

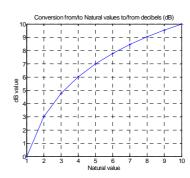
## **Outline**

- Link parameters
  - Decibel
  - Performance specifications
  - Satellite specificities
- Point-to-point link budget
  - Power
  - Losses
  - Noise
- Satellite link budget
  - Uplink&Downlink
  - Interferences
  - Overall link

# Decibel (dB)

$$X_{dB} = 10\log_{10} X \quad \Leftrightarrow \quad X = 10^{X_{dB}/10}$$

Ratio	Value in dB
1	0dB
10	10dB
1.02	0.1dB
1.26	1dB
2	3dB
3	4.77dB
π	4.97dB
4=2*2	6dB
5=10/2	7dB
6=2*3	7.77dB
7	8.45dB



- Use for a ratio (dB) or any unit (dBW, dBW/m<sup>2</sup>, dBJ, dBK, dBK<sup>-1</sup>)
- Easy handling of small numbers (1µW ⇔ -60dBW ⇔ -30dBm)
- Additive operations due to logarithms

# **Theoretical Performances**

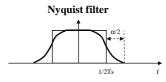
Spectral efficiency

$$\eta = \frac{R_b}{R} (b/s/Hz)$$

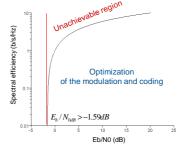
Spectral entered  $\eta = \frac{R_b}{B_N} \left( b/s/Hz \right)$  R<sub>b</sub> bit rate B<sub>N</sub> noise bandwidth R<sub>N</sub> volume that  $B_{N} = R_s \left( Hz \right)$  B<sub>N</sub> Nyquist bandwidth R<sub>s</sub> symbol rate R<sub>s</sub> symbol rate (maximum data rate)

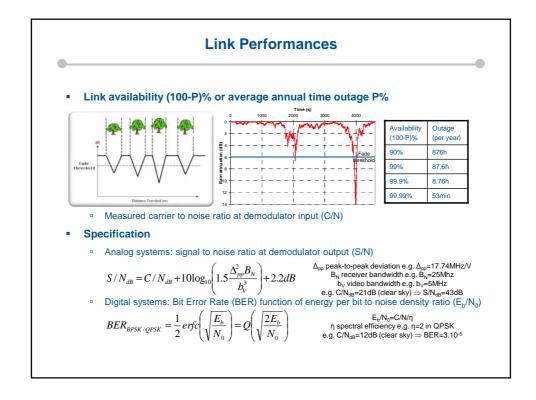
$$B_{vv} = R (Hz)$$

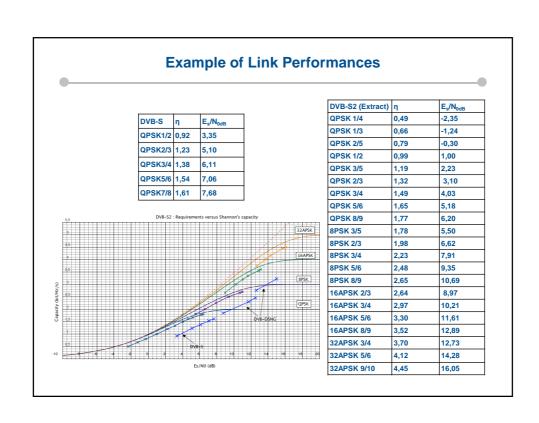
$$R_b = B_W \log_2 \left(1 + \frac{C}{N}\right) = B_W \log_2 \left(1 + \eta \frac{E_b}{N_0}\right) (b/s)$$

