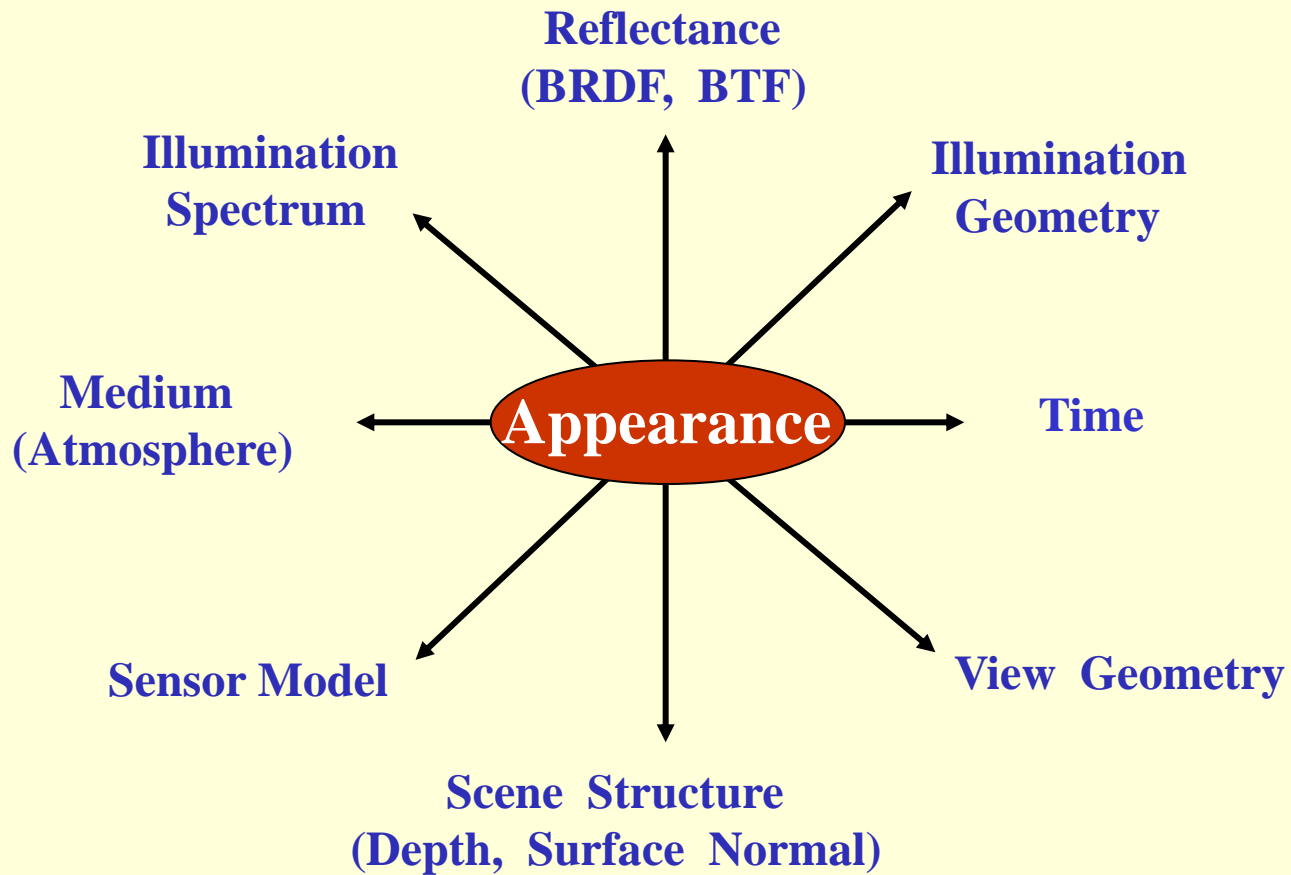


# Lighting and Shadows

Thanks to Langer-Zucker, Henrik Wann Jensen, Ravi Ramamoorthi, Hanrahan, Preetham

# Appearance of An Outdoor Scene



# Illumination Direction



**February 18<sup>th</sup> 2002, 10 AM**  
**Clear and Sunny**



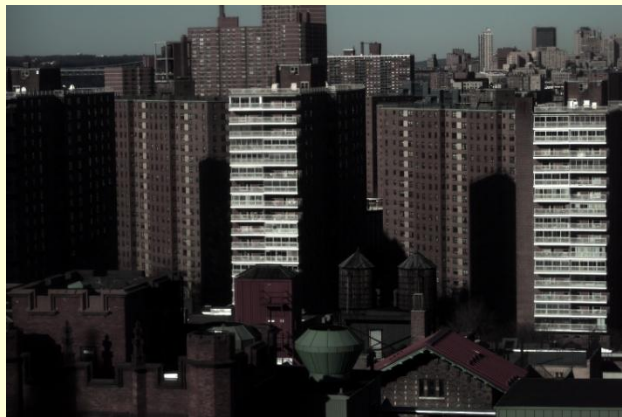
**February 18<sup>th</sup> 2002, 11 AM**  
**Clear and Sunny**



**February 18<sup>th</sup> 2002, 12 Noon**  
**Clear and Sunny**



**February 18<sup>th</sup> 2002, 2 PM**  
**Clear and Sunny**



**February 18<sup>th</sup> 2002, 3 PM**  
**Clear and Sunny**



**February 18<sup>th</sup> 2002, 4 PM**  
**Clear and Sunny**

# Illumination Spectra



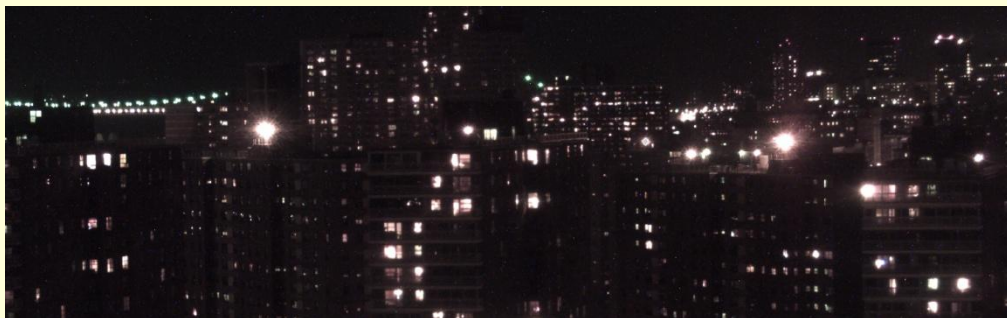
May 4<sup>th</sup> 2002, 6 AM  
Clear Day, **Sun Rise**



May 4<sup>th</sup> 2002, 12 Noon  
Clear Day, **Noon**



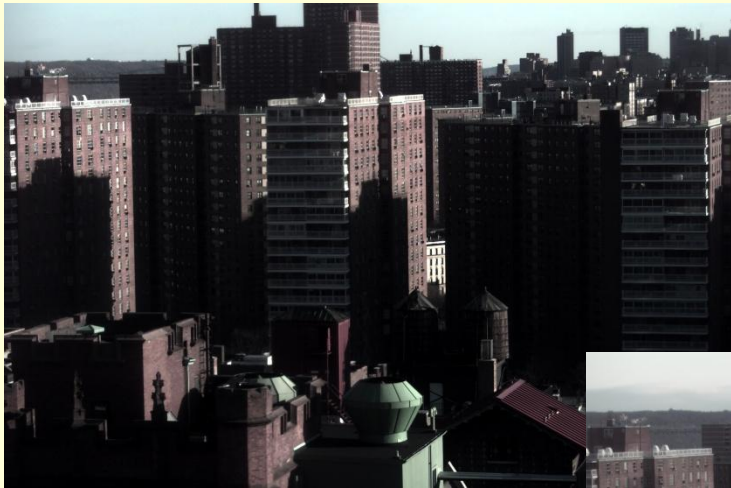
May 4<sup>th</sup> 2002, 6 PM  
Clear Day, **Sun Set**



