

TDT4205 Compilers

Exercise 3

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PART 1 Theory

Task 1.1 Parsing

1.1.1 LL(k)

Even if $LL(k)$ in theory can be extended with an \rightarrow *infinitely* number of lookaheads, this will not resolve the problems with left recursion. For each lookahead-symbol extra, the parse table grows, and at the end it will become humongous. To create and use such a table is both space and time consuming, and we will never have neither space nor time to parse languages and grammars with arbitrary use of left recursion, as it requires arbitrary much space and time. Also, $LL(k)$ needs the k to be defined, which sets an upper bound for the number of lookaheads before we begin parsing. We may set the k to 10000000000, and hope that the language will never exceed this number of recursions, but it will not be a *valid* parser for that language, as it can only handle a subset of the possible language constructs.

1.1.2 Left-recursive grammars

The left-recursive grammar:

```
F  →  f I v A w S x
A  →  P
P  →  P I | ε
S  →  S s | s
I  →  i
```

The equivalent non-left-recursive grammar:

$$\begin{aligned} F &\rightarrow f I v A w S x \\ A &\rightarrow P \\ P &\rightarrow I P \mid \epsilon \\ S &\rightarrow s S' \\ S' &\rightarrow s S' \mid \epsilon \\ I &\rightarrow i \end{aligned}$$

1.1.3 FIRST and FOLLOW & LL(1) Parsing table

FIRST and FOLLOW

Computing FIRST

- f is in $\text{FIRST}(F)$, since f is the first symbol in production of F , and f is a terminal, and thereby $\text{FIRST}(f) = f$.
- i is in $\text{FIRST}(I)$, since $\text{FIRST}(I) = \text{FIRST}(i) = i$
- i is in $\text{FIRST}(P)$, since $\text{FIRST}(P) = \text{FIRST}(I) = i$
- ϵ is in $\text{FIRST}(P)$, since P has a production $P \rightarrow \epsilon$
- i, ϵ is in $\text{FIRST}(A)$, since $\text{FIRST}(A) = \text{FIRST}(P) = i, \epsilon$
- s is in $\text{FIRST}(S)$ since $\text{FIRST}(S) = \text{FIRST}(s) = s$
- s is in $\text{FIRST}(S')$ since $\text{FIRST}(S') = \text{FIRST}(s) = s$
- ϵ is in $\text{FIRST}(S')$, since S' has a production $S' \rightarrow \epsilon$

Computing FOLLOW

- We start by adding $\$$ to F , since F is our *start-symbol*.
- We see from $F \rightarrow f I v A w S x$ that w is in $\text{FOLLOW}(A)$, x is in $\text{FOLLOW}(S)$ and v is in $\text{FOLLOW}(I)$
- $\text{FOLLOW}(P) = \text{FOLLOW}(A)$ since $A \rightarrow P$.
- $\text{FOLLOW}(S') = \text{FOLLOW}(S)$ since $S \rightarrow S'$.
- $\text{FOLLOW}(I)$ includes $\text{FIRST}(P)$ except ϵ since $P \rightarrow I P \mid \epsilon$, and rule 3, which makes $\text{FOLLOW}(I) = i, v$

NT	FIRST	FOLLOW
F	f	\$
A	i, ϵ	w
P	i, ϵ	w
S	s	x
S'	s, ϵ	x
I	i	i, v, w

LL(1) Parsing table

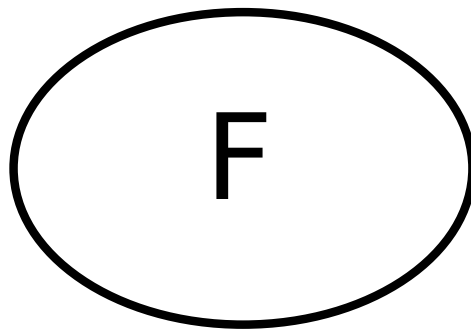
Followed page 224, Alg. 4.31

IF $A \rightarrow b$ AND $\text{FIRST}(b)$ contains c THEN add $A \rightarrow b$ to $M(A,c)$ and

IF $\text{FIRST}(b)$ contains ϵ , THEN add $A \rightarrow \epsilon$ to $M(A,c)$ $M(A,b)$ $M(A,c)$

Non-Terminal	Input Symbol						
	f	i	v	w	s	x	\$
F	$F \rightarrow f I v A w S x$						
A		$A \rightarrow P$		$A \rightarrow \epsilon$			
P		$P \rightarrow I P$		$P \rightarrow \epsilon$			
S					$S \rightarrow sS'$		
S'					$S' \rightarrow sS'$	$S' \rightarrow \epsilon$	
I		$I \rightarrow i$					

1.1.4 Parse tree for LL(1)



LL1-Par