

## Theorema 2.0: A First Tour

NB reached List of cells reached CellGroupData reached List of cells reached  
NullCell reached

We consider “proving”, “computing”, and “solving” as the three basic mathematical activities.

CellGroupData reached List of cells reached

### 1 Proving

We want to prove

$$(\forall_x (P[x] \vee Q[x])) \wedge (\forall_y (P[y] \Rightarrow Q[y])) \Leftrightarrow (\forall_x Q[x]).$$

To prove a formula like the above, we need to enter it in the context of a Theorema environment.

#### 1.1 Proposition (First Test, 2014)

$$\forall_{(x)} P(x) \vee Q(x) \wedge \forall_{(y)} P(y) \implies Q(y) \leftrightarrow \forall_{(x)} Q(x)$$

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cells reached

### 2 Computing

CellGroupData reached List of cells reached Cell reached

### 2.0.1 Global Declaration

$\forall$   
 $a, b$   
 $a = b$

### 2.1 [?]

$\forall_{Theorema'Language' RNG} [Theorema'Language'SIMPRNG [Theorema'Language'VAR [Theorema'Knowledge'VARbTM]]$   
 $Theorema'Language'SIMPRNG [Theorema'Language'VAR [Theorema'Knowledge'VARbTM]]$   
 $Theorema'Language'IffDefTM [Theorema'Language'AnnotatedTM [Theorema'Language'LessTM, Theorem$   
 $Theorema'Language'VAR [Theorema'Knowledge'VARbTM]], Theorema'Language'ExistsTM [Theorema'L$   
 $Theorema'Language'SubscriptTM [Theorema'Language'VAR [Theorema'Knowledge'VARbTM],$   
 $Theorema'Language'VAR [Theorema'Knowledge'VARiTM]]], Theorema'Language'ForallTM [Theorema'L$   
 $Theorema'Language'VAR [Theorema'Knowledge'VARjTM]], Theorema'Language'SubscriptTM [Theorema$

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Data reached List of cells reached Cell reached

### 2.1.1 Global Declaration

$\forall$   
 $K$

### 2.1.2 Global Declaration

$\text{Mon}[K] := \Delta_M$

### 2.1.3 Global Declaration

$\forall$   
 $m1, m2$

## 2.2 [?]

$\forall_{Theorema'Language' RNG} [Theorema'Language'SIMPRNG [Theorema'Language'VAR [Theorema'Knowledge'VARm1TM],$   
 $Theorema'Language'SIMPRNG [Theorema'Language'VAR [Theorema'Knowledge'VARm2TM]],$   
 $Theorema'Language'SIMPRNG [Theorema'Language'VAR [Theorema'Knowledge'VARm2TM]],$   
 $Theorema'Language'EqualDefTM [Theorema'Language'DomainOperationTM [Theorema'Knowledge'MonTM,$   
 $Theorema'Language'TimesTM] [Theorema'Language'VAR [Theorema'Knowledge'VARm1TM],$   
 $Theorema'Language'VAR [Theorema'Knowledge'VARm2TM]], Theorema'Language'TupleTM [Theorema'Language'$   
 $Theorema'Language'TimesTM] [Theorema'Language'SubscriptTM [Theorema'Language'VAR [Theorema'Knowledge'VARm1TM],$   
 $2], 1]], True, Theorema'Language'DomainOperationTM [Theorema'Language'IntegerIntervalTM [1,$   
 $Infinity, True, False], Theorema'Language'PlusTM] [Theorema'Language'SubscriptTM [Theorema'Language'VAR [Theorema'Knowledge'VARm1TM],$   
 $2], Theorema'Language'VAR [Theorema'Knowledge'VARiTM]], Theorema'Language'SubscriptTM [Theorema'Language'VAR [Theorema'Knowledge'VARiTM]],$   
 $2], Theorema'Language'VAR [Theorema'Knowledge'VARiTM]]]]]$

