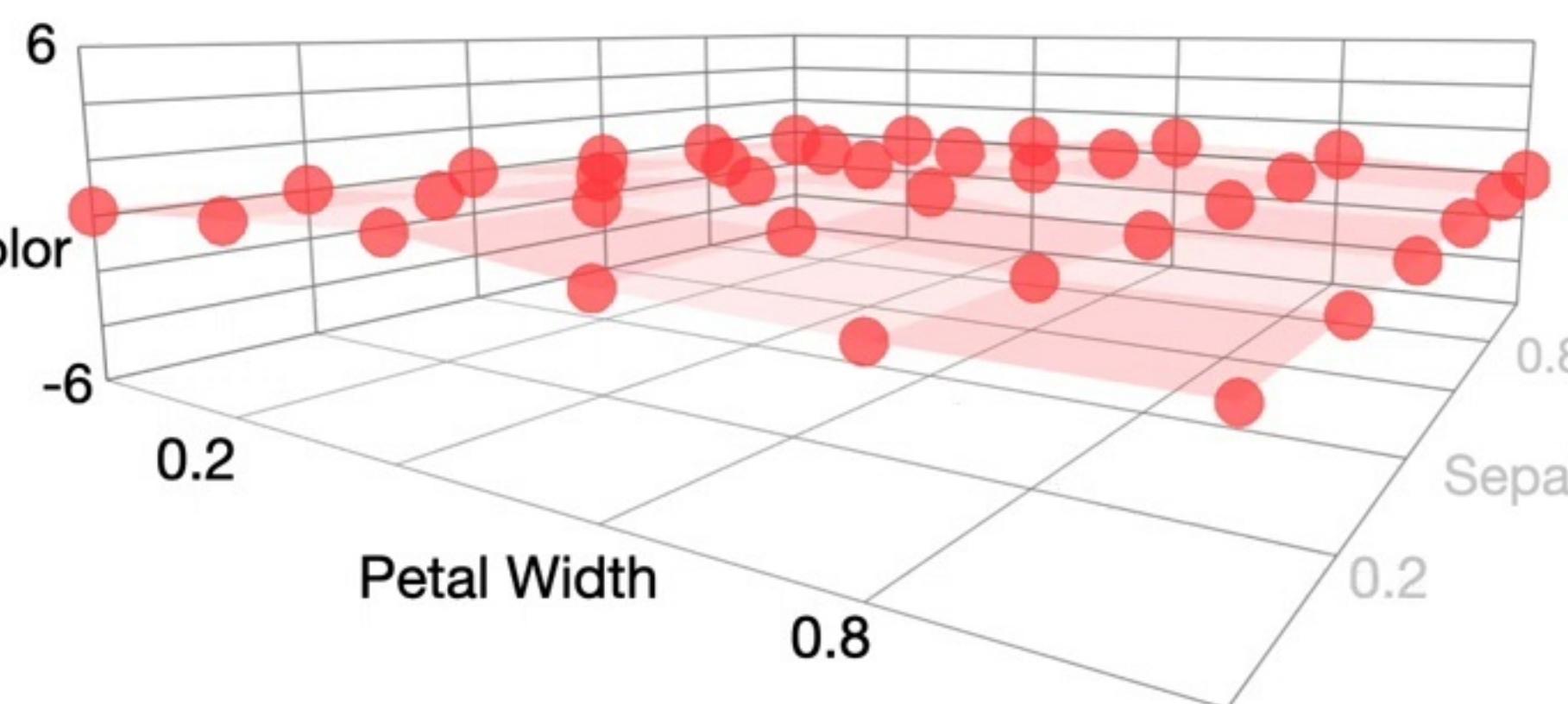


Now we add the y-axis coordinates from the two bent surfaces together...

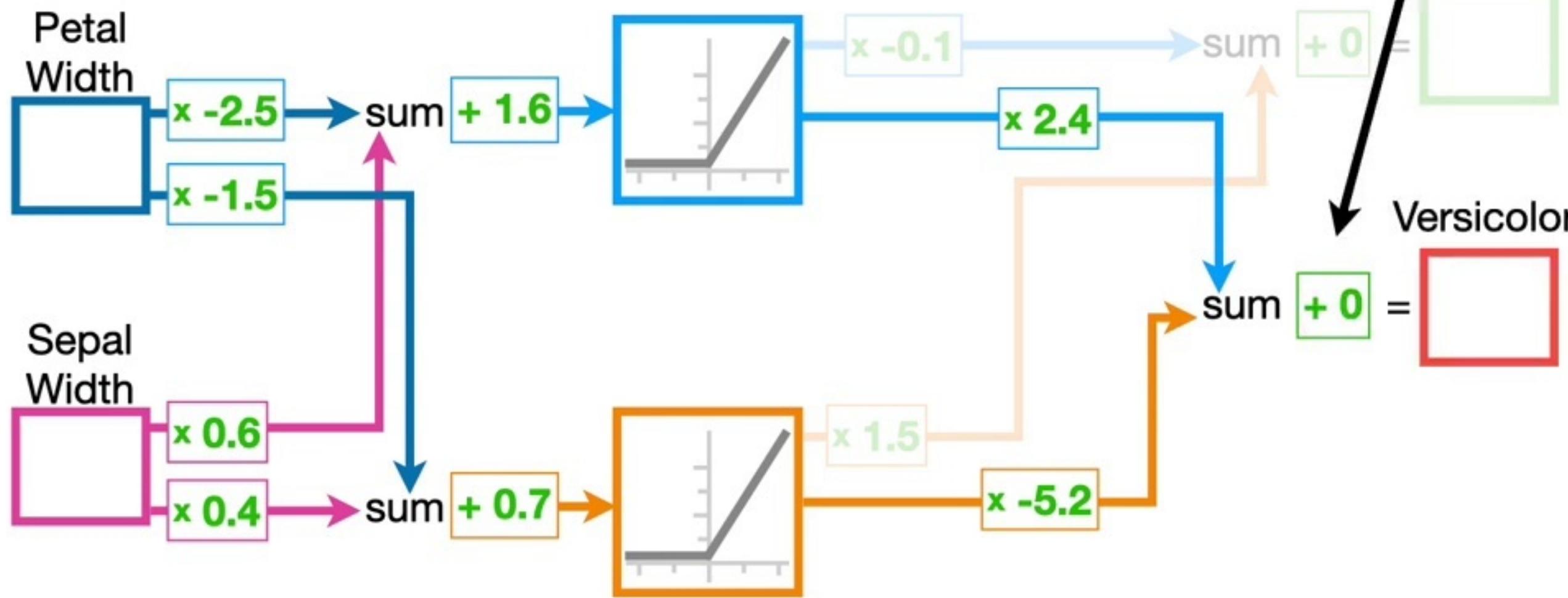




Versicolor

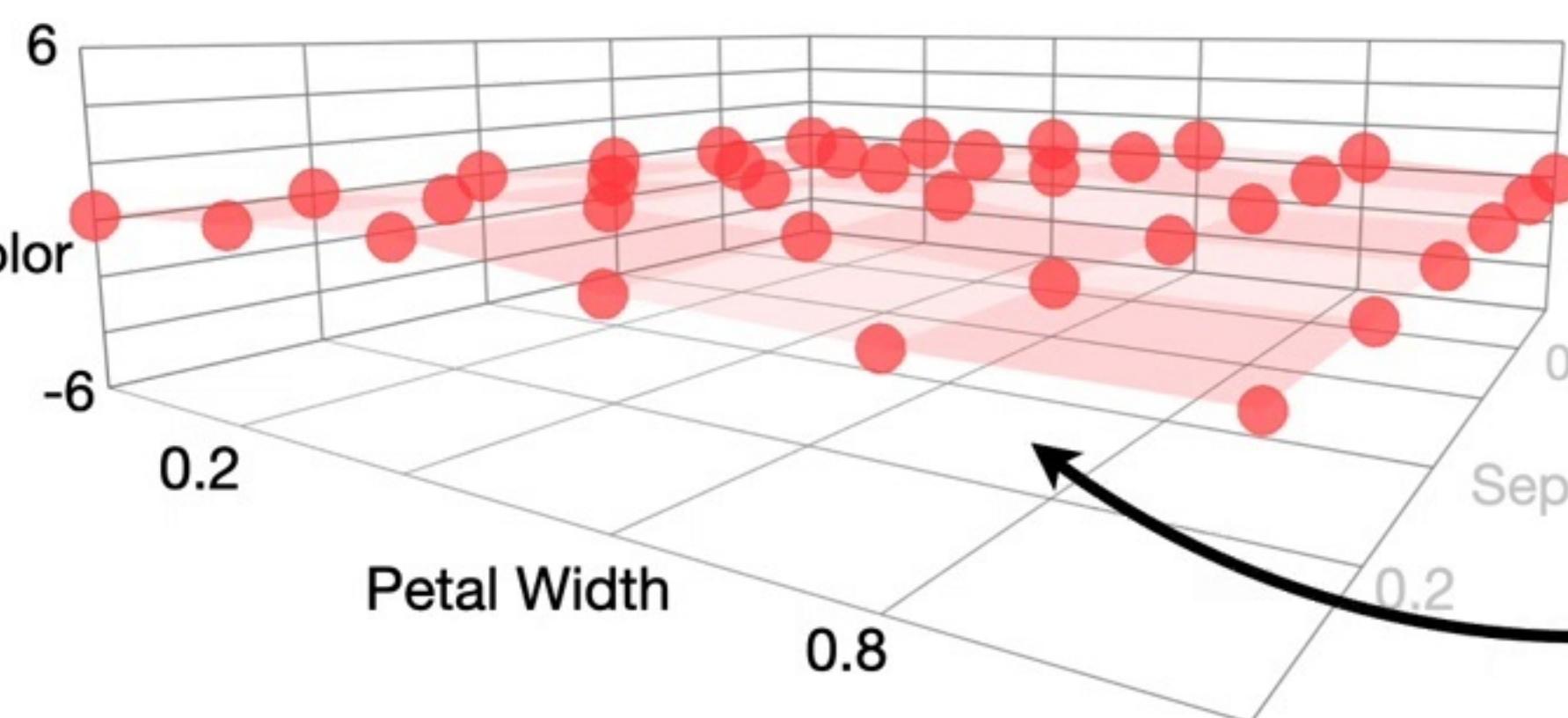


Lastly, we add the final **Bias, 0**, to the y-axis coordinates on the **red crinkled surface**...

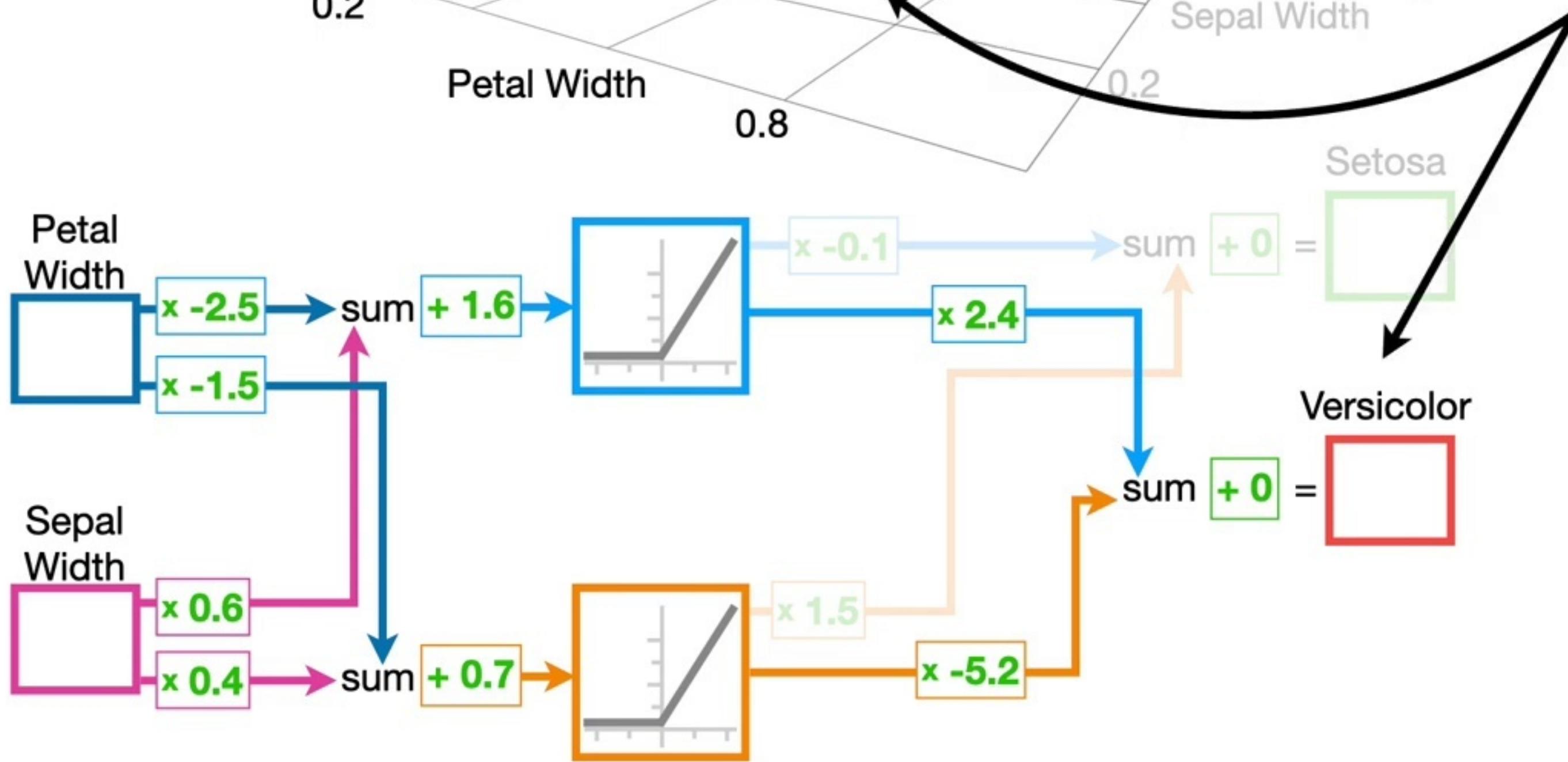




Versicolor



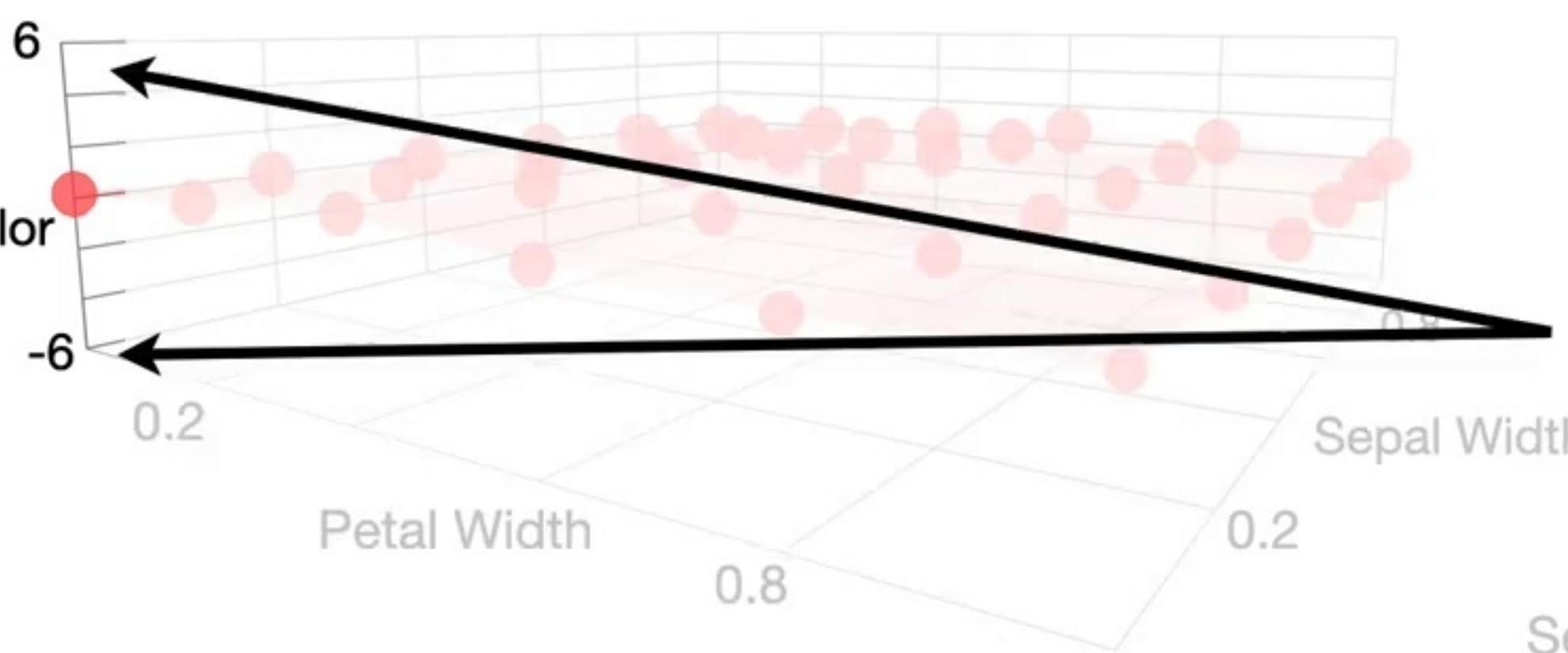
...and that gives us the final surface for predicting if the Iris species is **Versicolor**.





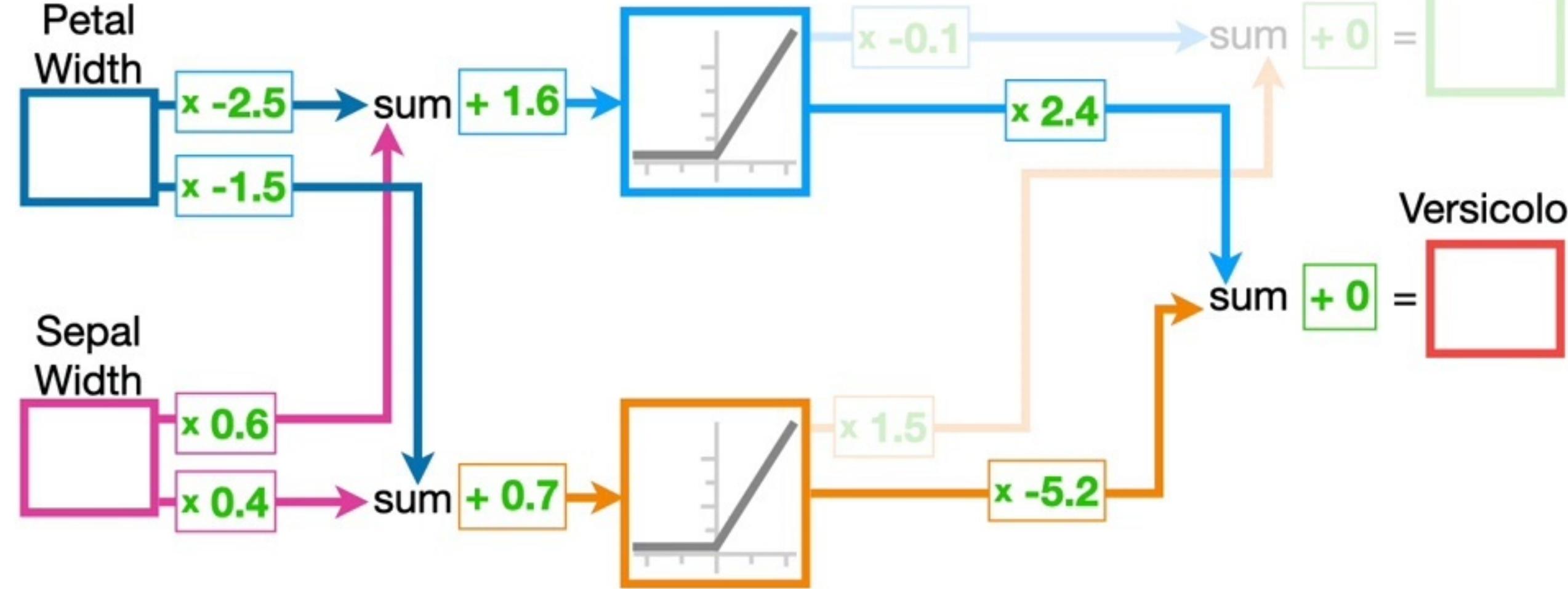
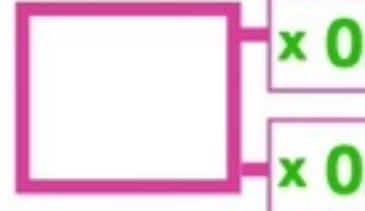
Versicolor

...but when we  
change the y-axis  
scale from -6 to 6...