May 4<sup>th</sup> 2002, 9 PM  
Clear **Night**



# Cloud Cover



March 22<sup>nd</sup> 2002, 7 AM  
Sunny, No Clouds



March 4<sup>th</sup> 2002, 7 AM  
Partly Sunny, Partly Cloudy



March 13<sup>th</sup> 2002, 7 AM  
Overcast

**Sharper Shadows**  
**Decreasing Cloud Cover**

# Weather Conditions



April 16<sup>th</sup> 2002, 3 PM  
Sunny, **Mild Haze**



April 12<sup>th</sup> 2002, 3 PM  
Overcast, **Light Rain**



April 19<sup>th</sup> 2002, 3 PM  
Overcast, **Dense Fog**



April 28<sup>th</sup> 2002, 3 PM  
Overcast, **Dense Mist**

# Visibility



**April 28<sup>th</sup> 2002, 6 AM**  
**Rain & Mist, Visibility 2.5 miles**  
**0.1 inches Precipitation last hour**



**April 28<sup>th</sup> 2002, 9 AM**  
**Rain & Mist, Visibility 1.5 miles**  
**0.23 inches Precipitation last hour**



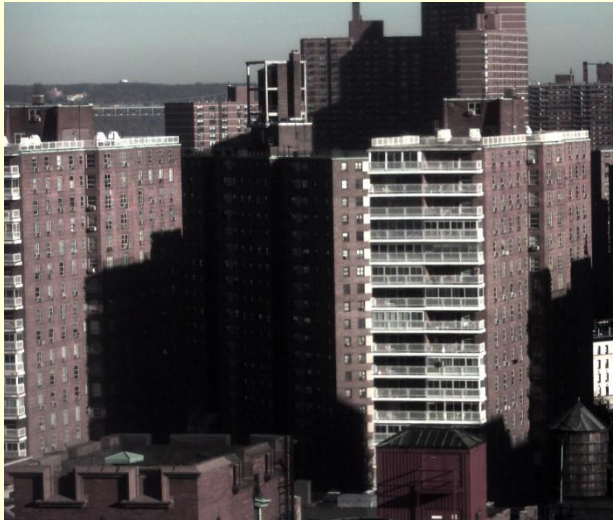
**April 28<sup>th</sup> 2002, 12 Noon**  
**Light Rain & Mist, Visibility 1.25 miles**  
**0.08 inches Precipitation last hour**



**April 28<sup>th</sup> 2002, 3 PM**  
**Dense Mist, Visibility 0.75 miles**  
**0.02 inches Precipitation last hour**



# Four Seasons ( New York )



**Winter**, January 4<sup>th</sup> 2002, 9 AM  
Clear and Sunny



**Fall**, September 9<sup>th</sup> 2001, 9 AM  
Clear and Sunny



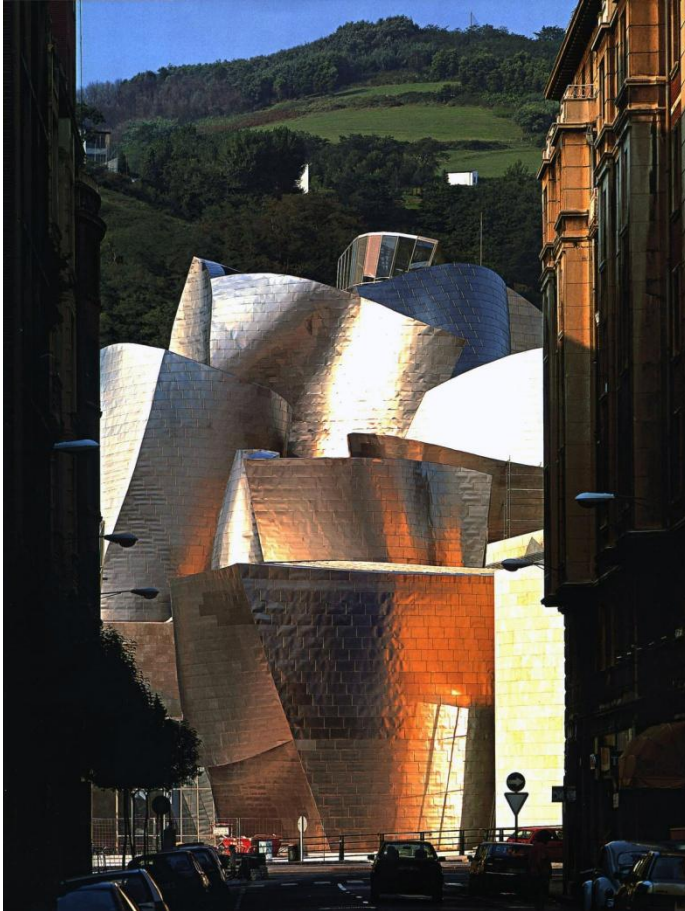
**Spring**, March 14<sup>th</sup> 2001, 9 AM  
Clear and Sunny



**Summer**, May 15<sup>th</sup> 2002, 9 AM  
Clear and Sunny

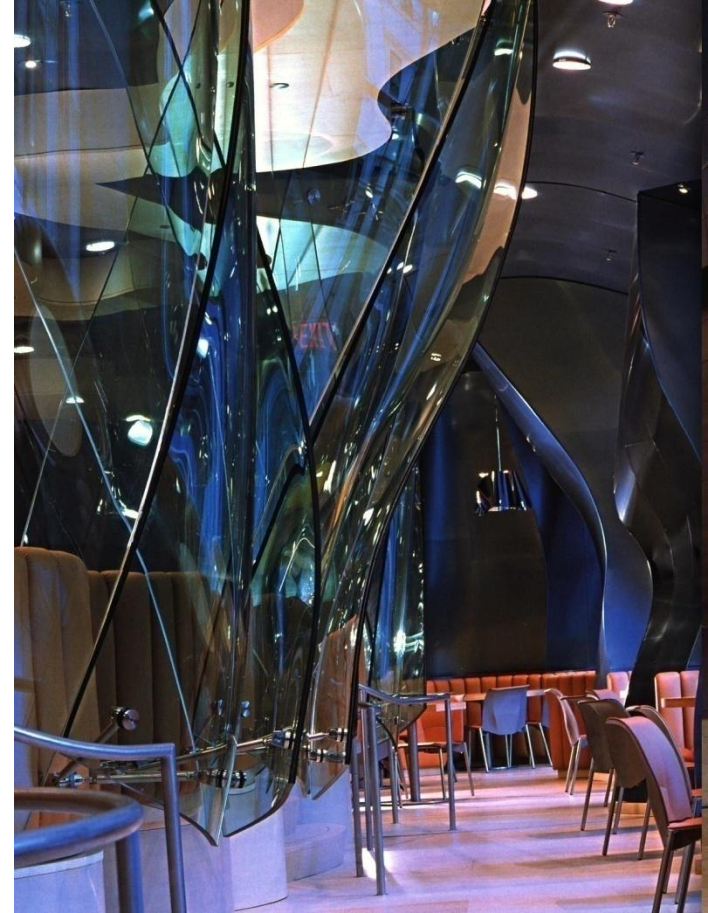


# Lighting Design



- From *Frank Gehry Architecture*, Ragheb ed. 2001

# Lighting Design



- From *Frank Gehry Architecture*, Ragheb ed. 2001

# Nomenclature for Lighting

Size:    point  
         line  
         area  
         volume

Distance:    infinity  
                 near-field

Directionality:    collimated  
                         divergent  
                         convergent

