Final Project

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 $Notes: \ Possible \ source \ of \ population \ data: \ http://www.abs.gov.au/AUSSTATS/abs@.nsf/DetailsPage/3105.0.65.0012014? \ OpenDocument$

Change working directory here

Load data (assumes file is in working directory)

```
#load the data
beerData<-read.csv("monthly-beer-production-in-austr.csv")

#cut off the last row which is NA
beerData<-beerData[-nrow(beerData),]
colnames(beerData)<-c("Month", "Production")

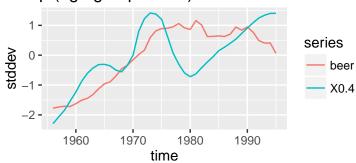
#turn into time series also hold back the last two years of data for forecasting
beerTS<-ts(beerData[1:(nrow(beerData)-24),2], frequency=12, start=c(1956,1))
beer_forecast<-ts(beerData[(nrow(beerData)-23):nrow(beerData), 2], start=c(1993,9), frequency=12)</pre>
```

Investigate possible deterministic relationship with population data

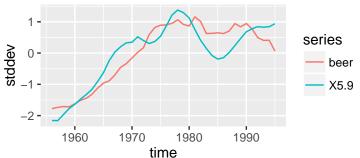
```
#load population data
library(reshape)
## Warning: package 'reshape' was built under R version 3.2.5
library(ggplot2)
## Warning: package 'ggplot2' was built under R version 3.2.5
#Clean up population data
pop_totalData<-t(read.csv("Pop_total.csv", row.names=1))</pre>
dropCols<-colnames(pop totalData) %in% c("Unspecified", "Period not indicated")
rownames(pop_totalData) <-c(1921:2011)
pop_totalData<-pop_totalData[paste(1956:1995),!dropCols]</pre>
#Aggregate beer data
beerYear <- seq(from = 1956, to = 1996, by = 1)
beerYear <- rep(beerYear, each=12)
beerYear<-beerYear[1:nrow(beerData)]</pre>
beerAg<-aggregate(beerData[,2], FUN=mean, by=list(year=beerYear))</pre>
#Attach to beer data
beerPop<-data.frame(cbind(beer=beerAg[,2],pop_totalData))</pre>
beerPopScale<-scale(beerPop)</pre>
beerPopRes<-melt(beerPopScale, variable.name="series")</pre>
colnames(beerPopRes)<-c("time", "series", "stddev")</pre>
allNames <-colnames (beerPop) [2:length(colnames (beerPop))]
```

```
par(mfrow=c(2,2))
for (name in allNames) {
  subset_data<-subset(beerPopRes, beerPopRes$series%in%c("beer", name))</pre>
  newPlot<-ggplot(subset_data, aes(time,stddev)) + geom_line(aes(colour = series)) +ggtitle(paste("Pop (age gr</pre>
}
```