Petal  
Width

Sepal  
Width

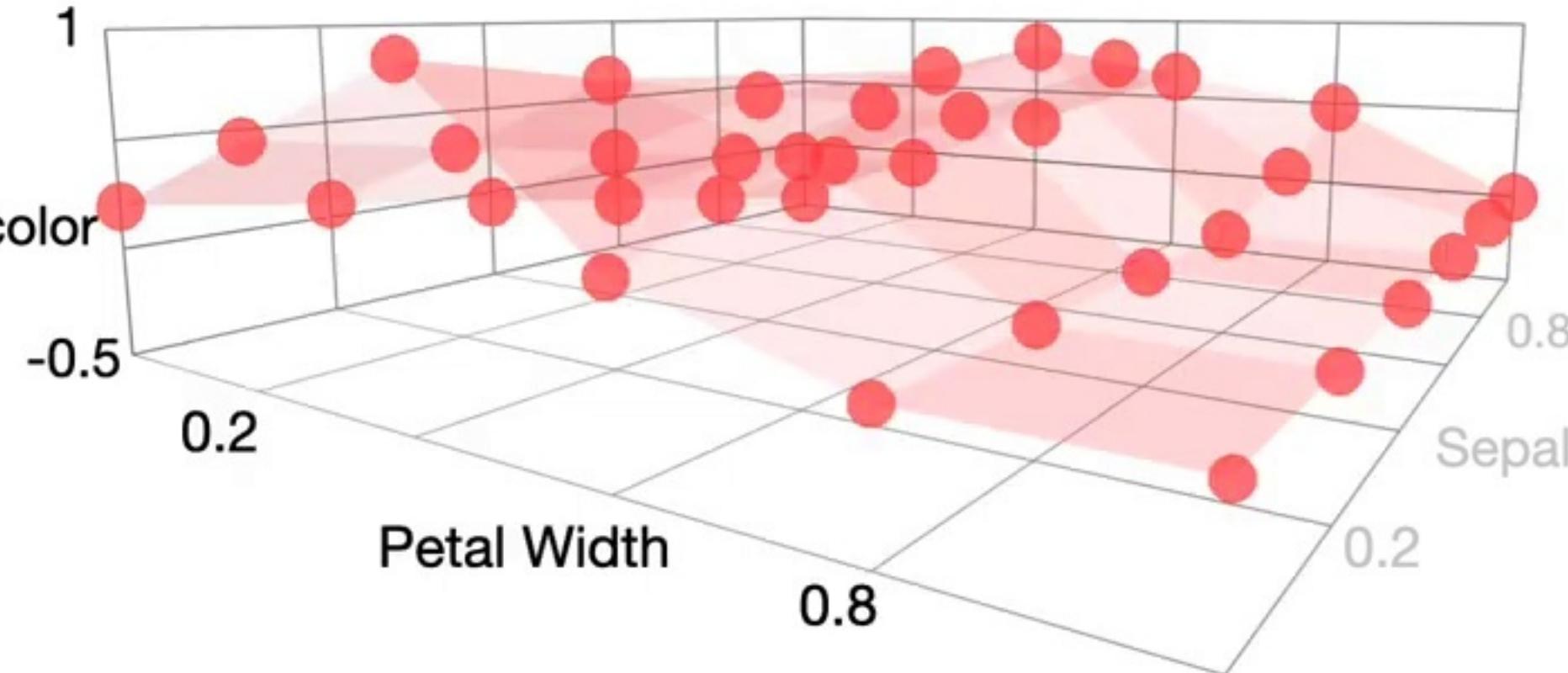


Setosa

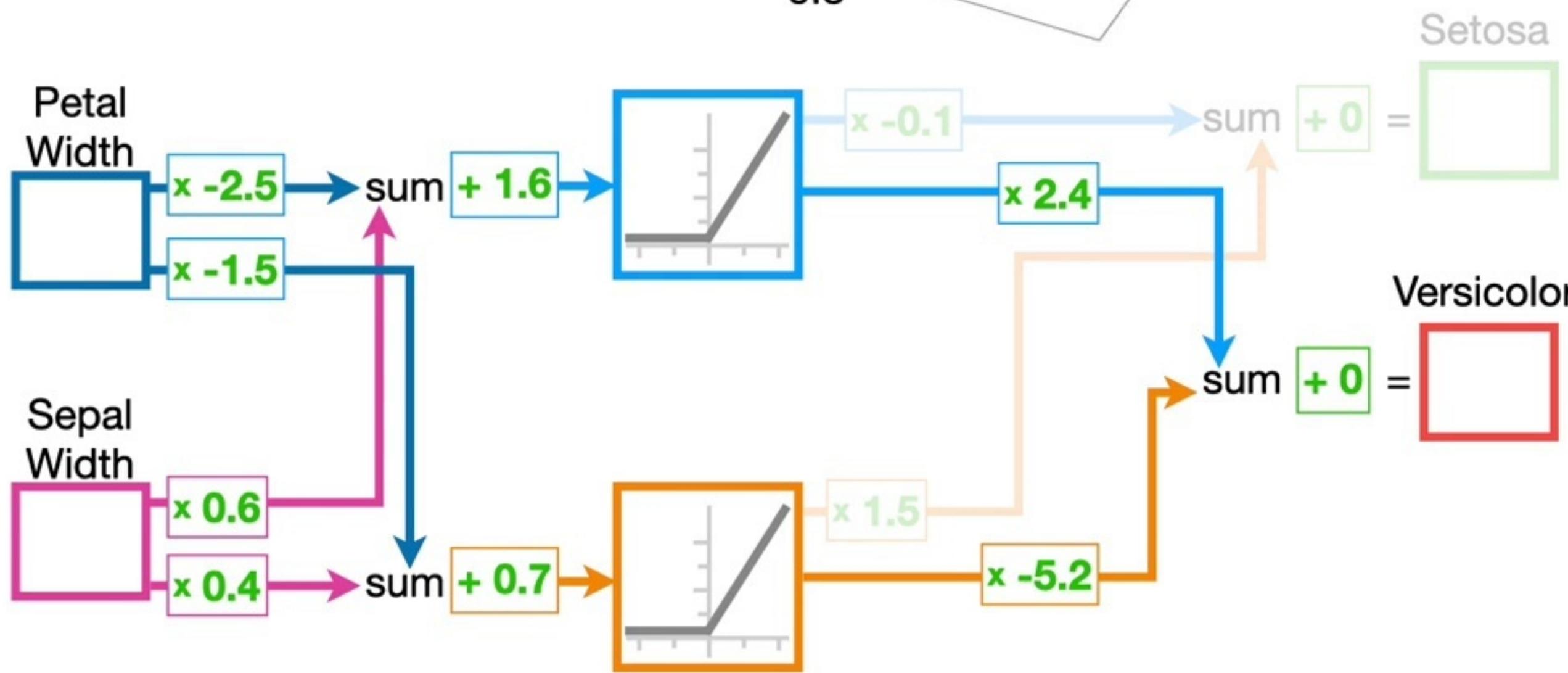
Versicolor

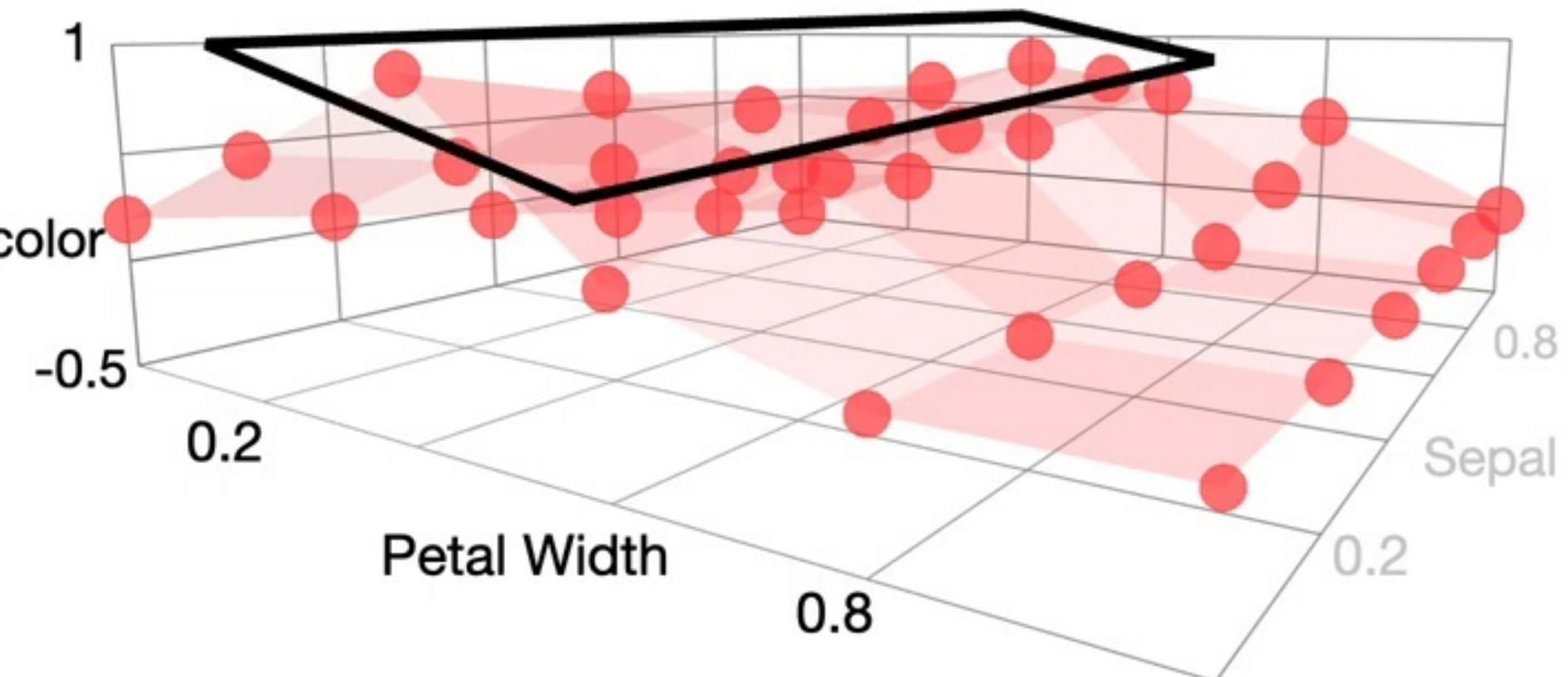


Versicolor

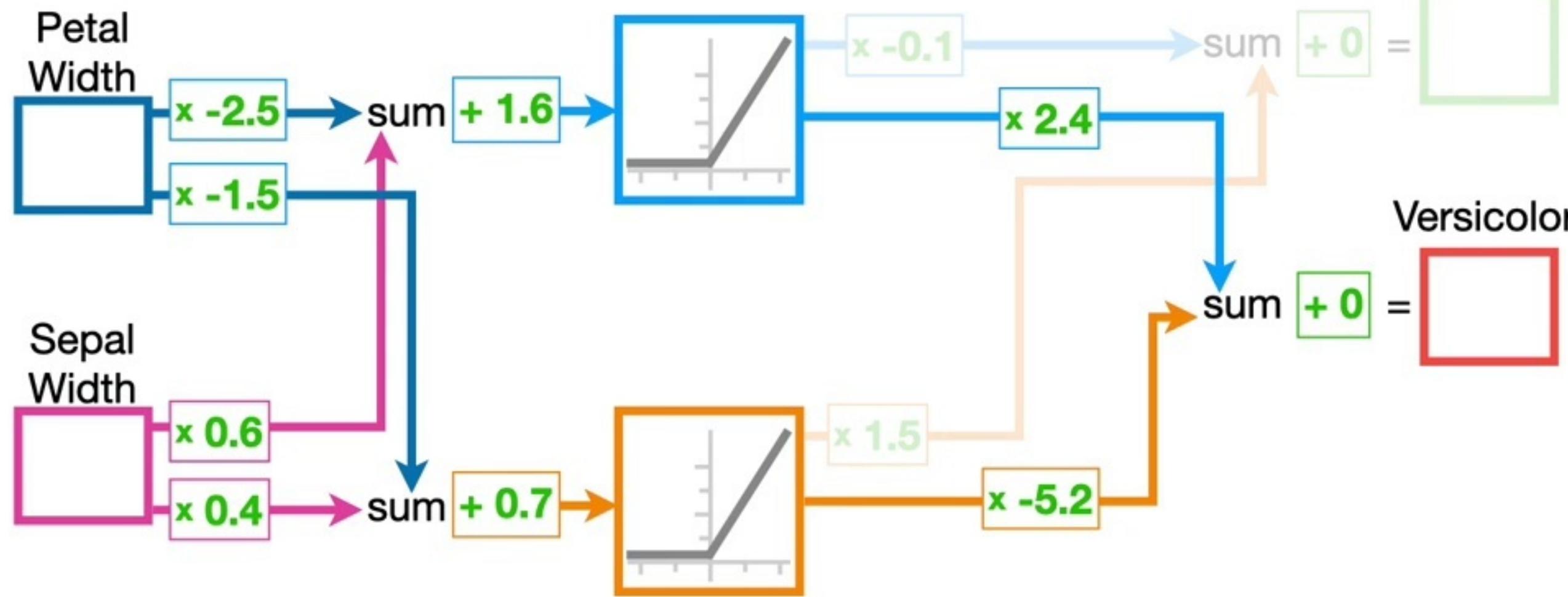


...to -0.5 to 1...



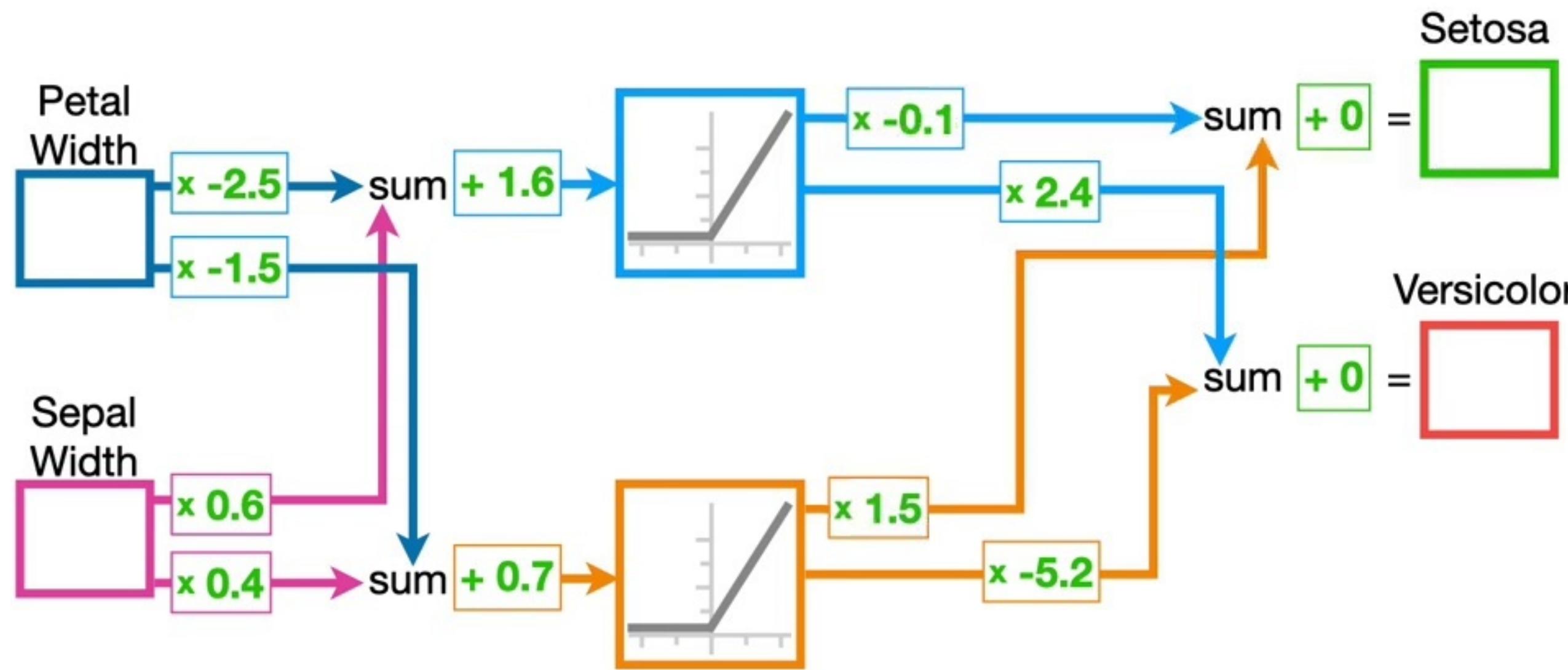


...we see that when **Petal Width** is close to **0.4**, we will get a high value for **Versicolor**.



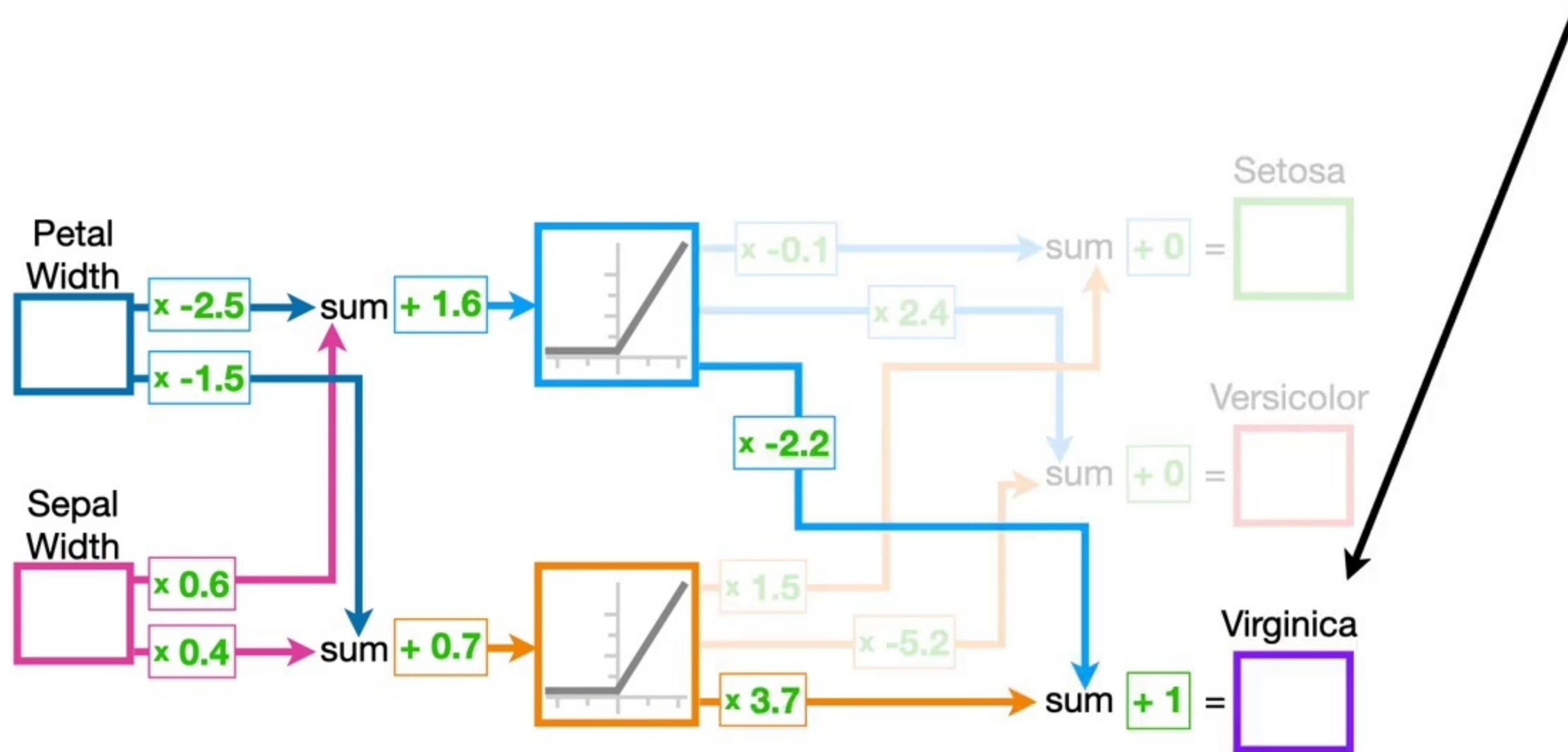


Now, just like we did for  
**Setosa** and **Versicolor**...



