

## Section 3

Solve by Jacobi Method For two steps and what The max. absolute relative error after Second iteration?

$$① 4x + 2y + z = 11$$

$$-x + 2y = 3$$

$$2x + y + 4z = 16$$

$$x_0 = \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix} \rightarrow x = \frac{11 - 2y - z}{4}$$

$$z = \frac{16 - 2x - y}{4}$$

$$y = \frac{3 + x}{2}$$

$$\begin{bmatrix} 4 & 2 & 1 \\ -1 & 2 & 0 \\ 2 & 1 & 4 \end{bmatrix}$$

$$E = \frac{x^{\text{new}} - x^{\text{old}}}{x^{\text{new}}} \times 100\%$$

n	x	e <sub>1</sub>	y	e <sub>2</sub>	z	e <sub>3</sub>
0	1	<del>50%</del>	1		1	
1	2	50%	2	50%	$\frac{13}{4}$	69.236%
2	$\frac{15}{4}$	<del>113.33%</del>	$\frac{5}{2}$	20%	$\frac{5}{2}$	30%

113.33%

max. = 113.33%

$$② x - 4y + z = -2$$

$$\rightarrow y + 2z = 3$$

$$\rightarrow 5x + 2y = 7$$

$$\begin{bmatrix} 1.2 \\ 0.8 \\ 1.2 \end{bmatrix}$$

$$x = \frac{7 - 2y}{5}$$

$$y = \frac{-2 - z + x}{-4}$$

$$z = \frac{3 - y}{2}$$

$$= 5x + 2y = 7$$

$$x - 4y + z = -2$$

$$y + 2z = 3$$

$$\begin{bmatrix} 5 & -2 & 0 \\ 1 & -4 & 1 \\ 0 & 1 & 2 \end{bmatrix}$$

n	x	e <sub>1</sub>	y	e <sub>2</sub>	z	e <sub>3</sub>
0	1.2		0.8		1.2	
1	1.08		1.47		0.75	
2	0.96		1.045		0.95	



3) Solve by gauss seidel two steps

$$56x + 23y = 2$$

$$66y - 13z = 3$$

$$3x - 5y + 47z = 1$$

$$X_0 = \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}$$

$$x = \frac{2 - 23y}{56}$$

$$z = \frac{1}{47}(1 - 3x + 5y)$$

$$y = \frac{1}{66}(3 + 13z)$$

It is diagonally dominant

n	x	y	z
0	0	0	0
1	$\frac{1}{28}$	$\frac{1}{22}$	0.02383
2	$\frac{3}{176}$	0.05014	0.02552

4) Solve by gauss seidel three steps

$$\begin{bmatrix} 3 & -5 & 47 \\ 56 & 23 & 11 \\ 17 & 66 & -13 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix}, X_0 = \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix} \rightarrow \begin{bmatrix} 56 & 23 & 11 & 2 \\ 17 & 66 & -13 & 3 \\ 13 & -5 & 47 & 1 \end{bmatrix}$$

$$x = \frac{-23y - 11z + 2}{56}, y = \frac{3 + 13z - 17x}{66}, z = \frac{1 + 5y - 3x}{47}$$

n	x	y	z
0	0	0	0
1	$\frac{1}{28}$	$\frac{67}{1848}$	$\frac{1985}{86856}$
2	$\frac{5675}{347424}$	$\frac{1042017}{22929984}$	$\frac{27051419}{1077709248}$
3	0.011994	0.047309	0.025437