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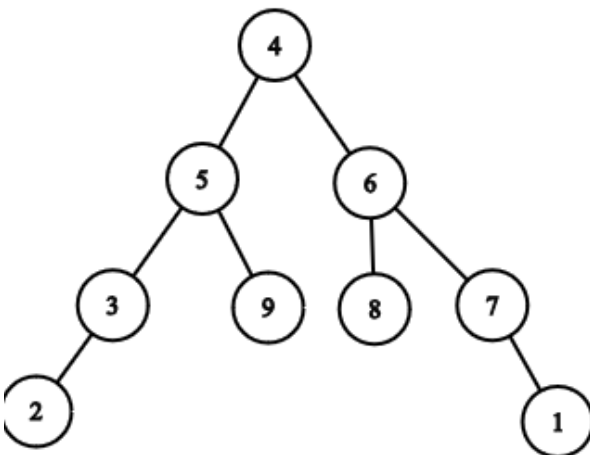
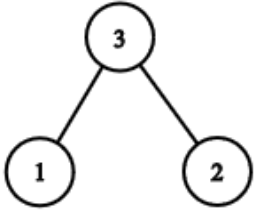
Question 1 [15 Points]

A path in a binary tree is a sequence of nodes that connect a starting node to an ending node, where each consecutive pair of nodes in the sequence is connected by an edge in the tree. In a path, if you select any pair of nodes that are consecutive, the second node will be the child of the first node.

We will call a path an **upward** path if the elements in the nodes of that path form a **strictly increasing** sequence. In a strictly increasing sequence, an element **must be greater** than its previous element. $1 \rightarrow 2 \rightarrow 3$ is a strictly increasing sequence, $1 \rightarrow 2 \rightarrow 2 \rightarrow 3$ is increasing but not strictly.

In this question, you are given the **root** of a binary tree. Write a function `count_upward_paths(root)` that counts the number of paths that **start** from the **root**, **end** at a **leaf** node and are **upward** paths. Assume the tree is constructed, so write only this function.

- Assume the `BTNode` class is given. You cannot use any other data structures.
- No library functions allowed. You can write as many helper functions as you need.

Sample Input:	Sample Output:	Explanation:
<p>Input Tree:</p> 	<p>Output:</p> <p>2</p>	<p>The paths from the root to a leaf in the given tree are:</p> <p>$4 \rightarrow 5 \rightarrow 3 \rightarrow 2$ [not upward] $4 \rightarrow 5 \rightarrow 9$ [upward] $4 \rightarrow 6 \rightarrow 8$ [upward] $4 \rightarrow 6 \rightarrow 7 \rightarrow 1$ [not upward]</p> <p>Only the 2nd and 3rd paths form strictly increasing sequences. Therefore, only these two are upward paths.</p>
<p>Input Tree:</p> 	<p>Output:</p> <p>0</p>	<p>There are no strictly increasing sequences formed by paths from the root to a leaf in this tree.</p>