

- ① $1 \text{ cm} = 10^{-2} \text{ m}$, $100 \text{ cm} = 1 \text{ m}$
- ② $1 \text{ g} = 10^{-3} \text{ Kg}$, $1000 \text{ g} = 1 \text{ Kg}$
- ③ $1 \text{ dyne} = 1 \text{ g} \cdot \text{cm/s}^2 = 10^{-5} \text{ Kg} \cdot \text{m/s}^2 = 10^{-5} \text{ N}$
- ④ $1 \text{ Ft} (12 \text{ in}) \rightarrow 1 \text{ in} = 2.54 \text{ cm}$
- ⑤ $1 \text{ lbs} \approx 4.448222$
- ⑥ $1 \text{ Slug} = 0.45359237 \text{ Kg}$
- ⑦ $1 \text{ h} = 60 \text{ min} = 3600 \text{ s}$
- ⑧ $1^\circ = \pi / 180 \text{ rad}$ (degree)
- ⑨ $1 \text{ t} = 1000 \text{ Kg}$ (ton)

Quantity	Dimension	unit	Quantity	Dimension	unit
Length	L	m	Torque	ML^2T^{-2}	N.m
Mass	M	Kg	Power	ML^2T^{-3}	N.m/s, W
Time	T	s	Impulse	MLT^{-1}	N.s
Area	L^2	m^2	Area moment of inertia	L^4	m^4
Volume	L^3	m^3	Mass // of //	ML^2	$\text{Kg} \cdot m^2$
Velocity	LT^{-1}	m/s	Mass density	ML^{-3}	$\text{Kg} \cdot m^{-3}$
Acceleration	LT^{-2}	m/s^2	weight density	$ML^{-2}T^{-2}$	N/m^3
Momentum	MLT^{-1}	N.s	Frequency	T^{-1}	s^{-1} , Hz
Force	MLT^{-2}	N	Angular displacement		rad*
work done	ML^2T^{-2}	N.m or J	Angular Velocity	T^{-1}	rad/s
Energy	ML^2T^{-2}	N.m, J	Angular acceleration	T^{-2}	rad/s ²
Moment Force	ML^2T^{-2}	N.m			

★ $V = V_0 + at$

★ ~~$V = V_0 + at$~~ $V^2 = V_0^2 + 2as$

★ $S = V_0t + \frac{1}{2}at^2$

PreFix	Multi. Factor	PreFix	Multi. Factor
Pico - (p)	10^{-12}	deca - (da)	10^1
nano - (n)	10^{-9}	hecta - (h)	10^2
micro - (μ)	10^{-6}	Kilo - (K)	10^3
milli - (m)	10^{-3}	mega - (M)	10^6
Centi - (c)	10^{-2}	hecto giga - (G)	10^9
deci - (d)	10^{-1}	tera - (T)	10^{12}

★ $\vec{F} = m \vec{a}$ (a \rightarrow acceleration)

★ $F = mg$ (g \rightarrow acceleration due to gravity)

★ $F = \frac{G m_1 m_2}{r^2}$ ($G = 6.673 \times 10^{-11} \text{ N.m}^2/\text{Kg}^2$)

★ Scalars \rightarrow Magnitude \rightarrow (Mass - length - time - ...)

★ Vectors \rightarrow Magnitude - direction \rightarrow (Velocity - acceleration...)

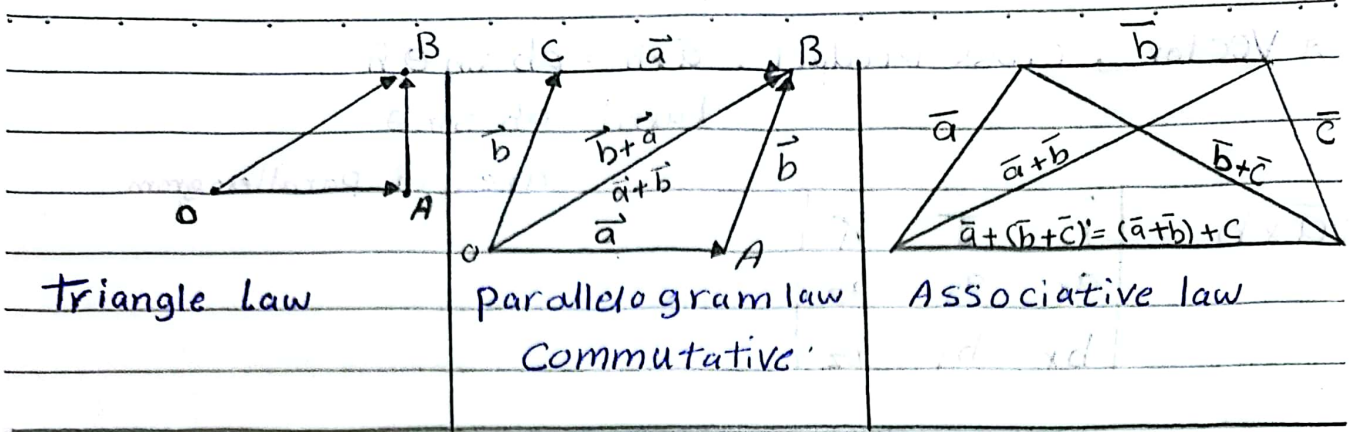
★ Unit Vector $\rightarrow \vec{a} = |\vec{a}| \hat{n} = a \hat{n} \rightarrow \hat{n} = \frac{\vec{a}}{|\vec{a}|}$