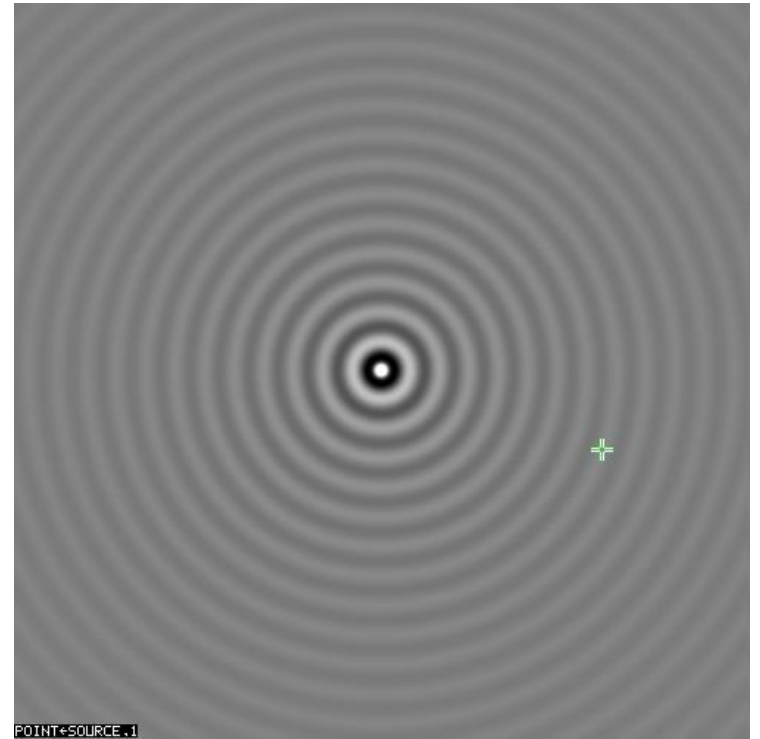
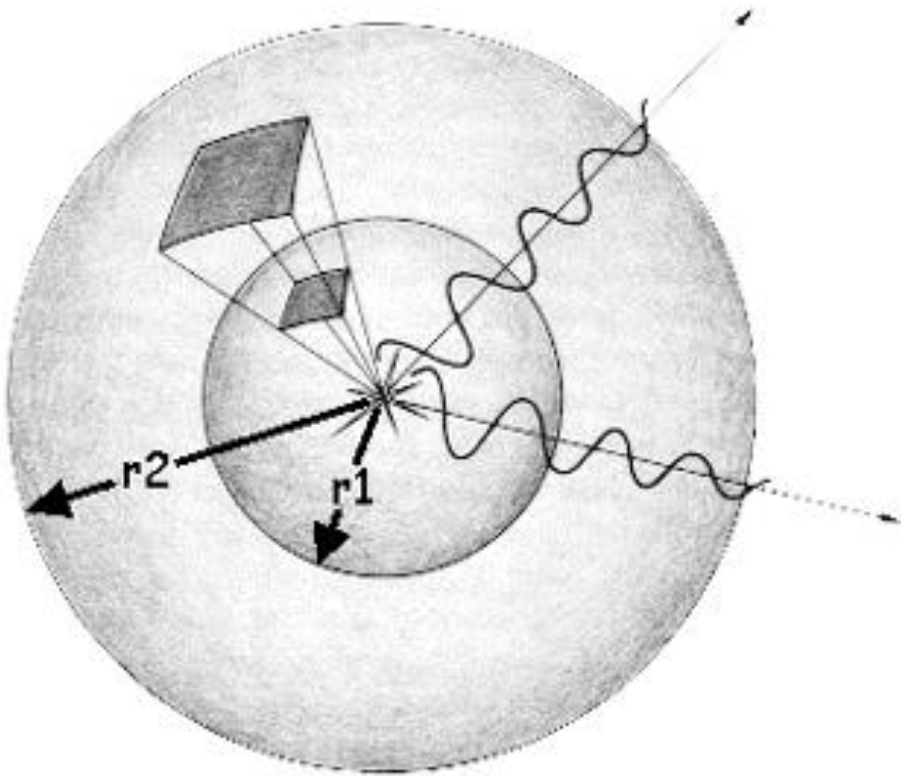
Temporal:    static  
                 time-varying

Natural        sun  
                 sky  
                 firefly  
                 moon

Artificial        halogen  
                 fluorescent  
                 flash  
                 projector  
                 laser



# Isotropic Point Light Source

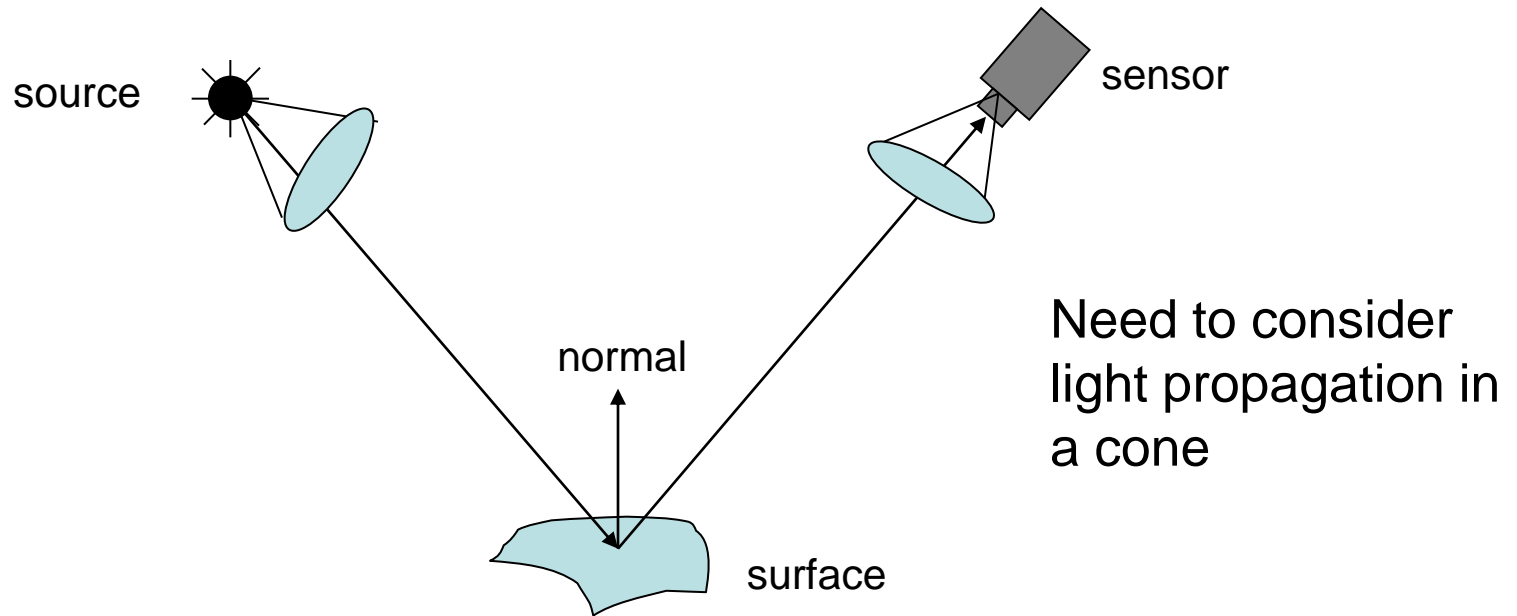


We see an inverse distance squared fall off in intensity.  
Here light does not weaken, but only spreads in a sphere.



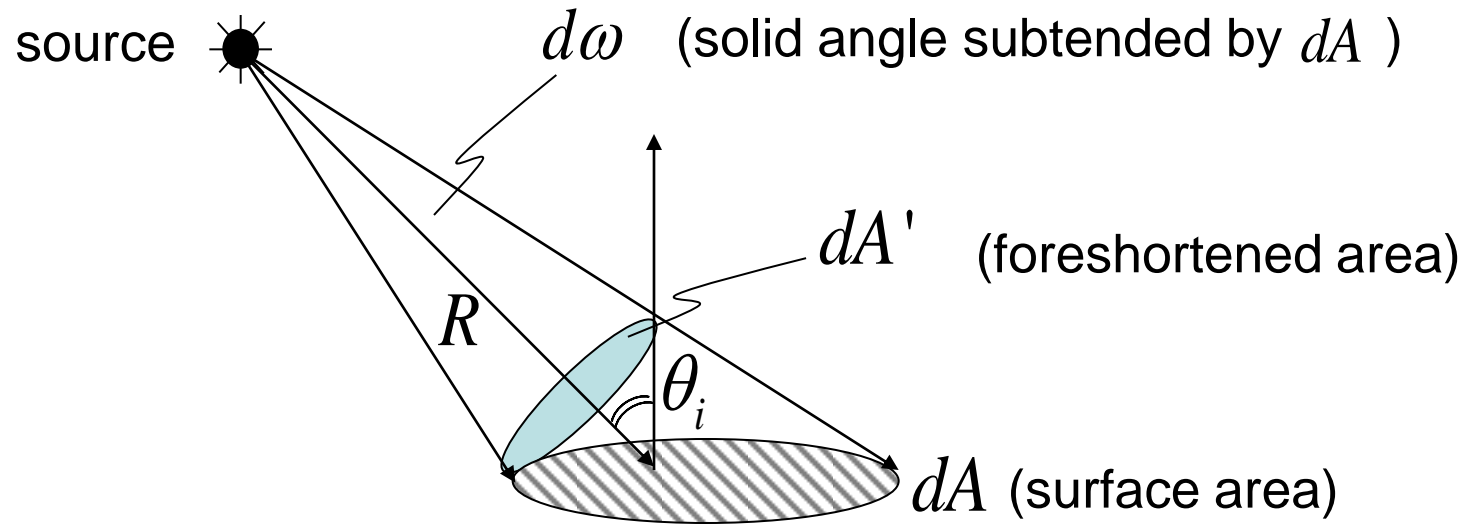
# How to quantify light?

