

## IT.2407 - IoT and Cellular Network

# TD La chaîne de transmission numérique

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## Problem 1: Single carrier modulation

## 1. Demodulation the signal to find back.

1) The form of the modulated signal is:

$$y(t) = \sqrt{SNR}[A_k \cos(2\pi f_0 t) - B_k \sin(2\pi f_0 t)] + Noise$$
 
$$A_k = A\cos(\varphi), the \ inphase \ component$$
 
$$B_k = A\sin(\varphi), the \ quadrature \ component$$

A - Amplitude

φ – the phase determined by the 16QAM constellation diagram

2)

$$A_k: y(t) * 2\cos(2\pi f_0 t)$$

$$ightharpoonup \cos(2\pi f_0 t) * \cos(2\pi f_0 t) = \frac{1}{2} [\cos 0 + \cos(4\pi f_0 t)] = \frac{1}{2} [1 + \cos(4\pi f_0 t)]$$

$$ightharpoonup \sin(2\pi f_0 t) * \cos(2\pi f_0 t) = \frac{1}{2} [\sin(4\pi f_0 t)]$$

Then,

$$y(t) * 2\cos(2\pi f_0 t) = \sqrt{SNR} \{A_k [1 + \cos(4\pi f_0 t)] - B_k \sin(4\pi f_0 t)\} + N$$

Remove high-frequency  $(\cos(4\pi f_0 t), \sin(4\pi f_0 t))$  components with a low-pass filter (with a frequency  $\frac{1}{duration\ of\ a\ symbol}$ ), to get  $\sqrt{SNR}*A_k$ .

3)

$$B_k$$
:  $y(t) * [-2\sin(2\pi f_0 t)]$ 

$$ightharpoonup \cos(2\pi f_0 t) * \sin(2\pi f_0 t) = \frac{1}{2} [\sin(4\pi f_0 t)]$$

$$ightharpoonup \sin(2\pi f_0 t) * \sin(2\pi f_0 t) = \frac{1}{2} [1 - \cos(4\pi f_0 t)]$$
 Then,

 $y(t)*[-2\sin(2\pi f_0t)] = \sqrt{SNR} \left\{ -A_k \sin(4\pi f_0t) + B_k \left[ 1 - \cos(4\pi f_0t) \right] \right\} + N$  Remove high-frequency  $(\cos(4\pi f_0t), \sin(4\pi f_0t))$  components with a low-pass filter (with a frequency  $\frac{1}{duration\ of\ a\ symbol}$ ), to get  $\sqrt{SNR}*B_k$ .

- 4) Based on  $A_k = Acos(\varphi)$ ,  $B_k = Asin(\varphi)$ , can get A and  $\varphi$ .
- 2. The processing of the received signal.

#### In-phase Component Processing Flow

- Receiving the Signal: receive the signal transmitted at a carrier frequency of 800 MHz.
- 2) Spectrum Analysis: Perform spectrum analysis on the received signal, finding that the signal has energy distributed around 0 GHz and 1.6 GHz (2 \* 800 MHz).
- 3) Multiplying the Signal by  $2\cos(2\pi f_0 t)$ : To extract the in-phase component  $A_k$ , multiply the signal by  $2\cos(2\pi f_0 t)$ . This generates a new signal containing components of the original signal and a high-frequency component.
- 4) Low-pass Filtering: Pass the product signal through a low-pass filter to remove high-frequency components around 1.6 GHz, retaining only the baseband signal. After filtering, the time-domain signal becomes clearer, mainly containing low-frequency oscillations representing different binary symbols and a small amount of noise.
- 5) Reading  $A_k$ : In the time-domain signal, read the in-phase component  $A_k$ .

These values correspond to the in-phase component of the original 16QAM modulated signal.

#### **Quadrature Component Processing Flow**

- 1) Multiplying the Signal by  $-2\sin(2\pi f_0t)$ : To extract the quadrature component  $B_k$ , multiply the signal by  $-2\sin(2\pi f_0t)$ . This generates a new signal containing components of the original signal and a high-frequency component.
- 2) Low-pass Filtering: Pass the product signal through a low-pass filter to remove high-frequency components around 1.6 GHz, retaining only the baseband signal. After filtering, the time-domain signal becomes clearer, mainly containing low-frequency oscillations representing different binary symbols and a small amount of noise.
- 3) Reading  $B_k$ : In the time-domain signal, read the quadrature component  $B_k$ . These values correspond to the quadrature component of the original 16QAM modulated signal.
- 3. Indicate the duration of the symbols.

(-1, 3) -> 0100

 $(1, 1) \rightarrow 1101$ 

(-1, -1) -> 0111

(3, 1) -> 1001

(-3, -3) -> 0010

```
(-3, 3) -> 0000
```

$$(-1, -1) -> 0111$$

$$(-1, -1) -> 0111$$

$$(-1, -3) -> 0110$$

$$(-3, 1) -> 0001$$

$$(-1, -1) -> 0111$$

$$(3, 1) -> 1001$$

## 4. Name of the song.



## Problem 2: OFDM signal

## 1. Find the spacing.

Between two neighbours' subcarriers:

- $ightharpoonup \Delta f = \frac{1}{T}$ , T is the duration of an OFDM symbol transmitted.
- $\triangleright$  N = 128, the number of the subcarriers.

$$ightharpoonup T = \frac{N}{FS}$$

$$ightharpoonup \Delta f = \frac{1}{T} = \frac{Fs}{N} = \frac{1.92 \times 10^6}{128} = 15 kHz$$

### 2. Find the data rate.

1) For using 32AQM, and the message occupies only 20 subcarriers:

$$f_s = \frac{1}{T_s} = 15k \ Baud$$

- 2) Information bits per symbol =  $20 * 5 * \frac{4}{5} = 80 \ bits/symbol$
- 3)  $R_{data} = f_s * information bits per symbol = 15000 * 80 = 1.2 Mb/s$
- 3. Find the 16QAM symbols transmitted.
  - (-1, -3) > 01010
  - (-3, -1) -> 01111
  - (-3, 3) -> 01100
  - (-1, -5) -> 00011
  - (-3, 3) > 01100
  - $(1, 3) \rightarrow 11000$
  - (-3, 3) -> 01100
  - (5, -1) -> 10111
  - (-5, 1) -> 00101
  - (-3, 5) -> 00000
  - (-1, 1) -> 01001
  - (-1, -5) -> 00011
  - (-3, 3) -> 01100
  - $(1, 3) \rightarrow 11000$
  - (-3, 3) -> 01100
  - (3, -3) -> 11110
  - (-3, 3) ->01100

```
(3, 1) -> 11101
```

(-3, 3) ->01100

(-1, -3) -> 01010

## 4. Name of the song.

