Slide 18

Cartesian vector addition:

$$\vec{a} + \vec{b} = \begin{cases} X_a & X_b \\ X_b & X_a + X_b \\ X_a & Y_b \\ X_b & X_b \end{cases} = \begin{cases} X_a + X_b \\ Y_b + Y_b \\ X_b & X_b \end{cases}$$

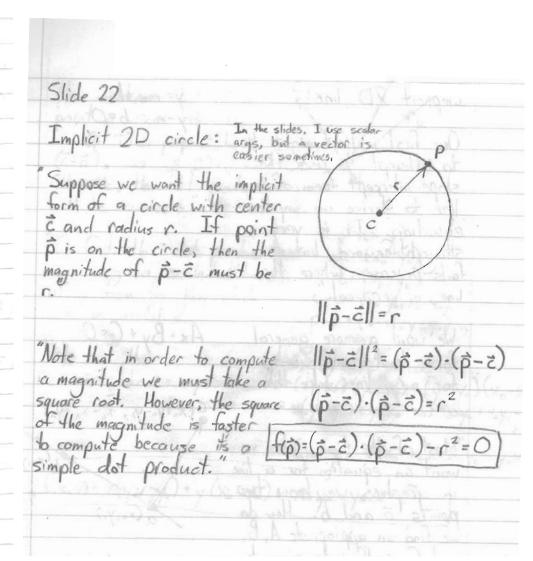
Cartesian dot product:

$$\vec{a} \cdot \vec{b} = \begin{cases} X_a \\ Y_a \end{cases} \cdot \begin{cases} X_b \\ Y_b \end{cases} = X_a X_b + Y_a Y_b + Z_a Z_b$$

$$Z_b = X_a X_b + Y_a Y_b + Z_a Z_b$$

Cartesian cross product:

$$\vec{a} \times \vec{b} = \begin{bmatrix} X_a \\ Y_a \\ Z_a \end{bmatrix} \times \begin{bmatrix} X_b \\ Y_b \\ Y_b \end{bmatrix} = \begin{bmatrix} y_a Z_b - Z_a Y_b \\ Z_a X_b - X_a Z_b \\ X_a Y_b - Y_a X_b \end{bmatrix}$$



Implicit 2D line:	y= mx +6 3 12
T	v-mx-h=0
"Our first instinct might be	Stop Of Halant
"Our first instinct might be to attempt to use the slope-intercept form of a	
slope-intercept form of	- All A tarky = 264 2"
line to desive an implicit	all a last a de la
line to derive an implicit equation. It is very	LT a la la
straightferward, but it	AL A H &
Cilor correction than the	31 ( 50 ) 15 ( 60 ) 1 ( )
fails in cases where the	Mary Trade and Sweet States
Time is vertical.	
"We want a more general form that would work?	1 0
We want a more general	Ax+By+C=0
form that would work	White that in action to c
for any line, like this	I SUM SW SHITTINGS OF
one. (369) (339) 3 may 3	
1 7 3 72	1 109 16 1a 1a)
"Most of the time, when we	P(xPx)
want an equation for a line	P(xPzho)
in graphics, we know two	
points a and b. How do	(x, y, )
Cil and and AR	a (Xasya)
and C coefficients given two	F 7
and C coefficients given two	b-a= (yo-yo)
l'	1/0-1/07
"The first step is to define	C-C = [Ya-Ya]
a third print such that	$C-a = \begin{bmatrix} y_a - y_b \\ x_b - x_a \end{bmatrix}$
"The first step is to define a third point such that IIC-all=11b-all and (c-a) is perpendicular to (b-a)"	L P
is personalization to the ?"	C= [ Ya - Yb + Xa]
be bendiental to to al	$C = \begin{cases} y_0 - y_b + x_a \\ x_b - x_a + y_0 \end{cases}$
	5 - 0 / 4 / 4 ]

Now we know that point p is on the line,  $(\vec{p}-\vec{a})$  is perpendicular to  $(\vec{c}-\vec{a})$ , so  $(\vec{p}-\vec{a})\cdot(\vec{c}-\vec{a})=0$ . Otherwise, the dot product will be non-zero. "In fact, this dot product is a signed, scaled distance of p from the line, which will be useful later." = (x-xa) (ya-yb) + (y-ya) (xb-x = x(ya-yb)+y(xb-xa)+xayb-yaxb f(x,y)= x(ya-yb)+y(xb-xa)+ Xayb-yb Xa=0

Implicit 3D plane: Sometimes when we want to define a plane, we know normal vector hand a point à. If we know, three points on the place instead, we can obtain a normal using a cross product."  $\vec{n} = (\vec{b} - \vec{a}) \times (\vec{c} - \vec{a})$ n·(p-a)=0 Then, we know for every port pon the plane, n.(p-a)=0, and it's non-zero atherwise, f(p)= n. (p-a)=0 is an implicit equation for a plane.

Slide 26 Parametric 3D line: If we know two points à and 6 on the line, we can easily obtain a parametric form by assuming f(0) = a and f(1)=b. t(+)= a+t(b-a) Suppose a sphere w/ center c and radius r. Let & the angle corresponding with longitude (-180°, 180°) and 0 be the angle corresponding with X= X + r cos & sin A y= yc+r sin \$ sin \$ Z= Z + r cos A

8=1 Slide 32 Y=0 Conversion from 2D Cartesian Note that a barycentric coord system can have gridlines like a Cortesian system." The b.c. components are just signed, weighted clistances from the axes. We know that the function of Y= Tob (x, y) the implicit form for a tab(xes ye) gives a signed, weighted distance to the line, but the weights B= fac(x,y) are probably not such that tab (xcs ye)=1; for example, so we divide. tac (Xb) yb) a=1-13-8

