

Lecture 5

Ellipse :

$$\frac{(x-h)^2}{a^2} + \frac{(y-k)^2}{b^2} = 1$$

 $\Rightarrow a > b \Rightarrow \text{horizontal ellipse}$

$$\Rightarrow c^2 = a^2 - b^2$$

Ex. $\frac{(x+1)^2}{9} + \frac{(y-2)^2}{25} = 1$ Find center, The line contain major and minor axis, The vertices, The end point of minor axes, Foci

 $a < b$ Center $(-1, 2)$

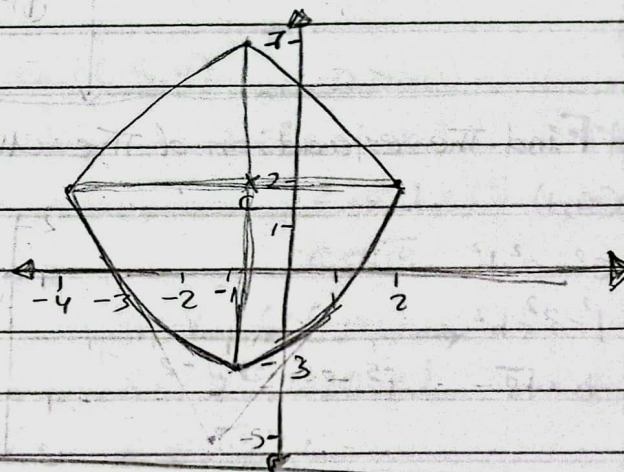
$$c^2 = b^2 - a^2 = 25 - 9 = 16$$

$$F_1 = (-1, 6) \quad F_2 = (-1, -2)$$

$$V_1 = (-1, 7) \quad V_2 = (-1, -5)$$

$$x = -1 \quad (\text{Major})$$

$$y = 2 \quad (\text{Minor})$$



$$\frac{(x-2)^2}{4} + \frac{(y+3)^2}{9} = 1$$

Center $(2, -3)$

$$b > a$$

$$c^2 = b^2 - a^2 = 9 - 4 = 5$$

$$c = \sqrt{5}$$

$$F_1 = (2, -3 + \sqrt{5}), F_2 = (2, -3 - \sqrt{5})$$

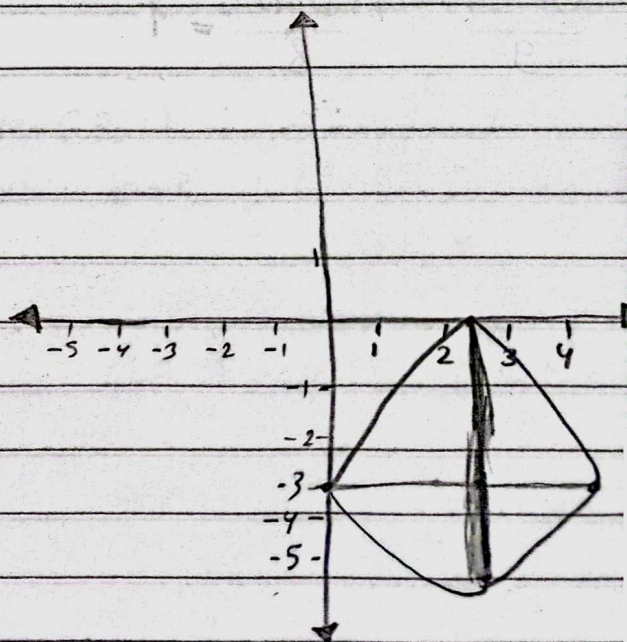
$$V_1 = (2, 0), V_2 = (2, -6)$$

$$V_3 = (0, -3), V_4 = (4, -3)$$

$$\text{Major } x = 2$$

$$\text{Minor } y = -3$$

$$e = \pm \frac{\sqrt{5}}{3}$$



$$\star \frac{x^2}{9} + \frac{y^2}{25} = 1$$

Center = (0,0)

$b > a$

$$c^2 = b^2 - a^2 = 25 - 9 = 16$$

$$c = \pm 4$$

$$F_1(0, 4), F_2(0, -4)$$

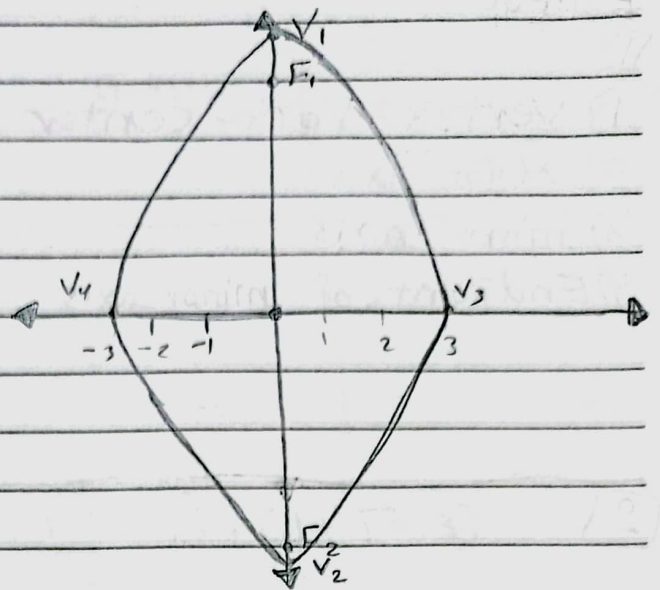
$$V_1(0, 5), V_2(0, -5)$$

$$V_3(0, 3), V_4(0, -3)$$

Major = $x = 0$

Minor = $y = 0$

$$e = \pm \frac{4}{5}$$



$$\star 12x^2 + 3y^2 - 30y + 39 = 0 \quad (\div 3)$$

$$4x^2 + y^2 - 10y + 13 = 0$$

$$4x^2 + (y-5)^2 + 25 + 13 = 0$$

$$4x^2 + (y-5)^2 = 12 \quad (\div 12)$$

$$\frac{x^2}{3} + \frac{(y-5)^2}{12} = 1$$

Center (0,5)

$$b > a \rightarrow c^2 = b^2 - a^2 = 12 - 3 = 9$$

$$c = \pm 3$$

$$F_1(0, 8), F_2(0, 2)$$

$$V_1(0, 5 + \sqrt{12}), V_2(0, 5 - \sqrt{12})$$

$$V_3(\sqrt{3}, 5), V_4(-\sqrt{3}, 5)$$

Major = $x = 0$, Minor = $y = 5$

\star Find The Standard Form of the eq. of the ellipse which has given properties Foci (0, ± 5), Vertex (0, ± 8)

$$\frac{x^2}{39} + \frac{y^2}{64} = 1$$

$$25 = 64 - x$$

$$x = 39$$