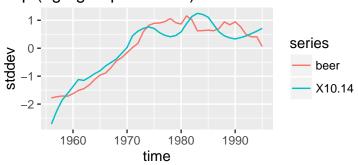
Pop (age group X0.4) and Beer Prod



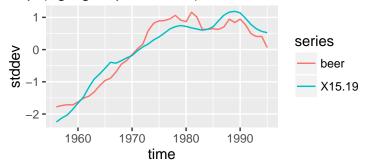
Pop (age group X5.9) and Beer Prod



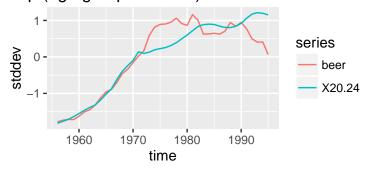
Pop (age group X10.14) and Beer Prod



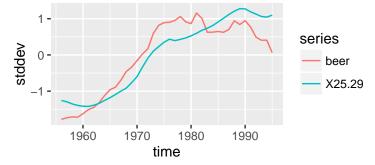
Pop (age group X15.19) and Beer Prod



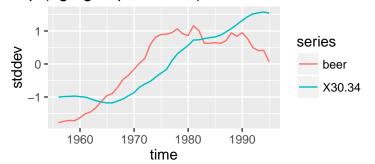
Pop (age group X20.24) and Beer Prod

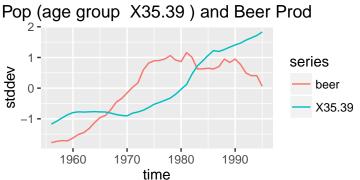


Pop (age group X25.29) and Beer Prod

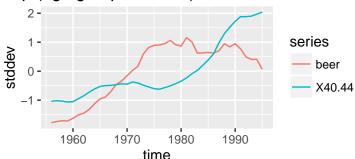


Pop (age group X30.34) and Beer Prod

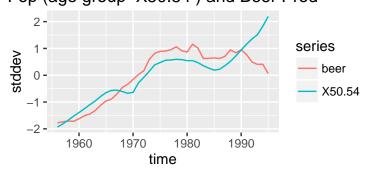




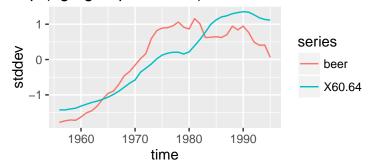
Pop (age group X40.44) and Beer Prod



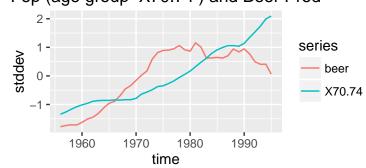
Pop (age group X50.54) and Beer Prod



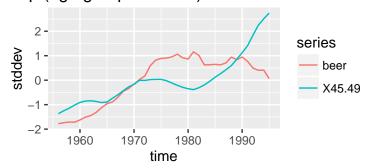
Pop (age group X60.64) and Beer Prod



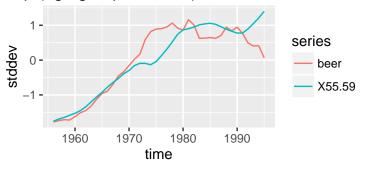
Pop (age group X70.74) and Beer Prod



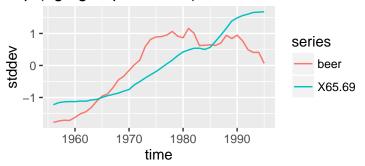
Pop (age group X45.49) and Beer Prod



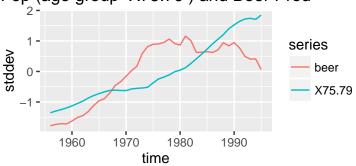
Pop (age group X55.59) and Beer Prod



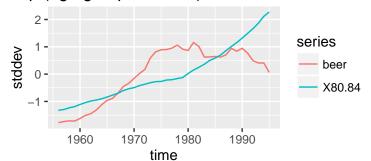
Pop (age group X65.69) and Beer Prod



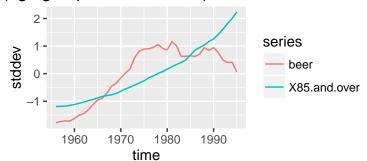
Pop (age group X75.79) and Beer Prod



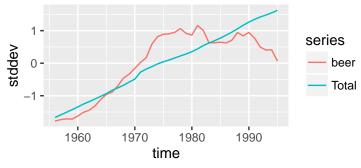
Pop (age group X80.84) and Beer Prod



(age group X85.and.over) and Beer Prod



Pop (age group Total) and Beer Prod



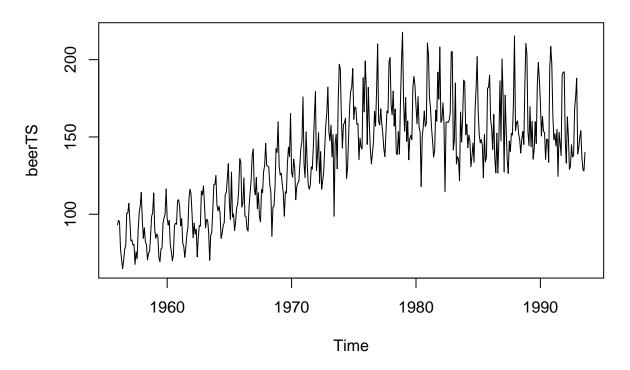
par(mfrow=c(1,1))

It appears that there may be a relationship with the 15-19 age block, which makes sense since the legal drinking age is 18. We may be able to use this as our deterministic trend.

Plot data

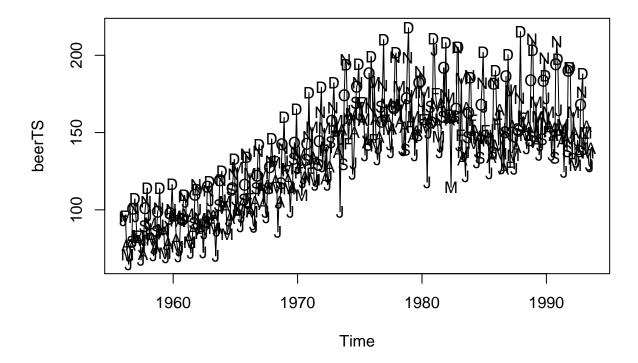
```
par(mfrow=c(1,1))
plot(beerTS, main="Beer Production in Australia by Month")
```

Beer Production in Australia by Month



plot(beerTS, main="Beer Production in Australia by Month (seasons marked)", type="1")
points(y=beerTS, x=time(beerTS), pch=as.vector(season(beerTS)))

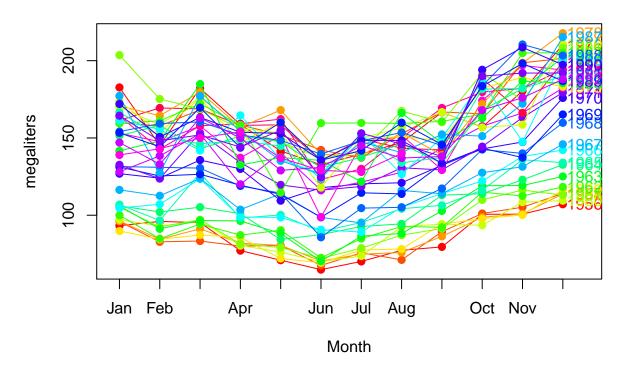
Beer Production in Australia by Month (seasons marked)



Another plot to show seasonality

```
require(fpp)
## Loading required package: fpp
## Loading required package: forecast
## Loading required package: zoo
##
## Attaching package: 'zoo'
## The following objects are masked from 'package:base':
##
       as.Date, as.Date.numeric
##
## Loading required package: timeDate
##
## Attaching package: 'timeDate'
##
  The following objects are masked from 'package:TSA':
##
##
       kurtosis, skewness
## This is forecast 7.0
##
## Attaching package: 'forecast'
## The following objects are masked from 'package:TSA':
##
##
       fitted.Arima, plot.Arima
## The following object is masked from 'package:nlme':
##
##
       getResponse
## Loading required package: fma
## Loading required package: expsmooth
## Loading required package: lmtest
seasonplot(beerTS, year.labels=TRUE, ylab="megaliters", main="Seasonal plot: quarterly beer production", col=rain
```

Seasonal plot: quarterly beer production

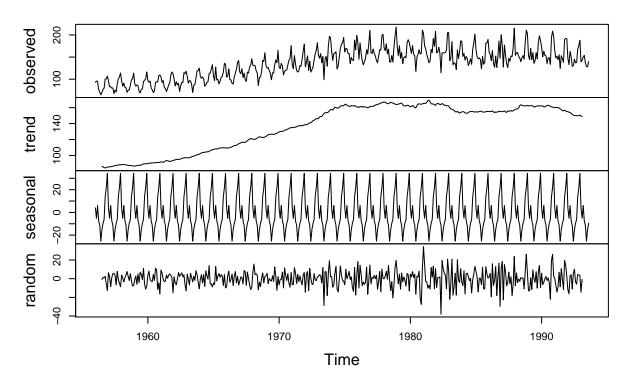


In the plot we see obvious seasonality with higher production in November and December and lower production in June and July. There is a trend which may be difficult to fit as it doesn't appear to be a "well known" function like a linear or quadratic function, so we'll have to experiment. It also looks like the variance of the data is larger in the middle, so we will probably want to take the log of our data to correct that varaince issue.