---



# Solid Angle

---

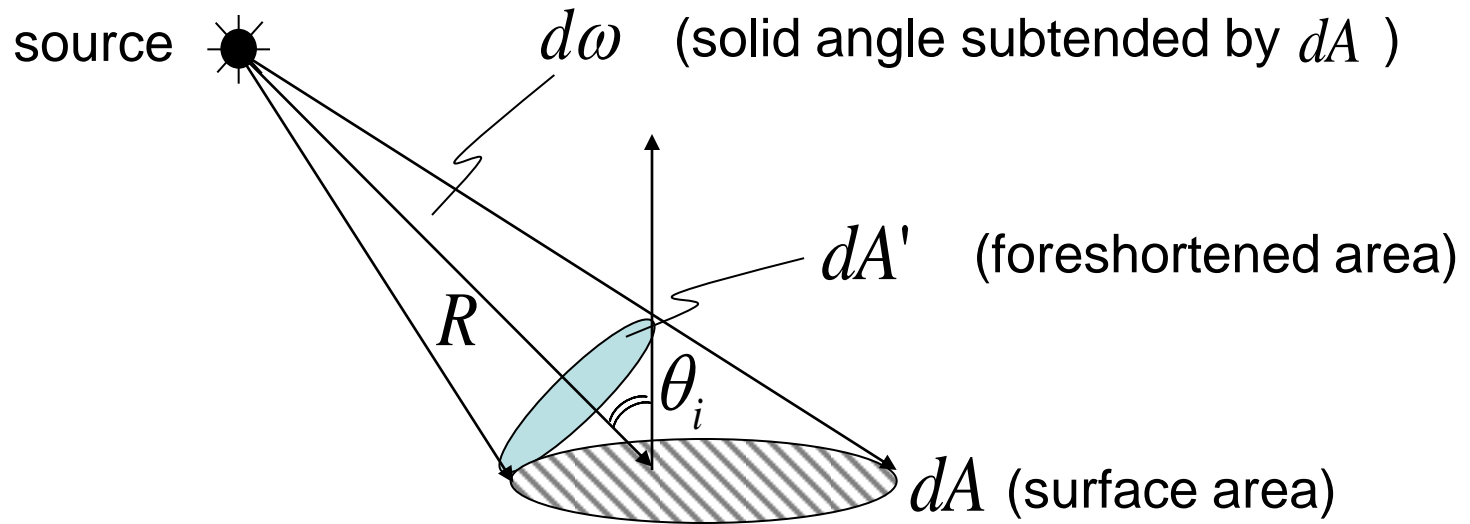


Solid Angle : 
$$d\omega = \frac{dA'}{R^2} = \frac{dA \cos \theta_i}{R^2} \quad (\text{steradian})$$

What is the solid angle subtended by a hemisphere?

# Radiant Intensity of Source

---

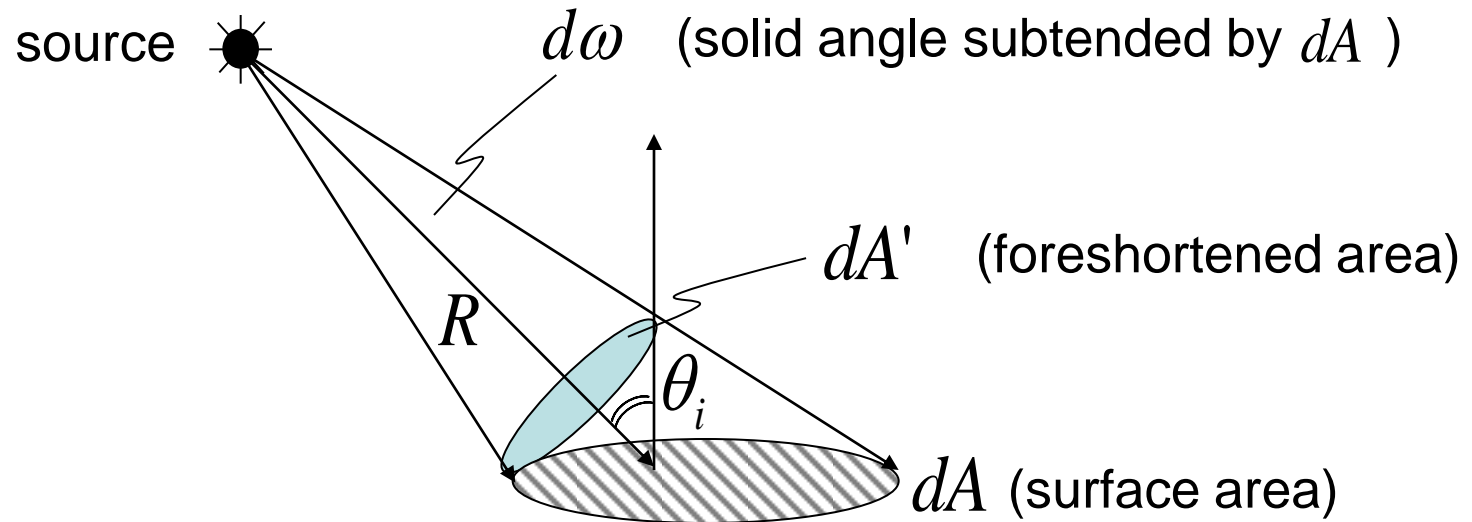


Radiant Intensity of Source : 
$$I = \frac{d\Phi}{d\omega} \quad (\text{watts / steradian})$$

Light Flux (power) emitted per unit solid angle

# Surface Irradiance

---



Surface Irradiance :

$$E = \frac{d\Phi}{dA} \quad (\text{watts} / \text{m}^2)$$

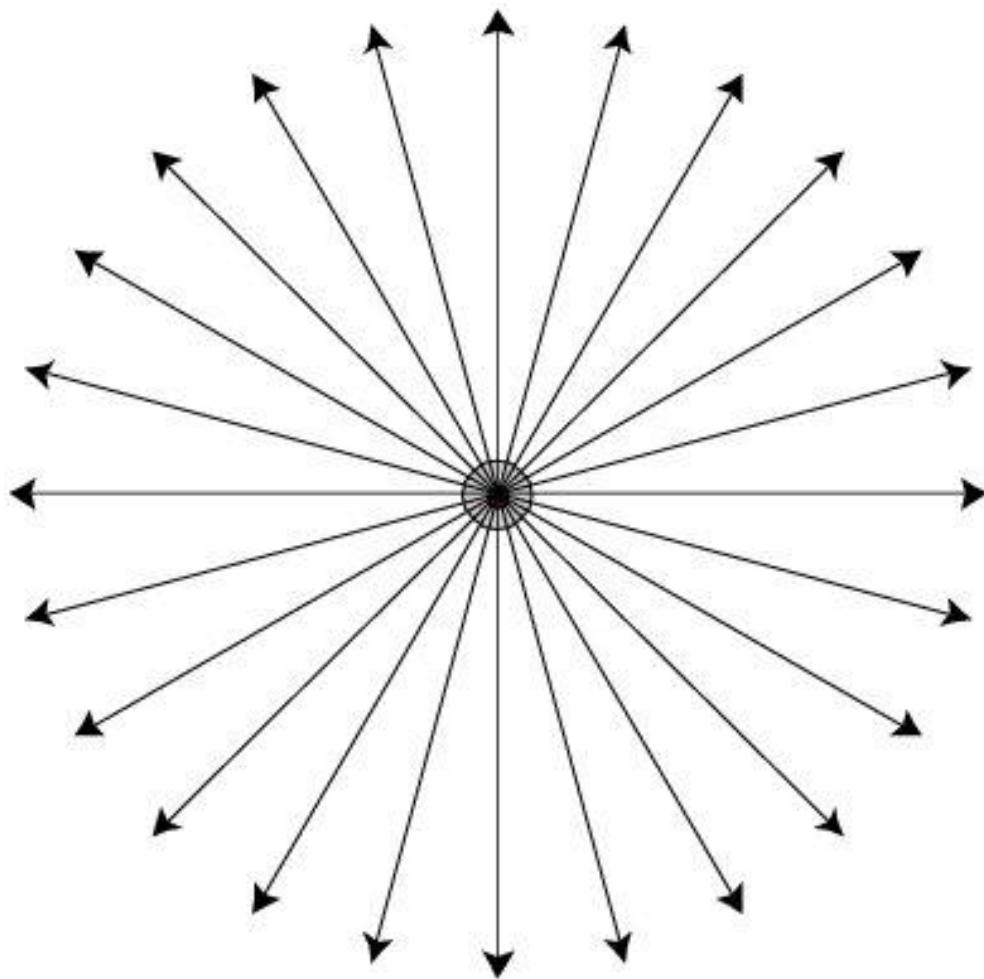
Light Flux (power) incident per unit surface area.

