

**17.** We can construct a parallelogram with sides  $|\mathbf{x}|, |\mathbf{y}|$  and diagonals  $|\mathbf{x} + \mathbf{y}|, |\mathbf{x} - \mathbf{y}|$ . It holds that

$$\begin{aligned} |\mathbf{x} + \mathbf{y}|^2 + |\mathbf{x} - \mathbf{y}|^2 &= |\mathbf{x}|^2 + 2\mathbf{x} \cdot \mathbf{y} + |\mathbf{y}|^2 + |\mathbf{x}|^2 - 2\mathbf{x} \cdot \mathbf{y} + |\mathbf{y}|^2 \\ &= 2|\mathbf{x}|^2 + 2|\mathbf{y}|^2, \end{aligned}$$

meaning that the sum squared of the parallelogram's four sides equals two times the sum squared of its two diagonals.

□