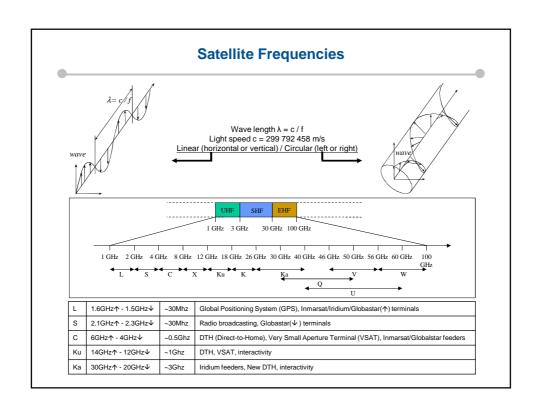


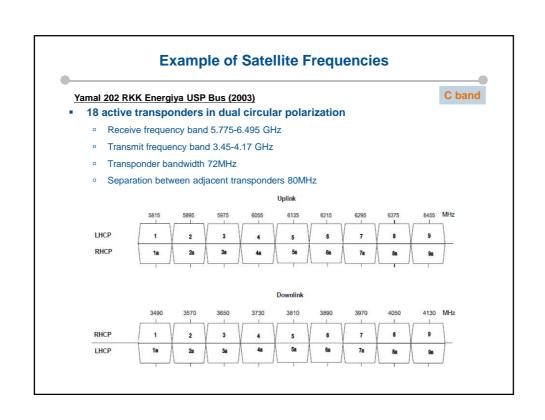
$$B_{N} = B_{W} \Longrightarrow \eta = \frac{R_{b}}{R_{s}} \Longrightarrow E_{b} / N_{0} = \frac{2^{\eta} - 1}{\eta}$$





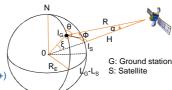






# **Satellite Geometry**

- Parameters
  - R<sub>E</sub>=6371km Earth radius, H satellite altitude,
     R distance from satellite to ground station
  - ξ central angle, Φ elevation, α nadir, Θ azimuth
  - L<sub>S</sub>&L<sub>G</sub> satellite & ground station longitudes (East +)
  - I<sub>S</sub>&I<sub>G</sub> satellite & ground station latitudes (North +)



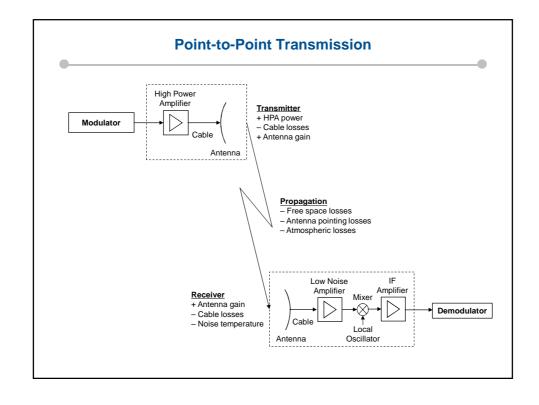
Satellite distance for a given (LEO) or fixed (GEO) elevation

$$R = R_E \left( \sqrt{\left( \left( R_E + H \right) / R_E \right)^2 - \left( \cos \varphi \right)^2} - \sin \varphi \right)$$

$$R = \sqrt{R_E^2 + \left( R_E + H \right)^2 - 2R_E \left( R_E + H \right) \cos \xi} \text{ with } \cos \xi = \cos \left( L_G - L_S \right) \cos \left( l_S \right) \cos \left( l_S \right) + \sin \left( l_S \right) \sin \left( l_G \right)$$

$$\varphi = \arctan \left( \left( \cos \xi - R_E / \left( R_E + H \right) \right) \sqrt{1 - \left( \cos \xi \right)^2} \right)$$

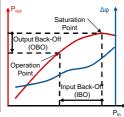
- Satellite azimuth depending on the position of S relative to G  $\theta = \tilde{\theta}(NE), \pi \tilde{\theta}(SE), 2\pi \tilde{\theta}(NW), \pi + \tilde{\theta}(SW) \text{ for } \tilde{\theta} = \arcsin\left(\sin\left(|L_G L_S|\right)\cos\left(l_S\right)/\sqrt{1 \left(\cos\xi\right)^2}\right)$
- Coverage radius  $R_c$  and percentage of Earth  $P_c$  for a minimum elevation  $\Phi_m$   $R_c = R_E \sqrt{(1-\cos\beta)/2}$   $P_c = 0.5(1-\cos\beta)$  for  $\beta = \arccos(\cos\varphi_m R_E/(R_E+H)) \varphi_m$