Decompsing the time series to see trends and patterns

```
decompbeer = decompose (beerTS, type="additive")
plot (decompbeer)
```

Decomposition of additive time series



by looking at the decomposed figures, i was wondering what if we plot a harmonic function with a quadradit polynomial... like imposing a sine curve with 2nd order poly?

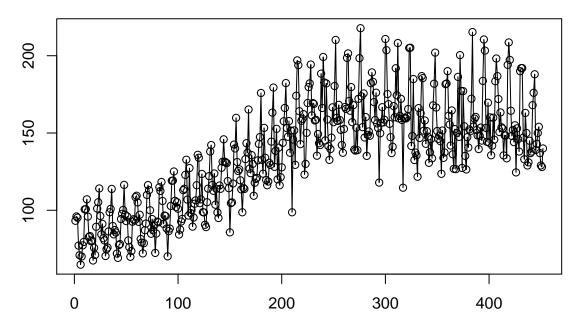
Try to figure out deterministic trend

```
t<-1:length(beerTS)
t2<-t^2
t3<-t^3
t4<-t^4
t5<-t<sup>5</sup>
quadFit<-lm(beerTS~t+t2)
summary(quadFit)
##
## Call:
## lm(formula = beerTS ~ t + t2)
##
## Residuals:
##
       Min
                 1Q Median
                                  3Q
                                         Max
   -46.861 -14.133 -1.991
                                      61.174
##
                             11.937
##
## Coefficients:
##
                  Estimate Std. Error t value Pr(>|t|)
  (Intercept) 6.560e+01
##
                            2.828e+00
                                         23.20
                                                  <2e-16 ***
                 5.429e-01
## t
                            2.883e-02
                                         18.83
                                                  <2e-16 ***
## t2
                -7.721e-04
                            6.163e-05
                                        -12.53
                                                  <2e-16 ***
##
## Signif. codes:
                    0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
##
## Residual standard error: 19.95 on 449 degrees of freedom
## Multiple R-squared: 0.6616, Adjusted R-squared: 0.6601
## F-statistic: 439 on 2 and 449 DF, p-value: < 2.2e-16</pre>
```

plot the data and the fitted quadratic trend function
plot(x=1:length(beerTS),y=beerTS,type='o',ylab="",xlab="Time - Number of Months Since Jan 1956",main="Quadrati
curve(expr = coef(quadFit)[1]+coef(quadFit)[2]*x+coef(quadFit)[3]*x^2+coef(quadFit)[4]*x^3,lty=1,add = TRUE, c

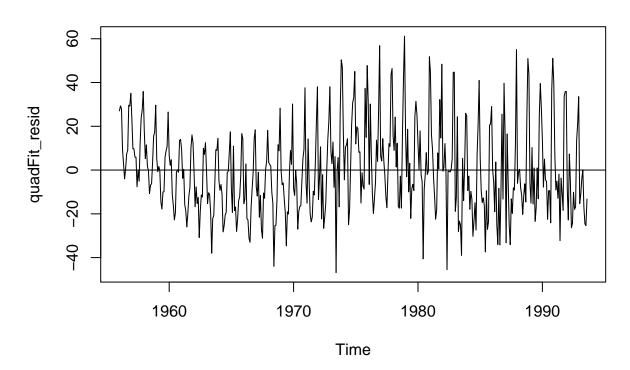
Quadratic Fit on Beer Production Data



Time - Number of Months Since Jan 1956

quadFit_resid<-ts(residuals(quadFit),frequency=12, start=c(1956,1))
plot(quadFit_resid, main="Residuals from a Quadratic Trend Fit")
abline(h=0)</pre>

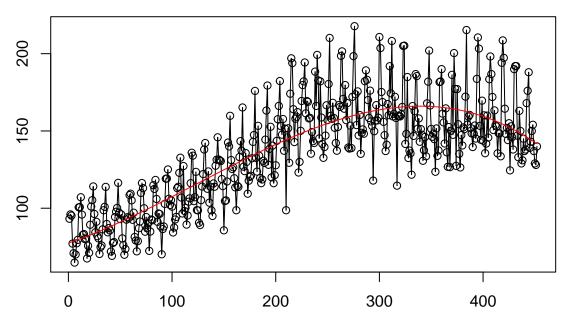
Residuals from a Quadratic Trend Fit



```
cubicFit<-lm(beerTS~t+t2+t3)
summary(cubicFit)</pre>
```

```
##
## Call:
##
   lm(formula = beerTS \sim t + t2 + t3)
##
## Residuals:
##
                10 Median
                                3Q
                                       Max
  -50.660 -13.783 -2.601
##
                           12.434
                                    57.639
##
## Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
##
  (Intercept) 7.745e+01 3.695e+00 20.963 < 2e-16 ***
##
                2.307e-01
                          7.056e-02
                                       3.270 0.00116 **
## t
                9.490e-04
                          3.617e-04
                                       2.624
                                             0.00900 **
## t2
                          5.249e-07
                                     -4.826 1.92e-06 ***
## t3
               -2.533e-06
##
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
##
## Residual standard error: 19.47 on 448 degrees of freedom
## Multiple R-squared: 0.6784, Adjusted R-squared: 0.6762
## F-statistic:
                  315 on 3 and 448 DF, p-value: < 2.2e-16
#### plot the data and the fitted quadratic trend function
plot(x=1:length(beerTS),y=beerTS,type='o',ylab="",xlab="Time - Number of Months Since Jan 1956",main="Cubic Fi
curve(expr = coef(cubicFit)[1]+coef(cubicFit)[2]*x+coef(cubicFit)[3]*x^2+coef(cubicFit)[4]*x^3,lty=1,add = TRU
```

