

$$\begin{aligned} Q1(a) \text{ Expected Return} &= 50\%(20\%) + 50\%(10\%) \\ &= 15\% \end{aligned}$$

$$\begin{aligned} \text{Variance} &= (0.5)^2(0.4)^2 + (0.5)^2(0.3)^2 \\ &\quad + 2(0.5)(0.5)(0)(0.4)(0.3) \\ &= 0.0625 \end{aligned}$$

$$\begin{aligned} \text{Volatility} &= \sqrt{0.0625} \\ &= 0.25 \\ &\approx 25\% \end{aligned}$$

(b) No, because by investing in these two stocks equally, you are getting higher returns with lower volatility.

(c) Yes. There is no other portfolio dominating over Fords Motor hence, it is efficient.

$$\begin{aligned} Q2(a) \text{ Portfolio Weight (Coke)} &= \frac{2}{3} \\ \text{Portfolio Weight (Intel)} &= \frac{1}{3} \end{aligned}$$

$$\begin{aligned} (b) \text{ Expected return} &= \left(\frac{2}{3}\right)(6\%) + \left(\frac{1}{3}\right)(26\%) \\ &= 0.126666 \\ &\approx 12.67\% \end{aligned}$$

$$\begin{aligned} Q3. \text{ Portfolio A Sharpe Ratio} &= \frac{12\% - 4\%}{8\%} \\ &= 1 \end{aligned}$$

$$\begin{aligned} \text{Portfolio B Sharpe Ratio} &= \frac{20\% - 4\%}{12\%} \\ &= 1.333 \end{aligned}$$

From here, we can see that Portfolio B is more efficient than Portfolio A.  
 $\therefore$  Portfolio A is not efficient.

Assuming to invest \$100,000,

$$\begin{aligned} \frac{8\%}{12\%} &= 0.6667 \\ &\approx 66.67\% \quad (\$66670 \text{ of } \$100,000) \end{aligned}$$

The new portfolio is to invest \$66670 in Portfolio A and the rest, \$33330 to be invested in risk-free rate.

$\therefore$  \$66670 at 12% with 8% volatility and \$33330 at risk-free rate.

$$\begin{aligned}
 \text{Q4.(a) Sharpe Ratio} &= \frac{E[R_p] - r_f}{SD(R_p)} \\
 &= \frac{20\% - 5\%}{20\%} \\
 &= 0.75 *
 \end{aligned}$$

$$\begin{aligned}
 \text{(b) Sharpe Ratio (Ebay)} &= \frac{11\% - 5\%}{40\%} \\
 &= 0.15
 \end{aligned}$$

$$\text{Correlation} = \frac{0.15}{0.75} = 0.2 *$$

$$\begin{aligned}
 \text{(c) Sharpe Ratio (SubOptima)} &= 0.8 \times 0.75 \\
 &= 0.6 *
 \end{aligned}$$

$$\begin{aligned}
 \text{Q5(a) Beta} &= \frac{0.2 \times 0.06}{0.16} \\
 &= 0.075 *
 \end{aligned}$$

$$\begin{aligned}
 \text{(b) Expected return} &= 4\% + 0.075 (10\% - 4\%) \\
 &= 0.0445 \\
 &\approx 4.45\% *
 \end{aligned}$$