Distributed Systems

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Leader Election

FloodMax algorithm (informal):

Every process maintains a record of the maximum UID it has seen so far (initially its own). At each round, each process propagates this maximum on all of its outgoing edges. After diam rounds, if the maximum value seen is the process's own UID, the process elects itself the leader; otherwise, it is a non-leader.

FloodMax algorithm (formal):

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states, consists of components:
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u, a UID, initially i's UID max-uid, a UID, initially i's UID status \in \{unknown, leader, non-leader\}, initially unknown rounds, an integer, initially 0
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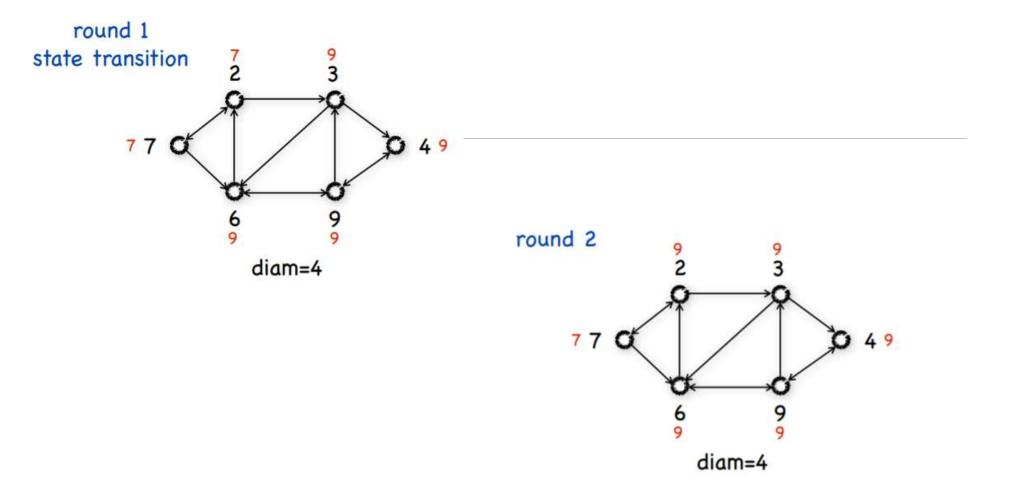
$msgs_i$:

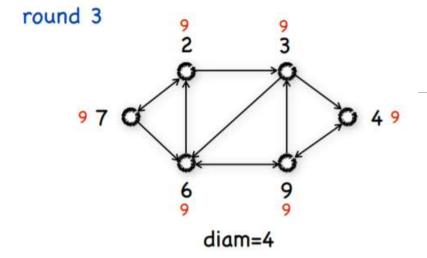
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if rounds < diam then
send max-uid to all j \in out-nbrs
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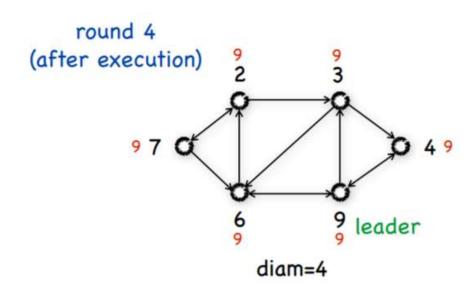
$trans_i$:

```
\begin{aligned} rounds &:= rounds + 1 \\ \text{let } U \text{ be the set of UIDs that arrive from processes in } in\text{-}nbrs \\ max\text{-}uid &:= \max(\{max\text{-}uid\} \cup U) \\ \text{if } rounds &= diam \text{ then} \\ \text{if } max\text{-}uid &= u \text{ then } status := leader \\ \text{else } status := non\text{-}leader \end{aligned}
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round 1 (send messages) 7 7 7 6 9 diam=4







Complexity

Time: Diam rounds

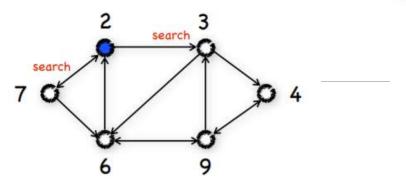
Message: diam.|E|

Breadth-First Search (BFS)

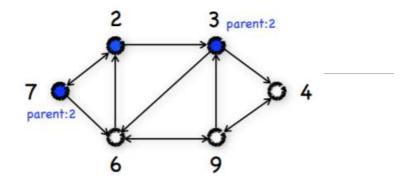
SynchBFS algorithm:

At any point during execution, there is some set of processes that is "marked," initially just i_0 . Process i_0 sends out a search message at round 1, to all of its outgoing neighbors. At any round, if an unmarked process receives a search message, it marks itself and chooses one of the processes from which the search has arrived as its parent. At the first round after a process gets marked, it sends a search message to all of its outgoing neighbors.

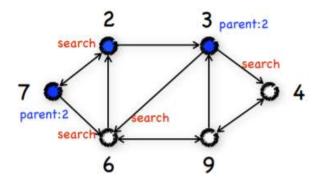
round 1



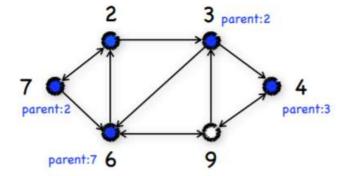
round 1



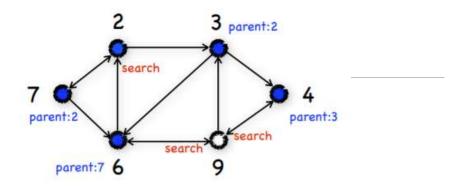
round 2



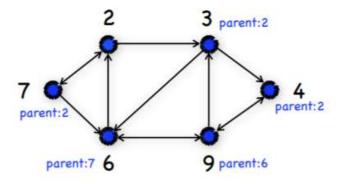
round 2



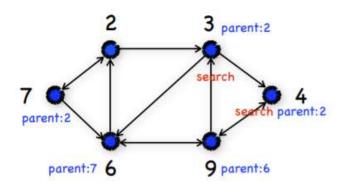
round 3



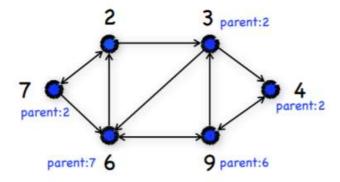
round 3



round 4



round 4



Complexity

Time: Diam rounds

Message: |E|