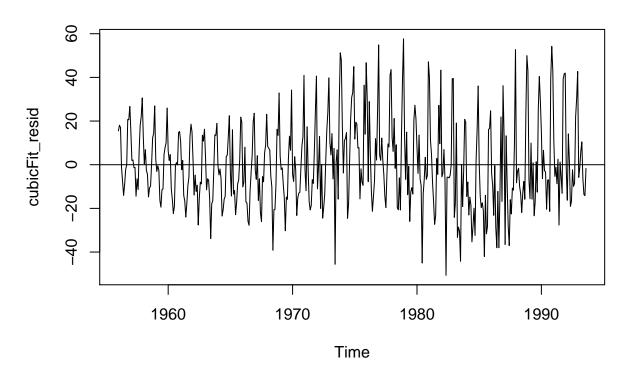
Cubic Fit on Beer Production Data



Time - Number of Months Since Jan 1956

cubicFit_resid<-ts(residuals(cubicFit),frequency=12, start=c(1956,1))
plot(cubicFit_resid, main="Residuals from a Cubic Trend Fit")
abline(h=0)</pre>

Residuals from a Cubic Trend Fit



```
order4polyFit<-lm(beerTS~t+t2+t3+t4)
summary(order4polyFit)</pre>
```

 $lm(formula = beerTS \sim t + t2 + t3 + t4)$

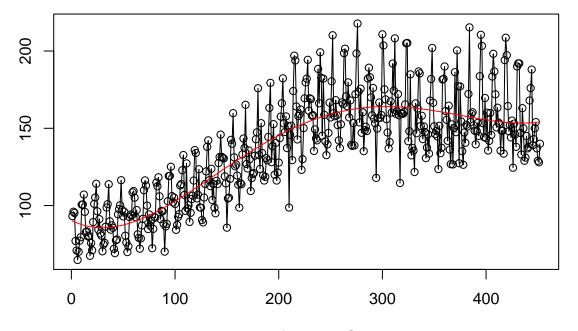
Call:

##

```
## Residuals:
##
       Min
                1Q Median
                                3Q
                                       Max
   -50.079 -12.721 -3.199
                            10.135
                                    57.983
##
##
##
  Coefficients:
                 Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 9.037e+01 4.536e+00
                                     19.924
                                             < 2e-16 ***
##
               -3.341e-01 1.384e-01
                                     -2.414
                                               0.0162 *
## t.2
                6.545e-03 1.241e-03
                                       5.276 2.07e-07 ***
                                     -5.285 1.97e-07 ***
## t3
               -2.173e-05
                          4.113e-06
                2.119e-08
                          4.504e-09
                                       4.706 3.38e-06 ***
## t4
##
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
##
## Residual standard error: 19.03 on 447 degrees of freedom
## Multiple R-squared: 0.6935, Adjusted R-squared: 0.6908
## F-statistic: 252.9 on 4 and 447 DF, \, p-value: < 2.2e-16
#### plot the data and the fitted 4th order polynomial trend function
plot(x=1:length(beerTS),y=beerTS,type='o',ylab="",xlab="Time - Number of Months Since Jan 1956",main="order4po
```

curve(expr = coef(order4polyFit)[1]+coef(order4polyFit)[2]*x+coef(order4polyFit)[3]*x^2+coef(order4polyFit)[4]

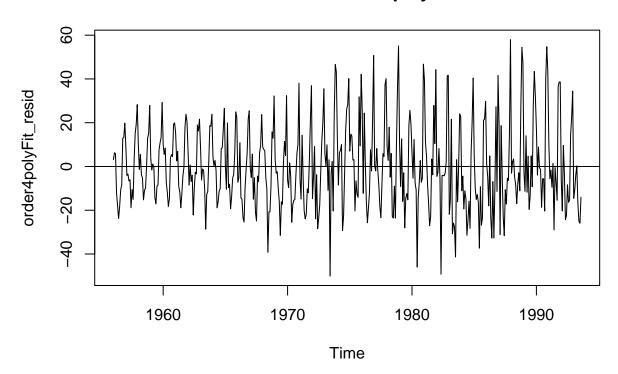
order4poly Fit on Beer Production Data



Time - Number of Months Since Jan 1956

```
order4polyFit_resid<-ts(residuals(order4polyFit),frequency=12, start=c(1956,1))
plot(order4polyFit_resid, main="Residuals from a order4poly Trend Fit")
abline(h=0)
```

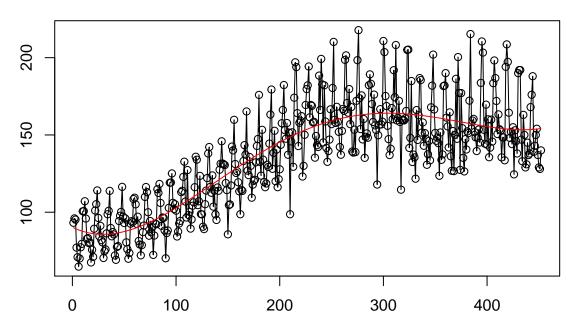
Residuals from a order4poly Trend Fit



```
order5polyFit<-lm(beerTS~t+t2+t3+t4+t5)
summary(order5polyFit)</pre>
```

```
##
## Call:
##
  lm(formula = beerTS \sim t + t2 + t3 + t4 + t5)
##
## Residuals:
##
       Min
                1Q Median
                                3Q
                                       Max
##
   -50.069 -12.729
                   -3.179 10.132
                                    58.012
##
  Coefficients:
##
##
                 Estimate Std. Error t value Pr(>|t|)
  (Intercept) 9.029e+01 5.483e+00
##
                                      16.469
                                                <2e-16 ***
## t
               -3.288e-01
                          2.436e-01
                                      -1.350
                                                0.1778
## t2
                6.463e-03
                           3.323e-03
                                       1.945
                                                0.0524
               -2.126e-05
                           1.858e-05
                                      -1.144
                                                0.2532
## t3
##
  t4
                2.000e-08
                           4.519e-08
                                       0.443
                                                0.6582
                1.049e-12
                                       0.026
                                                0.9789
## t5
                           3.970e-11
##
## Signif. codes:
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 19.05 on 446 degrees of freedom
## Multiple R-squared: 0.6935, Adjusted R-squared: 0.6901
## F-statistic: 201.9 on 5 and 446 DF, p-value: < 2.2e-16
```

