

# Theorema 2.0: A First Tour

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We consider “proving”, “computing”, and “solving” as the three basic mathematical activities.

## 1 Proving

We want to prove

$$(\forall_x (P[x] \vee Q[x])) \wedge (\forall_y (P[y] \Rightarrow Q[y])) \Leftrightarrow (\forall_x Q[x]).$$

To prove a formula like the above, we need to enter it in the context of a Theorema environment.

♦ **Proposition :** FIRST TEST, 2014  
 $((\forall x (P[x] \vee Q[x]) \wedge \forall y (P[y] \rightarrow Q[y])) \Leftrightarrow \forall x Q[x])$

## 2 Computing

### 2.1 [?]

$$\forall ab (LessTM_{lex}(a) b : \Leftrightarrow \exists (a_i < b_i \wedge \forall a_j = b_j))$$

## 2.2 [?]

$$\forall Km2 \left( Mon[K]_{TimesTM} (m1, m2) := \left( K_{TimesTM} (m1_1, m2_1), [PlusTM](m1_{2i}, m2_{2i}) \right) \right)$$

## 2.3 [?]

$$\forall Km2 \left( Mon[K]_{LessTM} (m1, m2) : \Longleftrightarrow LessTM_{lex} (m1_2) m2_2 \right)$$



# 3 Set Theory



## 3.1 [?]

$$\forall xy \left( x \subseteq y := \forall z \left( zx \rightarrow zy \right) \right)$$

■♦♦ **Proposition :** TRANSITIVITY OF  
 $\forall ac \left( (a \subseteq b \wedge b \subseteq c) \rightarrow a \subseteq c \right)$   
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