### **Transmitter**

- High Power Amplifier (HPA) characterized by AM/AM and AM/PM curves
  - Solid-State Amplifiers (SSPAs)
  - Klystron-tube Power Amplifiers (KPAs) or Travelling Wave Tube Amplifiers (TWTAs)

	400W Ku SSPA GaN	400W Ku SSPA GaAs	750W Ku TWTA	
Weight	30kg	80kg	37kg	
Volume	29 dm <sup>3</sup>	142 dm <sup>3</sup>	74 dm <sup>3</sup>	
Consumption	2.2kW	3.5kW	2.5kW	
(C/I <sub>3</sub> ,Δφ) at 24dBW	(-20.67dBc,1.0° /dB)	(-19.86dBc,2.0° /dB)	(-18dBc,3.5° /dB)	
(C/I <sub>3</sub> ,Δφ) at 23dBW	(-26.63dBc,0.8° /dB)	(-23.16dBc,1.5° /dB)	(-20dBc,3.0° /dB)	
(C/I <sub>3</sub> ,Δφ) at 22dBW	(-31.63dBc,0.5° /dB)	(-27.50dBc,1.0° /dB)	(-22dBc,2.5° /dB)	



Advantech Wireless comparison (2012)

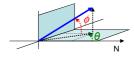
Cable

f (GHz)	2	4	6	8	10	12	14	16	18	26.5
A <sub>c</sub> (dB/m)	0.30	0.42	0.52	0.61	0.68	0.75	0.82	0.88	0.95	1.15

Sucoflex 404 - Ø 5.5mm (2011)

### **Antenna**

- **Geometric angles** 
  - Θ azimuth (look angle in the horizontal plane from North)
  - Φ elevation (look angle above the horizontal plane)



- Antenna gain (relative to an isotropic antenna)
  - $p(\theta, \Phi)$  transmitted power at the direction  $(\theta, \Phi)$
  - p<sub>0</sub> total transmitted power

- Maximum antenna gain for aperture antennas (horns, reflectors)
  - $_{0}$  η aperture efficiency, η = 0.5...0.85 (typical)
  - A physical aperture area, D circular aperture diameter
- Antenna beamwidth for a parabolic antenna ( $\psi$  angle with center axis)

  - Half-power beamwidth  $\theta_{3dB} = k \frac{\lambda}{D}(^{\circ}), k = 50...70 \text{ (typical)}$ Model with J<sub>1</sub>(x) 1st kind Bessel function (~x/2 for x small)  $g(\psi) = g_{\text{max}} \left( 2 \frac{J_1(\pi D \sin \psi / \lambda)}{(\pi D \sin \psi / \lambda)} \right)^2$
- Inverse roles of D and λ on gain and beamwidth

# Tx Antenna: Power & Flux Density

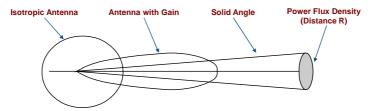
**Effective Isotropic Radiated Power (EIRP)** 

$$eirp = p_{Tx}g_{Tx}(W)$$
 with  $p_{Tx} = p_{HPA}l_c(W)$  and  $l_c = a_cd_c(W)$ 

- $^{\circ}$   $p_{Tx}$ ,  $g_{Tx}$  transmit antenna power, gain
- p<sub>HPA</sub> HPA power
- □ I<sub>c</sub>, a<sub>c</sub>, d<sub>c</sub> cable losses, attenuation per meter, length
- **Power Flux Density (PFD)**

$$\varphi = \frac{eirp}{4\pi R^2} \left( W / m^2 \right)$$

 $\,^{\circ}\,$  Power density at distance R for a spherical shell of surface  $4\pi R^2$  in a lossless medium