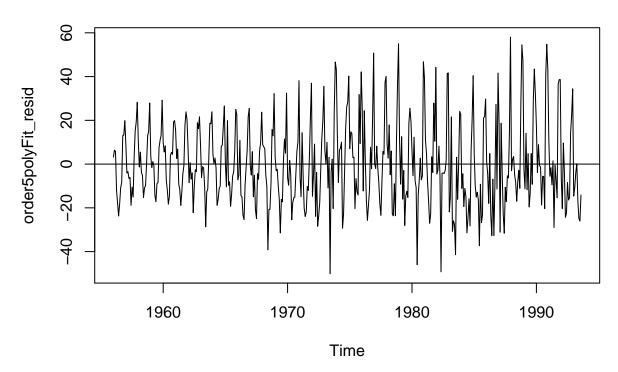
order5poly Fit on Beer Production Data



Time - Number of Months Since Jan 1956

order5polyFit_resid<-ts(residuals(order5polyFit),frequency=12, start=c(1956,1))
plot(order5polyFit_resid, main="Residuals from a order5poly Trend Fit")
abline(h=0)

Residuals from a order5poly Trend Fit



It looks like a 4th order polynomial might take care of the worst of it, the question is are we okay with using a 4th order polynomial or should we drop it down to a cubic function and just deal with it? I found population data and I would be interested to see if we can find a good correlation there (total population won't work, I already looked at that, but maybe a specific age group?)

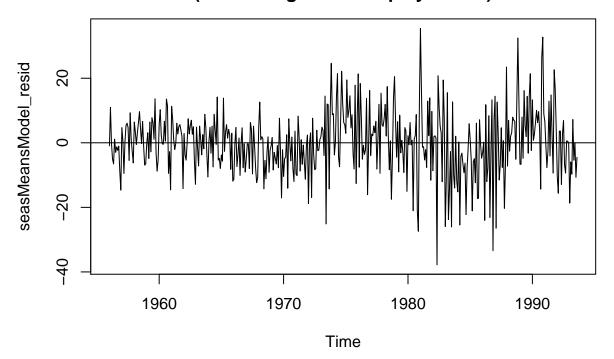
Assume we go with the 4th order polynomial for now. Let's see what we can do about the seasonality with a seasonal means model

```
library(TSA)
month=season(order4polyFit_resid)
seasMeansModel<-lm(order4polyFit_resid~month)
summary(seasMeansModel)</pre>
```

```
##
## Call:
##
  lm(formula = order4polyFit_resid ~ month)
##
## Residuals:
##
       Min
                 1Q
                     Median
                                  3Q
                                         Max
                              6.128
##
   -37.789
            -6.263
                      0.327
                                      35.453
##
## Coefficients:
##
                   Estimate Std. Error t value Pr(>|t|)
##
  (Intercept)
                      4.108
                                 1.652
                                          2.487 0.013268 *
##
   monthFebruary
                     -8.810
                                 2.336
                                         -3.771 0.000185
   monthMarch
                                 2.336
                      1.929
                                          0.826 0.409372
##
  monthApril
                    -11.085
                                 2.336
                                         -4.744 2.83e-06
  monthMay
                    -15.540
                                 2.336
                                         -6.651 8.65e-11
##
   monthJune
                    -29.051
                                 2.336 -12.434
                                                 < 2e-16
##
                                 2.336
   monthJuly
                    -19.403
                                         -8.304 1.25e-15
##
                    -13.661
                                 2.336
                                         -5.847 9.78e-09 ***
  monthAugust
                                 2.352
                                         -4.316 1.97e-05 ***
## monthSeptember
                   -10.151
```

```
## monthOctober
                     9.861
                                2.352
                                         4.192 3.34e-05 ***
## monthNovember
                    17.904
                                2.352
                                         7.612 1.66e-13 ***
  monthDecember
                    30.406
                                2.352
                                       12.927
                                                < 2e-16 ***
##
                   0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Signif. codes:
##
## Residual standard error: 10.18 on 440 degrees of freedom
## Multiple R-squared: 0.7181, Adjusted R-squared:
  F-statistic: 101.9 on 11 and 440 DF, p-value: < 2.2e-16
seasMeansModel_resid<-ts(residuals(seasMeansModel),frequency=12, start=c(1956,1))
plot(seasMeansModel_resid, main="Residuals from Seasonal Means Model \n(after fitting 4th order polynomial)")
abline(h=0)
```

Residuals from Seasonal Means Model (after fitting 4th order polynomial)



With an adjusted R-squared value of 71%, this is looking pretty good, but in the residual plot you can still the the variance increasing over time. In addition, there is a noticeable "wave" in the residuals that starts around 1970, but I'm not sure what to do about that yet. For now, let's go back, log the data, and apply both the 4th order polynomial and the seasonal means model at the same time.

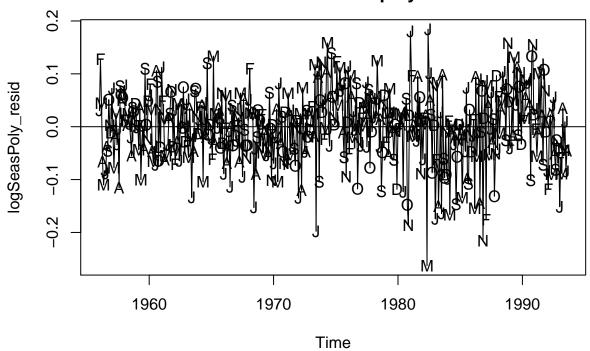
```
logBeer<-log(beerTS)
t<-1:length(logBeer)
t2<-t^2
t3<-t^3
t4<-t^4
month<-season(logBeer)

logSeasPoly<-lm(logBeer~t+t2+t3+t4+month)
summary(logSeasPoly)</pre>
```

Call:

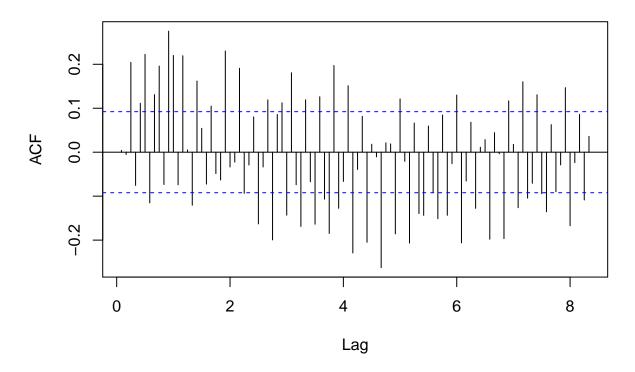
```
## lm(formula = logBeer \sim t + t2 + t3 + t4 + month)
##
## Residuals:
##
        Min
                   1Q
                         Median
                                       3Q
                                                Max
## -0.262750 -0.039816  0.003297  0.043475  0.184483
##
## Coefficients:
##
                   Estimate Std. Error t value Pr(>|t|)
                  4.506e+00 1.945e-02 231.675 < 2e-16 ***
## (Intercept)
## t
                 -1.796e-03 5.014e-04 -3.583 0.000378 ***
                  4.926e-05 4.494e-06 10.962 < 2e-16 ***
## t2
## t3
                 -1.745e-07 1.490e-08 -11.713 < 2e-16 ***
## t4
                  1.785e-10 1.631e-11 10.941 < 2e-16 ***
## monthFebruary -6.602e-02 1.580e-02 -4.178 3.56e-05 ***
## monthMarch
                  1.069e-02 1.580e-02 0.676 0.499268
## monthApril
                 -8.834e-02 1.581e-02 -5.590 4.02e-08 ***
                 -1.271e-01 1.581e-02 -8.042 8.39e-15 ***
## monthMay
## monthJune
                 -2.427e-01 1.581e-02 -15.354 < 2e-16 ***
                 -1.578e-01 1.581e-02 -9.984 < 2e-16 ***
## monthJuly
## monthAugust
                 -1.089e-01 1.581e-02 -6.890 1.96e-11 ***
## monthSeptember -7.261e-02 1.591e-02 -4.563 6.57e-06 ***
## monthOctober
                 6.706e-02 1.591e-02 4.213 3.06e-05 ***
## monthNovember 1.172e-01 1.592e-02
                                       7.363 9.03e-13 ***
## monthDecember 1.936e-01 1.592e-02 12.164 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.06889 on 436 degrees of freedom
## Multiple R-squared: 0.9365, Adjusted R-squared: 0.9344
## F-statistic:
                 429 on 15 and 436 DF, p-value: < 2.2e-16
logSeasPoly_resid<-ts(residuals(logSeasPoly),frequency=12, start=c(1956,1))
plot(logSeasPoly_resid, main="Residuals from Logged Beer\nseasonal Means and 4th order poly fit at same time",
points(y=logSeasPoly_resid, x=time(logSeasPoly_resid), pch=as.vector(season(logSeasPoly_resid)))
abline(h=0)
```

Residuals from Logged Beer seasonal Means and 4th order poly fit at same time



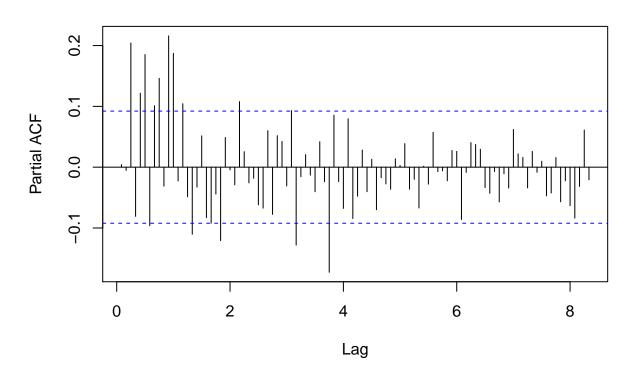
```
Let's take a look and see if we have a stationary series yet
adf.test(logSeasPoly_resid)
## Warning in adf.test(logSeasPoly_resid): p-value smaller than printed p-
## value
##
    Augmented Dickey-Fuller Test
##
##
## data: logSeasPoly_resid
## Dickey-Fuller = -5.3999, Lag order = 7, p-value = 0.01
## alternative hypothesis: stationary
pp.test(logSeasPoly_resid)
## Warning in pp.test(logSeasPoly_resid): p-value smaller than printed p-value
    Phillips-Perron Unit Root Test
##
##
## data: logSeasPoly_resid
## Dickey-Fuller Z(alpha) = -489.81, Truncation lag parameter = 5,
## p-value = 0.01
## alternative hypothesis: stationary
# p & q
par(mfrow=c(1,1))
acf(logSeasPoly_resid, lag.max=100)
```

Series logSeasPoly_resid



pacf(logSeasPoly_resid, lag.max=100)