## 2.3 [?]

$\forall_{Theorema'Language' RNG} [Theorema'Language'SIMPRNG [Theorema'Language'VAR [Theorema'Knowledge'VARm1TM],$   
 $Theorema'Language'SIMPRNG [Theorema'Language'VAR [Theorema'Knowledge'VARm1TM]],$   
 $Theorema'Language'SIMPRNG [Theorema'Language'VAR [Theorema'Knowledge'VARm2TM]],$   
 $Theorema'Language'IffDefTM [Theorema'Language'DomainOperationTM [Theorema'Knowledge'MonTM,$   
 $Theorema'Language'LessTM] [Theorema'Language'VAR [Theorema'Knowledge'VARm1TM],$   
 $Theorema'Language'VAR [Theorema'Knowledge'VARm2TM]], Theorema'Language'AnnotatedTM [Theorema'Language'AnnotatedTM [Theorema'Knowledge'VARm1TM],$   
 $2], Theorema'Language'VAR [Theorema'Knowledge'VARm2TM]], Theorema'Language'AnnotatedTM [Theorema'Knowledge'VARm1TM],$   
 $2], Theorema'Language'VAR [Theorema'Knowledge'VARm2TM]]]$

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## 3 Set Theory

CellGroupData reached List of cells reached Cell reached

### 3.0.1 Global Declaration

$\forall_{x,y}$

### 3.1 [?]

$\forall_{\text{Theorema'Language' } RNG} [\text{Theorema'Language'SIMPRNG} [\text{Theorema'Language'VAR} [\text{Theorema'Knowledge'VAR} yTM]]]$   
 $\text{Theorema'Language'SIMPRNG} [\text{Theorema'Language'VAR} [\text{Theorema'Knowledge'VAR} yTM]]]$   
 $\text{Theorema'Language'EqualDefTM} [\text{Theorema'Language'SubsetEqualTM} [\text{Theorema'Language'VAR} [\text{Theorema'Knowledge'VAR} zTM]]]$   
 $\text{Theorema'Language'ForallTM} [\text{Theorema'Language'RNG} [\text{Theorema'Language'SIMPRNG} [\text{Theorema'Language'VAR} [\text{Theorema'Knowledge'VAR} zTM]]]]]$   
 $\text{True, Theorema'Language'ImpliesTM} [\text{Theorema'Language'ElementTM} [\text{Theorema'Language'VAR} [\text{Theorema'Knowledge'VAR} zTM]]]$   
 $\text{Theorema'Language'ElementTM} [\text{Theorema'Language'VAR} [\text{Theorema'Knowledge'VAR} zTM]]]$   
 $\text{Theorema'Language'VAR} [\text{Theorema'Knowledge'VAR} yTM]]]$

■ Cell reached

### 3.2 Proposition (transitivity of $\subseteq$ )

$\forall_{\text{Theorema'Language' } RNG} [\text{Theorema'Language'SIMPRNG} [\text{Theorema'Language'VAR} [\text{Theorema'Knowledge'VAR} aTM]]]$   
 $\text{Theorema'Language'SIMPRNG} [\text{Theorema'Language'VAR} [\text{Theorema'Knowledge'VAR} bTM]]]$   
 $\text{Theorema'Language'SIMPRNG} [\text{Theorema'Language'VAR} [\text{Theorema'Knowledge'VAR} cTM]]]$   
 $\text{Theorema'Language'SubsetEqualTM} [\text{Theorema'Language'VAR} [\text{Theorema'Knowledge'VAR} aTM]]]$   
 $\text{Theorema'Language'VAR} [\text{Theorema'Knowledge'VAR} bTM]] \wedge$   
 $\text{Theorema'Language'SubsetEqualTM} [\text{Theorema'Language'VAR} [\text{Theorema'Knowledge'VAR} bTM]]]$   
 $\implies \text{Theorema'Language'SubsetEqualTM} [\text{Theorema'Language'VAR} [\text{Theorema'Knowledge'VAR} aTM]]]$

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