★ Null Vector \rightarrow magnitude = Zero

★ Negative of vector \rightarrow Same magnitude, opposite direction

★ Parallel Vectors \rightarrow Cross Product = Zero
(Coplanar vectors)

★ Perpendicular Vectors \rightarrow Dot Product = Zero



★ Resolution of a vector

$$\vec{a} = \vec{a}_x + \vec{a}_y = a_x \hat{i} + a_y \hat{j} = a \cos \theta \hat{i} + a \sin \theta \hat{j}$$

$$|\vec{a}| = a = \sqrt{a_x^2 + a_y^2}, \quad \theta = \tan^{-1} \left[\frac{a_y}{a_x} \right]$$

$$\vec{a} = \vec{a}_x + \vec{a}_y + \vec{a}_z = a [\cos \theta_x \hat{i} + \cos \theta_y \hat{j} + \cos \theta_z \hat{k}]$$

$$|\vec{a}| = a = \sqrt{a_x^2 + a_y^2 + a_z^2} \rightarrow \cos \theta_x = \frac{a_x}{a}, \quad \cos \theta_y = \frac{a_y}{a}, \quad \cos \theta_z = \frac{a_z}{a}$$

$$\hat{n} = \cos \theta_x \hat{i} + \cos \theta_y \hat{j} + \cos \theta_z \hat{k} \quad \star \cos^2 \theta_x + \cos^2 \theta_y + \cos^2 \theta_z = 1$$

★ Scalar, Dot Product : $\vec{a} \cdot \vec{b} = ab \cos \theta = (a_x b_x \hat{i} + a_y b_y \hat{j} + a_z b_z \hat{k})$

$$\cos \theta = \frac{\vec{a} \cdot \vec{b}}{a b}, \quad b \cos \theta = \frac{\vec{a} \cdot \vec{b}}{a} \quad \star \text{Projection of } \vec{b} \text{ on } \vec{a} = b \cos \theta$$

$$\star \text{Projection of } \vec{a} \text{ on } \vec{b} = a \cos \theta$$

$$\rightarrow \vec{a} \cdot \vec{b} = ab \cos \theta = ba \cos \theta = \vec{b} \cdot \vec{a} \quad (\text{commutative})$$

$$\rightarrow \vec{a} \cdot (\vec{b} + \vec{c}) = \vec{a} \cdot \vec{b} + \vec{a} \cdot \vec{c} \quad (\text{distributive})$$

$$\rightarrow \text{work done} = \vec{F} \cdot d\vec{r}$$

★ Scalar

$$\hat{i} \cdot \hat{i} = \hat{j} \cdot \hat{j} = \hat{k} \cdot \hat{k} = 1$$

$$\hat{i} \cdot \hat{j} = \hat{j} \cdot \hat{i} = \hat{j} \cdot \hat{k} = \hat{k} \cdot \hat{j} = \hat{k} \cdot \hat{i} = \hat{i} \cdot \hat{k} = 0$$

★ Vector

$$\hat{i} \times \hat{i} = \hat{j} \times \hat{j} = \hat{k} \times \hat{k} = \vec{0}$$

$$\hat{j} \times \hat{i} = -\hat{k} \quad \text{clockwise } (+)$$

$$\hat{i} \times \hat{j} = \hat{k} \quad \text{anticlockwise } (-)$$

* Vector , Cross Product : $\vec{a} \times \vec{b} = ab \sin \theta \hat{n}$

$$|\vec{a} \times \vec{b}| = ab \sin \theta$$

= area of parallelogram

$$\vec{a} \times \vec{b} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ a_x & a_y & a_z \\ b_x & b_y & b_z \end{vmatrix}$$

* $\vec{a} \times \vec{b} \neq \vec{b} \times \vec{a} \rightarrow \vec{a} \times \vec{b} = -(\vec{b} \times \vec{a})$ (Not commutative)

* $(\vec{a} \times \vec{b}) \times \vec{c} \neq \vec{a} \times (\vec{b} \times \vec{c})$ (Not associative)

* $\vec{a} \times (\vec{b} + \vec{c}) = (\vec{a} \times \vec{b}) + (\vec{a} \times \vec{c})$ (distributive)

* Scalar Triple Product :

$$(\vec{a} \times \vec{b}) \cdot \vec{c} = a_x(b_y c_z - b_z c_y) - a_y(b_x c_z - b_z c_x) + a_z(b_x c_y - b_y c_x)$$

$$(\vec{a} \times \vec{b}) \cdot \vec{c} = \begin{vmatrix} a_x & a_y & a_z \\ b_x & b_y & b_z \\ c_x & c_y & c_z \end{vmatrix} = |\vec{a} \times \vec{b}| |\vec{c}| \cos \theta$$

$\rightarrow (\vec{a} \times \vec{b}) \cdot \vec{c} = \vec{a} \cdot (\vec{b} \times \vec{c})$ (Commutative)

* Vector Triple product:

$$\vec{a} \times (\vec{b} \times \vec{c}) = \vec{b}(\vec{a} \cdot \vec{c}) - \vec{c}(\vec{a} \cdot \vec{b})$$