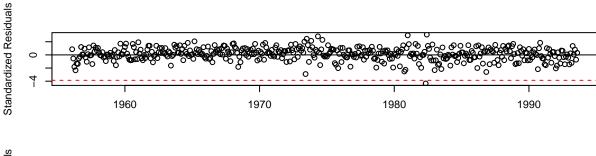
Series logSeasPoly_resid

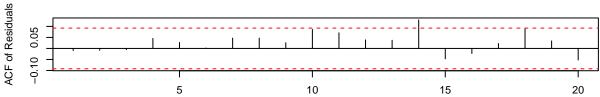


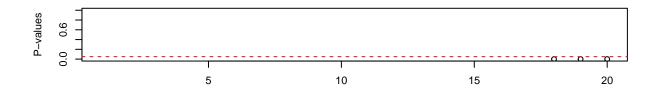
```
par(mfrow=c(1,1))
eacf(logSeasPoly_resid)
## AR/MA
##
     0 1 2 3 4 5 6 7 8 9 10 11 12 13
## 0 o o x o x x x x x o x x
                               0
## 1 x o x o o x o o x o x x o
## 2 o o x o x x o x x x x
## 3 x x x o o o o o o x
                            X
                               X
## 4 x x x o o o o o o o
                            x
                               0
## 5 x x x x x o o o o o o x o x
## 6 x x x x x o o o o o
                            o o x
## 7 x x x x x x o o o o
                            0
Try an AR(12) model and examine residuals
#Set up external regressors and dummy vars
library(forecast)
monthDummies <- seasonaldummy (logBeer)
externReg<-data.frame(t, t2, t3, t4, monthDummies)
ar12_poly<-arima(logBeer, order=c(12,0,0), xreg=externReg)</pre>
ar12_poly
##
## Call:
## arima(x = logBeer, order = c(12, 0, 0), xreg = externReg)
##
## Coefficients:
##
                                       ar4
                                               ar5
                                                                ar7
             ar1
                      ar2
                              ar3
                                                       ar6
                                                                         ar8
##
         -0.0185 -0.0373 0.0592 -0.0600 0.0852 0.1086 -0.0873
                                                                     0.0867
          0.0460
                  0.0449 0.0449
                                    0.0441 0.0443 0.0442
                                                             0.0443
                                                                     0.0438
## s.e.
##
            ar9
                    ar10
                            ar11
                                    ar12 intercept
                                                                 t2
                                                                         t4
                                                           t
##
         0.1421 -0.0077 0.2301 0.2099
                                             4.6792
                                                    -0.0009 0e+00
                                                                          0
## s.e. 0.0440
                  0.0440 0.0440 0.0453
                                             0.0781
                                                      0.0014
                                                              2e-04
                                                                           0
##
                      Feb
                               Mar
                                                                    Jul
             .Jan
                                        Apr
                                                 May
                                                          .Jiin
##
         -0.1923 -0.2566 -0.1788 -0.2787 -0.3181 -0.4344 -0.3506
         0.0154
                   0.0170
                            0.0156
                                    0.0165
                                              0.0167
                                                     0.0156
                                                                0.0167
## s.e.
##
                      Sep
                               Oct
             Aug
                                        Nov
##
         -0.3012 -0.2658 -0.1259 -0.0756
## s.e.
        0.0165
                   0.0157
                            0.0171
                                     0.0155
##
## sigma^2 estimated as 0.003593: log likelihood = 629.73, aic = -1203.47
We seem to be having trouble getting fits for the trend line, ask about this Monday, try just using the month dummies.
ar12<-arima(logBeer, order=c(12,0,0), xreg=monthDummies)
ar12
##
## Call:
## arima(x = logBeer, order = c(12, 0, 0), xreg = monthDummies)
##
## Coefficients:
##
            ar1
                    ar2
                            ar3
                                     ar4
                                             ar5
                                                     ar6
                                                              ar7
                                                                       ar8
##
         0.0631 0.0283
                         0.1255
                                 -0.0127
                                          0.1286
                                                  0.1447
                                                          -0.0733
                                                                   0.0983
## s.e.
         0.0464 0.0458 0.0458
                                  0.0457 0.0458
                                                  0.0460
                                                           0.0461
                                                                   0.0459
```

```
##
                     ar10
                                                                      Feb
            ar9
                             ar11
                                      ar12
                                            intercept
                                                             Jan
##
         0.1446
                  -0.0278
                           0.2102
                                   0.1670
                                                4.9720
                                                        -0.1925
                                                                  -0.2574
## s.e.
         0.0461
                   0.0461
                           0.0461
                                    0.0471
                                                0.2644
                                                         0.0152
                                                                   0.0169
##
             Mar
                       Apr
                                 May
                                          Jun
                                                    Jul
                                                              Aug
                                                                       Sep
##
         -0.1798
                   -0.2797
                            -0.3188
                                      -0.4349
                                                -0.3507
                                                         -0.3012
                                                                   -0.2657
                                                          0.0165
##
  s.e.
          0.0154
                    0.0165
                             0.0167
                                       0.0153
                                                 0.0167
                                                                    0.0155
            Oct
                      Nov
##
##
         -0.126
                  -0.0757
          0.017
                   0.0153
## s.e.
##
## sigma^2 estimated as 0.003946: log likelihood = 606.68, aic = -1165.36
```

tsdiag(ar12, gof.lag=20)

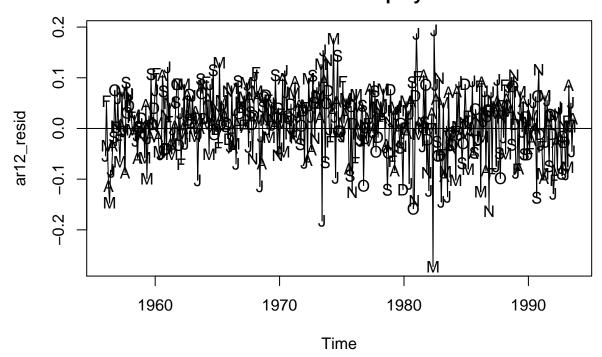






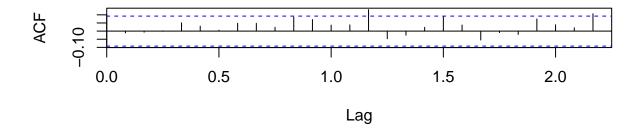
#residuals ar12_resid<-ts(residuals(ar12), frequency=12, start=c(1956,1)) plot(ar12_resid, main="AR 12 model Residuals from Logged Beer\nseasonal Means and 4th order poly fit at same t points(y=ar12_resid, x=time(ar12_resid), pch=as.vector(season(ar12_resid))) abline(h=0)</pre>

AR 12 model Residuals from Logged Beer seasonal Means and 4th order poly fit at same time

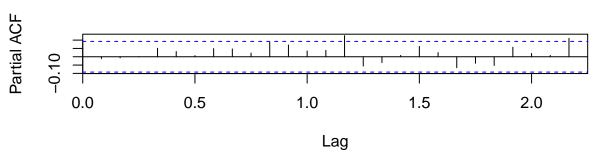


par(mfrow=c(2,1))
acf(ar12_resid)
pacf(ar12_resid)

Series ar12_resid



Series ar12_resid



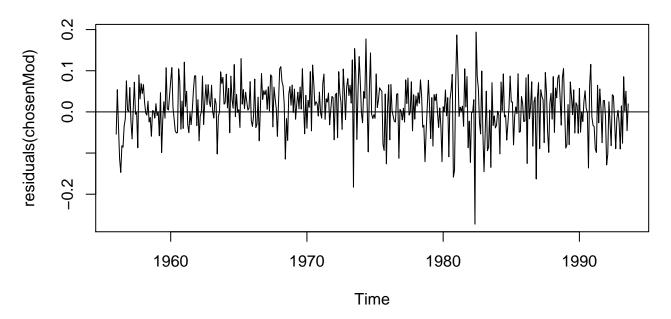
```
pacf_acf<-data.frame(acfVal=acf(ar12_resid, plot=FALSE)$acf, pacfVal=pacf(ar12_resid, plot=FALSE)$acf)
#print(pacf_acf)</pre>
```