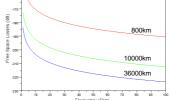
## **Rx Antenna: Free Space & Losses**

Aperture antenna

$$p_{Rx} = \varphi \eta A(W)$$

- P<sub>Rx</sub> receive antenna power
- Friis transmission formula

$$p_{Rx} = p_{Tx} g_{Tx} g_{Rx} \left( \frac{\lambda}{4\pi R} \right)^2 (W) \text{ with } l_{FS} = \left( \frac{4\pi R}{\lambda} \right)^2$$
• G<sub>Rx</sub> receive antenna gain



- L<sub>FS</sub> free space losses
- Real transmission formula

$$C = \frac{p_{Tx}g_{Tx}g_{Rx}}{l_{FS}l_{Pt}l_{Atm}}(W) \Leftrightarrow C_{dB} = P_{Tx} + G_{Tx} + G_{Rx} - L_{FS} - L_{Pt} - L_{Atm}(dBW)$$

 $^{\circ} \quad L_{Pt} \ \text{pointing losses with} \ \theta_{\Delta i} \ \text{off-boresight angles and} \ \theta_{3dB} \ \text{half-power beamwidth in degrees}$ 

$$L_{Pt} = 12 \sum_{i} \left( \frac{\theta_{\Delta i}^{2}}{\theta_{3JR}^{2}} \right)$$

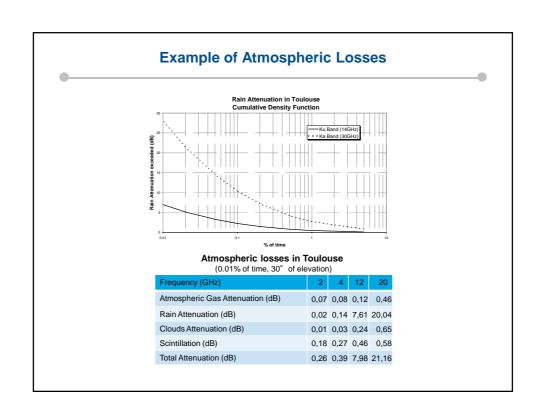
L<sub>Atm</sub> atmospheric losses ITU-R P.618-10 (10/09)

## **Atmospheric Losses**

- Atmospheric gas attenuation ITU-R P.676-9 (02/12)
- Precipitation attenuation and depolarization ITU-R P.618-10 (10/09)
  - Rain height ITU-R P.839-3 (02/01)
  - Maps of rainfall rate ITU-R P.837-6 (02/12)
  - Specific attenuation model for rain ITU-R P.838-3 (03/05)
  - Comparison with measures ITU-R P.678-1 (03/92)
  - Conversion of annual statistics to worst-month statistics ITU-R P.841-4 (03/05)
- Clouds and fog attenuation ITU-R P.840-5 (02/12)
- Tropospheric scintillation ITU-R P.618-10 (10/09)
  - Radio refractive index ITU-R P.453-10 (02/12)
- Total attenuation ITU-R P.618-10 (10/09)

$$L_{Atm}(p) = L_G + \sqrt{(L_R(p) + L_C(p))^2 + L_S(p)^2}$$

- L<sub>G</sub> gases attenuation
- $^{\rm u}$  ~  $L_{\rm R},L_{\rm C},~L_{\rm S}$  rain, cloud, scintillation exceeded attenuations for p% of time



# **Component Noise Temperature**

Power due to thermal noise

 $N = kT_{Ea}B$ 

- k = 1.379 10-23 W/K/Hz Boltzmann's constant (-228.6dBW/Hz/K)
- T<sub>Eq</sub> equivalent noise temperature (of a passive resistor giving same noise power per bandwidth)
- Noise power spectral density