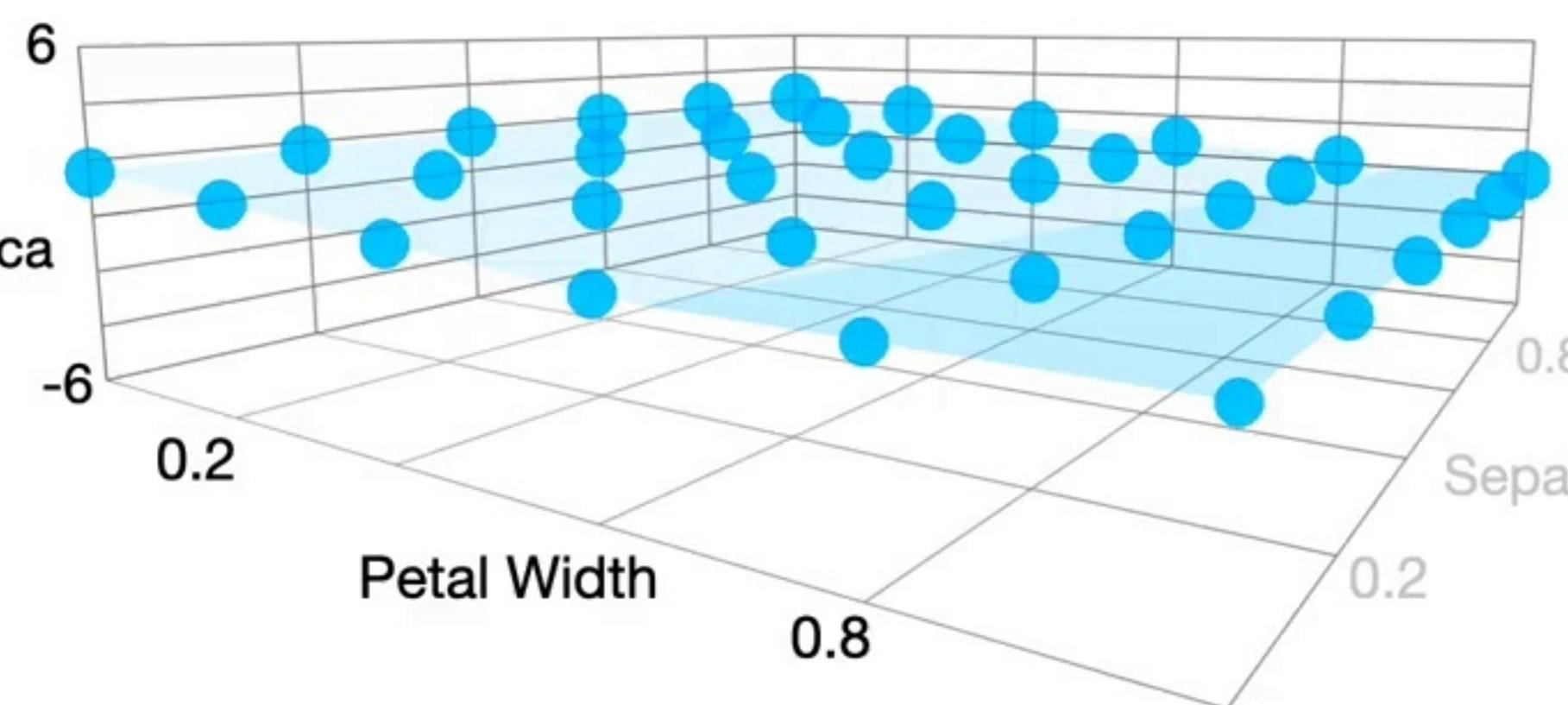


...let's determine the **crinkled surface** for **Virginica**.

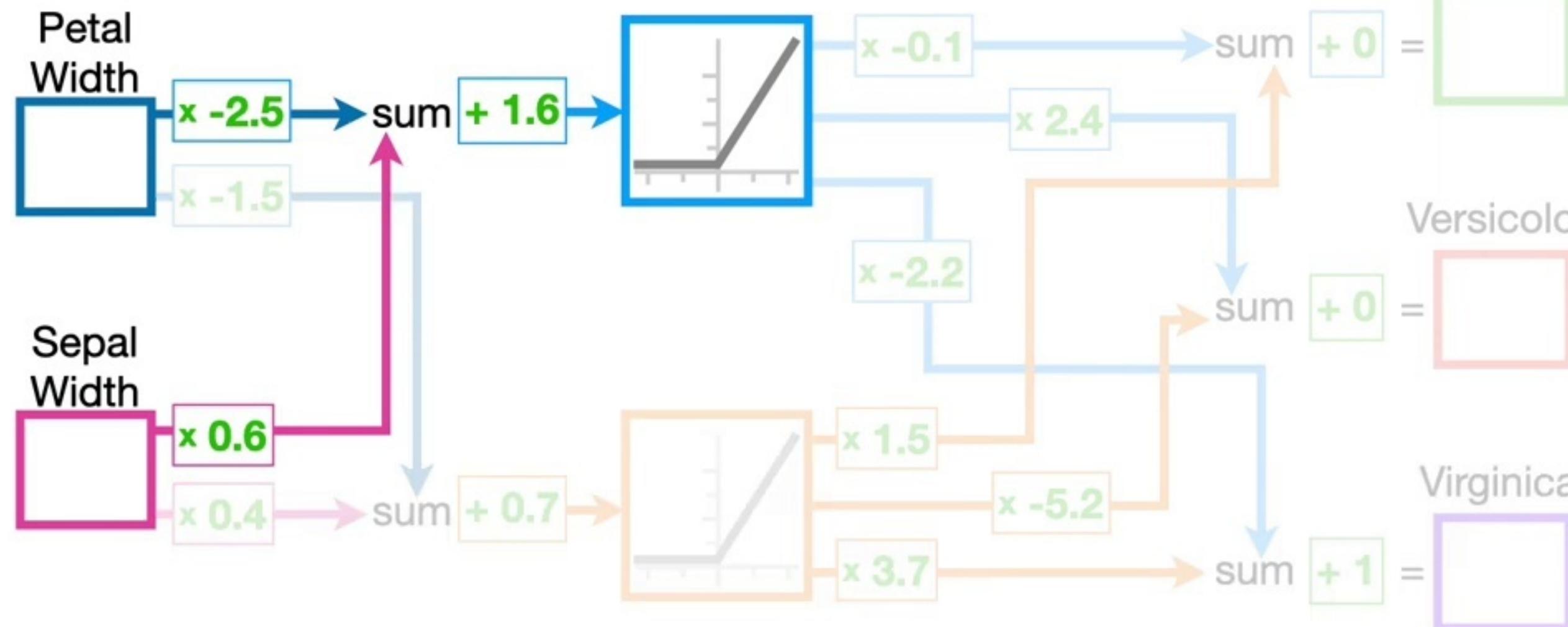




Virginica

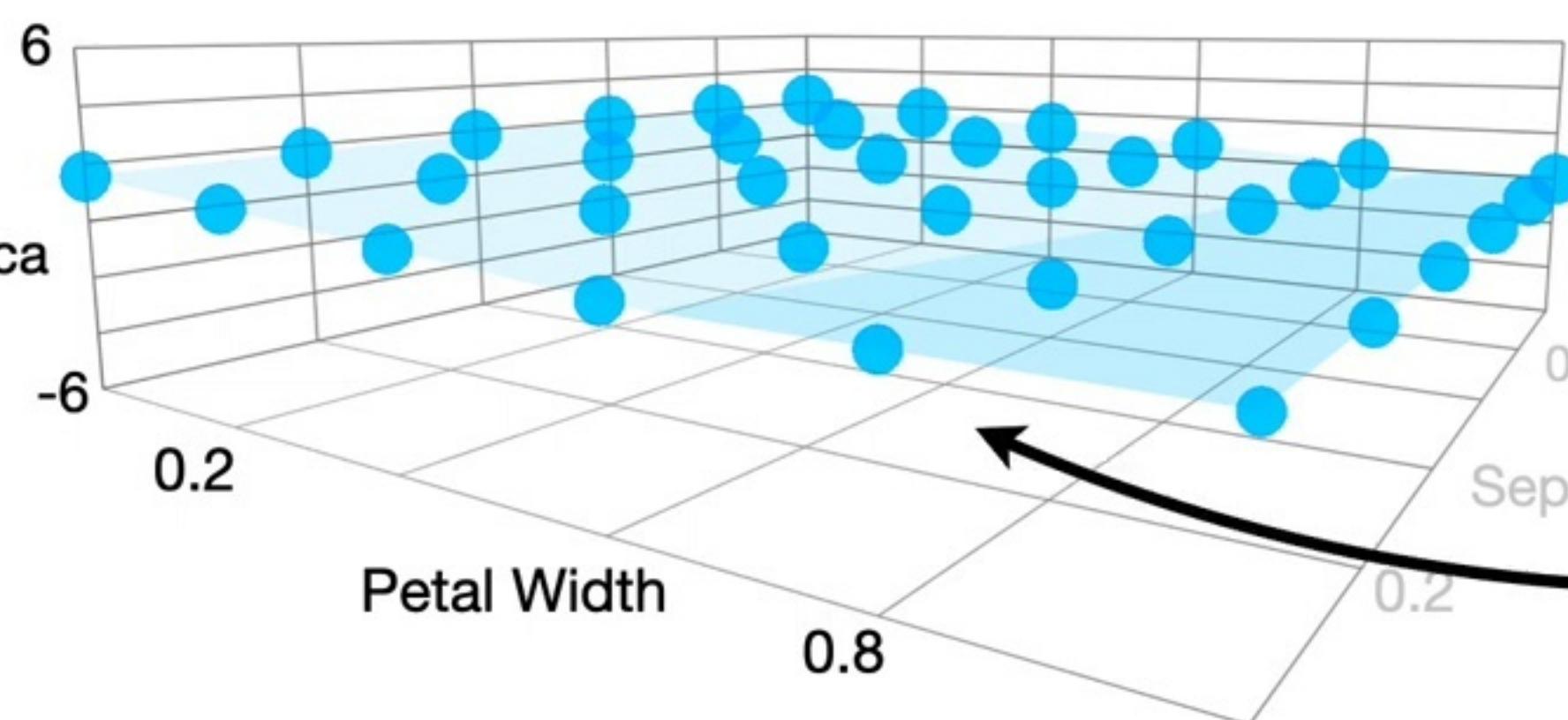


Just like before, we start with the **blue bent surface** from the top node in the **Hidden Layer...**



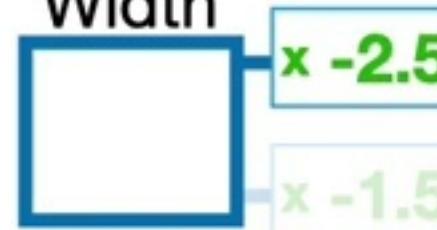


Virginica



...but now we multiply the y-axis coordinates by -2.2.

Petal Width



$$\times -2.5$$

$$+ 1.6$$

$$\times -1.5$$

sum

$$+ 1.6$$

$$\times -0.1$$

$$\times 2.4$$



$$\times -2.2$$

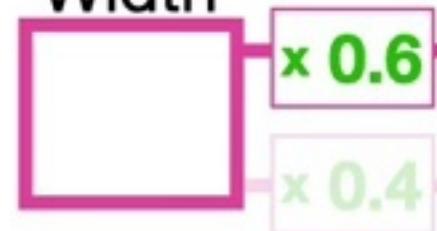
sum

$$+ 0$$



Setosa

Sepal Width



$$\times 0.6$$

$$+ 0.7$$

$$\times 0.4$$

sum

$$+ 0.7$$

$$\times 1.5$$

$$\times -5.2$$

$$\times 3.7$$



sum

$$+ 0$$



Versicolor

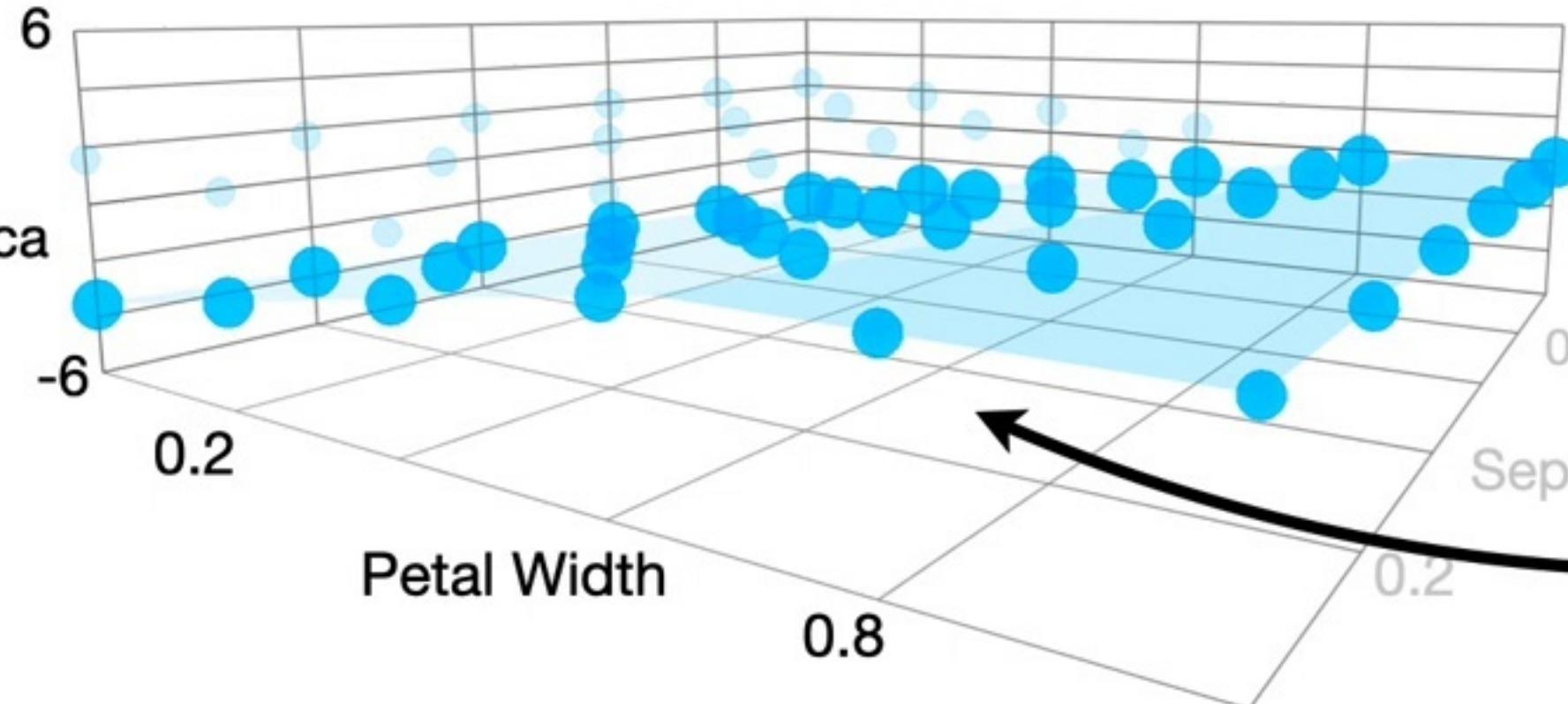
Virginica

$$+ 1$$



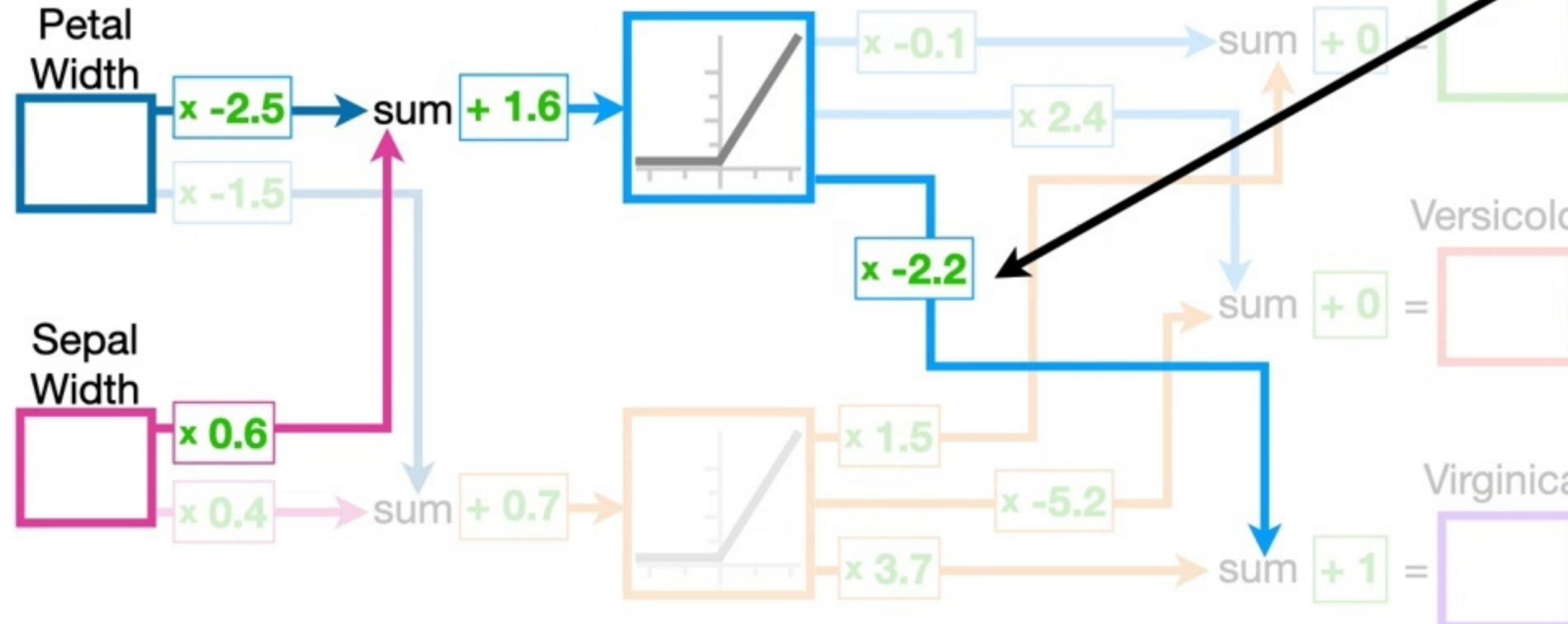


Virginica



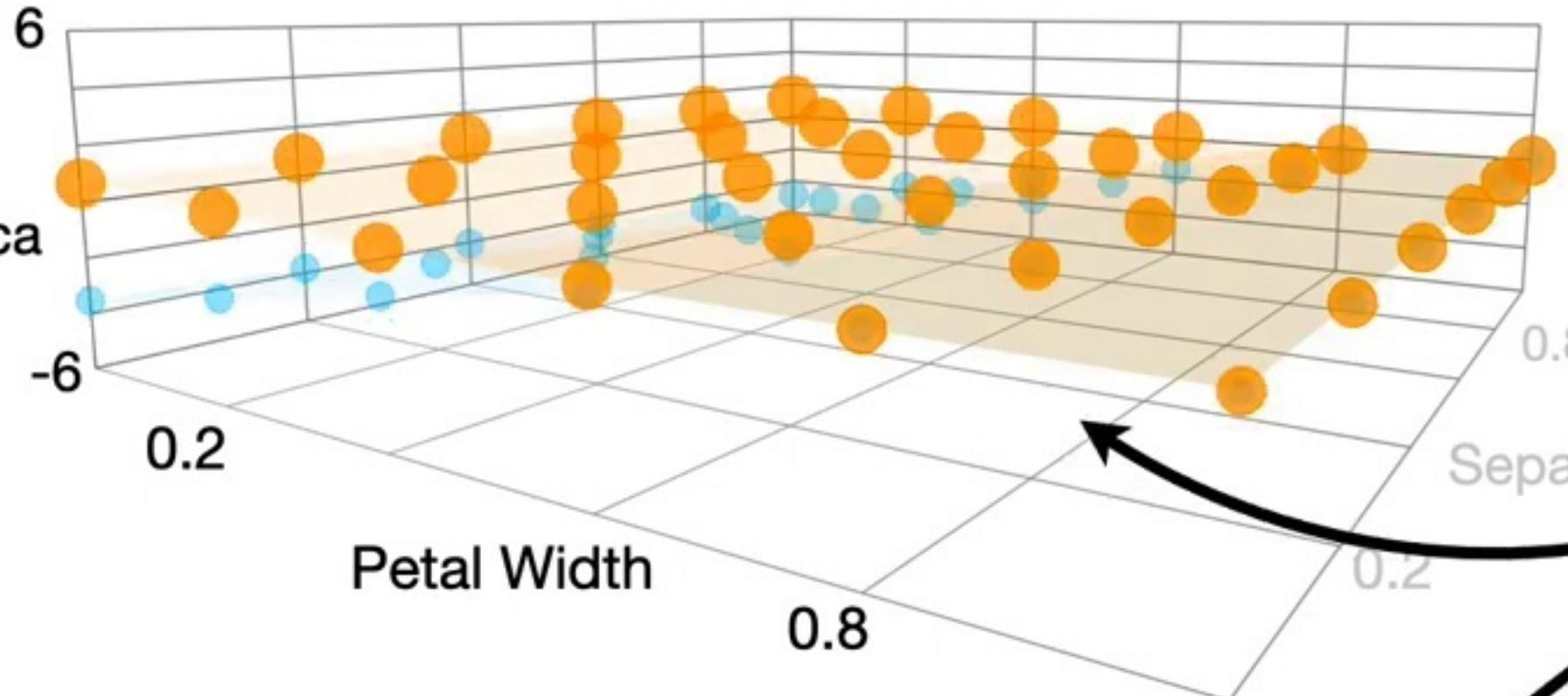
...but now we multiply the y-axis coordinates by -2.2.