After we choose a model, run all of the diagnostic tests

```
chosenMod<-ar12
modelString<-"SARIMA(12,0,0)(0,0,0)[12]"

par(mfrow=c(1,1))
plot(residuals(chosenMod), main=paste("Residuals of Model", modelString))
abline(h=0)</pre>
```

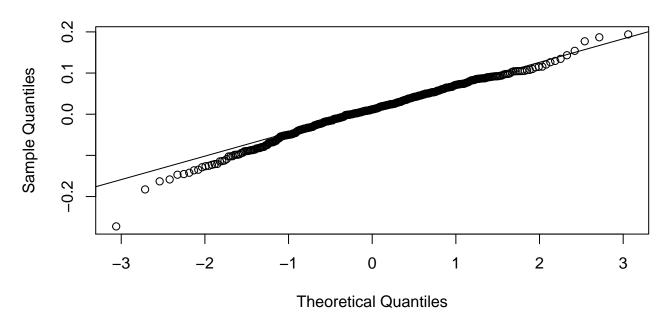
Residuals of Model SARIMA(12,0,0)(0,0,0)[12]



Comment:

```
par(mfrow=c(1,1))
qqnorm(residuals(chosenMod), main=paste("Normal QQ Plot of Residuals from", modelString))
qqline(residuals(chosenMod))
```

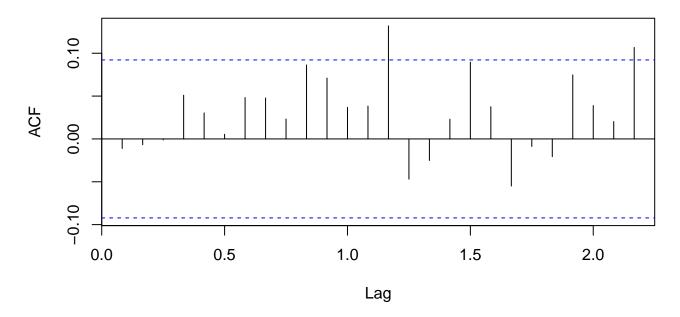
Normal QQ Plot of Residuals from SARIMA(12,0,0)(0,0,0)[12]



Comment:

```
par(mfrow=c(1,1))
acf(residuals(chosenMod), main=paste("ACF of Residuals from", modelString))
```

ACF of Residuals from SARIMA(12,0,0)(0,0,0)[12]



Comment:

shapiro.test(residuals(chosenMod))

```
## Shapiro-Wilk normality test
##
## data: residuals(chosenMod)
## W = 0.98657, p-value = 0.000348

Comment:

LB.test(chosenMod, lag=24)

##
## Box-Ljung test
##
## data: residuals from chosenMod
## X-squared = 30.485, df = 12, p-value = 0.002359

Comment:
```

Make the forecasts

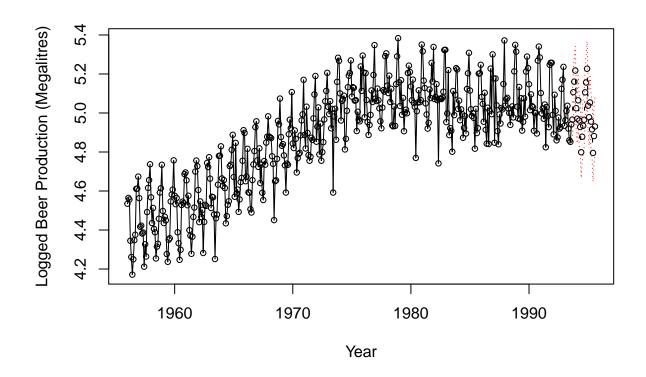
Set up external regressor data frame

```
newMonthDummy<-seasonaldummy(beer_forecast)
```

Plot the model forecasts

```
library(TSA)

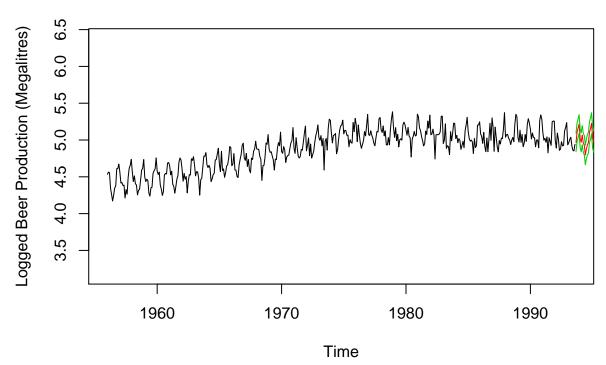
TSA::plot.Arima(chosenMod,n.ahead=24,n1=c(1956,1), newxreg=newMonthDummy,
type='b',ylab='Logged Beer Production (Megalitres)',xlab='Year', col="red", lty=2, cex=.75)
```



```
predictions<-predict(chosenMod, newxreg=newMonthDummy, n.ahead=24)
pred<-predictions$pred
uci<-pred+2*predictions$se
lci<-pred-2*predictions$se

ymin=min(c(as.vector(lci),logBeer))-1
ymax=max(c(as.vector(uci),logBeer))+1
plot(logBeer,ylim=c(ymin,ymax),main=modelString, ylab='Logged Beer Production (Megalitres)')
lines(pred,col=2)
lines(uci,col=3)
lines(lci,col=3)</pre>
```

SARIMA(12,0,0)(0,0,0)[12]



```
ymin=min(c(as.vector(lci),logBeer))-1
ymax=max(c(as.vector(uci),logBeer))+1
plot(logBeer,xlim=c(1993, 1996), ylim=c(4.5,5.5),main=modelString, ylab='Logged Beer Production (Megalitres)')
lines(pred,col=2)
lines(uci,col=3)
lines(lci,col=3)
lines(log(beer_forecast), col="black")
```

SARIMA(12,0,0)(0,0,0)[12]