Does not depend on where the light is coming from!



# Isotropic Point Source

---

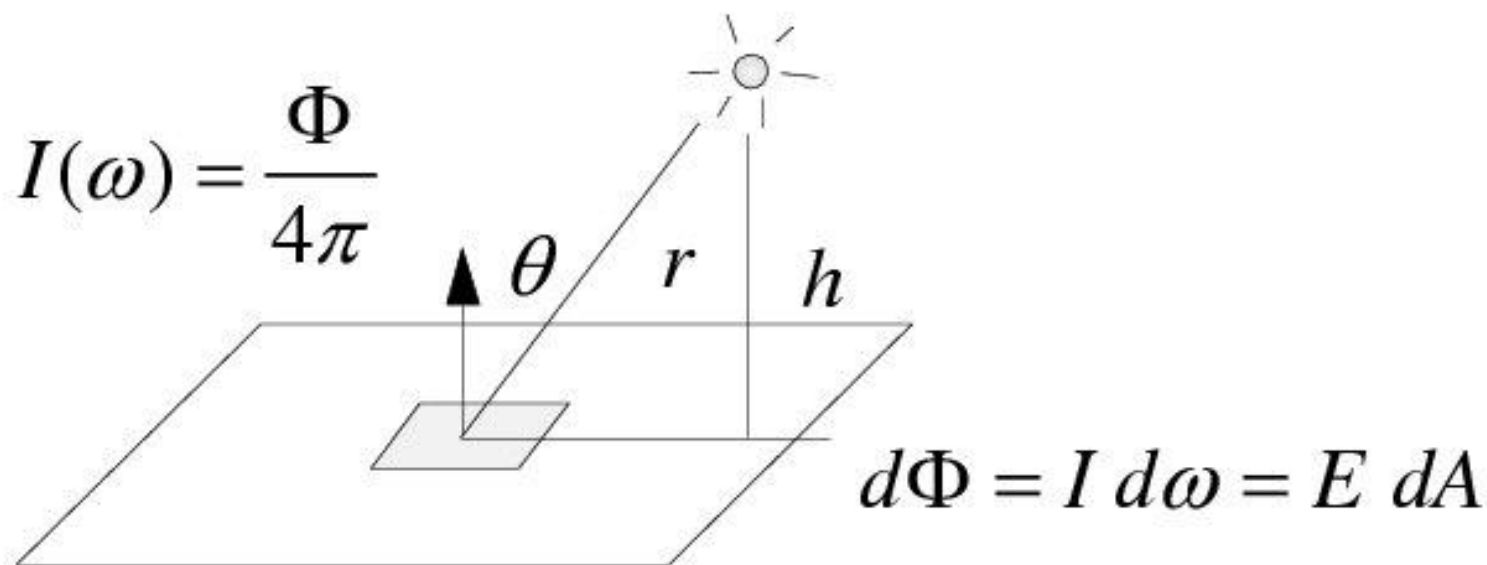


$$\Phi = \int_{s^2} I d\omega$$
$$= 4\pi I$$

$$I = \frac{\Phi}{4\pi}$$

# Illumination: Isotropic Point Source

---

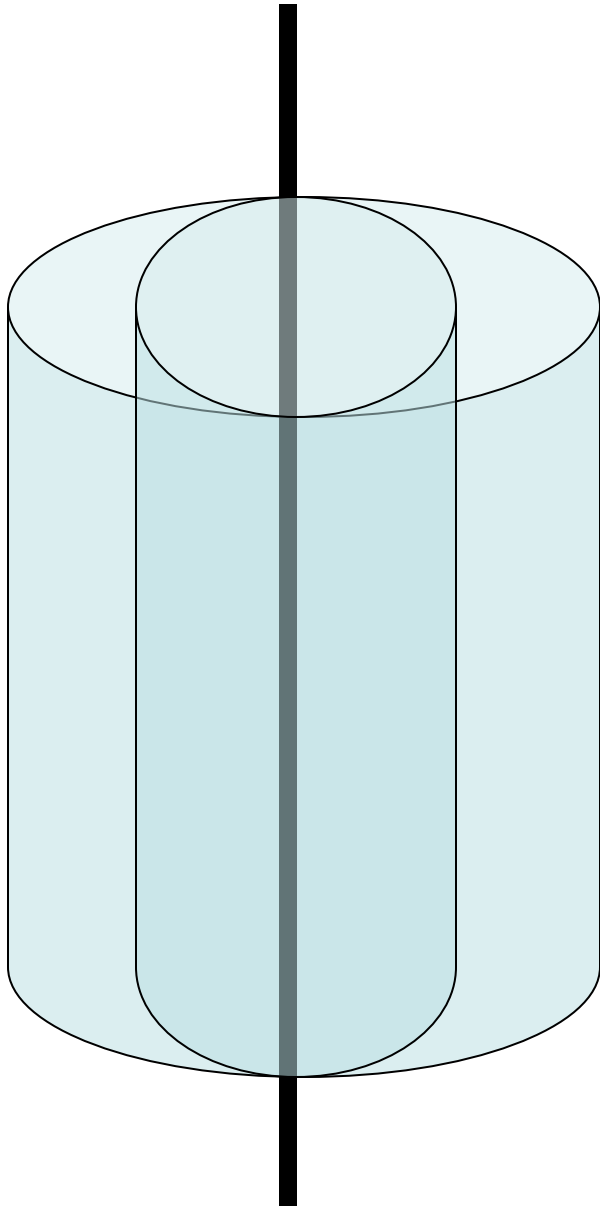


$$I d\omega = \frac{\Phi}{4\pi} \frac{\cos \theta}{r^2} dA = E dA$$

$$E = \frac{\Phi}{4\pi} \frac{\cos \theta}{r^2}$$

$$\frac{\Phi}{4\pi} \frac{\cos \theta}{r^2} \Rightarrow \frac{\Phi}{4\pi} \frac{\cos^3 \theta}{h^2}$$

# Infinite Line Source



Line source shows cylindrical symmetry.

The intensity fall-off is inversely proportional to distance from the line source. Why?

$$d\Phi = I d\omega = E dA$$

# Infinite Planar Area Source

- Assume every point on the plane is an isotropic point light source.
- We saw inverse squared fall off, inverse fall off...so, this must be...
- Intensity CONSTANT with respect to distance! WHY?

As distance increases,

$$d\Phi = I d\omega = E dA$$

Intensity from one point source decreases

But we add intensities from all point sources on the plane.



# Distant and Collimated Lighting

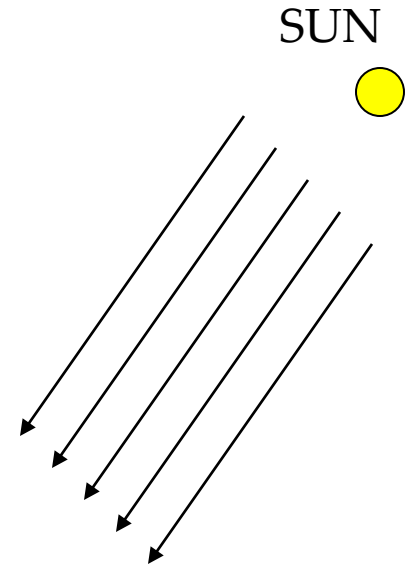
## Distant Lighting:

Essentially source at infinity

All surface points receive light from the same direction

Intensity fall must not be ignored!