Petal Width  
Sepal Width



double  
BAM!!  
**SQ!**

Virginica



And just like before, we create the **orange bent surface** from the bottom node in the **Hidden Layer**...

Petal Width



$$\times -2.5 \rightarrow \text{sum}$$

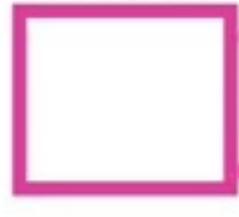
$$+ 1.6 \rightarrow \text{sum}$$

$$\times -1.5 \rightarrow \text{sum}$$



$$\text{sum} = \max(0, \dots)$$

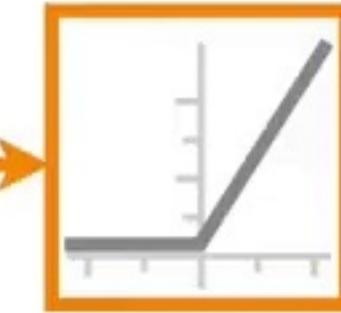
Sepal Width



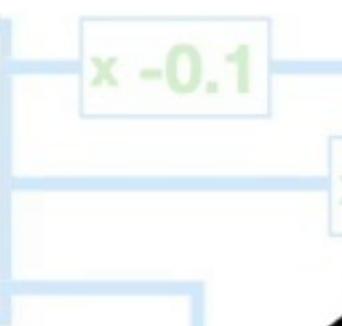
$$\times 0.6 \rightarrow \text{sum}$$

$$+ 0.4 \rightarrow \text{sum}$$

$$\times 0.7 \rightarrow \text{sum}$$



$$\text{sum} = \max(0, \dots)$$



$$\text{sum} = \max(0, \dots)$$



$$\text{sum} = \max(0, \dots)$$



$$\text{sum} = \max(0, \dots)$$



$$\text{sum} = \max(0, \dots)$$

Setosa



Versicolor

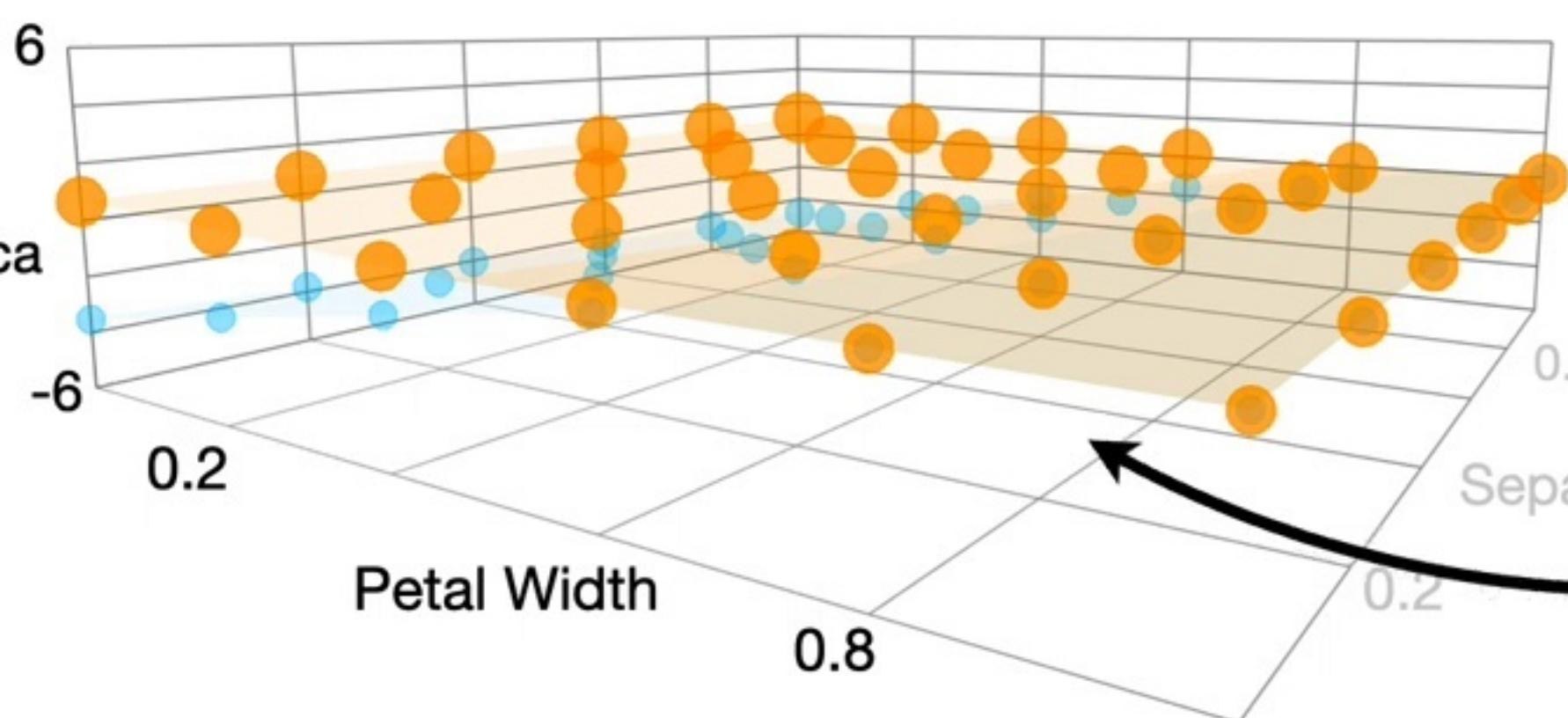


Virginica





Virginica



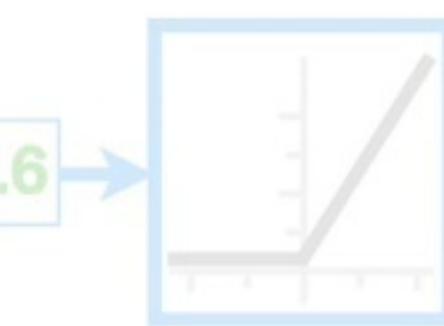
...but now we multiply  
the y-axis coordinates  
by 3.7.

Petal  
Width



$$\times -2.5 \rightarrow \text{sum}$$

$$+ 1.6 \rightarrow \text{sum}$$



$$\times -0.1 \rightarrow \text{sum}$$

$$\times 2.4 \rightarrow \text{sum}$$

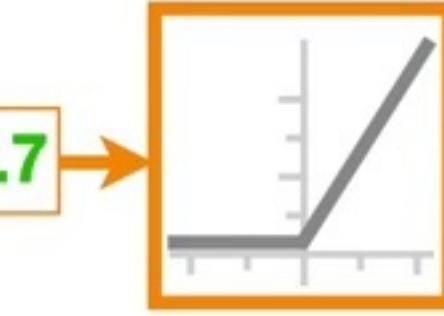
$$+ 0 = \boxed{\text{Setosa}}$$

Sepal  
Width



$$\times 0.6 \rightarrow \text{sum}$$

$$+ 0.7 \rightarrow \text{sum}$$



$$\times 1.5 \rightarrow \text{sum}$$

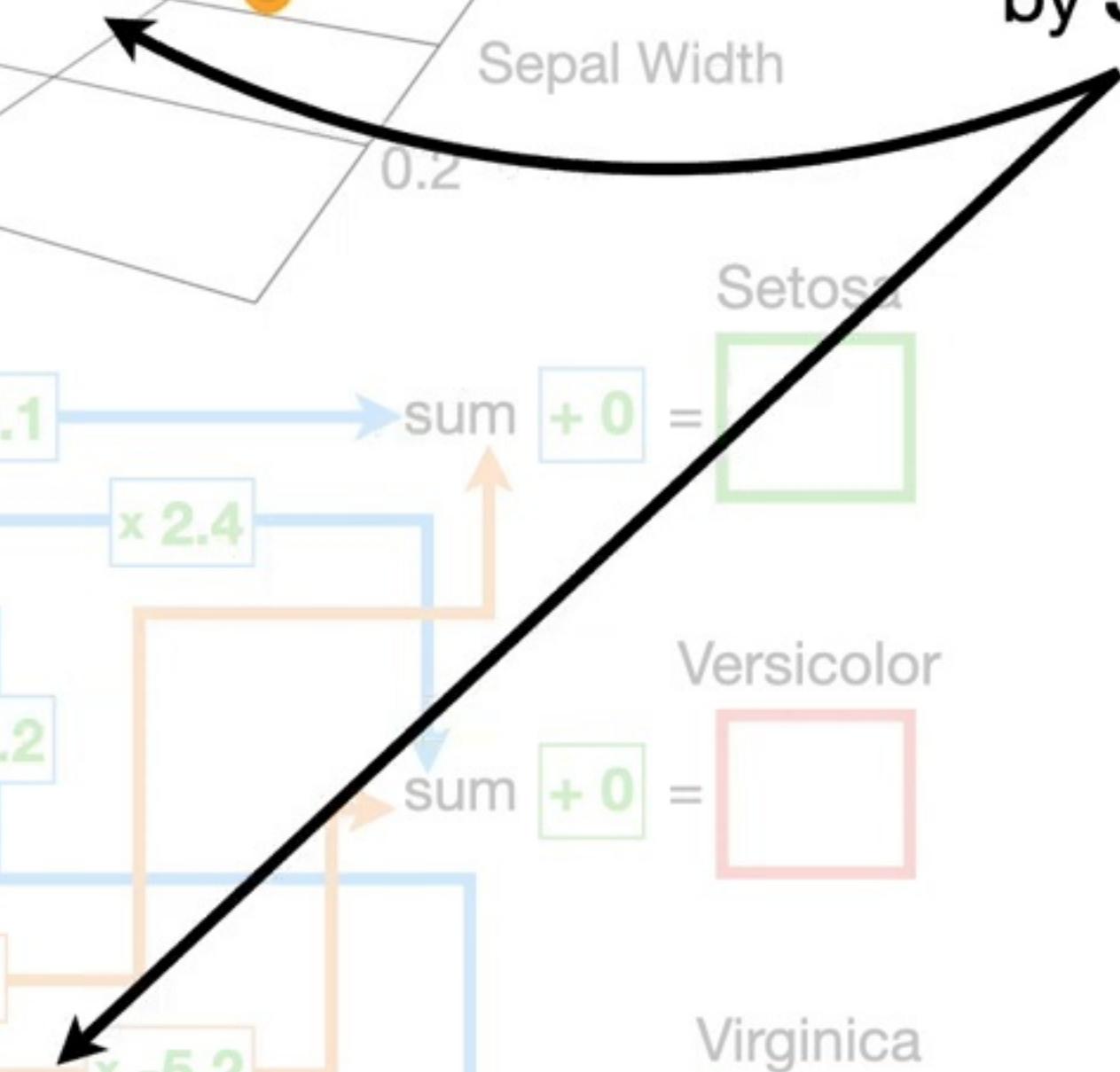
$$\times -5.2 \rightarrow \text{sum}$$

$$+ 1 = \boxed{\text{Virginica}}$$

Setosa

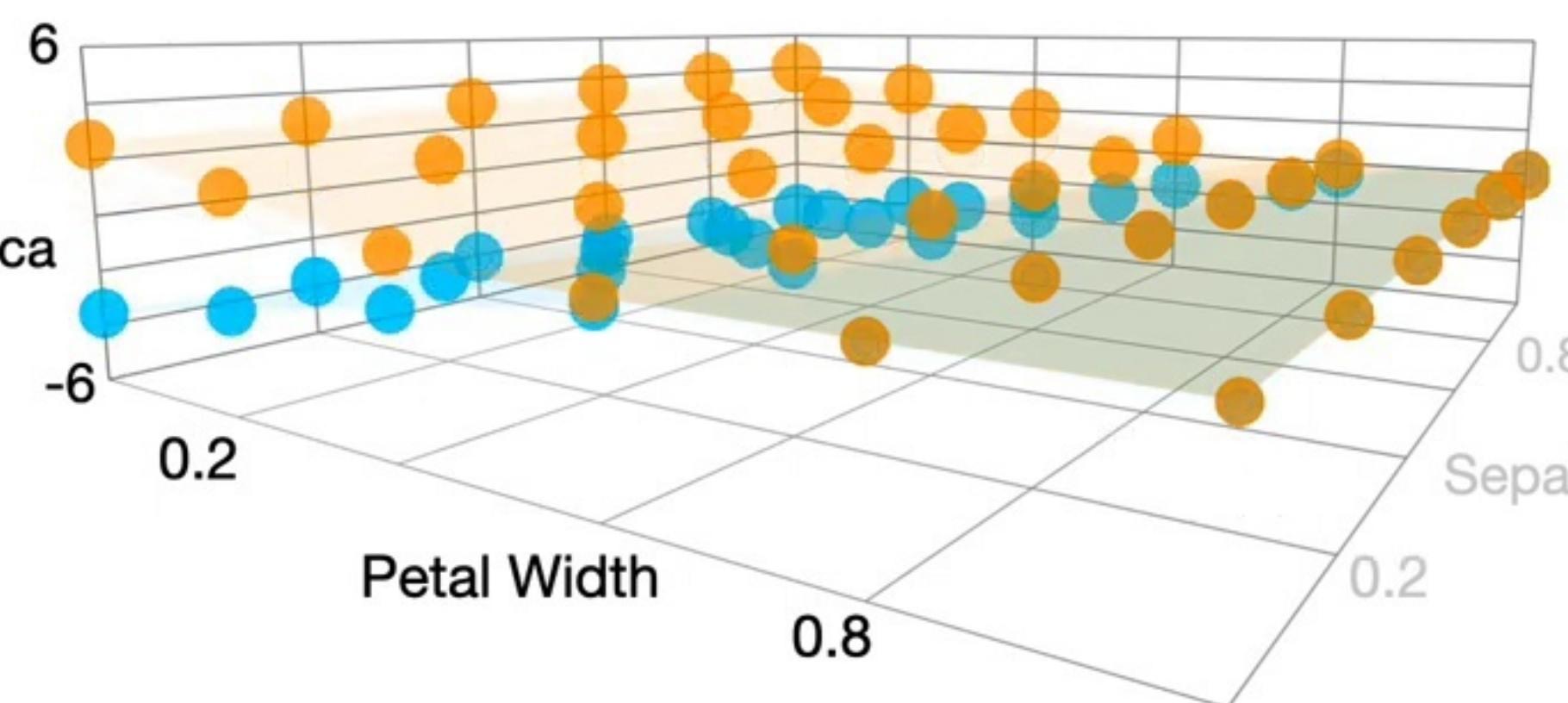
Versicolor

Virginica

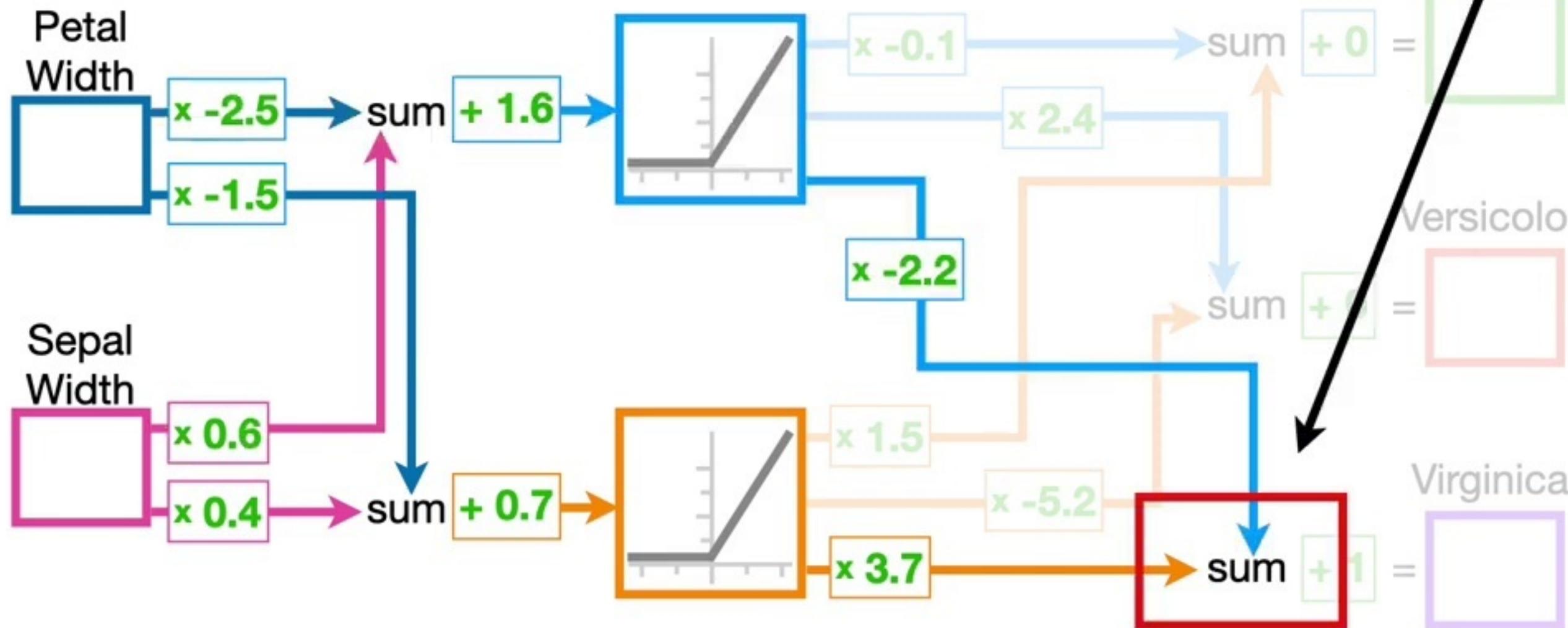




Virginica

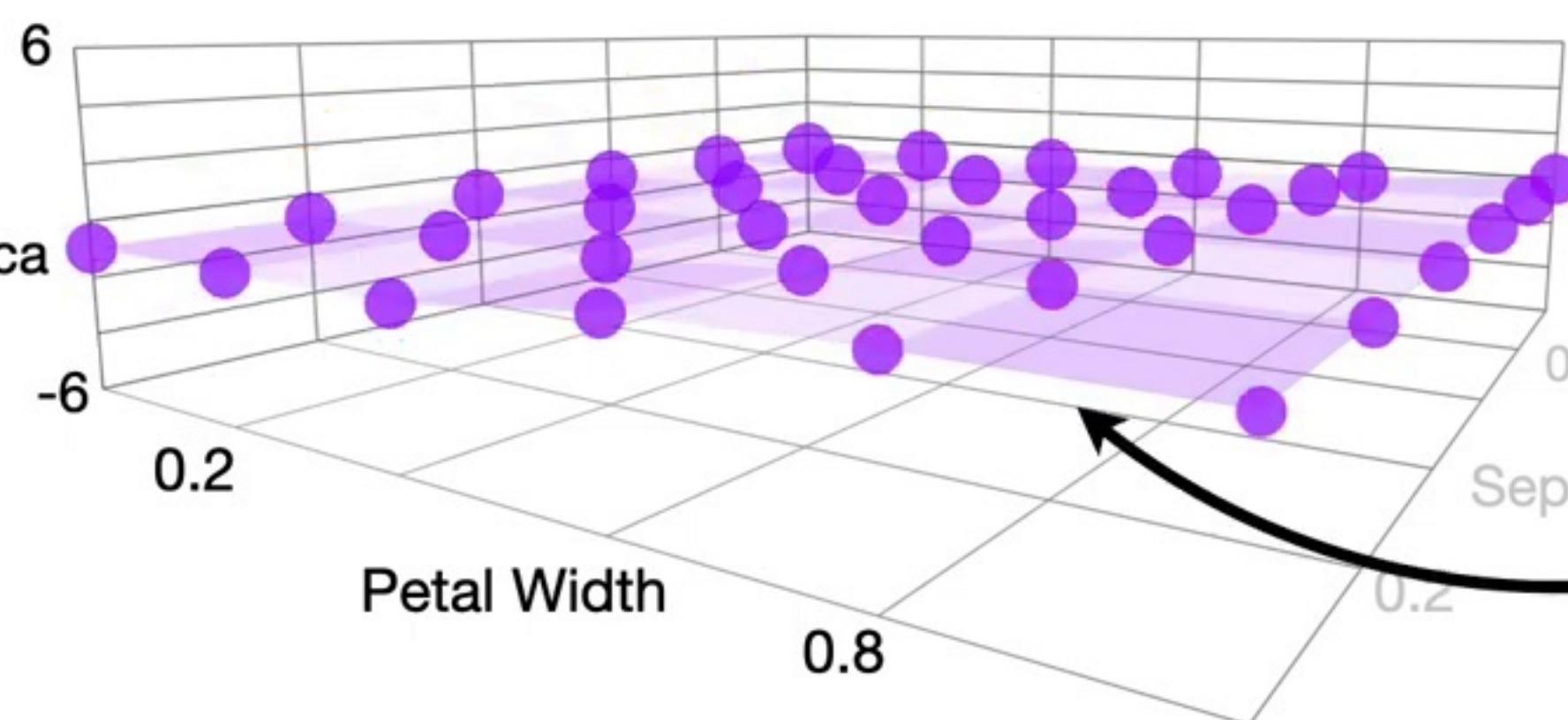


Now we add the y-axis coordinates from the two bent surfaces together...