 $N_0 = N/B = kT_{Eq}$ 

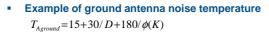
Lossy element noise temperature (output, input)

$$T_{output} = T_0 (1 - 1/l_e) \Leftrightarrow T_{input} = T_0 (l_e - 1)$$

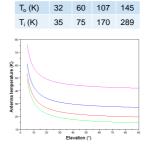
I<sub>e</sub> losses at T<sub>0</sub> noise temperature (290K)



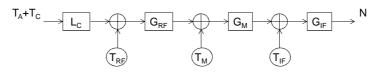
nf<sub>d</sub> noise figure (input over output signal to noise ratios)



D, Φ ground station diameter (m) and elevation (°)



### **System Noise Temperature**



$$N = g_{IF}kT_{IF}B + g_{IF}g_{M}kT_{M}B + g_{IF}g_{M}g_{RF}k((T_{A} + T_{C})/l_{C} + T_{RF})B$$

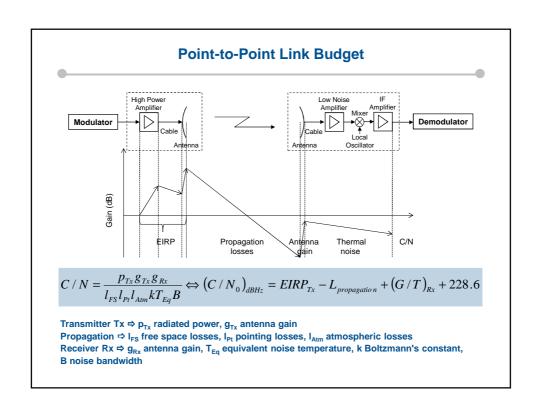
$$N = g_{IF}g_{M}g_{RF}kT_{Eq}B \quad \text{with} \quad T_{Eq} = (T_{A} + T_{C})/l_{C} + T_{RF} + \frac{T_{M}}{g_{RF}} + \frac{T_{IF}}{g_{M}g_{RF}}$$

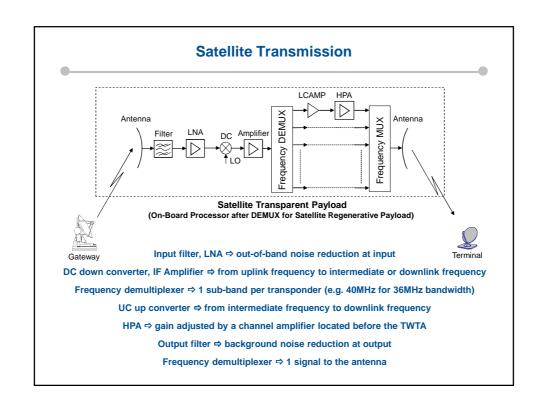
- Good Low Noise Amplifier (LNA)

Highest gain 
$$g_{RF}$$
 possible
Lowest temperature  $T_{RF}$  or noise figure NF<sub>RF</sub> possible
$$T_{Eq} \approx \frac{T_A}{l_C} + T_0 \left( 1 - \frac{1}{l_C} \right) + T_0 \left( n f_{RF} - 1 \right)$$

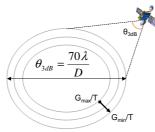
- Antenna noise temperature
  - $^{\circ}$  Pointing at Sun (12000f<sup>-0.75</sup>K), Moon (200-300K), Earth (290K), cosmic background (T<sub>S</sub>=2.7K)
  - $^{\circ}$  On ground with clear sky  $L_{G}$  (T  $_{G}$  =280K) or exceeded attenuation  $L_{Atm}$  (T  $_{R}$  =260K)

$$T_{Aclear} = \frac{T_{S}}{l_{G}} + T_{G} \left( 1 - \frac{1}{l_{G}} \right) + T_{Aground} \qquad T_{Aexceeded} = \frac{T_{S}}{l_{Atm}} + T_{R} \left( 1 - \frac{1}{l_{Atm}} \right) + T_{Aground}$$