Most vision and graphics algorithms assume this.

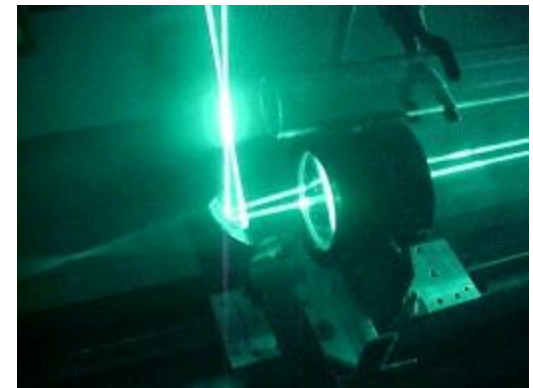


## Collimated:

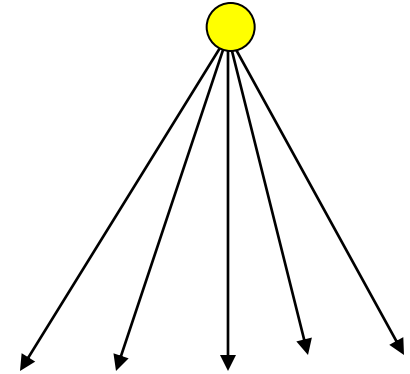
Parallel rays of light on the surface

Lasers (no fall off) - need not be at infinity

Lighting at infinity - (inverse squared fall off)



# Divergent and Near-field Lighting



- Every scene point can receive light from a different direction.
- Much harder to model.
- Examples: near by point sources, spot lights
- Assume distant lighting when size of scene is 10% of the distance to the source.

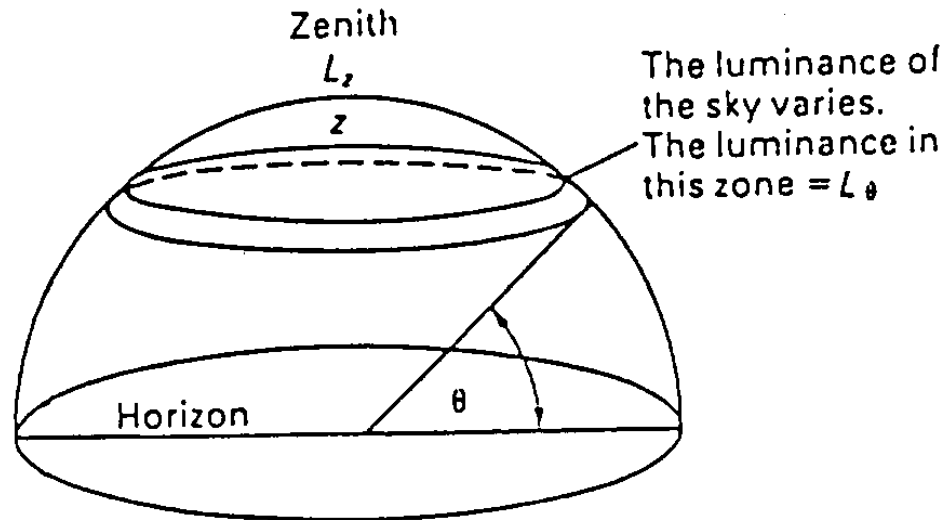
# Overcast Sky versus Clear Sky

Which is the brightest region in a overcast sky?

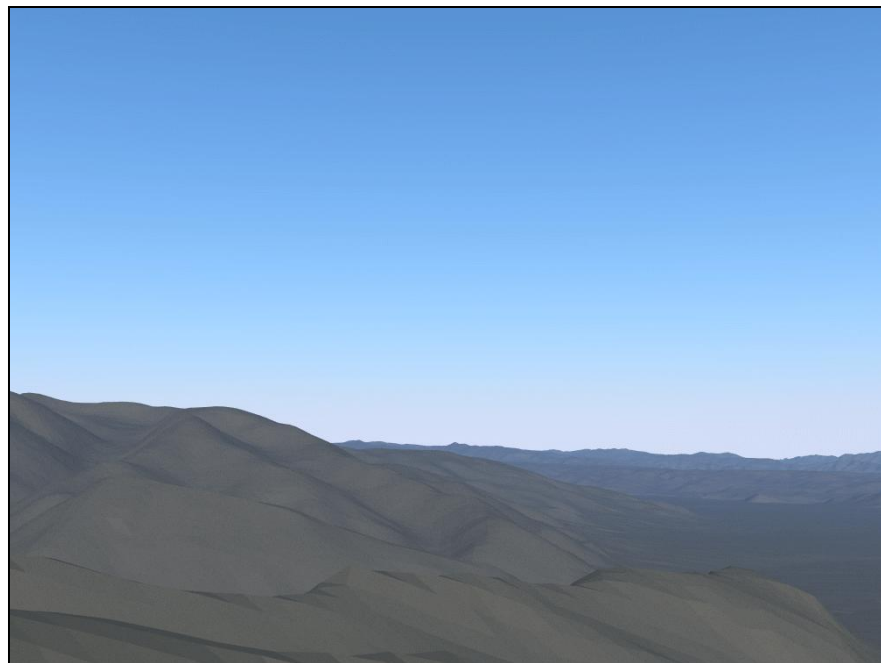
Which is the darkest?

Which is the brightest region in a sunny sky (apart from the sun)?

Which is the darkest?



# Overcast Sky versus Clear Sky



Notice reversal of brightness in the two skies.



# Fluorescent versus Incandescent Lighting

## Fluorescent:

Less heat generated.

More efficient lighting for the same brightness.

Flickers continuously.

Shows sparse, spikes in spectrum.

## Incandescent:

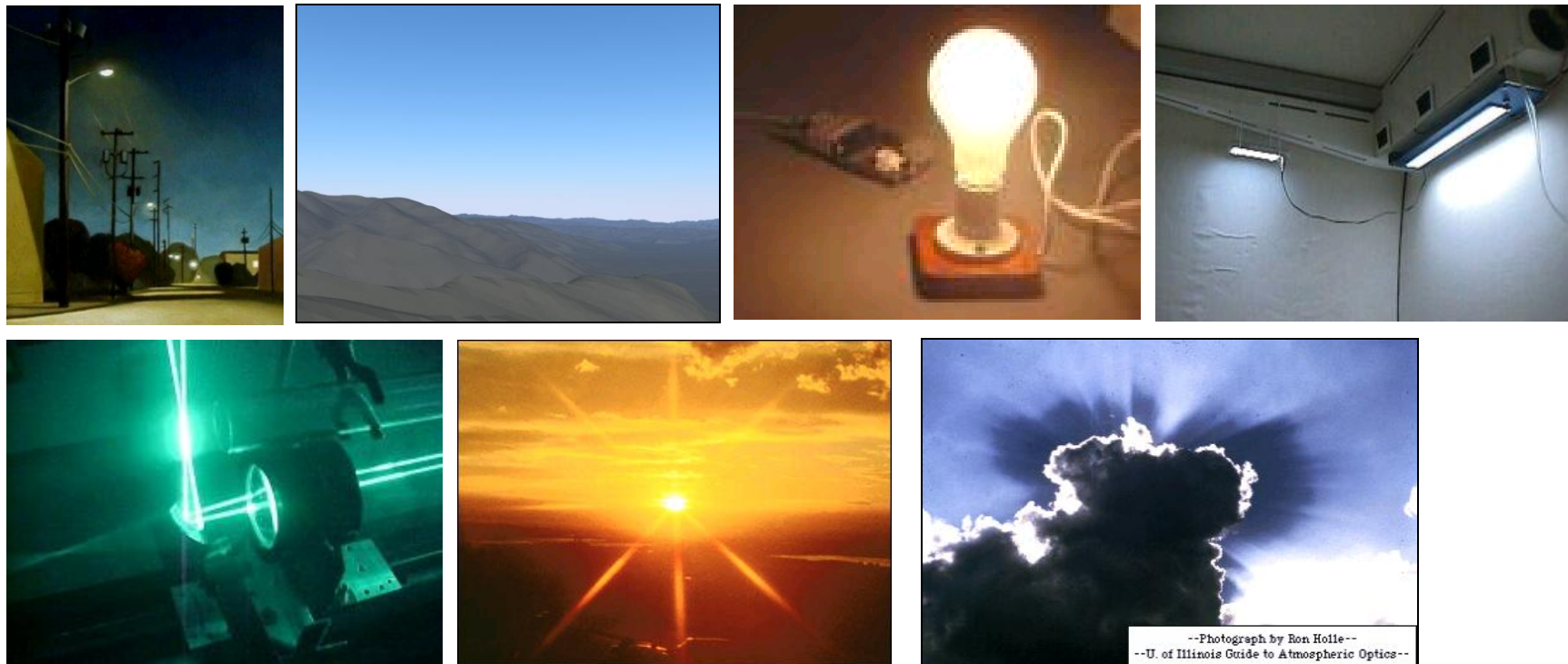
Lots of heat generated.