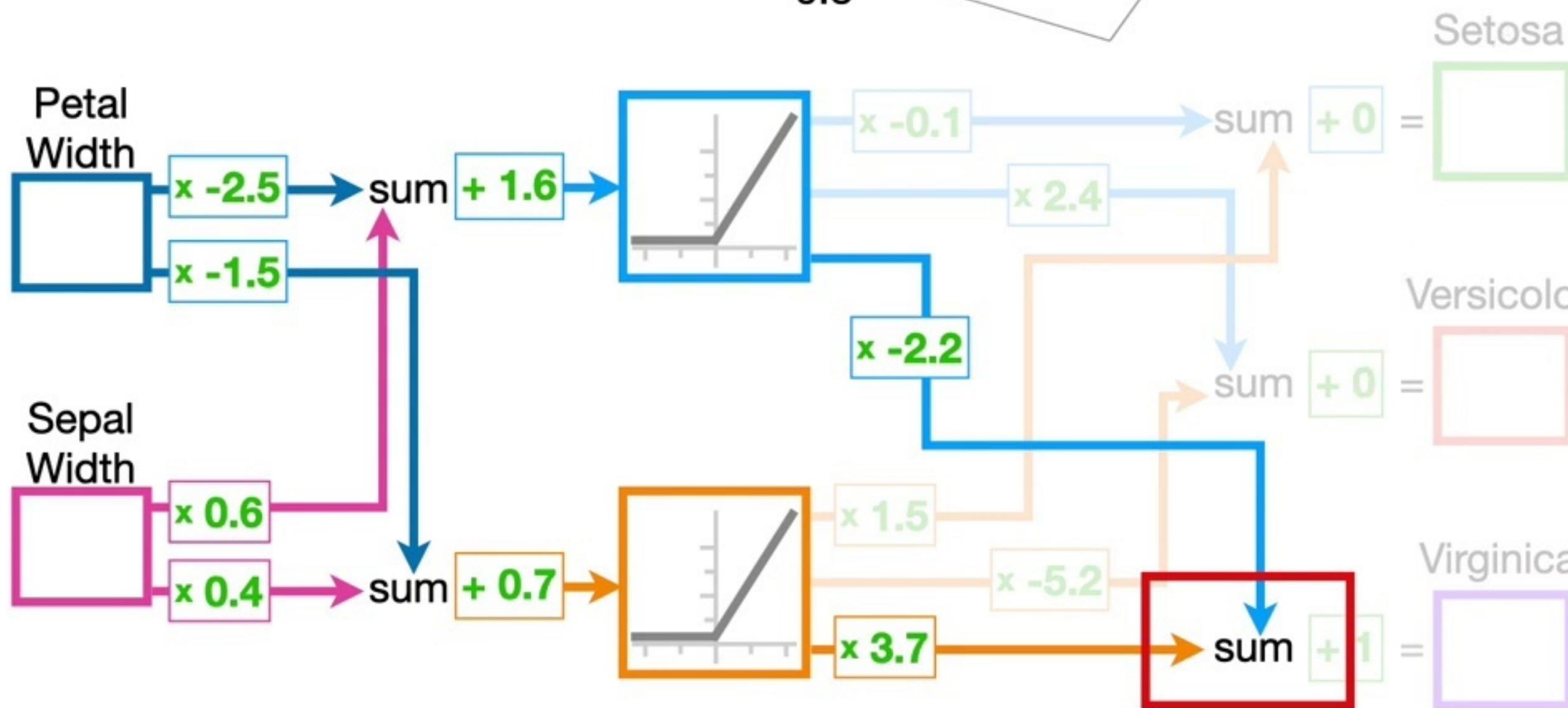




Virginica

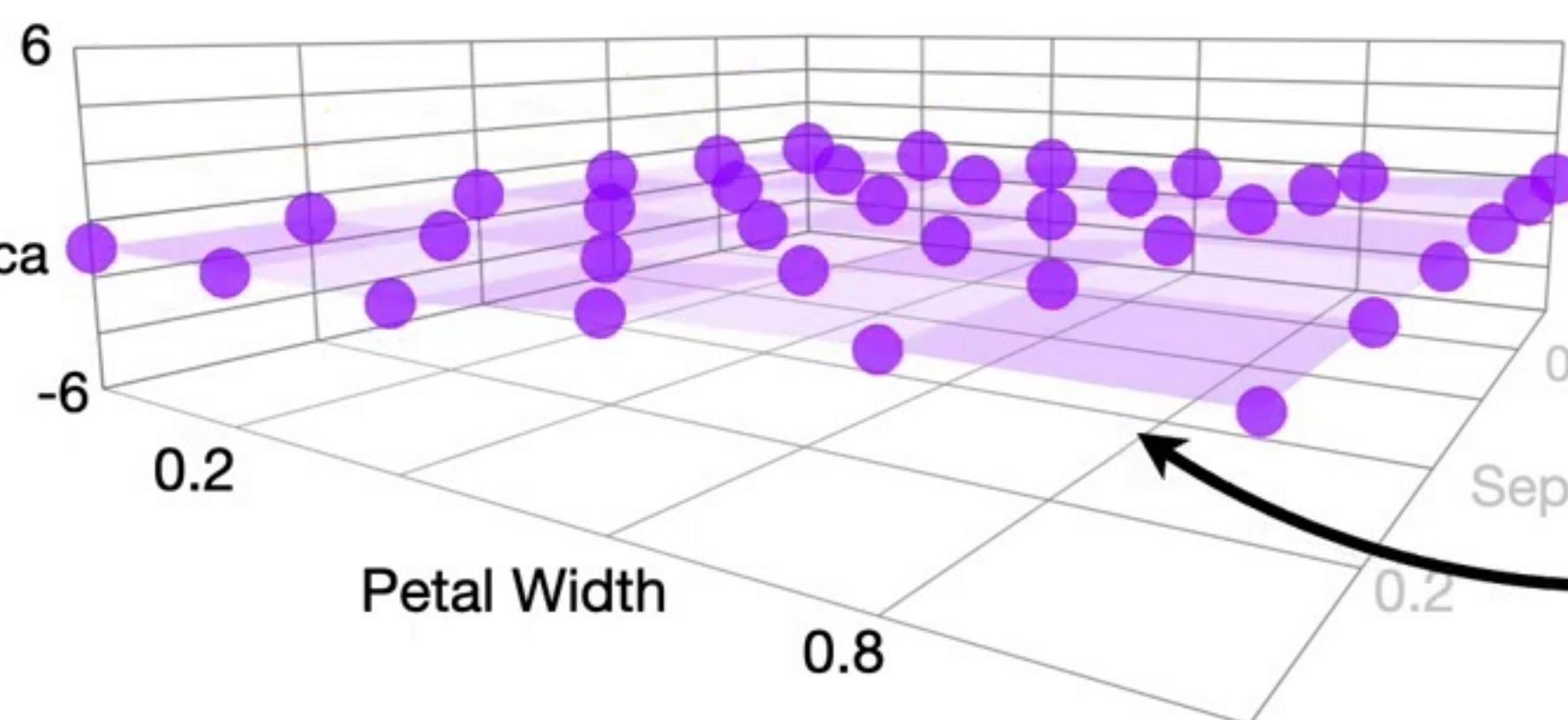


...and get this **purple crinkled surface**.

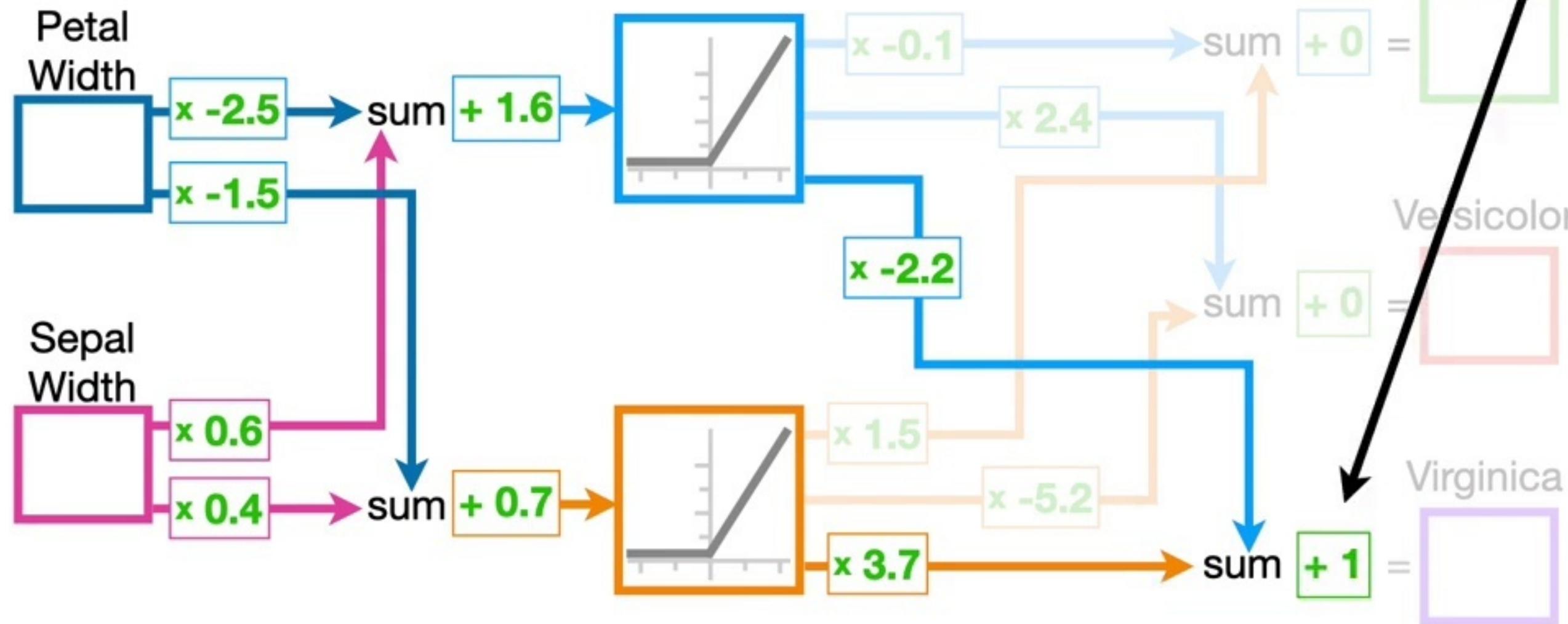




Virginica

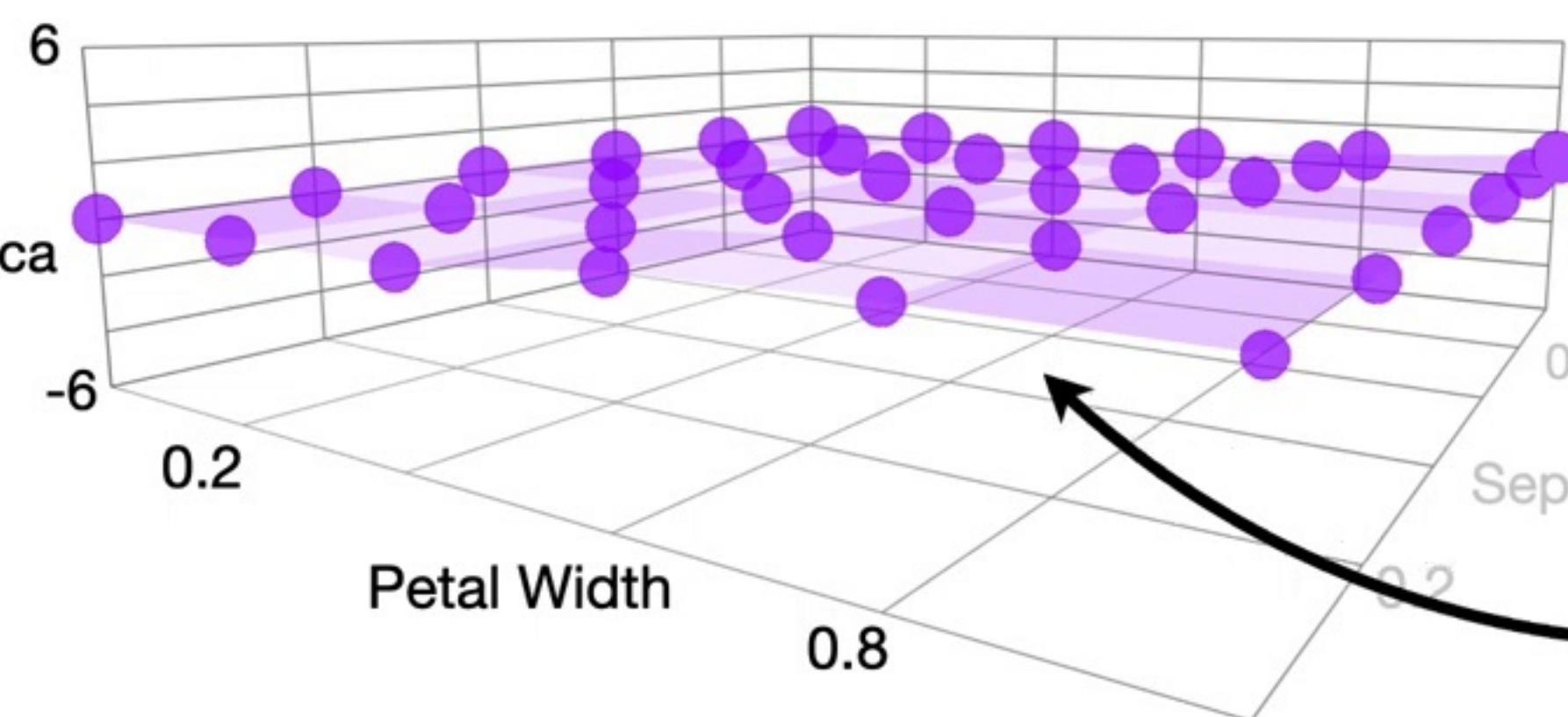


Lastly, we add the final **Bias, 1**, to the y-axis coordinates on the **purple crinkled surface**...

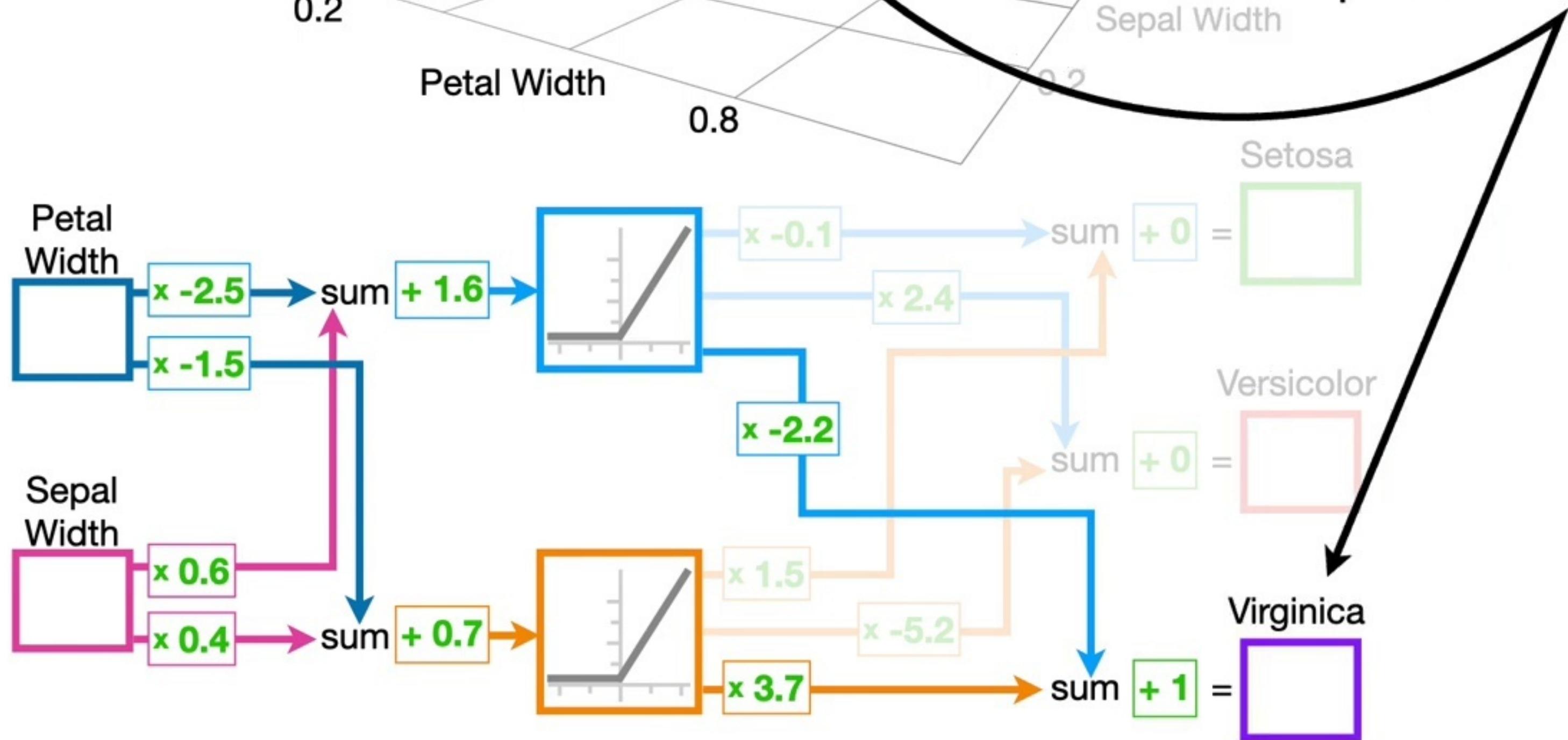




Virginica

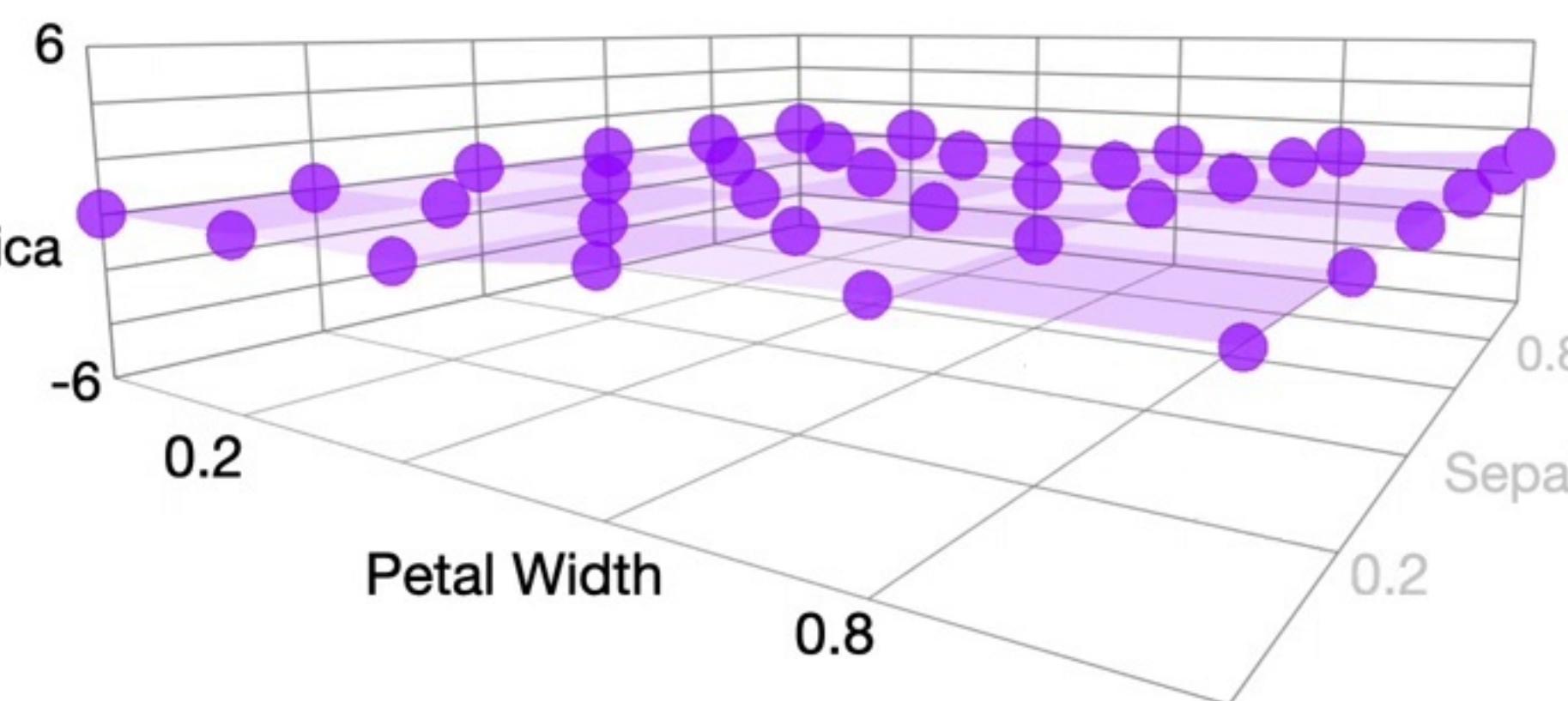


...and that gives us the final surface for predicting if the Iris species is **Virginica**.