# Satellite Uplink



$$G_{Sat} = 10\log_{10}\eta(70\pi/\theta_{3dB})^2$$

Satellite transponder
-Saturation Flux Density (SFD)
Power flux density for IBO=0
-Operation Flux Density (OFD)
Power flux density for IBO=OFD-SFD
-Coverage variations
Constant SFD+G/T

- Satellite beam (G/T or SFD in Rx)
- Ground station EIRP for a satellite transponder at saturation
  - Clear sky

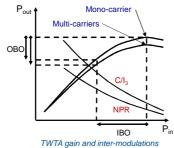
$$EIRP_G = SFD + 10\log_{10}(4\pi R^2)$$

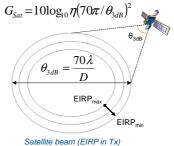
Atmospheric losses with Uplink Power Control (UPC)

$$EIRP_G = SFD + 10\log_{10}(4\pi R^2) + L_{Atm} + L_{Pt}$$

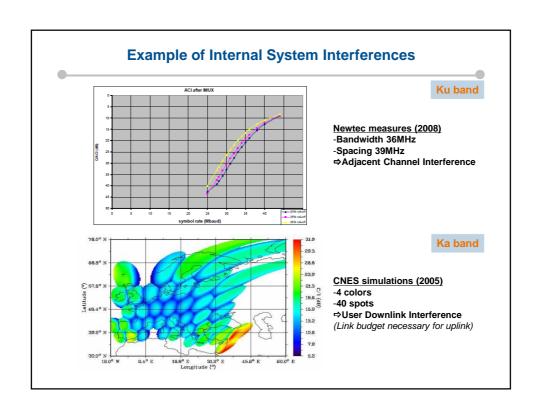
- Estimation of the atmospheric and pointing losses
  - Satellite unmodulated and temperature-stabilized beacon to use with narrow bandwidth filter
  - Satellite telemetry beacons to use with large bandwidth filter to minimize level variations

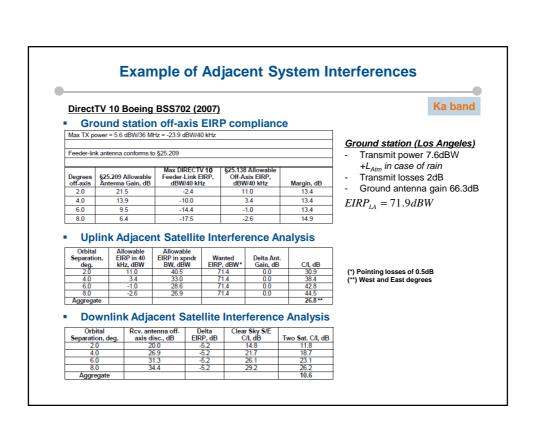
### **Satellite Downlink**



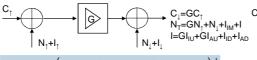


- Transponder gain adjustment
  - Fixed Gain Mode (FGM), gain steps at fixed SFD+G/T (multiple transmission sites)
    - ⇒ Ground station UPC required to keep the same operation point
  - Automatic Level Control (ALC), gain steps at fixed IBO (single transmission site)
    - ⇒ Uplink fading compensation at the cost of the uplink C/N degradation (possibly with UPC)
- Intermodulation noise C/I<sub>IM</sub>
  - $\ \, \text{Upper bound} \Rightarrow 3^{rd} \text{ order inter-modulations } \text{(C/I}_3\text{)} \Rightarrow \text{Mono-carrier, Small number of carriers}$
  - ${}^{\tt u}\quad \text{Lower bound} \ {}^{\rm p}{\rm Noise} \ {\rm Power} \ {\rm Ratio} \ ({\rm NPR}) \ {}^{\rm p}{\rm Multi-carriers}$