Less efficient lighting for the same brightness.

No flickers.

Shows continuous spectrum.

# Is there a unified representation for light sources?



How do we compare the light from a street lamp to that from an overcast sky?

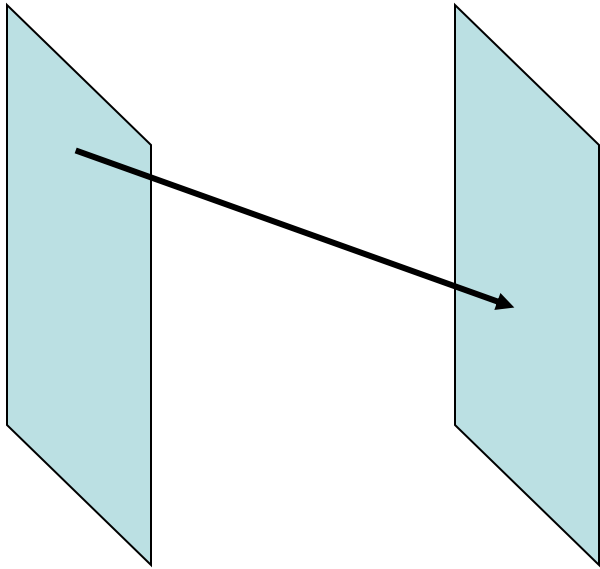
It is important to unify source representation so that algorithms may be developed for all sources instead of one per type of source.

Consider the SPACE of LIGHT RAYS!

# 4D Hypercube of Rays

(x,y)-plane

(p,q)-plane



- Assumes vacuum (no absorption or scattering)
- No fluorescence, phosphorescence

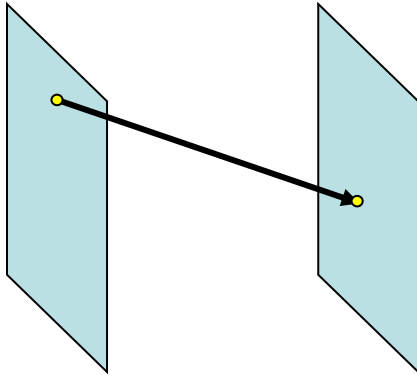
$$\mathcal{M}_{src} \equiv \left\{ (x, y, p, q) : x \in \left[-\frac{h_x}{2}, \frac{h_x}{2}\right], \right. \\ \left. y \in \left[-\frac{h_y}{2}, \frac{h_y}{2}\right], p \in \left[-\frac{h_p}{2}, \frac{h_p}{2}\right], q \in \left[-\frac{h_q}{2}, \frac{h_q}{2}\right] \right\}.$$

# Representation of Sources

Langer and Zucker, CVPR 97

$(x,y)$ -plane

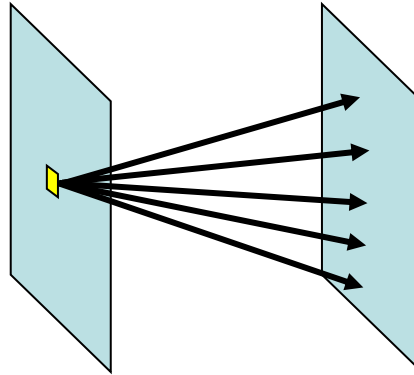
$(p,q)$ -plane



Laser beam – 0D

$(x,y)$ -plane

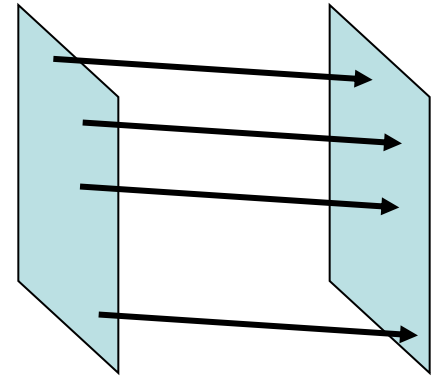
$(p,q)$ -plane



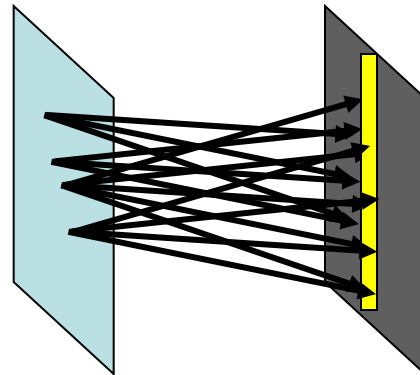
Point source – 2D

$(x,y)$ -plane

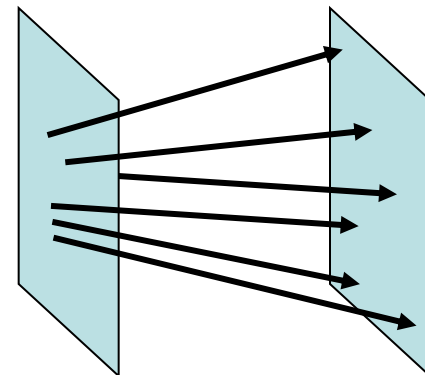
$(p,q)$ -plane



Distant Source (Sun) – 2D



Area source (Sky) with  
a crack in the door – 3D

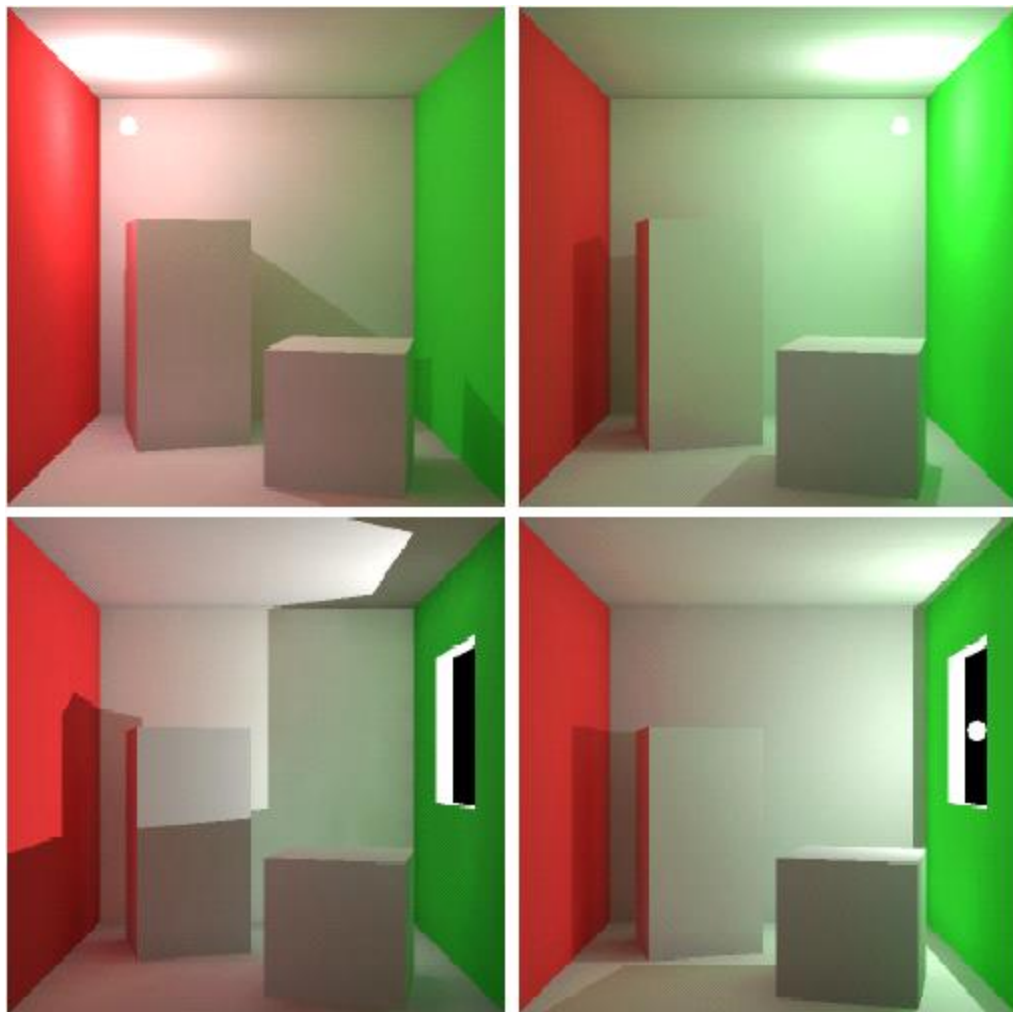
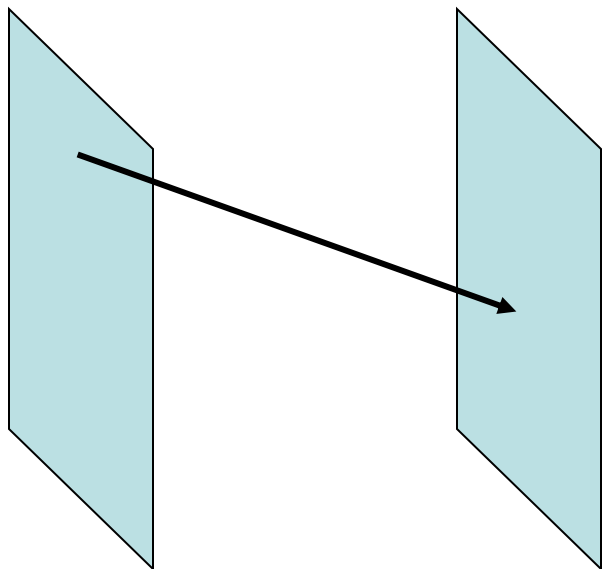