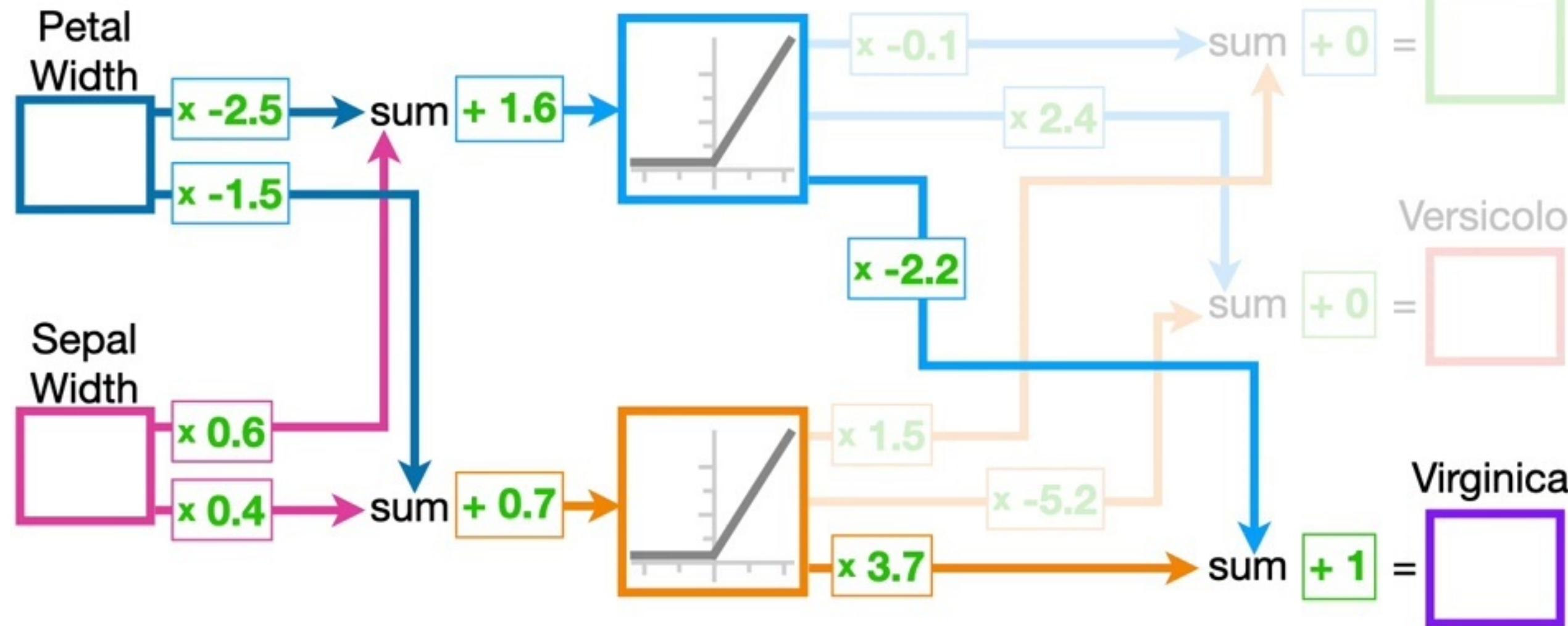




Virginica

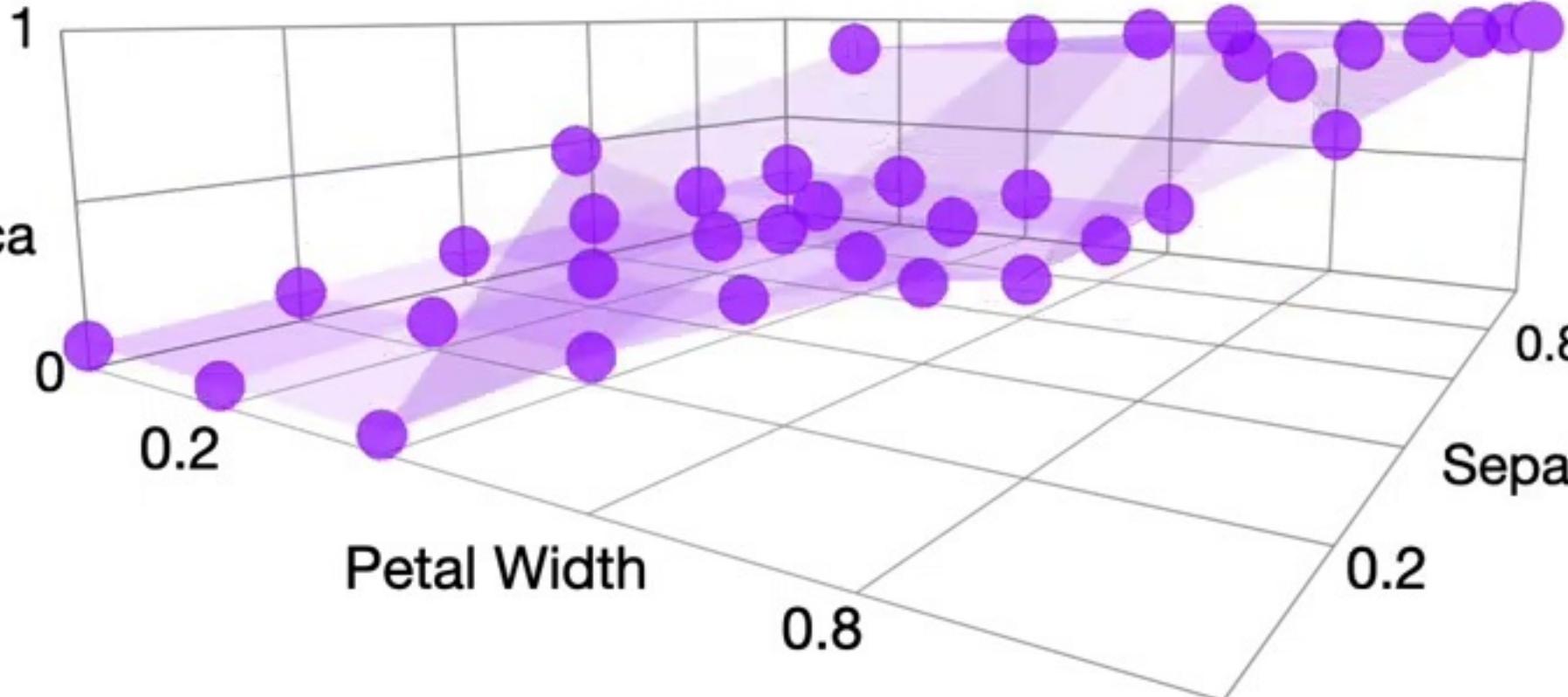


Now, so we can see what's going on, let's change the scale for the y-axis from -6 to 6...

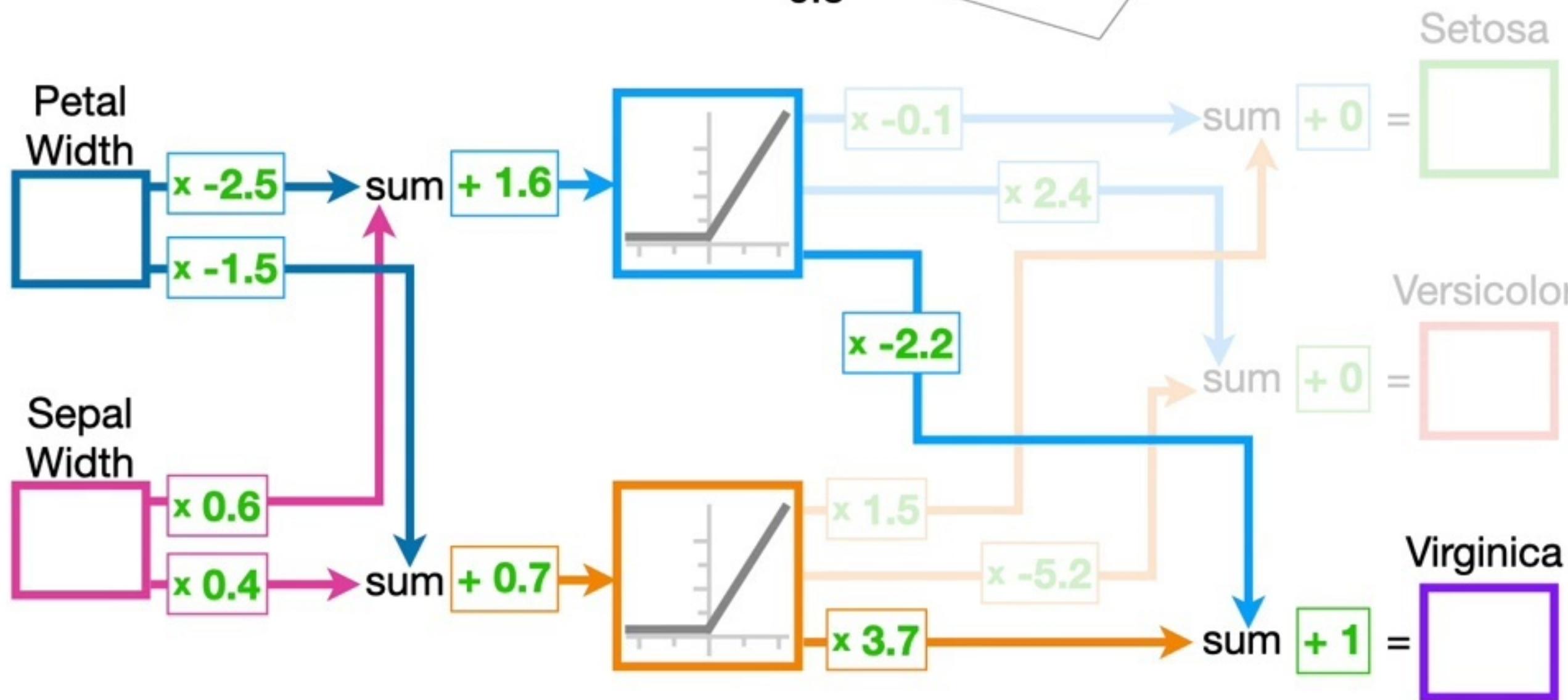




Virginica

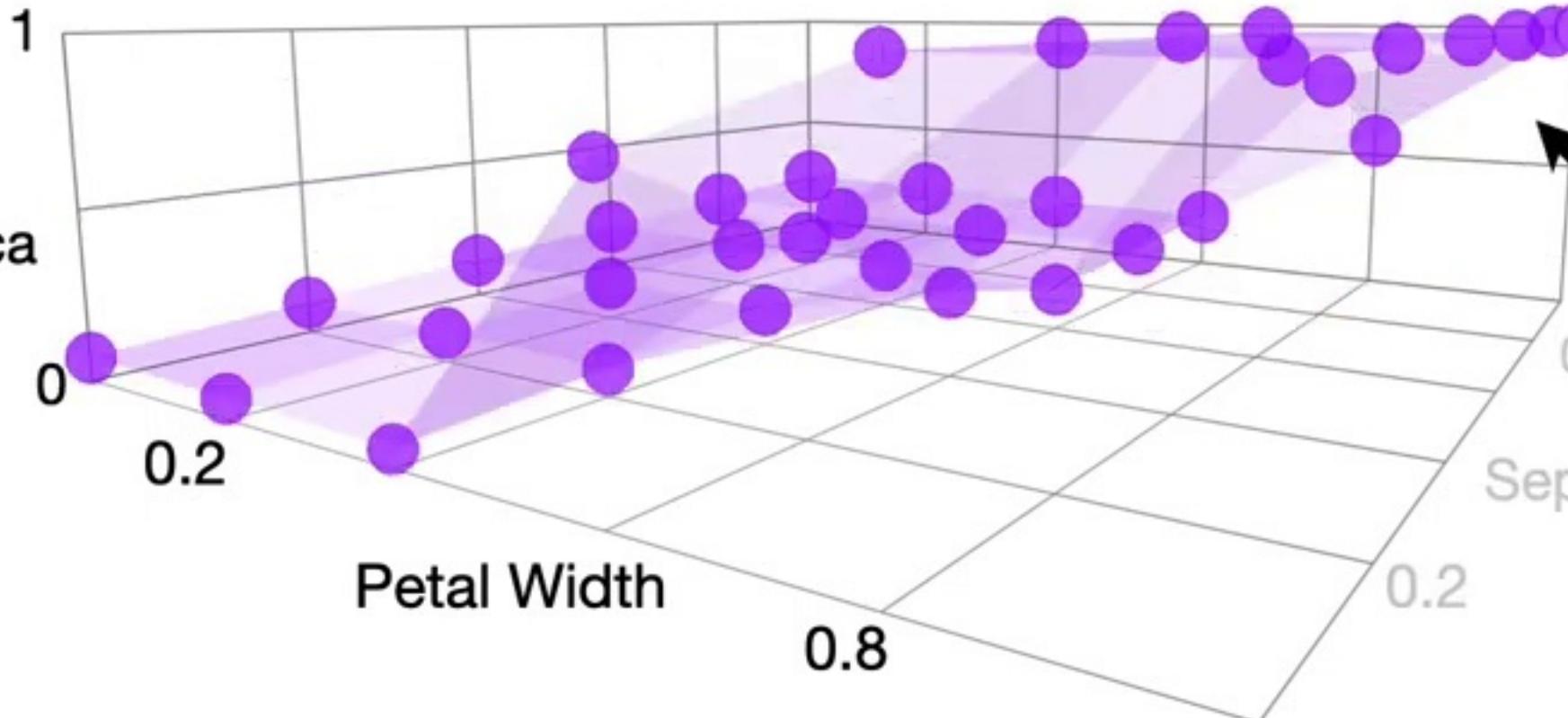


...to 0 to 1.

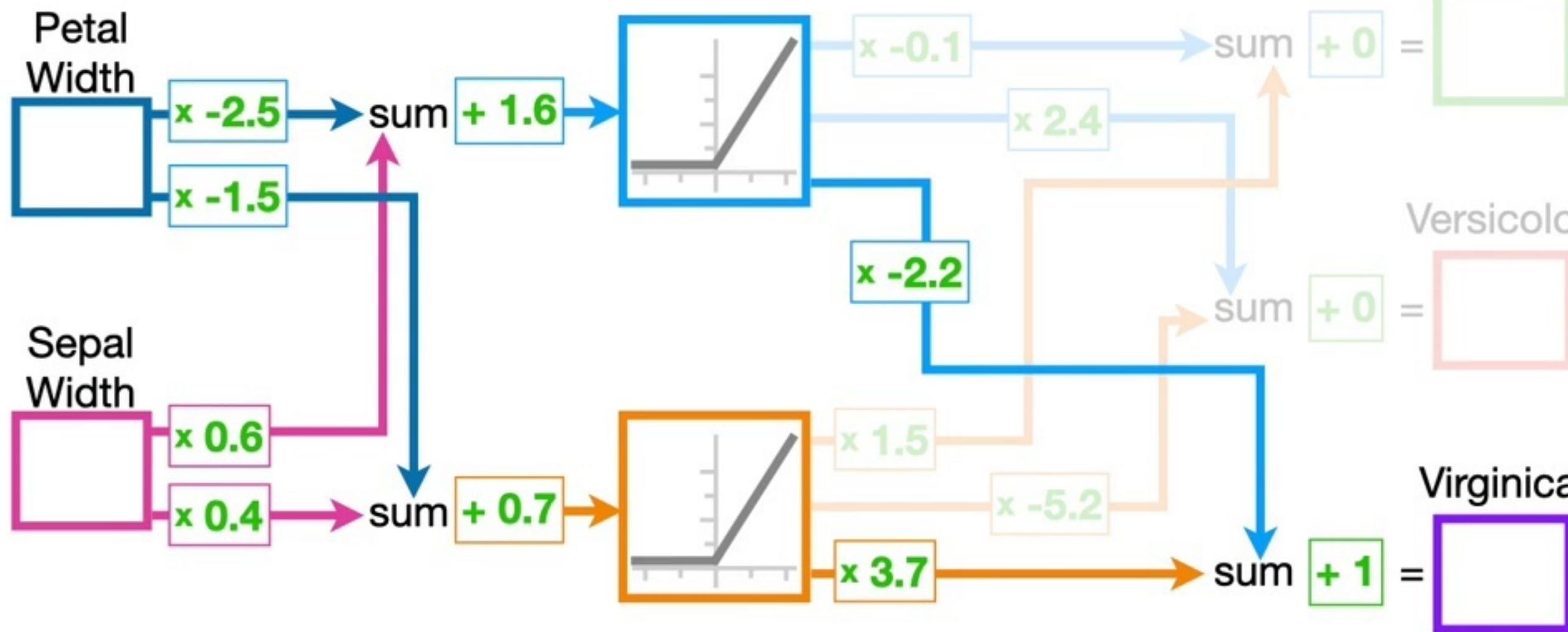


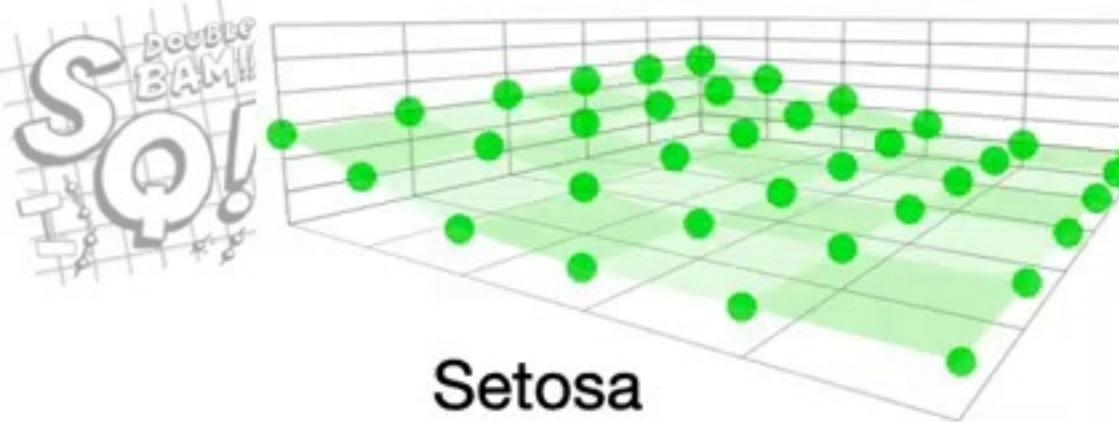
**SQ!**  
double  
BAM!!

