

4. Suppose not, then $\alpha > \beta$. We know that $\alpha \leq x$ and $x \leq \beta, \forall x \in E$. This is due to the fact that α is a lower-bound and β is an upper-bound to E . Then

$$x \geq \alpha > \beta,$$

which is a contradiction.