Area source (Sky) with  
door completely open – 4D

# Examples of sources

$(x,y)$ -plane

$(p,q)$ -plane





# What is a Light Source?

Is sky a source? If so, why not a white piece of paper?

Is a translucent object a source?

How to differentiate between source rays and non-source rays?

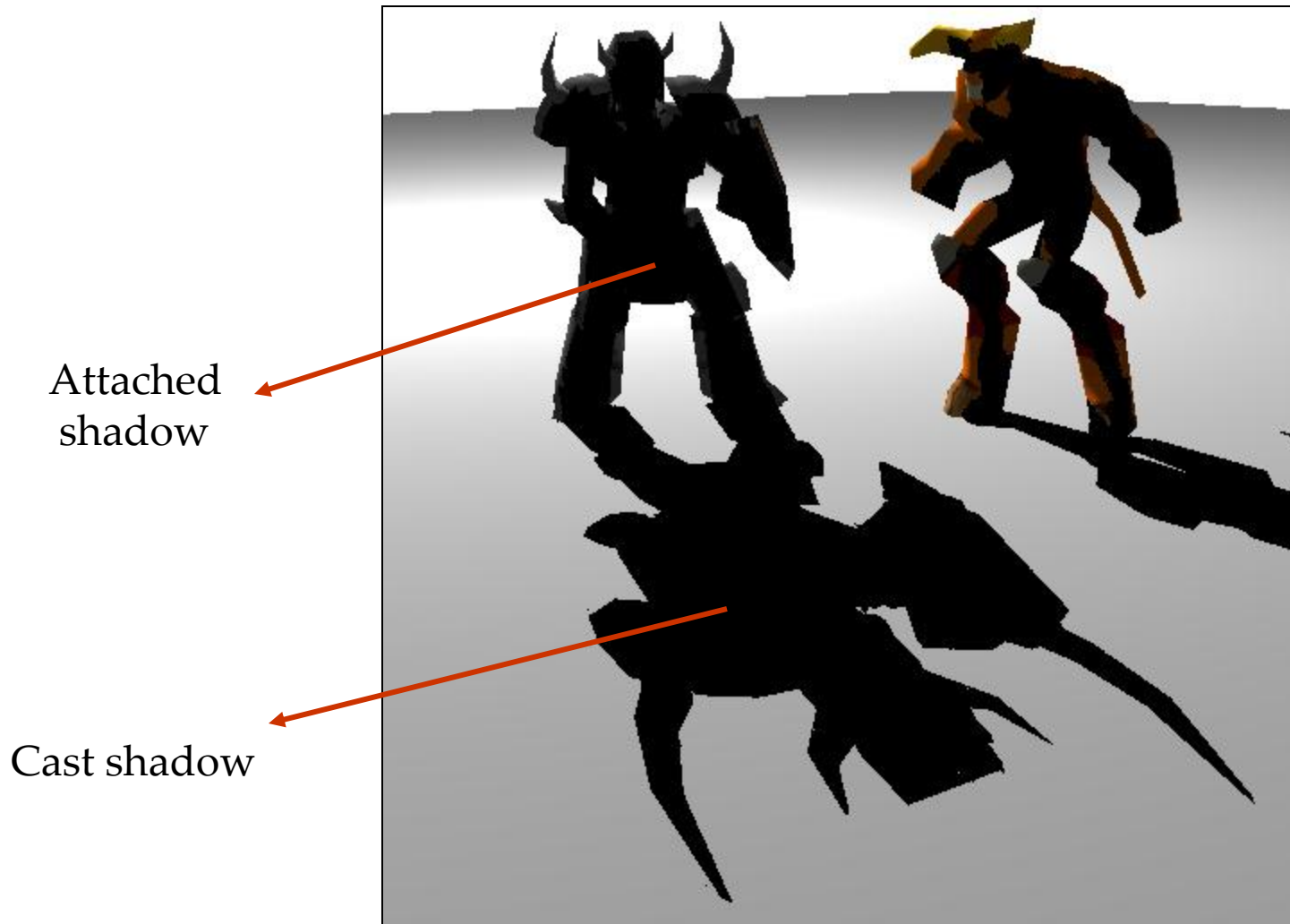
Define a minimum set of absorbants at the ends of rays so that the whole ray space is dark.

Shadows

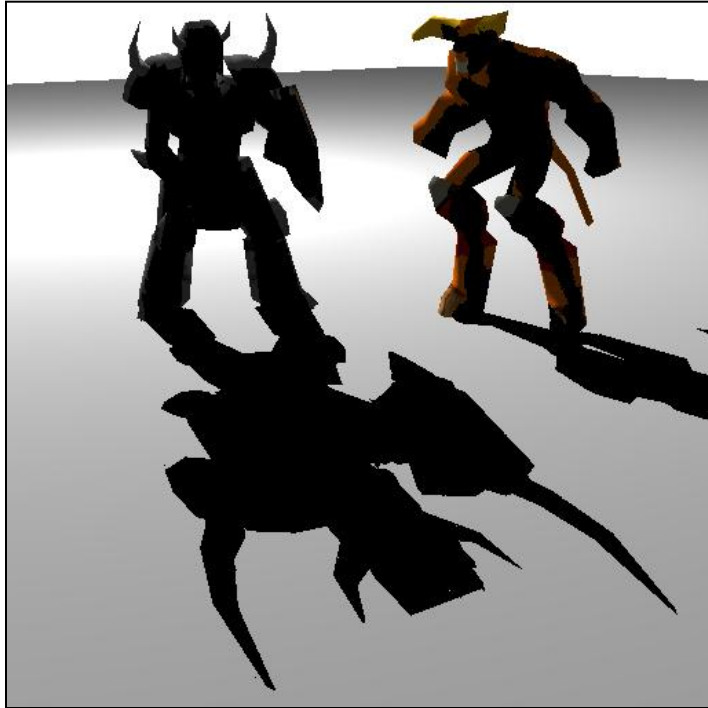




# Attached and Cast Shadows







*Sen, Cammarano, Hanrahan, 2003*

Very hard shadows



*Sloan, Kautz, Snyder 2002*

Very soft shadows

# All-Frequency Lighting and Shadows



**Teapot in Grace Cathedral**

# Sharper and Softer parts of Shadows



Point source model not good for rendering scenes.