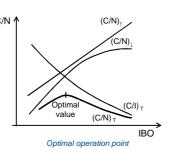
### Satellite Overall Link



$$(C/N)_T = ((C/N)^{-1}_{\uparrow} + (C/N)^{-1}_{\downarrow} + (C/I)^{-1})^{-1}$$

<u>NB:</u> Independent uplink and downlink if on-board processing (useful for symmetrical links requiring single hop)

$$C/I_{dB} = C/N_{dB} \Rightarrow C/(N+I)_{dB} = C/N_{dB} - 3dB$$
  
$$C/I_{dB} = C/N_{dB} + 10dB \Rightarrow C/(N+I)_{dB} = C/N_{dB} - 0.5dB$$



- Internal system interferences (polarization reuse, multi-beam frequency reuse)
  - Interferences due to the satellite reception antennas (C/I<sub>III</sub>)
  - Interferences due to the satellite transmission antennas (C/I<sub>ID</sub>)
- Adjacent system interferences
  - Interferences due to other ground stations (C/I<sub>AU</sub>)
  - Interferences due to other satellites (C/I<sub>AD</sub>)

# **Multiple Access Links**

Multiple-Frequency Time-Division Multiple Access (MF-TDMA)



MF-TDMA efficiency  $\Rightarrow \eta_{MF-TDMA} = \frac{N_U}{N_T} \frac{B_U}{B_T}$ 

- **Burst Plan in Time and Frequency**
- B<sub>U</sub> useful bandwidth
   B<sub>T</sub> total bandwidth
- N<sub>U</sub> number of useful bits per frame
- $N_T$  total number of bits per frame (with transmission during guard time)
- Multiple-Frequency Code-Division Multiple Access (MF-CDMA)
  - R<sub>c</sub> chip rate of the spreading sequence

 $E_b / N_0 = \gamma C / N$  with a processing gain  $\gamma = R_c / R_b$ 

 $\begin{array}{ccc} ^{\rm o} & {\rm L_{MU}~losses~due~to~multi-user~load~\eta_{MU}} \\ & L_{MU} = 10{\rm log_{10}} \Big(1/\big(1-\eta_{MU}\big)\big) \end{array}$ 

## **Mobile Satellite System Links**

#### Mobile channel

- Three state propagation conditions 

   ⇒ Clear line of site (LOS), Shadowing, Blockage
- Data bandwidth compared to path length ⇒ Narrowband fading (kHz), Wideband fading (MHz)

### • Friis transmission formula for a mobile link

$$p_{Rx} = p_{Tx} g_{Tx} g_{Rx} g(R) x_S \alpha_M^2(W)$$
 with  $g(R) = kR^{-n}$ 

- g(R) path loss factor (free space losses, two ray path losses)
- x<sub>S</sub> Gaussian random shadow fading (trees on roadway or buildings in urban area)
- α<sub>M</sub> Rice/Rayleigh distributed multipath fading (mountains or trees without shadowing)
  - ⇒ Fade depth exceeded for a percentage of time cumulating the three states

    Maritime/Land/Aeronautical channel ITU-R P.680-3 (10/99) / 681-7 (10/09) / 682-3 (02/12)

#### Wideband channel

- Signal spectrum distortion and error floor due to delay spread
- Mitigation techniques 
   diversity to reduce deep fades, directional antennas to reduce far-out
   echoes, equalizers to use energy in delayed taps, narrow bandwidth carrier multiplexing

### Satellite Link Budget Methodology

### Link constraints

- Satellite cost per bandwidth, frequency band, SFD, G/T, EIRP
- User subscription, data rate, availability, C/N

### Possible ground stations

- Transmission ground stations EIRP, UPC
- Reception ground stations G/T

### Satellite operation point

- Link budget on the uplink and satellite IBO
- Satellite OBO and link budget on the downlink

#### Interferences

- Internal system interferences
- Adjacent system interferences

#### System selection

- Margins for the overall link budget
- System redesign to converge on positive margins

http://logiciels.cnes.fr/PROPA/fr/logiciel.htm