#### Theorema 2.0: A First Tour

NB reached List of cells reached CellGroupData reached List of cells reached NullCell reached

We consider "proving", "computing", and "solving" as the three basic mathematical activities.

CellGroupData reached List of cells reached

### 1 Proving

We want to prove

$$( \mathop{\forall}_x (P[x] \vee Q[x])) \wedge (\mathop{\forall}_y (P[y] \Rightarrow Q[y])) \Leftrightarrow (\mathop{\forall}_x Q[x]).$$

To prove a formula like the above, we need to enter it in the context of a Theorema environment.

$$((\forall x\ (P[x] \lor Q[x]) \land \forall y\ (P[y] \to Q[y])) \iff \forall x\ Q[x])$$

Cell reached CellGroupData reached List of cells reached Cell reached CellGroupData reached List of cells reached

### 2 Computing

CellGroupData reached List of cells reached Cell reached Cell reached

# 2.1 [?] $\forall ab \; (LessTM_{lex} (a) \, b : \iff \exists \; (a_i < b_i \land \forall \, a_j = b_j))$

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2.2 [?] 
$$\forall Km2 \; \left(Mon[K]_{TimesTM} \left(m1, m2\right) := \left(K_{TimesTM} \left(m1_{1}, m2_{1}\right),_{[,PlusTM]\left(m1_{2i}, m2_{2i}\right)}\right)\right)$$

2.3 [?] 
$$\forall Km2 \; (Mon[K]_{LessTM} \, (m1, m2) : \iff LessTM_{lex} \, (m1_2) \, m2_2)$$

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### 3 Set Theory

CellGroupData reached List of cells reached Cell reached Cell reached

3.1 [?] 
$$\forall xy \ (x \subseteq y := \forall z \ (zx \to zy))$$

■Cell reached

## 3.2 Proposition (transitivity of $\subseteq$ )

$$\forall ac \ ((a \subseteq b \land b \subseteq c) \to a \subseteq c)$$

Cell reached CellGroupData reached List of cells reached Cell reached