Virginica

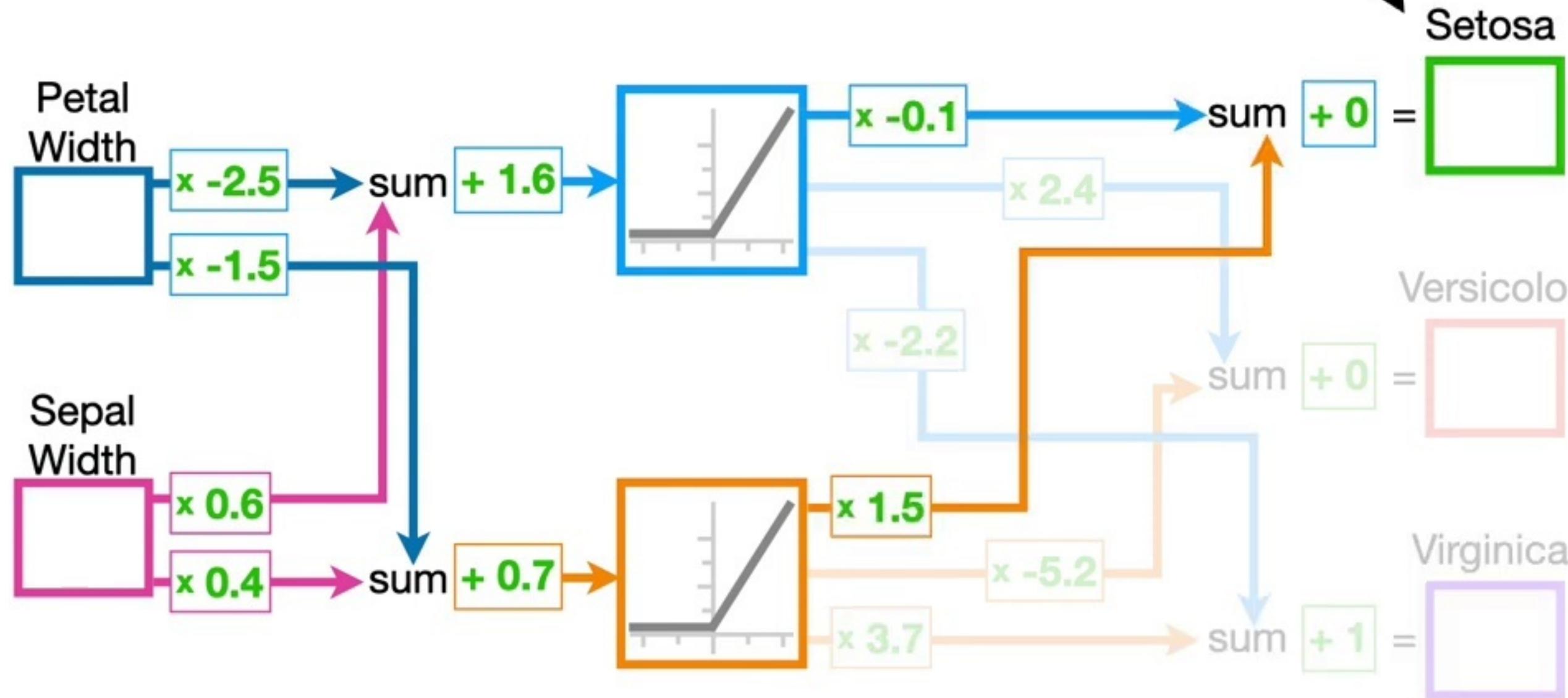


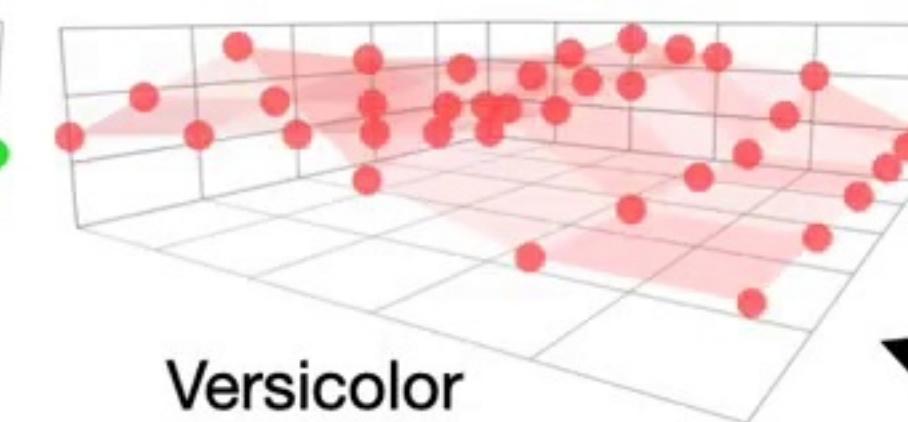
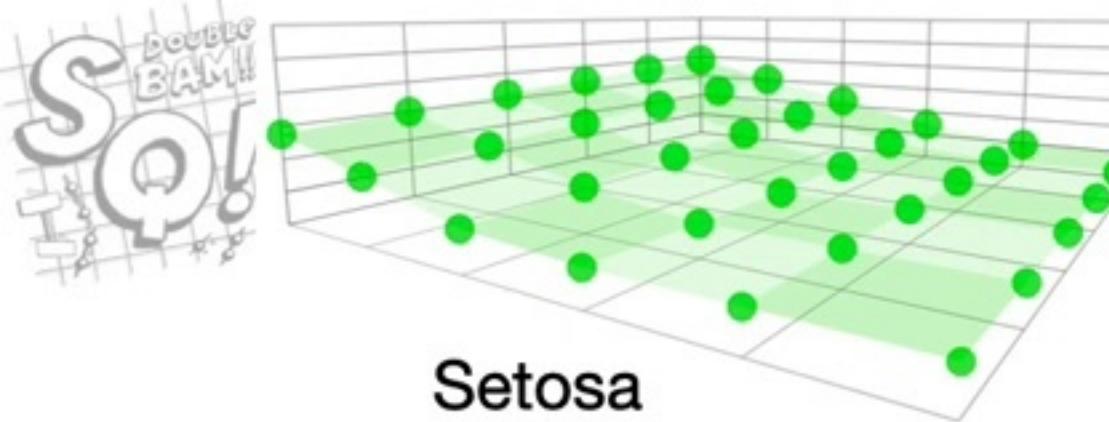
Now we see that when **Petal Width** is close to 1 (the widest), then we will get a high score for **Virginica**.



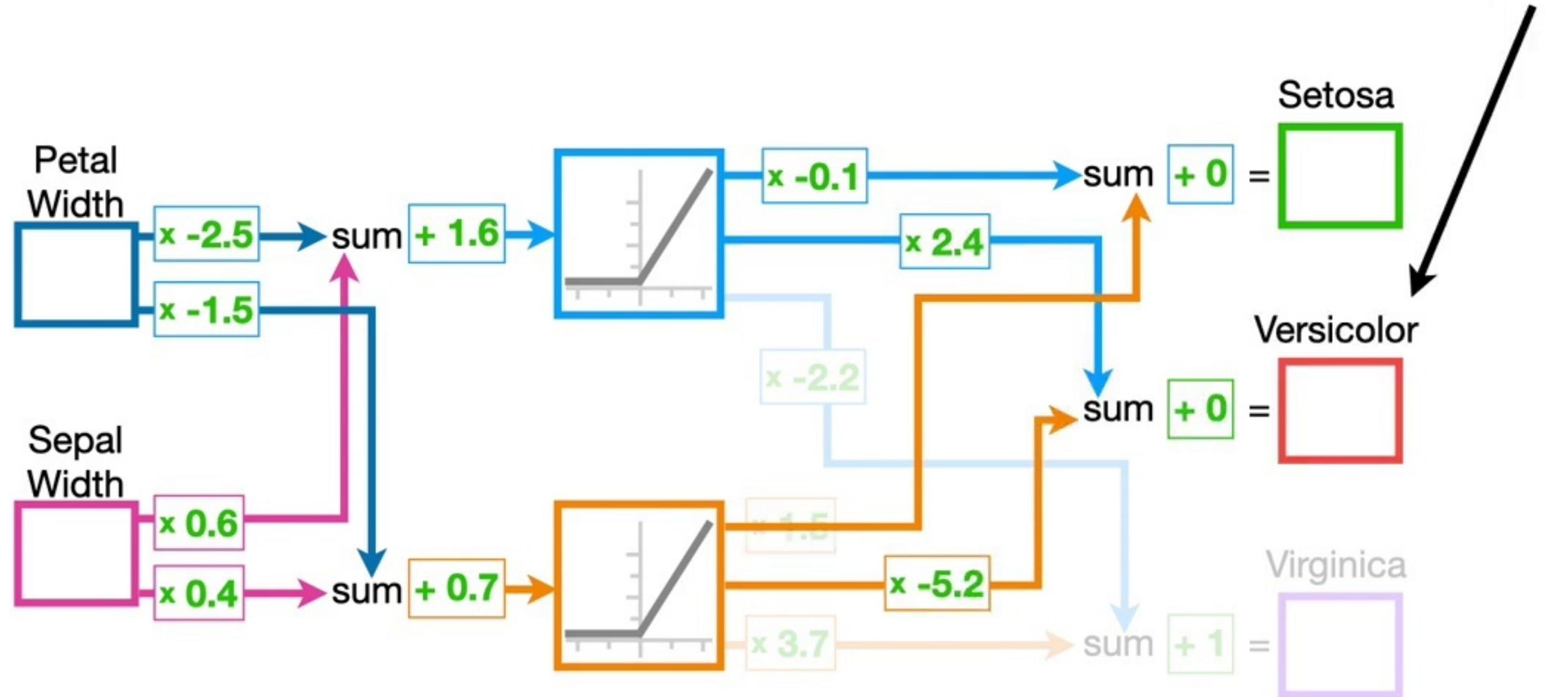


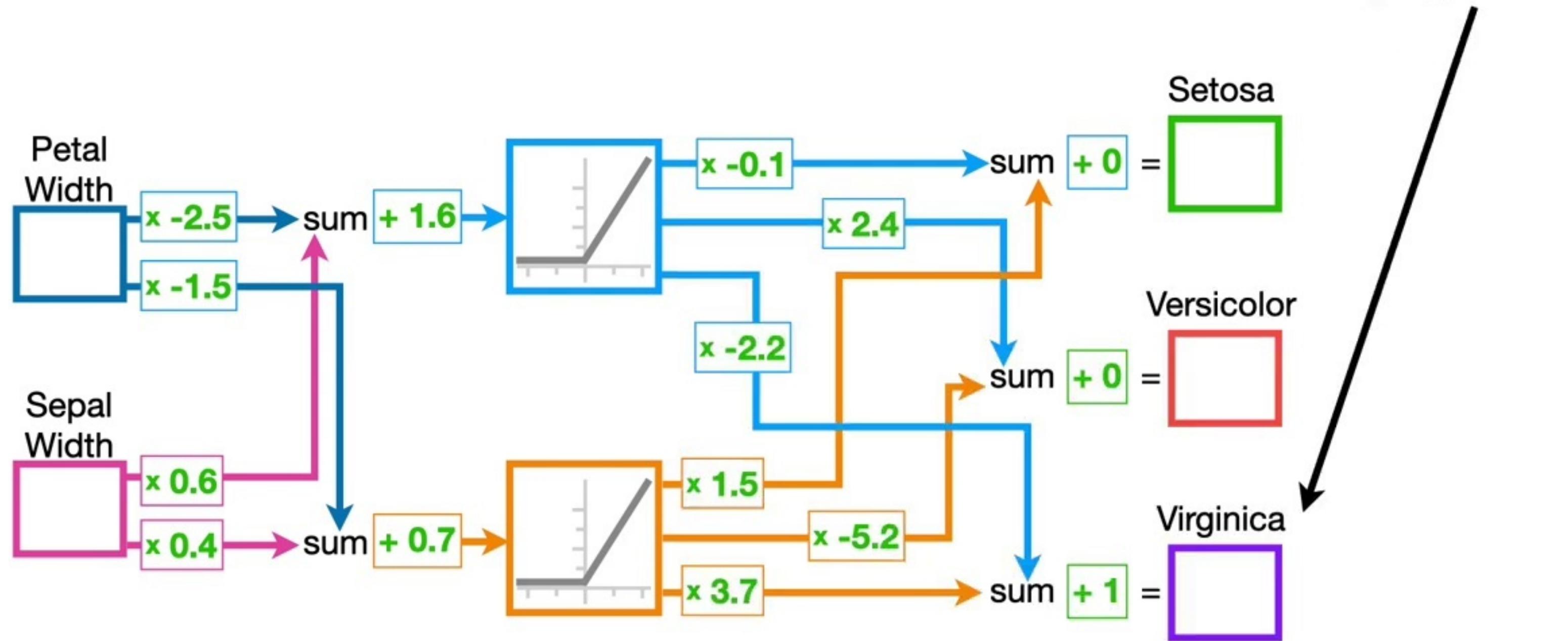
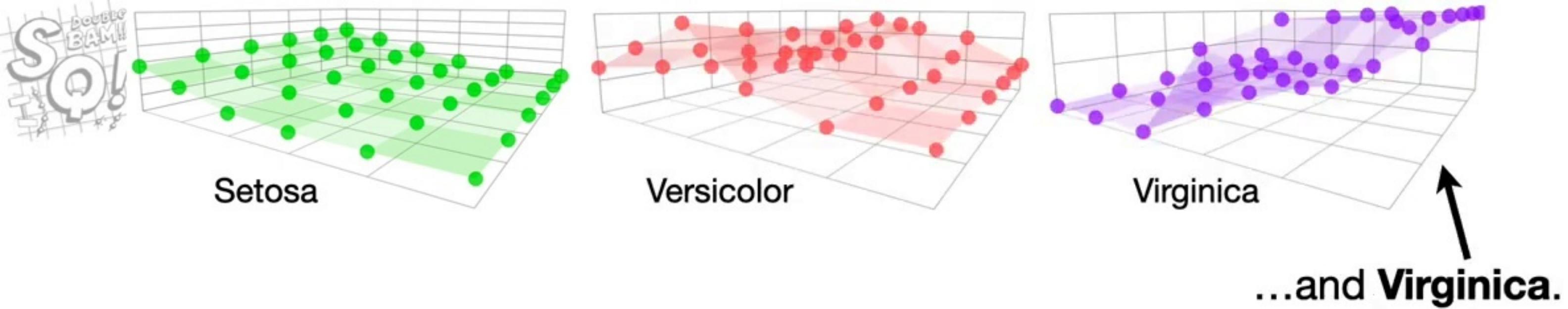
At long last, we have  
**crinkled surfaces** for  
**Setosa...**

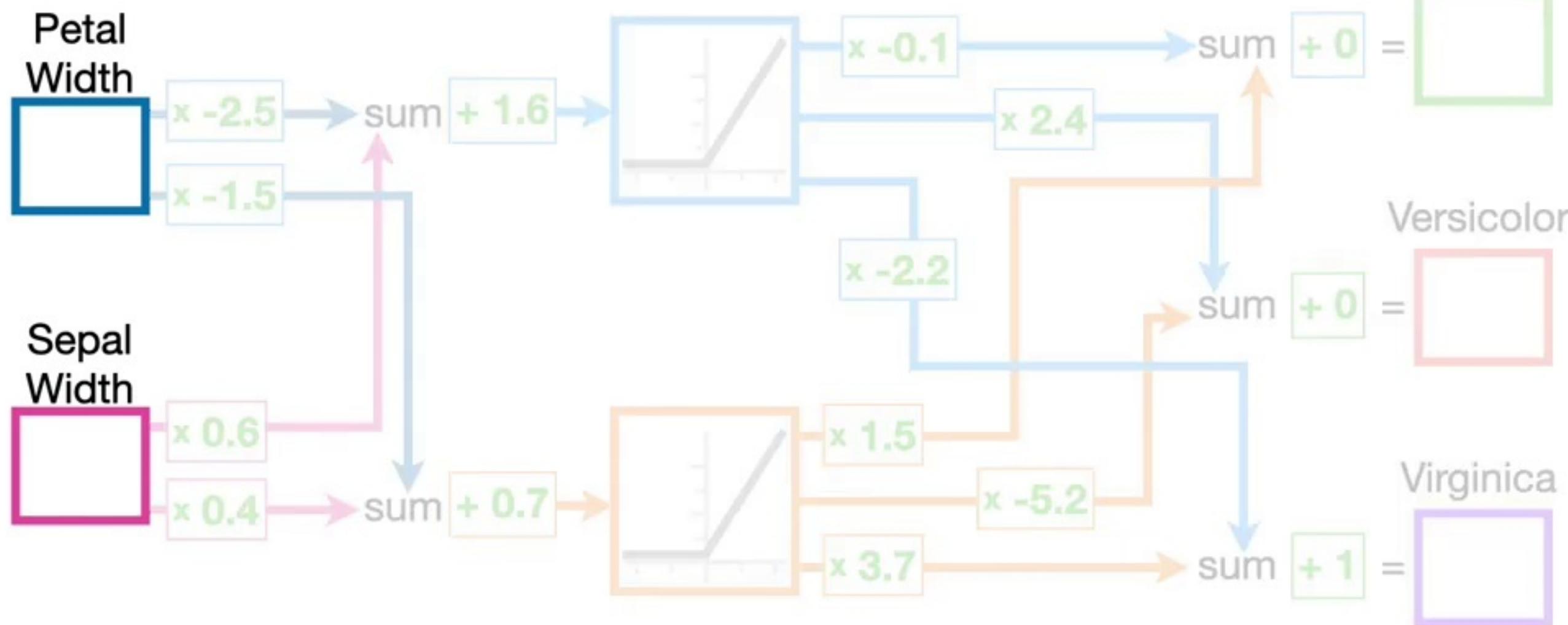
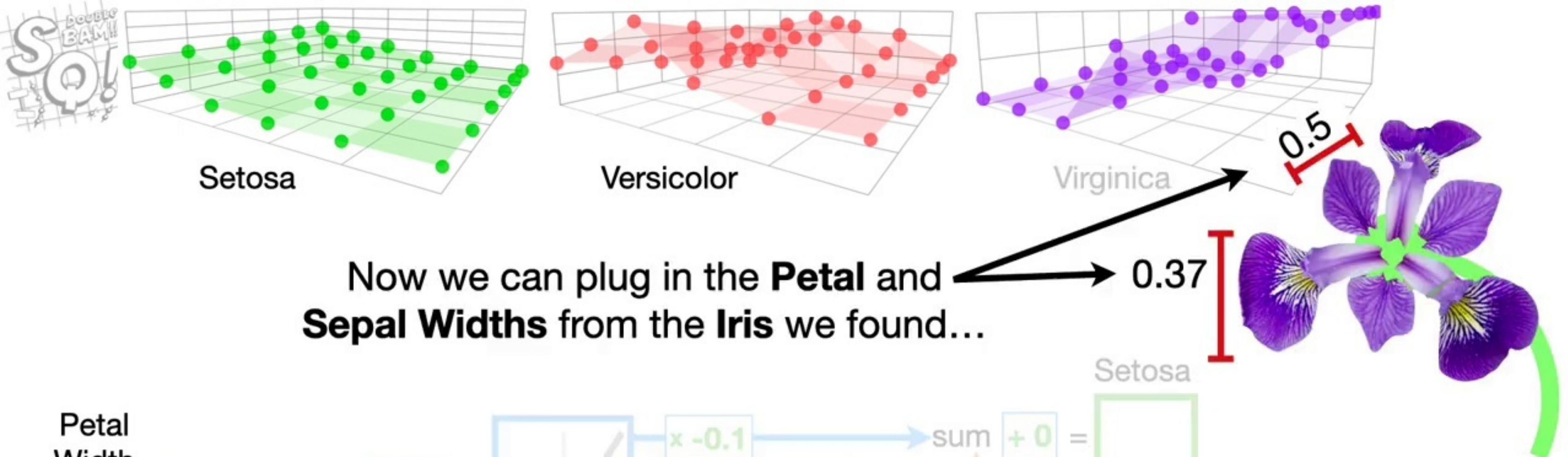


