

$$\theta(z) = \theta_0 \exp\left(\frac{N^2 z}{g}\right) \quad (1)$$

$$\Pi(z) = 1 + \frac{g^2}{c_p \theta_0 N^2} \left[\exp\left(\frac{-N^2 z}{g} - 1\right) \right] \quad (2)$$

$$p(\Pi) = p_0 \Pi^{c_p/R} \quad (3)$$

where the Schär gravity waves test case uses, $g = 9.81 \text{ m s}^{-2}$, $c_p = 1004 \text{ J kg}^{-1} \text{ K}^{-1}$, $\theta_0 = 288 \text{ K}$, $N = 1 \times 10^{-2} \text{ s}^{-1}$, $p_0 = 1000 \text{ hPa}$, $R = 287 \text{ J kg}^{-1} \text{ K}^{-1}$