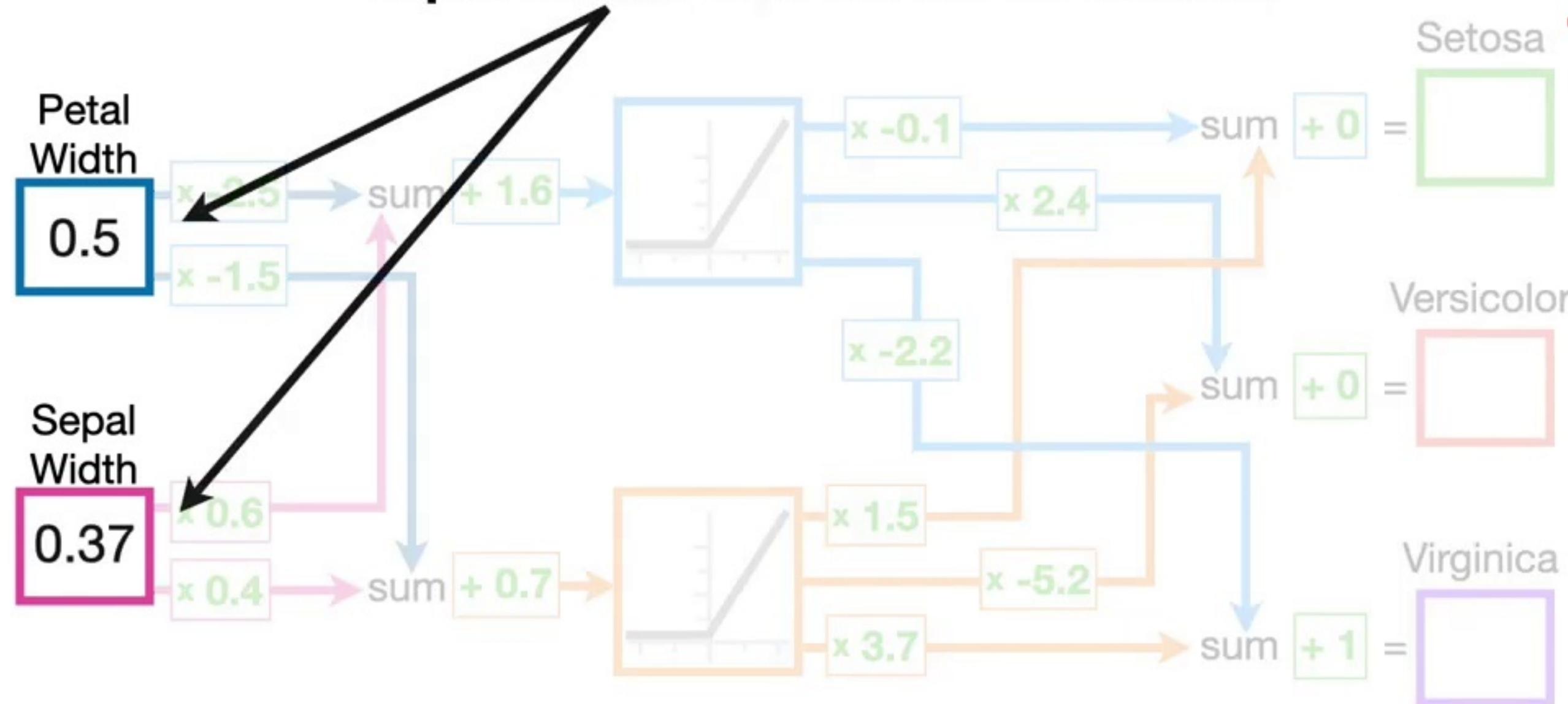
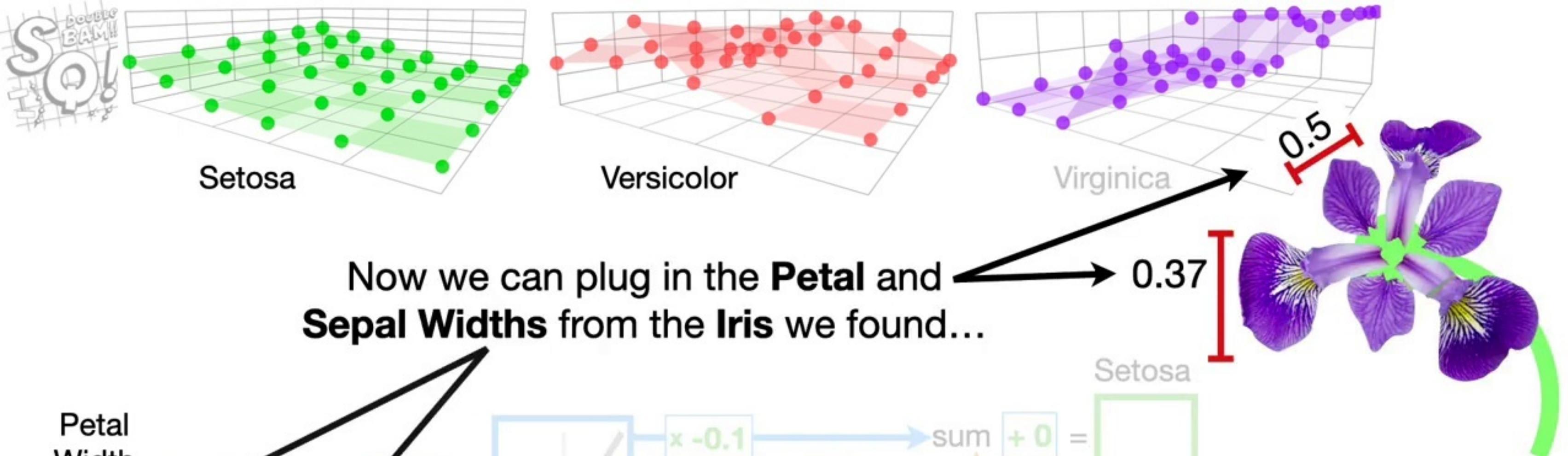


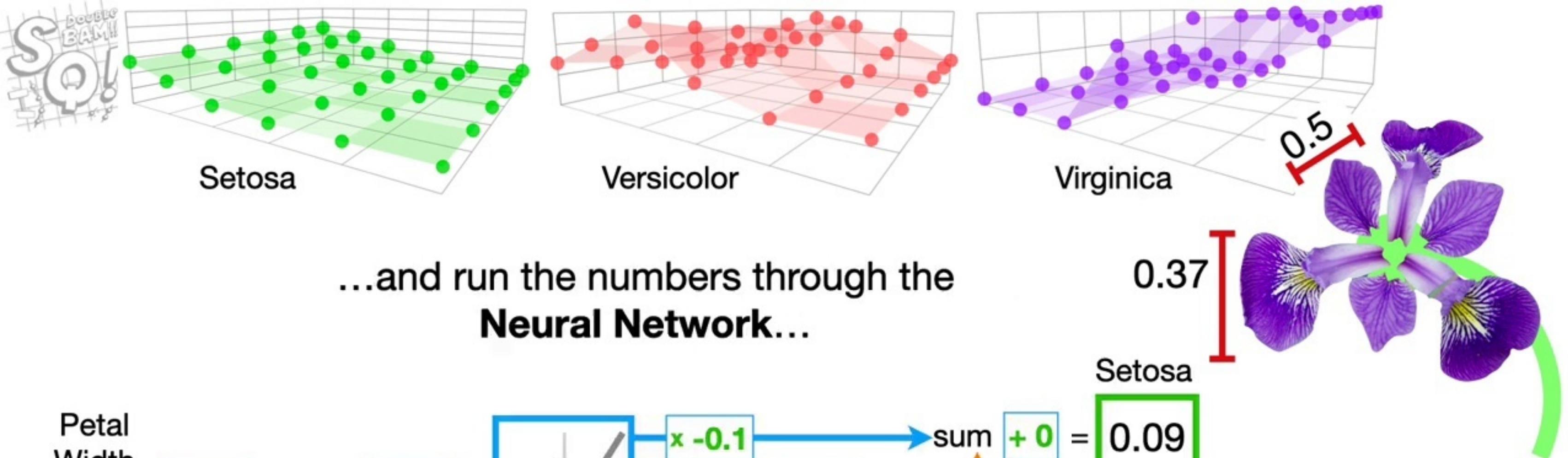
**...Versicolor...**



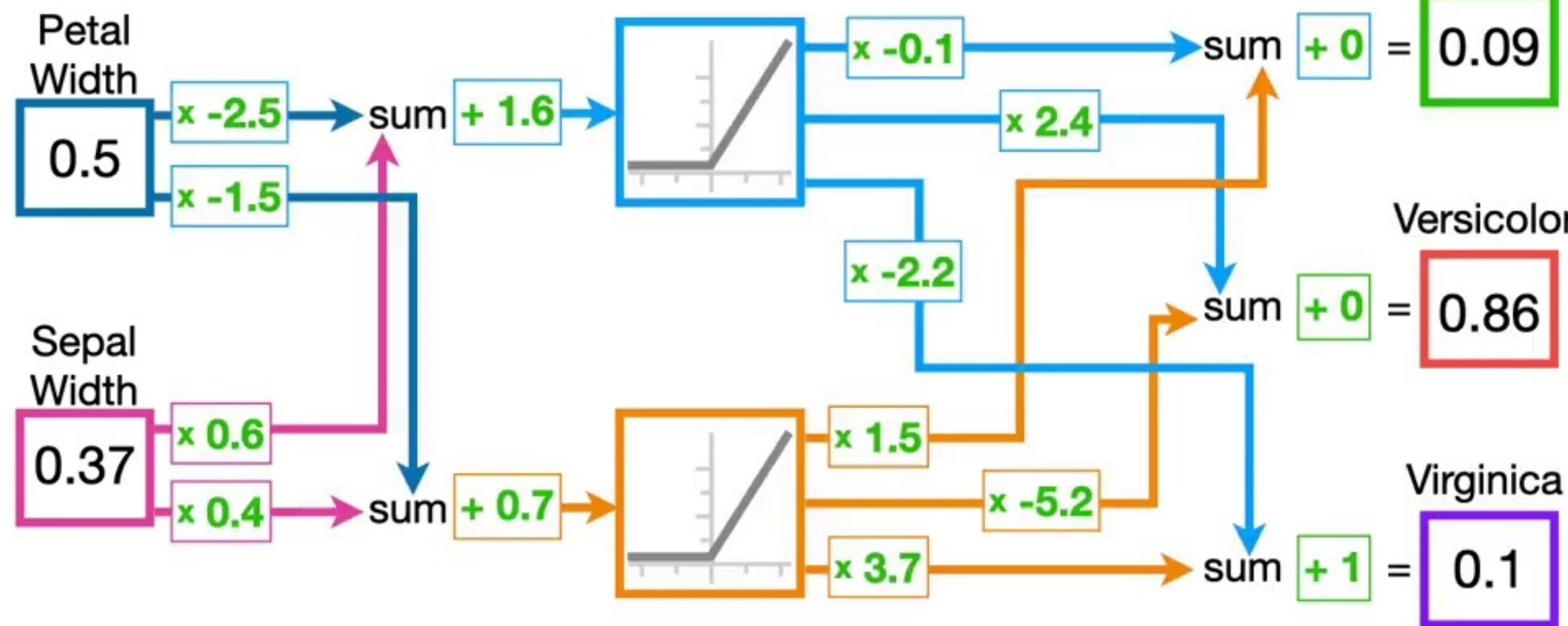


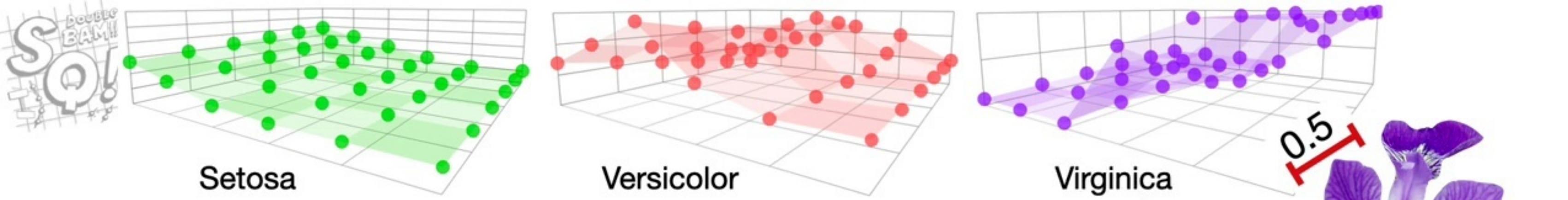




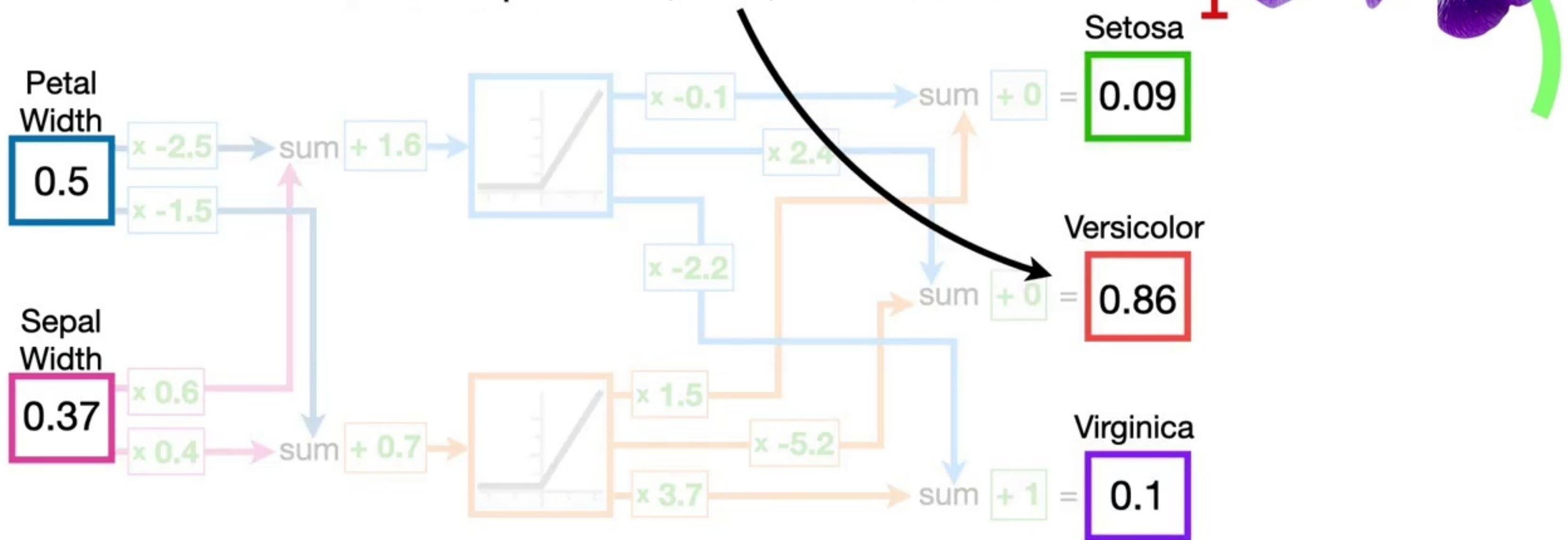


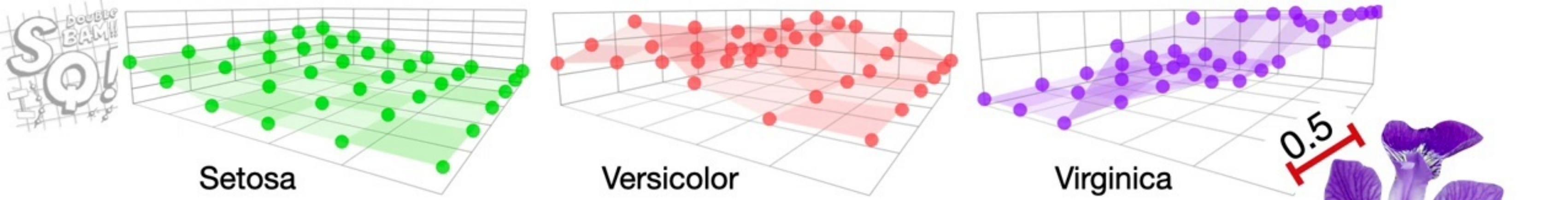
...and run the numbers through the  
**Neural Network...**



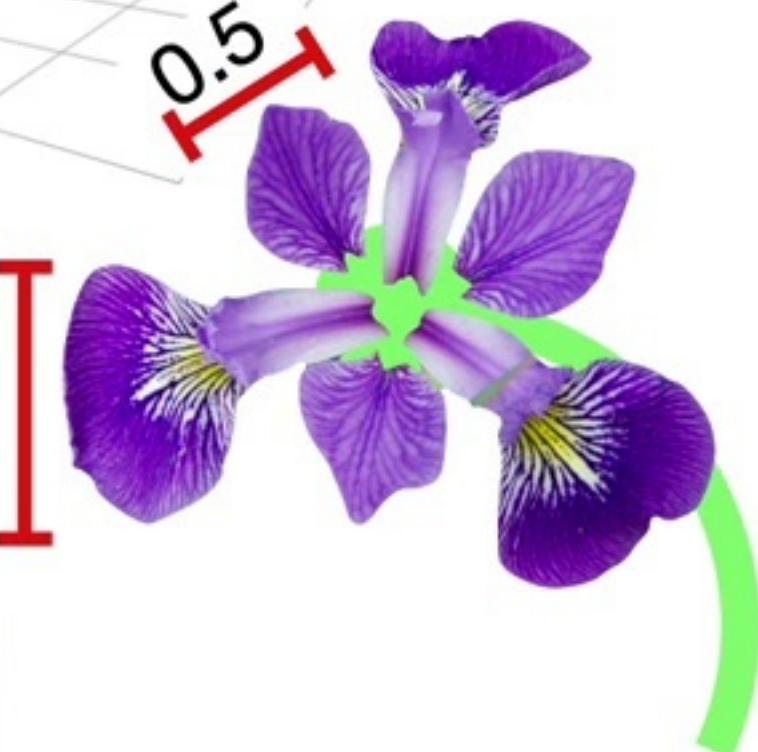
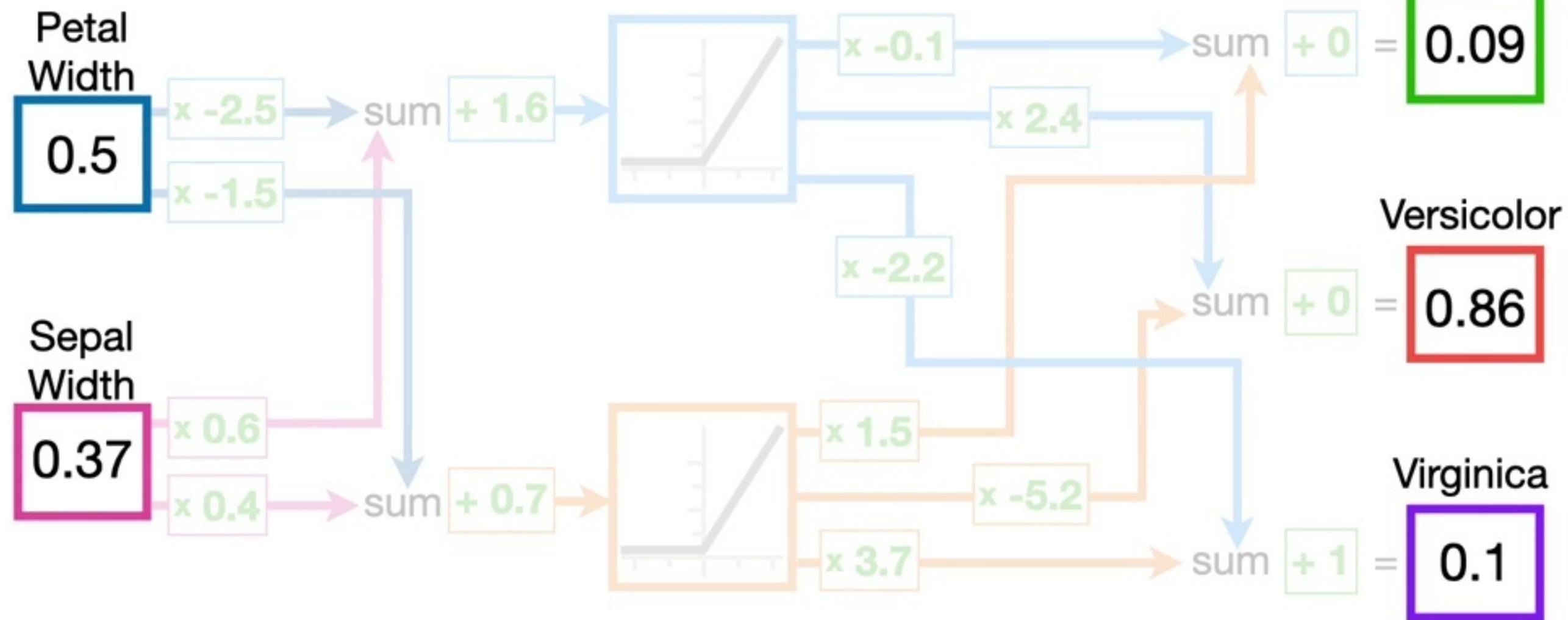


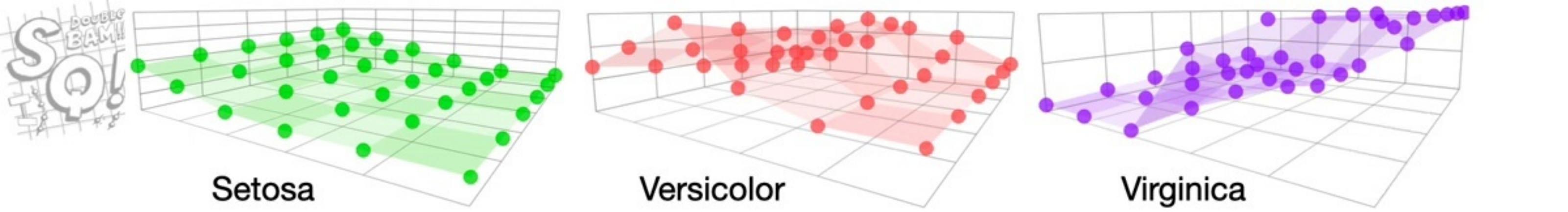
...and predict that this Iris is **Versicolor**,  
because that output value, **0.86**, is closest to 1.





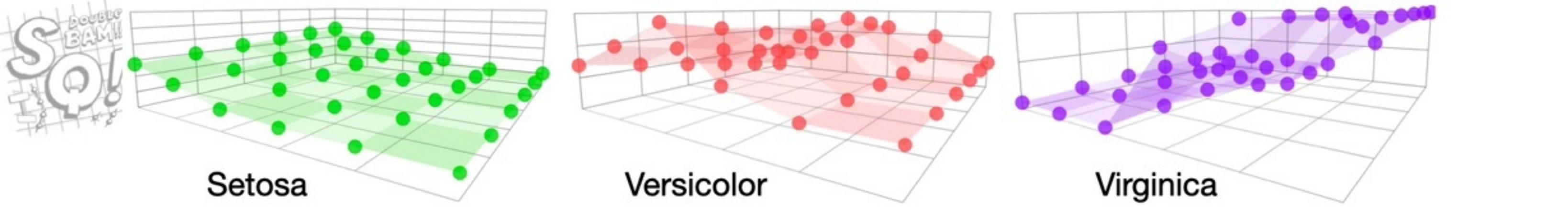
That said, usually when there are two or more output nodes...





...the output values are sent to either something called **ArgMax**...





...or something called **SoftMax** before a final decision is made.

